# HANDBUCH; DER ASTROPH,YSIK

#### HERAUSGEGEBEN VON

### G EBERHARD · A KOHLSCHUTTER H LUDENDORFF

BAND V / ZWEITE HALFTE
DAS STERNSYSTEM

ERSTER TEIL



BERLIN VERLAG VON JULIUS SPRINGER 1933

### DAS STERNSYSTEM

ERSTER TEIL

II

BEARBEITET VON

HEBER D. CURTIS · B. LINDBLAD K. LUNDMARK · H. SHAPLEY

> MIT 118 ABBILDUNGEN UND 2 TAPELN





BERLIN VERLAG VON JULIUS SPRINGER 1933



### HANDBUCH; DER ASTROPHYSIK

HERAUSGEGEBEN VON

G. EBERHARD · A KOHLSCHUTTER
H. LUDENDORFF

BAND V / ZWEITE HALFTE

DAS STERNSYSTEM

ERSTER TEIL



BERLIN VERLAG VON JULIUS SPRINGER 1933

### Inhaltsverzeichnis.

#### Chapter 4

#### Luminosities, Colours, Diameters, Densities, Masses of the Stars,

### By Prof Dr Knut Lundmark, Lund

(Continued.)

#### (With 12 illustrations)

d)	The Diameters of the Stars	575
ď	190). The Diameters of the Stars Rarlier Conceptions Pioneer Work	575
	19i Wilaing's Investigations	578
	192 Russell's Method 193 Diameters from a/T	582
	193 Diameters from $\epsilon_0/T$	. 584
	194. Diameters from Radiometric Measurements .	585
	195 Kalmán's Investigation	586
	196. Interferometer Measurements at Mount Wilson	587
	197 Varying Stellar Diameters 198. The Theoretical Investigations of M Hanv	590
	198. The Theoretical Investigations of M HAMV	591
	199 Danjon's Interferometer-Mothod	596
	200. The Companion of Strius (Strius B)	596
	201 Diameters from Scintillation-Observations	599
	202. The Fallacy in S Porrowsky's Method .	599
6)	The Densities of the Stars	600
	203. Densities of the Stars Pioneer Work	600
	204. Densities of Visual Binary Stars	600
	205 The Ratio of Densities in Double Stare .	603
	200. Donaities of Relinsing Binaries. Methodical	604
	207 SHAPLEY'S Work	605
	208 Paralloxes and Absolute Magnitudes of Religing Binaries	606
	209 Recent Statistics of the Eclipsing Binaries	607
n	The Massas of the Stars	608
-,	210 Mothods of Deriving Stellar Masses	608
	211 Are Derived Mass-Values Representative?	, 610
	212 Historical Notes Observational Evidences .	611
	242 Regularition of Stollar Reserv	617
	244 Sour Perware's and Barre's Study on Spectroscopic Bulleton	, 619
	214 Lunewhouse's Researches on the Masses of Spectroscopic Disaries	619
	216. Frommency of Stellar Masses for Different Spectral Classes.	, 622 626
	217 Sproul Determinations of Masses	627
	248 Pirray's Investigation	629
	219 Statistics of accurately Determined Stallar Masses	630
	220 Real and Apparent Masses	631
	221 SHARRS'S Researches	637
	222, Stollar Massos from Spectrographic Parallexes .	, 638
	223 Masses of F-K Stars	641
	224. Colour-Mass-Donalty Rulation	641
	225 VON ZEIPEL'S Method 236 'The Method of PREUNDLICH and HEISKAMEN.	64.
	296 The Method of Prednolici and Demander.	

#### Inhaltsverzeichnis

				Seite
		Martlns's Method		646
		Recent Work Concerning Masses of Spectroscopic Binaries		653
		Preferential Values of Stellar Masses Dwarf Nature of Spectroscopic Binaries		656 658
		Discovery of Mass Luminosity Relation	•	658
		Eddington's Mass-Luminosity Law and Cosmogonic Time-Scale		662
		Discrepancies between Seari's's and Eddington's Results		666
	234	JEANS'S Pheory		667
	235	The Cosmogonic Time-Scale by Jlans and Smart Brill's Theory and Parallax-Method for Binaries		672 673
		Mass-Reduction by Annihilation of Protons and Elections		676
		The Theory of RABE		678
		Convergence of Mass-Ratios with Increasing Age		682
		Vogr's Extension of Eddington's Theory		682
	241	Statistical Investigations Concerning the Mass-Ratio in Binaries Theoretical Derivation of the Mass-Ratio in Double Stars		683 684
		LUNDMARK'S and LUNTEN'S Differential Method		685
		The Masses and Luminosities of the Eclipsing Binaries		686
		The Upper Limit for the Stellar Masses		687
		Relation between Stellar Mass and Proper Motion		689
		Relation between Stellar Mass and Form of Orbits of Binary Stars  The Mass of the Orion Nebula		690 691
		Planetary Nebulae		692
		Mass of the Stellar System		693
	251	The Masses and Mass-Ratios of Stellar Systems		694
	252		•	695
	253 254	The Origin of Binary Stars Concluding Remarks	•	695 696
Αn		ix I. Catalogue of Stars Brighter than 5m,00 .		1077
		iix II Catalogue of Stellar Diameters		. 1135
•		,	•	,
		Chapter 5		
		Stellar Clusters.		
		By Prof II SHAPLEY, Cambridge (Mass)		
		(With 21 illustrations)		
a١	Int	roductory Survey ,		698
-,		The Significance of Clusters	. '	698
		Historical Notes on Clusters	•	698
b)	Clas	ssification, Number and Distribution .		700
٠	3	A Comparison of Galactic and Globular Clusters		700
	4	The Number of Clusters		700
		Classification of Galactic Clusters Classification of Globular Clusters		704
		Clusters in or near Obstructing Nebulosity	•	705 706
		The Apparent Distribution of Globular Clusters		708
	9	The Apparent Distribution of Galactic Clusters		710
		Peculialities in the Distribution of Galactic Clusters	•	710
c)		the Spectral Composition of Clusters		711
		Integrated Spectra of Globular Clusters		711
		Stellar Types in Globular Clusters On the Masses of Giant Stais		712 714
		Spectra in Individual Galactic Clusters		715
ď١		riable Stars in Star Clusters ,		717
{	15	The Frequency and General Properties of Variable Stars in Clusters		717
	16	A Summary of Known Variables .		718
e)	The	e Distribution of Stars in Globular Clusters		. 720
		Ate Cluster Stars Arranged Spirally?		720
		On the Laws of Distribution Luminosity Curves for Stats in Clusters		720 722

THUST AGAZOCHUM.	VΠ
i) The Forms of Clusters  20 Definition and Difficulties 21 The Elongation of Messier 13 22 Ellipticity and Orientation of Globular Clusters 23 Some Peculiar Clusters 24 The Structure of Galactic Clusters 25 liarly Investigations of Light Scattering 26 Blue Stars in Messier 13 27 Faint Blue Stars in the Milky Way 28 Colors in Other Distant Objects 29 Messier 5 and the Relative Speeds of Blue and Yellow Light h) The Distances and Dimensions of Clusters	VII 724 724 726 726 730 733 733 733 734 735
<ul> <li>30. The Photographic Period-Luminosity Curve</li> <li>31 Distances of Globular Clusters Obtained from Cephelds and Bright Stars</li> <li>32. Distances of Globular Clusters Obtained from Dismeters and Integrated Magnitus</li> <li>33 A Working Catalogue of Galactic Clusters (Appendix B)</li> <li>34 Parallexes of Galactic Clusters</li> <li>35 Radial Velocities of Globular Clusters</li> <li>36. Dimensions and Star Densities of Clusters</li> </ul>	737 737 740 740 744 746 747 748
i) Star Clusters in the Magallanio Clouds  37. Types of Clusters and Nebulae  38 The Globular Star Clusters  39. Distances of the Clouds  40. On the Relation of the Clusters to the Magallanic Clouds	750 750 751 752 753
i) Dimensions of the Galaxy  44 Membership in the Galaxy  42. The System of Galactic Cinsters  43. The Higher Systems of Globular Cinsters  44 The Distance to the Galactic Center  45 On the Size and Structure of the Galaxy  Appendix A. Catalogue of Globular Cinsters  4. Catalogue of Globular Cinsters	754 754 755 755 758 759
Appendix B. Catalogue of Galactic Clusters	, 766
Chapter 6.	
The Nebulae.	
By Prof. Hener D. Curris, Ann Arbor (Mich).	
(With 58 illustrations in the text and on a plats.)  a) Introduction	· · 774
b) The Diffuse Nebulae  5. Definition  6 Number and Distribution  7 Physical Characteristics of Diffuse Nebulae  8. Dark Nebulae  9. Cosmic Clouds  10. Distances and Dimensions of Diffuse Nebulae  11 Luminous Diffuse Nebulae  12 Proper Motions and Internal Motions (Visual)  13 Radial Velocities of Diffuse Nebulae  14. Turbulance Rifects in Diffuse Nebulae  15. Luminosity of the Diffuse Nebulae: Gaseous Spectra	. 77' . 77' . 77' . 78' . 78' . 78' . 78' . 79' . 79' . 79' . 79'

VI	II	Inhaltsyerzeichnis		
		S	oite	
	16		301	
	17	Luminosity of the Diffuse Nebulae Reflection or Resonance Effects	302	
	18		303	
	19	Evolutionary Status of the Diffuse Nebulae	805	
c)	The	Planetary Nebulae	306	
•	20	Definition of the Planetary Type	806	
			807	
			808	
	23		809	
	24	The state of the s	810	
			813	
			815	
	27		817	
			817 819	
			823	
		7	824	
		No.	825	
			831	
A)			833	
u,				
			833 838	
			839	
		Conspectus of Forms Assumed	840	
	38		842	
		Barred Spirals	812	
		Elliptical Spirals, the Provenance of the "Minute" Spirals	843	
	41	Integular and Magellanic Type Spirals	844	
		Occulting Matter in the Spirals, and its Bearing on Observed Distribution	844	
		Proper Motions of the Spirals	847	
		The Spirals as a System of Reference	850	
		Internal Motions of the Spirals, Visual Determinations	850	
		Rotation of the Spirals, Spectrographic	851	
		Spectra of the Spirals, Stellar Type Spectra of the Spirals, Emission Lines	852 853	
	40	Color Indices of the Spirals, the Results of Sharks	854	
	50	The Radial Velocities of the Spirals	855	
		Distances of the Spirals Parallaxes	858	
		Distances of the Spuals from Novae	858	ţ
		Distances of the Spirals from Cepheids	861	
	54	Distances of the Spirals from a Distance-Velocity Correlation	863	
		Distances of the Spirals Photometric, the "Average" Galaxy	868	
	_	Distances and Dimensions of the Spirals	873	_
		Masses of the Spiials Ten Bruggencare's Theory of Elliptical Spirals	870	
		Theories of Spiral Structure Introductory	877 878	
	60	Agreement of Spual Arms with Mathematical Spirals	879	
		Wilczynski's Gravitational Spiral	881	
			882	
	63	Brown's Theory of Spiral Structure	882	2
		LINDBLAD'S Theory of Spiral Structure	884	1
		Theories of Spiral Structure Summary	880	
		Evolutionary Status of the Spirals	88	
		Cosmogonical Deductions Introduction	88	
		The Charlier Infinite Universe	888	
		The Spirals and Relativity Universes Introduction Tolman's Critique of the DE Sitter Relativity Universe	89	
	74	An Expanding Relativity Universe the Work of Lemaitre, Fudington, McCrea,	89	1
	17	and McVittie	89	R
	72	The Size of the Universe According to Silberstein	903	
		Various Determinations of the "Radius" of Space-Time	90	
		Summary the Dilemma of Choice between an Expanding Relativity Universe	,	•
		and Distance-Velocity Correlation	90	3
	7	Other Cosmogonical Deductions an Aberration Effect	00.	å

	Inhaltaverzeichnis.	IX
	76 Further Considerations on the Apparent Recomion of the Spirals 77 Earlier Values of the Motion of our Galaxy in Space 78 Morssann's Modification of the Doppler Formula 79. Conclusion	905 906 907 907
a)	Appendices  i Finding List for Names frequently Used in the Older Literature  Finding Lists for Sir W Herschel's Classes and Numbers  Finding List for General Catalogue Numbers  Finding List for Sir J Herschel's Numbers  Systems of Nebular Classification  Fuhllshed Reproductions of Nebulae  Abridged Nebular Bibliographical Apparatus  A Test of the Morssard Modification of the Doppler Formula in a Universe of the Charler Type	908 908 910 918 919 919 922 931
	Kapitol 7	
	Die Milchstraße.	
	Von Prof. Dr B LINDBLAD, Stockholm	
	(Mit 28 Abbildungen und 1 Tafel)	
a)	Rinialtung	937 937 937
b)	Das visuelle Mitchstraßenbild	938 938 947 948
o)	Die Photographie der Milchstraße  6. Die prinzipiellen Verschiedenheiten der visuellen und photographischen Beobachtungen  7. Die photographischen Arbeiten einzelner Ferscher.  8. Milchstraßenselchnungen auf Grund photographischer Aufnahmen Photographische Photomotrie der Milchstraße	952 952 953 960
d)	Das allgemeine Blid der Milchstraße nach den visuellen und photographischen	2/2
	9 Der Verlauf der Mileistraße am Himmel in großen Zügen	962 962 963 967 972
o)	Der Einfiuß der diffusen Nebel auf das Milohstraßenbild ,	97!
	13 Die galaktischen Nebelfelder	975 975 975
ŋ	24 Die Absorption des Lichts im interstelleren Raume. ,	1009 1010 1022

I

			Scite
g)	Die	Dynamik der Milchstraße	1033
	26	Milchstraße und Gastheorie Rotation dei Milchstraße	1033
	27	Allgemeine statistische Mechanik des Sternsystems	1034
	28	Theorie der Sternströmung im typischen Steinsystem	1039
	29	Einheitliche Theorie des Milchstraßensystems	1042
	30	Die asymmetrische Geschwindigkeitsveiteilung in ihrei Beziehung zur Rotation	1048
	31	Differentielle Rotationseffekte in den beobachteten Geschwindigkerten	1056
	32	Die Beziehung zwischen dem Geschwindigkeitsellipsoid und der Rotation	1065
		Die Dimensionen, die Masse und die Rotationszeit der Milchstraße	1067
	34	Übersicht verschiedener Anschauungen über die Natur des Milchstraßensystems	1069
S	chy	verzeichnis	1151

#### Inhalt der ersten Halfte.

Chapter	1	Ann Arboi
Kapitel	2	Zur Statistik der Spektraltypen Von Dr FR BECKLR, Bonn
Kapitel	3	Die Temperaturen der Fixsterne Von Piof Di A Brill, Neubabelsbeig
Chapter	4	Luminosities, Colours, Diameters, Densities, Masses of the Stars By Prof.
		Di K Lundmark, Lund

		Erganzungen und Berichtigungen zu Band V.
		fabelle, dritte Zoile der eisten Kolumne lies $K/H\delta$ statt $K/H\gamma$
		Fig 9 hes OII 4076 statt OII 4016
Seite	177,	Gl (62) unter dem Integral hes $T_S$ statt $T_{Sl}$ , wo $T_S$ die schwarze Temperatur der Sternstrahlung für die Wellenlänge $\lambda$ bedeutet
Sorte	342,	Zoile 10 von oben lies at which statt of which
		Zeile 10 von unten lies working statt to work
Sorte	436,	Zeile 1 von unten, evcept ist zu streichen
		Zeile 17 von unten lies systems statt system
Sorte	482,	Zoile 13 von unten his and with spectrographically statt and spectrographically
Serte	497,	Fig 129 links hes Absolute Magnitude statt Apparent Magnitude Die Figur
		rührt nicht von Lönnguist, sondern von ten Bruggencate (Die Sternhaufen,
		Berlin 1927) her
Serte	513,	2 Gleichung lies $\Sigma = \Sigma$ statt $\Sigma - \Sigma$
Scite	530,	2 Tabelle, vorletzte Zeile lies F8 statt F0
Seite	535,	Fig 140, letztes Wort der Unterschrift hes magnitudes statt magnitude
Seite	570,	Zeile 10 von oben lies 20th statt 19th
Seite	572,	Zeile 17 von oben hes anagalactic statt galactic
Seite	641	Hinter der ersten labelle ist einzuschalten Wallenguist divided the stats
		into four groups according to bolometric magnitude, while von Zeipel and
		LINDGREN had divided them into four colour-groups, called g-giants, b- and
		a-type stars, f-dwarfs, and g-dwarfs Their results are given in the second part
		of the table together with the mean absolute bolometric magnitudes computed
		by Wallenguist for the different colour-groups used In both cases the mass
		of the stars in the second group has been selected as unity

#### Chapter 4.

# Luminosities, Colours, Diameters, Densities, Masses of the Stars.

Ву

#### KNUT LUNDMARK-Lund

(Continued.)

With 12 illustrations.

#### d) The Diameters of the Stars.

190. The Diameters of the Stars. Earlier Conceptions. Pioneer Work. The underestimation of the distance and the dimensions of the Sun that was a dominating feature of Greek astronomy, was adopted by the astronomers of the Occident and believed until the end of the 17th century Practically nothing was known about the physical nature of the stars until that time. The distances of the stars also were underestimated and that fact may explain why many observers thought that the stars displayed measurable diameters. It is clear that it was the irradiation and diffraction that deceived the pioneers. In order to illustrate the kind of rôle these phenomena sometimes play we quote some measurements of the "diameters" of different magnitudes

Apparent magnitudo	CANDAMISI	TYCHO THAMP	MAGNETUR	LANDS- BERGIUS	HOAM,	H pocsona*	Hewster'
1**	480"	120"	600"	60"	411	13",7-16",7	
3	360 240	90 65	330 240	40 30	6" 5	7 .9-12 .3 7.0	4.5 3.8
4 5	180 120	45 30	180	20 10	4 3	6,2 5,3	3.2 2.5
6	60	20	60	5	2	4,4	20

KEPLER<sup>8</sup> who must have had a poor eyesight, although not so poor as MAGINUS and CARDANUS, thought at first that the brightest stars displayed dismeters of 240" (Sirius), but, after the invention of the telescope, he states that when a larger magnification is used the diameters become smaller. He was con-

Noves coolestium orbium theoricae. Moguntiael (1608)

Uranometria, Middalburgi (1631).

Almagestum novum I, p. 424, 716 (1651).

<sup>&</sup>lt;sup>1</sup> Libelli duo, unus de supplemento almanach etc Norimbergae (1543)

Opera omnia 2, p 429 (1925); Astronomiae instauratae progymnasmata. Pragae (1602)

HORTENSIUS, Landsborgii commentationes in motum terrae Middelburgi (1630)

Mercurius in Solo visus, p. 92. Godani (1662)

Opera II, p 676, 689 (1859) Opera VI, p 335 (1866)

vinced that the stars had no appreciable diameters, but were "puncta mera" J Horrocks<sup>1</sup> also was of the same opinion A little later A Kirchi R<sup>2</sup> called attention to the optical phenomena tending to increase the size of small discs (e g diffraction) and concluded that the estimates of stellar diameters are ıllusory.

The thought that the stars displayed such appreciable drameters and the fact that no parallaxes could be derived from his observations convinced Tycho Brahe that the heliocentric system was not tenable and seem to have made

him start his short-lived compromise-system

The experiences of the telescope made it gradually clear that the diameters of the stars must be very small Llooke4 concluded that the dimensions of the stars were below 1" and later E HALLEY's reached the same conclusion

It was clear to I MICHELL that even in the case of Shins the apparent angular diameter must be less than 0",01 He pointed out that if the "native brightness" was in accordance with colour the white stars would have the largest

The different conceptions regarding the diameter of Surus since the middle ages are illustrated from the following summary

Authority	Diameter of Sirius	Authority	Diameter of Sirins
Albategnius	45"	Hewelke	6".57
Kepler	(240)	J Cassini	5
Galilfi	5,3	Michell	0 ,01
Van Dln Hove	10	W Herschel	<0 ,01
Riccioli	18	Actual value	0 ,0053

W. Herschel' examined a number of bright stars and used extremely high magnifying power in order to determine whether the stars have sensible dimensions He found that the telescopic discs appeared smaller with increasing telescopic power and accordingly he considered spurious the discs of light seen in telescopes He also used this phenomenon as a ready criterion for determining whether a small bright body has an appreciable size or only impresses the sense of sight by virtue of its intrinsic brightness

In 1835, F M Schwerd suggested a method for determining the diameters of the stars which is based on measurements with two different telescopes in order to climinate the influence of the diffraction and concluded that the

diameter of Altair is 0".104

The method applied by S STAMPFER® in 1852 is of much interest. The image of the Sun observed through a telescope was reduced through a globe of Mercury until it matched the image of a star seen in the same telescope. Stampfer concluded that the diameter of the first magnitude stars is 0",00491, which is a little to low, but of the right order of magnitude (0",0085)

<sup>2</sup> Ars magna lucis et umbrae, p 119 Romae (1646)

Wien Denkschr Akad Wiss II Cl 5, p 91 (1852)

<sup>&</sup>lt;sup>1</sup> Venus in Sole visa anno 1639, p 139, edited by HFVELIUS, see Note 7, p 575, De magnitudino fivarum Opera, p 61 (1672-78), ed by Wallis, London

Dpera omnia 2, p 429 (1925), Astronomiae instauratae progymnasmata Pragae (1602)
An Attempt to prove the Motion of the Earth, p 26 London (1674)

<sup>&</sup>lt;sup>8</sup> London Phil Trans p 853 (1718), p 3 (1720)

<sup>6</sup> London Phil Trans p 234 (1767) 7 Collected Works II, p 297 (1912)

<sup>&</sup>lt;sup>8</sup> Die Beugungserscheinungen aus der Undulationstheorie analytisch entwickelt Mannheim (1835)

In 1868 FIZEAU1 suggested a method for the direct measurement of the stellar diameters When interference is produced by the apparatus of Thomas YOUNG<sup>2</sup>, the murrors of FRESNEL<sup>8</sup>, or a biprism the apparent diameter of the light source must be very small, if the fringes are to be pure. If the diameter of the light source is varied, the sharpness of the fringes decreases as the diameter increases, and for a certain value of the diameter the fringes disappear Proportionality exists between the separation of the fringes and the limiting diameter of the source. The complete theory of this phenomenon has been given by A MICHRISON In 1890-924 He derived the condition that the fringes become myssible when the angular diameter D of the source is a little greater than the interval l that separates one fringe from the next Thus:

$$D = 1.22 l$$

The reason why the fringes disappear if the source has an extension is the following. Each separate point gives a system of pure fringes. The systems corresponding to different points will trespass upon each other's ground and mutually blend together. The condition for disappearance of the franges is that II uniform intensity should be produced, which happens when the law of MICHEL-BON is fulfilled.

The method of Fizeau was applied by Stephan at the Observatory of Marseilles in 1873 The objective of the 80 cm telescope was covered with an opaque screen that had two apertures placed symmetrically with regard to the contro. The two pencils converged at the focal plane and the image was examined under high magnification. The apparatus could not distinguish angular diameters less than 0",2. Since all the stars investigated gave very clear-cut fringes, it was possible to conclude that none of them had a diameter of 0".2, but that probably even the largest were far beneath this value.

The interferometer method was later independently applied by Michelson\*

and HAMY for the measurement of the satellites of Jupiter

In a paper of 1880 E.C Pickering gave a masterly treatment of the problem of determining the diameters of stars. He first derived the expression:

$$\log d_{\bullet} = \log d_{\odot} + 0.2 \, m_{\odot} - 0.2 \, m_{\bullet} - 0.5 \, \log_{1}.$$

d being the diameters expressed in seconds of arc and 1 the intrinsic brightness of the star (or in other words the ratio borne by the quantity of light emitted by the star to that emitted by the Sun from the same superficial area), me and mo the magnitude of the star and the Sun respectively

Substituting the numerical values then at his disposal the formula read:

$$\log d_{\phi} = 8,184 - 0.2 \, m_{\phi} - 0.5 \, \log_1.$$

PICKERING suggested the following way of determining the approximate value of j. An electric current heats a platinum-ridium wire to incandescence and the brightness of a short portion of it is compared with an artificial star, while the current is varied by a known amount. As the current increases the colour changes. The ratio of the blue light to red light may be determined by

<sup>1</sup> CR 66, p 932 (1868) Fixeau slee pointed out the possibility of using the phenomona of scintillation for the determination of stallar diameters,

London Phil Trans (1802), A Course of Lectures on Natural Philosophy, London (1807)

Ann Chim Phys I (1816); XI (1819), Paris Mom de l'Acad V (1826) 4 Phil Mag (5) 30, p 1 (1890), (5) 31, p 338 (1891); (5) 34, p 280 (1892); Amer J of Science (3) 39, p 115 (1890).

5 CR 78, p 1008 (1874)

6 Publ A S P 3, p 274 (1891)

<sup>7</sup> BA 16, P 257 (1899) Proc Amor Academy of Aris and Sciences 16, p 1 (1880)

inserting a double-image prism in the collimator of a spectroscope, and viewing the wire through it. The relative brightness of the two images is varied by a Nicol in the eye-piece, which can be turned a known amount.

Pickering also pointed out that only an approximate value of the comparative light emitted by equal areas of the two bodies can be obtained. The effect of absorption is not allowed for, and thus a difference of temperature is assumed to be the only cause of the observed difference in colour

As far as the author is aware this scheme was not put into practice before

it was applied in the Potsdam determination of stellar temperatures.

The term equivalent drameter, the drameter of the stars if they all had the same temperature as the Sun, was introduced by E.C Pickering by taking The following table gives this diameter for different magnitudes and represents very closely the means of the modern determinations where the temperature has been taken into account

_	Apparent	Equivalent	Apparent	Equivalent	Apparent	Equivalent
	magnitudo	diameter	magnitude	diameter	magnitude	diameter
	0 <sup>1n</sup> 1 2 3 4	0",0153 0 ,0096 0 ,0061 0 ,0038 0 ,0024	5 <sup>m</sup> 6 7 8	0",0015 0 ,0010 0 ,0006 0 ,0004 0 ,0002	10 <sup>m</sup> 11 12 13 14	0",00015 0",00010 0 ,00006 0 ,00004 0 ,00002

NORDMANN<sup>1</sup> has claimed that he should have priority for being the first who derived a formula how to compute the diameter of a star. In 1911 he derived the formula

$$\log\frac{R_*}{R_\odot} = \log\frac{\pi_{\rm O}}{\pi_*} - \left\{0.2\left(m_* - m_{\rm O}\right) + \frac{1}{2}\log\frac{E_*}{E_\odot}\right\},$$

where R are the diameters and E the "éclats intrinsèques effectives" or the surface brightnesses. The quantities  $\frac{R_*}{R_O}$  were computed for 10 stars from their effective temperatures

This attempt is certainly one of the first, but Nordmann cannot be given the priority, because Herrzsprung had already in 1906 advised essentially the same method<sup>2</sup>

Somewhat earlies than Nordmann wrote his paper also B v Harkanys had investigated the effective temperatures T of the stais and had derived formulae for computing the diameter of a star from T and  $m_{\rm vis}$  or  $m_{\rm ph}$ .

191. Wilsing's Investigations4. When estimating stellar colours several observers have remarked that the stars do not exhibit any other colouis than those represented in the radiation from cooling metals. The spectral-photometric work at Potsdam confirmed this view. It was found that the energy distribution in stellar spectra corresponded to that of a black-body radiator. If such is the case the colour or rather the effective temperature will be determined by a comparison with the energy distribution at the same temperature as the celestial body But the temperatures of terrestrial sources cannot be raised above 3000° It will then be necessary to transform the stellar radiation into radiation of a lower temperature This can be done by using mirrors that selectively reflect the incident light or by using absorbing media

<sup>&</sup>lt;sup>1</sup> CR 152, p 73 (1911)

<sup>&</sup>lt;sup>2</sup> Zf wiss Photogr 4, p 43 (1906)

<sup>&</sup>lt;sup>3</sup> A N 185, p 33 (1910), 186, p 161 (1910) <sup>4</sup> Potsd Publ No 76 (1920)

If a mirror is used with a reflection coefficient of  $ae^{-b/2}$ , then the reflected radiation is:

 $E = c_1 a \int_{\lambda^{-1}} \lambda^{-1} e^{-(a/T+b)\lambda^{-1}} d\lambda$ ,

and thus the reflected radiation corresponds to the temperature  $T_1$  which is determined by the formula  $c_1/T_1 = c_1/T + b$ . The only mirrors suitable for the purpose are those of gold. It was found by the aid of two parallel mirrors that after five reflections the effective temperature of the B and A stars could be brought to equality with that of an electric lamp. It was also confirmed that the spectral distribution did not change appreciably by the repeated reflexions. During the course of the work it was found that the use of a red-filter yields still better results than the reflection-method, and thus a red-wedge from Schott in Jenu was taken into use which has the property that its transmission is closely represented by means of the expression  $-(\beta_0 + \beta_1/\lambda)d\log s$ , where d is the thickness of the wedge. The red filter has been used in connection with a Zöllner photometer.

The intensity of radiation of wave length & outside our atmosphere is expressed

by means of  $a_1 \lambda^{-1} e^{-\gamma_0 - \left(\frac{c_1}{T} + \gamma_1\right) \lambda^{-1}}$ , where  $\gamma_0$  and  $\gamma_1$  are defined by the expression:  $\gamma_0 \log s = \log \left(1 - e^{-c_1/\lambda T}\right) - \frac{\gamma_1 \log s}{\lambda}$ ,  $\gamma_1 \log s = 0.0075 \cdot 10^{-3} (T - 3000)$ .

When the radiation has passed the atmosphere, its intensity is equal to

$$c_1 \lambda^{-1} s^{-\gamma_0 - \alpha_0 i} s^{-\frac{1}{\lambda} \left( \frac{\alpha_1}{T} + \gamma_1 + \alpha_1 i \right)}$$

where l is the relative path through the atmosphere at a certain distance from the zenith. This expression has further to be multiplied by the factor  $e^{-(k_1+\beta_i/k_1)}e^*$ , corresponding to the scale reading  $d=d'-\delta$ , where  $\delta$  is the scale-reading for the zero-point. The values for the photometer-lamp corresponding to T and  $e_1$  are T' and  $e_1'$ . By integrating the energy between  $\lambda$  4500 and  $\lambda$  6800 it is found that the equation can be divided into the two expressions:

$$c_1/T + \gamma_1 + \alpha_1 l + \beta_1 d' = c_1/T',$$
  
 $c_1 e^{-\gamma_1 - \alpha_2 l - \beta_1 d'} = c_1' \sin^2 \varphi.$ 

The reading of the intensity-circle gives the value  $\varphi$ . The first of the expressions gives the effective temperature in terms of T', d'; the constants are  $\alpha_1 = +0.938$ ;  $\beta_1 = +0.214$ . The ratio of the energy of two stars within the defined interval is given by the equation:

$$\log \frac{s_1}{s_1} = -2.5(m_1 - m_1) = 2(\log \sin \varphi_1 - \log \sin \varphi_1) - 0.138(l_1 - l_1) - 0.1420(l_1 - l_1) + \log \varphi(s_1) - \log \varphi(s_1).$$

 $\varphi(s)$  is the definite integral of the modified equation of Planck, viz.:

$$E = c_1 \int_{\frac{1-s_s}{s}}^{\frac{s_s}{2T}} \frac{d\lambda}{1-s} d\lambda = c_1' \sin^2 \varphi s^{\alpha_s l} + \beta_s d' \int_{\lambda-0}^{1-s} \frac{1}{\lambda} \left(\frac{s_s}{2} + h\right) d\lambda$$

$$= c_1' \sin^2 \varphi s^{\alpha_s l} + \beta_s d' \int_{\lambda-0}^{1-s} s^{-s_l l} dt = c_1' \sin^2 \varphi s^{\alpha_s l} + \beta_s d' \varphi(s),$$
or 
$$\varphi(s) = \left[\frac{s}{s} \frac{1}{\lambda^2} \left(1 + 3\frac{\lambda}{s} + 6\left(\frac{\lambda}{s}\right)^2 + 6\left(\frac{\lambda}{s}\right)^2\right)\right]_{\lambda+500}^{\lambda+600},$$
where  $s = \frac{a_s}{s} + \gamma_1$ .

A comparison between colorimetrically measured  $c_2/T$  and those derived from spectral-photometric values at Potsdam showed good agreement mean error for a three-day determination was in the former case in the mean

 $\pm 0.11$ , whereas the second method gave  $\pm 0.12$ .

Next a comparison was made between the colorimetrical magnitudes and the visual magnitudes in the Potsdam Durchmusterung. A somewhat unexpected result was found, namely that there was good agreement between the two different magnitudes. This agreement involves not only the possibility of the radiation in the whole spectral interval under consideration being represented by means of the radiation law, but it also involves proportionality between the radiated energy and the relative sensibility of the observer's eye to light of the different colours

The results of H E IVES1, H BENDER2, P G. NUILING8, and W. W COB-LENTZ concerning the visibility of radiation of the normal curve of the sensibility of the eye for different colours were collected and discussed. The physiological

intensity

$$\varphi_{\gamma}(\varepsilon) = \int_{0}^{2\pi} s_{1} \lambda^{-\delta} e^{-\varepsilon/\lambda} d\lambda$$

was determined by Wilsing, and it was found that  $\log[\varphi(\epsilon)/\varphi_s(\epsilon)]$  was remarkably constant. The limits for the wave lengths in the photographic region are 3600 A and 4850 A. The energy of this spectral region is then  $c_1 e^{-\gamma_0} \varphi_n(e_0)$ . where

$$\varphi_p(\varepsilon_p) = \int_{\lambda 3600}^{\lambda 1850} \lambda^{-5} e^{-\frac{\varepsilon_p}{\lambda}} d\lambda.$$

The following small table gives the values of this integral,

8	$\log \varphi\left(\varepsilon_{p}\right)$	z	$\log \phi (e_p)$
0,9	0,06	3,0	7,88
1,0	9,95	4,0	6,86
2,0	8,91	4,5	6,36

The difference  $\log \varphi_p(e_p + 1) - \log \varphi_p(e_p)$  is of sufficient constancy and thus

$$\varphi_{ps}(e_p) = \int_{\lambda 3600}^{\lambda 1850} s_p e^{-\frac{s_p}{\lambda}} d\lambda = a_p e^{-b_p s_p},$$

if  $S_n(\lambda)$  is the curve of sensibility of the plate

It is found that the proportionality between the radiation and the physiological intensity is not dependent on a symmetrical form for  $\varphi_s(\varepsilon)$  . Nor are the limits selected for the integration of much importance. In the case of the natrium cell the deviations from proportionality between the radiation and the intensity curve of the cell are considerable on account of the wider range in wave length (1 3650 to 1 5780)

The equations given above permit the establishment of a relation between the constants of the selective atmospheric extinction  $\alpha_0$  and the mean coefficient of transmission p The result of G MULLER that the influence of a selective absorption is negligible in the magnitude determinations of the stars was confirmed by Wilsing

Phil Mag 24, p 352 (1912).
 Dissert Breslau (1913)
 Phil Mag 29, p 301 (1915), Amer Illum Engin Soc Trans 9, p, 633 (1915).
 Scientific Pap Bureau Stand No 303 (1917)

With regard to the question of the physical meaning of the effective temperatures the measurements of the intensity in the solar spectrum are of much importance. It was found that the measured intensities could be very satisfactorily represented by means of the law of Planck, if the temperature was taken at 6070° abs By applying the radiation law of Winn certain systematic deviations were found. It was concluded that the solar radiation has the same properties as the black-body radiation if the deviations are neglected that are produced from the mixture of different temperatures that give rise to the solar spectrum.

The presence of the absorption-bands in the K and M stars 19 found to

influence the temperature to an amount of some 200°

It can thus be concluded that the effective and the real temperature of a star do not differ considerably. The diameters of the stars can then be approximated from the radiation law. The radiation in the visual and the photographic part of the stallar spectra can be represented by.

$$-0.4m_p = \log g \left(\frac{d}{d}\right)^8 e^{-\gamma_0 v} \int_{\lambda + 500}^{\lambda - 5} e^{-v d/\lambda} d\lambda + h_0$$

$$-0.4m_p = \log g \left(\frac{d}{d}\right)^8 e^{-\gamma_0 v} \int_{\lambda + 500}^{\lambda - 8} e^{-v d/\lambda} d\lambda + h_0$$

$$\lambda_{3600}$$

where d and  $\Delta$  are the diameter and distance of a star and g depends on the constant u in the Stefan radiation law and the radiation constant  $c_2$ . Further

$$\frac{1}{d} = 2 \frac{\pi}{\varrho_{\odot}} \sin \frac{1}{2} \varrho_{\odot}$$

is introduced, where  $\pi$  is the parallex,  $\varrho_{\odot}$  the linear diameter, and  $\varrho_{\odot}$  the apparent diameter of the Sun; then the equation is obtained

$$\log\left(\frac{e}{e_{\odot}}\right)^{n} = -0.4 \, m_{p} + 0.4 \, m_{\odot} + \gamma_{ep}(\epsilon_{p}) \log s - \gamma_{ep}(\epsilon_{\odot p}) \log s + \log m_{n}(\epsilon_{\odot p}) - \log m_{n}(\epsilon_{o}) - \log m_{n}(\epsilon_{o}) - \log m_{n}(\epsilon_{o})$$

which is simplified to

$$\log\left(\frac{\varrho}{\varrho_0}\right)^2 = -0.4 \, m_p + \gamma_{ep}(\varepsilon_p) \log \varepsilon - \log \varphi_p(\varepsilon_p) - 2 \log \pi - 1.35 \,,$$

putting  $m_{\odot} = -25^{m}.93$  and expressing m in seconds of erc.

The diameters corresponding to the visual magnitudes in P D are computed according to the formula:

$$\log\left(\frac{q}{q_{\odot}}\right)^{3} = -0.4 m_{\bullet} + \gamma_{\bullet \bullet}(r_{\bullet}) \log s - \log \varphi_{\bullet}(s_{\bullet}) - 2 \log \pi - 1.16.$$

The first formula was applied to 104 bright stars that had been measured for photographic magnitude by E. S. King<sup>1</sup> using the out of focus method. The following mean diameters for different spectral classes were found.

e/T	Spentral class	Diameter	п	a_fT	Spectral class	Diameter	
0,5-1,0 1,0-1,5 1,5-2,0 2,0-2,5 2,5-3,0	B B, A A, F F, G F, G	8,6© 5,9 2,1 5,0 8,9	12 4 8 12	3,0—3,5 3,5—4,0 4,0—4,5 4,5—5,0	G, K G, K K K, M	16,7⊙ 32,1 50,6 61,0	21 12 10 9

<sup>&</sup>lt;sup>1</sup> Harv Ann 59, Nr 6 (1912).

582

Wilsing computed a diameter value of  $\alpha$  Orionis of 0",0395 which is of a certain interest as being very close to the value 0",045, actually measured a year after Wilsing's prediction

It would certainly be of much interest to apply Wilsing's formula to the material in PD and Göttinger Aktinometrie, New Draper Catalogue, and other sources, and to derive the diameters from a consideration of existing values of

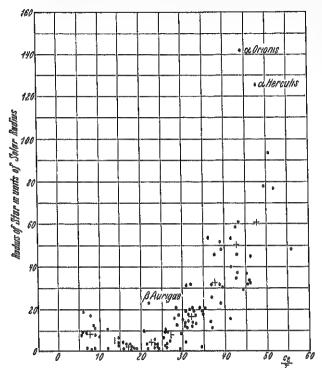


Fig 148 The radii of stars as a function of the inverse value of their effective temperature according to Wilsing's investigations. Dots denote individual values and crosses mean values. The minimum value of the radii around  $c_0/T = 20$ , corresponding to A stars, is no doubt caused by the selection in data because the main bulk of the investigated stars are giants. Compare the following figure

parallaxes or substitutes of parallaxes. In this way some 10000 star diameters of tolerable accumacy could be derived

J. Hopmann<sup>1</sup> has used the red-wedge coloumeter according to the construction of WIL-SING for measuring stars of spectral type N and red variable stars IIIs observations of twenty objects, mainly N stars, give for the temperature of the Na stars 2440° and for the Nb stars 2370°. HOPMANN has derived the diameter of 19 Piscium as 0",017 PETTIT and NICHOLSON® have computed the value 0".018 Thus the star might be measurable with the aid of the interferometer

thod. H. N Russell's Method. H. N Russell's discussed in 1920 the determination of the diameters of the stars If d is the apparent diameter, m the visual

magnitude and J the surface brightness of a star, it follows from elementary considerations that:

$$d = \text{const} \cdot 10^{-0.2m} J^{-\frac{1}{2}}$$

By inserting the data for the Sun the constant is found to be 0",0087, provided that the Sun's surface brightness is taken as unity. Further  $\gamma = -2.5 \log J$  is introduced The above equation may then be written

$$d = 0.0087(0.631)^{m-j}$$
.

The following method for determination of q was used. The difference

<sup>&</sup>lt;sup>1</sup> A N 222, p 237, 226, p 1 (1925); 226, p 225 (1926), <sup>2</sup> Mt Wilson Contr No 369 (1928), Ap J 68, p 279

<sup>8</sup> Publ ASP 32, p 307 (1920)

in surface brightness of two stars expressed in magnitudes is proportional to the difference in colour indices C. Thus for two stars

$$j_1-j_1=k(C_1-C_1)$$

The constant h depends on the wave lengths used in measuring the surface brightness and colour index, but is the same for all stars. As long as Wiren's formula can be applied,  $h = \lambda_{\rm phot}/(\lambda_{\rm vis} - \lambda_{\rm phot})$ , and at higher temperatures, when Planck's formula has to be used, the value of h gradually increases, since for an infinite temperature this formula gives infinite surface brightness, but finite colour index

The Sun permits a direct observational test of this law. The work of SCHWARZ-SCHLD, ABOTT, and LINDBLAD makes it very probable that different parts of the Sun's disc differ in colour and brightness, because at the centre we see down further and into hotter layers than near the limb where the lime of vision is more oblique. It can therefore be assumed that on passing from the centre to the limb of the Sun we meet successively with conditions very similar to those met with in the photospheres of cooler stars. Abbot's observations of 1913 have been used for a determination of k. In some cases the values closely agree with those predicted, but in others the discordances are considerable, probably on account of a departure from black-body conditions

The different scales of C have to be standardized on account of the fact that some of the scales are more open than the others. The standardization is made by deriving the ratios  $C/C_{Estan}$  in one and the same system. The colour index  $(C_{Katan})$  for K stars is then called the colour equation of the given system. A system for which  $C_{Katan}$  is exactly 1,00 was suggested by Pickering as a standard. Let K be the value of h, referred to such a system. For any other system of C, with a colour equation E, we have k = K/E. This new constant K is equal to  $f_{Astan} = f_{Estan}$ . In the case of Parkhursh's colour indices  $\lambda_{rh}$  is 5410 and  $\lambda_{rh} = 4280$  and thus k = 3.8. In order to correct for the systematic difference between his spectra and those of Harvard Russell takes E = 1.27 and hence K = 4.8. An independent system of colour indices has been derived by Rosenberg from photographic spectra and gives the intensity at  $\lambda$  4000 relative to that at  $\lambda$  5000. Arranging his data according to the Harvard spectral classification Russell finds  $C_E - C_A = 1.83 - 0.40$  and K = 6.7 for  $\lambda$  5200 A

Then the stellar temperatures determined by Wilsing and Schriner were used. By applying Planck's formula Russell has found K=4.0 for 25200 A. Also other astronomical data could be used, e.g. eclipsing binaries, or a comparison of densities of eclipsing binaries with the relation between density and surface brightness derived from visual double stars. Russell derived in

his address of 1914 the relation.

Spectral class	C	1	Spectral class	C	1
B	-0,3 0,0 +0.3	-1,2 0,0 +0,9	G M	+0,7 +1,6	+2,0 >4,5

Also the concomitant variations in magnitude and colour index of the Cephelds can be used, provided that the observed variation is due to changes of temperature in a radiating surface of constant area. This assumption is very dubious, as has been pointed out by Russell

Pop Astr 22, p. 339 (1914).

Method	K
PARKHURST, colour indices ROSENBERG, colour indices Wilsing and Scheiner, temperatures	4,8 6,7 4,0
U Cephei (direct observations) Echpsing variables (colour indices)	3,2 3,1
Comparison of eclipsing variables and binary stars Colour change of Cepheids	3,5 2,3
i	Mean 3.9 ± 0.4 Adopted 4.0

Then the colour indices of King, Schwarzschild, Parkhursi, and Haivard are expressed in units of  $C_K - C_A$  so that they all have C = 1,00 for K0 stars. The values of I are derived. The small table given here will facilitate considerably the computation of d When the parallax is known the linear diameter D is found by  $D = 9.22 (0.631)^{M-j}$ , the Sun's absolute magnitude being 4.83

Spectral class	-,	Spectral class	1	m-1 M-1	đ	D
B0 B2 B5 B8 A0 A2 A5 F0 F5	+3 <sup>m</sup> ,2 +3 ,0 +2 .7 +2 .5 +2 .1 +1 .7 +1 .3 +1 ,0 +0 ,6	F8 G0 G5 K0 K2 K5 Ma Mb	+0 <sup>tot</sup> ,1 0,0 -0,9 -1,9 -2,9 -3,3 -3,7 -4,0 -6,3	0, <sup>m</sup> 0 0, 5 1, 0 1, 5 2, 0 2, 5 3, 0 3, 5 4, 0 4, 5 5, 0	0",0087 69 55 43 34 27 22 17 14 11 0",0009	9,2 O 7,3 5,8 4,6 3,7 2,9 2,3 1,8 1,5 1,2 0,9

A number of diameter-values were computed by Russell, and among these were values of  $\beta$  Andromedae, Betelgeuze, and Antares Betelgeuze was measured about a year later with the interferometer, it was found then a very good agreement between the diameters actually measured and those computed by Russell, Wilsing, and others

193 Diameters from  $c_2/T$ . As has been described in the chapter on stellar colours, E HERTZSPRUNG1 has reduced the principal determinations of colours or colour equivalents of the brighter stars to a homogeneous system from which  $c_2/T$  is derived. These values have been used for a derivation of the angular diameter d of 734 stars according to the formula

$$5 \log \sin \frac{d}{2} = -43.44 + 2.3 (c_2/T)^{0.93} - m$$

All the available trigonometric parallaxes of these stars as well as all available spectrographic data have been collected by me and the values of the linear diameters computed in terms of that of the Sun Also  $n_{s\mu}$  has been used. It is evident that in many cases already a knowledge of the colour and proper motion will give the linear diameter of a star with fair accuracy

K F Bottlinger2 has derived the following linear diameter formula

$$\log D/2 = 0.2(m_{\rm O} - m_*) - \log \pi + (\log c_2/T_* - \log c_2/T_{\rm O}) + 5.3144$$

where D is the linear diameter in units of the diameter of the Sun; the magnitudes are reduced to the bolometric scale. The diameters were first computed

<sup>&</sup>lt;sup>1</sup> Leiden Ann XIV 1 (1922) <sup>2</sup> Berlin-Babelsberg Veröff 3, H, 4 (1923)

for 104 stars for which the colour index had been measured photo-electrically In a subsequent paper<sup>1</sup> the diameters have been computed for some 400 stars. The diagram connecting diameter and spectral class shows a certain resemblance with the Russell diagram. The dispersion in diameter on the giant branch is considerable and it does not seem quite impossible that we have, in fact, two branches, a giant and a supergiant branch. The fact that the diameter values computed on the basis of data of echpsing binaries do not deviate systematically from the values computed from the temperatures is of a certain importance

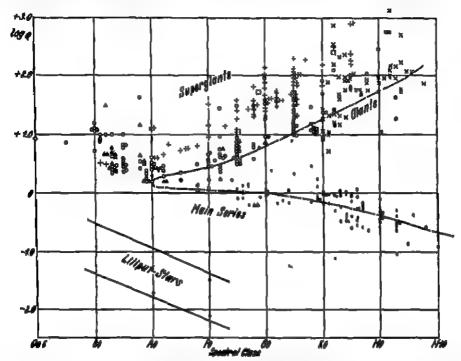


Fig. 449 Distribution of the logarithms of the diameters of stars within different spectral classes according to Bottlimer. The triangles denote collipsing binaries, dots trigonometric parallaxes or dynamical parallaxes of high weight, open circles theoretical parallaxes (moving clusters, companions) Further denote  $\times$  spectrographic parallaxes and + parallaxes of Cophekis. The two squares give the mean values of log  $\varrho$  for the  $\circ$  stars

BOTTLINGER suggests the name liliputian stars for the white dwarfs. The spectra should according to his proposal be denoted e.g. I B9

194. Diameters from Radiometric Measurements, PETTIT and NICHOLSON<sup>S</sup> have derived the following expression:

$$\log T = 2.638 - 0.1 (m_r - \Delta m_r) - 0.5 \log d$$

where d is the apparent diameter of the star in seconds of arc and T is the temperature,  $m_r$  the apparent radiometric magnitude of a star, and  $\Delta m_r$  the correction to no atmosphere including atmospheric absorption and losses in the telescope. The following table contains the diameters measured directly by PRASE, and the diameters computed from the above formula with temperatures

Seeliger-Festschr p 338 (1924).

<sup>&</sup>lt;sup>4</sup> Mt Wilson Contr No 369, Ap J 68, p. 279 (1928).

derived from water-cell absorptions and from heat indices, it further contains the temperatures computed from measured d, water-cell absorptions, and heat indices (comp ciph 187)

Object			Diameter		Absolute temperature		
		Mersured by interfero mater	Computed from m <sub>er</sub>	Computed from C <sub>II</sub>	From measured d and mr	Γrom ##≡	I rom C <sub>H</sub>
Arcturus Aldebaran Betelgeuze Antares β Pogasι W Herculis Λ ο Cett A (max )	•	0",020 0 ,020 0 ,047 0 ,040 0 ,021 0 ,030 0 ,056	0",031 0 ,033 0 ,071 0 ,062 0 ,029 0 ,065 0 ,038	0",028 0 ,031 0, 076 0 ,065 0 ,028 0 ,090 0 ,073	4300° 3890 3270 3270 3140 3320 2210	3440° 3080 2700 2680 2730 2340 2610	3580° 3170 2600 2620 2730 2030 1970

195 Kalmars Investigation 1 The author starts from the following formula which is easily derived

$$\log \varrho = 0.5 \log J_{\rm O}/J_{*} - 2.6243$$

where  $J_*$  is determined from the equation of Planck

$$J_{\pm} = C \int_{1}^{\lambda_{0}} \lambda^{-5} \left( e^{\frac{c_{0}}{\lambda T}} - 1 \right)^{-1} d\lambda.$$

C is equal to  $590\,\mu^2\,\mathrm{erg\,sec^{-1}}$ ,  $c_2=14600\,^\circ\mu$  degree Celsius. As limits for the integral  $\lambda_1 = 0.40 \,\mu$ ,  $\lambda_2 = 0.76 \,\mu$  have been taken. The following substitution 1s made

$$a=\frac{c_2}{\lambda_1 T}$$
,  $b=\frac{c_2}{\lambda_2 T}$ ,  $x=\frac{\frac{c_2}{\lambda T}-a}{b-a}$ ,

$$J_* = C(a-b) \left(\frac{c_2}{T}\right)^{-4} \int_0^1 \frac{[a-x(a-b)]^3}{[e^{a-x(a-b)}-1]} dx$$

The integral is then evaluated by means of mechanical quadrature If r and Rare the radius and distance of the star and of the apparent radius

$$r = R \operatorname{tg} \varrho$$

Introducing the parallax  $\pi$  and measuring R in light-years we have

$$\log \pi_0 = \log \pi + 0.2 \, m$$
, and  $R = \frac{3.228}{\pi}$ 

where  $\log \pi_0$  is the parallax reduced to apparent magnitude m=0.

From the derivation of stellar temperatures by BRILL<sup>2</sup> the following values have been taken

Spectral class	В	A	I,	G	К	M
$c_2/T$	1,22	1,51	2,06	2,81	3,74	4,17
For the	he Sun c	T = 2.39	$J_{\Omega}$	== 52,75	ergsec-1	u - 2

A number of the existing parallaxes had to be excluded on account of uncertainty The author has selected 260 parallaxes, from which the following values of  $\pi_0$  have resulted

A N 233, p 93 (1928) Also thesis in Budapest (Hungarian),
 A N 219, p 21 (1923).

	 В	В	A	•	B	=	G	#	K	35	14	В
Giants .	 0",170 —	21 —	0",138 0 ,284	13 26	0″,140 0 ,796	7 45	0",132 1 ,263	14 56	0",128 4 ,031	15 54	0 <sup>4</sup> ,122 6 ,158	7

From the data at hand the following results have been found by KALMAR.

Spect		Absolute temperature	Guriaen brightness J <sub>+</sub>	Mean opp.	Moon red dist. Re	J.inner radius
Glants	MKGFA	3500° 3900 5200 7100 9700	2,38 4,53 23,46 87,00 266,73	0",0198 0 ,0144 0 ,0063 0 ,0031 0 ,0019	26,5 26,0 24,6 23,0 20,9	34,8 ⊙ 24,8 10,3 4,7 2,7
Dwarls :	B F G K M	12000 9700 7100 5200 3900 3500	475,23 266,73 87,00 23,46 4,53 2,38	0 ,0014 0 ,0019 0 ,0031 0 ,0063 0 ,0144 0 ,0198	18,1 10,3 5,3 2,2 0,8 0,6	1,8 1,3 1,1 0,9 0,8 0,7

196. Interferometer Measurements at Mount Wilson. The reason why the interferometer method was not applied earlier to diameter measurements of stars must have been because astronomers have thought that atmospheric disturbances are a too serious source of arror. As a matter of fact observations have proved to be feasible even when visibility is poor. According to A. Michelson and F. G. Pease<sup>1</sup> the explanation is that the atmospheric disturbances, being uregularly distributed over the surfaces, simply blurr the diffraction pattern. In the case of two isolated pencils, too small to be affected by such an integrated disturbance, the resulting interference fringes, though in motion, are quite distinct unless the period of the disturbances is too rapid for the eye to follow them<sup>2</sup>.

As the diameter of the 100 inch reflector was not sufficiently large for the fringes to vanish, an interferometer with movable outer mirrors was constructed. The maximum separation was 20 feet.

Four mirrors,  $M_1$ ,  $M_2$ ,  $M_3$ ,  $M_4$ , and  $M_4$ , about 150 mm in diameter, inclined at 45° to the base, are mounted on slides.  $M_4$  and  $M_4$  are adjusted by three scrows at the back, and  $M_1$  and  $M_4$  can be adjusted about two horizontal axes by means of fine scrows at the ends of lever arms. The mirrors  $M_2$  and  $M_4$  are kept fixed at a constant separation of 114,2 cm, except that  $M_4$  has a motion of several millimetres along its slide and parallel to the beam.

The fringe pattern has a spacing equal to 0,02 mm and is easily visible with a magnification of 1600.

The observations are made at the Cassegrain focus, corresponding to an equivalent focal length of 40,84 m. Two pencils from the star are reflected from the outer mirrors,  $M_1$  and  $M_4$ , to  $M_2$  and  $M_3$ , and from there along the ordinary optical way to the large mirror, the convex mirror, the Coudé flat, and finally to the focus. The coincidence of the pencils at the focus is obtained by adjusting

Mt Wilson Contr No 184, 185 (1920) and No. 203 (1921), Ap J 51, p. 257, 263;

<sup>53,</sup> p 249
Recent work by W. A. CALDER at Harvard College Observatory [Harv Bull 885 (1931)] using the Harvard 15 inch refractor and a stellar interferements in front of the objective, emphasizes the importance of good seeing at interferements measures. Calder concludes: "... that the statements frequently found to the effect that, in contrast what might be expected, the interferements does not require excellent seeing conditions, are unduly optimistic. Atmospheric conditions appear to be the controlling factor, and seriously restrict the possibilities of the interference method."

the outer milios  $M_1$  and  $M_4$  and then tilting a plane parallel glass plate of 15 mm thickness in the path of one of the pencils. The equality of the paths of the pencils is obtained by setting the outer mirrors as nearly symmetrically as possible on the beam, and then by adjusting a double wedge of glass in the path of one of the pencils, the relative motion of the wedges alters the paths slowly and continuously.

In order to obtain "zero" fringes for purposes of reference the end of the telescope tube is entucly covered, except for two apertures in the beam 152 mm in diameter. The pencils entering these apertures pass through the wedges and the compensating plate, and produce an image of the star in the field of vision; when they have been adjusted for coincidence and equality of path, these pencils interfere and produce the zero fringes which cross the reference images

The interferometer images are next brought into the field of the eyepiece and made to coincide at a short distance from the zero star, thus forming a second star in the field. The parallel plate compensator is used only for differential deflection of the steel beam. When the wedge is moved in order to equalize the difference in the path of the interferometer pencils, the zero fringes disappear, and the number of turns of the rod are determined which are required to bring the first fringes into view. The mirror  $M_3$  is then moved a small amount in order to compensate for this difference. After several trials both sets of fringes are seen in the field of vision crossing their respective images.

The distribution of light in the disc to be measured is represented by the formula:  $I = I_0 (R^2 - r^2)^n$ 

where r is the distance from the centie, R the radius of the star, and n the exponent expressing the amount of darkening at the limb. The visibility V of the interference bands is defined by

$$V = \frac{1}{P} \sqrt{C^2 + S^2}$$

$$C = \int F(x) \cos kx \, dx, \quad S = \int F(x) \sin kx \, dx,$$

$$P = \int F(x) \, dx, \quad k = \frac{2\pi_b b}{l_{eff} d},$$

where

f

in which b is the distance between the two pencils entering the interferometer,  $\lambda_{\rm eff}$  the mean effective wave length of the light-source, d its distance, and F(x) dx is the total intensity of a strip of the source having a width of dx in a coordinate system where x, y are the coordinates of  $\epsilon$  luminous point in the disc of the star. The star disc must be symmetrical and thus.

$$V = \frac{C}{P}$$

Assuming the illumination to be a function of the distance from the centre in the way indicated above we have, when substituting  $r^2 = r^2 + y^2$ 

$$F(x) = \int_{0}^{\sqrt{R^{2}-x^{2}}} (R^{2} - x^{2} - y^{2})^{n} dy$$

Expanding in series and substituting in V Michelson and Pease 1 find:

$$V = \frac{\int\limits_{0}^{R} (R^{2} - v^{2})^{\frac{9}{2} \frac{n+1}{2}} \cos kx \, dx}{\int\limits_{0}^{R} (R^{2} - x^{2})^{\frac{2n+1}{2}} \, dx}$$

<sup>&</sup>lt;sup>1</sup> Mt Wilson Contr No 203, Ap J 53, p 249 (1921)

The following table computed under the direction of F R. MOULTON gives the values of the integral.

 $F(h,n) = \int_{0}^{1} (1-x^{2})^{\frac{2s+1}{2}} \cos hx \, dx.$ 

	s=0		n=0,5	_	g=1		<b>#</b> →2
100 130 160 230 240 280 320 360 440 440 520 600	F (h, n) +0.785 +0.507 +0.378 +0.243 +0.065 -0.024 -0.050 -0.100 -0.095 -0.053 -0.007 +0.036 +0.042 -0.011	30 60 90 120 150 180 240 240 257,45 270 300 330 360 390 420 480 510 540 570 600 630	F (h, n) +0,785 +0,765 +0,702 +0,607 +0,490 +0,363 +0,238 +0,127 +0,038 +0,000 -0,024 -0,057 -0,068 -0,059 -0,016 +0,005 +0,019 +0,009 +0,009 -0,002	30° 40° 80° 120° 160° 200° 240° 280° 320° 360° 440° 480° 520° 640° 640° 680°	F (h, s) +0.785 +0.785 +0.663 +0.536 +0.383 +0.237 +0.112 +0.024 -0.029 -0.045 -0.039 -0.030 +0.012 +0.013 +0.005 -0.004	40 80 120 160 200 240 280 320 360 400 440 480 520 640 680 720	F (A, n) +0.785 +0.761 +0.694 +0.590 +0.468 +0.342 +0.123 +0.054 +0.003 -0.019 -0.024 -0.006 +0.005 +0.005 +0.005

The authors point out the theoretical possibility of deriving the actual distribution of light in the source from observations of the visibility curve itself. Even if the present means are not able to give such a result, it does not seem impossible that future observations will do so.

If  $b_1$  and  $b_2$  are the distances for which the fringes vanish the first and second times, the following formula gives a fair approximation to the value of n:

$$n = -1 + 75 \left( \frac{b_1}{b_2} - \frac{1}{2} \right)^2.$$

Denoting the visibility of the first negative maximum by Vmax we have:

$$n = 0.22 \left(\frac{1}{V_{\text{max}}} - 7.8\right)^{0.7}$$

The value sought by the measurements is F(k, n) = 0 or the separation between the outer minors  $M_1$  and  $M_2$  for which the fringes vanish P. Merrill, when using the Anderson interferometer used for the investigation of the orbit of Capella, found that the visibility of the fringes of  $\alpha$  Orionis decreased, for the maximum separation of 100 inches, in that apparatus. As the decrease was independent of the position angle of the interferometer the star was certainly not a binary.

On December 19, 1920, after the adjustment of the instrument had been checked by means of settings on other stars,  $\alpha$  Orionis was investigated. A separation of 121 inches did not give any fringes for that star, although the zero fringes were quite visible. The disappearance of the interferometer fringes evidently could not be caused by any disturbances of an instrumental nature. The instrument was not provided at that time with means for continuously altering the distance between the movable mirrors

The effective wave length was assumed to be  $\lambda$  5750 for  $\alpha$  Onionis, and the angular diameter was thus found to be

$$d = 0'',047.$$

Somewhat later J A Anderson made an investigation of the effective wave length and found the value  $\lambda_{eff}$  5520, from which it follows that:

$$d = 0'',045 \pm 0'',0045$$
.

The stars for which a value of the diameter has been found by direct measurements are the following:

			Pai	rallax		Diameter in linear measure	
Star	Diameter	Trigo nometric	Spectro graphic	Spectral proper motion	Concluded value		
α Orionis	0",047	0",011	0",010	0",012	0",011	460 O	
α Bootis	0 ,022	0 ,085	0 ,131	0 ,158	0,090	26	
α Scorpn	0 ,040	0 ,026	0 ,013	0,010	0 ,020	160	
o Ceti ,	0,056	0 ,011	_	0 ,020	0,010	600	
a Herculis	0 ,021	0 ,030	0 ,002?	800, 0	0 ,007	320	
a Tauri	0 020	0 ,057	0 ,083	0,096	0 ,060	36	
β Pegasi .	0 ,021	0 ,019	0 ,023	0 ,028	0,020	110	
y Andromedae	(0 ,014)	0,010	0 ,007	0 ,024	0,010	(150)	
α Arietis	(0 ,011)	0 ,037	0 ,053	0,046	0,040	(30)	

The values within parentheses depend on extrapolation of the visibilitycurves and on a correction for seeing, and are hence uncertain and subject to changes when a larger separation can be used, so that the actual disappearance of the fringes will be estimated

The value for a Orionis is given above as 0",045 and the mean value of 8 determinations is 0",042. I have preferred to use the original value from

1920 The value for a Scorpii has been checked at different epochs

The linear chameter D is found from the formula  $D=107.5 \ d^{n}/\pi''$  On account of the importance of knowing the linear dimensions the existing values of the parallaxes have been discussed with great care, as an example, we give in some detail the discussion for  $\alpha$  Orionis,

 $\alpha$  Orionis Six trigonometric values of the parallax are known  $+0'',034 \pm 0'',024$  (Yale),  $+0'',018 \pm 0'',007$  (Schlesinger),  $+0'',022 \pm 0'',007$  (Led);  $+0'',013 \pm 0'',006$  (Mitchell),  $+0'',014 \pm 0'',006$  (Van Maanen), and  $-0'',005 \pm 0'',007$  (Alden) Spectrographic determinations are 0'',012 (Mount Wilson), 0'',014 (Norman Lockyei Observatory), 0'',009 (Victoria). The spectral proper motion method gives  $\pi_{8i} = 0'',012$ .

A weighted mean of the trigonometric values gives 0",014 and of the spectrographic values 0",010. The high luminosity of  $\alpha$  Orionis makes it probable that its mass is high. Thus a systematic difference ought to be present between  $\alpha_{tr}$  and  $\alpha_{s}$ . But if a mass factor is present the luminosity would be too small in the second case and the parallax too large. It thus seems that either the parallaxes available do not suggest such an effect or the mass is small

Anyhow it seems that the best parallax value to be derived from the material

is 0",011.

197. Varying Stellar Diameters. The most sensational discovery concerning the diameters of the stars is without doubt that of Pease<sup>2</sup> that the dimensions of  $\alpha$  Orionis vary between certain limits. Numerous tests have shown that the

Mt Wilson Contr No 222 (1922), Ap J 55, p 48

<sup>&</sup>lt;sup>2</sup> Publ ASP 34, p 346 (1922), Mt Wilson Reports 1920—1928

variation must be real. Thus it is proved that pulsations occur among the stars. The data are too few to admit the establishment of correlations between the apparent magnitude, the radial velocity, and the diameter. There seems to be some relation, but the observations are too few. Besides, the estimates of magnitudes are liable to considerable uncertainty on account of the lack of comparison stars and the rather exceptional colour of the star. The following determinations have been obtained by Pease.

Epoda	Apparent chameter	Rpoth	Apparent dissocion
December 1920	0",047	December 1924 . ,	0",044
Suptember-November 1921	0 ,054	December 1925 ,	0 ,034
October 1922	0 ,034	December 1926	0 ,041
December 1923	0 ,041	February 1928	0 ,037

Adopting the parallax above the following values of the linear diameter are found:  $460 \odot$ ,  $540 \odot$ ,  $330 \odot$ ,  $400 \odot$ ,  $430 \odot$ ,  $330 \odot$ ,  $400 \odot$ , and  $360 \odot$  respectively. This gives a mean value of  $400 \odot$  and a dispersion of  $\pm 71 \odot$  around the mean.

It is possible that the dimension of Mira Ceti also varies, but the observations available cannot decide this question.

The new interferometer with a maximum base of 50 feet was taken into use at the end of 1930, with this magnificent instrument the number of measurable stars will be increased to forty or more. In the Mt Wilson Report for 1931 it is stated that the adjustment and operation of the 50 feet interferometer have been continued by PEASE, who has observed fringes with mirror-separations up to 44 feet. Measurements of  $\alpha$  Orionis give an angular diameter of about 0",040 and of  $\beta$  Andromedae 0",046.

198. The Theoretical Investigations of M. Hamv. M Hamv' has proved that the light E of a point in a circular star can be expressed by the convergent series.

$$B = A_0 + A_1 (1 - \rho^2)^{\frac{1}{2}} + A_2 (1 - \rho^2) + A_3 (1 - \rho^2)^{\frac{1}{2}} + \cdots$$

where  $\varrho$  is the ratio between the angular distance of the point considered from the centre and the angular diameter, and  $A_0, A_1, A_2, \ldots$  are constants depending on the constitution of the stellar atmosphere

For the Sun and  $\lambda_{eff} = 5062 \,\mathrm{A}$  we have:

	Keibu	Kennag	e	Ethi	Rome
0.00	1,0000	1,0000	0,825	0,7196	0,7195
,20	0,9891	0,9882	0,875	0,6605	0,6607
40	0,9510	0,9505	0,92	0,5909	0,5911
.55	0,8998	0,9003	0,95	0,5289	0,5285
,65	0.8516	0.8521	0,97	0,4719	0,4721
.75	0.7871	0.7865	-177	0,1,1,2	*,,,=,

The values  $E_{\text{comp}}$  are formed from the following values of the constants derived by the aid of a least square solution:

$$A_0 = 0.257379$$
  $A_1 = 0.941025$   $A_2 = -0.255333$   $A_4 = -0.019945$ 

The formula for E has an interesting application to the measurements of the diameters of the stars,

<sup>&</sup>lt;sup>1</sup> CR 174, p 342 (1922); Journal de Mathématiques pures et appliquées 1917 and 1920; B A Mém et Var I, p. 198 (1920).

When two apertures are used the fringes of Young will disappear as soon as the well-known relation  $\varepsilon=1{,}22\frac{\gamma_{\rm eff}}{T}$ 

is fulfilled,  $\epsilon$  is the angular diameter of the star and l the distance between the apertures. The relation presumes the star disc to be uniform

It is also possible to determine the value of and the variation in the surface brightness of the star in cases where an absorbing atmosphere gives a non-uniform distribution of light over the disc, if the ratios of the intensities of the maxima and minima of the fringes have been observed

If l is the value for which the fringes disappear,  $K_i$  the ratio of the intensities when the distance is  $l_i$ , and  $\alpha_i = l_i/l$ , and if further  $m = \pi_0 \frac{ls}{\lambda_{eff}}$  and  $m_i = \pi_0 \frac{ls}{\lambda_{eff}}$  and thus  $m_i = m\alpha_i$ , we obtain, by using the expression above for E, the following equation

$$A_0[f_0(m_i) - K_i F_0(m_i)] + A_1[f_1(m_i) - K_i F_1(m_i)] + = 0$$

The value of the n constants is determined from n equations, that is, from n determinations of the K. The functions n and n are known and depend on the evaluation of an integral of the form

$$\int_{\lambda}^{1} (1-x^2)^{p+\frac{1}{2}} \cos qx \, dv,$$

where p is a whole positive number or zero and q has not a high value. In a subsequent note HAMY makes use of the following designations:

$$\begin{split} U_0 &= \sum_{n=0}^{n=\infty} (-1)^n \frac{m^{2n}}{(1\cdot 2 - n)^2} \frac{1}{n+1} = \frac{4}{\pi} \int_0^1 (1 - u^2)^{\frac{1}{2}} \cos 2mu \, du, \\ U_1 &= \sum_{n=0}^{n=\infty} (-1)^n \frac{m^{2n}}{(1 - 2 - n)^2} \frac{1}{(n+1)(n+2)} = \frac{8}{3\pi} \int_0^1 (1 - u^2)^{\frac{3}{2}} \cos 2mu \, du, \\ B &= \frac{A_0}{2} + \frac{A_1}{2} + \frac{A_2}{4} + \frac{A_3}{5} + \frac{A_1}{6}, \\ C &= A_0 \frac{U_0}{2} + A_1 \frac{1}{4m^2} \left( \frac{\sin 2m}{2m} - \cos 2m \right) + A_2 \frac{U_1}{2} \\ &\quad + A_3 \frac{9}{4m^2} \left[ \frac{1}{4m^2} \left( \frac{\sin 2m}{2m} - \cos 2m \right) - \frac{1}{3} \frac{\sin 2m}{2m} \right] \\ &\quad + A_4 \frac{1}{4n^2} \left( 2U_1 - U_0 \right) \end{split}$$

The coefficients  $A_0$ ,  $A_1$ ,  $A_2$ ,  $A_3$ ,  $A_4$  in the expression for C are tabulated in the table on p 593

Hamy shows that the maxima of intensity are proportional to B+C and the minima to B-C.

If  $l_0$  is used as a designation for the value for which the fringes disappear, the ratio K then equals unity If  $\alpha_1 = l_0/l$  and  $\mu = m_0/\alpha_1$  we have the following system

2C = 0

For  $l = l_0$ , m = n

外域

<sup>1</sup> CR 174, p 904 (1922)

$$\mu, \frac{A_1}{A_0}, \frac{A_0}{A_0}, \frac{A_0}{A_0}, \frac{A_3}{A_0}$$

The diameter  $\varepsilon$  is found from

$$\mu = \pi_0 \frac{I_0 z}{\lambda_{\text{eff}}}$$
.

In the case of the Sun the application is simple because the law of distribution of the intensity is known. If the diameter is a when consideration is taken of the variation in intensity on the solar disc, and a when no variation in intensity is supposed, the following relation is found.

In the case of super-giants and ordinary giants the correction is certainly much larger on account of the extended atmosphere and the rapid falling off in intensity towards the limbs

Later on HAMY<sup>1</sup> considered the case where the dimension of the apertures could not

Щ	4,	$A_1$	A <sub>1</sub>	A,	A,
0,0	+0,5000	+0,3333	+0,2500	+0,2000	+0,1667
0,1	.4975	,3320	,2492	,1994	1663
0,2	,4901	,3280	,2467	,1977	.1650
0,3	4779	,3215	2426	1949	,1630
0,4	.4611	,3125	.2369	,1910	,1601
0,5	,4401	,3012	2298	1861	.1565
0,6	4153	,2877	,2213	1802	1522
0,7	,3871	,2724	.2116	1735	1472
0,8	,3562	,2554	,2008	,1659	,1417
0,9	,3231	,2371	,1890	.1577	,1355
1,0	,2884	,2177	,1764	,1489	,1290
1,1	,2527	,1975	,1632	,1395	,1220
1,2	,2168	,1769	,1496	,1298	,1147
1,3	,1811	,1561	,1308	,1198	,1071
1,4	,1464	,1354	,1219	1097	,0993
1,5	,1131	,1152	,1080	,0996	,0916
1,6	,0817	,0957	,0944	.0895	,0838
1.7	,0527	,0771	0813,	,0796	,0760
1,8	,0265	,0597	0086	,0699	,0684
1,9	十0,0034	,0436	,0567	,0606	,0610
2,0	-0,0165	,0290	,0455	,0518	.0538
2,1	,0330	,0160	,0352	.0435	,0469
2,2	,0461	十0,0047	,0258	.0357	,0404
2,3	,0558	一(),0049	,0174	,0285	.0343
2,4	,0622	,0128	10104	,022()	,0286
2,5	,0655	10150	+0,(X)37	,0162	(1233
2,6	,0660	,0236	~-0,0016	0110	0486
2,7	,0640	,0267	,0059	,0065	0143
2,6	,0597	,0283	,0094	+0,0027	,0105
2,9	.0537	,0287	0119	-0.0005	,00 <del>7</del> 1
3,0	,0461	,0280	,0135	,0031	0043
3,1	,0376	,0263	,0144	0051	1 0,0018
3,2	,0284	,0238	,0147	,0066	-0,0002
3,3	,0190	,0207	,0143	,0075	,0018

be considered as negligible in comparison with the distance between them. In his earlier work he had reached an approximative solution,

,0096

,0148

.0210

,0258

-0,0007

+0,0076

0172

,0135

,0096

O058

-0.0021

十0,0012

[+0,0294 | + 0,0042 [-0,0x)35 |

,0135

,0123

,0109

,0091

,0073

,0054

3,4

3.5

3,6

3.7

3,8

3,9

If we denote the common width of the apertures by s, the distance between them by l, by  $\Theta$  the angular distance from the centre of a point in the focal image of the star taken parallel with the line joining the centres of the apertures, by w another angle in the same direction as  $\Theta$ , then the intensity I in the direction  $\Theta$  is proportional to the integral:

$$\int_{-e/2}^{e/2} \left(\frac{e^a}{4} - w^a\right)^b \left[ \frac{\sin \frac{m_e a}{\lambda_{eff}} (w - \Theta)}{\frac{m_e a}{\lambda_{eff}} (w - \Theta)} \right]^a \cos^a \pi_e \frac{I}{\lambda_{eff}} (w - \Theta) dw.$$

Putting:

でありにのできます。とないのでは、小なり

$$w = \frac{\epsilon}{2}u; \quad \theta = \frac{\epsilon}{2}\tau; \quad \frac{\epsilon}{l} = \alpha; \quad m = \frac{\alpha_l l \epsilon}{2 \lambda_{sl}},$$

38

0081

0082

,0080

.0076

.0069

,0061

-0,0052 -0,0046

,0030

.0039

10048

<sup>1</sup> CR 175, p. 1123 (1922).

BA 16, p 257 (1899)

one can write

$$I = 2 \int_{-1}^{+1} (1 - u^2)^{\frac{1}{4}} \left[ \frac{\sin m \, \alpha \, (u - \tau)}{m \, \alpha \, (u - \tau)} \right]^2 \cos^2 m \, (u - \tau) \, d\tau$$

Further we put

$$2m\tau = x$$

$$S(m) = \frac{4}{4\pi} \int_{0}^{1} (1 - u^{2})^{\frac{1}{2}} \cos 2mu \, du,$$

$$T(m) = \frac{4}{3\pi_{r}} \int_{0}^{1} (1 - u^{2})^{\frac{1}{2}} \cos 2m \, u \, du$$

Then one can easily derive.

$$\frac{4}{\pi_0} \int_0^1 u^2 (1 - u^2)^{\frac{1}{2}} \cos 2mu \, du = S(m) - 3 \Gamma(m),$$

$$\frac{4}{\pi_0} \int_0^1 u (1 - u^2)^{\frac{1}{2}} \sin 2mu \, du = 2mT(m)$$

The numerical values of S(m) and T(m) have been computed by Hamy as follows:

10	S(m)	$\Gamma$ (m)	nt	S (m)	$\Gamma(m)$
0,0	1,0000	0,2500	1,0	0,5767	0,1764
0,1	0,9950	0,2492	1,1	0,5054	0,1632
0,2	0,9801	0,2467	1,2	0,4335	0,1496
0,3	0,9557	0,2426	1,3	0,3622	0,1308
0,4	0,9221	0,2369	1,4	0,2927	0,1219
0,5	0,8801	0,2298	1,5	0,2261	0,1080
0,6	0,8305	0,2213	1,6	0,1633	0,0944
0.7	0,7742	0,2116	1,7	0,1054	0,0813
0,8	0,7124	0,2008	1,8	0,0530	0,0686
0,9	0.6461	0,1890	1,9	0,0067	0,0567
1,0	0,5767	0,1764	2,0	-0,0330	0,0455
			2,1	-0,0660	0.0352

Supposing  $\alpha$  to be small and including terms of the third order we can derive the following formula, taking  $2m\tau = x$ .

$$\frac{2}{\pi_{\delta}}I = 1 + S(m)\cos x - \frac{\alpha^{8}}{6} \left\{ \frac{x^{2}}{2} + \frac{m^{2}}{2} + \left[ \frac{S(m)}{2} x^{2} + 2m^{2}S(m) - 6m^{2}T(m) \right] \cos x - 4m^{2}T(m) x \sin x \right\}$$

S(m) is zero for  $m=m_1=1.916$  The intensity has maxima when  $v=2K\pi_0$  and minima when  $x=(2K+1)\pi_0$ , where K is an integral number. The fringes disappear when

 $m_1 = \frac{\pi_o l \varepsilon}{2 \lambda_{\text{eff}}} = 1,916,$ 

 $\varepsilon = 1.22 \frac{J_{\rm eff}}{I}$ 

This is the formula derived by Michelson

or

When a is small, but not zero, we get from the above formula

$$\frac{2}{\pi_0} \frac{\partial I}{\partial x} = -S(m) \sin x - \frac{\alpha^2}{6} \left[ x + [S(m) - 4m^2 T(m)] x \cos x - \left\{ \frac{S(m)}{2} x^2 + [S(m) - T(m)] 2m^2 \right\} \sin x \right]$$

It is known that if m is smaller than  $m_1$ , the equation  $\frac{\partial I}{\partial x} = 0$  has real roots near  $x = K m_0$ . Only the root x = 0 remains fixed when  $\alpha$  and m vary. In the neighbourhood of x = 0 we have

$$\frac{2}{\pi_{*}} \frac{\partial I}{\partial x} = -\pi \left\{ S(m) + \frac{\alpha^{*}}{6} \left[ 1 + (1 - 2m^{*}) S(m) - 2m^{*} T(m) \right] \right\} + \frac{\kappa^{*}}{6} \left\{ S(m) - \frac{\alpha^{*}}{3} \left[ (m^{*} - 3) S(m) + 5m^{*} T(m) \right] \right\} + x^{*} (...) + \text{higher terms.}$$

When m=0 the coefficient of x is negative. It remains negative as long as m is below the smallest positive value  $\mu$  that makes the coefficient disappear. The root x=0 then corresponds to a maximum of I

The coefficient of x cannot disappear more than for a value of m that makes S(m) of the same order of magnitude as  $x^n$ 

The equation

$$S(\mu) + \frac{\alpha^2}{6} [1 - 2m_1^2 T(m_1)] = 0$$

determines  $\mu$ . Developing  $S(\mu)$  in terms following powers of  $\mu = m_1$  and dropping  $(\mu = m_1)^n$ , which is of the order  $\alpha^4$ , one finds the equation:

$$\mu = \frac{\kappa_e I \epsilon}{2 \lambda_{eff}} = 1,916 + 0,236 \, \text{cm}^2$$

or:

$$a = \frac{\lambda_{eff}}{I} (1,22 + 0.15 \, a^2)$$

This formula is not strictly applicable when  $\alpha$  is not very small. When  $\alpha$  is a considerable fraction of the unit,  $\mu$  cannot be derived without a laborious numerical discussion.

HAMY has derived the values of  $\mu$  for the following cases:

In another paper! HAMY has made further studies of the problem. The study of variation in the intensity of the central maximum does not permit any conclusion concerning the value of the diameter of the light source.

The disappearance of the two minima encompassing the central maximum ought, on the other hand, to be able to give a value of s if the relation is known between s and i when such a disappearance occurs.

쁫• # 1,992 1,268 1,960 1,248 1,945 1.238 1,932 1,230 1,922 1,224 1,918 1,221 1,916 1,220

One can write the expression for the intensity:

$$I = \int_{-1}^{+1} (1-u^{2})^{\frac{1}{2}} \frac{2-\cos 2\pi (\alpha+1)(u-r)-\cos 2\pi (\alpha-1)(u-r)+2\cos 2\pi (u-r)-2\cos 2\pi \alpha (u-r)}{m^{2}\alpha^{2}(u-r)^{2}} du.$$

From this can be deduced:

$$\frac{I}{\tau} = 0 = \sum_{p=0}^{p=\infty} (-1)^p \frac{2 - (\alpha + 1)^{2p+4} - (\alpha - 1)^{2p+4} - 2\alpha^{2p+4}}{(2p+3)(2p+4)\alpha^2} m^{2p} \sum_{q=1}^{q=p+1} \frac{(2\tau)^{2q-2}}{I^{2}(2q)I^{2}(p+q+2)I^{2}(p-q+3)},$$

$$\frac{^{p}I}{\tau^{\frac{1}{4}}} = 0 = \sum_{p=0}^{p=\infty} (-1)^{p} \frac{2 - (\alpha + 1)^{2p+4} - (\alpha - 1)^{2p+4} - 2\alpha^{2p+4}}{(2p+3)(2p+4)\alpha^{\frac{1}{4}}} m^{2p} \sum_{q=1}^{q=p+1} \frac{(2\tau)^{2q-2}}{\Gamma(2q-1)\Gamma(p-q+2)\Gamma(p-q+3)}$$

<sup>1</sup> CR 176, p 1849 (1923).

The problem to be solved is to find the smallest positive value of m and the smallest value of  $\tau$  that simultaneously satisfy the equations. When  $\alpha$  is very small the following solution is found,

$$m = \mu_1 = 1,916 - 1,15\alpha^2,$$
  
 $2\tau = 2,914$ 

By taking "small" values of  $\alpha$ , for instance  $\alpha = \frac{1}{10}$ , and substituting neighbouring values, the unknowns are found by a process of interpolation

199. Danjon's Interferometer-Method 1. The apparatus used in applying this method is of the same type as the interferometer of Jamin, where the interference is caused by a system of thick glass plates. When observing through this instrument, the star to be measured is seen moving upon a field of bright and dark fringes. If the star has no sensible dimension it disappears completely when its light passes through the centile of the dark fringes. But if the stail has an appreciable disc, not all the points of this disc will disappear extinction will only be complete along a chord coinciding with the centre of the dark fringe On each side of this choid there are illuminated parts. When the star is circular and has its light uniformly distributed over the disc, the ratio y between the maximum and minimum brightness is defined by

> $\gamma = \frac{1 - J}{1 + I},$  $J = 1 - \frac{1}{2} \frac{n}{2^4} + \frac{1}{3} \frac{n^2}{(2\cdot 4)^2} - .$

where

and n is equal to  $\pi_{\theta}\varrho$ , where  $\varrho$  is the ratio between the angular diameter of the star and the distance between the fringes The determination of the apparent radius is thus dependent on actual photometric measurements of the quantity y No results of the experiments at Strassburg have been published as yet,

200. The Companion of Sirius (Sirius B). In his paper on the relation between the masses and luminosities of stars Eddington2 pointed out the possibility that Sirius B had a density of 53 000 that of the water, on account of the elections being in the capture sone of two or more nuclei simultaneously. The question whether such density really exists could be settled if the Einstein shift  $+0.62 \frac{\mathfrak{M}}{R}$  km/sec, amounting to 20 km/sec, could be measured. The possibility of testing the general theory of relativity as well as the theory of extremely dense matter was independently pointed out by Bottlinger and by Webi RJ

In 1925 W. S Adams4 communicated the results of measuring specirograms of Sirius B Direct measurements are difficult on account of the diffuse character of the lines, and the large registering photometer was accordingly used. Several observers have checked the measurements. The difference in velocity between Sirius A and Sirius B varies between 2 and 37 km for different special lines, but outstanding features of the results are the definite character of the positive displacement and its change with the amount of the wave length. The greater relative intensity of the spectrum of scattered light of Sirius A towards violet and the increasing influence of the superposition of the lines in its spectrum upon those of Sirius B will tend to reduce the amount of measured displacement. An approximate correction was derived from photometric measurements

Wash Nat Acad Proc 11, p 382 (1925)

CR 174, p 1408 (1922)
 M N 84, p 308 (1924)
 Berlin-Babelsberg Veroff 3, No 4 (1923), A N 220, p 189 (1924)

of the relative intensities of the continuous spectrum of Sirius A and Sirius AB The correction factor d is found from .

$$d = 1 + \frac{k_A}{k_B}$$

where  $k_A$  is the density of the spectrum of scattered light of Sirius A, and  $k_B$  that of the companion. By applying the correction factors the mean values were found

 $H_{\beta}$  . . . +26 km/sec +21 ... Additional lines . . +22 ...

The relative orbital velocity at the epoch is  $\pm 1.7 \, \mathrm{km/sec}$ . The remaining displacement of 24 km is interpreted as a relativity displacement. The following elements for Sirius B were derived by using Seares's values for surface brightness, on the alternatives of F0 or A5 for the spectral class.

	Yo	AJ
Surface brightness Radius	-0=,88 24000 km 30000 +0,23 A	( m,45 18 000 km 64 000 0,32 Å

The radial velocity of Sirius B also was determined at the Lick Observatory in 1928. J. H Moore<sup>1</sup> found the following values on the basis of 4 spectrograms;

| Number of lines | Relative density at \$17\$, composites, small cred light | 1928 Fobr. 13 +22 km/sec | 7 | 3,7 | 20 (+10) | 4 | 1,2 | 27 +29 | 6 | 10,0 (Underexposed) | March 20 +21 | 4,9 | 2,8 (Mean of two) | Mean 24 | |

The result of ADAMS in thus confirmed

Although the idea that Sirius B is an enormously dense body seems to be accepted generally, it seems fair to consider some other explanation. And others suggested that the light of the companion is reflected from a dark body. The fact that the spectrum is not identically the same as that of the primary does not make this theory impossible. Because of its general importance for stellar photometry we give a short review of Anding's paper.

A luminous surface element d/ with intensity I emits light at an angle of emanation s to an element df' at the distance r, and at an angle of incidence s'.

The light received by df' is:

$$dL = I d/\cos \frac{df \cos \theta}{dt}.$$

The element dj' not emitting light itself reflects the light dL' at an angle of emanation s' to another element dj'':

$$dL' = I d/\cos\epsilon \frac{1}{r^2} \frac{A}{\kappa_*} df' \cos\theta' \cos\theta' \frac{1}{r^2} df'' \cos\theta'',$$

where A is the albedo according to the definition of LAMBERT, A'' the angle of incidence of this element and A' its distance.

Applying this to Sirius we have the integral J (extended over an hemisphere):

$$J = \int I \, d/\cos \varepsilon,$$

<sup>1</sup> Publ ASP 40, p. 229 (1928).

AN 229, p. 69 (1926).

as the expression for the luminosity of the star. If  $D_s$  is the distance of Silius  $\Lambda$ from the Earth, the density of its light rays as observed by us is

$$H_{\scriptscriptstyle I\hspace{-.1em}I}=rac{J}{D_{\scriptscriptstyle I\hspace{-.1em}I}^{\scriptscriptstyle 2}}$$
 .

Further we introduce

$$df' = R_c^2 d\sigma'$$

where  $d\sigma'$  is the surface element of a sphere of unit radius and  $R_{\sigma}$  the radius of Sirius B. The angle between the radius vector Sirius-Companion and the radius vector Earth-Sirius is called  $\pi_o - \alpha$  Then we have

$$\int \cos i' \cos e' \, d\sigma' = \frac{2}{3} \left[ (\pi_0 - \alpha) \cos \alpha + \sin \alpha \right]$$

Further in the formula for dL' above r' stands for  $D_{\mathfrak{o}}$  (the distance of the companion from the Earth), and the value of the light  $H_c$  from the companion is.

$$H_o = J \frac{R_e^2}{r^2} A \frac{2}{3\pi_e} \{ (\pi_e - \alpha) \cos \alpha + \sin \alpha \} \cdot \frac{1}{D_e^2}.$$

The distance of Sirius A is equal to that of Sirius B, or  $D_0 = D_s$  We then get the expression for the ratio of the light of the two objects

$$\frac{H_o}{H_s} = A \frac{R_s^3}{r^2} \frac{2}{3\pi_o} \{ (\pi_o - \alpha) \cos \alpha + \sin \alpha \}$$

For simplifying purposes we assume A=1, r equal to the mean distance a between Sirius A and B, and  $\alpha = \frac{\pi_0}{2}$ 

Then

$$\frac{II_{\bullet}}{H_{\bullet}} = \frac{2}{3\pi_{\bullet}} \left(\frac{R_{\bullet}}{\Pi}\right)^{2}$$

or expressed in magnitudes

$$m_c = m_s + 1.7 - 5\log\frac{R_c}{a}$$

The value of a is 20 astronomical units and the mass of the companion equals the mass of the Sun If  $R_a$  is supposed to be equal to the Sun the following value is found

$$m_0 = 18^{\rm m} 15$$
.

Thus Sirius B should be ten magnitudes fainter than is the actual case. If  $R_{
m e}$ is computed from the value  $m_0 = 8.5$  it is found that  $R_0 = 100$  0 and the density would be 1/955000 of that of the Sun! The observations show the contrary to be the case, but it might be possible to explain the facts in favour of the reflection theory if the companion is surrounded by a swarm of dark bodies having the character of a dust-cloud

A detailed investigation does not make the existence of such a dust-cloud very probable Another hypothesis is that the companion of Sirius is a close binary system where one of the components is dark and has the same mass as the Sun. If the distance between the dark companion and Sirius B is equal to one planetary unit, the magnitude of the dark companion will be  $21^{\hat{m}},8$  on account of the light reflected from Sirius B, if the same distance is 0,1, the magnitude of the dark companion will be 16m,8.

In order to test the theory it will be necessary to observe the radial velocity of Sirius B at different epochs, because in the casm of an orbital motion the radial velocity of Sirius B will show corresponding variations

201. Diameters from Scintillation-Observations. G. Tichov<sup>1</sup> has used the colour changes caused by the scintillation of the stars for computing the apparent diameters. From 77 stars he finds the simple relation.

$$d = \frac{5.5036}{S} - 0.0607$$

where d is the diameter in seconds of arc, and S the number of changes in the colour in a second of time

The theory of scintillation shows that the blinking is related in a simple way to the apparent diameter of the stars Dufour has found that the red stars do not undergo such rapid changes as the white stars. Montigny has published a series of papers concerning the scintillation and he has given, in a catalogue, observations of the number of colour changes for 120 stars. I have used his data and tried to establish a relation analogous to that of Tichov, but so far without success. It seems that so many variables enter into the determination of the number of changes that the diameter is a very complicated function of S. Anyhow, it is clear that the diameters cannot be determined from the material of MONTIGNY with such an accuracy as when they are derived from observations of colour and magnitude The details of Tichov's investigation have not been accessible to me and it is possible that his data are more accurate than those of MONTIGNY.

202. The Fallacy in S. Poznowsky's Method. This method was based on the use of elliptically polarised light and was published at first in the year 1912. and later on in 1915. As plans have been made to apply the method in practice, EDDINGTON<sup>8</sup> took up the "ungrateful and ungracious" task of showing the breakdown of the method. The essential principle is the bringing into superposition of two widely separated beams that have been previously polarised in perpendicular planes. If the phase-difference is zero or  $\frac{1}{4}\lambda$ , plane polarized light is obtained, and circularly polarized light for phase differences of  $\frac{1}{4}\lambda$  or  $\frac{1}{4}\lambda$ . For intermediate values alliptically polarised light is obtained, which cannot be completely extinguished by a Nicol prism as is the case with plane polarised light. With point-source light the phase difference can be made zero and the image completely extinguished, but with a finite disc the difference will not be zero for all points of the disc simultaneously and the image will not wholly disappear. The angular diameter should result from the intensity of the residual image. The fallacy in the method arises according to Eddington from the fact that the intensity that is calculated by Pokrowsky is not that of the whole starimage, but the intensity at a cortain point in the focal plane. If the star is slowly displaced with regard to the instrumental axis, its image does not pop in and out, but bright and dark interference bands pass across the point considered.

The inadequacy of the treatment in the paper of Pokrowsky arises on account of the assumption that for a point-source plane waves emerge from the two apertures and travel in a particular direction. Owing to the diffraction, the waves travel in various directions inclined at angles that are not small compared to the angles, such as 0",003, occurring in the investigation.

Mittellungen Leshafts Inst Loningrad (Russian) 2, p 126 (1921).
 Recouli inaugural de l'Université de Lausanne (1892). La sointiliation des étolies.

Bull de l'Aced Roy Belg Ser. II, 25, p. 631 (1868); 29, p. 80 (1870), 29, p. 455 (1870); 37, p. 165 (1874); 38, p. 300 (1874) (Catalogue', 42, p. 255 (1876); 44, p. 694 (1877); 43, p. 391 (1878); 46, p. 17 (1878), 46, p. 328 (1878), 46, p. 598 (1878), 47, p. 755 (1879); 48, p. 22 (1879) Ser. III, 1, p. 231 (1881), 6, p. 426 (1883), 9, p. 85 (1885); 16, p. 160, 553 (1888); Ann de l'Obe Bruxelles 1878, p. 245.

<sup>&</sup>lt;sup>4</sup> Ap J 36, p. 156 (1912); AN 192, p. 21 (1912); BA 29, p 305 (1912), <sup>5</sup> Ap J 41, p 147 (1915).

<sup>8</sup> M N 87, p. 34 (1926).

#### e) The Densities of the Stars.

203. Densities of the Stars. Pioneer Work. The densities of the stars can, of course, be derived as soon as their masses and dimensions have been computed. A determination of the density itself is only possible in cases of visual binaria's

and eclipsing variables and involves a knowledge of the mass ratio

E C, Pickering and later on W H S Monck have separately derived at equation for binary stars with known orbital elements which renders it possible to determine the relation between brightness and mass of these stars quite independently of their distance. It is easy to show that the formula disch not distinguish between the extent of the surface and the temperature difference in mass-brightness may be due to variety in mean density (diameter) or to variety in surface brilliancy or temperature. The effects observed will be quite the same Pickering realized that if the temperatures were considered as not varying from star to star the mean densities of binary stars could be easily derived

In a paper of 1891 E. W MAUNDER<sup>8</sup> drew attention to several culturations that indicate that the spectral class marks a difference in constitution in this than a difference in the stage of development. In this paper the author computed the densities of 51 double stars assuming that the intrinsic brightness per unit of surface is the same for all the stars, which is far from truth. He found for the Sirian stars the mean density  $\bar{\rho}=0.0211$  O and for the solar stars  $\bar{\rho}=0.10260$ He also determined the ratio of the absolute brightness of the two groups of stars as 45,6/70,5, corresponding to a difference in absolute magnitude of  $10^{\rm M}$ , 15, whereas it should be  $-3^{M}$ ,3 The author also points out the possibility of using the double stars for studying the differences in absolute magnitude of different spectral groups

204. Densities of Visual Binary Stars The densities of visual binary stars have recently been computed by E OPIK1, who derived a relation giving the mean densities o, expressed in terms of the elements of the orbit and of the masses  $\mathfrak{M}_A$  and  $\mathfrak{M}_B$  (Solar mass is taken as unit ) If R is the radius of the primary star in linear measure and  $I_A$  the surface brightness of the primary expressed in that of the Sun as unit,  $v_A$  the apparent brightness, and  $\pi$  the parallely,

the relation '

$$\frac{r_A}{T_A} = R^2 \pi^2 \sin^2 4''$$

is immediately derived Further we have the well-known equation:

$$\mathfrak{M}_A + \mathfrak{M}_B = a^3 \pi^{-3} P^{-2}$$

Further

$$\mathfrak{M}_A = \varrho_A R^3$$
,  $\mathfrak{M}_A + \mathfrak{M}_B = \varrho_A R^3 \left( 1 + \frac{\mathfrak{M}_B}{\mathfrak{M}_A} \right)$ 

And

$$\log \varrho_A = \log \frac{a^3}{P^3} + \frac{3}{2} \left( \log I_A - \log \iota_A \right) - \log \left( 1 + \frac{\mathfrak{M}_B}{\mathfrak{M}_A} \right) - 3 \log 206265$$

Taking the stellar magnitude of the Sun to be -26m,60, we have:

$$m_A + 26,60 = -2,5 \log i_A$$

Expressing the surface brightness in stellar magnitudes and taking the Sun as unit: '  $I_A = -2.5 \log I_A$ 

Proc Amer Acad of Arts and Sciences 16, p 1 (1880)
Obs 10, p. 96 (1887) <sup>8</sup> JBAA 2, p 35 (1891); Astronomy and Astrophysics 11, p 145 (1892), <sup>4</sup> Ap J 44, p 293 (1916).

and after substitution, the following formulae

$$\log \varrho_A = \log \frac{a^3}{P^4} + 0.6(m_A - j_A) + 0.02 - \log \left(1 + \frac{\Omega l_A}{\Omega l_A}\right),$$
$$\log \varrho_B = \log \frac{a^4}{P^4} + 0.6(m_B - j_B) + 0.02 - \log \left(1 + \frac{\Omega l_A}{\Omega l_B}\right).$$

give the densities of the two components.

The surface temperature depends on the absolute temperature and thus, also, on the spectral type. This dependence can be derived from the colour index, but OPIK preferred to use the effective temperatures of 109 stars, as determined by Wilsing and Scheiner If  $\lambda_{\bullet}$  and  $\lambda_{O}$  denote the wave lengths of maximum spectral energy of the two sources, Planck's formula gives for the spectral region  $\lambda$ :

$$\frac{I_{\pm}}{I_{\odot}} = \frac{e^{\frac{4.965 \, Z_{\odot}}{L}} - 1}{e^{\frac{1}{L} - 1}}.$$

For visual light we have  $\lambda = 0.56 \,\mu$ ,  $\frac{4.965}{\lambda} = 8.87 = c$ , and the difference (in magnitudes) of the visual surface brightnesses of a star and the Sun becomes

$$j = 2.5 \log \frac{e^{2\lambda_0 - 1}}{e^{2\lambda_0 - 1}}$$

From Wien's formula,  $\lambda_{\bullet} T = 2940$ ,  $\lambda_{\bullet}$  can be computed if T is known

The effective temperatures determined by Wilsing and Schemer are probably systematically too low. The temperature of the Sun, 5130°, corresponds to a value, 1,16 cal/cm<sup>-8</sup> of the solar constant, which is much smaller than the value observed, 1,6—1,7 cal/cm<sup>-8</sup>. The value for  $T_{\odot}$ , 6250°, as derived by Abbot and Fowle, was therefore assumed as a zero-point, and the Potsdam temperatures were differentially corrected.

Ork finds from the table giving the means of T for various spectral subdivisions and the mean reduced wave length of the spectral energy-maximum that the temperature varies somewhat irregularly with spectral class. The fact that the spectral scale is qualitative makes it possible that the abrupt changes in T

between some stellar classes may be real

The mass-ratio must also be known for a computation of the densities. There are few cases where such a determination has been possible, and it is necessary to assume that the relation between  $M_B - M_A$  and  $\mathfrak{M}_B/\mathfrak{M}_A$  is known. Eleven cases were available, and from them the following table was derived.

The results as to the densities are not reviewed here because the following investigation by Bernewitz contained a more extensive material than that at disposal in 1916.

In 1921 E. Bernewitz<sup>1</sup> published an investigation concorning the densities of

Ma-Ma	THE BLA	Ma-Ma	TRA/NO.	
0 <sup>1</sup> ,0 0 ,8 1 ,0 2 ,0	1,00 1,00 0,95 0,88	3 <sup>M</sup> ,0 5 ,0 10 ,0	0,76 0,60 0,30	

binary stars. The formula giving  $\varrho_4$  was adopted in the form;

$$\log Q_A = \log \frac{g^2}{p^2} + 0.6(m_A - j_A) - \log \left(1 + \frac{\Omega Q_B}{\Omega Q_A}\right) + 0.089.$$

<sup>1</sup> AN 213, p 4 (1921).

The determination of the surface magnitude 1 is based on the equation of Planck

$$\frac{I_*}{I_{\bigcirc}} = \frac{\left(\frac{c_3}{e^{\overline{I}I_{\bigcirc}} - 1}\right)}{\left(\frac{c_3}{e^{\overline{I}I_{\bigcirc}} - 1}\right)} = 2.512^{-J_1}$$

The quantity  $\eta_{\mathcal{A}}$  has to be defined in the same way as the apparent magnitude m and thus account must be taken of the visibility curve  $g(\lambda)$  of the human eye. We can assume

$$-0.4\log\int_{0}^{\infty} \left[ \frac{c_{1}^{\gamma-5}}{c_{1}^{\gamma-5}} \right] g(\lambda) d\lambda = m$$

The function g(1) is taken in accordance with Henning's icsult1 as

$$g(\lambda) = \left[\frac{5520}{\lambda} e^{1-\frac{5520}{\lambda}}\right]^{140} + 0.1 \left[\frac{4600}{\lambda} e^{1-\frac{4600}{\lambda}}\right]^{1000} - 0.07 \left[\frac{6600}{\lambda} e^{1-\frac{6600}{\lambda}}\right]^{1000}$$

The values of the integral are computed by means of numerical integration. The following corrections have to be applied to the visual magnitudes

Spectral class	Correction	λυπ	Spectral class	Correction Am	Jett
A0	+0 <sup>14</sup> ,049	5420	Ko	-0 <sup>m</sup> ,035	5580
G0	0,000	5490	K5	-0 ,041	5630
G5	-0,022	5540	Mc	-0 ,039	5680

The effective temperatures were used as determined by Wilsing The following values of j were found

Spectral class (ADAMS)	$\frac{c_1}{T}$	1	Spectral class (ADAMS)	$\frac{c_s}{T}$	1
B0 B5 B8 A0 A2 A5 A8 F0 F3 F5 F8	1,45 1,45 1,48 1,53 1,62 1,72 1,87 1,99 2,16 2,29 2,50	- 1 <sup>th</sup> ,93 -1,93 -1,87 -1,76 -1,58 -1,37 -1,07 -0,83 -0,49 -0,24 +0,18	G0 G3 G5 G8 K0 K3 K5 K8 Ma Mb	2,64 2,85 3,00 3,28 3,52 3,92 4,18 4,48 4,62 4,76 4,87	+0 <sup>m</sup> ,45 +0 ,86 +1 ,15 +1 ,70 +2 ,16 +2 ,94 +3 ,45 +4 ,03 +4 ,51 +4 ,78

For the determination of the mass-ratio 10 pairs were used and the following relation resulted:

d m	90? B 90%.4	A m	902 <u>n</u> 902 t	र्थ ११६	$\frac{\mathfrak{M}_A}{\mathfrak{M}_B}$
0 <sup>™</sup> ,0	1,00	2 <sup>™</sup> ,0	0,81	4 <sup>™</sup> ,0	0,68
1 ,0	0,90	3 ,0	0,74	5,0	0,62

For 31 out of 63 pairs, only the mean density of both components could be computed. An attempt was made to find a relation between absolute magnitude and density. The results are given in the following table.

Jahrb d Radioakt u Elektronik 1919, H 1.

The data under the heading II refer to the remaining material when 5 spectroscopic pairs and α Centauri were excluded By forming the part I of the table o• Eridani, Sirius B and s Hydrae were excluded We see from the table

<u>II</u>	I		п		Limits of
	-0	7	<u> </u>		spectral class
OM,8 1 ,5 2 ,6 3 ,5 4 ,6 5 ,6 6 ,2 7 ,9 10 ,8	0,08 @ 0,20 0,26 0,24 0,58 0,43 0,45 0,47 2,81	4 6 10 9 12 12 9 5 2	0,08 @ 0,14 0,23 0,24 0,45 0,40 0,50 0,47 2,81	4 9 9 11 11 8 5	A0-F3 A0-F2 (F1) A0 (A2)-G0 A2-K2 F1 (I4)-G5 F5-K0 F2-K5 K2-K5 Mb

that there is a steady increase in the mean density from 0,080 to about 0,50 Between 5" and 10"  $\bar{\rho}$  is sensibly constant, but seems to increase for  $M > 10^{\rm M}$ ,0 There also seems to be a certain increase in  $\bar{\varrho}$  with spectral class from A2 to Mb, but the evidence

is rather uncertain

4 ,0-4 ,9

A. R. Thompson 1 has recently derived the formulae for computing the density of binary stars, evidently without any knowledge of carlist work. In several cases the agreement with earlier results is not very good. The principal cause of such deviations is to be sought in different assumptions concerning the temperature. The uncertainties arising from uncertain mass-ratios and uncertain orbital elements are not of nearly such importance as those arising from differences in the scale of effective temperatures

I have derived the absolute magnitudes of most of the objects in Thompson's list and have found the following dependence between M and  $\bar{\varrho}$ :

ø Brighest-0™,0 0,33 @ 64,0- 74,9 2,43 O 16 0<sup>™</sup>,0—0 ,9 8 ,0-10 ,9 3 0,14 3,50 Krā 60 A 0,36 16 1,0-1,9 2 ,0-2 ,9 17 0,94 3 ,0-3 ,9 17 Kra. 60 B 0.54 o³ Erid. B 15

There seems to be a general relation between the absolute magnitude and the density, but the dispersion is considerable. In spite of all the uncertainty that is undoubtedly connected with the derivation of  $\bar{\rho}$ , it is difficult to avoid the impression obtained from a close scrutiny of the inaterial that the actual relation between M and g is not a one to one correspondence. This question has undoubtedly some bearing on the question of the character of the mass-luminosity law.

Sidus B

205. The Ratio of Densities in Double Stars. From the formula quoted earlier it follows immediately that

$$\log \varrho_A - \log \varrho_B = 0.6 (m_A - m_B) - 0.6 (j_A - j_B) + \log \frac{m_A}{m_B}$$

If both the spectra are known and the mass-ratio can be approximated, the ratio of the densities can thus be computed without any knowledge of the elements of the orbit. The mass-ratio can be computed from the formula:  $\frac{m_s}{m_A} = -0.61 + 0.36 (M_B - M_A)$  derived from a least square solution using existing material.

If both spectra have been observed the above formula will give us the change in logarithm of density  $\Delta \log \varrho$  for different groups. We can also form the

<sup>1</sup> JBAA39, p. 247, 253 (1929).

mean values of  $d \log \varrho / dS$ , where dS gives the change in spectral index. Putting

$$\frac{\Delta \log \varrho}{\Delta S} = \varphi(S)$$

it will be possible, by applying a process of graphical integration, to find the curve

$$\log \varrho = \psi(S)$$

which gives the relation between density and spectral class. An attempt has been made to derive this curve but it seems that the present material is rather scanty and that we should wait for a more extensive material. A practical difficulty arises on account of the selection in the material which favours small  $\Delta S$  (equal spectra). This part of the material can be used for a derivation of the dispersion in  $\log \varrho$  for the different spectral classes. The following small table gives the results hitherto obtained

Spectral class	∆ log q	σdloge	Mean spectral index (B=1,0, M=5,0) and its dispersion	п
B	0,68	士0,50	0,4 ± 0,3	19
A	0,47	士0,38	1,4 ± 0,3	11
F	0,23	士0,35	2,5 ± 0,2	11
G	-0,07	士0,41	3,3 ± 0,2	7
K	+0 13	士0,41	4,7 ± 0,4	5

206 Densities of Echpsing Binaries. Methodical. The possibility of deriving the mean density of an echpsing binary system was first pointed out by Meriau<sup>1</sup> in 1896. We have

$$P^{2} = \frac{k a^{3}}{\mathfrak{M}_{A} + \mathfrak{M}_{B}} = \frac{3 k a^{3}}{4 \pi_{c} (r_{A}^{3} \varrho_{A} + r_{B}^{3} \varrho_{B})}$$

where k is a constant, P the period, a the semi-axis major of the orbit,  $\varrho_A$  and  $\varrho_B$  the densities of the two components,  $r_A$  and  $r_B$  then radii Putting  $r_A = a n_A$ ,  $r_B = a n_B$ , and  $3 k / n_o = k_1$ , we have

$$P^{0} = \frac{h_{1}}{4 (n_{A}^{3} \varrho_{A} + n_{B}^{3} \varrho_{B})},$$

$$\bar{\varrho} = \frac{n_{A}^{3} \varrho_{A} + n_{B}^{3} \varrho_{B}}{n_{A}^{3} + n_{B}^{3}},$$

when  $\bar{\varrho}$  is the mean density of the two components

In the case of a circular orbit the duration of the eclipse is  $2\pi_0 t/P$  where t is the duration of the light variation. Further let i be the inclination of the orbital plane. Then

$$n_A + n_B = \left(1 - \cos^2 \frac{\pi_a t}{P} \cos^2 t\right)^{\frac{1}{2}}$$

and thus

$$\bar{\varrho} = \frac{(n_A + n_B)^3}{4 (n_A^3 + n_B^3)} \frac{k_1}{P^2 \left(1 - \cos^2 \frac{\pi_e \, b}{P} \cos^2 z\right)^{\frac{3}{2}}}.$$

The term  $(n_A + n_B)^8$  is  $\leq 4(n_A^3 + n_B^3)$ . If  $r_A = r_B$ , the limiting value of the first factor of the expression for  $\bar{\varrho}$  is 1, and if  $r_B = 0$  (no eclipse then takes place), the same factor has the value  $\frac{1}{4}$   $n_A$ ,  $n_B$ , P, t, and t can be derived from the light-curve and the value of  $k_1$  is taken from solar data:

Thus  $\bar{\varrho}$  can be computed

$$k_1 = 5,56 \sin^3 46' 2''$$

<sup>1</sup> C R 122, p 1254 (1896).

In the case of an elliptical orbit the formulae become very complicated.

A. W ROBERTS discussed in 1899 the densities of four Algol stars and derived the following expressions for the densities

$$\begin{split} \varrho_A & \coloneqq \frac{(0,0092)^n}{p^n} \left( \frac{\mathfrak{M}_A}{\mathfrak{M}_A + \mathfrak{M}_n} \right), \\ \varrho_B & \coloneqq \frac{(0,0092)^n}{q^n P^n} \left( \frac{\mathfrak{M}_B}{\mathfrak{M}_A + \mathfrak{M}_n} \right), \end{split}$$

where P is the period (in years), p and q the diameters of the components, expressed in terms of the semi-axis major of the system,

As the two mass terms must always be less than unity or rather as only one of them can ever approach unity, a limit is given in one direction by the expressions

 $\lim \varrho_A = \frac{(0,0092)^4}{\hat{\rho}^2 P^2}, \quad \lim \varrho_B = \frac{(0,0092)^4}{q^4 P^2}.$ 

The following results were obtained:

	llm ∉₄	lbn ea
X Carinao , , ,	0,25	0,25
S Volorum , ,	0,61	0,03
RR Centauri , , ,	0,27	0,27
RS Segittarii	0.16	0.21

At the same time H. N. Russell's made a derivation of a limiting value for the mean density of 17 variable stars of the Algel type and found.

$$\bar{\varrho}_{AB} \approx \frac{\mathfrak{M}_A + \mathfrak{M}_B}{4\pi_* (r_A^2 + r_B^2)}$$

Now

$$r_A^2 + r_B^2 \ge \frac{1}{4} (r_A + r_B)^2,$$

the sign of equality only holding good when  $r_A = r_B$ 

At the first and fourth contacts we have the projection of the distance between the centres of the two stars upon a plane perpendicular to the line of sight  $= r_A + r_B$ . The arc described during the time from the beginning to the middle of the eclipse is  $n_i t/P$ , where t is the duration of the light variation, and the projected displacement is  $a \sin n_i t/P$ , where a is the radius of the orbit. Then we have the condition:

$$r_A + r_B \gtrsim a \sin \frac{\pi_a t}{D}$$
.

The sign of equality only holds good when the transit is central. Besides there is the relation

 $\mathfrak{M}_A+\mathfrak{M}_B=h\frac{\pi^*}{128}$ 

and thus:

$$\tilde{\varrho}_{AB} \leq \frac{3h}{\pi_{e}P^{4}\sin^{6}\frac{\pi_{e}I}{P}}.$$

Taking the Earth density as 5,53 Russell found  $3k/n_0 = 44.1$  (the unit of the time being  $1^n$  and the unit of density that of water), and derived the densities for 17 stars.

207. Shapley's Work. In 1915 H Shapley published his extensive research concerning the orbital elements of 90 eclipsing binaries based on nearly 10000 magnitudes obtained with the polarizing photometer of the observatory at

<sup>&</sup>lt;sup>1</sup> Ap J 10, p. 308 (1899)

PRINCETON¹ The memon discusses the theory of the orbital determination, and then all existing observational data were used for deriving the elements. The total number of observations used is 27094. A general experience in the discussion of this extensive material is that the light curves of eclipsing binaries are, in general, symmetrical, smooth, and regular. The niegularities and anomalies that are often reported in the older literature do not gain any support from accurate photometric work. The investigations of Shapley also disposed of the supposition so prominent in earlier days that one component of the ordinary Algol star is non-luminous. The disparity in brightness of the eclipsing binaries is even smaller than in the case of visual binaries. In all cases except for five or six eclipsing binaries there is positive evidence that the fainter star is itself luminous.

The existence of a darkening toward the limb of the same order of magnitude as in the Sun seems to be well established. It was also found that there is general agreement between the actual gravitational elongation of eclipsing binary stars and the theoretical ellipticity of homogeneous fluid bodies according to G. II. Darwin's investigations

By assuming that the components of each binary are equal to the Sun in mass the "equal mass densities" were computed according to the formulas

$$\varrho_A = (5.29 P^{\frac{9}{8}} r_A)^{-8}, \quad \varrho_B = (5.29 P^{\frac{9}{8}} r_B)^{-8},$$

where P is the period in days,  $r_A$  and  $r_B$  the radii, the radius of the relative orbit being taken as unit, and  $\varrho_A$  and  $\varrho_B$  the densities. These were corrected for polar flattening and for the mass-ratio. The mean density is independent of the total mass of the system relative to the Sun, but a knowledge of the mass-ratio is essential for a derivation of the mean densities of the components. At that time the spectroscopic data for eclipsing binaries were very scanty

The corrected densities for "darkened" solutions were compared with the spectral classes and the following distribution, which is still of interest, was found:

Spectral class	В	A	F	G	K	Spectral class	13	٨	ŀ	G	к
+0.5 to 0.0 0.00.5 -0.51.0 -1.01.5 -1.52.0	8 5 3	11 24 13 6	7 3	1 1		-2,0 to -3,0 -3,0 ,, -4,0 -4,0 ,, -5,0 -5,0 ,, -6,0	1 1		1	2	1

208. Parallaxes and Absolute Magnitudes of Eclipsing Binaries. The parallaxes of eclipsing binaries have been derived by H N Russell and H Shapley on basis of the following considerations. If the radius and the surface brightness of a certain star are R and J, expressed in units of the solar radius and surface brightness, respectively, we have

$$M = 4.75 - 5 \log R - 2.5 \log J$$

The elements of the eclipsing systems give us the value of r, that is the radius of the brighter component expressed in units of the mean distance a of the components. The mass is assumed to be  $2\mathfrak{M}$  times the Sun's mass. Taking the radius of the Sun as unit and expressing the period, P, in days the mean distance will be

$$a = 5.29 P^{1} \mathfrak{M}^{1}$$

<sup>&</sup>lt;sup>1</sup> Princeton Obs Contr, No 3 (1915)

Hence

$$R = ar = 5.297P^{1}M^{1}$$
.

Setting for brevity  $5,297P^{\dagger} = A$ 

we find.

$$M = 4,75 - 5 \log A - 4 \log \mathfrak{M} - 4 \log J$$

A may be derived from the known elements of the eclipsing system. The parallax  $\pi$  is then found from the formula:

$$M = m + 5 + 5 \log \pi$$

For computing M and  $\pi$  two assumptions have thus to be made, viz. the value of M and of J When the spectral class is known, both the quantities can be fairly approximated and thus also a tolerable value of M or  $\pi$  computed. In this way the parallaxes of some 400 eclipsing binaries have been computed. In the cases where the masses are known the individual densities of eclipsing binaries can be derived with a considerable degree of accuracy.

209. Recent Statistics of the Eclipsing Binaries. These stars give valuable contributions to our knowledge of several of the physical properties of the stars. Also in those cases where no orbits have been calculated but the celipsing nature of the pair is known, the maximum possible mean density can be derived.

DEAN McLaughlin has discussed the data of eclipsing binaries Altogether photometric orbits have been derived for 116 stars. The densities of the brighter components of each binary are tabulated against spectra as follows.

		L	AS-PS	148 G5	X-M	Bons
<0,001 0,001-0,01 0,01 -0,05 0,05 -0,10	2 6 4	1 2 7	1 1	2 2 1		6 15 20
0,10 -0,30 0,30 -0,70 0,70 -1,0 >1,0	3	31 16 2	4 7 1	1	4	38 24 3 4

Relation between spectrum and density.

Mean values of the radii  $r_A$  were derived for certain period intervals as is shown in the next table.

- Perioda	Mosn period	Monn period Radius of carbit in ken.		Radius of beighter star		
- Persona	(A) CHART IN WALL		in parts of a	la lon		
< 14,0	04,6	4,2-10	0,37	1,6 - 10	16	
$1^4.0 - 2.2$	1,6	8,0	0,30	2,4	24	
2,2-3,2	2.7	11,4	0,23	2,6	21	
3 ,2 - 4 ,25	3 .7	14,0	0,21	3,0	17	
4,25 - 5,3	4 .7	16,4	0,19	3,2	13	
5,3 — 7,0	6,0	19,3	0,19	3.5	9	
7,0 - 10,0	8 ,5	24.3	0,10	2,4	4	
10 -100	25	50	0,14	7,1	9	

The radii of the orbits have been calculated from the formula  $80 = \frac{4}{10^{10}} \cdot \frac{a^2}{P^2}$ . The average mass of eclipsing binaries is, in fact lower than that value but

RUSSELL and SHAFLEY, Ap J 40, p. 417 (1914) and subsequent papers by numerous workers within this field.

A J 38, p. #5 (1927).

even if we take the value of  $\mathfrak{M}_A + \mathfrak{M}_B$  equal to 4,50 as suggested from spectro scopic eclipsing binaries, the computed radii will be diminished by only 16 percent

The radii of the stars are more nearly constant than the radii of their orbits. The stars of the period group <1d,0 days are probably smaller than has been

calculated, since they are dwarfs which are less massive than has been assumed

It seems likely that the discovery-chance has resulted in an unduly large radius for stars of periods 1d,0—10d,0 since the greater radii will mean longe duration of eclipse. Then it is quite possible that the average radius will be nearly constant.

## f) The Masses of the Stars.

210. Methods of Deriving Stellar Masses. The laws of gravitation furnish a method of deriving the masses of heavenly bodies. As soon as a gravitational effect exercised by one body on another can be measured the mass is easily determined. Inasmuch as the motions of the stars are not known to such at extent and accuracy that we can determine any curvature of the orbits it is not possible to derive any masses. The only cases for which it has been possible to determine individual masses is when the absolute orbit of a visual double start has been derived with accuracy or when the Doppler displacements in both spectra of an eclipsing binary star have been measured. When both spectra is an ordinary spectroscopic binary are exhibited and their displacements measured the mass-ratio can be accurately determined. When the relative orbit of on component of a visual binary is known the sum of the masses of the component can be determined. In the case of spectroscopic binaries showing one spectrum a rather complicated function of the mass can be derived, which treated statistically can yield results of value concerning the mean mass of groups of stars.

For groups of visual binaries for which the orbital motion has been observed but the orbital elements are unknown, the mean value of the masses can be derived

if the distances are accurately known.

Finally there seems to be some gravitational effect in the upper layers of the atmosphere of the stars affecting the intensity of certain lines in spectra. The problem cannot be said to be solved as yet, but some mass-effect seem to be present in the spectrographic parallaxes, which fact will probably lead methods of determining the stellar mass from certain spectral characteristic

In the case of clusters or agglomerations of stars of cluster structure it possible to determine the mass-ratios of such groups of members as have a different spatial distribution and hence a different distribution when projected a photographic plate. The differences in the space densities are effects of the gravitation (e. g. heavy bodies will be more concentrated towards the centre the agglomeration than less massive ones) and when the distribution in span of the separate groups is known the mass-ratios can be derived. This, of cours involves accurate determinations of the distance of the agglomeration.

The cases mentioned are the only ones where a direct determination of the masses or the mean masses of groups can be performed. In order to extend or knowledge to ordinary stars we have to search for simple relations between the

masses and other characteristics of the stars.

Such a relation is known to exist between mass and spectral class; there also a relation between mass and luminosity, which was first found empiricall but later on derived from the theory of radiative equilibrium. The establishment of the mass-luminosity relation is of fundamental importance and too many effor can scarcely be made with regard to the accurate derivation of this relation fro empirical data and theoretical deductions. It is possible that the mass-luminosi

relation only represents a first approximation and that the actual relation should include a second variable, the effective temperature,

The mass can also be related to the reduced proper motion, which is sometimes of advantage. There probably exists a relation between the density and the mass, but it cannot at present be established with any accuracy. There seems to be a relation between the mean mass of a group of stars and the mean squared space- (or radial) velocities of the same group (equipartition of energy).

The sum of the masses of the two components in a binary system is found

applying the third law of KEPLER ("the harmonic law"). We have:

$$\mathfrak{M}_A+\mathfrak{M}_B=\frac{\sigma^4}{\pi^4P^4},$$

if we select as units the year and the solar mass. The major axis a is taken in seconds of arc as well as the parallex a.

In the case of spectroscopic binaries this equation can be written:

$$\mathfrak{M}_A + \mathfrak{M}_B = \frac{4\pi !}{h!} \frac{(a_A + a_B)^2}{P^4}$$

(A is the Gaussian constant,  $\log k = 8,23558 - 10$ ) or:

$$\mathfrak{M}_A + \mathfrak{M}_B = k' \frac{a^3}{i^3}$$

where P is the period expressed in days, a the major axis expressed in km, and b' a numerical constant. We do not know a or  $a_A + a_B$  but only its projection a sins and thence we have in multiply both members with  $\sin^2 t$  where t is the inclination of the orbit.

Thus: 
$$(\mathfrak{M}_A + \mathfrak{M}_B) \sin^2 i = k' (a_A \sin i + a_B \sin i)^2 P^{-2}.$$

From the theory of the determination of orbits of spectroscopic binaries we have:

$$a_A \sin i + a_B \sin i = K'(K_A + K_B) P \sqrt{1 - c^2}$$

where  $K_A$  and  $K_B$  are the semi-amplitudes of the radial velocities of the two components, expressed in km/sec, and h'' is a constant, hence.

$$(\mathfrak{M}_A + \mathfrak{M}_B) \sin^2 i = k_1 (K_A + K_B)^2 P (1 - e^2)^{\frac{1}{2}}.$$

The numerical value of log &, is 3,01642 - 10.

If both spectra have been measured we have:

$$\mathfrak{M}_{A} \sin^{3} i = h_{1} (K_{A} + K_{B})^{3} K_{B} P (1 - e^{2})^{\frac{1}{3}},$$
  
$$\mathfrak{M}_{B} \sin^{3} i = h_{1} (K_{A} + K_{B})^{3} K_{A} P (1 - e^{2})^{\frac{1}{3}}$$

In fact.

$$\frac{\mathfrak{M}_A}{\mathfrak{M}_A} = \frac{K_A}{R_A}.$$

When only one spectrum (of component A) is visible another formula has to be used:

$$\frac{\mathfrak{M}_{\mathcal{A}}^{n} \sin^{n} f}{(\mathfrak{M}_{\mathcal{A}} + \mathfrak{M}_{\mathcal{A}})^{n}} = h_{1} K_{\mathcal{A}}^{n} P (1 - e)^{\frac{1}{2}}.$$

At any rate it is necessary to assume a mean value for sin\*4. We have.

$$\overline{\sin^2 i} = \int_{\frac{\pi d^2}{\sin^4 i} di}^{\frac{\pi d^2}{\sin^4 i} di} = \frac{3}{16} \pi_0 = 0.59.$$

Because of the preference for high values of  $\iota$ , it is better to adopt a somewhat higher value for  $\sin^{8}\iota$  than 0,59, for instance 0,66 Sometimes even as high a

value as 0,93 has been adopted1,

We have seen above how the mass-ratio can be determined in case of spectroscopic binaries. If such a system also is observed as an eclipsing binary the value of i can be found when deriving the orbit and thus the masses of the pair can also be computed. In case of visual binaries the mass-ratio can be determined in the following way.

Let A and B denote the two components of a binary and C be a star that does not take part in the motion of the system AB, or in other words does not

belong to the system

Let

 $\varrho_{AC}$  = the angular distance between A and C

 $\partial_{CA}$  = position angle of C with respect to A

 $v_A, v_A$  = the rectangular coordinates of A with C as origin, the v-axis being directed toward the North Pole

 $x_0, y_0$  = the rectangular coordinates of the centre of gravity O of the system AB with C as origin

 $\xi_0$ ,  $\eta_0$  = the coordinates of O with A as origin

 $\varrho_{AB}$  = the distance between A and B

 $\partial_{BA}^{m}$  = the position angle of B with respect to A.

 $k = \frac{\mathfrak{M}_A}{\mathfrak{M}_A + \mathfrak{M}_B}$ 

The coordinates of the centre of gravity of AB are

$$x_0 = x_A + \xi_0,$$
  
$$y_0 = y_A + \eta_0,$$

which may be written in the form

$$\begin{aligned} x_0 &= +k \, \varrho_{AB} \cos \theta_{BA} - \varrho_{AO} \cos \theta_{OA} \,, \\ y_0 &= +k \, \varrho_{AB} \sin \theta_{BA} - \varrho_{AO} \sin \theta_{OA} \,. \end{aligned}$$

The motion of the centre of gravity O with respect to C is rectilinear and thus we can write

$$x_0 = a + b (t - t_0),$$
  
 $y_0 = a' + b' (t - t_0),$ 

where a, a', b, and b' are constants, t a certain epoch of observation, and  $t_0$  an initial epoch

Thus 
$$a + b (t - t_0) - k \varrho_{AB} \cos \theta_{BA} = -\varrho_{AO} \cos \theta_{OA}$$
,  $a' + b' (t - t_0) - k \varrho_{AB} \sin \theta_{B1} = -\varrho_{AO} \sin \theta_{OA}$ .

The problem is, in fact, nearly identical with the problem of determining the trigonometric parallax of a star, only that the period is much longer than a year, and the same methods can be applied with advantage in practice. It seems that observers have not always appreciated the great advantage of connecting visual doubles with a sufficient number of stars being independent of the system. The student is adviced to consult the two observing lists for the determinations of mass-ratios as given by Attken [Lick Bull 7, p 3 (1912)] and by VAN BIESBROECK [A J 29, p 173 (1916)]

211 Are Derived Mass-Values Representative? It will certainly be asked whether we have any right to extend our knowledge concerning the masses of the densities of the double stars to ordinary stars. The following facts may be

<sup>&</sup>lt;sup>1</sup> Kreiken, MN 89, p 589 (1929)

mentioned which show that the double stars do not form an exceptional group

among the stars of the stellar system

The distribution of double stars on the sky is the same as the distribution of ordinary stars. Our knowledge concerning the special distribution of the former is scanty, but the evidence so far shows the general agreement in the distribution in space of the two groups (LEWIS1, KREIKENS).

The motions of the double stars do not differ from the motions of the single stars in any known respect. The present writer has investigated the proper motions and radial velocities of some 150 binaries without finding any pecu-

liar behaviour, C LUPLAU-TANBSEN® has determined the apex of double stars and found the values  $A = 265^{\circ}$ .  $D = +26^{\circ}$ , V = 17.1 km/secJ. OORT has found the adjoined mean residual radial velocities of binary stars.

Man toutding Actourt &.									
Spertral class	Apactementic Magries	л	Single state (Campurily)						
B0—B9 A0—A9 F0—F9 G0—K9	6,6 km/sec 12,0 12,4 16,0	43 30 20 18	6,5 km/soo 11,0 14,1 13,6	225 177 184 492					

Many rouldwal walcolly 5

He derives the ratio  $V_{\text{single stars}}/V_{\text{binaries}} = 1.03 \pm 0.05$  and concludes that the average mass of the brighter component of a visual binary is about equal to

that of a single star of the same spectrum and absolute brightness.

The double stars exhibit typical stollar spectra (Miss Cannon\*, LRONARD\*, and others). No such spectral peculiarities are found among double stars as to place them among the special groups of stars. The RUSSELL diagram of the binary stars as first constructed by F. C. LEGNARD, has the same form as that of single stars. Applying a different method the present writer and W. J LUYTEN later on derived a typical RUSSELL diagram on the basis of some 300 double stars

As far as all the evidence goes it is only the fact that two or more bodies are moving within the activity-spheres of each other's gravitation that places the double or multiple stars in a certain class. With regard to motion, space distribution, physical properties, absolute magnitudes, temperatures, donsities, general chemical and physical constitution the double stars are typical citizens of the stoller realm.

Thus it seems justifiable to conclude that the masses or densities of binaries should not differ systematically from the masses or densities of the ordinary stars.

212. Historical Notes. Observational Evidences. The first star for which it was possible to obtain accurate knowledge of its dimonsions, mass, and density was our Sun. When the first trigonometric parallaxes of stars had been secured, and orbital elements of double stars had been computed, the third law of KEPLER ("the harmonic law") was applied and it was evident that the masses of neighbouring stars did not differ systematically from that of the Sun Already in Madras about 1850 Jacon found the mass of the a Centauri system. to be 10 and interpreted this result as showing that the mass of the system is of the same order of magnitude as the mass of the San. On account of the slow progress of the determinations of stellar parallax our knowledge of the masses of the stars also advanced slowly. A table in Agnes M Clerke's well-known work "The System of the Stars" (1905) is, I think, representative of the knowledge possessed of the stellar masses at that time. The sums of the masses - mom R A S 56 (1906).

A N 203, p 9 (1916); Ksbenhavn K Acad Forhandl Oversigt 1916, No. 1.

A J 35, p. 141 (1924)

B Lick Bull 6, p. 125 (1911).

Harv Ann 56, No. 7 (1912).

A J 35, p. 93 (1923).

AJ 35, p. 93 (1923).

MN 10, p 170 (1850).

in twelve binary systems are given in that table. The values range between 0,670 and 12.66 O. It is of a certain interest that Capella is included with a minimum value of 2.140 derived on the strength of the observations at Greenwich in 1905, when the separation was estimated as 0".05 These observations could not be confirmed at Lick and the Greenwich results were not generally accepted. A comparison by J. HAAS1 of the positions derived on basis of the orbital elements from the Mount Wilson interferometer measurements with the Greenwich estimates in 1905 has made it very probable that Capella actually was seen as oblong by the Greenwich observers—a very remarkable observation!

The astronomers of the 19th century certainly took a keen interest in the development of methods to determine physical characteristics of the stars. In 1844 Bessel noticed that the proper motions of Sirius and of Procvon were variable This led him to investigate in a masterly written paper the possible causes of changes in proper motions of the stars. He found it most probable that the changes in Sitius and in Procyon were caused by the gravitation of a possible dark companion to the brilliant star It is well known how after many disappointments on account of presumed, but not confirmed, discoveries this theoretical investigation finally led to ALVAN CLARK's discovery of the companion of Silius in 1862. It is also well known how the investigations of Bessli and the later work of Auwers3 led to the discovery by I M Schaeberle of the companion of Procyon in 1896 The point that concerns us here is that these investigations have developed the methods of determining the mass-ratio in double stars in such a definite way that at present we have no leason to change of modify the classical formulae.

This method depends on accurate determinations of periodic changes of small amplitude in the proper motions. It is very difficult to obtain reliable results. When T Lewis published in 1906 his large catalogue of the  $\Sigma$  double stars, he collected the results then existing concerning the value of  $\mathfrak{M}_{4}/\mathfrak{M}_{H}$ On the basis of the material he arrived at the wrong conclusion that the fainter component in a binary system is generally the more massive one. The evidence accumulated later shows that this conclusion is not tenable. The mass-ratios known hitherto are still affected by considerable uncertainty in the case of visual binaries but their general accuracy has much increased since 1905. We also have nowadays the possibility of deriving accurate mass-ratios from spectroscopic binaries giving impressions of both spectra on photographic plates

Of the different computations of the mean masses of the binary stars we mention here only a few In 1910 R G AITKEN® used the material in the parallax catalogue of KAPTEYN and WEERSMA? and found the masses to vary between 0,002@ and 3710, most of the variation being attributable to the uncertainty of the parallax measurements. It could be assumed that the real variation in the size of stellar masses is very small

In the following table the results of some computations of the total mass of stellar systems, generally not specially mentioned or reviewed in the text, are collected. No completeness is aimed at The sole purpose is to illustrate the general development during the last decades of our knowledge of stellar masses

<sup>&</sup>lt;sup>1</sup> Obs 47, p 376 (1924). <sup>2</sup> AN 22, p 145 (1844), Abhandlungen von Friedrich Wilhelm Bessel, herausg von R Engelmann II, p 306 (1875)

<sup>3</sup> AN 58, p 33 (1862) Mem R A S 56 (1906) <sup>5</sup> Lewis did not care to derive  $\mathfrak{M}_A+\mathfrak{M}_B$  from his material, but pointed out the possi bility of doing so [Mem R A S 56, p. XXI (1906)]

\*\*Total Astron. 18 to 483 (1910). 

\*\*Groningen Publ. No 24 (1910).

Anthority	Mean value	Range	4	Rpoch	Source
AUWERS	1,6⊙	1,04 - 2,200	2	1892	AN 129, p 232.
Young .	1,6	0,33 - 3,1	4	1899	General Astronomy.
GORB	5	1,9 -15	5	1907	AstronomicalEssays
DOBBRCE	11/3		few causes	1908	A N 178, p. 381
NEWCOMB-ENGELMANN	1,4	0,1 3,5	7	1911	Populare Astrono- mie, IV. Aufi
	1,4	0,3 — 3,2	9	1921	Populare Astrono- mio, VI Aufl
DOBERCK	2,46	0,43 -372	11	1912	A N 191, p. 425
ATTKEN	2,5-3,0	0,002 371	24	1910	Pop Astr 18, p 483
CAMPBELL	1,9	1,0 - 5,0	6	1913	Stellar Motions
Foucut	2,0	0,3 - 7,8	13	1916	BSAF 30, p 90.
AITKEN	1,76	0,45 - 3,3	14	1918	The Binary Stars,
VAN MAANEN.	4,2	0,18 - 45,7	39	1919	Publ ASP 31, p.231
MITCHELL , , , ,	10	0,38 — 71,3	19	1920	Ma Cormick Publ
MILLER and PITMAN .	5,44	0,11 -134.5	68	1922	AJ 34, p 127.
LUNDMARK , , ,	1,7	0,2 -150	250	1929	Card Catalogue,

In 1916 R. T. A INNES discussed the size of the stellar masses. For 50 stars fairly reliable orbits had been computed. Because of the lack of data concerning the parallaxes of these stars the author assumed that the absolute magnitudes were constant and equal to the absolute magnitude of the Sun. INNES prefers the term "gravitative power" instead of mass, as the last term suggests a body of matter and it is an assumption to consider mass as equivalent to gravitative power. Among the many interesting conclusions in INNES's paper we quote the one that few of the double stars have a gravitative power equal to that of the Sun In general the mass must be considerably smaller than the solar mass. It seems probable that the spectrum varies with the mass. On account of his assumption the masses of the B stars in INNES's list came out too low and the masses of red dwarfs too high. Some of the conclusions are naturally influenced by this fact. Only a few years later the situation with regard to our knowledge of stellar parallaxes had changed in such a favourable way that the order of magnitude of the mean masses of different spectral classes could be determined with fair accuracy.

In 1919 A. VAN MAANEN® derived the masses of 55 binaries, of which the parallaxes of 39 could be accepted as fairly well determined. The dispersion in the values is very small; indeed, it only amounts to 2,1 ©. Two stars which had a mass larger than 10 © were excluded and the lowest of the values was 0,18 © When the masses were plotted against the absolute magnitudes a quite definite relation was found, which was in good agreement with later theoretical derivations of the mass-luminosity relation. Also a relation between mass and velocity was sought for, but no definite result was found.

In 1922 B MEYERMANN<sup>8</sup> computed the masses of the components of 59 pairs. The mean values are  $\mathfrak{M}_A = 1.4 \odot$  and  $\mathfrak{M}_B = 1.2 \odot$ , and the dispersion is very small indeed. In a subsequent paper<sup>4</sup> the relation between mass and proper motion (reduced to km/sec by means of the known parallexes) was investigated and gave as a main result:

Nea	γ	п
3,7 O	19,8 km/100	19
1,2 O	25,4 II	39

Bouth African Journal of Science.
 A N 216, p. 301 (1922).
 A N 216, p. 385 (1922).
 A N 216, p. 385 (1922).

Mass-natios Visual Binaries.

System	a 1900	ð 1900	ለያያ (visual)	908 <i>m</i> /918 <sub>1</sub>	Authority	Ma/MA (adopt )	Period (years)
∑ 3062 13 Ceti	0 <sup>h</sup> 1 <sup>m</sup> ,0 0 30,1	+57°53' - 4 9	1,0 0,8	1,0 1,32	Boss Paraskevopou- 108	1,0	106 6,88
η Саязгоровае	0 43,0	+57 17	3,6	0,92 0,27 0,5 0,76 0,34	Pogo Struve Lewis Boss Mitchell		
o <sup>g</sup> Eridani BC	4 10,7	- 7 49	2,0	0,27 1,08 1,0 0,47 0,42	VAN BIESBROLCK LEWIS MITCHTLL VAN DEN BOS AI DLN		346
80 Tauri	4 24,4	+15 25	3,3	0,64	ABETTI VAN DEN BOS	0,45	150,2
α Aurigae Sirius	5 9,3 6 40,7	+45 54 -16 35	0,5	0,79 0,47 0,5	MERRILL AUWLRS SEC	0,79	0,28
Castor	7 28,2	+32 6	0,86	1,0	Boss Furner Mitchpll Rabe	0.44	50,2
Procyon	7 34,1	+ 5 29	13.0	0,60 0,2 0,33 0,31	RABE SEC Boss Boss	0,80	306
9 Argus	7 47,1	-13 38	0,6	0,315	MITCHELL	0,31	40,3
Cancri E Hydrae	8 6,5 8 41,5	+17 57 + 6 47	0,24	0,4 1,0 6 0,9	O Seruve Secliger Lewis Seei iger	1,0	23,1
& Urs Majoris	11 12,9	+32 6	0,5	1,0 1,5 1,0 0,72	MITCHELL BOWYER BOSS ABETH	0,95	15,3
v Virginis .	12 36,6	- 0 54	0,0	1,0	IIER12SPRUNG LEWIS Boss	1,0	59,8
25 Can Venati corum	13 33,0	+36 48	1,9	2,0	FURNER	2,0	220
or Contaurl ,	14 32,8	-60 25	1,37	1,05 0,96	ELKIN GILL ROBERTS		
\$ Boots .	14 46,8	F-19 31	2,0	0,85	Boss Bowyer	0,07	80,09
ξ Scorpn σ Cor Borealis	15 58,9 16 10,9	-11 6 +34 7	0,3	0,87 1,3 4 1,1 0,47	Boss S horr Lewis Hadley Boss	0,87	151,4
λ Ophiuchi ζ Hetculis	16 25,9 16 37,5	+ 2 12 +31 47	2,1	2,6 4,3 1,0 0,43 0,88	ABETTI LEWIS LEWIS BOSS CHANG	1,5	500
70 Ophruchi	18 0,4	+ 2 31	1,70		PRBY COMSTOCK LAU Boss	0,7	34,46

Mass-ratios. Visual Binaries. (Continued)

Bystom	a 1900	å 1900	(visual)	10 n/10 A	Anthority	SR a/SR a (more)	(years)
70 Ophluch!	18 <sup>b</sup> 0™,4	+ 2°31′		0,56	PAVEL		
		]	1	0,79	Mitchell,	ا م	Da a
f Delphini .	20 32,9	+14 15	1,0	0,89	CHANG DIRECTOR	0,8	87.7 26.8
h rechunt .	20 32,9	T14 13	1,0		HADLEY	1,1	20,0
т Судоц	21 10,8	+37 37	4,2	0.89	HADLEY		
. 5,622.	mt raid	1 1137 37	7100	0,89	VAN BIESDROECK		
		ĺ	1	0,77	ABETH	0,9	49,2
r Pegani	21 40,1	+25 11	0,5		HENROTRAU	0.40	11.6
Krueger 60	22 24.5	+57 12	1.5	1,14	RUSHELL		
•		'*' -		0,83	MITCHELL		
			}	0,45	Rugarit.		
			1	0,91	ALDEN		
		<b>l</b>	1	0,83	PAVEL and		
		ļ	)	ļ	Bernewitz	0,8	44,2
85 Pogasi , , ,	23 56,9	+26 33	5,15	4	Furner		
		]	1	3	LEWIS		
		1	1	1,0	Boss	'	1
			1	1,7	COMBLOCK	l	١
				1,78	VAN BIZEBROEGE	1,7	25,42

Computing the total space motions on the basis of data for 15 objects

The masses that are derived on the basis of double star data are dependent on the amount of the gravitation between the components. Thus the total mass of the binary system is obtained, i.e. not only the mass of the two suns, but also of planets and other dark bodies that may be present. There are 40 typical Sun stars for which the mass has been determined with a fair degree of accuracy. The mean value of the masses is  $1,05 \odot \pm 0,11 \odot$  and the mean value of the absolute magnitudes M = 4,76. It seems that these systems cannot be of a structure radically different from that of our solar system.

A remarkable event was the discovery of J S PLASKETT in 1922 that the O star BD + 6° 1309 was a very massive system. The two components had the mass values.

 $\mathfrak{M}_{A} = \frac{75.6}{\sin^{3} f} \circ, \quad \mathfrak{M}_{B} = \frac{63.3}{\sin^{3} f} \circ.$ 

The system has later been carefully watched for changes in the magnitudes, but so far without positive results. Plaskett's star does not seem to be an eclipsing binary system and therefore it is justifiable to conclude that the sum of the masses is at least 160 O

In Eddington's first theory of stellar evolution 40 © was determined as the upper limit for the mass of a star H von Zeipel has pointed out several times in his lectures that this was not a necessary consequence; if there is an upper limit it has a very high value. In the final theory of Eddington there seems to be no low limit for the possible size of stellar masses; on the other hand it seems that a limit exists, and it must be a quite exceptional case if a stellar mass is much above 400 ©.

The tables on p. 614 to 616 summarize the results hitherto found for the massratios in visual binaries and collipsing variables. There exist also some 100 well

<sup>&</sup>lt;sup>1</sup> MN 82, p. 447 (1922).

determined mass-ratios of spectroscopic binailes where both spectra have been observed. These have been excluded because of the lack of data for the magnitude of the components. The student interested in these stars should consult the catalogues by J. H. Moore [Lick Bull 11, p. 141 (1924)] and A. Beer [Beelin-Babelsberg Veroff 5, H. 6 (1927)]

Eclipsing Binaries.

		Tr C11	psing	Binari	es,			
Object	<b>≡ 1900</b>	411	603 - 40m -	Radius	Density	Pirillax	M	50
Onject	<b>■ 1900</b>	4111	901,B/901,A	of bright	or comp	T. IL. Olierx	712	ap
HD1337 .	0h 12h,5	1,2	0,93	23,80	0,00270	0",002	6.0	O8,5n
110 100/	0 12 3	1,22	6,00	23,0 U	0,002/0	0 ,002	4.8	O8,5n
TV Cassiopeiae .	0 13 .9	1,82	0,59	2,54	0.112	0 .0047	+0.8	Aon
		1,02	1 777	,,,,,	,,,,,	,,,,,,,	-1-2.6	AO
/ Tauri	3 55 1	1,49	0,33	5,35	0,024	0 ,0095	-1,1	133
			)				-1-0,4	
# Aurigae ,	5 52 ,2	0,00	0,98	2,83	0,11	0 ,030	4-0,6	Aon
		Į.			Į		+0,6	Aon
WW Aurigae	6 25 ,9	-	0,86	1,9	0,32	0.010	+2,2	A.7
Castor C	7 28 ,2	0,21	0,90	0,76	1,4	0 ,074	-1-9,6	Mile
37 10							+9,8	***
V Puppis .	7 55 ,4	0,45	0,77	7.5	0,050	0 ,004	-2,0	Bin
S Anthae		0.54	0.00		0.04	0 000	1,5	133n   A8n
o Milling	9 27 ,9	0,74	0,56	1,34	0,31	0 ,007	+2,9	A8n
W UrsacMajoris	9 36 ,7	0.04	0.72	0.00	1,92	0 ,013	+ 3,6	F8n
TO CHADILAJOUS	7, 06, 6	0,04	0,72	0,72	1,72	0 1013	+ 5,4	178n
RS Can Venati-	i	1	1	1			אינו בך	7.015
corum	13 6.0	0.92	1.00	7,1	0,004	0 ,0022	-0.0	F3n
	'' '',''	(0,52	1,00	1 "	0,004	0 1002	-1-0,9	Ko
i Bootis .	15 0 ,5	0,0	1,00	0,6	2,2	0 ,152(?)		G2
	1		1 -,	1	-,	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	6,3	}
U Cor Borealis	15 14 ,1	2,96	0,38	2,94	0,19	0 ,0037	+0,4	B3n
							4-3,4	B3n
U Ophinchi	17 11 ,5	0,18	0,88	3,23	0,18	0 ,0059	+0,2	133n
	{		l .	1	ĺ	į	+0,4	B5n
u Ilerculis	17 13 ,6	0,88	0,40	4,64	0,094	0 ,0071	-0,8	133n
TX Herculis		0.00	1 - 45	1			+0,1	B3n
TX Fierculis	17 15 ,4	0,68	0,87	1,57	0,53	0 ,0053	+2,3	A28
Z Herculis	17 53 ,6	0,35	0,87	4 57	0,28	0 ,013	+3,0	A28 F28
m Tiordatia	17 33 ,0	0,33	U,0/	1,77	0,20	0 1013	+3,5	F2
RXHercubs .	18 26 ,0	0.12	0,95	1,95	0,280	0 ,0064	-1-1.8	B9n
	10 20 ,0	1 01.2	0,73	1195	0,200	0 10004	1,9	B9n
β Lyrne	18 46 ,4	_	0,41	13,6	0,0012	0 ,005	-3.1	B20p
	( ' '- ''	(	( "	(	( -,		-2,6	cB8
RS Vulpeculae	19 13 ,4	2,35	0,31	4,22	0,06	0 ,0045	-0,4	B8n
	1	1			1		+2.0	B9
Z Vulpeculae .	19 17 ,5	1,45	0,45	4,54	0,052	0 ,0018		B3n
	[		1		İ	1	+0.7	<b>133</b>
σ Aquilae .	19 34 ,3	0,36	0,82	3,48	0,15	0 ,0060		B8n
Y Cygni .	}	1	0.00	1 4 40	1		+0,2	B8n
Y Cygni .	20 48 ,1	0,38	0,92	4,60	0,17	0 ,0022	1	B2n
	I		ř	)	ì	1	-0,4	B2n

I think that the first table will show how imperfect our knowledge of the mass-ratios of visual binaries still is. The length of the periods makes it difficult in most cases to cover even one period by observations. The values in the second table are by far more accurate than those in the first table.

The mass-ratios when plotted against differences in magnitudes show certain deviations from the curve computed in accordance with the mass-luminosity relation. There seems to be some systematic difference between the mass-ratios

of visual and eclipsing binaries. The considerable dispersion in the mass-ratios does not seem to be dependent on the errors in the individual determinations alone

218. Equipartition of Stellar Energy. J. Halm<sup>1</sup> was one of the first to apply the law of equipartition of the energy to the derivation of the average mass of the stars. According to the Maxwellian law the number of molecules of mass  $\mathfrak{M}$  with velocities between u, v, w and u + du, v + dv, w + dw is.

where A and k are constants.

The kinetic energy of a single molecule of mass IR is:

$$\frac{1}{2}\mathfrak{M}(w^{2}+v^{2}+w^{2}).$$

Hence the total energy of all the molecules.

$$E = \frac{1}{2} A \Re \int \int_{-\infty}^{+\infty} \int e^{-\mu^2 \Re (u^2 + v^2 + w^2)} (u^2 + v^2 + w^2) du dv dw,$$

or:

$$E = \frac{1}{8} \frac{A}{k^3} \sqrt{\frac{\kappa_e}{k^3 \Omega k}} \times$$

$$\left[\int\limits_{-\infty}^{+\infty}e^{-h^{2}\Xi\left(\pi^{2}+\pi^{2}\right)}dv\,dw+\int\limits_{-\infty}^{+\infty}e^{-h^{2}\Xi\left(\pi^{2}+\pi^{2}\right)}du\,dw+\int\limits_{-\infty}^{+\infty}e^{-h^{2}\Xi\left(\pi^{2}+\pi^{2}\right)}du\,dv\right],$$

or, the three integrals in the brackets being identical,

$$E = \frac{3}{8} \frac{A}{h^2} \sqrt{\frac{\kappa_i}{h^2 \Omega i}} \int_{-\infty}^{+\infty} e^{-h^2 \Omega i} e^{(p^2 + w^2)} dv dw.$$

The total number of molecules is:

$$N = A \int \int \int \int e^{-M \, \mathrm{d} x \, (x^2 + x^2 + x^2)} \, du \, dv \, dw = \frac{1}{2} \, A \, \sqrt{\frac{\kappa_s}{k^4 \, \mathrm{d} x}} \, \int \int \int \int e^{-M \, \mathrm{d} x \, (x^2 + x^2)} \, dv \, dw \, .$$

Hence.

$$\overline{E} = \frac{E}{N} = \frac{3}{4M},$$

i. e. the average kinetic energy is independent of the mass. If Q denotes the average speed we thus find:

TRΩ\* = const.,

i. e. the average speed is inversely proportional to the square root of the mass. HALM says that it is certainly not illogical to associate the rate of development from earlier to later types with the mass of a star. If stars of different masses started their development at the same time, it would be expected a priori that the lighter stars would cool down more quickly, and hence arrive at the more advanced spectral stages sooner than the heavy stars. The average mass of the "earlier" spectral classes will be larger than that of the more "advanced" spectral classes. In this way the lesser average speed of the earlier stars could be explained.

<sup>1</sup> MN 71, p. 610 (1911).

HALM quotes the results of KAPTLYN

Spectral class	Mean radial volocity	18	Spectral class	Mean radial velocity	13
B-B9	6,0 km/sec	64	GG5	12,6 km/sec	26
A-A5	11,2 ,,	18	KK5	15,4 ,,	55
F-F8	14,5 ,,	17	Ma	19,3 ,,	6

HALM points out that the ratio Mn/M, is probably independent of spectral class and quotes the following results

Group	901 <i>11</i> /901 <sub>4</sub>
Spectroscopic binaries	10.77 "Orion type"
Visual binaries	0,83 Other classes

Thus it is admissible to assume that the ratios of the average values of the mass-function Mi sini 2

 $(\mathfrak{M}_{d} + \mathfrak{M}_{n})^{2}$ for different types are practically identical with the ratio of their combined masses From spectroscopic binaries showing both the spectra HALM derived.

Orion type 
$$(\mathfrak{M}_A + \mathfrak{M}_B) \sin^3 s = 16.4 \pm 3.4 \bigcirc$$
 Classes A-G  $1.9 \pm 0.3 \bigcirc$ 

Ratio of average mass Orion stars/other classes = 8,6

Using the binaries where only one component was seen, i.e where only the mass-function is determined, it was found.

Period	Mass ratio Orion stars/other classes	11
5 <sup>d</sup> —30	8,6 O 4,6	29 24
>30	6,2	20

The square roots of the two values of the mean ratio of Orion stars/other classes are 2,9 and 2,5 Thus it is justifiable to assume that the Onion stars are on the average more massive than the stars of more advanced type.

From the above table of KAPILYN

the ratio of average speed of Orion stars/average speed of other classes is 0,42, whereas the inverse square root of the mass-ratio of the two groups is 0,34 or 0,40 Thus the agreement is good, a fact that seems to support the equipartition of energy

HALM has used the average parallaxes according to KAPPEYN's formula. and found (see close by) H N RUSSELL<sup>1</sup> had

Apparent Group  $\bar{n}$ M magnitude Orion stars 0",0066 -01/0 5,0 A stars . 8000, 0 5,0 0,0 F-K stars 5,0 0 ,0224 +1,8

found (see close by)

Combining his results with the preceding conclusion concerning the heavier mass of the earlier stars. HALM makes the remarkable statement that. "we may also say that intiinsic brightness and mass are in direct relationship "

Spectral class	Apparent magnitude	75	M
F8 G-G2 G5 K K5 M	7,0 7,8 8,6 7,4 8,2 8,3	0",044 0 ,029 0 ,064 0 ,119 0 ,254 0 ,221	5 <sup>11</sup> ,2 5 ,1 7 ,6 7 ,8 10 ,2

This is the first time, as far as the present writer knows, that a massluminosity relation has been thought to exist among the stars

<sup>&</sup>lt;sup>1</sup> A J 26, p 147 (1910)

HALM's investigation does not tell us anything concerning the size of the dispersion in stellar mass. It is not possible to determine this element without making complicated investigations. The method is of much value in any case, because of its possibilities for determining the average mass of the stars that do not belong to such selected groups as double stars or stellar clusters.

The relation between the mean speed and M is perhaps not applicable to all classes of stars. The O stars and the planetary nebulae are undoubtedly heavy bodies, but do not move as slowly as the B stars. When reviewing Seares's results we will see who the law of equipartition in general fits modern

data concerning the space motion of the stars

214. Schlesmer's and Baker's Study on Spectroscopic Binaries. An early contribution to this subject was made by Schlesinger and Baker', who analysed data derived from spectroscopic binaries. Considering first the systems in which spectra of both components have been observed they found without exception that the brighter component of a spectroscopic binary is always the more massive of the two. The close correspondence between mass and relative brightness (one could also say absolute brightness) is shown from the following summary where I stands for the (absolute) intensity

Ma/Da	Islia	•	Majitta	$I_B I_A$	п
0,99 0,91	1,00 0,73	2 3	0,74 0,66	0,53 0,40	3 4

The authors assumed that the discovery-chance of spectroscopic binaries is  $\infty$  sin; Thus  $\sin^2 t$  will be equal to 0,68, a value which is considered somewhat too low newadays. They concluded that in fifteen pairs showing both spectra the average mass was between  $4 \odot$  and  $5 \odot$ . They also concluded that this statement could not be extended to other spectroscopic binaries. The difficulties arising from the use of the mass-function were pointed out. From 44 pairs showing only one of the spectra it was concluded that the masses of spectroscopic binaries are of very different orders, some being much greater than that of our sun, while others are doubtless insignificant in comparison.

The peculiar law of distribution of the values  $\frac{2}{(N_A + N_A)^2}$  for Copheid variables was also commented upon Reasons were also given for the considerable uncertainty affecting several of the data for  $M_A/M_A$  collected or derived by Lewis, which were not in agreement with the conclusions of the authors

215. Lubranoras's Researches on the Masses of Spectroscopic Binaries. As a rule only the "mass-function", f, is determinable for a spectroscopic binary, vis

 $f = \frac{\mathfrak{M}_{b}^{2} \sin^{2} i}{(\mathfrak{M}_{A} + \mathfrak{M}_{B})^{3}} = +0.03993 \frac{(a \sin i)^{3}}{P^{3}}.$ 

LUDENDORFF puts  $\mathfrak{M}_B/\mathfrak{M}_A = \alpha$ .

Hence:  $f = \frac{\alpha^2}{(1+\alpha)^2} \, \mathfrak{M}_A \sin^2 i$ 

There is a wide disparity in the values of f. The numbers do not give much guidance for forming conclusions concerning the size of stellar mass. The situation turns out more favourably when the dependence between  $a \sin i$  and P is used. If the spectroscopic binaries are divided into groups according to the size of the period, and means are formed, a regular increase with  $\overline{P}$  is found in  $\overline{a \sin i}$ , in such a way that f or  $0.03993 \frac{(\overline{a \sin i})^a}{(P)^a}$  is rather constant.

<sup>&</sup>lt;sup>1</sup> Publ Alleghouy Obs 1, No. 21 (1910)

AN 189, p. 145 (1911).

The stars were divided into two groups containing the stars of the spectral classes Oe5—B8 and A—K. The mean numbers are given below, being still of interest.

When  $\overline{P}$  is plotted against  $\overline{a \sin \iota}$  the points of the two groups define a smooth curve. The smoothed values are given under the heading  $A \sin J$  The constant C is defined from the equation.

 $a\sin i - 1\sin J$ 

-0.70

-0.54

+0.09

-1.75

-2,50

+7,57

十3,97

-2,98

-0.67

-1,23

十0,11 一0,98

-1,43

+0,22

+0,90

+0,79

B	s	ta	r	S
	#1		Ì	

2

5

4

4

3

2

2

3

2

4

4

4

4

3

2

A-K stars

A sin /

0.74

3,84

5,28

6,92

9,32

18,90

50,13

54,44

1,71

2,65

3.76

7,09

9,94

16,21

24,22

30,72

æ sipe s

0.040

3,30

5.37

5.17

6,82

26,47

54,10

51,46

1,04

1,42

3.87

6,11

8,51

16,43

25,12

31,51

P

04,22

2,58

4,16

6,23

9.75

28,15

121,62

137 ,64

1<sup>d</sup>,35

2,60

4,39

11,38

18,89

39 ,34

71,80

102 ,56

$A \sin J =$	$\left(\frac{C\overline{P}^{8}}{0.03993}\right)^{\frac{1}{8}},$
--------------	---

and has the following values.

 $C = 0.34 \odot$  for the B stars

C = 0.11 O for the A-K stars. For 8 stars of such a period that they could not be included

in the graphs the agreement with the A-K curve was still good

Next Ludendorff inquies concerning the significance of the relations.

B stars 
$$\frac{\alpha^8}{(1+\alpha)^2} \mathfrak{M}_A \sin^8 i = 0.340$$
,  
A-K stars.  $\frac{\alpha^8}{(1+\alpha)^2} \mathfrak{M}_A \sin^8 i = 0.110$ 

The difference in C can be explained in different ways. The inclination for B stars might be systematically higher than for other stars on account of a preference of the former to move in orbits parallel with the galactic plane. This explanation does not seem very likely, because no dependence can be found between  $\overline{a\sin i}$  and the galactic latitude, but the material available was meagre

Another explanation is that the mass-ratio should be systematically larger for the helium stars than for other systems. As soon as  $\alpha$  deviates from unity small changes in  $\alpha$  give rise to considerable changes in f. A means of testing the possibility of the hypothesis is found in the cases where both spectra have been observed. Ludendorff finds

( <u>M 1+M 1)</u> sin <sup>3</sup> :	<u>or</u>	п	Group		
8,5 ⊙	0,70	9	B stars		
2,6 ⊙	0,80		A—K stars		

The scanty material rather suggests that the differences in mass-ratio work in the opposite direction, as regards the values of C, to that found above. Ludenderf therefore thinks that the difference in C is best explained by an actual difference in mass, as is also indicated from the numbers given above for  $(\mathfrak{M}_4 + \mathfrak{M}_B) \sin^3 i$ 

LUDENDORFF pointed out that the results concerning the higher mass of the B stars in comparison with the other stars are preliminary, and that the difference may be explained partly by other causes. On account of the higher accuracy attainable when measuring spectra of later types, smaller changes will be more easily discovered than in the case of B stars. Thus small amplitude B stars will not, as a rule, be discovered, which makes the mean value of the masses for

the later types apparently too low A closer study of the material available showed that no such dangerous effect had crept in among the numbers used.

The stars with the  $\epsilon$  and ac character in their spectra were not used, because of their poculiar position as regards the value of / This constant which is on an average 0,0034, suggests that  $\alpha$  is of the order 0,1 for these stars.

In general no conclusions can be made from the value of / concerning the size of the sum of the masses. If we have an infinite number of stars, sin\*s is 0,59 Because of the preference of high values of s, the value will be higher. LUDENDORFF assumes the value to be 0,75. Thus the mean masses are

$$\mathfrak{M}_A = 0.45 \frac{(1+\alpha)^8}{\alpha^8} \odot \quad \text{(B stars)} \,, \qquad \mathfrak{M}_A = 0.15 \frac{(1+\alpha)^8}{\alpha^8} \odot \quad \text{($\Lambda$-K stars)}.$$

For different values of  $\alpha$  the following table gives the values of  $\mathbb{R}_{\lambda}$  and  $\mathbb{R}_{n}$ .

			B stam			AK state	
railo a	$\frac{(1+a)^2}{a^2}$	W.	Ra	教者十数者	<b>W</b> ₄	W2	数4+数3
0,1	1210	544 O	54 O	598 O	181 ①	18 ①	199 ①
0.2	180	81 28	16	97	27	5	32
0,3 0,4 0,5	63	28	8	97 36	9	3	12 6,4
0.4	31	14	6	20	4,6	1,8	6,4
0,5	18	8	4	12	2,7	1,4	4.1
0,6	11,8	5.3	3,2	8,5	1,8	1,1	2,9
0.7	8,4	3,8	2,7	6,5	1.3	0,9	2,9 2,2
0,7 0,8	6,3	2,8	2,2	5,0	0.9	0,7	1,6
0,9	5,0	2,3	2,1	4,4	0,8	0,7	1,5
1,0	4,0	1,8	1,8	3,6	0,6	0,6	1,6 1,5 1,2

LUDENDORFF<sup>1</sup> returned to the subject in a later paper. A considerably increased material was at his disposal owing to the energy of the American astronomers who went in for the determination of orbits of spectroscopic binaries.

The following groups were excluded as before: the c and ac stars, some stars whose orbits were dependent on the displacements of the H and K lines, some stars where the orbital motion is not very well established (e. g.  $\alpha$  Orionis), v Sagittarii, stars with variable amplitude such as 12 Lacertae and  $\beta$  Cephei, Boss 1275, where the period used is probably much too large, and, lastly, five stars with periods  $>1000^4$ . The following mean values were found, the f being computed from f=0.03993  $\frac{a \sin t^2}{B^2}$ :

P	ë shi ë	#	7		¥	# Hal	и	ľ
	Os-	Qo5	_				Á	
154,66	21,60	3	1,6		14,49	1,57	4	0,07
	'Flo	—B5			2 .57	1,60	5	0,02
					3,62	2,43	4	0,04
1 ,18	1,55	4	0,11		4,02	4,09	4	0,17
2,54	3,12	5	0,19		6 82	4,72	4	0.09 0.10
3 ,81	4,94	5	0,33		10 21	5,92		0,08
5 12	6,02	4	0,33	0,25	17 .37	9,67	5	0,12
7 60	6,92	5 1	0,23		47 47	23,50	4	0,23
20 ,24	11,18	4	0,14		114 79	31,71	] ;	0,10
123 ,54	53,36	5	0,40		י אוידיי ן	3.17.		0,10)
0 ,5.			•		1		F	
	<b>38</b>	and B9			1 ,38	0,51	1 5	0,003 )
1 ,82	2,68	I 4 I	0,23 )		4 ,52	2,97	1 7	l ont l
4 41	3,75	4	0,11	0,15	10 .87	6,88	É	0,11 0,06
47 ,54	17,13	3	0,09	0,13	49,89	16,94	5	0.08
					עם עד ן <del>ע</del>	דעוטו ן	ر ا	V <sub>2</sub> UG
1 A 1	7 211, p	105 (192	Ю)					

If  $\alpha$  and vare on an average the same for the different spectral classes, then  $\mathfrak{M}_B/\mathfrak{M}_{B8}=1.7$ ,  $\mathfrak{M}_B/\mathfrak{M}_A=2.5$ ,  $\mathfrak{M}_B/\mathfrak{M}_1=4$ , where  $\mathfrak{M}_B$ ,  $\mathfrak{M}_{B8}$ ,  $\mathfrak{M}_A$ ,  $\mathfrak{M}_1$  are the mean masses of stars of the spectral classes B0—B5, B8—B9, A, and b respectively. The stars of the Oc class seem to have a very large mass.

There are only few binaries with known orbits in the G and K class, and there is a lack of short periods among the former stars. Four K stars give f = 0.02, which suggests even a lower mass for these stars than for the F stars

LUDENDORF then made investigations as to whether the stars of the same class give a constant value for  $\widetilde{f}$ . He remarks that this quantity seems to increase with increasing period. At first it might, therefore seem natural to think that systems of long period also have large masses, but a closer inquiry will show that this is not the case

216 Frequency of Stellar Masses for Different Spectral Classes. The important problem concerning the frequency of stars of different mass has been investigated by E von der Pahlen<sup>1</sup> For that purpose he makes use of the number of stars of different spectral classes and the relation between stellar mass and spectrum. Besides this the relation between spectral class and mean velocity is also used as an indicator of the mean mass for different classes, or in other words the equipartition of energy is supposed to hold also within the stellar system.

It is not enough to use these two series of data. It is also necessary to possess knowledge of the cosmogonic time scale or the time for each stage of development from the stage when a star starts more or less as a giant until it becomes more and more dwarfish. Before the theory of Eddington was worked out there was no possibility whatever of overcoming the difficulty. By the aid of a hypothetical assumption explained later on, v.d. Paillen computed the frequency. Other assumptions involved in his investigation are that the visible stellar system is in a stationary stage, in such a way that the number of visible stars in each spectral subdivision is constant with respect to the time. Putting the assumption in another form it means that for each interval of time just as many stars of each mass enter as giants as there are stars of the same mass developing into dwarfs through cooling, and thus becoming invisible.

The following notation is used

 $N_B$ ,  $N_A$ , ,  $N_M$ , Number of stars within each spectial class  $V_B$ ,  $V_A$ , ,  $V_M$ , Mean radial velocities for each spectial class

 $\mathfrak{M}_B$ ,  $\mathfrak{M}_A$ , ,  $\mathfrak{M}_M$ , Masses of the stars which at the top of their evolution reach the spectral classes given as subscripts

 $n_B$ ,  $n_A$ , . . .  $n_V$ , Frequency of stars of masses  $\mathfrak{M}_B$ ,  $\overline{\mathfrak{M}}_A$ , etc

 $v_B$ ,  $v_A$ , ,  $v_M$ , Mean radial velocities of stars of masses  $\mathfrak{M}_B$ ,  $\mathfrak{M}_A$ , etc.

 $T^{(B)}$ ,  $T^{(A)}$ , ,  $T^{(A)}$ , The lengths of time or periods during which stars of masses  $\mathfrak{M}_B$ ,  $\mathfrak{M}_A$ , etc are visible,

 $t_B^{(B)},\,t_A^{(B)},\,$  ,  $t_M^{(B)},\,$  The periods for a star of mass  $\mathfrak{M}_B$  to pass the spectral classes  $B,A,\,$  , M

 $t_A^{(A)}, t_F^{(A)}, \dots, t_M^{(A)}$ , The same quantities for a star of mass  $\mathfrak{M}_A$ .

 $t_F^{(P)}$ ,  $t_M^{(P)}$ , The same quantities for a star of mass  $\mathfrak{M}_P$ .

 $t_M^{(M)}$ , The same quantity for a star of mass  $\mathfrak{M}_M$ .

<sup>1</sup> AN 216, p 309 (1922)

l

Instead of the absolute periods i and T of time the following ratios are used

$$\begin{aligned} \tau_{A}^{(h)} &= \frac{f_{A}^{(h)}}{T^{(h)}}; \quad \tau_{A}^{(h)} &= \frac{f_{A}^{(h)}}{T^{(h)}}, \quad \tau_{B}^{(h)} &= \frac{f_{A}^{(h)}}{T^{(h)}}; \quad \tau_{B}^{(h)} &= \frac{f_{A}^{(h)}}{T^{(h)}}, \quad \tau_{A}^{(h)} &= \frac{f_{A}^{(h)}}{T^{(h)}}; \quad \tau_{B}^{(h)} &= \frac{f_{A}^{(h)}}{T^{(h)}}; \quad \tau_{B}^{(h)} &= \frac{f_{A}^{(h)}}{T^{(h)}}; \quad \tau_{A}^{(h)} &= \frac{f_{A}^{(h)}}{T^{(h)}}; \quad \tau_{B}^{(h)} &= \frac{f_{A}^{(h)}}{T^{(h)}}; \quad \tau_{B}^{(h)} &= \frac{f_{A}^{(h)}}{T^{(h)}}; \quad \tau_{A}^{(h)} &= \frac{f_{A}^{(h$$

Of these 21 quantities the last one is known and has a value = 1 because a star, having the mass  $\Re_M$ , belongs during all the time it is visible to spectral class M.

Then we have the equations:

$$N_B = n_B \tau_A^{(b)}$$
 $N_A = n_B \tau_A^{(b)} + n_A \tau_A^{(d)}$ 
 $N_M = n_B \tau_A^{(b)} + n_A \tau_A^{(d)} + n_B \tau_A^{(b)} + n_B \tau_A^{($ 

and:

clph 216.

$$V_B = v_B$$

$$V_A = \frac{v_B \, n_B \, \tau_A^{(B)} + v_A \, n_A \, \tau_A^{(A)}}{n_B \, \tau_A^{(B)} + n_A \, \tau_A^{(A)}}$$

$$V_{M} = \frac{v_{B} s_{B} \tau_{B}^{(B)} + v_{A} s_{A} \tau_{B}^{(A)} + v_{F} s_{F} \tau_{B}^{(A)} + v_{B} s_{G} \tau_{B}^{(B)} + v_{B} s_{B} \tau_{B}^{(B)} + v_{M} s_{M} \tau_{B}^{(A)}}{s_{B} \tau_{B}^{(A)} + s_{A} \tau_{B}^{(A)} + s_{B} \tau_{B}^{(A)} + s_{B} \tau_{B}^{(A)} + s_{B} \tau_{B}^{(A)} + s_{B} \tau_{B}^{(A)}}.$$

The unknown v's can be eliminated by using the equipartition of energy in the following form:

$$\mathfrak{R}_{\mathcal{S}} v_{\mathcal{S}}^{\dagger} = \mathfrak{R}_{\mathcal{S}} v_{\mathcal{S}$$

The second equation then becomes:

$$n_B \tau_A^{ib} \left( V_A - V_B \right) + n_A \tau_A^{ib} \left\{ V_A - \left( \frac{\Omega R_B}{\Omega R_A} \right)^{\frac{1}{2}} V_B \right\} = 0 \; .$$

Further notation introduced is as follows:

$$n_B \tau_B^{(l)} = p_B;$$
  $n_A \tau_A^{(l)} = p_A;$   $n_B \tau_B^{(l)} = p_B;$   $n_G \tau_B^{(l)} = p_G;$   $n_K \tau_B^{(l)} = p_K;$   $n_H \tau_B^{(l)} = p_H;$   $V_A - V_B = C_A^B;$   $V_A - \left(\frac{\mathfrak{M}_B}{\mathfrak{M}_A}\right)^{\frac{1}{2}} V_B = C_A^A;$  ... and in general:

$$C_A^R = V_B - \left(\frac{\Omega R_B}{2V_B}\right)^{\frac{1}{2}} V_B.$$

 $(\phi_{\mathcal{S}})$  is the number of stars of spectral class S).

The equations then take the form

$$\begin{split} N_{B} &= \phi_{B} \\ N_{A} &= \phi_{B} \frac{\tau_{A}^{(B)}}{\tau_{B}^{(B)}} + \phi_{A} \\ N_{F} &= \phi_{B} \frac{\tau_{F}^{(B)}}{\tau_{B}^{(B)}} + \phi_{A} \frac{\tau_{F}^{(A)}}{\tau_{A}^{(A)}} + \phi_{F} \\ & \cdot \cdot \cdot \\ C_{A}^{B} \phi_{B} \frac{\tau_{A}^{(B)}}{\tau_{B}^{(B)}} + C_{A}^{A} \phi_{A} &= 0 \\ C_{F}^{B} \phi_{B} \frac{\tau_{F}^{(B)}}{\tau_{B}^{(B)}} + C_{F}^{A} \phi_{A} \frac{\tau_{F}^{(A)}}{\tau_{A}^{(A)}} + C_{I}^{I} \phi_{F} &= 0 \end{split}$$

The system of equations is indeterminate on account of the appearance of the quantities  $\tau_s^{(0)}$ , of which we do not know much, if anything at all. If we represent the development of a star passing through the spectral classes by means of a curve that is some function of the time, then the mass is the parameter that will determine the form of this curve. It seems plausible that a continuous change in mass corresponds to a continuous change in this curve, and that when the masses do not vary within too wide limits, the different curves show some general resemblance. This will be the same as if the ratios of the periods expressing the times it takes for  $\blacksquare$  star to pass through the spectral classes, will oscillate around some values valid for a star of mean mass. Approximately the ratios of periods for corresponding spectral stages (counting from the highest stage attainable for a star of given mass) will be equal for all stars

In this way we reach the necessary number of conditions to enable us to solve the above system v. d. Pahlen is aware that the assumption is rather bold. According to the theory of Eddingson the difference between two stars of which one can reach the B stage and the other the A stage is some 3 ©. On the other hand the same difference for two stars of classes K and M is only some  $\frac{1}{20}$  O. If the idea of v. d. Pahlen were to be worked out strictly it would be necessary to make a new spectral division fulfilling the condition that the masses increase in arithmetical proportion from class to class

According to the assumption made above we have:

$$\begin{split} \frac{\tau_{d}^{(B)}}{\tau_{B}^{(B)}} &= \frac{\tau_{G}^{(A)}}{\tau_{d}^{(A)}} = \frac{\tau_{G}^{(F)}}{\tau_{B}^{(F)}} = \frac{\tau_{H}^{(G)}}{\tau_{G}^{(B)}} = \frac{\tau_{H}^{(F)}}{\tau_{K}^{(F)}} = \sigma_{A} \\ & \frac{\tau_{F}^{(B)}}{\tau_{B}^{(B)}} = \frac{\tau_{G}^{(A)}}{\tau_{d}^{(B)}} = \frac{\tau_{A}^{(F)}}{\tau_{F}^{(F)}} = \frac{\tau_{H}^{(G)}}{\tau_{G}^{(B)}} = \sigma_{F} \\ & \frac{\tau_{G}^{(B)}}{\tau_{B}^{(B)}} = \frac{\tau_{A}^{(A)}}{\tau_{A}^{(A)}} = \frac{\tau_{H}^{(F)}}{\tau_{A}^{(F)}} = \sigma_{G} \\ & \frac{\tau_{H}^{(B)}}{\tau_{H}^{(B)}} = \frac{\tau_{H}^{(A)}}{\tau_{A}^{(B)}} = \sigma_{R} \\ & \frac{\tau_{H}^{(B)}}{\tau_{H}^{(B)}} = \sigma_{M}. \end{split}$$

Hence'

$$\begin{split} N_B &= p_B \\ N_A &= p_B \sigma_A + p_A \\ N_F &= p_B \sigma_F + p_A \sigma_A + p_F \\ N_G &= p_B \sigma_G + p_A \sigma_F + p_F \sigma_A + p_G \\ N_R &= p_B \sigma_R + p_A \sigma_G + p_F \sigma_F + p_G \sigma_A + p_R \\ N_M &= p_B \sigma_M + p_A \sigma_R + p_F \sigma_G + p_G \sigma_F + p_K \sigma_A + p_M \end{split}$$

and:

$$\begin{split} C_{A}^{n}\dot{p}_{B}\sigma_{A} + C_{A}^{4}\dot{p}_{A} &= 0 \\ C_{F}^{n}\dot{p}_{B}\sigma_{F} + C_{F}^{4}\dot{p}_{A}\sigma_{A} + C_{F}^{n}\dot{p}_{F} &= 0 \\ C_{G}^{n}\dot{p}_{B}\sigma_{G} + C_{G}^{4}\dot{p}_{A}\sigma_{F} + C_{G}^{n}\dot{p}_{F}\sigma_{A} + C_{G}^{n}\dot{p}_{G} &= 0 \\ C_{F}^{n}\dot{p}_{B}\sigma_{E} + C_{F}^{4}\dot{p}_{A}\sigma_{G} + C_{F}^{n}\dot{p}_{F}\sigma_{F} + C_{F}^{n}\dot{p}_{G}\sigma_{A} + C_{F}^{n}\dot{p}_{E} &= 0 \\ C_{F}^{n}\dot{p}_{B}\sigma_{M} + C_{F}^{4}\dot{p}_{A}\sigma_{E} + C_{F}^{n}\dot{p}_{F}\sigma_{F} + C_{F}^{n}\dot{p}_{G}\sigma_{F} + C_{F}^{n}\dot{p}_{F}\sigma_{A} + C_{F}^{n}\dot{p}_{M}\sigma_{A} &= 0 \end{split}$$

From these all  $\phi$ 's and  $\sigma$ 's can be determined.

The following data were used:

Spectral class	Ж	ν	Tomperature	178
B F G M	3196 8852 7950 7400 9090 684	6,8 km/sec 11.3 ;; 14.5 ;; 15,4 ;; 16,4 ;; 17,2 ;;	17000° 10000 6750 4750 3700 3100	4,27 @ 1,23 0,59 0,32 0,20 0,15

The numbers in the second vertical row give the numbers of stars brighter than 8<sup>m</sup>,0 per 10000 square degrees according to Tab. 11 in Groningen Publ No. 30.

In the computations it was necessary to include the M stars in the K group.

The results are:

	In persont	
ng == 1582	4.3	😘 🖚 0,337
$n_0 = 2802$	7.5	ε <mark>∰ →</mark> 0,177
m <sub>p</sub> = 6033	16,3	r <del>ja</del> → 0,080
$n_d = 17266$	46,5	$\tau_q^{(B)} = 0.217$
m <sub>p</sub> - 9486	25,5	$r_{K}^{(B)} = 0.189$

According to the author these numbers are to be taken only as a first rough

approximation.

It is also of importance to know the frequency function of masses for stars in a certain volume of space. This problem can be solved by reducing the number of stars  $n_B, n_A \dots$  in the above equations to equal volumes. Because of the lack of parallaxes Eddington's theory is used in such a way that the absolute (belometric) magnitudes, M, are used which are computed from the supposition of constant space-density

The space unit is a sphere with such a radius that the stars of mass  $\mathfrak{M}_B$  in stage B which are situated on its surface are of apparent magnitude  $+8^{m}$ ,0.

Thus:

$$M_B + C_B = 8^{\rm m},0,$$

where  $M_B$  is the bolometric magnitude of a star of mass  $\mathbf{R}_B$  and  $C_B$  the reduction to be applied to  $M_B$  to give it the absolute visual magnitude of spectral

class B. The ratio of the distances  $r_1$  and  $r_2$  of two stars of equal apparent magnitude having the absolute magnitudes  $M_1$  and  $M_2$  is

$$r_1/r_2 = 10^{-0.2(M_1 - M_2)}$$

and the ratio of the two volumes  $v_1$  and  $v_2$  with radii  $r_1$  and  $r_2$  is.

$$v_1/v_2 = 10^{-0.6(M_1-M_2)}$$
.

A star of mass  $\mathfrak{M}_B$  in spectral stage A has a visual magnitude  $M_B+C_A$  and thus  $n_B$  in the equations related to stage A has to be multiplied by the factor

In the equations corresponding to stages F, G, etc  $n_B$  appears multiplied by the factors  $10^{-0.6(C_F-C_B)}$ ,  $10^{-0.6(C_G-C_B)}$  etc

In the same way we find for  $n_A$  in the equation for the A stage the factor  $40^{-0.6}(M_A+\sigma_A-M_B-\sigma_B) = 10^{-0.6}(M_A-M_B) \cdot 10^{-0.6}(\sigma_A-\sigma_B)$ 

We introduce

$$\overline{n_A} = \eta_A \, 10^{-0.6(M_A - M_B)} \\
\overline{n_T} = n_F \, 10^{-0.6(M_F - M_B)} \\
\vdots \\
\overline{n_K} = n_K \, 10^{-0.6(M_A - M_B)}$$

The following values were used in the calculation

$$M_B = -2^{m},3$$
  $C_B = +1^{m},8$   $M_1 = +0,2$   $C_A = +0,3$   $M_b = +2,2$   $C_b = 0,0$   $M_0 = +4,0$   $C_0 = +0,2$   $M_h = +5,0$   $C_k = +0,8$ 

from which it was found that

			In percent	
$\overline{n_{A}} =$	850	$n_{\rm A} = 20389000$	88,92	$\tau_B^{(R)} = 0.589$
71 <sub>0</sub> ===	376	$n_0 = 2268000$	9,89	$\tau_A^{(\beta)} = 0.039$
71 p ===	464	$n_p = 232000$	1,01	$\tau_{k}^{(R)}=0.035$
$\overline{n_A} = 1$	1123	$n_A = 35500$	0,15]	$\tau_{\theta}^{(B)}=0.070$
11 n ==	5424	$n_B = 5500$	0,02	$\tau_{\rm A}^{(B)} = 0.267$

Another computation was undertaken of the frequency function of the masses of stars brighter than 8m,0, in which attention was paid to the change in the visual magnitude with the colour. The following results were found

Spectral class	907,21	MA	908 <sub>2</sub> m	Me	W <sub>K</sub>	Sum	Mean masses
B	3196	Q	0	0	0	3196	$\mathfrak{M}_{R}=4.27 \mathfrak{O}$
A	1679	7176	l o	0	0	8855	M, = 1,81
F	2008	1248	4698	0	0	7954	$\mathfrak{M}_{k} = 1.62$
G	3210	748	410	3028	0	7396	$\mathfrak{M}_{q}=2,14$
Iζ	5 5 2 5	680	141	152_	3267	9773	$\mathfrak{M}_{K}=2,56$
Sum	15618	9860	5249	3180	3267	37174	

217. Sproul Determinations of Masses In 1922 J A MILLER and J II. PITMAN<sup>1</sup> made use of the material available for computing the masses of the visual binary stars. The original parallax programme of the Sproul Observatory was outlined with a view to determine the masses of these stars. All the visual binaries

<sup>1</sup> A J 34, p 127 (1922)

with well-determined orbits have been included, together with objects for which tolerable elements will be known in the near future. Most of these objects have also been included in the other parallax observatories, so in most cases determinations of several modern parallax values are available.

Most of the pairs in question are so close together that the combined images on the plates at Sproul are sensibly round. The question then arises whether the orbital motion will not change the shape of the photographic image and vitiate the determination of the parallaxes. PITMAN and Miss POWELL have made an investigation with regard to this question using the equation

$$C + i\mu + i\pi + \frac{\theta}{2}\sin\theta = d,$$

in which d is the total displacement, and the fourth term on the left side takes into account the apparent orbital motion, q and  $\theta$  being the radius vector and the position angle of the star in its orbit. For the stars with  $\Delta m$  smaller than  $2^m$  it was found that there were the following changes in the parallaxes:

According to the opinion of the present writer the errors in the trigonometric parallaxes, other things being equal, are alightly larger in the case of double than in the case of single stars. As the orbital motion contributes so little to the error, the discrepancy is certainly caused by other factors, which are mainly dependent on the nearness of the images

An	#
0",000—0",001 0 ,002 0 ,004 0 ,009	11 1 1

The average sums of the masses within the different spectral classes are as follows according to MILLER and PITMAN:

Openiral clear	В	_A	It.	G	K	П
Wa + Wa	(14,91 ①) B	3,490	3,92 © 11	1,77 @	1,570	0,650

The mass of the B stars was taken from other sources

218. Primar's Investigation. An extensive presentation of the existing material for deriving the masses of the binary stars was given by J. H. Pitman in 1929<sup>1</sup>. The orbits of the binaries are generally those given by van den Bost together with a few orbits, new or revised, published since the latter's paper appeared. The parallaxes are taken from the manuscript catalogue of the Sproul Observatory. In general only modern determinations are used. These are corrected for systematic errors and weighted according to the method given in Pop Astr 31, p. 244. The corrections reduced the determinations of trigonometric parallaxes to the same system as Adams's spectroscopic results; in this sense the parallaxes tabulated are absolute.

The objects are divided into three groups, which are given in separate tables. Table I contains 33 stars for which the probable error of the parallax does not exceed fifteen per cent of the parallax itself. Table II contains 20 stars for which the probable error lies between fifteen and thirty per cent of the parallax, while Table III contains 54 cases in which the probable error exceeds thirty per cent and those for which only one trigonometric determination has been made. In each case the trigonometric parallax has been made the basis of classification.

The results are summarized in the following table, where the absolute magnitudes are visual values. The second lines in the table give the average masses and absolute magnitudes for the single components. The numbers #

<sup>&</sup>lt;sup>1</sup> A J 39, p. 57 (1929). <sup>8</sup> B A N 3, p. 149 (1926).

			Visital	al binaries				-	chpsm	Echysing binaries				Spe	ctrosc	Spectroscopic binaries	23	
Spectral	Trigo	Тпдовошецис 🛪	20	Spe	Spectrographic x		Ing	Ingonometric 7	L.	Spe	Spectrograpine л	ш.	Trigo	тиголошение т		Spec	Spectrographic 1	۲
	Mean mass	M	**	Mean mass	M.	1 %	Mean mass	M	n n	Wean mass	M	#	Vean mass	Ж	16	Mean mass	M	
0 - Bo			_							70,10	-4 <sup>x</sup> ,26	64	17,40	24,39	61	85,00	-4 t 3	
									<u> </u>	35,0	-2,68	4	8,7	28	44	42,5	-3 ,55	10
B1-B3				12,90	-1 <sup>2</sup> ,14	44	20 870	-	_	15,24	-1 ,54	1	15,5	1 99' 0	ণ	9,91	-1	'n
,				6,45	-0 ,27	7	10 44	09,		7,62		44	7.75	1 29	4	5 22	0 -	~ - ~+
B4-B8				1	,		787	10 74	-	7,18	₽, 0-	*	1,58	5. 5.	বল	11,21	8,0	0
							38	+1 26	4	3 39	1,04	00	0,79	3,50	Ø	5,37	o ú	
B9-A1	2 650	2 K	9	2 69	2 ,23	6	4,71		-	4,61	0 ,51	4	1,88	0 ,61	4	2,60	O ní	
	1 52	ιυ !Ο			20, 21	15	2,37	7, 0-		2,36	1,52	7	96.0	1,66	00	1,30	4	30
A2-A6	929	**	4	5,47	1 ,16	6			-	4,29	1,30	ମ	320	0 12	ŧ٦	2 52	4,	
	Lr tr	C.		2.74	2 ,07	18	_		-	2,15	2 ,23	4	1,60	1 18	9	1,26	2 4.	دn
A7-F2	7.7	c		5.17	1.88	40				1,17	0 ,53	<del>-</del>	2 95	3,89	~	1,73		9
	1.50	4		*****	3 32	3				0,58	1 30	7	1,48	4 ,57	C)	0,86		-
표3 - 표7	244	2			51.5	11	2,90	4,82	7	2,76	2 ,21	63	2,02		١٠	2,56		
	134	4			4 54	28	1,45			1 59	2 83	<del>ش</del>	1,01	3,64	2	1,28	ω Ģ	77
G0-G2	2,11	3 .76	18	2,22	3 ,70	24	1,26	5,60	C)	1 26	5 ,13	C1	2,01	-	44	2,2	2	
	1 06	4. 9.			4 75	45	0 63	5 83		1 08	5 09	٧,	9	5 16	CI.	90	ή·	· ^
63-69	4,75	9,			4 92	11			_				1 38	4 22	N.	7 33		_
	2,28	6 13				23							69 0	5 61	4	69,0	√ 4	
M	1,54	6			5,38	7				_		,		_	,			
	0 78	7 43				16			_	1,74		**						
×	200	10 ,43			9 97	ч	1,20	8 22,	77	1,20	8,20	7		_				-
						1	0) (			000		•		•		-		-

628

represent the numbers of stars, only in the case of the trigonometric parallaxes of visual binaties the *n* represent the weights given to the mass-values

PITMAN has reduced the M's to bolometric values and has made detailed companisons between his results and the mass-luminosity diagram of Eddington. A change of -1-0,15 m in the parallax will increase M by  $0.3\,$  and decrease  $\log \mathfrak{M}$  by 0.48, while  $\mathfrak{u}$ change of  $-0.15\pi$  in the parallax will increase  $\log \mathfrak{M}$  by 0.21 and decrease M by 0,35 Seventy-five per cent of the first-class determinations fall within these limits of the curve. There are, however, a few cases that would require changes of  $0.50 \pi$  or more in the parallax With regaid to the values denived from the spectrographic parallaxes there is a marked concentration of stars of approximately the same mass and absolute magnitude as the Sun There is also a very large scattering, which may or may not be due to errors in the observed data

The spectroscopic binaries that show both spectra were also investigated From the "Third Catalogue of Spectroscopic Binaries" and various other sources Pitman collected

<sup>&</sup>lt;sup>1</sup> Lick Bull 11, p 141 (1924)

75 such systems and compared the minimum values of M with the mass-luminosity law. The comparisons of PITMAN show that there is a correlation between M and log M. The value of the coefficient of correlation can be estimated m having a value of about 0,7. Another question is whother such a correlation has a physical meaning such as that expressed in the mass-luminosity law. For the present it hardly seems possible to answer this question even if the material available seems to suggest a revision of the constants in Eddington's formula.

819. Statistics of accurately Determined Stellar Masses. E B. Wilson and W. J Luyten<sup>1</sup> made an investigation with a view to discuss the material concerning stellar masses as a set of precise astronomical measurements.

To begin with they quote the 8 cases of stellar mass determinations given by Eddington in his well-known book, "Stellar Movements" The figures expressed in terms of the mass of our Sun are in order of size 0,7, 1,0, 1,0, 1,3, 1,8, 1,9, 2,5, 3,4, from which  $\Re = 1.7 \pm 0.2$ . As no masses muy be negative and there is no restriction, except through disintegration by internal light-pressure or dynamical fission upon the upper side, it is natural to discuss the distribution, not of the mass itself, but of its logarithm. The 8 results are -0,155, 0,000, 0,000, 0,114, 0,255, 0,279, 0,398, 0,532, from which  $\log \mathfrak{M} = 0,178 \pm 0.05$ . The dispersion  $\sigma$  is 0,21  $\pm$  0,035 and the probable error  $\varrho = \frac{1}{2}\sigma = 0,14$ . The geometric mean mass is 1,5 and coincides with the median. If the distribution is normal a departure of  $9\mu = 1.26$  in the logarithm from its mean 0.18 could not occur; because there is only one chance in a billion and a half that log IR should exceed 1,44 and an equal chance that it should be less than 8,92-10, and there are probably less than one billion stars nearer than 2000 parsecs, which makes it certain that no such numbers could possibly be registered on the best photographic plate. There are at least three known binaries the mass of which exceeds 10<sup>1,44</sup> = 27,5 ©. It is clear, therefore, that a normal distribution as determined from these data has no correspondence in the stellar world.

Then the authors use the following 45 systems<sup>a</sup> as having reasonably well-determined masses:

```
a Aurigne
          7,50 ① = 4,18 ① + 3,32 ①
                                   5 Cassiopoiso 1,13 ⊙ ~ 0,89 ⊙ + 0,24 ⊙
                                               1,09
# Aurigae
           4,72 = 2,38 + 2,34
                                    ₽ Bootis
                                                     = 0.58 + 0.51
                         +0.96
a Can Mai
           3,41
                 2.45
                                    Sun
                                               1,00
80 Tanri
                = 1.85 + 0.72
           2,57
                                    85 Pogosi
                                                0,93
                                                     = 0.60
                                                              十 0.33
a Contauri 2.11
               = 1,14 + 0,97
                                    #Horonlis BC 0.88
                                                     = 0.44
                                                              + 0,44
70 Ophiuchl 1,82 = 0,96 + 0,86
                                    Krueger 60 0:43
                                                     = 0,30
                                                             + 0,13
ζ Hercults 1.60 = 1.12
                                   el Eridani BC 0,41
                                                     = 0,21
                         + 0,48
                                                             + 0,20
a Can. Min. 1,50 - 1,13 + 0,37
```

The mean  $\overline{\mathbb{R}} = 1.97 \pm 0.28$ , the median is still 1.50,  $\overline{\log}$  is 0.18  $\pm$  0.06, and  $\sigma_{\log}$  = 0.34  $\pm$  0.04. The mean deviation  $\vartheta$  is 0.27 and the test  $\sigma_{\overline{\mathbb{R}}} = 1.25 \vartheta$  for normality is perfect. A study of the distribution of the log  $\mathbb{R}'$ s with regard to the size of the probable error,  $\varrho = 0.23$ , also gives evidence of the satisfactory normality of the frequency function. The  $\mathbb{R}$  is 1.50. The larger material in this second case has increased the size of the error by a fifth. The authors say that even considering the small size of samples 8 and 15 it is difficult to reconcile the relative magnitudes of the standard deviation and their probable errors; the difficulty would have been even greater if the additional 7 had been treated as a second sample. The fact is that the two sets probably do not belong to the same statistical universe—one at least of the samples is not fair.

Wash Nat Ac Proc 10, p. 394 (1924)

From HERTEEPRUNG's paper in BAN2, p. 15 (1923).

If charmed with the excellence of the normal distribution of the 15 cases one would derive the probability of a binary with  $\log \mathfrak{M}$  as great as 0.18  $\vdash 9\varrho$  = 2.21 it is found that the chance will be one in a billion and a half for a star of mass 1620. The authors points out that we have Plaskeri's star with such a mass, and that 27 Canis Majoris probably has a still larger mass.

Of course, considerable uncertainty is involved on account of imperfect parallax data. The figures may be inaccurate by 30 percent, which means a variation of some 0,12 in the individual logarithms. If there is nothing systematic in such errors the error in the mean will be about 0,03. As far as the accidental errors go, the mean will be reasonably well-established although the error is liable to increase when a more extensive material is at hand

A similar discussion is given for the 29 stars of Herizsprung's list when each component of a binary is counted separately. The  $\overline{\mathbb{M}}$  is then 1,07  $\pm$  0,42 and the median mass 0,86 and the distribution is skew. The log  $\overline{\mathbb{M}}$  is 9,984  $\pm$  10  $\pm$  0,044, the median 9,934  $\pm$  10, and  $\overline{\mathbb{M}}$  = 0,965. The dispersion is 0,357  $\pm$  0,030, and checks perfectly with  $\overline{\mathbb{M}}$  Its value is not greater to 29 stars than for 15 systems. The mean is better determined statistically in the first sample than could be expected before when one remembers that the scanty material has only been doubled.

220. Real and Apparent Masses If the mass of a star undergoes a steady decrease from spectral class B to M, as is indicated by the work of Spares, various suggestions present themselves as an explanation of this phenomenon B. A Kostitzin<sup>3</sup> has applied the results of Majorana<sup>3</sup> with regard to a possible absorption of the gravitation. The real mass of a star is designated by  $\mathfrak{M}_r$ , and the apparent mass by  $\mathfrak{M}_\sigma$ . Let further r be the radius,  $\bar{\varrho}$  the mean density, and  $\alpha$  the coefficient of absorption = 7.59  $\cdot$  10<sup>-12</sup> for the Sun. Then the attractive force will be diminished in accordance with the "law of progressive absorption" and in the case of a homogeneous liquid mass, where  $\bar{\varrho}$  is equal to the true density, the following equations hold good

$$\mathfrak{M}_{\alpha} = \frac{\pi_{\alpha} \gamma^{3}}{\alpha} \left[ 1 + \frac{e^{-2\alpha \overline{\varrho}r}}{\alpha \overline{\varrho}r} + \frac{e^{-2\alpha \overline{\varrho}r}}{2\alpha^{2} \overline{\varrho}^{3} r^{2}} - \frac{1}{2\alpha^{2} \overline{\varrho}^{3} r^{2}} \right], \qquad \mathfrak{M}_{r} = \frac{4}{3} \pi_{\sigma} \overline{\varrho} r^{3}.$$

Introducing a new variable  $2\alpha \tilde{\varrho}r = v$  and putting

$$\varphi(v) = [(1 + v) e^{-v} + 0.5 v^2 - 1] 3 v^{-3}$$

Kosticzin finds the relation;

$$\mathfrak{M}_{a} = \mathfrak{M}_{r} \varphi (v)$$

Accordingly  $\varphi(v)$  is the ratio between the apparent density and the true density. If the above value of  $\alpha$  and  $\mathfrak{M}_r = 5.3$  times the apparent mass of the Sun are accepted for the Sun, it is found that for a stai with the same real mass as the Sun and  $r = 9 \, r_{\rm O}$  the apparent mass  $\mathfrak{M}_a$  is nearly equal to its real mass, viz 5.3 times the apparent mass of the Sun. If  $r = 3 \, r_{\rm O}$  the apparent mass is four times the apparent mass of the Sun. The diameters thus derived for different spectral classes are of the same order of magnitude as the computed ones.

H N Russell has pointed out that if the absorption of gravitation is accepted there are a number of important astronomical consequences. The true masses of the planets have been computed according to this theory and it is found that the inertial masses cannot be equal to the true masses. If they are assumed

<sup>&</sup>lt;sup>1</sup> Mt Wilson Contr 226 (1922)

<sup>&</sup>lt;sup>2</sup> Publ Obs Astrophys Centr Russ Moscou 2, p 289, 303 (1923)

<sup>&</sup>lt;sup>2</sup> Phil Mag 39, p 488 (1920) <sup>1</sup> Ap J 54, p 334 (1921), Mt Wilson Contr 216.

to be equal to the apparent gravitational masses we are led to such discrepancies in the case of the tides that the conclusion is unavoidable that the coefficient of absorption cannot exceed <sup>1</sup>/<sub>5000</sub> of the value assigned to it by MAJORANA.

221. Seares's Researches. In an extensive paper of 1921 F. II. Seares's has made an interesting study of the masses and densities of the stars partly along new lines. The salient point in his method is a comparison between the absolute magnitude  $M_d$  as derived from the dynamical parallex  $n_d$  and the spectrographic magnitude M as derived from n. The well-known relation

$$\mathfrak{M}=\mathfrak{M}_A+\mathfrak{M}_B=\frac{a^2}{\pi^2P^4}$$

gives.

$$\log \mathfrak{M} = k - 0.6 M_{\star}$$

where

$$M = m + 5 + 5 \log n$$

and

$$h = 3\log a - 2\log P + 0.6m + 3.$$

The assumption used in the computation of  $\pi_2$  is  $\mathfrak{M} = 2 \odot$ . Thus if the orbital elements are known:

$$0.30 = k - 0.6 M_{\star}$$

and;

$$\log \mathfrak{M} = 0.30 - 0.6 (M - M_d) = 0.30 - 0.6 \Delta M$$

and for a group of stars:

$$\log \overline{M} = \log \overline{M} = 0.30 - 0.6 (\overline{M} - \overline{M_e}) = 0.30 - 0.6 AM$$

The next last equation only holds good for individual stars in the case of binaries where the elements are known, because the mean inclination of the orbital planes is involved in the dynamical parallaxes. The last equation holds good for any group of stars.

At that time, in the case of the binaries investigated, only  $M_d$  was known, and thus an indirect process was necessary. Sharks used  $M_d$  from single stars of known parallax, whose selection with respect to the stars as a whole presented the same characteristics as those of the binaries themselves.

If  $\overline{M_s}$  represents the mean absolute magnitude of a certain spectral type of single stars of known parallax, and  $\overline{M_b}$  the corresponding value for binaries of the same type, we have:

$$\widetilde{M_s} = \widetilde{M_s} + \delta M_s$$

Thus o'M expresses the influence of difference in selection. We may write:

$$\overline{M_b} - \overline{M_d} = \overline{dM} = \overline{M_b} - M_d + \delta M = \overline{dM_b} + \delta M.$$

Shares has derived  $\partial M$  from the some hundred binaries of measured parallax and calculated  $\overline{\partial M}_s$  for each spectral type by comparing the 550 stars in the lists of Jackson and Fuener with the homogeneously selected single stars of known parallax. Then  $\overline{\partial M}$  was formed and  $\mathfrak M$  computed. The underlying assumption is that the mass-luminosity relation is the same for both binaries and ordinary stars.

The binaries and single stars of known parallax were grouped according to apparent magnitude and spectral class. The comparison between 505 binaries and 1152 parallax stars from Adams's catalogue in Mt Wilson Contr 199 and from

Mt Wilson Contr, No. 226 (1922), Ap J 55, p. 165 (1922).

Kapteyn's investigation of the parallaxes of the helium stars gave the following table

Median		В			A			Г		G5-	-K5	(,	K
apparent magnitude	B	J&F Pi	K&A Pi	BS	J&r Pl	K & A	B	J&b Pi	K&A Pi	B	J&F Pi	K&A Pi	k & A Pl
3,5	0,1			0,1			0,4			1			
4,5	0,2	7	34	0,2	3	17	0,3	3	12	3	3	3	0,4
5, 5	0,2	2	13	0,6	2	4	0,3	2	6	0,8	2	4	1,5
6,5	1,0	1,0	1,0	1,0	1,0	1.0	1,0	1,0	1,0	1,0	1,0	1,0	1,0
7,5	000	0,52	0,00	1,6	0,29	0,18	1,5	0,38	0.25	2,2	0,80	0,33	0,46
8,5	00	0,08	0,00	1,5	0.04	0,03	1,8	0,10	0,05	3,5	0.54	0,08	0,34
9,5	-	0,00	0,00	0,2	0,00	0,02	0,7	0,01	0,01	0,5	0,02	0,02	0,12
B	binai		J &		JACK	son &	FURN	ER	K & A		APTEY	N & A1	MM5
S 8	ingle	stars	, F	1	I	PICKE	RING	,	Pı		Pici	KERING	

If the selection for the two lists were the same, the ratios of the corresponding numbers would not vary with magnitude, and if the selection were homogeneous the ratios for the different classes would show the same change

The number of A stars in the spectrographic list then available was small, and in order to obtain a test Seares used the star counts of W II Picki RING<sup>2</sup>.

The degree of homogeneity is satisfactory and the only deviations of a serious nature are those of the faint G5—K5 stars and the faint B stars. The absence of pronounced irregularities in the curve  $M_d = f$  (Sp Class) shows that the error in the corresponding  $\overline{AM_d}$  must be small. The limitation in this value for called B stars, on account of the fact that Kapteyn's investigations do not include stars fainter than  $6^m$ ,0, will not be of much consequence

The increment  $\delta M$  determines the zero-point, which can easily be proved. Sharks has used the spectrographic parallaxes alone, since they are based on a homogeneous system

A diagram given in fig 450 was constructed giving  $\overline{M}_s$  and  $\overline{M}_d$  as functions of the spectral class. The table shows the value of the zero-point for different spectral classes, the two lists of Jackson and Furner being treated separately:

Spectral class	$M_b-M_d$	d Ma	8 M	78	Spectral class	$\overline{M_b-M_d}$	4 Ma	37.1	n
A7 F2 F5 G0 G4 K2 K8	-0 <sup>31</sup> ,7 -0,6 -0,1 0,0 +0,4 +0,4 +0,5	-0 <sup>4</sup> ,5 -0,2 0,0 +0,4 +0,6 +0,7 +0,8	-0 <sup>1</sup> ,2 -0,4 -0,1 -0,4 -0,2 -0,3 -0,3	3 14 13 18 10 7	A9 F5 G0 K3	-0 <sup>1</sup> ,8 0,0 +0,3 +0,3	-0 <sup>11</sup> ,4 0,0 +0,4 +0,8	-0 <sup>M</sup> ,4 0 ,0 -0 ,1 -0 ,5	11 7 9
Mean			-0 ,29	69		1		-0 ,27	36

From 69 and 36 stars respectively mean values of  $\delta M = -0^{\rm M}$ ,29 and  $-0^{\rm M}$ ,27 were found, thus as a mean  $\overline{\Delta M} = \overline{\Delta M}_{\rm s} - 0^{\rm M}$ .3

was adopted The fact that there is no marked progression in the values of  $\delta M$  with spectral class confirms the conclusion concerning the homogeneity of the selection.

In the determination of the zero-point a certain systematic difference was found between the results of Jackson and Furner with regard to  $\pi_d$  as determined

Mt Wilson Contr, No 82, 147, Ap J 40, p 43 (1914), 47, p 146, 255 (1918)
 Publ A S P 33, p 140 (1921)

from known elements or from arcs of relative motion. In the former case the agreement between  $\overline{\pi}_s$  and  $\overline{\pi}_d$  was excellent. In the second case the following systematic difference was found

$$\overline{\pi}_s = \overline{\pi}_t \sim 0^{\circ}.010$$

The stars occurring in both lists give  $\overline{\pi}_i = \overline{\pi}_i - 0''.007$ .

The value  $\overline{AM}$ , determines the rate  $\Delta M/AS$ , where AS is the change in spectral index S, while the constant  $\partial M$  determines the zero-point. For the determination of  $\partial M$  only spectrographic parallaxes have been used In computing  $M_* - M_d$  it has to be borne in mind that the  $M_*$  correspond to the most probable values of the parallaxes and thus are not the most probable values of the magnitudes themselves. Thus a small correction of  $+0^M,08$  to the

tabular values was adopted.

The following geometrical mean masses were derived:

Spectral class	H,	M.	Visual binaries IR	Single stars
BO B5 A0 A5 F0 F5 G0 G5 K0 K5	- 1,60 - 0,70 + 0,70 2,40 3,32 4,35 5,90 7,80 + 9,80	(-0.25) +1.00 1.65 2.15 2.70 3.27 3.95 4.60 5.20 6.30 8,95	18 © 14 10.5 6,9 4,4 2,7 1,7 1,3 1,2 1,1	10 © 8,3 6,0 4,0 2,5 1,5 1,0 0,76 0,68 0,62 0,59

In order to test the influence of selection on the values of ER on account of the lack of more distant stars the following comparison was made:

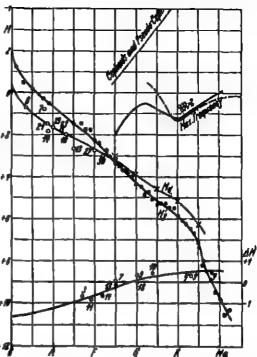


Fig. 150. SEARRS's determination of the masses of the stars from the different stants of the stars in the Russell diagram. The curve M, is the line of maximum frequency of M for the B stars of KAFTEYN and the dwarfs from the list of spectroscopic parallaxes. M<sub>d</sub> is the similar curve for the absolute magnitudes as based upon the dynamical parallaxes derived by Jackson and Furner. The differences in the ordinates, corrected for zero point, are shown by the curve below (AM). The straight line "Copheids and Pasudo-Coph." Is the absolute magnitude spectral relation according to Reduce The difference in the ordination of the line of maximum frequency for giants and the full drawn curve the mass line M = 2.

Ìř	Šþ	4) 0 1	я	a.	57	d lag (t)	
0",018 0 ,026 0 ,032 0 ,046	F2 F6 G1 F7	-0,08 -0,12 -0,08 +0,03	10 10 10	0",061 0 ,102 0 ,270	G3 G1 G8	-0,04 +0,04 +0,12	10 10 9

The slight systematization of the numbers shows that the mean masses of more distant stars have been computed too large. This suggests that the variation of  $\mathbb R$  with spectral class has been influenced by selection, and in order to make the data fully representative a constant correction to the log  $\mathbb R$  of -0.08 has to be applied. The values given above contain this correction.

In deriving the geometrical mean masses  $\mathcal{M}$  of single stars a constant value of  $\mathfrak{M}_R/\mathfrak{M}_A = 0.75$  was assumed.

The probable dispersion in the mass for dwarfs of F0 to M was determined as:

$$\sigma_{\log NR} = \pm 0.22$$
.

This is not the true dispersion, but includes the errors in M and  $M_d$  as well. The dispersion in M is not well known and thus only the following dependence can be indicated:

1Ko	o log M	Limits for probable ercor	σμ	g log M	Limits for probable error
士0 <sup>M</sup> ,35 0 ,30 0 ,25	士0,07 0,13 0,16	(0,85-1,18) M (0,74-1,35) M (0,69-1,45) M	0.15	±0,18 0,20	(0,66-1,51) W (0,63-1,58) W

If the kinetic theory of gases can be applied to the stars, this implies the equipartition of energy of translation so that:

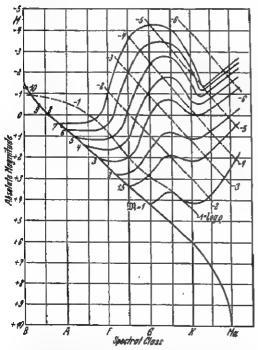


Fig. 151. Nomogram showing distribution of mass (full curves) and mean density (broken curves) of stars derived by Seares from the principle of equipartition. The full-drawn curve running downward to the right is the line of the maximum frequency of the dwarfs or the main series.

$$\mathfrak{M}_n \overline{V_n^i} = \text{const.}$$

The theory for a collection of stars is much simpler than for a gas, because encounters and collisions occur so seldom that they may be neglected. The effective agency for the transfer of energy is only that which arises from the attraction of the bulk of stars upon individual members of the system. The effect of this simplification is an enormous increase in the time of relaxation and for that reason several theorists have rejected the analogy between the stellar system and a collection of gases. On the other hand, JEANS concurs with the application of the theory of gases to the stellar universe.

Several objections are considered by Seares, who finds that equipartition has not been obtained within the stellar system, but that there may be an approach to that state.

The distribution of the logarithms of the space velocities can be represented by means of a normal (Gaussian) distribution. By applying the mean value theory to the frequency function it is found that

$$\log \overline{V^{\scriptscriptstyle B}} = 2 \log \overline{V} + 0.148 = 2 \log V + 0.296.$$

Further, as has been shown by CAMPBELL, the mean space velocity is equal to twice the mean radial velocity. On determining  $\log (\mathfrak{M}V^2)$  for different spectral

classes remarkable constancy was found. The total range of the values is only from 3,21 to 3,66 and most values are very close to the mean, 3,57. It thus seems justifiable to evaluate the masses. For spectral classes F5, G5, K3, and Ma a mass-luminosity relation was found as follows.

The surface brightness was derived by the aid of STRFAN's law. The following expression was derived for the surface brightness

$$f = M_{\text{Vis}} - M_{\text{Bol}} - 10 \log T_{\bullet} + \text{const.}$$

This formula was tested by comparison with the one derived by Hertzsprung in 1906 which was based on Planck's law and the measurements of visual sensibility by Langley,

Speciral class	<b>9</b> R				
H	FS	(+5	КЗ	Ma	
-3 1 1 +2 3 4 5 6 7 8	6,0 © 5,5 4,8 4,2 3,2 2,0 1,0 0,6	5.5 © 4.2 3.2 2.4 1.9 1.5 1.1 0.9 0.8 0.6	5,3 O 2,8 1,9 1,5 1,2 1,0 0,9 0,8 0,7 0,6	9,5 © 4,4 2,6 1,7 1,2	
10			4,4	0,5	

ABNEY, and others. The formulae involve quadratures. The excellent agreement is illustrated here

T	Myn-Mad	BRARES.	/RESTRICTED	T	Myls-Mad	Heaves	/ HERTELPHIAN
2540° 3000 3600 4500 6000	+2 <sup>M</sup> ,59 +1 ,71 +0 ,95 +0 ,35 0 ,00	+6=,32 +4 ,72 +3 ,17 +1 ,60 0 ,00	+6 <sup>10</sup> ,32 +4 ,68 +3 ,16 +1 ,58 0 ,00	7500° 9000 10500 12000	+0 <sup>M</sup> ,02 +0 ,12 +0 ,31 +0 ,53	-0 <sup>to</sup> ,95 -1 ,64 -2 ,12 -2 ,48	-0",93 -1 ,62 -2 ,09 -2 ,45

The connection of these results with the spectral classes was obtained by the aid of the spectral-photometric measurements of Wilsing giving of of 199 stars, mainly giants. In order to include dwarfs use was made of the un-

published colour indices determined by SEARES which should be regarded as provisional<sup>2</sup> but which take account of the important difference in colour between giants and dwarfs. This difference must be considered in any discussion of the surface brightness of stars of "late" spectral classes,

The change A<sub>1</sub>/ΔM could not be determined with accuracy and some extrapolation was necessary. A partial con-

Poted Publ No. 74 (1919)
 Mt Wilson Comm 59, Wash
 Nat Ac Proc 5, p 232 (1919)

Spectral	Giania	Qi <u>ania, 24</u> ==0		Dwarfs			
- class	4/2	1 7	o <sub>o</sub> /T		AL		
Bo B5 A0 A5 F0 F5 G0 G5 K0 K5 Ma Mb	1,36 1,43 1,55 1,76 2,04 2,35 2,70 3,10 3,70 4,37 4,65 4,82 4,94	-2°,28 -2,14 -1,89 -1,45 -0,88 -0,26 +0,44 +1,24 +2,41 +3,71 +4,25 +4,81	2,35 2,48 2,60 2,93 3,47 4,30	-0*,26 0,00 +0,25 +0,90 +1,96 +3,58	+3*,3 +4 ,4 +5 ,2 +5 ,1 +7 ,1 +9 ,8		

Olijeri,	ar Oxlonia	er Dootin	a Sonepii
Bpactral class  M	Ma — 2 <sup>M</sup> ,6 +4 ,6 +4 ,4 252 ① 235 ② 8 ②	HO +0H,1 +2,2 +2,4 250 270 30	Map -4 <sup>1</sup> / <sub>2</sub> 2 +4 ',5 +4 ',5 506 O 513 O 15 Q

trol of j was afforded by measurements of the diameter of three stars as performed by Pease

The following formulae given by Seares connect the angular diameter d, the linear diameter D, the mass  $\mathfrak{M}$ , the density  $\varrho$ , the surface brightness  $\eta$ , and the apparent and absolute magnitudes

The values of the masses and densities were also revised by means of Cepheids. If the pulsation theory is correct the mean density will vary inversely as the square of the period

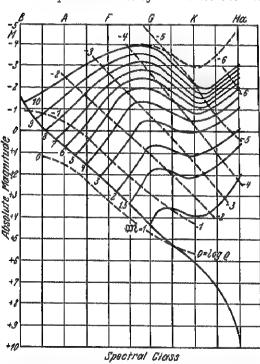


Fig 152 Nomogramaccolding to Seares showing distribution of mass and mean density revised with the aid of Cepheids. The dotted curve at the top indicates the reduction to bolometric absolute magnitude for stars of spectral class F8—Ma of  $\mathfrak{M}=10$   $\mathfrak{O}$ 

$$\log \rho = -2\log P + \text{const.}$$

Further the period-luminosity relation taken as.  $M = a - b \log P$ , where a and b are constants, determines the absolute magnitude. Thus the next last equation can be written.

$$\log \mathfrak{M} = -2 \log P - 0.6(M - 1) + \text{const.}$$

Only small corrections to the data gained from other evidence were obtained from the 28 Cepherds for which the mass could be computed.

The decrease in mass may be partly or perhaps wholly accounted for by selection, but the possibility that mass may decrease with loss of energy by radiation is also suggested, a possibility which agrees with the theory of relativity and is not necessarily in conflict with Newton's mechanical principles.

Immediately after the work of Seares was published H. N. Russell pointed out that the spectrographic parallaxes ought to be dependent on the mass, and that thus by their very nature they are not very suitable for a determination of the dispersion in stellar mass. The

spectrographic magnitude  $M_s$  is a function of the temperature T and the density  $\varrho$ . The equation giving the density is easily transformed into

$$\log \mathfrak{M}_s = \log \varrho + 0.6j - 0.6/(j, \varrho) + \text{const.}$$

The masses  $\mathfrak{M}_{\mathfrak{g}}$  are identical for stars with the same density and the same surface brightness, but the real masses may differ. Thus the masses computed by Seares should not be adopted in order to obtain the real dispersion in  $\mathfrak{M}$  and Russell suggests the use of trigonometric parallaxes for such a determination.

Ap J 55, p. 238 (1922), Mt Wilson Contr 226

The present writer found in 1924 the following results, which remain to-day (1929) substantially unchanged.

Trigonometric parallaxes . ±3,4 O
Spectrographic parallaxes . ±3,0 O
Spectral proper-motion parallaxes . ±4,0 O

222. Stellar Masses from Spectrographic Parallaxes. In an extensive paper dealing with the ionization in stellar atmospheres A Pannekoek took up the question of a possible dependence between the intensities of the absolute magnitude lines and the masses. The Mount Wilson spectrographic determinations of parallaxes are founded on the relative intensity of some enhanced lines and some are lines of the stars. The relative intensities of are lines and enhanced lines of a certain element are wholly determined as far as their dependency on the degree of ionization is concerned by the relative position in the pressure-temperature-diagram of the ionization curve and the atmospheric curve, defined by

$$\log \dot{p} \approx -10^{n-\tau} + 2.5\tau - 6.49,$$
  
$$\tau - \tau_1 \approx /\left(\log \dot{p} - \log \frac{g}{h}\right)$$

where  $\phi$  is the pressure of the ionized gas,  $\tau$  the logarithm of the absolute temperature, and  $\varkappa$  a parameter depending on the ionization potential of the element.

The position of the atmospheric curve depends on the effective temperature T and the factor g/k. Stars of the same effective temperature, i. e of the same spectral class, will show differences depending on the factor g/k. On account of the lack of data the coefficient of mass-absorption k has to be assumed to be constant. Further  $g = f \Re / R^n$  and  $L = 4n_n \sigma R^n$ , where  $\sigma$  is the surface brightness of a star. Then:  $g \approx \sigma \Re / L$ .

The reduction curves used at Mount Wilson have been adjusted by means of directly measured parallaxes for each separate spectral class. The real quantity measured at Mount Wilson is not L but  $L\mathfrak{M}_0/\mathfrak{M}$ , if  $\mathfrak{M}_0$  is the mean mass for the spectral interval considered.

In order to test the theory use was made of dynamical parallaxes. We then

have the relations.  $\mathbb{R}_{dyn} = 2 \left(\frac{\pi_d}{\pi_0}\right)^3$ ;  $\mathbb{R}_{rp} = \left(\frac{\pi_{rp}}{\pi_{tr}}\right)^3 \mathbb{R}_0$ .

As is evident from the following summary there seems to be a correlation between the two sets of masses:

log sa—log sty	log frig	log Widya	log Map	=
+0,53	+0,53	+1,59	+1,06	5
+0,14	+0,10	+0.42	+0,32	6
+0.06	+0,13	4-0,18	1-0,26	9
-0.04	+0.06	-0.12	+0,12	a á
-0,09	-0,05	-0.27	-0,10	7
-0.17	-0,12	-0.51	-0,24	7
-0,23	-0,25	-0.69	-0,50	4
-0,44	-0,47	-1,29	-0,94	4

From the double stars the following table was obtained:

MY-H'	log We p	76	Ma-lis		*
-0 <sup>M</sup> ,3	0,09	10	-1*,3	0,26	10
-0 ,8	0,18		-2 ,9	0,36	9

<sup>&</sup>lt;sup>1</sup> BAN 1, p 107 (1922), Obs 46, p. 304 (1923).

Predictions of the masses were made for a number of stars. The result, namely that the Cepheids should have small masses, and that the companions of the three pairs,  $\alpha$  Herculis (3<sup>m</sup>,5; 5<sup>m</sup>,4; Mb, F9), Bu 8144 (6,5, 8,6, K2, F0), and  $\gamma$  Delphini (4<sup>m</sup>,5, 5<sup>m</sup>,5; K1, F6), have a greater mass (13, 3 and 5 times greater) than the absolutely much brighter principal star of redder colour is of general interest.

Later on P. Doig¹ compared the theory of Pannekoek with the evidence from binary stars. The following fourfold table in which  $\pi_{\text{spectral}}$  denotes the parallax derived on basis of the mean value  $\overline{M}$  of the absolute magnitude of different spectral classes is of interest.

 $\pi_{ ext{spectral}}$   $\pi_{ ext$ 

This indicates the existence of a pronounced positive correlation between  $\pi_{\text{spectral}}$  and  $\pi_{\text{spectral}}$ . When this happens the stars in question are more luminous than the normal star of their class and thus also more massive

The masses of 19 stars derived directly when compared with those computed according to Pannekoek's formula did show rather good agreement. On the other hand, the present writer<sup>2</sup> found at the same time that there were no such systematic differences between the masses computed on the basis of frigonometric, spectrographic and spectral proper-motion parallaxes as were demanded by the theory of Pannekoek but it has to be added that we have to wait for more extensive data before any safe statements can be presented

Further investigations, which cannot be reviewed in detail here, have convinced me that there are no such deviations between masses derived from trigonometric and spectrographic and proper-motion parallaxes as make it possible to determine even mean mass values from an analysis of different parallaxes. This does not exclude, of course, the possibility that there is a mass effect in the spectrographic parallaxes. It is only to be regretted that this effect is evidently so small that it will require much work on the refinement of the trigonometric and spectrographic methods of determining the absolute magnitude before we can derive masses for single stars.

Another way of showing the smallness of the mass-factor in spectrographic parallaxes is to use the relation

$$\Delta M = \Delta m$$

This relation does only hold good when no errors in m and M are present. In case of each quantity having mean errors of  $\varepsilon_M$  and  $\varepsilon_m$ , respectively, we can write  $\Delta M \pm \varepsilon_M = \Delta m \pm \varepsilon_m$ 

Even reasonable treatment of the data concerning spectroscopic binaries in the Mount Wilson material will lead to errors in M of the same size as those derived from single stars. If we had a mass-factor the equation would be

$$\Delta M + a' \pm \varepsilon_M + f(bM + cM^2) = \Delta m \pm \varepsilon_m$$

if  $\log \mathfrak{M}$  is supposed to be  $= a + bM + cM^2$ . Although the material is small it seems that no appreciable mass-factor can be derived

223. Masses of F-K Stars. Gerasimovič<sup>3</sup> has determined the masses of the stars of spectral classes F-K, starting from the following assumptions 1 the reversing layer of a star is in radiative and hydrostatic equilibrium. The absorp-

JBAA 34, p 144 (1924)
 VJS 59, p 203 (1924)
 AN 227, p 145 (1926), Charkov Obs Publ, No 1, p 12 (1927)

tion lines that determine M are not of a chromospheric character, i. a they arise in the level where the selective radiation pressure is small in comparison to the gas pressure, 2 each line arises at the same optical depths in the reversing layers of all stars of the same spectral type. If these hypotheses are correct the intensity of a given spectral line is a function of the effective temperature and the gravity at the surface only. The chief cause of a variation in an intensity-ratio must be a change in the gravity. The following equation can be established:

$$M-2.5 \log \Re I = \varphi(M_a, T_a) = M_a + f(M_a, T_a)$$

where J is the surface brightness and  $T_s$  the effective temperature and the subscript s stands for spectrographic data. It follows from the above equation that:  $\overline{I(M_s,T_s)} = -2.5 \log \Re T.$ 

On account of the lack of data the direct method cannot be applied and we must proceed by successive approximations. At first it is supposed that

$$\log \mathfrak{D} = 0.4 [M - M_s] - \log J + \overline{\log \mathfrak{D} J}.$$

From an analysis of the Victoria list of spectrographic parallaxes the following abbreviated results were found when the differences between the spectrographic and trigonometric magnitudes were grouped according to the magnitude:

These values are only approximate on account of my condensation of the data.

The systematic course of  $M_s - M_{tr}$  is very striking and according to GERASI-

Abudate	P vien		Ci otas	G stars		X stars	
magnitude Ms—Mir = #		Me-Mu	16	Ma-Mu	8		
<0,0-0,9 1,0-2,9 3,0-3,9 4,0-4,9 5,0-5,9	+0 ,1	6 26 40 28 13	+1 <sup>M</sup> ,0 -0 ,6 -0 ,3 +0 ,1 -0 ,6	30 29 19 28 20	10 <sup>M</sup> .7 0.0 1.1 1.1 -0.3	26 18 13 10 14	

MOVIČ cannot be explained as a consequence of some systematic error in the trigonometric parallexes. The same phenomenon as is illustrated above has been noted by van Rhijn<sup>1</sup>, who made a comparison between the Mount Wilson  $M_t$  and  $M_{tr}$  based on the Groningen determinations of  $\bar{\pi}$  as a function of proper motion and apparent magnitude. Van Rhijn explains the phenomenon by the lack of sensitiveness of the spectrographic criteria for luminous stars. From the fact that the systematisation in question also exists among the dwarfs Gerasinovič concludes that we cannot neglect the influence of stellar masses on the spectrographic parallexes.

The largest uncertainty involved in the method is the determination of  $T_{\epsilon}$ . The author made use of the values of the surface intensity given by SEARES which are based on the data of Potsdam and Mount Wilson observers. In this way the

following results were found:

-	G stern					
	iog O)	M	#	Joy Wt	Ħ	16
0",010-0",020 0,021-0,030 0,031-0,060 000, 0-100, 0 001, 0	+0,558 +0,034 -0,101 -0,230 -0,383	+0 <sup>1</sup> ,3 +1 ,6 +3 ,0 +4 ,3 +5 ,3	20 24 43 24 18	+0,424 -0,023 -0,421 -0,476 -0,377	+0 <sup>14</sup> ,4 +1 ,3 +1 ,9 +4 ,9 +6 ,5	26 14 17 10 14

 $\log \mathbb{R}$  clearly depends on the value of  $\sigma$  and the same dependence also exists in the  $\Gamma$  stars. The dependence is partly caused by the well-known selection of

<sup>&</sup>lt;sup>1</sup> Gron Publ, No. 34, p. 60 (1923).

<sup>&</sup>lt;sup>a</sup> Ap J 55, p 198 (1922)

stars in all parallax-piogramms and partly by a general dependence between M and  $\mathfrak{M}$ . A special investigation of the F stars proved that there is no dependence between  $\pi$  and  $\mathfrak{M}$  inside this spectral class.

Using 15 stars with known masses among the Victoria objects Gerasimovič

found the following relation

$$\mathfrak{M}_{\rm calc} = 0.80 \, \mathfrak{M}_{\rm obs}$$

The author points out that the conclusion of Pannekoek that the Cepheids probably have a very small mass cannot be maintained because the method it depends upon only gives the effective gravity, i.e. the gravity diminished by radiation pressure.

Further on an examination is made with regard to whether the principle of the equipartition of the energy holds good  $\widetilde{\mathfrak{M}V^2}$  was computed as follows. At first the space velocity  $V_1$  of a star relatively to the Sun was computed. If  $V_0$  is the velocity of the Sun relatively to the centroid of the stars and K expresses the systematic correction in the radial velocities to be applied to stars of a given spectral class, then

 $\overline{\mathfrak{M} V^2} = \overline{\mathfrak{M} V_1^2} - \overline{\mathfrak{M}} (V_0^2 + K).$ 

For  $V_0$  the value of W W CAMPELL (20 km/sec) was adopted From his earlier work Gerasimovic adopted K=+3.4 km/sec and +3.0 km/sec for F dwarfs and G grants respectively For other groups K=0 was assumed The following results are found

The weighted mean is 3,50, which may be compared with Seares's value 3,57. The good agreement is a fact that speaks strongly in favour of the correctness of the method. The considerable dispersion in  $\log \mathfrak{M}V^2$  prevents that quantity being treated as constant for each star.

A detailed investigation of the probable errors of the calculated masses was next undertaken. The following orders of magnitude of the probable error were found:

が Prob error 0'',010 ±2,5 駅 0 ,050 ±0,52 駅 0 ,100 ±0,29 駅 0 ,200 ±0,19 駅

Thus the mass of a giant stai cannot claim individual accuracy, but when the parallax exceeds 0",070 the mass will possess some degree of individual accuracy. The masses computed by the aid of the Victoria parallaxes were also compared with the values that resulted from the Mount Wilson and Norman Lockyer parallaxes. The agreement of the data for small and moderate masses appears to be very satisfactory. It is not so good for the larger masses, and values of masses larger than 200 are probably illusory. The mean masses were computed according to the following summary

	$M < 3^{11},0$	18	$M \ge 3^{\mathrm{M}}$ ,0	n
F stars G stars K stars	3,3⊙	33	1,5 〇	82
	3,6	55	0,9	70
	4,3	54	1,0	26

Next the mass-luminosity iclation was investigated. The curves for the different spectral classes are somewhat different from the theoretical curve of Eddingion<sup>1</sup>

<sup>&</sup>lt;sup>1</sup> M N 84, p 308 (1924)

This difference cannot be explained by the variation of log IN J, but it can be explained by the assumption of a slight variation of the molecular weight during the evolution of the star.

Also the luminosity-density curve was derived on the basis of BOTTLINGER's photoelectric determinations of the colour indices. A linear relation between log density and absolute magnitude  $M_B$  was found for each spectral class:

Gerasimovič , 
$$\log \varrho = 0.63 \ M_B - 2.17$$
  $\log \varrho = 0.54 \ M_B - 2.52$   $\log \varrho = 0.57 \ M_B - 1.33$   $\log \varrho = 0.57 \ M_B - 2.55$ 

A catalogue of the masses of 71 stars, for which  $\pi > 0''$ ,070, is appended to the paper The mass of Arcturus comes out as 1.60 and that of 61 Count as

2,2 O and 3,5 o respectively.

224. Colour-Mass-Density Relation. G ARETTI investigated in 1922 the masses and densities as derived from the data of double stars. The parallax-data were mainly based on Mount Wilson parallaxes or proper motion parallaxes according to KAPTEYN'S and VAN RHIIN'S formula. The table summarizes the most important of the results'

	Specin	d class	H <sub>A</sub>	Difference in			Despity	
	A	В		colour ladex		Mana		
Giants	K2 G3	F0 17		+0=,80 ± 0=,10 +0 ,22 ± 0 ,13		15 O 14	<0,1 @ <0,1	9
Intermediate	A2 F3 F7	A4 I78 G4	1+2 .5	-0,06±0,04 -0,14±0,07 -0,24±0,09	十1 ,1 ±0 ,4	9 4,4 2,2	0,2 0,3 0,4	14 10 12
Dwaris, , ,	G3 G7 K4	G5 K1 K6	+4 ,8 +5 .7	-0 .07 ± 0 .04	+0 4±0,2 +1,0±0,3 +0,8±0,3	1,5 1,2 1,1	0,5 0,6 0,8	7 7 9

Later on ABETTI has determined the colour indices of the components of 35 double star systems.

ADETTY has also applied the theory of PANNEKOEK for the derivation of atellar masses

225. Vow Zerpel's Method. Up to 1921 the stars in the clusters were considered to have equal masses. This year H YON ZEIPHL published his interesting method which is derived from considerations concerning the distribution of molecules of a gaseous mass enclosed in a sphorical space. The method can be applied to star clusters where a concentration of massive members has taken place around the centre and to star clouds in the Milky Way and it can certainly also be applied to clusters of anagalactic nebulae (galaxies). The problem of deriving the spatial distribution of stars within stellar clusters was at first attacked by E. C. Pickering, who studied the globulars 47 Tucanao,  $\omega$  Centauri and M 13. He proved that the law of apparent distribution of stars, derived from the projected images of the clusters upon photographic plates, was the same for the three objects investigated. He tried to express the law analytically by the formula  $(1-r)^n$ , where r is the distance from centre and s a constant Some years later the problem of finding the spatial distribution from the projected distribution was solved by H. von Zeipel and next year a successful attempt was made by him to apply the results obtained from the dynamical theory of gases to the law of distribution of stars in globular cluster systems.

<sup>&</sup>lt;sup>1</sup> Aco del Lincel Rend 31, 1° Sem, p 359; 2° Sem, p 93 (1922).

Acc del Lincel Rend 33, p. 554 (1924). <sup>4</sup> Harv Ann 26, p 213 (1897). Ann Obs Paris, Méin 25, F (1906).

CR 144, p. 361 (1907)

The idea of treating the distribution of astronomical masses as the distribution of the molecules of mass of gas can be traced back to Lord Kelvin's and G. H. DARWIN's part in the discussion concerning the meteoric hypothesis by Sir N. Lockyer. Later on Lord Kelvin also discussed from the point of view of dynamical theory of gas the distribution of stars in our stellar system in relation to its age. Poincarés suggested in 1906 investigations based on the analogies between stellar systems and masses of gases and emphasized the great possibilities for extending our knowledge as to the construction of the Milky Way system. He also pointed out the difference between stellar systems and masses of gas. In the second case the mean free path is small when compared with the dimensions of the molecules but in the first case the mean free path is large in comparison with the dimensions of the stars. In the stellar system a very long time must elapse before a stage of equilibrium is reached and Poin-CARÉ assumed the Milky Way system to have not reached this stage as yet. In the globular clusters the influence of one star on the other is more pronounced and Poincaré suggested that the distribution of stars in clusters obeys the same law as that expressing the distribution of molecules in a mass of gas only subject to its own gravitational force.

The first step in the development of the theory is to compute a spherical distribution from knowledge of a circular one<sup>4</sup>. The photographs give us the number of stars  $\angle (r)$  per unit of area at the distance r from the centre. These apparent densities must be transformed into space densities D(r). If r is the projected distance,  $\varrho$  the radius vector, and  $l = \sqrt{\varrho^2 - r^2}$ , von Zeipel<sup>5</sup> derives the equation:

$$\Delta(r) = 2 \int_{0}^{\sqrt{R^{2}-r^{2}}} D(\varrho) dl,$$

where R is the limiting distance from the centre of the cluster. In order to eliminate dl this relation can also be written:

$$\Delta(r) = 2 \int_{r}^{R} \frac{D(\varrho) \varrho d\varrho}{V \varrho^{3} - r^{3}}.$$

Integrating by parts we have:

$$\Delta(r) = 2D(R)\sqrt{R^2 - r^2} - 2\int_{r}^{R} \sqrt{\varrho^2 - r^2}D'(\varrho)\,d\varrho.$$

This equation is differentiated:

$$\Delta'(r) = -2D(R)\frac{r}{\sqrt{R^2-r^2}} + 2r\int_{-\pi}^{R} \frac{D'(\varrho)\,d\varrho}{\sqrt{\varrho^2-r^2}}.$$

Further we multiply with  $\frac{dr}{\sqrt{r^2-r_1^2}}$ , where  $r_1 < R$ , and then the integration between  $r_1$  and R is performed. Then we obtain:

$$\int_{r_1}^{R} \frac{d^r(r) \, dr}{\sqrt{r^2 - r_1^2}} = -D(r) \int_{r_1}^{R} \frac{2r \, dr}{\sqrt{(R^2 - r^2)(r^2 - r_1^2)}} + 2 \int_{r_1}^{R} \frac{r \, dr}{\sqrt{r^2 - r_1^2}} \int_{r_1}^{R} \frac{D'(\varrho) \, d\varrho}{\sqrt{\varrho^2 - r^2}} \, .$$

<sup>&</sup>lt;sup>1</sup> London Phil Trans 180 A, p. 1 (1889).

<sup>2</sup> Phil Mag 6th Ser. 2, p. 161 (1901).

<sup>&</sup>lt;sup>6</sup> BSAF 25, p. 153 (1906).

<sup>6</sup> K Svenska Vet Akad Handl 61, No. 15, p. 109 (1921).

The order of integration is changed in the second integral

$$2\int_{0}^{R}D'(\varrho)\,d\varrho\int_{0}^{\varrho}\sqrt{(\varrho^{4}-r^{4})(r^{4}-r^{4})}$$

Further it is found that

$$\int\limits_{0}^{\theta} \frac{2r\,dr}{\sqrt{(q^k-r^k)(r^k-r^k)}} = \pi_0\,,$$

Hence.

$$\int_{0}^{R} \frac{d'(r) dr}{\sqrt{r^{2}-r_{1}^{2}}} = -\pi_{0}D(r) + \pi_{0}\int_{0}^{R}D'(Q) dQ = -\pi_{0}D(r_{1}).$$

Instead of  $r_1$ , r is used and instead of r,  $\varrho$  Then:

$$D(r) = -\pi_0^{-1} \int_{-r}^{R} \frac{\Delta'(p) \, dp}{\sqrt[3]{e^{2r} - r^{2r}}} = -\pi_0^{-1} \int_{-r}^{A'} \frac{\Delta'(\sqrt[3]{r^2 + r^2})}{\sqrt[3]{r^2 + r^2}} \, dl.$$

Next, you ZEIFEL makes the substitution:

$$p(r) = -\frac{1}{r} \frac{d d(r)}{dr}$$

which gives:

$$D(r) = \pi_0^{-1} \int_0^{\sqrt{p} - r^2} \dot{p} \left( \sqrt{p} + r^2 \right) dl.$$

The star counts give  $\Delta(r) + \Delta_0$ , where  $\Delta_0$  can be presumed to be a constant value due to the foreground and background stars. As can easily be shown, this effect will be eliminated,

The value of  $\dot{p}(r)$  could be computed by the formulae for numerical differentiation, but as according to the above definition of  $\dot{p}(r)$  it is not valid for small values of  $\tau$ , the following expansion into series will be used:

$$p(r) = \frac{1}{n_1} \left\{ \frac{1}{288} \left( 28 \, n_1 - 11 \, n_1 + n_2 \right) - \frac{r^4}{1920} \left( 10 \, n_1 - 5 \, n_1 + n_2 \right) \right\},\,$$

where s is the number of stars in the region in question. Finally:

$$D(r) = \frac{\infty}{\sigma_c} \left\{ \sum \rho \left( \sqrt{r^2} w^2 + \overline{r^2} \right) - \frac{1}{2} \rho(r) \right\},$$

where  $\omega$  is an interval of l taken sufficiently small and l=0,1,2... in succession. [The problem of deriving a spherical distribution from a (projected) circular distribution on a plate has been solved more recently from a somewhat different point of view by S. D. Wickelli.]

The dynamical stage of a certain stellar agglomeration at the moment is expressed by the correlation surface of the 7th order:

$$\varphi(x, y, x, k, y, k, \mathfrak{M}, t) dx dy dx dk dy dk d \mathfrak{M}$$
,

where x, y, z are the coordinates and x, y, z the velocities. By applying a method of Gibbs it can be shown that the most probable state is expressed by:

$$\varphi = f(\mathfrak{M}) = -h \mathfrak{M} (\dot{x}^2 + y^2 + x^2 - 2F(y)),$$

I Lund Medd Sar I, No 104 (1924).

where V(r) is the potential of the group and r the distance from the centre Further  $f(r, \mathfrak{M}) \, dx \, dy \, dz \, d\mathfrak{M}$  is the frequency of stars of mass  $\mathfrak{M}$  and of coordinates r, y, z. Then

$$f(r,\mathfrak{M}) = \iiint_{-\infty}^{+\infty} \varphi \, dx \, dy \, dz$$

and according to the last equation but one which expresses the Maxwellian distribution

$$f(r,\mathfrak{M}) = \beta(\mathfrak{M}) e^{2h\mathfrak{M}V(r)} = \gamma(\mathfrak{M}) [/(r,1)]^{\mathfrak{M}}$$

The function  $\gamma(\mathfrak{M})$  is independent of r and the equation can be written

where the subscript i refers to a certain subgroup,  $C_i$  is a constant independent of r, and  $\mathfrak{M}_i$  is the mass of a certain group or the mass-ratio of the group if one of these is selected as unit. The method thus gives the relative masses and not the absolute ones. The theorem of von Zeiffel thus says that for two sub-groups of stars in a stellar agglomeration there is proportionality between the mass-ratios and the logarithms of the spatial densities. The method cannot, of course, be employed when the objects are too few to permit a decent determination of the spatial densities.

VON ZEIPEL and LINDGREN<sup>1</sup> applied the method to the determination of the mass-ratios in Messier 37

As photographic magnitudes were used in von Zeipel's and Lindgren's work a reduction to bolometric magnitudes proved necessary. Such a reduction was made by A Wallenguist<sup>2</sup>, who obtained the following results

Wallphquist			von	Zeteri & Lind	GREN
$\overline{M}_{\mathrm{bol}}$	8051/905°	n	Alboi	971/971	11
1 <sup>31</sup> ,0 2 ,2 3 ,2 4 ,1	1,60 ± 0,09 1,00 1,23 ± 0,05 (0,85 ± 0,06)	231 312 556 757	1 M, 1 2 , 6 4 , 2	1,76 1,00 0,673 (0,360)	57 795 682

The values of the last group are uncertain, as the colour indices have not been observed directly

A WALLENGUIST<sup>8</sup> has measured the magnitudes of the open clusters M36 by applying the same method as von Zeipel and has also computed the mass-ratios

Maol	9024/908 <sub>3</sub>	n
-0 <sup>11</sup> ,8	1,57 ± 0,09	46
+1 ,8	1,00	130
+3 ,4	0,67	297

These results cannot be considered as accurate as those in the case of Messier 37, on account of the paucity of the stars that build up Messier 36, which makes the derivation of the spatial densities uncertain

A WALLENGUIST has recently applied the method of von Zeipel to the determination of the mass-ratios of special star-groups in Messier 3 The material

<sup>&</sup>lt;sup>1</sup> K Svenska Vet Akad Handl 61, No 45 (1921)

Ark Mat Astr Fys 20 A, No 26 (1928), Upsala Medd 36

<sup>8</sup> K Svenska Vet Akad Handl (3) 4, No. 8 (1928), Upsala Medd 32

<sup>\*</sup> BAN 5, p 67 (1929)

consisted of 848 stars in Shaplky's and Miss Davis's Catalogue<sup>1</sup> The stars were divided into four groups, for which the following results were found

Group	94	W/W.	75	von Attenti's theory	Kommuron's fermula	Mad
Red "hyporgiants" White "hyporgiants" Ordinary red giants White stars	14*,69	1,297 ± 0,031	268	3,88 ()	3,90 @	-0 <sup>1</sup> ,31
	15 ,65	1,000	267	2,99 ()	2,98 O	+0 ,65
	16 ,66	0,898 ± 0,117	197	2,69 ()	2,10 O	+1 ,66
	17 ,09	0,620 ± 0,123	122	1,86 ()	1,86 O	+2 ,09

Mo, the mass of the white "hyperglants", has been selected as unit

In order to reduce the determined mass-ratios into absolute masses the parallax of the cluster must be known. As the most probable value of the parallax  $\pi = 0''$ ,00010 is accepted. This leads to the numbers in the last columns. If SHAPLEY'S value for the M of the cluster type variables had been used the four values of M would have been 5,480, 4,220, 3,790, and 2,620 respectively.

226. The Method of Freundrich and Herranen. Independently of von ZEIFEL, R FERUNDLICH and W. HEISKANEN have developed an analogous method According to Shapley there seems to exist a "galactic" plane in the globular clusters in the sense that only the brightest stars have a spherical distribution, whereas the fainter stars show an elliptical distribution. Let R./R. be the ratio of the total mass of the elliptically distributed stars to the total mass of the spherically distributed stars, and let a and b be the axes of the ellipsolidally distributed stars and s' a measure of the ellipticity of the equipotential surfaces, then:

$$e'\left[1+\frac{3\Omega_a}{3R_a}\left(1+\frac{3}{5}\frac{b^a\lambda^a}{a^a}\right)\right]=\frac{3}{10}\frac{3R_a}{3R_a}\frac{b^a\lambda^a}{a^a},\quad\text{where}\quad\lambda=\frac{a^a-b^a}{b^a}.$$

If the equipotential surfaces cut the equator at the distance s and the polar axis at the distance  $\epsilon$ , then  $\epsilon' = \frac{a}{\epsilon} - 1$ 

According to H. C. Plumber and von Zeifel the density in the cluster increases ~ 7 . Applying the alightly medified formula to Shaplay's material in M13 gives M,/M, :, 0,5 This means that the mass of the spherically distributed stars, which amount to only 0,01 of the total number, should be at least two thirds of the total mass of the cluster. This will make the mean mass of the apherically distributed K and M giants 500 0, which seems incredible starthorn then repented Shapley's star counts on the basis of his star catalogue. and that of LUDENDORFF It was found that there were such individual deviations in the distribution of the different classes of stars that the authors think it is doubtful whether the above formula can be applied. They therefore turned their attention to investigating the relative concentration towards the centre of the different classes and to applying the theory of gases. If q<sub>i</sub> is the number of molecules in unit space of a gas of atomic weight  $\mu_i$ , V the gravitational potential, and h and go certain parameters depending on the temperature and density at the centre, we have the equation

$$m = \varrho_0 \, e^{-2k\mu_0 V}$$
.

<sup>&</sup>lt;sup>2</sup> Z f Phys 14, p. 226 (1923). Mt Wilson Contr No. 176 (1920).

Mt Wilson Contr No. 170 (1920).
 M N 71, p 460 (1911), 76, p 107 (1915).
 If Svenaka Vet Akad Handl 51, No. 5 (1913)
 Potzdam Publ 15, No 50 (1905)

The theory has been applied to the clusters M3 and M13. The colour malaces corresponding to the A and E stars have been taken together to form one groups, those corresponding to G, K, and M stars to form another. Consider two special elements at distances  $r_1$  and  $r_2$  from the centre and attribute the subscripts  $\sim 1$  and  $\sim 1$  to the two spectral groups. Then

$$\begin{split} \underline{m}_{A} &= \frac{\log \varrho_{1}^{1} - \log \varrho_{1}^{3}}{\log \varrho_{K}^{1} - \log \varrho_{A}^{3}}, \\ \varrho_{A}^{1} &= \varrho_{0}^{(A)1} \cdot e^{-2h} \underline{m}_{A} V_{1}, \quad \varrho_{1}^{3} = \varrho_{0}^{(A)3} \cdot e^{-2h} \underline{m}_{A} V_{1}, \\ \varrho_{K}^{1} &= \varrho_{0}^{(K)1} \cdot e^{-2h} \underline{m}_{K} V_{1}, \quad \varrho_{A}^{3} = \varrho_{0}^{(A)3} \cdot e^{-2h} \underline{m}_{K} V_{3}, \end{split}$$

where

From the observed number of stars on the plates the numbers in space we be derived according to you Zeifel's formula. The following results were defined

Distance	Page Val	M3	Distance	MII	M3
from centre		W <i>K/</i> WA	from centre	WA/WI	90A/91
2′ 3′ 4′	1,420 1,135 1,240	1,761 1,865 1,518	5' 6'	1,215 1,190	1,326

227. Martens's Method!. In order to obtain a handy expression of the exhaustion of the potential energy of a stellar cluster Martins assumes that the effects of collisions and passages are negligible when compared with the effect of the gravitation from the cluster. Further it is assumed that the mesh values of kinetic energy per degree of freedom are constant for all degrees a freedom and independent of the coordinates of position. These two assumptions mean in other words the assumption of dynamical equilibrium and equipart toon of energy.

MARTENS then performs a closer examination on basis of JIANS'S WOFF "The Dynamical Theory of Gases", in order to find out if the two assumptions are concordant

The stellar system under consideration consists of n stars having 3n court nates  $q_1 = q_{2n}$ . Instead of the velocities  $dq_i dd_i$ , the variables  $p_i$  are introduced

The life history of the stellar system is represented by a certain curve if the 6n-dimensional space determined by the rectangular coordinates of positival and velocities

Next a great number of stellar systems is considered, so selected that 11 initial values of the 6n quantities  $q_i$  and  $p_i$  are so near each other that the 2n presentative points can be treated as forming a continuous medium. The munits of points per unit of 6n-dimensional volume or the density of this medium is if t is the time, the equation of continuity takes the form

$$\frac{\partial \tau}{\partial t} + \sum_{i=1}^{8n} \left\{ \frac{\partial}{\partial p_i} \left( \tau \frac{d p_i}{d t} \right) + \frac{\partial}{\partial q_i} \left( \tau \frac{d q_i}{d t} \right) \right\} = 0.$$

Combining this equation with the equations of motion and taking  $D\tau$  as representing the increase in  $\tau$  as we follow the group of points in its motion. JEANS<sup>2</sup> has shown that

$$\frac{D\tau}{Dt} = \tau \sum_{i=1}^{8n} \frac{\partial^3 I}{\partial q_i \partial p_i},$$

<sup>&</sup>lt;sup>1</sup> A Research on the Spherical Dynamical Equilibrium-Distribution of Stars Unequal Masses Göteborg 1928 <sup>3</sup> The Dynamical Theory of Gases Fourth Edition Cambridge 1925

where  $\frac{dE}{dt} = -2F$ , E being the total kinetic energy of the system and 2Fbeing a quadratic function of the velocities and giving the rate of dissipation of energy. JEANS has shown that the right member of this equation is always  $\geq 0$ , and only = 0 if F = 0 It then follows as a consequence of collisions between stars that mechanical energy is transformed into heat and that the points representing different initial configurations of the stellar systems are crowded together and that, independently of the initial states, the final states of the stellar systems are the same

It can be shown on basis of J Ohlsson's investigations that the effect of collisions and passages can be fully neglected. Ohrsen thus estimates the time of relaxation measuring the rate at which the Galaxy as an effect of collisions approaches to equilibrium to be of the order of 1001 years. The corresponding time as an effect of passages is found to be of the order of 10th years. These quantities are certainly much smaller in globular and open clusters but still the passages and then a fortiori the collisions have been neglected in MARTENS's

work

Then: F = 0 and  $D\tau/Dt = 0$  (Liouville's theorem)

A part of the stellar system consisting of N stars is then considered. The stars have not equal masses but can be ordered into y groups. The stars N, in each group have the same mass Mr. Honce.

$$\sum_{i=1}^r N_i = N.$$

The stars are assumed to be material points. Every star then possesses three degrees of freedom and its state is determined by 6 quantities:

The space containing the N points is divided into \* equal elements of volume. The state of the stars is then statistically determined by certain quantities au. giving the number of stars of mass M. contained in the 4th element of volume We have then:

 $\sum a_{ij} = N_j.$ (j = 1, 2, ...

Similarly to this distribution, called A by Jeans, there exists another distribution B, determined by the numbers  $b_{ij}$ , and so on. The task is to determine the  $a_{ij}$ in such a way that distribution A becomes the most probably one.

By variation of the last equations above the following a conditions are

found:

found:  $\sum_{i=1}^{n} \delta a_{ij} = 0, \qquad (j = 1, ..., *) \quad (a)$ The  $N_j$  stars can be permutated in  $\frac{N_j!}{a_{ij}! a_{ij}! ... a_{nj}!}$  ways without changing the distribution A. The most probable distribution is the one that makes the volume containing the points of distribution A a maximum This leads to the equations of condition:

$$\sum_{i=1}^{r} \sum_{i=1}^{n} \left[ \log \frac{n a_{ij}}{N_j} + 1 + \frac{1}{2 a_{ij}} \right] \delta a_{ij} = 0.$$
 (b)

Finally using the equation E =constant and taking:

$$\frac{\partial E}{\partial a_{ij}} = a_{ij}$$

<sup>&</sup>lt;sup>1</sup> Lund Medd Ser. II, No. 48 (1927).

and disregarding terms of higher order of  $\delta a_{ij}$  it is found by variation from the energy equation

 $\sum_{i=1}^{1} \sum_{i=1}^{n} \varepsilon_{ij} \, \delta \, \alpha_{ij} = 0 \tag{c}$ 

The set of variation-equations (a) is multiplied by the arbitrary factors  $l_j$  and the last one (c) by a factor m. The expressions are then added to the equation (b). It is then found that the  $a_{ij}$  have to satisfy the equations

$$\log \frac{na_{ij}}{N_j} + 1 + \frac{1}{2a_{ij}} + l_j + me_{ij} = 0$$

The  $a_{ij}$  are supposed to be so great that  $\frac{1}{2a_{ij}}$  can be neglected. Further it is assumed that  $e_{ij}$  is independent of  $a_{ij}$ , although dependent of the other  $a_{ij}$ . The equation is then solved into.

 $a_{11} = \frac{N_1}{n} e^{-(1+l_1)-m\,\varepsilon_{l_1}}$ 

Introduce a function  $\tau_j$  so that  $\tau_j d\phi_{j1} d\phi_{j2} d\phi_{j3} d\phi_{j1} d\phi_{j5} d\phi_{j6}$  gives the number of stars within the limits  $d\phi_{jk}$ , where k=1 6, and whose masses are  $\mathfrak{M}_i$ 

Then  $\tau_1$  is proportional to  $a_{i1}$  and we can write

$$\tau_1 = C_1 e^{-m \, \varepsilon_1},$$

where  $C_1$  is a constant and  $\varepsilon_1$  a smooth function of the values  $\varepsilon_{i\,1}$   $\varepsilon_1$  is assumed to have the form

$$e_1 = \frac{1}{2} \beta_{11} \varphi_{11}^2 + \frac{1}{2} \beta_{12} \varphi_{12}^2 + \frac{1}{2} \beta_{13} \varphi_{13}^2 + \frac{1}{2} (\varphi_{11}, \varphi_{15}, \varphi_{10})$$

Then

$$\tau_1 d\varphi_{11} d\varphi_{12} d\varphi_{13} d\varphi_{14} d\varphi_{15} d\varphi_{16} = C_1 \left( e^{-\frac{1}{4}m\beta_{11}\varphi_{11}^2} d\varphi_{11} \right) ... \left( e^{-m\beta_1} d\varphi_{11} d\varphi_{15} d\varphi_{16} \right).$$

This shows that the distributions of the coordinates are independent of one another

The mean value of the contribution of  $\varphi_{11}$  to the energy 15

$$\frac{1}{2}\beta_{11}\varphi_{11}^2 = \frac{1}{2m}, \text{ and also } \frac{1}{2}\beta_{12}\varphi_{12}^3 = \frac{1}{2}\beta_{13}\varphi_{13}^2 = \frac{1}{2m}$$

It can also be shown that

$$\frac{1}{2} \mathfrak{M}_{j} \left( \frac{dq_{jk}}{d} \right)^{2} = \frac{1}{2m} \qquad (k = 1, 2, 3, j = 1, ..., \nu)$$

which expresses the law of equipartition of energy

The assumption that the  $\varepsilon_{ij}$  are independent of  $a_{ij}$  is then made subject to a special examination on basis of Charlier's<sup>1</sup>, Jeans's<sup>2</sup> and Ohi ston's<sup>3</sup> work and it is found that the assumption is justified when dealing with stellar systems and that equipartition of energy exists in a state of dynamical equilibrium. The author emphasizes the extreme difficulties presenting themselves when a search is made for the mechanism resulting in the equipartition of energy when collisions and passages are neglected. He quotes a postulate formulated by Charlier' "Each population of individuals approaches asymptotically that state which can be proved to possess the greatest probability"

<sup>&</sup>lt;sup>1</sup> Lund Medd Ser II, No 16 (1917)

<sup>&</sup>lt;sup>2</sup> M N 76, p 70, 555 (1915—16), Problems of Cosmogony and Stellar Dynamics Carn bridge 1919

<sup>&</sup>lt;sup>3</sup> Lund Medd Ser II, No 48 (1927) Also Dissertation Lund

<sup>4</sup> Publ ASP 37, p 125 (1925)

MARTENS finds that if the equations which determine the most probable distribution of the positional coordinates are solved, the  $a_{ij}$  will be found to be independent of i, which means that the stars would be uniformly distributed over the whole space. But the task is not to seek for the most probable distribution among all possible eness but for the most probable distribution among those having a certain value of their potential energy. This is proved by applying the theorem of the virial i

If  $q_k$  are the rectilinear coordinates of N stars and  $Q_k$  the components of the acting forces in the same direction the equations of motion will be

$$\Re_k \frac{d^k q_k}{dt^k} = Q_k. \qquad (k = 1, \dots, N)$$

We designate by S the summation over all three directions of coordinates, then  $S \geq \mathbb{R}_k q_k^2$  is the moment of inertia of the system, and, as we are seeking stationary distributions, we write

$$\overline{\frac{d^3}{dt^3}S\sum_{k=1}^M \mathfrak{M}_k q_k^3} = \overline{S\sum_{k=1}^M \mathfrak{M}_k \frac{d^3}{dt^3}q_k^3} = 0,$$

the bar over an expression denoting an average over a long time. The virial  $\vec{V}$  of CLAUSIUS is then found to be:

$$\vec{V} = -\frac{1}{4} S \sum_{b=1}^{K} q_b Q_b.$$

The following deductions are made on the assumption that the system is spherically distributed. The radius of the sphere is called R. It follows from the assumption of a limiting radius that the total gravitational force of all stars outside this sphere is zero. Thus only the forces due to the stars inside the sphere shall be taken into account. On another hand a number of stars will escape from the sphere at a certain moment, but these losses are counterbalanced by outside stars passing into the sphere and as it is assumed that the distribution is stationary, both outside and inside the limiting sphere, the counterbalancing effect appears to be more or less the same as if the outgoing stars met an elastic wall and were reflected by it. Of course, the identity is not kept after the imaginary reflection; it is another star that pursues the broken orbit. The expression of potential energy is not changed except in the immediate neighbourhood of the limiting sphere and this applies also to the law of distribution which is a function of the potential energy. These circumstances overcome the principal difficulties presented by the escaping and invading stars.

If N stars move under the sole influence of their gravitational interactions it follows that a simple relation exists between the virial V and the exhaustion Q of potential energy of the forces, which has the form:

$$Q = \frac{1}{2} \sum_{k=1}^{N} \sum_{l=1}^{N} \kappa \, \mathbf{m}_{k} \, \mathbf{m}_{l} \, \frac{1}{[S(q_{l} - q_{k})^{2}]^{k}}.$$

The apostrophe by the second  $\sum$  sign means that during the summation k = l must be excluded. \*\* is a numerical constant depending on the units used.

<sup>&</sup>lt;sup>1</sup> The virial is the sum of the attractions between all the pairs of particles of a system, each multiplied by the distance between the pair

Comparing the expressions for V and  $\Omega$  it is found in accordance with Eddington<sup>1</sup>

$$V = -\frac{1}{2} S \sum_{k=1}^{N} q_{k} \sum_{l=1}^{N} Q_{k \, l} = \frac{1}{4} \sum_{k=1}^{N} \sum_{l=1}^{N} \kappa \, \mathfrak{M}_{k} \, \mathfrak{M}_{l} \, \frac{1}{[S(q_{l} - q_{k})^{3}]^{\frac{1}{4}}} = \frac{1}{2} \, \Omega$$

Applying the virial-theorem earlier quoted it follows that

$$T - \frac{1}{2}\Omega = 0$$

The equations of motion possess the wellknown integral

$$-\frac{1}{4}h = T - \Omega$$

where h is an arbitrary constant. Thus

$$Q = h$$
 (d)

Next  $\Omega$  will be expressed as a function of the quantities  $a_{ij}$ . The expression for the exhaustion of potential energy can be written:

$$\Omega = \sum_{k=1}^{N} \sum_{l=1}^{k-1} \kappa \, \mathfrak{M}_k \, \mathfrak{M}_l \, \frac{1}{[S(q_l - q_k)^2]^l}$$

if the indices k are chosen in such a manner that  $Sq_k^2 < Sq_{k+1}^2$ . The neglection of irregular forces permits to substitute for the attraction of a number of discrete stars the attraction of a homogeneous sphere having the same mass as the sum of the masses of the discrete stars. The terms expressing the exhaustion of potential energy of attraction on the mass  $\mathfrak{M}_t$ ,  $\mathfrak{R}\mathfrak{M}_t \overset{s-1}{\underset{t=1}{\sum}} \mathfrak{M}_t [S(q_t-q_s)^2]^{-\frac{1}{2}}$  are thus substituted by the expression  $\mathfrak{R}\mathfrak{M}_t [Sq_s^2]^{-\frac{1}{2}} \overset{s-1}{\underset{t=1}{\sum}} \mu_t$ 

In the distribution A determined by the numbers  $a_{ij}$  the stars having the same index i are situated within a spherical shell. The harmonic mean distance of these stars from the centre is  $r_a$ . The stars in the element s contribute to the exhaustion of potential energy by a quantity

$$\varkappa^{\frac{\sum\limits_{j=1}^{s}a_{ij}\,\mathfrak{M}_{j}}{\gamma_{s}}}\sum_{i=1}^{s-1}\sum_{j=1}^{i}a_{ij}\,\mathfrak{M}_{j}$$

and observing (d) we obtain:

$$\Omega = \varkappa \sum_{i=1}^{n} \frac{\sum_{j=1}^{i} a_{ij} \, \mathfrak{M}_{j}}{r_{i}} \sum_{i=1}^{s-1} \sum_{j=1}^{r} a_{ij} \, \mathfrak{M}_{j} = h. \tag{e}$$

The variations  $\delta a_{ij}$  are to be connected by the condition

$$\varkappa \sum_{s=1}^{n} \sum_{j=1}^{\nu} \delta a_{sj} \left\{ \frac{\mathfrak{M}_{j}}{r_{s}} \sum_{i=1}^{s-1} \sum_{j=1}^{\nu} a_{ij} \mathfrak{M}_{j} + \mathfrak{M}_{j} \sum_{i=s+1}^{n-1} \frac{\sum_{j=1}^{\nu} a_{ij} \mathfrak{M}_{j}}{r_{i}} \right\} = 0.$$

Further is

$$\sum_{j=1}^{n} \sum_{s=1}^{n} \delta a_{sj} \left\{ \log \frac{n \, a_{sj}}{N_j} + 1 + \frac{1}{2 \, a_{sj}} \right\} = 0$$

and '

$$\sum_{i=1}^n \delta \, a_{ij} = 0$$

<sup>1</sup> M N 76, p 525 (1916)

The  $a_{ij}$  are then found by using the method of indetermined multiphers Neglecting the term  $1/2a_{ij}$  the following set of equations is found.

$$\log \frac{n \, a_{ij}}{N_j} + 1 + l_j + m \, n \, \mathfrak{M}_j \left( \frac{1}{r_i} \sum_{i=1}^{s-1} \sum_{j=1}^{r} a_{ij} \, \mathfrak{M}_j + \sum_{i=s+1}^{s-1} \frac{\sum_{j=1}^{s} a_{ij} \, \mathfrak{M}_j}{r_i} \right) = 0, \quad (f)$$

where  $l_j$  and m are arbitrary factors. To these  $s \cdot j$  equations are joined the j equations  $\sum_{i=1}^{n} a_{ij} = N_j$  and equation (e) above. We have thus  $s \cdot j + j + 1$  equations to determine the  $s \cdot j + j + 1$  unknown quantities  $a_{ij}$ ,  $l_j$  and m.

The radius of the sphere enclosing the stars in the system considered is R. If W is the volume then the volume of each cell is W/n and  $na_{ni}/W$  gives the density in stars of mass  $\mathfrak{W}_i$  at the distance  $r_i$  from the centre—Further is introduced:

 $f_j(y_i) = \frac{n \, a_{ij}}{W}.$ 

If  $r_{s+1/s}$  is the radius of the spherical surface separating the cell s from the cell s+1 we have.

$$\frac{W}{n} = \int_{r_{a-\frac{1}{2}}} 4\pi_a r^a dr \quad \text{and} \quad a_{aj} = \int_{j} (r_j) \int_{r_{a-\frac{1}{2}}} 4\pi_a r^a dr$$

On considering the quantities  $f_j(r_r)$  as being continuous functions of r and assuming the cells to be thin we may put:

$$\alpha_{ij} = \int\limits_{\tau_{i-\frac{1}{2}}} 4\pi_i \tau^{a} /_{j}(r) d\tau$$

Then the equations (f) are transformed following the same assumption. Applying the Laplacian operator  $\nabla^a$  to the expressions (f) and dropping the index s it is finally found:

$$\nabla^{1}\left[-\frac{1}{m + M_{j}} \log \left(\frac{W}{N_{j}} e^{1+k_{j}} f_{j}(r)\right)\right] = -4\pi_{0} \sum_{k=1}^{p} \Re_{j} f_{j}(r). \qquad (j = 1, \ldots, r)$$

This gives the equation

$$\frac{d^{2} \log f_{j}(r)}{dr^{2}} + \frac{2}{r} \frac{d \log f_{j}(r)}{dr} = 4\pi_{0} m \kappa \sum_{i=1}^{r} \Re f_{i}(r) \qquad (i = 1, ..., r)$$
 (g)

Each one of these equations contains in its left member one of the unknown functions but in its right member all the unknown functions. By considering the equations for the potentials of gravitation it is found that:

$$\frac{1}{m \times \mathfrak{M}_{t}} \left( \log \frac{\mathcal{W}}{N_{t}} e^{1+I_{t}} f_{t}(r) \right) = \frac{1}{m \times \mathfrak{M}_{t}} \left( \log \frac{\mathcal{W}}{N_{f}} e^{1+I_{t}} f_{t}(r) \right)$$

$$\left( \frac{\mathcal{W}}{N_{t}} e^{1+I_{t}} f_{t}(r) \right)^{1/\mathfrak{M}_{t}} = \left( \frac{\mathcal{W}}{N_{t}} e^{1+I_{t}} f_{t}(r) \right)^{1/\mathfrak{M}_{t}},$$
(h)

or:

which are the relations used by von Zeipel and Lindgren.

Introducing '

$$C_{i,j} = \frac{N_i}{W} \left( \frac{W}{N_j} \right)^{\frac{m_i}{m_j}} e^{-(1+i\alpha) + \frac{m_i}{m_j}(1+i\alpha)}$$
$$f_{i,j}(r) \approx C_{i,j} [f_{i,j}(r)]^{\frac{m_i}{m_j}}.$$

we have.

1	٠.	
، [	۵	+0 007 +0 009 +0,011 -0,038
a	log/scalc	8 306—10 8,255 8,143 7,998
4	log f <sub>3 obs</sub>	8,313-10 8,264 8,154 7,960
	٥	++0 013 ++0,013 +0,001 -0,008
3	log facale	8 888 – 10 8,861 8,789 8,692 8,484 8,484
."	log foobs	8,901-10 8,882 8,693 8,693 8,476 8 161
	⊲	1 + + + 1   0.009
in the	logfeste	9,613—10 9,572 9,465 9,321 9,012 8,608
	logfobs	9,604—10 9,581 9,505 9,367 8,993 8,526
	∢	++0,079 +0,079 -0,079 -0,084 -0,034
4	log /1 calc	9,15410 9,082 8,893 8,640 7,383
	log /1 obs	9,233 – 10 9,182 8,972 8,556 7,927
	1087	0,000 0,602 0,602 1,398 1,800

and the differential equation then becomes

$$\frac{d^2 \log f_j(r)}{dr^2} + \frac{2}{r} \frac{d \log f_j(r)}{dr} = 4\pi_o \kappa m \mathfrak{M}_j \sum_{i=1}^{r} \mathfrak{M}_i C_{ij} [f_j(r)]^{\mathfrak{M}_i/\mathfrak{M}_j},$$

where both the membra only contain one of the unknown functions. In order to find all functions of distribution we need only to solve one of the  $\nu$  equations. The other  $\nu \to 1$  functions are then found by aid of the relations (h).

For the application of this theory to a cluster there are required observations on functions of distribution of different groups of stars, classified according to attributes correlated to the masses of the stars. As such observations of globular clusters were not accessible Marrins compared the results of his theory with the distributions in the open cluster M37 (NGC 2099) observed by YON ZEIPL and LINDGREN These authors divided the stars of M 37 according to their magnitudes and colour indices into four groups, p, q, u, w The p-stars were interpreted as g-grants, the q-stars as b- and a-stars, the u-stars as l-dwarfs and the w-stars as g-dwarfs From then observations von ZFI-PEL and LINDGREN have calculated the distributions faobs in space of the four types of stars given in the adjoining table Martens compared these observed distributions with those calculated (freate  $f_{3,ale}$ ) on the supposition that the cluster is in its most probable state

It is obvious from the distribution of the differences A = obs—cale that the value of m determined for different groups would be about the same. This is an indication of equipartition of energy on the different masses. Further the differences show that the stars are more concentrated to the centre of the cluster than is required by the calculated distribution This phenomenon, well-known for distributions in globular clusters, disregarding unequalities of masses of the stars, is usually interpreted as displaying that the clusters are built up in adiabatic equilibrium instead of in isothermic. According to the theory here developed there is, however, another possible explanation. Doubtless there are within the cluster stars that are not lummous enough to be observed. These stars do not influence the observed distributions, but as they contribute to the potential of the cluster they are able to affect the calculated distributions, as has been shown on the preceding pages, in a direction to diminish and perhaps abolish the differences of the table

Among other results found by Mariens the fact may be mentioned that if equipartition has taken place in a stellar cluster then the most probable state of distribution is expressed by the Maxwellian law Such a system has no limitation in space of, in other words, its radius is infinite. If the mass-ratios exceed 3/2 within such a system, the number of the smaller masses must be infinite, whereas the number of the greater masses is finite. It seems that

the adiabatic distribution in globular clusters can be explained by the assumption that within these objects the mass-distribution is the most probable one

228. Recent Work Concerning Masses of Spectroscopic Binaries. It is only four and a half decades since the first discovery of a spectroscopic binary was anounced. At present orbital elements are known for some 250 systems. When both spectra have been observed and also the system is an eclipsing binary. we obtain complete and, in most cases, very accurate knowledge of the components. When the system is not an eclipsing bluary, but both spectra are known, we get the minimum values of the masses, because the orbital determination gives the quantities Masin\* and Masin\* d. Reasonable assumptions concerning the value of sin's can also be made and thus our knowledge of the mean value of M for certain groups of binaries can be considerably advanced

The third case, i.e. when only the spectrum of one of the components is registered, presents several difficulties as far as the determination of the mass is concerned. This case is certainly the most common one. As soon as the components in a double star system differ two magnitudes or more, the chances are vary small that both spectra will appear on the plates. The observations of a spectroscopic binary give in the case of one spectrum the so-called mass-function,  $/=\mathbb{R}_{n}^{2} \sin^{2} (\mathfrak{M}_{A} + \mathfrak{M}_{B})^{-3}$ , which can be written

$$(\mathfrak{M}_A + \mathfrak{M}_B) \sin^6 i = [3,01642 - 10] K_A^6 \left(1 + \frac{\mathfrak{M}_A}{\mathfrak{M}_B}\right)^6 P \left(1 - \sigma^6\right)^{\frac{1}{4}}.$$

where  $K_A$  is the semi-amplitude of the velocity variation for  $\mathfrak{M}_A$  and P the period in days

R G. ATTREN has expressed doubts in his book "The Binary Stars", with regard to whether the mass-function can give any information concerning the masses of the store. Generally the value  $K_A$  or a corresponding expression has been used and then, of course, the range is considerable. It is fair to use  $K_A$  in order to get a quantity that is proportional to the cube root of the mass, because in direct determinations of stellar masses we cannot get more than a fair knowledge of  $(\mathfrak{M}_A + \mathfrak{M}_B)^{\dagger}$  from our best determinations of stellar parallaxes. The use of  $K_A$  has also been recommended by Otro Struve<sup>1</sup> and others.

STRUVE has assumed:

$$R_A = CP^{-\frac{1}{2}},$$

which is justifiable for certain groups of stars. The curve combining P and K corresponds very nearly to the equation  $K = CP^{-\frac{1}{2}}$  for P = 9 years to P = 2.45 days,  $(\log C = 2.0695)$ . LUDENDORFF has reached a number of important conclusions which are given already in clph. 215 of this chapter.

Extensive use of STRUVE's formula has been made by BRER in his paper, "Zur Charakterisierung der spektroskopischen Doppelsterne". This extensive and valuable monograph cannot be reviewed here excepting from the point of view of determination of stellar masses

From 434 objects BEER finds the value  $KP^{\frac{1}{2}}$  = 125,4. He makes use of the above relation for a discussion of the probability of a certain group of stars exhibiting variable radial velocities being binaries (c. g. the Cepheids) and classifies the real binaries according to the characteristics of the P, K-curves.

Ap J 60, p. 167 (1924)
 Barlin-Babaisbarg Veröff V, H 6 (1927)

Bedr has collected 88 pairs showing both spectra, and finds the following frequencies of the values  $(\mathfrak{M}_A + \mathfrak{M}_B) \sin^3 \iota$ 

$(\mathfrak{M}_A + \mathfrak{M}_B) \sin^a i$	5t	(M) (+-101)n) sin³ :	n	$\{\mathfrak{M}_A \mid \mathfrak{M}_B\}$ $\sin^a \imath$	71
>100 (	2	8 -90		3,0-3,50	3
50-100	1	78	2	2,5-3,0	13
40- 50		6 7	i	2,0-2,5	1.1
30 40	3	5 - 6	5	1,5-2,0	1.1
20- 30	.5	4,5 5,0		1,0-1,5	8
10- 20	4	4,0~ 4,5	4	0,5-1,0	Ó
9 10	6	3,5- 4,0	3	<0,5	1

This table seems to lend some support to the theory of Hell RICH<sup>1</sup> assuming the existence of preferential mass values (cf. ciph. 229)

The relation between mass and spectral class is illustrated in the following summary:

Spectral class	4 ania 1 (05	Wasin <sup>a</sup> 1	Range for (MA + Wln) sin* i	23
06-B4 B5-A4 A5-F4 F5-G4 G5-K4	13,180 2,71 1,80 1,01 0,87	10,50 ① 1,73 1,24 0,89 0,68	139 —2,600 26,4 —0,21 13,4 —0,52 3,37—0,87 2,10—1,05	21 30 18 15

In 33 cases the individual masses were known. By assuming  $\sin^3 i = 0.667$  the following mean values were found

Spectral class	$\mathfrak{M}_A + \mathfrak{M}_B$	11	$[\mathfrak{M}_A + \mathfrak{M}_B]$	f)	Adopted mean
O6-B4	17,17 ① 10,15 4,47 2,70 1,42 1,94	9	20,28 ①	10	18,8
B5-B9		4	10,64	5	10,4
A0-A4		7	3,53	14	3,8
A5-F4		4	3,00	12	2,9
F5-G4		7	3,54	8	2,6
G5-K4		2	2,25	1	2,0

The values  $\overline{\mathfrak{M}_A+\mathfrak{M}_B}$  are the mean values derived directly from known inclinations (eclipsing binaries), whereas  $[\overline{\mathfrak{M}_A+\mathfrak{M}_B}]$  are the means derived from the above assumption as to the mean value of  $\sin^3 i$ .

The group of stars later than F0 consists of 12 giants and 17 dwarfs No systematic difference with regard to the mean masses can be found which is contrary to what is the case when the masses of visual binaires are derived:

Spectral	G	ilants		Dwaris		
olass	(MA+MB) sina :	101A+101A	13	$\overline{(\mathfrak{M}_A+\mathfrak{M}_B)\sin^3\imath}$	$\mathfrak{M}_A + \mathfrak{M}_B$	11
F0—F4 F5—G4 G5—K4	1,90 () 2, <b>3</b> 8	2,85 O 3,57	7 5	2,34 () 1,69 1,55	3,51 ⊙ 2,53 2,32	4 10 3

The mass-ratios  $\mathfrak{M}_B/\mathfrak{M}_A$  have a mean value of 0,75. The distribution with regard to spectral class is as follows

<sup>&</sup>lt;sup>1</sup> A N 220, p 249 (1924)

Spectral		Mean				
	0,11—0,30	0,510,50	0,51-0,70	0,710,90	0,91—1,00	man catlo
06-B4 B5-A4 A5-P5 F5-G4 G5-R4	4 1	3414	4 6 2 1	7 9 7 5	4 7 8 6	0,74 0,68 0,81 0,83 0,76
Sum	5	10	13	30	25	

A tendency of  $\mathbb{R}_n/\mathbb{R}_n$  to increase in the course of evolution seems to be present, but is not very pronounced.

There seems to be some relation between  $\mathfrak{M}_B/\mathfrak{M}_A$  and  $(\mathfrak{M}_A + \mathfrak{M}_B)\sin^2 i$ 

as follows:

大地和東	(#4十版) almi i	#	Na/Na	(DA+112) arr;	•
0,32 0,52 0,69 0,79	7,15 4,37 7,54 3,68	10 10 10	0,86 0,89 0,95 0,99	5,09 6,53 4,38 5,01	10 10 10 10

The dispersion within the individual groups is considerable and the general relation cannot be established at present.

BEER uses the quantity  $f^{\dagger} = \Re_B(\Re_B + \Re_A)^{-1}$  and divides the material into binaries showing one spectrum (n=151) and two spectra (n=95). Periods of  $1000^d$  or more have to be excluded, as has been pointed out by Ludendorff, as they are not comparable with short periodic systems on account of the very nature of the function f. The following correlation surface is found for the remaining 233 systems.

	<u> </u>												
Special date	- 1											10 lo<9,1	Secon
O6-B4	ono owi	4 8	14	3	3 2	2 2	1 2	3	3	4	3	5	32 19
B5-A4	one two	2 2	_	3	3	4	12	4	10 1	8	7	_	38 34
A5~ F4	one two	1	_	4	2	•	4	3	4 2	2		_	21 19
F5 G4	two	=	_	1	2	3 4	2 5	4 2	-	9	-3	1	27 18
G5~K4	ono owt	=	_	1	=	3	6	4	6	-1		1	22
K5-M7	one two					_	1	1	=	1			3
Sum	one two	11	4	3	5 9	10 19	17	19	27	25 7	18	9	143

BERR has investigated the mean errors in the mean values of / and confirms the conclusion of LUDENDORFF that within each spectral class the mean value of / is practically constant and thus vary suitable for a derivation of the mean value of the meas,

The ratio of the masses of B stars and A stars (including A stars and the following classes) is found to be 3,42 and 5,80 for stars showing one and two spectra respectively. A direct computation from the direct data which avoids using / gives 5,48 for the second group

The material concerning the spectroscopic binaries is given in J II Moore's "Third Catalogue of Spectroscopic Binary Stars" (which includes the material to July 1st, 1924) in Lick Bull No 355 (1924) and in Belen's paper (which includes the material to March 1927) On pages 122—124 Beer gives corrections and additions to the Third Catalogue. The student of spectroscopic binaries is recommended to consult these two sources, which give a complete collection of the material up to 1927, whenever investigations of a general nature concerning these objects are to be undertaken

The correlation between the frequencies of one and two spectra is comparatively low. An analysis of the two frequencies has not yet been undertaken,

but would undoubtedly reveal several points of interest

BEER forms the equation

$$\left(\frac{\mathfrak{M}_{n}}{\mathfrak{M}_{A}}\right)_{t} = \frac{f_{t}^{\frac{1}{2}} f_{tt}^{-\frac{1}{2}} \left[\mathfrak{M}_{n} / (\mathfrak{M}_{A} + \mathfrak{M}_{B})\right]_{tt}}{1 - f_{t}^{\frac{1}{2}} f_{tt}^{-\frac{1}{2}} \left[\mathfrak{M}_{B} / (\mathfrak{M}_{t} + \mathfrak{M}_{B})\right]_{tt}}$$

where the subscripts I and II refer to the groups with one and two spectia respectively. He finds from his material

Spectral	(901 n/901 1)11		(1) W/K(C)		11
class	(SOURISM INT	11	(20(2)38 ()1	/t	/ii
Λ	0,683	30	0,415	36	32
F	0,806	19	0,466	21	18
G	0,826	13	0,508	27	15

229. Preferential Values of Stellar Masses. In order to determine the masses and the mass-ratios of spectroscopic binaries J Hetterich has investigated 173 pans, of which 61 exhibited the spectra of both components. The Cepheids, stars of the same type as  $\beta$  Canis Majoris, and stars with periods larger than 1000<sup>d</sup> were excluded. Hellerich¹ found that stars of the classes A to G did not have very different mean masses.

Spectral class	(MA +MB)sin**	71
A	2,72 ①	22
F	2,08 〇	13
G	2,07 〇	3

Within the classes Oc—B9 the range in the mass value is from 10 to 1390. On account of this dispersion no mean values were formed for these spectial classes. Besides, the material suggested that the masses were grouped around

certain maxima of frequency, viz 320, 220, 160, 100, and 2,5-3,00. Although the material is small, it nevertheless seems difficult to explain the

preferential values as due to chance. The frequency of large masses decreases very rapidly with the increase in the value of the mass.

The adjoining distribution of the values  $\mathfrak{M}_B/\mathfrak{M}_A$  was found

The mean values are

$\mathfrak{M}_{H}/\mathfrak{M}_{A}$	Oe-B9	AG	Mu/Ma	Oc139	A⊷G
0,1-0,2 0,2-0,3 0,3-0,4 0,4-0,5 0,5-0,6	3 1	1 1	0,6-0,7 0,7-0,8 0,8-0,9 0,9-1,0	3 3 4 7	5 5 10 13

Spectral class	1 HE/14	28-	Spectral class	Ma/M t	13
B0-B5 B8-B9 A	0,64 0,76 0,79	13 4 22	F G	0,88 0,86	13

No relation was found between the mass-ratio and  $(\mathfrak{M}_A + \mathfrak{M}_B) \sin^3 i$ 

<sup>&</sup>lt;sup>1</sup> A N 220, p 249 (1924)

HELLERICH recommends the use of the quantity /t and investigates the frequency of this quantity in his material. A decided difference with regard to the distribution of the /t values is found between the systems for which one spectrum has been observed and those for which both spectra have been observed. In the first case these values are considerably lower than in the second case.

This remarkable difference may arise from a number of causes. It does not seem likely that a systematically different orientation in space of the orbits

Spectral class		-	}	<del></del>
-,,-	Ome spectrum		Two species	я
A sters . F sters	0.367 0.280	27 20	0,543 0,587	22 13

of the two groups can be present. Nor can any systematic difference be assumed in the mass values themselves or in the mean eccentricities. An inspection of the material shows that the mean periods of the two groups are not very different. The only possible explanation seems to be to assume that the mass-ratios of the binaries with double spectra really are systematically larger than the mass-ratios of the binaries with a single spectrum, which means that the dispersion in the single masses in the former case should be smaller than the dispersion in the latter.

Comparing the values of  $R_B/R_A$  and excluding stars for which  $R_B/R_A$  is smaller than 0,80 Hellerich finds for group I the following values for the mean mass-ratio:

Spootral class	数1/数1	
A stors	0,37 0,29	27 20

In those cases where the companion has a considerably lower brightness than the principal star the mass of the companion will also be very small in comparison with that of the more

massive star. The theory implies that the dispersion in stellar mass is larger than has generally been assumed but it scarcely gains support from an investigation of visual binaries. Mass-ratios as low as 0,3 seem to be rather exceptional among the 50 pairs so far investigated. The enormous difference in luminosity of 150000 between Procyon and its companion corresponds to a difference in the masses of only 0,9  $\odot$ .

In a subsequent paper Hellerich returns to the question, if preferential values of stellar mass exist. He points out that the results at the Cape Observatory by Halm concerning the preferential values of colour indices also pointed in the direction that there are six maxima in the frequencies of masses computed from the absolute magnitude and temperature. Halm's maxima are

From the material at hand of spectroscopic binaries HELLERICH found five maxima, viz 330, 220, 160, 100 and 2,5-3,50

The values 2,8  $\odot$  and 10  $\odot$  are common to both series, the value 1,3  $\odot$  is weakly indicated in the spectroscopic material. The small values 0,66  $\odot$  and 0,32  $\odot$  are wanting in the spectroscopic material as they correspond to very small amplitudes in the curves of radial velocity. On the other hand, the large mass values 16  $\odot$ , 22  $\odot$ , 33  $\odot$  are not extant in HALM's sories, for the stars used by him are of classes  $\Gamma$  to K and, therefore, cannot have large masses, as is known from other investigations.

HALM's series of the frequency-maxima of stellar masses nearly forms a geometrical progression with the proportion 1/a. Extrapolating this series to large masses, one obtains 23  $\odot$ , 46  $\odot$ , 92  $\odot$ , 184  $\odot$ . The comparison with the

<sup>&</sup>lt;sup>1</sup> AN 221, p 49 (1924)

Report of H M. Astronomer at the Cape of Good Hope 1922, p 4.

second series shows that the value 23 O is extant. Further, we know two spectroscopic binaries with masses not too far from 920 and 1840 respectively.

Testing Halm's series with the material offered by visual binaries. Illiting it

finds indications of a frequency maximum between 0.90 and 1.50

230. Dwarf Nature of Spectroscopic Binaries. E A Kreiking has advanced the idea that spectroscopic binaries are generally dwarf stars. From the catalogues of I Moore and A BEER 97 systems with two spectra were collected The value of sin; was found to be much larger than has been assumed carlier When the log's of the values Masin<sup>3</sup> 1 and Masin<sup>3</sup> 1 were plotted against spectral class a rather definite curve was found. As there is no reason why the mean value of Msm3; should systematically depend on spectral class, the actual relation between M and spectrum will be found when the plotted curve is shifted over an interval corresponding to the logarithm of sing. The masses of the giants were computed according to Eddington's theory and the masses of the dwarfs according to Brill's investigation. The following table shows the result

Spectral	lo <sub>1</sub>	g Wi	log M sin *	log9)}-log9)} sin3 *		
class	Ginnts	Dwarfs	Ind the state 1	Glants	Dwirfs	
O5		2,00	1,90		+0,10	
B0	0,87	1,00	1,10	-0,23	-0,10	
B5	0,65	0,65	0.44	+0,21	+0,21	
A0 j	0,56	0,44	0,22	+0,34	+0,22	
A5	0,54	0,30	0,11	-1-0,43	+0.19	
Fo	0,52	0,18	0,05	+0,47	+0,13	
<b>F</b> 5	0,45	0,08	9,99	+0,46	+0,09	
G0	0,44	0,00	9,95	+0,49	+0,05	
G5	0,43	-0,08	9,90	十0,53	+0,02	
Ko	***	-0,16	9,86	1	-0,02	

Although in the case of the dwarf hypothesis theresiduals, exhibit a systematic run there is no doubt that they should not be preferred Uniontainty is involved in the computation of the mean masses because the frequencies in the Russell dia-

gram used have not been reduced to equal space. Anyhow it is evident that the dwarf hypothesis might be worth a serious consideration. Kreiken found for dwarf stars the value  $\log \sin^3 i = 9.905 - 10$  and thus  $\sin i = 0.927$  and for grant stars  $\log \sin^3 i$ =9,525 -10 and  $\sin i = 0,695$  which is very near the value 0,667 generally adopted

In order to test the result the hypothetical distances were derived from the masses computed by multiplying Msin32 by the two values 0,927 3 and 0,695 a corresponding to the dwarf and giant hypotheses. The masses were converted into distances by means of Eddington's mass-luminosity formula A comparison between the distances thus obtained and the distances derived from trigonometric parallaxes or spectrographic determinations of the absolute magnitude decides in favour of the value  $\sin i = 0.927$ 

281 Discovery of Mass-Luminosity Relation, The relation between stellar mass and luminosity was at first indicated in Eddington's works concerning the radiative equilibrium of the stars. It was concluded that the luminosities of giants vary approximately as M2 and of the dwarf stars as M2. The first time n mass-luminosity relation was established in an empirical way was, as fat as I am aware, in a paper by Hertzsprung in 1919 in which he derived the formula:

$$\log \mathfrak{M} = -0.06 M = -0.06 (m + 5 + 5 \log n)$$

Somewhat later C Luplau-Janssens went over Herrzsprung's material again, but preferred to leave the coefficient AM/AM unchanged. At the same

<sup>&</sup>lt;sup>1</sup> M N 89, p 589 (1929) <sup>2</sup> Berlin-Babelsberg Veröff VII, Heft 1 (1927) 3 M N 77, p 596 (1917) <sup>4</sup> A N 208, p 96 (1919)

<sup>&</sup>lt;sup>8</sup> Undersøgelser over Doppelstjerner III (1919)

time independently of Hertzsprung A van Maanen' derived a mass-luminosity relation of practically the same form. From van Maanen's paper the following table has been prepared giving the mean values of M, M and  $\log M$  together with

the corresponding dispersions around the means

The curvature of the line connecting the mean values of M and M and the small dispersion in the values below  $M \approx 4.5$  are notable results in this investigation. The

M±sn	10十一個	logWite log M	n
0,42 ± 0,33 1,63 ± 0,44 3,00 ± 0,35 4,63 ± 0,27 5,77 ± 0,40 10,7 ± 0,81	7.99 士 8.2 3.42 士 2.04 1.72 士 1.47	0,94 ± 0,46 0,75 ± 0,33 0,46 ± 0,25 0,13 ± 0,33 0,08 ± 0,11 -0,21 ± 0,14	4 6 6 12 8 3

mean values of the mass compare favourably with later investigations when more extensive material has been available.

Of the subsequent treatments of the mass-luminosity relation we shall only mention those of F. H. Seares and W. J Luyten The latter derived the expression  $\log \Re = -0.09 \, (M - 4.8)$ .

In 1923 Herzzerrung<sup>4</sup> returned to the question. From a list of 15 first-class determinations, which included our Sun, he determined the diagram reproduced in fig. 153 The general decrease of mass with luminosity is clearly shown.

The faint companion of Sirius +# is extraordinarily massive in # comparison with its small intrinsic brightness.

HERTZSPRUNG assumed the following linear relation:

 $\log \mathfrak{M} = -0.084 (m + 5 \log n)$ but remarked that the quadratic expression

##-5log #=-11log IR+2(log IR)\*
would represent stars of great
mass somewhat better

He introduces the conception of angular mass being

$$(\mathfrak{M}_A + \mathfrak{M}_B) \cdot \pi^a = \frac{a^a}{\bar{P}^4}$$

Knowing  $\mathbb{R}_A/\mathbb{R}_B$  and  $a^2/P^2$  we find the absolute magnitudes of each component reduced to the mass of the Sun to be:

$$m_A + 5 \log n + \frac{1}{2} \log \mathfrak{M}_A$$
,  $m_B + 5 \log n + \frac{1}{2} \log \mathfrak{M}_B$ .

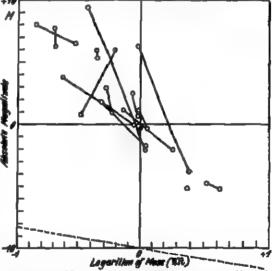


Fig 153 Mess-luminosity diagram according to HERTEPHUNG The full-drawn lines join the components of double stars. The single circle near the origo indicates the position of our Sun.

From the relation between mass and absolute magnitude it is possible to compute the parallax of a double star from  $m_A$ ,  $m_B$ , and  $a^a/P^a$  The formula will be  $0.86 \log \pi = \log \pi_d - \frac{1}{2} \log \left[1 + 10^{-0.084 (m_B - m_d)}\right] + 0.028 m_A$ .

The dynamical parallax  $n_i = \frac{s}{P_i^2}$  is computed in this case by assuming the mass-sum to be equal to the mass of the Sun.

If the above quadratic formula holds good the computation of  $\pi$  will be more complicated. Herezsprung has given a table in his paper from which

<sup>1</sup> Publ ASP 31, p 231 (1919)
Barv Ann 85, No 5 (1923).

Mt Wilson Contr 226, Ap J 55, p. 165 (1922)

<sup>4</sup> BAN 2, p. 15 (1923).

the value of  $\log \mathfrak{M}_A$  is found by double interpolation, using  $m_B - m_A$  and  $5 + m_A + 5\log \pi_d$  as arguments. In accordance with the above quadratic formula,  $M_A$  is found and from the difference  $M_{\rm nig} - M_{\rm dyn}$  the ratio  $\pi_d/\pi_l$ , from which  $\mathfrak{M}_A + \mathfrak{M}_B$  is found.

Heretzsprung's Table of values of  $m_A + 5 \log n_d + 5$  (for  $\mathfrak{M}_A + \mathfrak{M}_B = 1$ )

$\log \mathfrak{M}_A$	]	$m_B - m$ (									
- VIA	0m	110	2m	3m	4m	51n	10 <sup>1</sup> n	00	m 1 + 5 + 5 log va		
1,0	16,84	16,78	16,73	16,69	16,65	16,62	16,49	16,33	18,00		
0,9	15.52	15,46	15,42	15,37	15,34	15,30	15,17	15,02	16,52		
0,8	14,25	14,19	14,14	14,10	14,06	14.02	13,89	13,75	15,08		
0,7	13,02	12,96	12,91	12,86	12,82	12,78	12,66	12,51	13,68		
0,6	11,82	11,77	11,71	11,66	11,62	11,59	11,46	11,32	12,32		
0,5	10,67	10,61	10,55	10,51	10,47	10,43	10,30	10,17	14,00		
0,4	9.56	9,49	9,44	9,39	9,35	9,31	9,18	9,05	9,72		
0,3	8,48	8,42	8,36	8,31	8,27	8,23	8,10	7,98	8,48		
0,2	7,45	7,38	7,33	7,28	7,23	7,19	7,06	0,95	7,28		
0,1	6,46	6,38	6,33	6,28	6,23	6,19	6,07	5,95	6,12		
0,0	5,50	5,43	5,37	5,32	5,27	5,23	5,11	5,00	5,00		
+0,1	4,59	4,52	4,55	4,40	4,35	4,31	4,19	4,09	3,92		
0,2	3,72	3,64	3,57	3,52	3,47	3.43	3,31	3,21	2,88		
0,3	2,88	2,80	2,74	2,68	2,63	2,59	2,47	2,38	1,88		
0,4	2,09	2,01	1,94	1,88	1,83	1,79	1,67	1,59	0.92		
0,5	1,34	1,25	1,18	1,12	1,07	1,03	0,92	0,83	0,00		
0,6	0,62	0,54	0,46	0,40	0,35	0,31	0,20	0,12	0,88		
0,7	-0,05	-0,14	[-0,22]	~0,28	-0.33	-0,37	-0.48	-0,55	-1,72		
0,8	0,68	0,78	0,86	0,92	0,97	1,01	1,12	1,19	2,52		
0,9	1,28	1,38	1,46	1,52	1,57	1,61	1,72	1,78	3,28		
1.0	1,83	1,94	2,02	2,09	2,13	2,17	2,28	2,33	4,00		
1,1	2,34	2,45	2,54	2,60	2,66	2,70	2,79	2,85	4,68		
1,2	2,82	2,93	3,02	3,09	3,14	3,18	3,27	3,32	5,32		
1,3	3,25	3,37	3,46	3,53	3,58	3,62	3,71	3,75	5,92		
1,4	3,64	3,77	3,87	3,94	3,99	4,02	4,11	4,15	6,48		
+1.5	-4,00	-4,14	-4.23	4,30	-4,35	-4,39	-4,47	-4.50	- 7,00		
n tote	it wor	le 20041	\$X7 C		•		TY Was	TT	F 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		

In joint work with W S Adams and A H Joy, II. N Russill has compared dynamical and spectrographic parallaxes in order to derive the masses of the stars. The number of stars for which such a comparison could be made was 327, including giants and dwarfs of spectral classes from O8 to M6. The stars were grouped in the following way.

Spectral class	$M_d$	Md-Me	$\pi_i/\pi_d$	Residual	M	11
08-B2	-i,2	+1,31	0,54	-0,02	6,20	40
B3B8	+0,5	+1,24	0,56	-0,07	5,6	10
B9A1	+1,2	+0,61	0,75	+0,09		3.0
gG9-gM6	+1.2	+0,67	0,73	+0,07	2,4	35
gF6-gG8	+1.6	+0,96	0,64	-0.04	2,5	28
A2-A4	+2.0	+0,55	0,78		3,8	31
A5-A9	+2.5	+0,50	0,80	+0,07	2,1	29
$F_0-F_3$	+3.2	+0,69	0,73	+0,06	2,0	35
F4F5	+3.3	+0,40	0.83	-0,02	2,6	17
dF6-dF8	+4.4	+0,68		1-0,07	157	24
dF9-dG0	+4,3	+0.39	0,73	-0.08	2,5	28
dG1-dG5	+5.2	+0,63	0,84	+0,03	1,7 [	25
dGo-dK1	+5.6		0,75	-0,09	2,4	24
dK2-dK6	+6,5	+0,56	0,77	-0,09	2,2	25
dK7-dM6	+9,2	+0,25	0,89	-0,01	1,4	21
dA-dF	+10.8	+0,01	1,00	-0.02	1.0	7
08-B1		-0,32	1,16	十0,07	0,6	2
B2-B9	-1,4	+1,64	0,47	-0,08	9,7	9
	十0,6	+1,39	0,53	-0,07	6,8	22

<sup>1</sup> Publ ASP 35, p 189 (1923)

The values in the two last rows are derived from Kapthyn's cluster parallaxes  $M_d$  is the absolute magnitude corresponding to the combined light of the pair and is based on the assumption that the sum of the masses of the components is = 0  $M_d$  is the absolute magnitude based on the spectrographic parallax. The mass  $\mathfrak{M}$  corresponds to the geometrical mean mass, from the ratio  $n_d/n_d$  which in its turn is the value corresponding to  $\mathfrak{M}_d = \mathfrak{M}_d$ .

The authors remark that the mean mass is by no means a simple function of the spectral class. But if the masses are plotted against the absolute magnitudes all the stars full into a straight line. The white dwarfs are no longer outstanding exceptions, their mass is small in the proportion to be expected from their low luminosity.

As a first approximation the relationship can be taken as linear and the

straight line:

 $\pi / \pi_s = 0.62 + 0.045 M_s$ 

us the relation curve. The residuals are given in the above table.

The values for the masses of B and A stars found by these authors did not amount to much more than 50 per cent of these found by SEARES. The discrepancy suses from the following cause: SEARES's material consisted of the stars known to be in relative motion, and for more distant pairs this involves a selection in

the sense that distant pairs of allow apparent motion are not included The result of this is too high an estimate of the mean rate of motion, and of the mean mass. A correction was applied by SEARES for the effect in question, but the later results show that the value has evidently been too small In the investigation now under review all well observed pairs were included, even if the apparent motion was very small Also, on account of the more extensive material, the

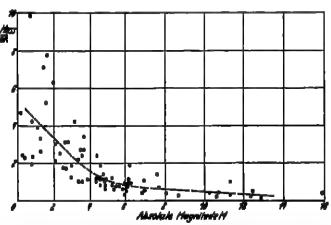


Fig 154. Relation between absolute magnitude M and massix according to LUNDMARK. For this diagram the masses of double stars were derived using all available determinations of orbits and trigonometric parallesses up till 1924. The dotted line represents the course of the mean values of various groups with regard to M.

values in the above table are certainly entitled to more weight as far as the early spectral classes are concerned

In this paper the necessity of improving the dynamical parallexes by means of correction factors depending on the size of the mass was also pointed out

The dynamical parallaxes ordinarily given,  $\pi_d$ , should be multiplied by the factor  $(\mathfrak{M}_A + \mathfrak{M}_B)$  in order to be comparable with the parallaxes used in the above formula.

The dependence between mass and luminosity is really to be expected as follows from easy calculations. Combining the equation giving the

662

mass-sum in visual binaries with the equation of definition for the obtain  $\mathfrak{M}_A + \mathfrak{M}_B = 10^{3(\log n + 1) - 2\log P} \cdot 10^{0.6(m - M)}$ 

The empirical data show that there is some slight dependence  $\ln (w_{t+1})$  and the expression  $40^{3(\log a+1)-2\log P}$ , but a more obvious dependence  $\ln (w_{t+1})$  expression and the absolute magnitude. We can write

$$\mathfrak{M}_A + \mathfrak{M}_B = 10^{\gamma(m, M)} \cdot 10^{0.6M}$$

There is, using the actually determined masses, no dependence shown? m and M and there are not easons that such a dependence should exist M cipal point of the mass-luminosity relation thus can be derived with theoretical deductions provided that  $\log \mathfrak{M}$  can be expressed as a power of M. The higher terms in the expression

$$\log \mathfrak{M} = \sum_{i=1}^n a_i M^i$$

are derived on the basis of theoretical work, be it along the lines in length of in Jeans's theory of radiative equilibrium

Although the former in connection with his original theory of the new of the stars showed that there is a general relation between mass and a magnitude it is not within the scope of this paper to present a length account of earlier theoretical work. The student interested in this problem adviced to consult Vol III/i of this Handbook

A theory concerning the stellar absorption coefficient ought to lead to lead to determining the absolute magnitude of the giant stars for which the magnitude effective temperature are known. In order to avoid a determination of the solute values of the constants the observational data of Capella are the absolute magnitudes of ordinary stars are computed at a basis of the theory, regardless of whether they are giants or dwarfs. Are the stars of mass and dwarf theory the absolute magnitude is a double-valued for the of mass and effective temperature. A star of mass 1 and temperature is the star of mass 1 and temperature is the star of mass 1 and temperature is the star of the Sun at present and that of the star of the sun at passed through the same temperature on the up grade with a star planer surface area than now

The suggestion underlying the theory is that the dense stars like the first are in the condition of a perfect gas and will use in temperature if they will a star are "grants". Theoretical reasons are given in the part of Eddington which assert that the stellar matter should be able to control an enormously high density before deviation from the laws of a parter of the becomes appreciable

The results of Hertzsprung and of Russell, Adams, and Joy, while  $\frac{3}{2}$  and  $\frac{1}{2}$  been reviewed earlier, indicated that M plotted against  $\mathfrak{M}$  resulted in a condition of the plane, a conclusion which is difficult to reconcile with the giant and dwarf there are

According to the theory of radiation we have

$$1 - \beta = 0.00309 \, \text{M}^2 \mu^4 \beta^1$$

where  $\mu$  is the average molecular weight and  $1-\beta$  is the ratio of two the pressure to the whole pressure. The total radiation L of a star is propositive at  $\mathfrak{M}(1-\beta)/k$ , where k is the coefficient of absorption. In Edding 1972 and the work k was believed to be approximately independent of temperature  $\mathfrak{M}$ .

<sup>&</sup>lt;sup>1</sup> M N 84, p 308 (1924)

density  $\varrho$ . The theory of nuclear capture and Kramers's theory, as well as other evidence suggest the form  $\hbar \sim \varrho/\mu T^{\frac{1}{4}}$ . By the aid of this proportionality the following expression for the total radiation is found

$$L = \text{const.} \mathfrak{M}^{\frac{1}{2}} (1-\beta)^{\frac{1}{2}} \mu^{\frac{1}{2}} T_{\bullet}^{-\frac{1}{2}}.$$

The value of  $\mu$  is likely to be about 2,2 for Capella and Eddington adopted  $\mu$ =2,11. The following values computed from his formula show the general course of the mass-luminosity relation

1-β	Mass	Musi	Myja	T.	Spectral class
0,80	90,63 ①	- 6,71	_	26200°	Ö
0.75	56,15	<b>— 5,88</b>			_
0,70	37.67	- 5,16		22 500	Oo
0,65	26,66	- 4,52	(-2,2)		· —
0,60	19.62	- 3,92	(-1,1)	-	
0,55	14,84	- 3,35	` `	_	
0,50	11,46	- 2,81	(-1,1)	17460	B2
0,45	8,98	- 2,26	l   —	· ·	~
0,40	7.12	- 1,72		_	
0,35	5,67	- 1,16	_		-
0,30	4,53	- 0,56	0,00	13260	B7
0,20	2,83	+ 0,81	0,87	10520	ΛO
0,10	1,58	+ 2,82	2,88	8250	A8
0,05	1,00	+ 4,64	4,55	6 290	I/8
0,030	0,75	+ 5,93	6.45	7.60	G4
0,025	0,67	+ 6,38	6,17	5 160	G4
0,015	0,51	+ 7,63	0.00	4 540	Ko
0,010	0,41	+ 8,61	8,03	4 540	17.0
0,004	0,26	+10,82	11,9	3210	K9
0,0025	0,20	+11,95	1 —	_	
0,0015	0,16	+13,17	-	-	_
0,0010	0,13	+14,14	17,0	2 5 5 0	Md

In this table have also been inserted the absolute visual magnitude and the corresponding effective temperature and mean spectral class.

In this table as in the corresponding fig. 4 in Eddington's paper, the same effective temperature as that of Capella, 5200°, is assumed. For other temperatures the correction  $-2\log{(T_{\star}/5200)}$  has to be added to  $M_{\rm bol}$ . The whole range from 3000° to 12000° only introduces a correction of  $1^{2}$ ,2.

The following table gives the correction to the magnitudes arising from the temperature term as well as the correction for reducing visual magnitude to bolometric magnitude as derived by EDDINGTON in his earlier work<sup>1</sup>

_								
$T_{\rm d}$	-2 log T <sub>c</sub> /5200	Man Man	$T_{\bullet}$	-2 log T / 5200	Myte-Mbel	$T_{\theta}$	—2 lon T./5200	H <sub>vis</sub> -M <sub>bel</sub>
2000 °	+0 <sup>™</sup> ,82	_	6000°	-0 <sup>M</sup> ,14	0,00	18000°	-1 <sup>12</sup> ,10	-
2500	+0 .62	+2,65	7000	-0,28	+0.02	20000	-1 .19	_
3000	+0,46	+1,71	8000	—o ,39	+0,05	25000	-1 ,38	
3500	+0 ,32	+1,04	9000	-0,49	+0.12	30000	—1 ,54	_
4000	+0,20	+0,80	10000	-0,59	+0,23	35000	-1 .68	
4500	+0 10	+0.35	12000	-0 ,74	+0,53	40 000	一1 .79	
5000	+0 ,02	+0,14	34000	-0,88				
5500	-0 ,07	+0,05	16000	-1,00				ļ

The theoretical curve was compared by Eddington with the following observational data: 8 first-class determinations of masses of binary stars together with the mass of the Sun; 24 second class determinations of masses of binary stars. To these are added 5 double stars in the Hyades, 5 Cepheids, and 13 eclipsing binaries. The agreement between the 54 used mass-values derived

<sup>1</sup> MN 77, p. 605 (1917).

from the best observational data and the curve computed according to the theory is good, indeed. The average of the residuals is  $\pm 0^{M}$ , 56, most of which might fairly be attributed to errors in the observational data, and the maximum discordance is 1<sup>M</sup>.7 Certain refinements of the nature of a second approximation are suggested by Eddington, who derives the following relation between a change in the molecular weight and a change in the absolute magnitude1

$$-\Delta M = \frac{9\beta + 8}{4 - 3\beta} \log e^{\frac{\Delta \mu}{\mu}}$$

At the time this investigation was carried out the first approximation certainly sufficed. The accumulation of further data since then may invite us to make a second approximation

The masses of the Cepheids were computed on the basis of the pulsation theory. The method is that of successive approximations. A value of M is assumed From To (spectral class) the radius is deduced and then the mean density The central density  $\varrho_o$  is 54,25 times the mean density. The period Pis then obtained from the expression

$$P \varrho_{o}^{\frac{1}{2}} = 0.29 (\gamma \alpha)^{-\frac{1}{2}}$$

where  $(\gamma a)^{\frac{1}{2}}$  is taken from M N 79, p 15, table V with  $1-\beta$  as argument. The process is repeated until P stands. The highest value is 26,20 for Y Ophruchi and the lowest 4,14 @ for RR Ly1ae

EDDINGTON inquires if, assuming that the gas-laws hold good for ordinary stars, we then should expect that each star will have the precise luminosity deducible from its mass and effective temperature or, in other words, whether the theory is accurate individually or only statisfically. The sources of residual differences are principally abnormal composition and abnormal rotation. With regard to the first source an unduly large proportion of hydrogen would make the stai fainter. With regard to rotation it has been shown by E.A. Milne that a rapid iotation makes the star slightly fainter, but that the effect is very small until the speed is sufficient to deform the star considerably. What is to be feared, concludes Eddington, is that the observed spectrum misleads us concerning the true value of  $T_a$ . An unsuspected binary ought to betray itself by having a magnitude fainter than that predicted from a knowledge of its combined mass

The very interesting theoretical considerations as to whether it is physically likely that a dense star such as our Sun can obey the laws of a perfect gas cannot be given here The student is referred to § 9 in Eddington's paper

The high density of the white dwarfs is not abound. At a very low effective temperature smaller than that of a dwarf of spectral class M the star Sirius B is probably able to produce in some way "an imitation of leading features of the F spectrum sufficiently close to satisfy the expert observer" The deviation of this star from the mass-luminosity curve is not surprising if the density is 53,000  $\odot$  new considerations enter into the calculation of k, since the elections are in the capture zone of two or more nucler simultaneously. Also the deviation from the gas-laws may be considerable. On the other hand the star  $o^2$  Eridani B agrees quite well with the mass-luminosity relation.

In Kramers's theory the absorption coefficient k contains an additional factor  $\infty (1 + h r_1/RT)$  The effect of this factor was calculated and found to vary between +0,2 and -1,6 There are general reasons for accepting a correction factor of this form, which represents the ratio of the energy given up on capture

<sup>&</sup>lt;sup>1</sup> M N 84, p. 323 (1924)

at the mean ionization level to the mean free energy before capture. If the mass is supposed to be constant during the course of stellar evolution, then the mass-luminosity law is in disagreement with the views on stellar evolution accepted on the basis of Hertzspeung's and Russell's work Eddington points out that the giant and dwarf theory definitely held the view that the influence of mass on luminosity was small and unimportant. It was thought that the stars along the main series had in the mean a lesser mass than the stars along the giant branch. The most generally advocated view was that the stars with smaller mass traversed their course more quickly than the heavier stars, although the theoretical arguments tend to show that the latter would reach the end-stage first. The results of Eddington show that the systematic difference in mass is not a minor detail, and that the correction to be applied before the Russell diagram can give the evolutionary course of individual stars is considerable.

Another possibility is that a star gradually duminishes its mass during its evolution. This would happen if the star is "burning itself away", i c if it obtains its energy of radiation by annihilating electrons and protons. A star burning itself up may increase continuously in density and internal temperature, although the effective temperature first rises, but then falls.

If the theory of annihilation of matter holds good the relative number of stars of different spectral classes can be computed, because the frequency of

a certain evolutionary stage will be proportional to the duration

The abundance of any stage should be proportional to the duration of of the stage. If our is the amount of mass carried off as radiant energy during the stage then

 $\partial t \sim \int \frac{d\mathbf{R}}{L} .$ 

Approximately L is proportional to  $\mathfrak{M}(1-\beta)^2/\beta$  if the factor  $T^{-\frac{1}{2}}$  in k is neglected. Then

 $dt \sim \frac{\beta}{(1-\beta)^4} \frac{d\Omega}{\Omega t}$ , or,  $\sim \frac{4-3\beta}{(1-\beta)^3} d\beta$ .

Integrating we find

$$\delta i \sim \delta \left\{ \frac{\frac{1}{2} + 3(1-\beta)}{(1-\beta)^2} \right\}.$$

The following table gives the cosmogonical time-scale according to EDDING-TON. Under the duration of stage is given the time it takes to develop between succesive values of mass or M<sub>bel</sub> given as arguments

However large the initial mass, there cannot be more than 20 left at the end of a billion years. If a cluster contains stars > 20, the age of the agglomeration cannot exceed 10<sup>18</sup> years. Now since most of the clusters contain absolutely faint and bright stars mixed

Мая	]	M	1		Deration of stage		
35 " 10 "	35 © 10 3,7	-5 <sup>M</sup>	to	3₁ 5×1	м,5		10 <sup>18</sup> year
3.7 1.73 0.92 0.53 0.31	1,73 0,92 0,53 0,31 0,18	0 2 5	5	5 7 10 12	.5	0,93 5,21 36,3 281 2190	

together the faint stars cannot have evolved appreciably. But, asks Eddingron, if we have to deny the evolution of dwarf stars in clusters is there any point in assuming the evolution of dwarf stars in general?

Nature 117, Suppl. p. 25 (1926)

The numbers under the heading "duration of stage" should be proportional to the frequency of the absolute magnitudes or  $\varphi(M)$ . The theoretical luminosity-curve also agrees fairly well with the one found from observational evidence. This fact seems to the present writer to be the strongest support we have, at present, in favour of the theory of evolution by the loss of mass

The frequencies of stellar masses among different absolute magnitudes have been derived by Luyten<sup>1</sup> on the basis of the mass-luminosity relation found by him,  $\mathfrak{M} = L^{0,225}$ , and the luminosity law of Kapteyn. Similar calculations have been made by J Ohlsson<sup>2</sup>, who has derived the distribution of stellar masses within ten parsecs on the basis of the material of the present writer and the mass-luminosity law of Eddington and of Jeans

	ΔIυ	$\varphi(M_v)$	TH	y (M)
1 H 1 3 5 7 9 11 13	to 0 <sup>31</sup> 2 4 8 10 12 14 15	5 13 39 42 62 30 12 3	3,16-4,00 O 1,99-2,50 1,26-1,60 0,79-1,00 0,50-0,63 0,32-0,40 0,20-0,25 0,13-0,16	5 17 53 57 45 19

Eddington has also given a discussion of the fundamental quartic equation of the theory of radiative equilibrium in which the gradual increase in  $\mu$  from the centre to the boundary of the star is taken into account

For several practical purposes it has been thought to be conventent to express the mass-luminosity

law in a quadratic form of log M A least square solution of EDDINGTON's material has given

 $\mathfrak{M} = 10^{+0.6144 - 0.1576 M + 0.00112 M^4}$ 

This curve represents the material available with a sufficient degree of accuracy

288 Discrepancies between Seares's and Eddington's Results. (7 Shaha) has compared the masses as computed according to the theory of Shares and according to that of Eddington. The agreement is unsatisfactory for the giant stars, and the divergence is of a systematic character. Eddington's masses of very high luminosity for late spectral classes are greater than the corresponding values of Seares, and the difference increases with increasing luminosity. For giants of early classes Seares's values are greater than Eddington's, while for late spectral classes the reverse is the case

Observational data of double stars, part of which have been obtained by Shajn at Pulkowa, lead to the following paradoxical result

Spectra	al class	dm	М	bol	M nj	Ī T	
Primary	Secondary	(belom )	Primary	Secondary	EDDINGTON	SHARRS	71
K <sub>1</sub> G <sub>2</sub> F <sub>2</sub>	A8 A5 A5	2 <sup>tn</sup> ,19 1 ,26 0 ,90	+0 <sup>M</sup> ,3 +0 ,6 +1 ,0	+2 <sup>17</sup> ,5 +1 ,9 +1 ,9	0,43 0,60 0,74	1,37 1,42 1,13	28 36 75

The result derived on the basis of Seares's theory is in conflict with other evidence concerning the mass-ratios in binaries and it does not seem very probable that so many systems like those of 85 Pegasi and  $\beta$  Lyrae should exist. It seems that  $\blacksquare$  revision of the data used by Seares would be of much interest

<sup>&</sup>lt;sup>1</sup> Harv Ann 85, No 5 (1923) <sup>8</sup> AN 225, p 305 (1925)

<sup>&</sup>lt;sup>2</sup> Lund Medd Ser II, No 48 (1927).

Ap J 55, p 179; Mt Wilson Contr 226 (1922)

234. Jeans's Theory. Sir James Jeans has brought rather severe criticism against Eddington's researches on the mass-luminosity relation. It is not possible to give a full account here of the contents of Jeans's papers or to declare which method is to be preferred. It seems that the results reached by both the eminent authors by means of analysis do not differ very much as regards a good representation of the observational material.

JEANS claims that, when the problem is treated in a sufficiently general way, the supposed mass-luminosity law disappears entirely as a theoretical law, so that a star of given mass can always adjust itself so as to radiate energy at whatever rate may happen to be required by the generation of energy in its interior A general relation is found to exist between the mass, luminosity and surface-temporature so that the said adjustment can be made in only one way. The whole interior constitution of a star is uniquely determined by its mass and its rate of generation of energy

The main point of difference between Jeans's work and that of Eddington is that the former considers the ratio  $\lambda$ , gas-pressure over radiation-pressure, or  $\beta/(4-\beta)$  to vary within one and the same star, whereas Eddington assumes this quantity to be constant throughout a star. Jeans is of opinion that in those cases most favourable for constancy  $\lambda$  varies  $\infty$   $T^{\frac{1}{2}}$  and that a variation of 1000 between different regions in the same star can hardly be dismissed as impossible.

The gas-pressure, p, and radiation-pressure, q, are defined as follows.

$$\phi = \frac{\Re}{m\mu} qT; \quad q = \frac{1}{3} \epsilon T^4,$$

where m is the mass of the hydrogen atom, a the radiation constant,  $\mu$  the mean molecular weight,  $\Re$  the universal gas-constant, and  $\varrho$  the density

The dynamical equation of equilibrium is then

$$\frac{d}{dr}(p+q) = -\frac{70}{r^2} \int_{r}^{r} 4\pi_{\theta} \varrho r^{\theta} dr, \qquad (1)$$

Where  $\gamma = 6.66 \cdot 10^{-8}$  (gravitation constant).

If H is the outward flux of radiant energy per unit area, then the equation of transfer of radiation is.

$$H = -\frac{16\sigma T^0}{360} \frac{\partial T}{\partial \tau} \tag{2}$$

where  $\sigma$  is STEFAN's constant of radiation =  $\frac{1}{2}aC$  and c the opacity of the star at the point considered. The energy is generated at a rate of  $4\pi a$  per unit volume and the average value of s inside a sphere of radius r is denoted by  $\bar{s}$ . The flux of energy accross a sphere of radius r surrounding the centre of the star must be equal to the total generation of energy inside this sphere so that

$$4\pi_{\bullet}r^{\bullet}H=4\pi_{\bullet}\int_{0}^{r}4\pi_{\bullet}s\varrho r^{\bullet}dr$$

The second of the above equations then takes the form

$$\frac{4aCT^{k}}{3o}\frac{dT}{d\tau} = -\frac{\bar{a}\varrho}{r^{k}}\int_{0}^{r} 4\pi_{k}\varrho r^{k}dr$$

<sup>&</sup>lt;sup>1</sup> MN 85, p 196 (1925).

All theories agree that the main part of c is  $\sim \varrho/\mu T^3$  Eddington assumes an additional factor  $T^{-1}$  and Jeans puts  $c = \frac{\varkappa \varrho}{\mu T^3} T^{-n}$ , where  $\varkappa$  is a constant. The integral, that is common to the equilibrium-equation and the radiation-transfer-equation can be eliminated and then the following is obtained

$$\frac{d}{dr}(p+q) = \frac{3C\Re\gamma}{a\kappa m} \frac{T^n}{\bar{\epsilon}} \frac{q}{p} \frac{dq}{dr}$$

Further it is assumed that  $\tilde{\epsilon} = \tilde{\epsilon}_0 T^l (l)$  being a small and positive constant and  $\tilde{\epsilon}_0$  another constant). This expresses the tendency of  $\tilde{\epsilon}$ , the average generation of energy, to decrease from the centre as we pass out to the cooler external regions

We can now put 
$$\frac{\mathcal{I}^{n-l}}{\overline{\epsilon}_n} = \zeta q^s \tag{3}$$

where, since  $q = \frac{1}{2} a T^{1}$ , we have 4s = n - l Putting  $p = \lambda q$  and denoting  $K = \frac{3}{a \times m} \frac{C \Re \gamma \xi}{a \times m}$  the equation (3) becomes

$$q\frac{\partial I}{\partial q} = \frac{Kq^*}{I} - (\lambda + 1)$$

or taking  $Kq^s = x^2$ .

$$\frac{1}{2}\operatorname{st}\lambda\frac{\partial\lambda}{\partial\nu}=v^{2}-\lambda(\lambda+1)$$

The most general solution of this equation is obtained by assuming for  $\lambda^2$  an expression of the form

$$\lambda^{2} = x^{8} (A + B x^{-1} + C x^{-2} + D x^{-3} + \cdots + x^{-4/8} (\alpha + \beta x^{-1} + \gamma x^{-2} + \delta x^{-3} + \cdots + y^{-8/8} (\cdots)) + \cdots$$

The method of equating coefficients of equal powers leads to

$$\lambda^{2} = \frac{2}{s+2} x^{2} \pm \frac{4}{s+4} \left(\frac{2}{s+2}\right)^{\frac{1}{2}} x + \frac{2}{s+4} \pm \frac{4(s+2)}{(4-s)(s+4)^{2}} \left(\frac{2}{s+2}\right)^{-\frac{1}{2}} x^{-1} + \cdots + \alpha x^{-\frac{1}{2}} \left[1 \mp \frac{2}{s} \left(\frac{s+2}{2}\right)^{\frac{1}{2}} x^{-1} \right]$$

The first part of this equation is the standard solution for  $\lambda^2$ . In the interior of a star, in regions where x is large in comparison with its value at the boundary, the actual solution may be supposed to coincide with the standard solution. The series in which the standard solution is expressed is convergent in the special case of s=0 as long as  $Av^2>\frac{1}{4}$  or  $\lambda>0.207$  or  $1-\beta<0.828$ , which corresponds to a mass less than 1240. When s is  $\pm 0$  the limits of convergence will be different but as the value of s will be small the series can be assumed to converge for all reasonable mass-values.

Further it is shown that p+q can be taken equal to  $S\varrho^n$ , where  $n=k\varphi$  and  $\varrho \sim \mu \varrho^p$ 

The mass of a star is found from the equilibrium-equation to be

$$\mathfrak{M} = -\frac{r^2}{\gamma \rho} \frac{d}{dr} (p+q) = -\frac{r^2 S_{11}}{\gamma} \varrho^{n-2} \frac{d\varrho}{dr}$$

The equilibrium-equation is transferred to the standard form discussed by Emden<sup>1</sup>, viz.

 $\frac{1}{R^2}\frac{d}{dR}\left(R^2\frac{d\sigma}{dR}\right)+\sigma^{\frac{1}{n-1}}=0,$ 

<sup>&</sup>lt;sup>1</sup> Gaskugelu p 61 (1907)

where  $r^2=\frac{\pi S}{(n-1)\,4\pi_{e7}}R^2$  and  $\varrho^{n-1}=\sigma$  The only solutions of astrophysical interest are those for which  $d\sigma/dR$  vanishes when R=0. The most general solution will be

$$\sigma = /\sigma_1, \quad R = /\frac{n-2}{2n-2}R_1$$

where f is a constant and  $R_1$  and  $a_1$  refer to the particular solution tabulated by EMDEN When  $\lambda$  is large the expression for  $\Re$  becomes:

$$\log \mathfrak{M} = \frac{3}{4(2s+3)} \log \bar{s}_0 + \frac{3n-4}{2n-2} \log f + \text{const.},$$

where the constant term contains only absolute constants of nature.

For very small values of  $\lambda$ 

$$\log 2R = \frac{6}{4s+3}\log s_0 + \frac{3n-4}{2n-2}\log f + \text{const.}$$
 (4)

The consideration is restricted to the simple case l=0, which corresponds to uniform generation of energy. Then the emission E is equal to  $4\pi_s \tilde{c}_s \mathfrak{D}_s$  or.

$$\log \bar{s}_{\bullet} = \log E - \log \Re + \text{const}$$

The two equation (3) and (4) then take the form

$$(2s+3,75)\log \mathfrak{M} = \frac{3}{4}\log E + (2s+3)\left(\frac{3n-4}{2n-2}\right)\log f,$$

$$(4s+9)\log \mathfrak{M} = 6\log E + (4s+3)\left(\frac{3n-4}{2n-2}\right)\log f$$

At the surface of the star the following equations are valid

$$\frac{1}{3} a T^4 = \frac{E}{8\pi \cdot Cr^2} = \frac{(n-1) \cdot 7}{2Cn SR!} E / \frac{n-2}{n-1}.$$

Hence.

$$4\log T = \log E - \log S - \left(\frac{n-2}{n-1}\right)\log f + \text{const}$$

and from the dynamical equation of equilibrium combined with the equation by Emden  $\log \mathfrak{M} = \frac{3}{2} \log S + \left(\frac{3n-4}{2n-2}\right) \log f + \text{const}$ 

If S is eliminated from these last two equations we have

$$4\log T + \frac{2}{3}\log \mathfrak{M} = \log E + \frac{2}{3(n-1)}\log I + \text{const}$$

By eliminating f from this equation and (4) and introducing absolute magnitude and temperature the resulting equation becomes:

 $c_1 \log T + c_2 \log \mathfrak{W} + c_1 M = \text{const.}$ 

where:

$$c_1 = 36(\varphi - 1) + 18(\varphi - 24) s$$
,  
 $c_8 = -(2s + 3,75) + 6(\varphi - 1) + (3\varphi - 4) s$ ,  
 $c_9 = 0.3[-1 + 12(\varphi - 1) + (6\varphi - 8) s]$ .

If the values of T, M and  $\mathfrak{M}$  were known for at least three stars with very high accuracy, it would be possible to use the data to evaluate the ratio of  $c_1: a_1, c_3$  and so to determine the values of  $\varphi$  and s. Instead an average solution of six stars (Sun, Capella A and B,  $\alpha$  Centauri A and B, and Sirius A) was carried out. The best fit is obtained from the approximate expression:

$$\frac{1}{2} \log T + 8.75 \log \mathfrak{M} + M = 11.17$$

The computation of the values of s and  $\varphi$  led to impossible results and then the equation was adjusted to

$$M + 2 \log T + 11,92 \log \mathfrak{M} = \text{const}$$
 (\lambda \text{large})

For stars of small &s the following equation was derived

$$M + 4 \log T + 3,25 \log \mathfrak{M} = \text{const}$$

Jeans points out that these results are in some respects in very good agreement with those obtained by Eddington. For small masses ( $\lambda$  large) the equation of Jeans shows that for T = const the total rate of energy-emission  $\varepsilon$  is  $\sim \mathfrak{M}^{1,7}$ , whereas in Eddington's theory it is  $\sim \mathfrak{M}^{1,1}$ . For stars of very great mass Jeans finds  $\varepsilon \sim \mathfrak{M}^{1,3}$ , while Eddington has  $\varepsilon \sim \mathfrak{M}^{1,1}$ 

EDDINGTON'S theory, which was based on the assumption s = 0, predicted a hard-and-fast relation between the rate of emission of radiation and the mass  $\mathfrak{M}$ . This relation will be represented by a single curve in a diagram in which s and  $\mathfrak{M}$  are taken as coordinates. According to Jeans's theory there is an infinite number of such curves in the s and  $\mathfrak{M}$  plane as soon as s differs even infinitesimally from zero. The only part of the plane that is ruled out is that in which the star would not be in a gaseous state

The two equations for  $\mathfrak{M}$ , T, and M give the limiting forms of the curves in regions where  $\mathfrak{M}$  is small and large respectively, and from these the assembly of curves can be constructed as in Jeans's fig 2. Eddington's curve would be approximately represented by any one of the curves for which T= constance and the element of the curves for which T= constance temperature constant during its evolution, so that evolution along a mass-luminosity curve would seem to be entirely improbable

One of the curves in the diagram will correspond to the temperature  $T_1$  which divides dark stars from visible ones. The observed values will, of course, all fall above that curve. A surface temperature  $T_2$  may also be imagined such that when the surface of a star has temperature in excess of  $T_2$  it radiates energy with such extreme rapidity that its surface temperature falls almost immediately below  $T_2$ . The observed stars will fall below that upper-limit curve. This seems to agree approximately with the observed facts as for instance shown in Eddingson's diagram

In a subsequent paper 1 Jeans assumes a solution in ascending powers of s of the differential equation treated above as follows

$$\lambda = \Lambda_0 + s \Lambda_1 + s^2 \Lambda_2 + \cdot$$

and finds:

$$\lambda = \left[ \left( x^2 + \frac{1}{4} \right)^{\frac{1}{2}} - \frac{1}{2} \right] + \left\{ -\frac{x^2}{4x^2 + 1} \right\} A_0 s - \left[ \frac{x^4 + x^2}{(4x^2 + 1)^2} + \frac{x^4 - x^2}{2(4x^2 + 1)^2} \right] A_0 s^2 + \cdots,$$

where  $A_0 = (x^2 + \frac{1}{4})^{\frac{1}{2}} - \frac{1}{2}$ 

The solution is rapidly convergent for small values of s. It is found from the data that the closest fit is for s around 1/18. For such values the terms containing  $s^2$  can be omitted. A table in the paper gives  $A_0$ ,  $\psi_0 = \frac{A_0}{s}$ ,  $1 - \frac{s^2}{4s^2 + 1}$ ,  $1 - \beta$  and  $\mathfrak{M}$  with s as argument

By using the new expression of the mass-luminosity law the following is derived, viz

$$(2s+2.5)\log M + 4s\log T - (s+0.5)\log E + (2s+4)\log \mu + (4s+7)\log \psi = \text{const}$$

<sup>1</sup> M N 85, p 394 (1925)

In this formula  $\psi = 1/x$  and  $\log E = -0.4M + \text{const.}$  Introducing M we obtain

$$(2s + 2,5)\log M + 4s\log T + 0,2(2s + 1)M + (4s + 7)\log \psi = \text{const.}$$

From the six stars used before the value s = 1/18 is derived and hence

$$m + \log T_0 + 11,75 \log M + 32,5 \log \psi_0 = 8,332$$

A comparison has been made between this formula and Eddington's material by J Ohlsson<sup>1</sup> The agreement is just as good as between Eddington's formula and his material

In a reply to JEANS's criticism EDDINGTON<sup>2</sup> states that the principal point at issue is the dependence of M on  $T_s$ . He writes the fundamental equation of the theory in the form:

$$\begin{split} d\left(p + \frac{1}{3} a T^4\right) &= \frac{4 \pi_0 c G \Re}{L \bar{a} u} d\left(\frac{1}{3} a T^4\right), \\ d\left(p + \frac{1}{3} a T^4\right) &= -g_Q dr, \end{split}$$

where p is the gas-pressure,  $\frac{1}{4}aT^n$  the radiation-pressure, E the mass, L the energy radiated per second, e the absorption coefficient, e the velocity of light, E the constant of gravitation;  $\tilde{e}$  is unity at the boundary and varies inwards in a way determined by the distribution of the source of the star's energy. As long as the mass is unaltered the solutions of these equations are homologous. If, keeping the mass of every element fixed, we multiply its linear dimensions by E, the following factors must be introduced: E is multiplied by  $E^{-1}$ , e is unaltered. The equation then continues to be satisfied. Hence

$$L \sim R^{-n}$$

Purther:

$$L = 4\pi_a R^a \frac{1}{4} a c T_a^i$$

By eliminating R and converting into absolute magnitude:

$$-\delta M = \frac{10\pi}{2+\pi} \delta \langle \log T_4 \rangle.$$

For Eddington's law of absorption  $n=\frac{1}{4}$ , and the same correction is obtained as was given in his paper of 1924. To make n differ greatly from  $\frac{1}{4}$  would, as Eddington states, "be to reject altogether the law of absorption on which I have based my conclusions; but, of course, I do not suppose the law to be exact, and I have nothing against values of n reasonably near to 1, say, between 0 and 1".

EDDINGTON points out that if a given rate of generation of energy is greater than the rate of radiation L, fixed by the formula, then the energy of the stars is increasing, and the star is expanding indefinitely. By the above formula L varies as  $R^{-s}$  and therefore diminishes.

An analysis of Jeans's paper has convinced Eddington that there is nothing singular about his value  $n = \frac{1}{4}$  and that the exponent 4 does not affect the magnitude-mass-temperature relation in the two cases considered. Furthermore the mass-luminosity relation is not reached by treating  $\lambda$  as a variable quantity. Jeans's generalisation of the problem consists in limiting  $\lambda$  between the two values 0 and  $\infty$ .

M N 85, p 403 (1925).

Lamd Medd Ser II, No 48 Also thesis Land (1927)

235. The Cosmogonic Time-Scale by Jeans and Smart. The results reached by von der Pahlen (cf ciph 216) could certainly be improved if the cosmogonic time-scale established by Jeans of Eddington (see ciph 232) were used. The procedure according to Jeans was taken into account that possibly positive and negative electric charges fall together and annihilate one another, their energy being transformed into radiation. The discovery of the mass-luminosity relation increased the probability of this conjecture enormously.

$$\frac{d\mathfrak{M}}{dt} = -\alpha \mathfrak{M}^3,$$

where  $\alpha = 5.2 \cdot 10^{-88}$  is found by taking the values for the solar system  $\mathfrak{M} = 2 \cdot 10^{33}$ ,  $-\frac{d\mathfrak{M}}{dt} = 4.2 \cdot 10^{12}$  Solving the equation he finds the time required for a star to pass from mass  $\mathfrak{M}_A$  to mass  $\mathfrak{M}_B$  to be given by

$$t = \frac{1}{2\alpha} \left( \frac{1}{\mathfrak{M}_B^*} - \frac{1}{\mathfrak{M}_1^*} \right)$$

JEANS has also given in this connection the following interesting theorem concerning the relation between mass and size of orbit of a star

From the motion of a particle under a central force  $\mathfrak{M}/r^2$  the equation

$$\frac{d}{dt} \left[ \frac{1}{2} \left( \left( \frac{dr}{dt} \right)^2 + r^2 \left( \frac{d\theta}{dt} \right)^2 \right) - \frac{\mathfrak{M}}{r} \right] = -\frac{1}{r} \frac{d\mathfrak{M}}{dt}$$

is readily deduced1, which becomes

JEANS has derived the relation1

$$\frac{d}{dt} \binom{\mathfrak{M}}{2a} = \frac{1}{r} \frac{d\mathfrak{M}}{dt}$$

when a is the major axis of the orbit

Averaging over a complete revolution, JEANS finds

$$\frac{d}{dt}\left(\frac{\mathfrak{M}}{2a}\right) = \frac{1}{a} \frac{d\mathfrak{M}}{dt},$$

from which follows

$$\mathfrak{M}a = \text{const}$$

If our Sun ever was a B star or if its mass ever was 40 the time elapsed since this epoch must be about 7.1 · 10<sup>12</sup> years

SMART<sup>2</sup>, who has connected the above differential equation with the theory of Eddington, finds a scale in substantial agreement with that of Jlans. By three different procedures he has derived the following values of t necessary for a star to pass from different values of  $\mathfrak{M}_A$  to  $\mathfrak{M}_B = 10$ 

The scale must be still longer, because no account is taken of the increase in mass necessary on account of the meteor frequency. The investigations of the frequency of meteors show that they are not restricted to our solar system but are universal phenomena. Taking into account the frequency of meteors we find that the mass of the Sun will be doubled during a period of 10<sup>18</sup> years. Thus the increase of the stellar mass due to encountering meteors will partly counterbalance the secular decrease of the mass.

<sup>&</sup>lt;sup>1</sup> M N 85, p 2 (1924)

<sup>&</sup>lt;sup>3</sup> M N 85, p 423 (1925)

286. Bril's Theory and Parallax-Method for Binaries. According to the theory of radiative equilibrium  $hs^{\frac{1}{4}}$  should be constant within a certain star (\* is the mean absorption coefficient of the total radiation) but should vary from star to star with the size of the mass. If we assume the relation.

$$1 - \beta = 7.83 \cdot 10^{-10} 100^{0} \mu^{4} \beta^{4}$$

to hold good, it follows from statistical considerations of data concerning magnitudes, parallaxes, and masses that the relation.

holds good for nearly all stars. In order to see the reason for this we must transform the expression. If a is the constant in Stepan's law and M is the gas constant, we have the equations:

$$\varrho = \frac{\mu a \beta}{3 \Re (1 - \beta)} T^0,$$

$$h = 3.28 \cdot 10^{37} \cdot \frac{a}{3 \Re 1 - \beta} T^{-\frac{1}{2}}.$$

Further the contral temperature  $T_o = 4.7 T$  is introduced and the radius R Then:

$$T_o = \frac{6.9011 \Re}{\mu \beta R} \left( \frac{3(1-\beta)}{\kappa_0 a G} \right)^{\frac{1}{6}}.$$

According to the definition-equation

$$1 - \beta = \frac{40}{45.0G}$$

and thus.

$$\varepsilon = \frac{12\pi_{\circ} G \Re}{3,28 \cdot 10^{47}} \frac{(1-\beta)^{0}}{\beta} \left(\frac{T_{\circ}}{1.7}\right)^{\frac{1}{2}}$$

and.

The central temperature is rather constant, varying as it does between  $35 \cdot 10^6$  and  $40 \cdot 10^6$  degrees. The constancy of  $hs^{\frac{1}{6}}$  is mainly determined by the quantity  $\beta^{\frac{1}{6}}$ . If  $\mathfrak{M}$  varies between  $10 \odot$  and  $0.16 \odot$ , the corresponding variation in  $\beta^{\frac{1}{6}}$  is from 0.73 to 1.00.

Independently of the theory of the stellar absorption coefficient the quantity has can be expressed in quantities furnished by observational work. If the stars are in radiative equilibrium, the radiated energy is equal to the energy produced in the interior of the star:

$$\pi_{\bullet}acR^{2}T^{i}_{\bullet}=s\mathbb{R},$$

where  $T_4$  is the radiation temperature

If the value of  $ks^{\frac{1}{2}}$  from the above definition-equation is substituted in the present expression, k becomes equal to  $4G(1-\beta)\Re(\kappa R^{\frac{1}{2}}T_{0}^{\frac{1}{2}})^{-1}$  and thus:

$$h\sqrt{s} = 4G(\pi_s s)^{\frac{1}{2}} s^{-\frac{1}{2}} (1-\beta) \mathfrak{M}^{\frac{1}{2}} R^{-1} T_s^{-2}.$$

Introducing the numerical values of the constants and selecting solar units we obtain as the final equation:

$$\log k \sqrt{\varepsilon} = 3.459 + 2\log\frac{a_0}{T_0} - \log\frac{R}{R_0} + \log(1-\beta) + \frac{1}{2}\log\frac{\Re k}{\Re R_0}.$$

Berlin-Babelsberg Veröff 7, H i (1927)

In order to determine the numerical value of  $k\sqrt{\epsilon}$  the material of RABE<sup>1</sup> (38 pairs  $\pi < 0''$ ,040) and that of Bottlinger<sup>2</sup> (17 eclipsing variables) together with data for the Sun and Capella were used. The value 2,85 for  $\log k\sqrt{\epsilon}$  resulted from 68 stars

Brill discusses at length the derivation of  $T_{\rm e}$ , the radiation temperature corresponding to the radiation temperature of the bolometric magnitude of the central part of the star disc. The colour temperature of a star refers to the course of the energy curve in a certain part of the star spectrum and corresponds to the

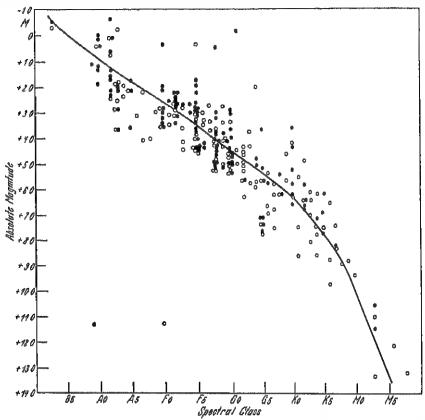


Fig 155 The Russell diagram as derived by Brill on basis of parallaxes of binaries using the theoretical relation \*kst\* = const\* Full circles refer to primaries and open circles to secondaries of binary stars

temperature of a black body radiator whose energy curve in the same part has the same form as that of the star. The radiation temperature refers to the intensity of the emitted radiation and corresponds to a black body radiator that emits radiation in equal intensity to that of the star. If the conception of effective temperature is to be preserved it ought to be defined as the temperature of a star for which the total emission of a black body radiator equals that of the star.

In order to obtain accurate values of the colour temperature it is necessary to supplement the visual and photographic measurements with bolometric,

<sup>&</sup>lt;sup>1</sup> A N 225, p 217 (1925).

<sup>&</sup>lt;sup>2</sup> Atti della Pontificia Accad (1924).

radiometric, and thermoelectric measurements in the ultra-red. The radiation temperature cannot be determined without a knowledge of the stellar diameter. Only a few stars have been measured as yet with interferometric methods; thus our knowledge of the radiation temperature is very restricted. For the Sun the following values of the radiation temperature are derived

Endiation temp of the Sun from Biology, data Visual data Photogr data Moan solar radiation . 5775° 6075° 5835° Contral solar radiation 6075° 6435° 6190°

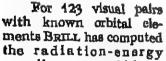
The following are the results from the stars:

Object	Spectral class	Rallys	Apprent magnitude	Rad temp. of the vis. magn.	Colone temperatura
Sun . Arcturus Akicharan Butelgeuze Antares 8 Pogusi	G0	961",2	-26=,90	c_T = 2,36	c <sub>y</sub> /T=2,05
	K0	0 ,0100	+ 0 ,24	3,44	3,50
	K8	0 ,0100	+ 1 ,06	3,82	4,39
	M1	0 ,0235	+ 0 ,92	4,69	4,65
	M2	0 ,0200	+ 1 ,22	4,66	4,77
	M3	0 ,0105	+ 2 ,61	4,66	4,61

At present we can do no better than assume equality between the radiation and the colour temperature.

The following temperature scale was assumed.

- 1	ture sem	6 Weig 1189	umed.	+47	_\$		_	Ц.
	Special diss	7	NT	- 40		$\nabla$		Γ
	Os	28 000°	0,51	+45				Γ
	330	20800	0,69	+4				ſ
	<b>3</b> 5	16900	0,85	+40			7	k
	Ao As	13000	1,10	+41				┡
	Fo	10200 8300	1,40	rdBar		<u> </u>	-	Ľ
	gF3	7200	2,00					L
	dF5	7 200	2,00	1 1				Г
	gGo dGo	6 050 6 240	2,37	-41				┢
	gG5	4880	2,30 2,96	7-4		Н	_	ŀ
	dGs	5 560	2,58	-40		-	-	-
	gK0 dK0	4310	3,33	-46				L
	gK5	4 910 3 380	2,92 4,24					L
	dK5	3 940	3.67	749				
	gMo	3 200	4.49	~**			_	r
	dMo	3420	4,20	~2	•	_		_



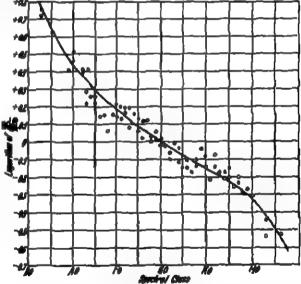


Fig 156. Relation between logarithm of stellar mass and spectral class according to BELL. Full circles refer to primaries in binary stars and open circles to secondaries.

parallaxes  $\pi^{m}$ , which enter into the expression log  $R/R\odot$  owing to the relation:

 $\log R/R_{\odot} = 0.2 (M \rightarrow m - \Delta m) - \log n_m + 4.946$ 

where M is the surface-intensity magnitude, m the apparent visual magnitude and  $\Delta m$  the correction to bolometric magnitude. The computation of  $n_{20}$  has to be performed by means of successive approximations. For this purpose an extensive table is given in Brill's paper with  $1-\beta$  as argument,  $\log (1-\beta)$ ,  $\log \mathbb{R}/\mathbb{R}_{\odot}$ , and  $\Delta \log (1-\beta)$ ;  $\Delta \log \mathbb{R}/\mathbb{R}_{\odot}$  as functions. Further the expressions  $\frac{1}{2} \log \mathbb{R}/\mathbb{R}_{\odot} + \log (1-\beta)$  and  $\Delta \log \mathbb{R}/\mathbb{R}_{\odot} \cdot \Delta \left(\frac{1}{2} \log \mathbb{R}/\mathbb{R}_{\odot} + \log (1-\beta)\right)$  are given in order to facilitate the necessary interpolations.

The agreement between  $\pi_{ro}$  and  $\pi_{tr}$  or  $\pi_{s}$  is very good indeed. The masses, mass-ratios, dimensions, densities, and central temperatures are also determined and entered in the catalogue.

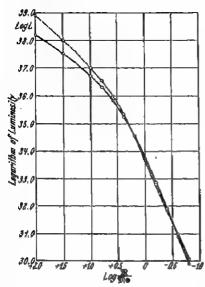


Fig. 157. Relation between logarithm of stellar luminosity and mass. The full-drawn curve is the relation derived by Brill on the assumption that kell const. and the dotted curve is the relation according to Eddington.

The agreement of the derived Russell diagram with the observed one shows that the relation between the mass and the product  $ke^{\frac{1}{2}}$  as derived by Eddington is in agreement with the observations. Furthermore it also proves the probable reality within a wide range of the formula of Brill ( $ke^{\frac{1}{2}}$  = const), which is partly based on the theory of radiative equilibrium and partly on an empirical foundation.

The agreement between the mass-luminosity relation according to Eddington and according to Brill is very good. There are practically no deviations for the luminosity range  $\log L = 30.0-36.5$  (M8 to B0 stars roughly) or for the entire main series.

287. Mass-Reduction by Annihilation of Protons and Electrons. C. Lönnguist<sup>1</sup> has examined various hypotheses concerning the evolution on the basis of Eddington's theory by using the empirical Russell diagram as guidance and test.

The investigations of EDDINGTON in 1924 showed that it is the difference in mass and not in intensity that causes the considerable difference in the luminosity

of the giants and dwarfs. Although it is still possible that the stars develop from the giant stage to the dwarf stage in the traditional way there is no longer any explanation why they should develop in just that way. But if such an evolution takes place, then the mass reduction must be investigated. Such a reduction is not only dependent on a possible throwing off of matter into space. The stars also radiate away enormous quantities of energy, and as energy is equivalent to mass the stellar masses must be diminished in the course of time, if no compensating factors exist.

It has been shown by EDDINGTON that the energy lost by radiation cannot be fully compensated by the energy liberated by contraction since the time-scale thus obtained is altogether too short. If the mass 11,5 © is taken, such a contraction-development from the giant M to the giant F stage would take only 30000 years, and for the Sun itself 1,5 • 107 years. From geological evidence it is found that the age of the Earth must be 109 years at least and the minimum age of the Sun ought to be at least 1010 years.

The investigations of F. W. ASTON in 1920 gave rise to the hypothesis of EDDINGTON<sup>2</sup> that the helium in the stars is built up of hydrogen. This process involves a change of 0,008 of the mass into energy. It seems also that something

<sup>&</sup>lt;sup>1</sup> Ark Mat Astr Fys 20 Λ, No. 21. Also thesis Upsala (1927).

<sup>&</sup>lt;sup>1</sup> Brit. Assoc. Report 1920, p. 45. This theory seems also to have been presented independently by J. Perrin: Annales de Physique 2, p. 89 (1919), and Revue du Mois 21 p. 113 (1920).

similar can be postulated concerning the composition of other light atoms, but the effects in these cases might be considerably smaller. It seems hardly possible to reach an amount exceeding 0,010 of the mass. The time the Sun would require for such a mass-reduction is 1,5 · 10<sup>11</sup> years, which is sufficient for geological demands if the Sun has from the boginning an abundance of hydrogen of 10 per cent. But if this hypothesis is accepted the evolution will principally follow a mass line, as has been pointed out by Lönnguist, and the Russell diagram cannot mark the evolution-course of the stars, but only the loci of the most stable equilibrium points of the stars

EDDINGTON points out that helium must have been produced somewhere The doubts of some physicist that the interior of the stars may not have a sufficient temperature are met with the advice "to seek a hotter place" EDDINGTON seems to assume that the processes of building up the atoms already occur in the nebulae so that they have taken place to a great extent while the stars are in an early stage of evolution. The stars can hardly contain hydrogen any longer. EDDINGTON's arguments against the occurrence of hydrogen in the

stars are based on the following views.

A large percentage of hydrogen would decrease the molecular weight  $\mu$  so much that the radiation pressure would become insignificant in comparison with the gas pressure even in case of the most massive stars known. The radiation pressure would lose most of the importance ascribed to it as an explanation of the fact that the stellar masses are situated within comparatively narrow limits

On account of the change in the value of  $\mu$ , entering in the luminosity formula with the expression  $\mu^{\sharp}$ , a considerable amount of hydrogen would alter the mass-luminosity relations. Besides, if the abundance of hydrogen differed for stars of the same mass, the stars would not lie along a mass-luminosity line, but would exhibit greater or smaller deviations from it. Lönnquist finds from a lengthly discussion that the assumption of the importance of the radiation pressure for the size of the star-masses is untenable, and that it does not form any valid argument against the presence of hydrogen in the stars. While a not inconsiderable proportion of hydrogen appears necessary for Capella in order to obtain agreement between the theoretical and observed luminosity, varying proportions of hydrogen in stars of the same mass appear to lead to not inconsiderable deviations from the luminosity as computed from EDDINGTON's luminosity law. The testing of that law by means of stars of known masses and lummosities cannot be made with such accuracy as to allow a decision concerning the nature of the individual deviations. The theory requires special revision as regards the abundance of hydrogen.

The radioactive hypothesis cannot explain, in its original form, a considerable mass reduction. The radioactive processes have, as far as is known, the property of being independent of temperature and density. In order to have an important mass reduction one would have to imagine, with Jeans, another kind of radioactivity. He has suggested an annihilation of matter within the atom nuclei together with a liberation of energy. To describe this as radioactive would then be an accentuation of these processes—just like the radioactive—being inde-

pendent of density and temperature.

JEANS'S theory introduces a third hypothesis, the boldest of them all, namely the annihilation of protons and electrons with transformation of the mass into energy. This idea is not new and it arose even before the question of the evolution of the stars had advanced any considerable way. EDDINGTON mentions J. LARMOR as one of the precursors of this theory and as early as in 1904 JEANS expressed

himself in favour of this line of thought, while Eddington suggested the hypothesis for the first time in 1917. MACMILLAN also supposes the contrary process to take place, i.e. a transformation in space of the radiations of the stars into matter, into protons and electrons from which the nebulae arise. In this way a circulation is obtained between mass and energy, which is certainly of much importance for cosmology

The annihilation of protons and electrons may be supposed to be a nucleus process analogous to the radioactive ones or the result of a collision between a free electron and a nucleus proton. EDDINGTON conceives both possibilities In the former case the process evades every calculation regarding dependence on the outer physical conditions. The process might possibly depend on the very constitution of the atom nucleus. In the second case the density and

temperature may be thought of as deciding the rate of the process.

Lönnguist's paper is partly devoted to an examination in detail of the second of the above-mentioned cases, which the author calls the hydrogen hypothesis. He finds that the known facts concerning the components of the double stars seem on the whole to agree with the hydrogen hypothesis. For the development of the widely separated binaries from close pairs an evolution with mass reduction seems necessary. The long time-scale associated with such an evolution is of extreme importance for cosmogonic problems. The evidence of the clusters has also been investigated. The facts scarcely decide in favour of one or the other theory of evolution, but they do not seem to confirm Russell's evolution scheme. Stars are probably formed with very different masses. Only the larger ones are checked in the giant stage, while the smaller ones go directly into the main series.

288. The Theory of RABE. The aim of this investigation was to establish the relation between the absolute magnitude, the temperature, and the mass of dwarf stars. It has to be assumed that there exists a one to one relation between  $M=T_{\bullet}$ , and  $\mathfrak{M}$ , which is also in agreement with the empirical and theoretical results. On account of the comparatively high density of the dwarfs it is comparatively easy to define the conception of the stellar surface that is necessary for the theory developed. It is sufficient to start from the surface conditions of our Sun and to assume that the thickness of the layer from which the visible radiation has its origin is small in comparison with the radius of the star. But on the other hand, it has to be assumed that the layer in question has such radial extension that the surface radiation can be considered to be emitted by a black-budy radiator. Above such a surface a cooler atmosphere may be situated, which, of course, would absorb part of the radiation. The results of spectral analysis show that the amount of this absorption is comparatively small for classes earlier than F, but becomes appreciable in that class, and increases continuously to the end of the main series. The absorption is certainly selective so that the coefficient of transmission is a (unknown) function of the wave length. It is then necessary to use a mean value of the coefficient which is a function of the surface temperature and the mass, as the gravitative power exerts an influence on the general atmospheric condition of a star. The stars have to be assumed to be perfect spheres and the size of the surface is thus determined by means of the mass and tho mear density. This quantity can be considered, at least at a first approximation to be a function of the surface temperature and mass. Although BERNEWITZ' could not establish ■ definite relation between the mean density and the mass still the probability that such I relation exists is very greats.

<sup>&</sup>lt;sup>1</sup> A N 225, p. 217 (1925). <sup>8</sup> AN 213, p. 1 (1921). <sup>8</sup> In fact, such a relation was established by Abetti in 1922.

Let  $s_0$  be the intensity of radiation of a surface element,  $\phi$  the mean value of the coefficient of transmission, T the effective surface temperature, and o a factor of proportionality, then the observable radiation i of a surface element is

$$s = pi_0 = ap(c_0/I)^{-4}.$$

Let further  $\varrho$  be the mean density and C another factor of proportionality. Then the total radiation of I the star is

$$I = C (\mathfrak{M}/\rho)^{\frac{1}{2}} \phi (c_1/T)^{-4}$$

If this quantity is transformed into magnitudes we have:

$$M + \Delta M = \Phi + 10 \log c_0 / T - \frac{1}{2} \log \Re + \frac{1}{2} \log \varrho - \frac{1}{2} \log \varrho. \tag{1}$$

dM is the correction of the visual absolute magnitude M to belometric magnitude and  $\Phi$  a constant.

As a result of numerous trials RABE selected the following expression for  $\varrho$  and  $\dot{p}$ .

 $\varrho = c (c_0/T)_1^n \mathfrak{M}^1,$   $\phi = (T/T_0)^n \mathfrak{M}^n \le 1.$ 

 $T_0$  is the limiting temperature for which at unit mass an appreciable atmosphere sets in. The second equation does not seem very plausible from a theoretical point of view but RABE gives a reason for its use. If we pass over to solar units the above equation takes the form  $\varrho = (T_0/T)^* \mathfrak{M}^2$ .

Then the equation (1) takes the form

$$M + \Delta M = (10 + \frac{1}{2}\kappa + \frac{1}{4}\nu)\log c_0/T - \left[\frac{1}{4}(1-\lambda) + \frac{1}{4}\mu\right]\log \mathfrak{M} + \Phi - \frac{1}{4}\kappa\log c_0/T_0 - \frac{1}{4}\nu\log c_0/T_0.$$
 (2)

The unknowns  $\kappa$ ,  $\lambda$ , r,  $\mu$ , and  $T_0$  can be determined from the observational data. If  $\dot{p}$  should be larger than one, the terms containing  $\nu$  and  $\mu$  must be dropped. The masses were determined from 38 dwarf binaries with a parallax equal to or larger than 0",040. The values of  $\Delta M$  were derived from the radiation law of Planck and the spectrophotometric measurements of Wilsing. Further  $M_{\odot} = 4.79$ , the observed value of  $c_0/T$  for the Sun = 2,40,  $\dot{p}_{\odot} = 0.71$ , and hence  $c^0/T_{\odot} = 2.40 \cdot \dot{p}_{\odot}^{\dagger} = 2.20$ , and  $\dot{\Phi} = 1^{\rm m}.42$  were used.

Next the value of  $\lambda$  is determined. For stars earlier than F5 it has very nearly the value 1 and thus the density-ratio of such stars can be determined without any knowledge of  $\phi$ . The author finds  $\lambda = 0.293 + 0.012 \, \pi$ . The value of  $\pi$  is situated between 2.5 and 3 and the last value is adopted. The coefficient of log  $\mathfrak M$  in the above equation,  $b = -[4 (1 - \lambda) + \frac{1}{2} \mu]$ , is determined from binaries of equal spectra and varies with the spectral class:

Spectral class		л	Spectral class	à	
Go	1,98	11	K0	-2,28	7
G4	2,35		K4	-4,23	6

This, if real, suggests a complicated form for the functions  $\varrho$  and  $\dot{\rho}$ . At present it does not seem possible to decide whether the variation is real or not. If b is taken as -2.71,  $\mu$  is found to be  $\frac{1}{2}$ .

It is unavoidable that the determination of the different constants must be affected with some uncertainty owing to the paucity and in several cases the uncertainty of the data. RABE finds the following two formulae:

Stars without atmosphere (p=1):  $M_{\rm bol}=15\log c_{\rm s}/T-\frac{1}{2}\log \mathfrak{M}-0.29$ . Stars with atmosphere (p<1):  $M_{\rm bol}=20\log c_{\rm s}/T-\frac{1}{2}\log \mathfrak{M}-1.63$ .

In order to have one formula the following expression is adopted

$$M_{\rm bol} = \frac{1.5}{1} \log \frac{c_2}{T'} - \frac{2.5}{5} \log M + 0.90.$$

Here  $c_2/T'$  has to be selected in such a way that both the formulae are represented

The essential point in the theory of RABE is that M is considered to depend on the temperature much more than is the case in the theory of Eddington. The theory is of considerable interest and ought to be compared with the empirical data as soon as more observations have been collected.

The  $c_2/T$ -value in the above formulae corresponds to the surface temperature and is related to the effective temperature  $T_s$  in the following way

$$\log (c_2/T_s) = \frac{9}{2} \log \frac{c_2}{T} - \frac{1}{6} \log \mathfrak{M} - 0.134$$

The effective temperatures that result from the material of Rabe are in very good agreement with those computed according to the methods of Spares and of Brill If the  $c_2/T$ -values are diminished by ten per cent they are in very good agreement with the corresponding values derived by M N Saha¹ on the basis of his theory of ionization. It is certainly very interesting that the theory of Rabe is able to explain most of the differences between the results of Brill and Saha

Using the temperature-scale thus established RABE has computed the absolute magnitudes and the masses and derived the following mean errors

Spectral	14	fenn errors	
class	in M	in log M	11
A0—F9 G0—G9 K0—Mdp	士0 <sup>11</sup> ,34 土0 ,48 土0 ,32	士0,19 士0,17 士0,11	22 23 20

RABE then makes a revision of his system and finds from a discussion of the values of  $m_{\text{O}}$  and  $c_2/T_{\text{O}}$  a correction that should be added to the constants in his equation. He finds

$$\log \frac{c_2}{T} = \frac{1}{6} \log \varrho - \frac{1}{6} \log \mathfrak{M} + 0.342$$

For the application to binaries the equations giving the mass-luminosity relation are changed into the following forms:

Stars without atmosphere:

$$\log \pi = 9\log \frac{c_2}{T} - \frac{2}{3}\log \frac{\mathfrak{M}_A}{\mathfrak{M}_A + \mathfrak{M}_B} - 2\log a + \frac{4}{3}\log P - \frac{3}{5}(m+5+\Delta m_{\rm bol}) - 0.288.$$

Stars with atmosphere

$$\log \pi = -6\log \frac{c_2}{T} + \frac{5}{6}\log \frac{\mathfrak{M}_4}{\mathfrak{M}_A + \mathfrak{M}_B} + \frac{5}{2}\log \alpha - \frac{5}{3}\log P + \frac{3}{10}(m + 5 + \Delta m_{\text{bol}}) + 0.546.$$

Computing the parallexes and comparing with those actually determined RABE has found the mean error of one value to be  $\pm 0.295\pi$ .

The mass-ratio of stars where both the spectra have been observed but no orbital elements are known can be computed from the formula

$$\log\left(\frac{\mathfrak{M}_B}{\mathfrak{M}_A}\right) = \frac{9}{25} \left[ 20 \left( \log \frac{c_2}{T_B} - \log \frac{c_2}{T_A} \right) - (m_B - m_A) - (\Delta m_B - \Delta m_A) \right]$$

<sup>&</sup>lt;sup>1</sup> Zf Phys 6, p 40 (1921), Ap J 50, p 220 (1919), Phil Mag (6) 40, p 809 (1920), 41, p 267 (1921), London R S Proc (A) 99, p 135 (1921)

The following table summarises the results of RABE

Spectrali class	Temperature T	18	e	4	n
Λ 2,3	9400°	2,29 ⊙	0,43 @	1,74 ⊙	3
17 3,4	7900	2,78	0,77	1,42	- 11
17 8,0	6600	1,07	0,98	1,02	- 8
G 1,0	6400	0,92	0,98	0,96	12
G 6,0	6100	0,88	1,22	0,88	10
IX 1,7	5600	0,61	1,27	0,78	9
K 5,0	50 <b>0</b> 0	0,69	1,96	0,70	8
M 2,5	3800	0,36	3,58	0,45	4

The diameters d are accurately represented by means of the linear relation d = 1.03 + 0.00023  $(T - 6500^{\circ})$ .

In a subsequent paper RABE<sup>1</sup> has taken up a remark by BRILL that the mass and the surface temperature cannot be considered to be independent of each other. In order to decide between the influence of the temperature and the mass upon the absolute magnitude it is appropriate to consider stars of unequal mass but of the same spectral class. RABE used a number of new data, but could not find that his general conclusions ought to be changed. In order to show that the correlation between mass and luminosity is not as high as in generally believed he quotes the following well-determined cases where the absolute magnitude has been computed from Eddington's mass-luminosity law.

Object	Spanica) chas	12	My	Mod	Menin	Make - Made
M Pogasi A  y Virginis A  M Pogasi B  r Cygni A  Procyon A  Scorpli A  9 Argus A  B  Sun  Urs Majoris A	F3 F0 (F5) F1 F2 G0 (G2) G0 F9	8,60 © 4,48 4,00 2,48 1,13 1,02 10,96 4,38 1,00 0,68	1 <sup>24</sup> ,79 2 ,39 2 ,29 2 ,14 2 ,92 3 ,04 3 ,46 4 ,06 4 ,90 5 ,26	1 x,78 2 .37 2 .29 2 .12 2 .92 3 .03 3 .43 3 .98 4 .89 5 .25	-2×,42 -0 ,85 -0 ,45 0 ,96 3 ,92 4 ,29 -2 ,79 -0 ,41 4 ,56 6 ,28	+4*,20 +3 ,22 +2 ,74 +1 ,16 -1, 00 -1 ,26 +6 ,22 +4 ,39 +0 ,33 -1 ,03

The difference  $M_{\text{obs}} - M_{\text{calc}}$  shows such a definite dependence on  $\mathfrak{M}$  that it seems to indicate that M does not depend on  $\mathfrak{M}$  in such a high degree as was prodicted in the theory of Eddington.

The author gives the following mass-luminosity-temperature relation

Special class	Absolute magnitude	Tamparature	111	e/I
B0 B5 A0 A5 F0 F5 G0 G5 K0 K5	-3 <sup>M</sup> ,0 -0 ,4 +1 ,1 1 ,9 2 ,5 3 ,3 4 ,5 5 ,2 6 ,0 7 ,6	20400° 12400 9800 8900 8200 7300 6500 6100 5800 5000	15.7 O 7.2 3,8 2,2 1,8 1,4 1,10 0,94 0,75 0,63 0,43	0,70 1,15 1,45 1,60 1,74 1,95 2,20 2,33 2,47 2,85 3,43

<sup>&</sup>lt;sup>1</sup> AN 231, p 79 (1927).

289. Convergence of Mass-Ratios with Increasing Age. One of the important consequences of the theory of Eddington was pointed out by Vogt<sup>1</sup>. It follows from the theory that \( \Delta N \) waries in direct proportion to \( \Delta \). In the case of double stars the mass-ratio  $\mathfrak{M}_A/\mathfrak{M}_B$  must thus become smaller and more nearly equal to one the "older" the pair is. Vogr mainly made use of 85 double stars in LEONARD's dissertation<sup>9</sup>. The mass-ratios were not known and had to be computed from Eddington's mass-luminosity relation. In the table giving the results  $S_A$  denotes the spectral class of the principal star.

S₄	MA/MA	п	$S_A$	901 A f 301 B	11
gM gK gG gF B	18,4 2,7 1,9 3,0 4,6	2 6 9 5 8	A dF dG dK dM	1,6 1,3 1,25 1,23	9 23 18 11

In order to investigate the possibility that the mass becomes smaller with the age of the star, one can also make use of the relation:

$$\frac{\Delta \, \mathfrak{M}_A}{\Delta \, \mathfrak{M}_B} \! \sim \! \frac{L_A}{L_B} \, ,$$

where L is the luminosity. Voct computes the values  $[\mathfrak{M}_A/\mathfrak{M}_B]$  for a double star whose principal component is of spectral class A with a mass of 2,5 @ and  $\mathfrak{M}_A/\mathfrak{M}_B=1.6$  and whose components undergo in the course of evolution a massreduction in proportion to their luminosities. These values compare with the mass-ratios actually derived in the following way:

S₄	W <sub>A</sub>	[107] A   100 B ] obs	[Ma/Whale]
A F G K M	2,5 1,5 1,0 0,7 0,4	1,6 1,3 1,25 1,23 1,19	1,6 1,2 1,10 1,06 1,04

According to Vogt the probability is thus comparatively great in favour of the opinion that the Russill diagram gives the general course of stellar evolution.

240. Vogt's Extension of Edding-TON'S Theory. The theory of EDDINGTON

is based on the assumption that the product kQ is constant, where k is the coefficient of mass-absorption and Q the mean value of the energy produced per unit mass and time within a sphere with the radius r. H. Vogra has derived the mass-luminosity relation in the case when kQ is not constant, but varies in some general way with r. The two fundamental equations give:

$$L = \frac{4\pi_{c} a cg r^{2}}{3 k} \frac{dT^{4}}{dP} = \frac{4\pi_{c} cG}{k} \mathfrak{M} (1 - \beta) \left[ 1 + \frac{P}{1 - \beta} \frac{d(1 - \beta)}{d l^{2}} \right],$$

where  $dP = -g \varrho dr$ ,  $P = \Re \varrho T/\mu + \frac{1}{3} a T^4$  or the sum of the gas-pressure and light-pressure, and  $g = G\mathfrak{M}/r^2$ .  $\mu$  is the molecular weight, g the gravitational force,  $\varrho$  the density, T temperature,  $\mathbb{M}$  the universal gas constant = 8,26 · 107, and m STEFAN's constant =  $7.63 \cdot 10^{-15}$ . L and M correspond to the values within a certain radius r, but their total values may be introduced if P,  $1 - \beta$ , and k are referred to the layers near the surface. The equation can be transferred by applying the relations:  $T^4/T_1^4 = (1-\beta)/(1-\beta_1) \, \mathfrak{M}^3/R^4 \quad \text{and} \quad T/T_1 = \beta/\beta_1 \, \mathfrak{M} \, \mu/R$ 

$$T^4/T_1^4 = (1-\beta)/(1-\beta_1) \mathfrak{M}^2/R^4$$
 and  $T/T_1 = \beta/\beta_1 \mathfrak{M} \mu/R$ 

existing between  $1-\beta$ , M, and  $\mu$  in the case of homologous stars. In these equations the subscript one refers to a homologous star of unit mass, the

<sup>&</sup>lt;sup>1</sup> Z f Phys 26, p. 139 (1924). 8 A N 226, p. 302 (1926).

<sup>&</sup>lt;sup>B</sup> Lick Bull 10, p. 169 (1923).

radius and mean molecular weight of which are equal to one. By eliminating T between the above equations we get:

$$\frac{(1-\beta)}{\beta^4} = \frac{1-\beta_1}{\beta_1^4} \mathfrak{M}^0 \mu^4 = \varphi(\mathfrak{r}) \mathfrak{M}^0 \mu^4,$$

where  $\varphi(t)$  is a function of the distance  $\tau$  from the centre of the star expressed in units of the radius  $\tau$ . It follows from the last equation that:

$$\frac{1}{1-\beta}\frac{d(1-\beta)}{dt} = \frac{\beta}{4-3\beta}\frac{1}{\varphi(t)}\frac{d\varphi(t)}{dt}.$$

Further:

$$\frac{1}{a} = \frac{1}{P} \underbrace{\frac{dP}{dt}}_{\frac{1}{\varphi(t)} \frac{d\varphi(t)}{dt}}$$

is introduced. The luminosity-mass equation then becomes:

$$L = \frac{4\pi \epsilon \sigma G}{\hbar} \Re(1-\beta) \left[1 + \epsilon \frac{\beta}{4-3\beta}\right].$$

The coefficient of absorption k corresponds to the homologous niveausurfaces, and its dependence upon  $\mathfrak{M}$  and R can be taken  $\sim \varrho^1 T^*$  where  $\lambda$  and  $\tau$  are arbitrary powers of the density and of the temperature,  $\lambda$  is then brought into the form:

$$h = \text{const} (1 - \beta)^{r/4} \Re^{1+r/3} / R^{3+r}$$

Further  $L = 4\pi_{\epsilon}R^{\epsilon} + a\sigma T^{\epsilon}_{\epsilon}$  and R can thus be eliminated and the effective temperature substituted.

In reality kQ is not such a function of P, T and q that the stars are homologous systems.

Because of that,  $\sigma$  and  $\varphi(t)$  will vary with M just as the density-distribution

varies from star to star with the total mass.

241. Statistical Investigations Concerning the Mass-Ratio in Binaries. E. B. Wilson and W. J. Luyten¹ have used accurate mass-ratios for 69 spectroscopic binaries for a statistical investigation. By taking  $z = \log \mathbb{R}_k/\mathbb{R}_d$  and by taking the mass-ratios  $\mathbb{R}_d$  and  $\mathbb{R}_d$  both ways in each pair a symmetrical distribution was necessarily obtained of the 438 values of z. The dispersion  $a_s$  is  $\pm 0.26 \pm 0.02$  and the ratio of the fourth moment about the mean to the square of the second moment about the mean is  $4.3 \pm 0.4$ , whereas a normal error curve gives 3.0. In a provious note the authors have found for 14 binaries and the Sun the value of the dispersion of  $\log \mathbb{R}$  to be  $0.36 \pm 0.03$ . The value of  $\sigma$  for the logarithm of the mass-ratios of these 14 systems is  $0.30 \pm 0.04$ .

If 7 is the coefficient of correlation between the logarithmic masses of the components in binaries we have:

$$r = 1 - \sigma_s^3/2\sigma^3$$

By using the above data r is found to be 0,74 and thus there appears to be a high degree of correlation between the masses in the pairs or a great tendency for the masses to be equal, which is also a very general assumption. It should not be overlooked, however, that there is probably a strong observational selection at work. The authors inquire what would be the standard deviation of x for the statistical distribution of the 406 hypothetical binaries that could be constructed by pairing in all possible ways the 29 stars used in a previous note (see ciph. 219)

Wesh Nat Ac Proc 10, p. 433 (1924).

with  $\sigma = \pm 0.36$ . They find  $\sigma_w' = 0.50$  or nearly double the value of  $\sigma_x$ . In the material of 69 actual binaries that was investigated there is not one with a mass-ratio greater than 5, whereas in the 406 hy pothetical binaries there are 79. Assuming that these high mass-ratios, if they existed, would not be observed and measured the authors find for the remaining 327 pairs a dispersion of 0,31, which is not far from the value of 0,26 that is actually found.

The following table is computed on the basis of the material available:

WB/DLA	Discovery- chance	Luminosity ratio	MB/WA	Discovery- chance	Lumbosity ratio
1/20 1/10 1/5 1/3	1/9000 1/220 1/14 1/3.7	1/100000000 1/400000 1/25000 1/600	1/2 1/1.5 1	1/1,6 1/1,2 1	1/70 1/11 1

In view of the very great luminosity ratios it might appear reasonable to believe that the discovery-chances have been overestimated, and that when the discovery-chance is considered the observed mass-ratios are more scattered than would be the case if the two components were selected at random. It seems that there is considerable probability that the apparent clustering of the mass-ratios about unity is due to observational selection.

242. Theoretical Derivation of the Mass-Ratio in Double Stars. The question whether the Russell-diagram represents loci of equilibrium during the evolution course or an actual course of evolution ought, as has been pointed out by G. Shajn1, to benefit from an examination of double stars. Because of the equation  $\Delta m = \Delta M$  we can write, applying Eddington's theory and denoting the secondary by the subscript A and the primary by B,

$$-0.44m = \frac{7}{4} (\log \mathfrak{M}_A - \log \mathfrak{M}_B) + \frac{8}{4} [\log (1 - \beta_A) - \log (1 - \beta_B)] + \frac{4}{8} (\log T_A - \log T_B).$$

The mass-ratio cannot be determined without a knowledge of the temperature and of  $\frac{1-\beta_A}{1-\beta_B}$  as a function of  $\frac{\mathfrak{M}_A}{\mathfrak{M}_B}$ . The observational material was augmented by using systems for which the absolute magnitude is known only by indirect or statistical methods. Thus computations were made for 342 systems, most of which are certainly physical pairs. The results are summarised as follows:

Giants			Dwarfa		
Spectral index	MA/MB	n	Spectral index	1014/901B	8
0,0 — 0,4 0,5 — 0,9 1,0 — 1,4 1,5 — 1,9 2,0 — 2,4 2,5 — 2,9 3,0 — 4,5	0,88 0,72 0,66 0,62 0,45 0,56 0,37	78 12 33 20 18 9	0,0-0,4 0,5-0,9 1,0-1,4 1,5-1,9 2,0-4,5	0,88 0,85 0,70 0,63 0,35	65 16 15 12 4

For systems with components of B stars the vulues of  $\mathfrak{M}_A/\mathfrak{M}_B$  for the first three spectral intervals are: 0,68, 0,41, and 0,34 respectively. The fact that the spectral index increases with Am and the result of LEONARDa that in giant systems the spectrum of

the companion belongs to an earlier class than that of the primary, whereas in the dwarf systems the spectrum of the secondary is of a later class, lead to the conclusion that these relations indicate the course of the stellar evolution, which will be that indicated by Russell.

<sup>&</sup>lt;sup>1</sup> M N 85, p. 245 (1925).

<sup>&</sup>lt;sup>2</sup> Lick Bull 10, p. 169 (1922).

ATTERN<sup>1</sup> has shown that the mass-ratios of spectroscopic binaries increase with advancing spectral class from B to G. The same relation results from Shajn's material

Биаји				Arress	
Spectral chara	数点概念		Spectral class	缺少数。	
110139 A0 A9 F0 F9	0,60 0,77 0,78	50 69 109	B0-B8 B9-A5 F	0,70 0,75 0,92	11 16 3

SHAJN does not think that these facts can be taken as proving that a gradual decrease of mass takes place during the lifetime of a star. The existence a priori of systems of very unequal masses can be expected. Further, the two spectra are not independent of each other. When the primary is M or K, the companion

may exhibit a spectrum of gM-A, but very seldom of a late spectral class. In a dwarf system of, say, class K the spectrum of the secondary is dK or dM. Thus it is natural to expect an average decrease of  $\Delta S_P$  with increasing  $\mathfrak{M}_A/\mathfrak{M}_B$  as is actually found.

248. Lundhark's and Luyren's Differential Methods. The statistical relationship between the two forms of energy in the stars, the radiant energy, expressed as absolute magnitude, and the inert energy, expressed as mass, was derived from differential data of spectroscopic binaries. When both spectra of a spectroscopic binary have been observed an accurate value for the mass-ratio or Alog M is found from the amplitudes  $K_1$  and  $K_2$  by means of the relation:

$$-\Delta \log \mathfrak{M} = \log K_1 - \log K_2 = a.$$

In many cases there are estimates of the relative brightness of the two spectra and thus also the Fig 158 The relation between absolute magnitude and mass as integrated from mass-ratios and differences in luminosity in spectroscopic binaries. For comparison purposes Eddingtonia curve [M N 84, p. 308 (1924)] has been inserted and the curve derived on basis of double stars for which the orbital elements and the

parallax are known (Compare fig. 154.)

difference in absolute magnitude  $\Delta M$  can be determined. If the spectroscopic binary is an Algol variable the value of  $\Delta M$  can be determined comparatively accurately from the determination of the orbit.

Suppose we have the relation.

$$M_A = f(\log \mathfrak{R}_A),$$
  

$$M_B = f(\log \mathfrak{R}_B),$$
  

$$M_A = \psi(M_B).$$

and

The problem is then to solve the equation:

$$/(\log \mathfrak{M}_{4}) = \psi[/(\log \mathfrak{M}_{4} + \epsilon)]$$

<sup>&</sup>lt;sup>1</sup> The Binary Stars, p 207 New York (1918)

Ark Mat Astr Fys 20 A, No 18 (1927); Upsala Medd No. 34.

or to determine the form of when  $\psi$  and a are given. In practice it will be sufficient to use a graphical method and to construct the curve  $M = f(\log \mathfrak{M})$  from values of  $\frac{d \log \mathfrak{M}}{dM} = \frac{d \log \mathfrak{M}}{dM}$  for given values of M. The following mean values for the differential quotient were obtained:

$M_{AB}$	A M A M	11	$M_{AB}$	Alog Wi I M	11
Brightost to $-2^{M},0$	-0,168	4	+2 <sup>M</sup> ,0 to +4 <sup>M</sup> ,0	-0,060	6
$-2^{M},0$ , 0,0	-0,221	16	4,0,, 6,0	-0,060	9
0,0, $+2$ ,0	-0,102	17	6,0,, faintest	-0,073	3

As constant of integration the value  $\mathfrak{M}=1\odot$  for M=5.0 was selected. The following relation resulted:

н	log 90t	D)\$	Ы	log M	939
-2 <sup>N</sup> ,0	0,780	6,0 ⊙	+5 <sup>™</sup> ,0	0,000	4,0
-1,0	0,595	3.9	6,0	-0,060	0,87
0.0	0,410	2,6	7,0	-0.130	0,74
+1,0	0,295	2,0	8,0	-0,200	0,63
2,0	0,195	1,6	9,0	0,275	0,53
3,0	0,130	1,3	10 ,0	-0,350	0,45
4,0	0,065	1,2			

The agreement between this curve and that derived by Eddington is comparatively good. The values  $\triangle M$  were not reduced to bolometric magnitudes, but an inquiry has shown that such a reduction will not materially change the results. The same applies to the inclusion of new material available.

244. The Masses and Luminosities of the Eclipsing Binaries. Dean Mc Laughlin<sup>1</sup> has discussed the contribution of the cclipsing variables to stellar luminosities and masses. Altogether 48 eclipsing stars have been observed for radial velocities. In 28 cases the two spectra have been measured and in 3 others the rotation effect has been observed. In 21 cases the mass-ratio is known from the amplitude-ratio  $K_1/K_2$ . The mass-ratio has been plotted against  $L_A$ , the luminosity of the brighter star, and a smooth curve has been drawn. From this curve the value of the mass-ratio corresponding to any value of  $L_A$  could be read. It was then possible to calculate the hypothetical mass of each component. Altogether the masses have been calculated in 41 systems, and in 38 of these linear dimensions and densities are known. Hence absolute magnitudes and hypothetical parallaxes may be calculated. By using Seares's values for surface brightness  $J_A$  the formula:

$$M_A = J_A - 5 \log r_A + 4,75.$$

where  $r_A$  is the geometrical mean of the major and minor axes of the star, gives the absolute magnitude. The apparent magnitude  $m_A$  of the bright component alone is obtained from:

$$m_{AB} - m_A = 2,5 \log(1 - L_A),$$

where  $m_{AB}$  is the apparent magnitude of the system at maximum brightness. Then;

$$\log n = 0.2 \, (M_A - m_A) - 1$$

gives the hypothetical parallax. Further:

$$\Delta M = m_B - m_A = 2.5 \log[L_A/(1-L_A)].$$

<sup>&</sup>lt;sup>1</sup> A J 38, p. 21 (1927).

<sup>&</sup>lt;sup>2</sup> Ap J 55, p. 198 (1922).

The bolometric magnitudes have been calculated from the formula given by EDDINGTON.  $M_{\rm bol} = 4.75 - 5.0 \log r_{\rm A} - 10 \log T_{\rm A}/5860^{\circ}$ 

The bolometric magnitudes have been reduced to Eddington's standard curve for  $T_{\bullet} = 5200^{\circ}$  by applying the temperature correction term:

$$2\log\frac{T_s}{5200^{\,\alpha}}.$$

The Russell diagram shows that the dwarf sequence is well determined by the eclipsing binaries. Yellow and red giants are almost totally lacking. The relation of mass to spectral class is shown in the following synopsis.

Spectral class	0	Blare	Palm
08,5	35 O	2	1
H0 B2	16,6	6	4
B3~B5	5,2	12	8
138 A0	3.1	18	14
A2-A8	2.7	- 8	5
F0-F5	0.7	5	3
F8-G5	1,1	10	5
Mi	0,6	2	1

Then the mass-luminosity diagram was formed The scattering around the relation curve was found to be comparatively large. The sources of appreciable errors must be limited to the radii and the effective temperatures. It does not seem likely that in any case errors of the radii could affect the result by as much as one magnitude, which would correspond to an error of roughly 30%

in the radius. The effective temperature should not introduce an error greater than half a magnitude. Thus a deviation of 1<sup>M</sup>,5 ought to be relatively infrequent, but at least five well-determined stars equal or exceed that limit, and several others of less certain mass so far exceed it that no reasonable adjustment of temperature will bring them within 1<sup>M</sup>,5 of the relation curve. The author is of the opinion, which is also shared by me, that we are not justified in saying that the mass and effective temperature of a star determine a unique value of the luminosity.

McLaughlin has pointed out that if there is a strict one-to-one correspondence between mass and luminosity within a group of stars with the same effective temperature but with different masses, the density of each star would be uniquely determined. The curves of constant dimensions and temperatures have been calculated from Eddington's mass-luminosity relation. The figure provides a check on the calculated density, since the point for any given star will fall in a position corresponding to the assumed radius, regardless of whether the star satisfies the theory or not.

Few of the stars show such great deviations from the theoretical densities that the calculated ones would have to be multiplied or divided by 8 or a greater factor. It is very doubtful whether as great a change of radius as 50 per cent would be permissible in any of these cases. Considerable deviations are also shown in other cases. Nor would an adjustment of the scale of effective temperatures remove the disagreement between observation and theory.

245. The Upper Limit for the Stellar Masses. H. Voct has discussed this important question. The observations suggest that an upper limit exists and the theory concerning the interior of the stars indicates that unstable conditions must arise as soon as the radiation pressure equals the amount of the gas pressure. Voct assumed an arbitrary law of density distribution within a star  $(\varrho = F(r))$  possessing spherical symmetry. The amount of energy  $L_r$  passing in unit time through the alveau-surface at a distance r from the centre is

$$L_r = -\frac{4\pi_e \pi c r^2}{3h\varrho} \cdot \frac{dT^1}{dr},$$

$$L_r = \frac{4\pi_a cG}{\hbar} \mathfrak{M}_r (1-\beta) \left[ 1 + \frac{P}{1-\beta} \frac{d(1-\beta)}{dP} \right],$$

where  $\mathfrak{M}_r$  is the mass within the distance r. If a star is compared with a homologous star with  $\mathfrak{M}=1$ , R=1, and the mean molecular weight m=1, the following relations exist:

$$\begin{split} T^4/T_1^4 &= (1-\beta)/(1-\beta_1)\,\mathfrak{M}^2/R^4\,,\\ T/T_1 &= \beta/\beta_1\,\mathfrak{M}\,m/R\,. \end{split}$$

Putting:

$$\varphi(\mathfrak{r}) = (1 - \beta_1)/\beta_1^1,$$

we have:

$$(4-\beta)/\beta^4 = \varphi(\mathfrak{r}) \mathfrak{M}^2 m^4,$$

from which we obtain:

$$\frac{1}{1-\beta}\cdot\frac{d(1-\beta)}{dt}=\frac{\beta}{4-3\beta}\cdot\frac{1}{\varphi(t)}\cdot\frac{d\varphi(t)}{dt};$$

combining with the equation for  $L_r$  we obtain:

$$L_r = \frac{4\pi_e c G}{k} \Re_r (1 - \beta) \left[ 1 + \psi(r) \frac{\beta}{4 - 3\beta} \right]$$

where:

$$\psi(t) = \frac{1/\varphi(t) \cdot d\varphi(t)/dt}{1/P \cdot dP/dt} = \frac{1/\varphi(t) \cdot d\varphi(t)/dt}{1/P_1 \cdot dP_1/dt}.$$

Denoting by  $Q = L_r/\mathfrak{M}_r$  the mean energy produced we have:

$$kQ = 4\pi_0 cG(1-\beta)\left[1 + \psi(t) \cdot \beta/(4-3\beta)\right].$$

The equation says that within homologous stars the quantity kQ varies comparatively little as the mass becomes larger. It is also clear that when we are considering very heavy stars, a small change in the function kQ will correspond to a change in  $\psi(t)$  that is as much larger as is the value of the mass. If the mass approaches an infinite value, the formation of a star is only possible if kQ is independent

of r and has a constant value equal to  $4\pi_{c}G$ .

If kQ is not a constant, but proportional to a function of  $\mathfrak x$ , it can be shown that  $1-\beta$  reaches, either in the central parts or in the shells near the surface, the value 1 according as kQ increases as we proceed to or from the centre. Then the upper limit for the value of the mass is reached, as every further contribution of matter to the star will be driven away by the radiation pressure. — In reality the condition kQ = const. will not be fulfilled in the interior parts of a star, because it is very unlikely that the quantity kQ is such a function of temperature, density, and pressure that it would have a constant value for such a distribution as corresponds to the condition kQ = const. Already for that reason the masses of the stars must have an upper limit.

In the preceding lines it is assumed that the stars do not rotate. If rotation

is taken into account the conclusions will remain principally unchanged.

The question whether an upper limit exists for the stellar masses has also been discussed by W. Anderson<sup>1</sup> and later by G. I. Pokrowski<sup>2</sup>. The former starts from the energy formula:  $E = \frac{3kM^3}{5\pi}$ ,

where k is the constant of gravitation, E the potential energy, and r the radius. The formula is valid if infinitely scattered matter is united into a homogeneous sphere (star) of radius r. In the cosmical cloud from which the sphere is formed

<sup>&</sup>lt;sup>1</sup> A N 218, p. 205 (1923); Z f Phys 53, p. 597 (1929). 
<sup>2</sup> Z f Phys 49, p. 587 (1928).

the potential energy E is assumed to have been uniformly distributed if the material mass of this cloud is  $\mathfrak{M}'_1$ , the mass corresponding to E  $\mathfrak{M}_2$ , the mass of other energy present  $\mathfrak{M}''_1$ , and the total mass  $\mathfrak{M}$  so that

$$\mathfrak{M}=\mathfrak{M}_1'+\mathfrak{M}_1''+\mathfrak{M}_2=\mathfrak{M}_1+\mathfrak{M}_2,$$

we have  $\mathfrak{M}_1 = E/c^2$ , where c is the velocity of light. The above equation can then be transformed into

 $E^2 - {5rc^4 \choose {7k}} - 2\mathfrak{M}_1c^2 h + \mathfrak{M}_1^2c^1 = 0$ .

which when solved gives

$$L = \frac{5rc^4}{6k} - \mathfrak{M}_1 c^6 + \left[ \frac{25r^6c^6}{36k^6} - \frac{5rc^6\mathfrak{M}_1}{3k} \right]^{\frac{1}{2}}$$

E has thus real values only when

Thus the mass of a star has an upper limit A maximal value of M is derived from the above inequality and this gives a maximal value for the total mass of the cosmical cloud

 $\mathfrak{M} = \frac{5r\ell^{9}}{6k} = \begin{pmatrix} 5 \\ 6 \end{pmatrix} \begin{pmatrix} 2 \\ 4 \end{pmatrix} \begin{pmatrix} 3 \\ 2 \end{pmatrix} \begin{pmatrix} 3 \\ \pi_{\bullet} e^{\frac{1}{2}h} \end{pmatrix} ,$ 

where  $\rho$  is the density of the star

In an analogous way Pokrowski has derived a maximum value that only differs from that of Anderson in the respect that the numerical factor (1) is not present

The upper limit corresponds to a value of log M = 35 and thus enormous masses could exist

246. Relation between Stellar Mass and Proper Motion. When the masses of visual double stars are being derived the great difficulty is the determination of the parallex. The data must necessarily be selected. The systems for which orbits have been determined must either be exceptionally massive or the linear separation must be relatively small. It seems very reasonable to suppose that the latter provides the greater part of the explanation.

J JACKSON<sup>1</sup> has tried to use the proper motion materal of the parallaxes in order to test the masses independently. The proper motions were divided by the dynamical parallaxes  $\pi_t$  and the resulting linear motions analyzed by Airy's method. The following results were found

Stars with known orbits.

Spentral rium	Contibutes of apex	Velocity outr mains per year	2007	•
A2	258",5   32",0	2,18	13,4()	21
F5	267 ,5   20 ,1	3,07	4,81	52
G2	290 ,6   41 ,6	4,79	1,27	30
K2	269 ,3   10 ,2	8,17	0,26	12

Stars with short ares only

Aprotest class	Contributes of apex	Velocity nate units per year	101	
136	278°   12°	2,07	12,6 ⊙	24
A2	267 ,2 + 15 ,8	2,16	11,02	83
1:4	261 ,0   24 ,2	3,91	1,87	102
(-3	293 .6   41 .7	6,63	0,38	74
K1	269 ,1   25 .6	4,87	0,96	42

<sup>1</sup> M N 83, p. 444 (1923)

A comparison was made with the mass values of Seares. The agreement is good when the fact is taken into account that SEARLS's results refer to geometrical mean masses and Jackson's to [mi]3. Owing to the small dispersion in M the two values do not differ much.

The present writer has derived mass-proper-motion relation. The derivation of the masses on the basis of spectral proper-motion parallaxes has convinced me that it will be possible to find a rather definite relation between Mt and  $H = m + 5 + 5 \log \mu$ . Such a relation will be of use for deriving the frequency of stellar masses from the frequency of absolute proper-motion magnitudes,

Using 62 cases of well-determined individual masses the following relation

has been found by a least-squares solution:

$$\log \mathfrak{M} = 0.9750 - 0.1021H + 0.00131H^2.$$

Using the relation between mass and absolute magnitude as derived in ciph. 232 (p. 666) and making the assumption that M = H - 5.6 the following formula was found:  $\log \mathfrak{M} = 1,6262 - 0,2037H - 0,00412H^8$ .

247. Relation between Stellar Mass and Form of Orbits of Binary Stars. Already in the early material it seemed suggested that there is a relation between the total absolute magnitude and excentricity of binaries. As the difference in mass  $\Delta \mathfrak{M}$  is directly dependent upon the difference in M the existence of the thought relation would prove a relation between stellar mass and form of the orbit of double stars. It seems obvious that no definite relation can be established. Using different determinations of trigonometric and spectrographic parallaxes of stars the absolute magnitudes of 347 binaries have been approximated by me. The coefficient of correlation between excentricity, c, and absolute magnitude M was found to be:

$$r = +0.388 \pm 0.048$$

and the regression lines:

$$M = 0.360 s + 1.586$$
,  
 $e = 0.032 M + 0.273$ .

The correlation found is not very high but should probably be taken as real. This result has been doubted by H. Siedentoff<sup>2</sup> who finds when treating the spectroscopic and the visual binaries separately no correlation between M and e and thinks that the correlation above is spurious and a result of selection in the material3.

Earlier C. D. Perrine has dicussed the question of a dependence of orbital excentricity upon the absolute magnitude of the components of binary stars. He used the difference  $\Delta M$  and compared with  $\epsilon$  and found the following relation:

Linits of s	ē	ī Mí	n
0,00 to 0,29	0,19	0,60	7
0,30 ., 0,44	0,37	1,29	16
0,30 ,, 0,44	(0,37) 8	(0,95)	(15)
0,45 ., 0,58	0,50	1,32	18
0,59 and larger	0,71	2,04	16
0,59 ,, ,,	(0,71)8	(1,47)	(15)

<sup>Ark Mat Astr Fys 20 A, No. 12 (1927); Upsala Medd No. 20.
Göttingen, Univ Sternw Veröff H. 3 (1928).</sup> 

s If so the conclusions concerning stellar masses and their relation to luminosity will also be affected to a certain extent.

<sup>4</sup> A J 33, p. 180 (1921).

<sup>&</sup>lt;sup>5</sup> Excluding 85 Pegasl.

Excluding Sirlus.

This seems to be a pretty well established relation but on another hand a similar grouping made by me on basis of 116 pairs and represented graphically in Fig. 159 does not seem to reveal any correlation between e and M. It thus seems that we have here one of the many problems where our present material is insufficient to give a definite answer upon the inquiry

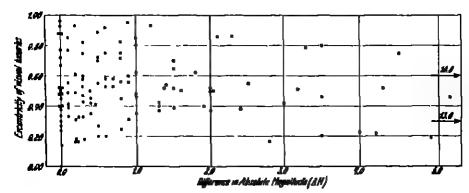


Fig. 159 Test for a supposed relationship between excentricity of visual binaries and the difference in absolute magnitude 4M between the components

248 The Mass of the Orion Nebula. The method of determining stellar masses is not restricted to the binary stars. It applies to every cases of a rotating body where the period of revolution can be determined for a particle at a certain distance. Thus the mass of the solar system could be approximated when an outside observer had observed the difference in velocity between the Sun and Neptune as soon as he had a knowledge of the linear distance between the two bodies

It was found by Fabry, Buisson, and Bourger when they were applying the interferometer method, that internal motions existed within the Orion nebula and that the character of the motion was that of rotation. Later on Campurla and Moore<sup>1</sup> determined the radial velocities of 96 points near the Trapezium. The motion is of rotational character, although considerable individual deviations occur. In order to determine the amount of rotation it has been assumed that the nebula rotates as a rigid body within a distance of 2' from the centre. With the aid of a least square solution the plane was found that gives the closest representation of the velocities. This corresponds to a rotational component in the radial velocity amounting to 5 km/sec at a distance of 2'

If  $\mathfrak{M}$  is the central mass and m the (infinitely) small mass of a particle at the distance  $\tau$ , v the linear velocity, and k the gravitation constant, we have

Œ

$$\mathfrak{M} + m = 0.001129 \frac{\sigma^{\mu}}{\pi} v^{3},$$

where a'' is the distance of the point considered in seconds of arc, v is the linear circular velocity at this point measured in km/sec. Next the parallax has to be derived. In a paper of mine still unpublished it has been found that the value:

$$\pi_{\text{Orina}} = 0'',0030,$$

Lick Publ 13, p 96 (1918).

derived from a discussion of absolute magnitudes, proper motions, motions of binaries etc., and the distribution of stars in front of the dark nebula accompanying the bright one is the best that can be derived from the existing data.

Thus the minimum mass of the nebula is found to be 48 0, which is not astonishing when one remembers that the trapezium-stars alone are certainly

very massive<sup>1</sup>.

The value thus derived is the minimum mass of the nebula; on account of that we cannot locate the axis of rotation and the observed rotation is thus a component of the actual rotation.

The method can also be applied to the anagalactic objects.

249. Planetary Nebulae. The central stars of planetary nebulae are O stars that evidently do not differ from the ordinary O stars in any other way except that they are surrounded by nebulosity. W. H. WRIGHT has said that the disparity among the central stars in planetaries is no larger than the disparity among non-nebulous O stars,

The extensive survey of the spectra of 125 bright-line nebulae at Lick Observatory has revealed the important fact that several planetaries show internal motions that are most likely interpreted in terms of rotational motions. The internal motions are in several cases of a very complicated nature and there are certainly other phenomena present that change the spectral lines, such as a possible extension or outward motion of the gaseous envelope, differential effects of radiation pressure, ZEEMAN or STARK effects, etc. Still, it seems to be justifiable to try to find a general rotational component.

In 23 cases it seems possible to derive a rotation component. The uncertainty is considerable, but still there seems no doubt that the planetaries are very massive

and bodies of a low temperature.

Obje	ect	Distance from centre	Rotation component in km/seo	Parallax #	Mass of Star and nobula	Density of central	Temperature of central star
NGC	1535	4",4	4,0	0",0017	46 O	4390 ⊙	38 - 103
J 320	_	3 .1	6,6	0 ,000.62	240	22400	34 + 103
IC	2165	4 ,2	2,8	0 ,00025	149	9320	51 · 10 <sup>0</sup>
NGC	2392	15 ,Q	16,0	0.0015	2900(?)	4470	27 · 10 <sup>0</sup>
	2452	10 ,0	14,0	0 ,00019	11 500 (?)	100.0000000 (?)	85 105
	3242	0, 13 5, 5	4,4 6,2	8100, 0	156	40,900	58 · 10 <sup>0</sup>
IC	4593	2,05	2,15	0 ,00095	13.3	480	22 · 10 <sup>5</sup>
NGC	6210	3 .5 4 .5	6,4 4,0	0 ,0014	113 57	7270 ] 3650 ]	36 - 100
	6543	3 ,5	5,0	0 ,0023	43.5	5,600	40 - 103
	6565	3 ,0	7,0		-	<u> </u>	
	6572	4,0	2,8	0 ,0019	19,4	540	31 • 103
	6567	1 ,8	7.5	0 ,0005	220	58000	45 · 10 <sup>0</sup>
	6720	25 ,0	2,0	0,0012	94	415000	72 · 10 <sup>0</sup>
	6741	4 ,1	2,4	0 ,00025	107	128 000	58 · 10 <sup>8</sup>
	6807	1,0	4,3	0,00019	1100	2860000	66 · 10 <sup>8</sup>
	6818	9,0	2,4	0 ,0011	54	2090000	70 · 10 <sup>8</sup>
	6826	10 ,4	4,0	0,0020	94	4820	34 · 10 <sup>8</sup>
	6886	2 ,8	5,0	0,00032	250	156000	52 · 108
$\mathbf{IC}$	49 <b>97</b>	2 4	5.7	0,00019	460	26800	35 • 103
NGC	7009	4 ,5 9 ,0	4,5 6,1	0 ,0029	36 132	178000 } 650000 }	50 · 10 <sup>a</sup>
	7026	3 .7	18,4	0 ,00045	3100	8140000	45 - 100
	7027	5 ,5	10,0	0 ,00044	1420	18000000	86 · 10°
	7662	5 ,6	8,0	0 ,0018	230	151000	52 · 10 <sup>9</sup>

Land Obs Circ 3, p. 64 (1931).

To this table should be added the remark that the densities have been computed on the assumption that all the mass is concentrated into the central star. This seems reasonable when one considers recent work concerning the formation of gaseous nebula.

The parallaxes are generally the ones derived by H ZANSTRA<sup>1</sup> In some cases parallaxes have been derived by me according to the same method. The

same applies to the temperatures of the central stars

Although the dispersion in the density values is considerable there seems to be a rather definite relation between the temperature and density. Thus

T	8
32000°	3800
17 (x)O	18000
75000	6000000

This may be due to a systematic error in the temperatures but it might also be a real phenomenon. It is interesting to see that the densities, although high in many cases, still are not above the upper limit assigned to the density of matter. Thus E C STONKE has on basis of Eddington's theory on stellar evolution computed an upper limit for the central densities of the stars on reasonable assumptions, he finds this limit to be 5.10° ©

250. Mass of the Stellar System. The total mass of the stars in the Milky

Way System is given by

$$\mathfrak{M}_{\mathrm{lot}} = N \iiint D(\alpha, \delta, r) \, \mathfrak{M}(M, \alpha, \delta, r) \, d\alpha \, d\delta \, dr \, dM$$
,

in which  $\mathfrak{M}(M, \alpha, \delta, r)$  is the mass of an individual star of absolute magnitude M at the point  $\alpha, \delta, r$ , and N the number of stars per cubic parsec in

the vicinity of the Sun

At present we cannot suppose anything else than that the mean mass of a certain number of stars is the same everywhere, that is, that  $\Re(M,\alpha,\delta,r)$  is independent of position Luytun has adopted the density law of Kaptkyn. The above formula simplifies to

$$\mathfrak{M}_{lot} = \overline{\mathfrak{M}} \cdot N_{\infty}$$

where  $N_{\infty}$  is the total number of stars in the universe and is obtained by means of the relation

$$N_{\infty} = 0.0451 \int_{0}^{\infty} 4\pi_{\rm s} (5,102)^{2} \, \varrho^{2} \Delta (\varrho) \, d\varrho$$

 $\varrho$  being the polar semi-diameter of the homologous ellipsoids around the Sun and  $\Delta(\varrho)$  the density of stars in space. Further according to Kapikyn

$$\log \Delta(\varrho) = -5.356 + 4.890 \log \varrho - 1.200 \log^{9} \varrho$$

LUYTEN funds:

$$N_{\infty} = 1.5 \cdot 10^{0}$$
.

For R lie adopts 0,945 @ and thus

<sup>&</sup>lt;sup>1</sup> Z f Astrophys 2, p 329 (1931)

<sup>&</sup>lt;sup>1</sup> M N 92, p. 662 (1932)

Harv Ann 85, No. 5 (1923)

The value of  $N_{\infty}$  is perhaps six times too small, as is suggested if we adopt the results of Seares1. On the other hand Luyten's value of M seems to be too large. I have adopted  $\overline{\mathfrak{M}} = 0.6 \odot$ . Thus the total mass should be:

$$\mathfrak{M}_{tot} = 5.4 \cdot 10^9 \, \odot.$$

251. The Masses and Mass-Ratios of Stellar Systems. In 1916 V. M. SLIPHER<sup>2</sup> announced that the spiral nebula NGC 4594 rotates in its own plane approxmately as a rigid body. This conclusion was confirmed by the subsequent work of F. G. Pease's at Mount Wilson. Later on the rotational motion of the Andromeda nebula was also established by means of the measurements of Pease and ADAMS4. Already in 1914 M. WOLF5 had found a rotational component in the motion in Messicr 84, but details were not published until later on. The results given below for Messier 33 and Messier 51 are poor, as the rotational motion is based on the difference in motion between the centre and one outside object in each case, NGC 598 and NGC 5194, respectively.

The method of computing the mass is the same as in the case of double stars. Uncertainties are involved principally on account of the uncertainties in the parallax adopted and the inaccuracy in assuming that the inclination of an anagalactic object is derived from its ellipticity.

C	bject	M <sub>lot</sub>	Mist
Audromeda	Nebula	1,8 - 10 <sup>9</sup>	-17,8
Mession 81		7,6 · 10 <sup>11</sup>	-24,2
NGC 4594		3 • 1010	17,0
Messier 33		1,5 · 10 <sup>10</sup>	-15,1
Messler 51		1 · 10 <sup>10</sup>	-16,6
Our Milky	Way System .	1 · 1011	-16

The mass derived from values for the spectrographic rotation is dependent on the immediate effect of the gravitation. The gravitational mass thus also includes the dark matter within the anagalactic objects, such as extinct stars, dark nebulae, and meteors. On the other hand an approximation of the mass of an anagalactic object can be derived from the total absolute magnitude. This involves the assumption that the mass-luminosity relation is the same in different parts of the universe. On account of the fact that the proportions of different spectral classes within different galaxies do not vary considerably, and that hence the himinosity curve seems to be rather equal, it seems justifiable to assume as a first approximation the universality of the mass-luminosity relation. The luminous mass so derived does not include the dark matter and thus it will be possible to obtain an approximation of the ratio, Dark matter/Bright matter, in the cases where both the mass-values have been estimated.

Ratio:  $\frac{\text{Dark} + \text{bright matter}}{\text{Bright matter}}$ 

Object	Ratio	Object	Ratio
Messier 84	100:1 30:1 20:1	Messler 51	10:1 6:1 10:1

<sup>1</sup> Mt Wilson Contr No. 301 (1925); Ap J 62, p. 320. 3 Wash Nat Ac Proc 2, p. 517 (1916).

<sup>&</sup>lt;sup>8</sup> VJS 49, p. 162 (1914). 4 Wash Nat Ac Proc 4, p. 21 (1918).

Upsala Medd No. 40; Ark Mat Astr Fys 21, No. 10 (1928); Popular Astronomisk Tidskrift 10, p. 19 (1929).

In the case of double nebulae the mass-ratio of the components can be determined from measurements of the spectrographic rotation. Let two particles, in each of the two components, be at the same angular distance d'' from the centre, then their linear distances are equal and the mass-ratio will be

$$\mathfrak{M}_{h}/\mathfrak{M}_{A} = V_{h}^{1}/V_{A}^{2}$$

where  $V_A$  and  $V_B$  are the circular velocities at the said distance. The application of the method will involve much observational work, but it does not seem to be impossible to find cases where one ought to be able to photograph both the spectra of regions at such distances from the nucleus that decent values of  $\mathfrak{M}_B/\mathfrak{M}_A$  can be derived

Assuming that the mass-luminosity law holds good we can take the ratio  $E = I/\mathfrak{M}$ , where I is the luminosity and  $\mathfrak{M}$  the mass within unit space. Then

$$\pi_{AB} = \frac{i_A}{E_A d_A} \binom{V_0}{V_1}^3 = \frac{i_B}{E_B d_B} \binom{V_0}{V_B}^3$$

where  $V_0$  is the velocity of the Earth, d'' the angular distance from the contre, s the apparent intensity Determinations of  $V_A$  and  $V_B$  can make a contribution to the value of B in both systems or test the binary character of the pair.

252. The Angular Moments of Visual Binaries. Shinzo Shinjo and Yoshikatsu Watknari derived in 1918 the masses and the angular moments of visual double stars. If H denotes the angular momentum of a system we have

$$H = 2\pi_a a^a l^{a-1} = \pi^{-1} (1 - a^a)^{\frac{1}{2}} \mathfrak{M}_A \mathfrak{M}_B (\mathfrak{M}_A + \mathfrak{M}_B)^{-1}$$

if the terms caused by the rotation of the components are neglected

The authors conclude that the masses and angular moments of star systems are, on the whole, of the same order of magnitude. The multiple systems have somewhat greater angular moments, the masses on the other hand remaining about the same. For spectroscopic binaries, the angular moments are comparatively less than for visual binaries, the masses, however, being considerably greater. Our solar system has an angular momentum over hundred times less.

It is really very remarkable that the values of H are of the same order of magnitude, when one remembers that the fifth power of the parallaxes enters into the determination of the moments. It is difficult to avoid the conclusion that this result has a certain cosmogonic bearing. The authors compute the angular momentum of a primordial swarm of meteorites, which possesses spherical symmetry and is isolated from other external influences, and also suggest a theory for the explanation of the celestial rotation, perhaps the most enigmatic problem in cosmogony

263. The Origin of Binary Stars. H. N. Russkl. has pointed out that the problem whether the binaries are the result of fission or condensation in nebula can be advanced by means of studies of the triple and multiple systems. Systems originating from independent nuclei should not show any definite relations between masses or relative distances. An analysis of the problem shows that if a gaseous mass divides by fission without external distance into two parts the distance of the centres at the time of division is greater and the density

Mom Coll of Sc Kyoto Imp Univ 3, No 7, p 199 (1918).

Ap J 31, p. 185 (1910)

less the more unequal the parts (components) are. The ratio in which the initial distance can be increased by tidal action increases as the components become more unequal. The smaller component has the greater density immediately after the separation. The contraction necessary for a second fission is less for the more massive component. The ratio of the dimensions of the separate masses in the case of the second fission to that in the case of the first is always small. The increase in density between the fissions is very great.

The distribution of masses that is found among binaries makes the fission theory very probable. As the orbital elements are known only to a small extent, it is necessary to investigate the distribution of the (projected) distances,  $S_8$ and  $S_1$ . Only pairs with common proper motion were used; of 800 such pairs 74 are triple or multiple. It seems that the fission theory accounts for existing peculiarities of arrangement and gives a simple and fairly detailed account of their origin. The stars for which the separation is 1000 astronomical units exhibit two maxima of frequency, of which one,  $S_2/S_1 = 0.15$ , can be accounted for by fission theory, but the second,  $S_9/S_1 = 0.40$ , cannot. The theory that multiple stars have developed from nebulae that originally had well defined nuclei corresponding to the members of the system must in any case be called on in order to account for such wide groups as the Trapezium in Orion. In the case of the binary stars it seems reasonable to adopt the fission theory.

254. Concluding Remarks. Whereas the magnitude of the stars can be measured directly and their colour estimated or their colour equivalents derived in terms of magnitudes, the dimensions and the masses of the stars cannot be measured by any direct method except in the case of the apparently brightest stars, the diameters of which can be measured by the aid of interferometer methods.

The important elements, stellar dimensions and stellar masses, are thus derived or inferred quantities that are therefore not only affected by the errors in the observed quantities, but also by the uncertainty concerning the constants in the equations connecting the given quantities and those required for. The dimensions can be derived for all stars for which we possess tolerable knowledge of the quantities M and  $c_0/T$ . It cannot be said that we have a reliable temperature-scale as yet, in spite of all the varied research work carried out within this branch. As regards the masses our knowledge must be restricted for a long, long time to binary stars, and the application of the results to ordinary stars will certainly be justifiable, but will, no doubt, increase the uncertainty of the conclusions.

The third element considered here, the density of the stars, can be determined from observations of binary stars. The parallax does not enter and thus the density will be determined with fair accuracy as soon as the temperature is known.

The present situation with regard to the possibilities of deriving stellar dimensions and stellar masses seems rather satisfactory. The standardization of the temperatures (colours) inaugurated by Herrzsprung could easily be extended to embrace several thousand intermediate stars. The parallaxes available will give linear dimensions of fair accuracy for at least a thousand stars. The new interferometer at Mount Wilson will furnish a means of measuring the dimensions of perhaps fifty stars or more, thus making it possible in the near future to standardize the system of computed diameters.

It might at first seem that the further extension of our knowledge of stellar masses will advance very slowly. But the discovery of new eclipsing binaries or the orbital determination of pairs that have been previously insufficiently

observed will add many good cases within a short time to our previous stock. The discovery by Attken of a number of visual binaries of short period makes it possible for us to obtain within the next ten or twenty years orbital elements of a number of binaries. Many of these Attken pairs are very imperfectly known as regards their parallax, proper motion, spectral class, and other attributes, but they can easily be entered on current programmes. It also seems likely that the publication of Attken's extension of the Burnham General Catalogue of double stars will considerably increase the number of new binary star orbits. It does not seem to be too optimistic to expect to have gained a knowledge of 500 individual stellar masses ten years from now Anecessary condition for the proper increase in data concerning the masses is intimate co-operation between the astrophysicist and the representatives of astronomy of position

The approximations to the spectral-mass relation, mass-luminosity relation, and mass-temperature-luminosity relation hitherto reached will no doubt be more accurately established within a short time from now. The results of Eddison, Jeans, and others concerning the theoretical mass-luminosity relation will certainly be improved upon by the aid of now observational data in the near future.

An application of the interferometer methods to the method of determining the mass-ratios seems to be of interest. If stars that take no part in the motion of the components of binaries, but that are not too far from them, are measured interferometrically, the results concerning the mass-ratios should be obtained in a much shorter time than when the derivations are based on meridian observations

The general attitude of astronomers towards the problems we have dealt with in this paper sometimes seems to involve a certain overestimation of the bearing of certain theoretical results. It sometimes happens that the reasoning goes round in a circle, or go if the mass of a star does not agree with Eddington's curve this does not prove anything concorning the correctness or incorrectness of the result. This is a commonplace, but still it seems to me that it should be pointed out. It has often happened that when new results have been presented it has been asked "How does that result compare with Eddington's, Jeans's or Russell's formula"? Of course, such comparisons should be made, but if there is only poor agreement it is not necessary for the observers to apologize and to regret that the observations do not fit the theoretical demands

I am so far from denying the value of investigations of theoretical problems within astronomy that I wish to say that many efforts must be made on the part of the theorists in order to advance a number of questions on the basis of the new available material. We really should feel under much obligation to the theoretical astronomers for their splendid contributions, theories give us the best guidance with regard to the requirements of future work and, what is most important, theories discover and formulate the general laws of Nature. Without any theories the astronomical observations would be a quite worthless collection of dead figures and descriptions.

But the theoretical interpretations of astronomical facts are always changing. Theories do good service and are dismissed. New theories are advanced and serve for a longer or shorter time. The solid construction on which astronomical theories are embroidered consists of the vast accumulation of recorded facts that has been going on from antique times up to recent days

## Chapter 5.

## Stellar Clusters.

By

H. SHAPLEY-Cambridge, Mass.

With 21 illustrations.

## a) Introductory Survey<sup>1</sup>,

1. The Significance of Clusters. We designate as star clusters those groupings of stars in which the members are known to be gravitationally associated or may be assumed from their apparent positions relative to each other to constitute distinct physical organizations. Such a category includes both the typical globular systems and the more numerous and less well defined open clusters which range, for instance, from the Hyades to the fairly compact system of Messier 11.

There are also, in all parts of the sky, among the faint stars thousands of less obvious groupings. The studies of star distribution on the astrographic charts by Turner<sup>2</sup>, and by Opik and Lukk<sup>3</sup>, indicate that the distribution is not at random. Working on this problem with Harvard plates<sup>4</sup>. I have shown that the clusterings and vacancies are real and are not to be attributed to occultation by nebulosity. The observed irregularities in the star counts, beyond those allowed by the law of chance, are to be attributed in general to the very prevalent stellar associations, which are not commonly recognized by casual inspection, and cannot be separated from surrounding stars except through laborious investigations.

The typical star clusters, however, are in themselves numerous and widely distributed, and their many problems are intimately interwoven with some of the most significant questions of stellar organization and galactic evolution. The general study of clusters deals with a wide variety of subjects. It involves, for instance, the problems of super-giant stars, stellar luminosity curves, irregularities in stellar distribution, star streaming, island universes, and the genesis of galactic systems; it considers primarily, however, the composition, structure, distribution, and cosmic position of the easily recognizable galactic and globular clusters, and in the following sections these groups will receive almost exclusive attention.

2. Historical Notes on Clusters. The history of the scientific study of star clusters is neither extensive nor very significant. Several clusters of naked eye

<sup>&</sup>lt;sup>1</sup> Since the manuscript for this chapter was submitted to the publisher in May 1930, several important studies of star clusters have appeared. Only a few of these could be considered in the course of proof reading. November 1932.

Obs 48, p. 173 (1925).
 Publ Obs Asír Univ Tartu (Dorpat) 26, No. 2 (1924).

stars-for example, the Plendes, Praesepe, Coma Berenices-have of course always been known, though their definite assignment to the cluster category came with the work on proper motions in the last fifty years. In a few constellations the majority of the brighter stars are now known to he near together in space, and to form physical systems. Among such constellation groups are Taurus, Orion, Ursa Major, Perseus, Scorpio, Sagittarius, and Vela But no close physical connection exists for the bright stars of Cassiopela, Lyra, Aquila, Can is Major, and many others,

A score of the brighter galactic clusters and half a dozen of the globular clusters can be seen with the naked eye under good conditions. These objects were probably all known, therefore, to the ancients, but only a few appeared in our permanent records before the second half of the eighteenth century

The records of HIPPARCHUS contain references to the double cluster in Perseus and to Praceape, although neither was recognized as a group of distinct stars until the invention of the telescope. Both were first resolved by GALILEO, who described "the nebula called Praesope", "not one star, only, but a mass of more

than forty small stars"

Messier 22, the first globular cluster to be recorded as such, was discovered by IIILE? in 1665, a Centauri was noted as a lucid spot in the sky by HALLEY in 1677, and had previously been known to BAYER as a hazy star, and to PTOLEMY as a star in the cloud on the Horse's back; in 1702 Kirch discovered Messler 5, and the famous Messier 13 (the Hercules cluster), the brightest in the northern sky, was accidentally found by HALLEY in 1714.

The open cluster Messler 11 had already been recorded by KIRCH in 1681, but the majority of bright galactic clusters, except the Plotades and the Hyades, were first recorded as such by MESSIER<sup>3</sup> in 1774. The conspicuous groups of stars around a Carinao and the cluster near a Crucis were discovered by Sir

JOHN HERSCHEL

For both open and globular clusters, as well as for bright nebulae of all kinds, the systematic listing by MESSIER in 1784 marked an epoch in the recording of observations of star groups. The Herschells advanced the work materially Especially significant were the General Catalogue published by Sir John Herschel in 1864, and its important sequels by Drayer in the New General Catalogue and the Index Catalogues,

SCHULTZ and BARNARD were among the pioneers in determining visually the positions of the individual stars in globular clusters. The powerful photographic method of charting positions was first used by the HENRYS and Govern for galactic clusters, and by Schringe, Lunknioners, and von Zeiper for globular systems.

The Pleindes, the Hyndes, Praesope, h and z Persel, and some of the other bright galactic groups have, for the past fifty years or more, been the subject of frequent investigations of positions and proper motions. It is not unfair to say, however, that, except for studies of these nearby objects, the work done on individual clusters before the present century is now of little value. The devecopment of photographic methods, the modern large telescope with its rapid spectroscope, and the standardizing of magnitude sequences have all tended to make the carlier work obsolete. The present views of the nature, dimensions, and significance of the globular clusters are less than twenty years old

GALILEO, Sidorous Nunchus, 1610, ALLEM, Star Names and their Meanings, p 113 (1899); see Shapley and Howarth, A Source Book in Astronomy, p 49 (1929)

R Wolly, Geschichte der Astronomie, p 420 (1877)

Hist de l'Acad R des Sci., Paris 1771, p 423

A very full bibliography of the work done on clusters is to be found in Appendix E of Star Clusters, Harv Obs Monograph No 2 (1930)

In striking contrast to the present conception of a hundred globular clusters and hundreds of thousands of extra-galactic nebulae spread throughout measured millions of light years, with diameters of hundreds of light years for the clusters, and thousands of light years for the star clouds and nebulae, is the picture suggested by HALLEY's comment on his discovery of the Hercules cluster:

"But a little patch—and similar to the lucid spot around Theta Orionis (Orion Nebula), Andromeda (Andromeda Nebula), and in the Centaur (or Centauri)—most of them but a few minutes in diameter; yet since they are among the fixed stars.", they cannot fail to occupy spaces immensely great, and per-

haps not less than our whole solar system."

## b) Classification, Number, and Distribution.

8. A Comparison of Galactic and Globular Clusters. It is proposed to adopt in the present treatment only two main divisions—globular clusters and galactic clusters. The principal characteristics of globular clusters are strong central concentration and richness in faint stars (fig. 4 and 2). The galactic clusters (fig. 3), looser and much less populous, are extremely varied; for example, Messier 11 is relatively rich, Messier 35 is irregular, the Pleiades and Messier 16 are nebulous, and Messier 103 and N.G.C. 1981 may be but accidental groupings. The so-called moving clusters are merely the brighter and nearer of the galactic types in which radial or transverse motions have been measured.

In future studies, especially in the Magellanic Clouds, we may find examples of clusters in a transitional stage between the richer galactic groups and the most open globular clusters. At present, however, there seems to be a rather sharp division which distinguishes the globular clusters as a special group of sidereal organizations—a group limited to about one hundred objects. The galactic clusters grade indefinitely into multiple stars in one direction, and in another into the condensed systems like Messier 11 and N.G.C. 2477 which closely simulate loose globular clusters.

Clear discrimination between galactic and globular clusters is also possible on the basis of distribution in the sky. The most conspicuous feature of the distribution is that galactic clusters are almost exclusively in the Milky Way and distributed irregularly throughout all galactic longitudes, while the globular clusters are rather widely scattered in latitude, but quite restricted in longitude. The globular clusters are, in fact, mostly in one half of the sky, as will be shown in subsequent diagrams.

4. The Number of Clusters. Thousands of new nebulae and millions of stars have been disclosed by modern telescopes and photographic plates, but the essentially complete listing of globular clusters antedated photography. Every recognized globular cluster except one bears a number from the New General Catalogue of Drever, and all but a few were catalogued more than ninety years ago in the earlier Herschelian lists. This early completion of the discovery of the globular clusters led Bailey<sup>2</sup> to suggest that the limit of the region occupied by these systems had been reached, a suggestion that appears to be supported by subsequent work<sup>3</sup>.

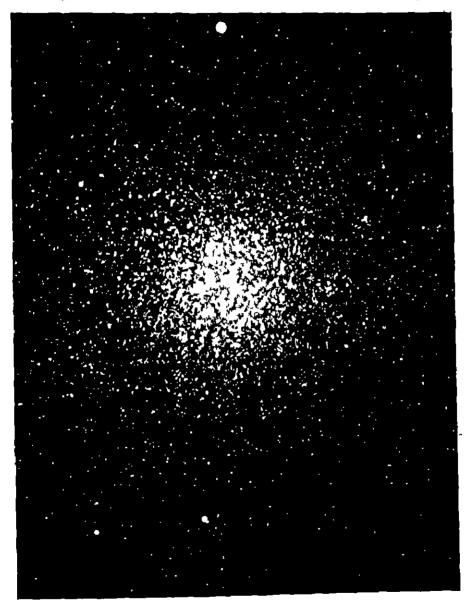
There is, however, a vast difference between cataloguing an object and

<sup>&</sup>lt;sup>1</sup> The term galactic cluster, suggested by TRUMPLER [Publ ASP 37, p. 307 (1925)] and others, is a natural name for the non-globular cluster, which is almost without exception near the galactic plane. It replaces the term "open cluster" which has caused some confusion because of the open type of globular cluster.

<sup>2</sup> Harv Ann 76, No. 4 (1915).

A special study now in progress at Harvard, of the environs of the Large Magellanic Cloud adds several new globular clusters to the list; some of them may not be outlying members of the Cloud, and two or three are not N.G.C. or I.C. objects. In A N 246, p. 171 (1932) LAMPLAND and TOMBAUGH report that N.G.C. 5694 is stypical globular cluster.

recognizing its true character. Many of the entries given in the New General Catalogue (N G C) as globular clusters have proved to be something else, generally galactic groups or extra-galactic nebulae, and thirty-four of the globular clusters now recognized were not described as such in the New General Catalogue.



1/1g 4 (Hobular cluster ω Contauri, taken with 43-inch Boyden tolescope at the Harvard Observatory

The large photographic telescopes have been of service in recent years in examining many faint and doubtful NGC objects, and an occasional addition to the list of globular clusters has resulted. A number of remote groups are still

questioned, however, even after some of them have been tested with large reflectors. The most doubtful globular clusters, which are marked with daggers in Appen dix A, are the following1:

N.G.C.	Radec	Galacilo	Distance <sup>3</sup>	Notes
5946 6352	0438~71 1528~50 1718~48	295+04 308-07	32,2 19,7	Rejected; see Harv Circ 271 (1925). A small, poor, loose cluster in a rich region. A comparatively large cluster of very laint stars, on the edge of the Milky Way.
	1759~00 1759~08		26.7 38.7	A small cluster on the edge of a rich region, with few stars.  A very faint cluster in a large obscured area.

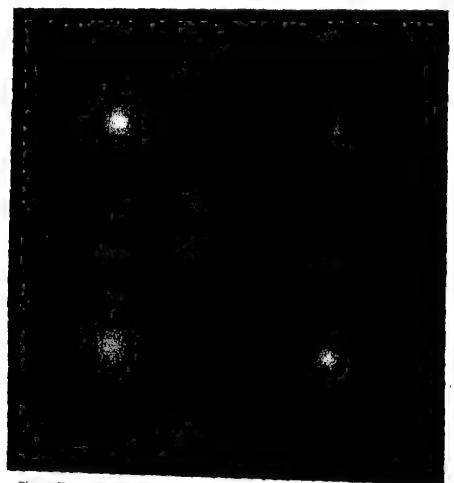


Fig. 2. Four exposures of the globular cluster Messier 13 taken at Mount Wilson.

SAWYER and SHAPLEY, Harv Bull 848 (1927).

The approximate positions for 1900 in equatorial coordinates are conveniently contracted for tabulation into the form here given; the first four ligures give the hours and minutes of right ascension, and the sign and subsequent figures indicate the declination in degrees (and may be extended to minutes, II desired). The distance in kiloparsees is estimated on the assumption that the clusters are globular.

The numbers of globular clusters have been discussed by Bailer, Hinks, Bohlin, and Miss Clerke, but the data on which their estimates are based lack homogeneity. Melotte's catalogue, however, which was made from the Franklin-Adams plates and contains eighty-three globular and one hundred and sixty-two galactic clusters, constitutes a fairly homogeneous list of all clusters with diameters greater than one minute of arc and brighter than the exteenth or seventeenth photographic magnitude. His list of galactic clusters is revised and extended in Appendix B, which contains 249 entries. From his list of globular clusters a few objects have been dropped, others have been added, mainly as a result of Hundle's work and my own with the 100-inch and 60-inch reflectors at Mt. Wilson. The total number accepted for the table in Appendix A is 103,



Fig 3 Galactic cluster NGC 3552 taken with the 13-inch Boydon telescope at the Harvard Observatory

including ten globular clusters in the Magellanic Clouds. An example of a recent addition is the observation at the Lowell Observatory, verified at Mount Wilson,

BAILEY, Harv Ann 76, p 43 (1915), Hinks, M N 71, p 693 (1911). Bonus, Svenska Vet Akad Handl 43, No 10 (1909), Clerks, Problems in Astrophysics (London) p.428 (1903).
 Mem R A S 61, p 75 (1915).
 See Footnote 3 on page 700.

that the object NGC 2419, described in the NGC as "pB, pI, lE 90", vgbM, \*7 8 267", 4" dist", and not listed by MEIOTER, is in fact a remote globular cluster in a part of the sky that is otherwise devoid of these systems

Some of the faint extra-galactic nebulae, as yet unresolved, may prove to be essentially globular star clusters, perhaps with greater distances and dimensions than those now known. A comparative study of the distribution of light throughout the images can, however, give us some indication of their nature, then distribution with respect to other extra-galactic objects will probably show most of them to be sidereal systems of a higher order than globular clusters

5. Classification of Galactic Clusters. In the studies of galactic clusters at Harvard we have for some time followed a two-dimensional classification. One parameter is related to the apparent number and concentration of the stars and may be called compactness, the other depends on the distribution of spectral classes among the cluster members.

The classification based on appearance is intended to cover the whole range of galactic clusterings, from multiple stars to globular clusters. The subdivisions

are as follows

a) Field irregularities. That there are many deviations from random stellar distribution is obvious from star counts, or even from a casual inspection of photographic plates in nearly any region of the sky. There seems to be no immediate need of attempting to unravel or catalogue such non-uniformities in stellar fields, but the assignment of a classification letter to the field irregularity is recognition of its significance in stellar distribution.

b) Star associations. In this category fall wide-spread moving clusters, such as the Ursa Major group, and the peculiar stars of high and parallel velocities. The class will be recruited largely through studies of proper motion and radial

velocity. It grades imperceptibly into the next class

c) Very loose and megular clusters, typified by the Hyades and the Pleiades. The large cluster of bright stars around a Perser might be placed in this class, or better, perhaps, placed with the Orion Nebula cluster in class b Classic corresponds in general with BAILEY'S D3 and with MFLOTIL'S IV

d) Loose clusters Messier 21 and Messier 34 are examples of a class

equivalent to BAILLY'S D2 and MIJOTIE'S III

e, f, g) Compact clusters. These three groups are equivalent to Bailey's D1 and Merotre's II. The division into three types is on the basis of richness and concentration, examples are Messier 38, Messier 37, N G C 2477. In the classification of clusters the globular systems follow immediately after class g. In fact, several of the most compact class g galactic clusters appear more nearly like globular clusters than do the loosest globular clusters classified as such by criteria other than appearance.

In practice the galactic clusters are generally taken to comprise only classes at to g. The distribution among these classes of the 249 clusters listed in Appendix B.

15 as follows

Class	Number
c	22
d	85
e	67
f	46
g	29

I have found it convenient to divide galactic clusters also into two principal groups on the basis of the spectra or colors of the component stars (1) The Pleiades type, and (2) the Hyades type Each includes members of classes c to g

In the Pleiades type the stars, almost without exception, lie along the "main branch" of a Russell diagram, with the earliest classes B or A; in the Hyades type, yellow spectral classes occur with the same apparent brightness as the predominant A stars,

More than ninety-five per cent of the galactic clusters for which spectral classes or colors have been determined fall into one or the other of these two groups, which are about equally numerous. There are a few aberrant clusters. Messuer 67, for instance, appears to be a variant of the Hyades type in that blue giant stars are absent. Prominent examples of the Plolades type are the double cluster in Perseus, Messier 36, and Messier 34; the Hyades type includes Messier 14, Messier 37. Praescop, and the scattered cluster in Coma. Barenices

TRUMPLER has also proposed and used a classification of galactic clusters based on spectral composition. For clusters that he has so far observed he uses Types 1a, 1b, 2a, and 2f, with provision for other types if found. Type 1 is equivalent, in general, to my Pleiades type, and type 2 corresponds to the

Hyades type

6. Classification of Globular Clusters. Notwithstanding the general similarity of globular clusters in size, form, content, and absolute brightness, there are many deviations from the average Clusters such as Messler 19 and  $\omega$  Centauri are conspicuously elongated; Messler 62 is strikingly non-symmetrical; N.G.C. 4147 is deficient in giant stars; and nearly one third of the globular systems are so loosely organized that their inclusion in the list depends on such further criteria as high galactic latitude, the presence of cluster-type variables, and the appearance of thousands of faint stars on long exposure photographs.

Until recently no systematic attempt has been made to classify the globular clusters beyond noting that some were variable-rich, some variable-poor; some open, some compact. A detailed examination by Miss Sawyer and the writer of the globular clusters on good Bruce photographs, which are available in the Harvard collection for practically all the 103 systems now listed as globular, shows that many intermediate forms exist between the loosest and most concentrated clusters. Instead of classing the clusters, therefore, in the two or three broad and obvious categories, such as compact, medium, loose, we arrange them in finer subdivisions, in a series of grades on the basis of central concentration. For the classification of individual clusters reference may be made to Appendix A. Class I represents the highest concentration towards the center, and Class XII the least. The distribution among the various classes and the mean photographic magnitude for each class are as follows:

Class	Magnitude	Number	C	Magnitudo	Mumber
A A A I I I	8,85 7,80 6,76 9,01 7,88 8,91	4 7 7 12 12 11	XII XI XIII AIII	7,90 7,85 8,84 8,88 9,54 9,58	8 10 10 9 9

The present classification of globular clusters is essentially a description of apparent central concentration. It is interesting therefore to note that there is no correlation of class with integrated photographic magnitude as determined

١

<sup>&</sup>lt;sup>1</sup> Publ A S P 37, p. 307 (1925). A more recent study of galactic clusters is presented by Tauarrier in Lick Bull 14, p. 154 (1930), where he gives a more complex, three-dimensional classification. The investigation also includes statistical material on distances, magnitudes, dimensions, and spectra.

from Harvard plates of small scale. The distribution of magnitude among the various classes is shown in the scatter diagram in Figure 4, where also the mean magnitude for a given class is plotted as a cross, and the average class for each interval of one magnitude is plotted as a circle.

To maintain homogeneity, the classifications of globular clusters were all made on plates with the scale of 1 mm = 1'. Superposed stars have occasionally interfered somewhat with the assignment of the class, especially for N.G.C. 4147, 6284, 6453, 6553, 6569, 6624. A few peculiarities were noted that are not completely taken care of by our classification based on central condensation alone. For

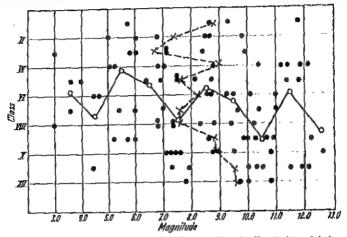


Fig. 4. The scatter diagram of classes of globular clusters (ordinates) and integrated photographic magnitudes. Circles and crosses indicate means.

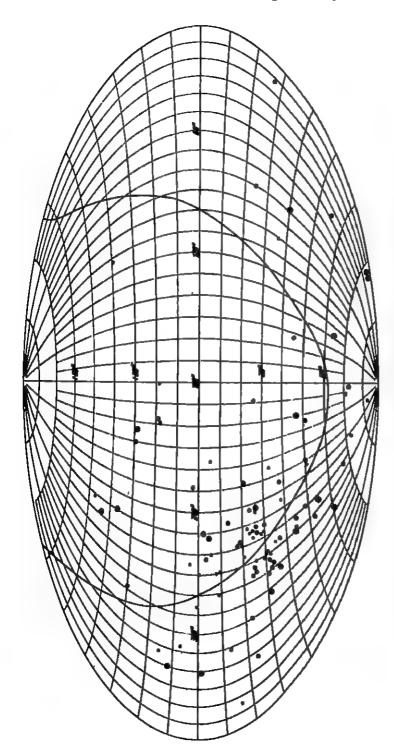
instance, the bright cluster  $\omega$  Centauri is peculiar in what appears to be a remarkable uniformity in the magnitudes of the brighter stars. Clusters somewhat similar to  $\omega$  Centauri in this respect are N.G.C. 5272 (Messier 3), 5927, 6273, 6656 (Messier 22). These clusters also resemble each other in their moderate concentration (Classes VI to VIII), and two of them,  $\omega$  Centauri and Messier 3, are the richest of all in variable stars. It should be noted, however, that the clusters with many variable stars are scattered throughout all classes.

In conclusion we observe that the classes of globular clusters are probably indicators of developmental age. They should prove increasingly useful in studies of linear diameters, motions, luminosity curves, and the deeper problems of the origin and life history of stellar clusters.

Table 1. Typical Globular Clusters of the Twelve Classes.

Class	N.G.C.	R.A. (1900)	Dec. (1900)	Pg. Mag.	Class	N.G.C.	R.A. (1900)	1200, (1900)	l'g. Mag.
II V V V V V V V	104 1866	21 34 .7		5,7 5,0 3,0 8,0 6,4 4,6	VII VIII X X XI XI XI	6402 6218 288	0 47 ,8	-23° 59' - 3 11 - 1 46 -27 8 -31 10 -16 10	3,6 7,4 6,0 7,2 4,4 10,8

7. Clusters in or near Obstructing Nebulosity. The large groups of bright B stars in Orion, Scorpio, and elsewhere are associated with important bright and dark nebulosity. The Pleiades nebulosity is well known. A number of



The galactic circle is shown torial coordinates. Small dots indicate more distant chistons. The clusters in the Magallanic Clouds have been contribed. 5. Distribution of globolar circturs m equatorial coordinates.

by a heavy line. The chatters in ti

nebulous galactic clusters, such as Messier 8, are on record, and clusters of the sort also appear in the Magellanic Clouds. It is doubtful, however, it must would be known of the nebulosity in these galactic clusters if their distance.

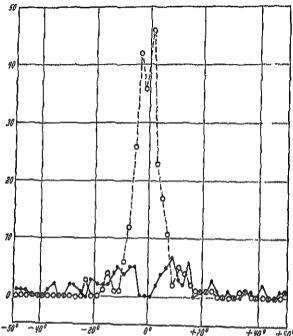


Fig 6 Numbers of galactic clusters (chicles) and globular clusters (dots) for two degree intervals in galactic latitude

were for times access of By implication, there fore, includesity in galastic clusters may be more common, than, appear from general mepsystems

There are a few its तेस्पतिहर्ष स्थानित । अस SIGNATURE NOT 61 Pl. and N G C 6569, that are more more po cognized dark or finns nous nebular Of these, the first appears to be dumined by one of the long dark treatter a from the Coal Sack, the second is at the edge of the heavy is Ophim to nebulosity N tell 18569 15 Black the day light in Sagittains but may also be involved in wepseld obscuring achidosity

Fo what extent the magnitudes and colors in galactic and globular

clusters are directly affected by associated nebulosity is not as yet deletimined. For individual nebulous stars Spares and Hubbit have found a rolen effect and presumably a corresponding deficiency in apparent brightness

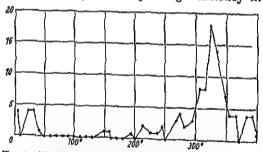
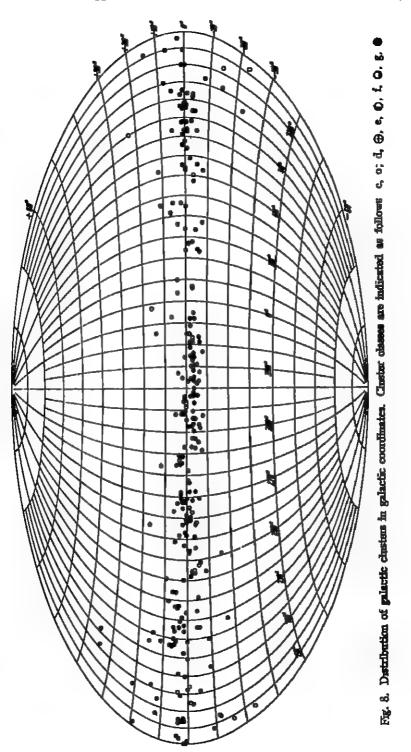


Fig 7 The frequency distribution of globular clusters in galactic longitude. Ordinates are numbers of clusters, abscissae, degrees of longitude.

8. The Apparent Distribution of Globular Clusters.
In ligne 5 is shown the distribution of globular clusters;
theremarkable contrast in the
galactic affiliation of the galactic and globular clusters is
shown in Figure 6. The equatorial and galactic coordinates
of globular clusters are given
in Appendix A, and a discussion of their distribution in
space appears in later mections,
The remoteness of these clus-

account for their observed scarcity near the galactic equator without vericusly affecting at the same time the distribution of the nearer galactic clusters

In Figure 7 is shown the distribution of globular clusters in galactic longitude. From this diagram and the preceding figure we find that the center of the system



of globular clusters lies in the direction of galactic longitude 327°, galactic latitude 0°. The probable error of this determination is about one degree. The corresponding equatorial coordinates are right ascension 17h 28m, declination -20°.

9. The Apparent Distribution of Galactic Clusters. The distribution of galactic clusters in galactic coordinates is shown in Figure 8. The high concentration in low latitudes is evident. The galactic clusters with latitudes greater than ±15° are given in Table 2. The high latitudes for Coma, Praesepe, the Pleiades, and the Hyades, are not remarkable, because the parallaxes are relatively large and the linear distances from the galactic plane are relatively small. The fainter galactic clusters in high latitude merit further detailed study.

Table 2.	Galactic	Clusters	with	Latitudo	Grentor	than	15°	4

N.G.C.	Gala		Rømarks		
2110101	Longitude	Latitudo	<u> </u>		
188	90°	+23°	}		
752	105	23	ì		
Melotte 22	134	-22	Ploinclos		
Melotte 25	147	~23	Hyades		
2243	206	16	1		
2281	142	- 18 - + 18	1		
2420	166	+21	1		
2548	196	+17	1		
2632	174	+34	Ргаеворо		
2682	184	+33	Messior 67		
Melotte 111	200	+85	Coma Boronices		
I 4665	358	+16	1		

An interesting and significant result of the special surveys that have been made of objects once doubtfully classed is the evidence that nearly every faint little-condensed cluster in galactic latitude higher than 15° or 20° is really globular, although for many of them short exposures and visual observations had originally recorded few stars. Long exposures, however, bring out the globular nature of such clusters. Nearly all the similar faint objects along the galactic equator remain open groups, with no condensed background of faint

stars appearing on long exposures.

10. Peculiarities in the Distribution of Galactic Clusters. The clusters listed in the catalogue in Appendix B do not extend deep into the galactic structure; they tell us nothing of the center or of the boundaries. There is significance, however, in certain peculiarities of their distribution. Already we have noted that in contrast with globular clusters they are rather uniformly dispersed in galactic longitude, and also that they are largely confined to the low galactic regions where globular clusters are scarce. There are two additional features of their distribution that are worth consideration: (1) the infrequency of galactic clusters in the first quadrant of galactic longitude; there are very few of these systems in the Aquila-Cygnus region of the Milky Way; (2) the narrow restriction of the clusters to low galactic latitudes in the direction of the galactic center and their wide dispersion in galactic latitude in the opposite part of the sky.

This second phenomenon might be explained as a consequence of the motions of galactic clusters in long orbits around the nucleus in Sagittarius. If their orbital inclinations differ from zero, when seen from the earth's eccentric position in the Galaxy those in the direction of the center would on the average appear to be in lower latitudes than those away from the center. It is probable that none of the galactic clusters that are now beyond the center of the Galaxy enters

our catalogue.

The alternative and, I think, preferable interpretation is that galactic star clusters are associated largely with particular galactic star clouds. Irregularities of distribution and concentration in low galactic latitude are therefore merely consequences of the distribution of the nearer star clouds. If the galactic clusters are closely affiliated with various star clouds, we may find them differing systematically in spectral and structural characteristics from one part of the aky to another We already have an indication of such diversity in the orientation of the axes of clongation, discussed in ciph 24 below. The brighter clusters of Auriga are rich and not strongly condensed (Messier 36, Messier 37, Messier 38); many of the small condensed clusters of Sagittarius are nebulous, and the groups in Carina are systematically bright,

# c) On the Spectral Composition of Clusters.

11. Integrated Spectra of Globular Clusters. Integrated spectra were determined for several clusters many years ago at the Lick, Mount Wilson, and Lowell Observatories, mainly by FATH1 and SLIPHER1, who found spectra of composite character, principally classes F and G. The HENRY DRAFER Catalogue records without close classification the integrated spectra of numerous clusters.

Miss Cannon has recently examined closely all available Harvard photographs showing spectra of globular clusters. The results are briefly summarized in Table 3, which gives the N G.C designation, the cluster class, and the spectrum. For some clusters, such as N.G C 4147 and 6624, the observed spectrum may be largely due to one or two stars, and they of course may be foreground objects.

Table 3 Spectra of Globular Clustera,

		F	4.000	0-410-0-1	
N.G.C.	Citaler Class	Spootral Cimu	n.g.c.	Class Class	Speciful Class
104 362 1261 1851 1866 1904 2808 4147 4590	A W H H H H H H H H H H H H H H H H H H	GS GS GG GO F8 F8 KO A7: Note	6293 6304 6316 6333 6341 6356 6388 6397 6441	IV III III III III III III III III III	G5 K: G5 K0 K0 G: K0 G:
5272 5286 5824 5904 5986 6093 6121 6205 6229 6254 6266 6273 6284	AH A	G G F8 G F8 K0 G0 Note Note K0 G5:	6624 6626 6637 6652 6715 6723 6752 6864 6934 7078 7089 7099	A A A A A A A A A A A A A A A A A A A	MO G5 K2 K5 F8 G5: G0 G0 F F5 F8

N.G C. 4590 Dark lines are seen in the violet.

5024 Dark lines  $H\partial$ , H, and K faintly seen.
6229, Several dark lines are seen, apparently including H and K. 6254. Dark lines in the violet appear to be H, R, and H \( \zeta \).

<sup>1</sup> Lick Bull 5, p. 74 (1908); Mt Wilson Contr 49 (1911).

Elary Bull 868 (1929).

A frequency diagram of the classes is given in Figure 9; classes F, G, and K of Table 3 are taken as Fo, Go, and Ko. The class of spectrum does not appear to be closely related to cluster class, apparent magnitude, or any other significant property of the clusters. We have here only an indication of the probable diversity

AS FO FS F8 GO GS NO KE KS NO Fig. 9. Frequency curve of integrated spectra of globular clusters. Coordinates are numbers of clusters and spectral classes.

in predominant type of the stors that are effective in producing the integrated spectrum.

12. Stellar Types in Globular Clusters. From integrated spectra and colors we pass to the types of individual stars in globular clusters, noting some similarities to the distribution of types in the Galaxy, but also some important differences.

a) Common Spectral Classes. The color indices in various globular clusters show a normal range from about -0.3 to +1.6. This indicates, no doubt, the presence of all spectral classes from B to M; and normal spectra have in fact been directly observed from A to G. The average color index\* in Messier 13 is -|-0.55, corresponding to the spectrum gF4.

Seventeen per cent of the stars in Messier 13 brighter than the working limit

(photovisual magnitude 15.5) have negative color indices. In Messier 3, on the other hand, there is a smaller proportion of negative color indices (4,7 per cent down to photovisual magnitude 17,00), but an excess of Class A stars of about the magnitude and color of the cluster type variables. It should be noted, however, that an error in the zero point of either photovisual or photographic magnitudes would shift the spectral frequency curve bodily. Such error may exist, and may not be inappreciable.

b) The Color-Magnitude Arrays. The distribution of color indices and photovisual magnitudes are shown for Messier 22 in Table 4. The tabulated quantities are numbers of stars? The last tabulated line or two are near the practical fainter limit for magnitude work and may be deficient in numbers and inaccurate. The color classes, b, a, f, ..., corresponding to the color index intervals -0.4 to 0.0, 0.0 to +0.4, +0.4 to +0.8, ..., are nearly analogous to the spectral classes B. A. F. . . . This analogy is close because the cluster stars under study are all giants; the agreement would not be so satisfactory for dwarfs.

In the array for Messier 22 the dispersion of magnitude within any one color class is conspicuously small. All stars are included which are brighter than the magnitude limit of the photovisual plates and within 5' of the center of the

<sup>1</sup> SHAPLEY, Mt Wilson Comm 44 (1917).

SHAPLEY, Mt Wilson Contr 116 (1917); see also Frase, Mt Wilson Ann Rop 9. p. 219 (1913); 10, p. 268 (1914); SAMFORD, Mt Wilson Ann Rep 14, p. 212 (1918); Pop Astr

<sup>27,</sup> p. 99 [1919].

Harv Obs Mon 2 (1930); Harv Bull 874 (1930). Ten Bruggencate has plotted the courdinates (my magnitudes and colors) for the individual stars used in making the color-magnitude summaries for Messier 13 and Messier 3. (Die Sternhausen, Borlin, 1927). I think there is little gain and some deager in defailed subdividing of the observational material. Experience with the photometric measures in globular clusters leads to a bollel that the group values presented in my color-magnitude arrays go as far as is justifiable in subdivision.

Sharks, Mt Wilson Comm 16 (1915).

Table 41 Color-Magnitude Array for Messier 22

							Color	Class						
Limits of Photoviscal Magnitude	< ъо	b0 to b5	b S to a O	10 15	4 5 10 10	fo lo f5	15 to g0	g O to g S	6 5 10 k0	k O to k 5	k S io an O	to to to	>= 5	All Culcus
10,20-,39 ,40-,59 ,60-,79 ,80-,99 11,00-,19 ,20-,39 ,40-,59 ,60-,79 ,80-,99 ,40-,59 ,60-,79 ,80-,99 ,13,00-,19	11111111111111	11111111111111	1111111111111	1111111111111	11111111111111		1 2 1 3 1 6		1 1 1 1 1 1 2 3 8 5 5 5 3 3 3 3	1 1 1 1 1 2 2 5 1 2 2 2 1 1 1	1111334444	3611	1 1 3 3 1	1 4 7 9 5 5 14 13 25 11 10 20 23
,40—,59 ,60—,79 ,80—,99 14,00—,19 ,20—,39 ,40—,59	1	11111	1 2 11 19 3	- 1 1 40 26 -	1 4 17 61 20	8 12 34 39 39 39 2	59 12 3 -	6 16 7 - -	1		111111			57 106 71 156 68 3
Totals	1	3	36	68	105	138	123	57	45	17	10	12	8	623

cluster It is of interest that more than six per cent of the stars have negative color indices, the cluster resembling in this respect Messier 13 rather than Messier 1.

No correction has been made in the color-magnitude array for superposed stars. The cluster lies in a rich star cloud in Sagittarius, and probably ten per cent of the stars included in this discussion are not cluster members. The color-magnitude array is therefore applicable both to the cluster and to the star cloud, and the small dispersion in brightness of both together suggests that the two are associated. The color-magnitude arrays establish the fact that in the condensed clusters, as well as in some loose galactic groups, the average color is redder the higher the visual brightness. The result naturally bears on current considerations of the evolution of stars.

The general similarity of globular clusters, especially in the color-magnitude relation for giant and supergiant stars, is shown by a comparison of the brightest stars in Messier 3 and Messier 13 with the brightest stars in the faintest and most remote globular cluster known. N G.C. 7006 is five times as distant as Messier 3 and Messier 13, yet the most luminous stars in all three clusters have about the same average color and the same progression of color with magnitude. The mean results are as follows

	Mone Photographic	Mumber of	Mean Color
	Magnitude	Blass	Todax
N.G C. 7006	16,46	38	+1,09
	13,17	35	+1,15
	12,72	36	+1,02

<sup>1</sup> Sec Hery Bull 873 (1930)

<sup>\*</sup> Mt Wilson Contr 155, p. 8 (1918).

A similar result is found in all globular clusters tested, though some, such as

N.G.C. 4147 and N.G.C. 5053, are less populous in giant stars.

13. On the Masses of Glant Stars. The color-magnitude array can be transformed into a relation between spectral class and mass by means of the observed mass-luminosity relation for galactic stars. It is necessary to assume that we can safely replace color class by spectral class for giant stars; the uncertainties involved both in this assumption and in the temperature scale, used for reduction from photovisual to bolometric magnitude, are not negligible, but still they are not serious enough to falsify the results except for stars of extreme color. It is possible that the chief source of error lies in the mass-luminosity curve itself, which depends mainly on nearby double stars and possibly is inappropriately applied to single stars, especially in a globular cluster.

The computation of the stellar masses in terms of the sun's mass for successive intervals of magnitude and color has been carried through for Messier 22; the results are shown in Table 5. The distance modulus,  $m_{pv} - M_{pv} = 14,16$ ,

Table C. The Mass-Spectru	n Relation for Mesa	ior 22.
---------------------------	---------------------	---------

Apparent Pv. Mag.	Spectrum	Absolute Pv. Mag.	Absolute Bol. Mag.	Mass
11,2	M2,5	~2,96	-4,62	29:
,4	159.0	-2.76	<b>−4,10</b>	22,4:
.б	IC5,8	-2,56	-3,72	17,8
.8	173,0	-2,36	- 3,13	14,1
12,0	K1,0	-2,16	-2,74	41,7
,2	G9,0	-1,96	2,41	40,0
, <del>4</del>	G7,0	-1,76	2,10	8,3
,6	G5,5	-1.56	- (,84	7,4
,8	G4,0	-1,36	-1,58	6,5
13,0	G2,5	-1,16	-1,30	5,9
,2	G1,2	-0.96	- 1,16	5,4
,4	F9,8	-0,76	-0,80	4,8
,6	F7.8	-0,56	-0,58	4,5
.8	F5,8	~0,36	-0,36	4,1
14,0	F3,0	~0,16	~0,16	3,9
,2	A9.5	+0,04	+0.04	3.7
,3	A6,8	+0,14	+0.07	3,6
.4	B7.5	+0,24	~0,49	5.7

is taken from Appendix A; the reduction to bolometric magnitudes and the computation of the masses are made with the aid of tables given by EDDINGTON 1. The masses of the reddest stars would have been from ten to twenty per cent less with Brill's scale of temperatures and corrections to bolometric inagnitude. The values of photovisual magnitude and spectrum in Table 5 are read directly from the curve drawn through a plot of the colors and magnitudes of the individual stars that appear in the color-magnitude array.

Masses for the average giant stars of various spectral classes in Messier 22 are as follows:

A0,		4		<4.8	F5 .		,	4.0	Ko				,	10.8
A5.	ě			<3,5	Go ,	,	,	4.9	IK5	ï	,			16.5
F0.			÷	<3,6	G5,			7,0	Mo	,	,	4		24,0

It is possible to give only upper limits of average mass for classes A0, A5, and F0 because of the incompleteness of the observational material for the corresponding intervals of color index.

<sup>1</sup> Internal Constitution of the Stars, Chapter VII (1926). Babelsberg Veröff 5, p. 16 (1924).

For the rich galactic cluster Messier 37, von Zeipel and Lindgren find the mass of the giant g5 stars 2,15 times as large as the average mass of the b and a stars, in good agreement with the present results. They have used space distribution of the stars as a criterion and a measure of the masses of different types.

It is interesting to note the small dispersion in color for stars of a given photovisual magnitude. Accepting the mass-luminosity relation, we can only conclude that in a globular cluster such as Messler 22 the grant stars of a given

mass have a very small spread in surface temperature.

- 14. Spectra in Individual Galactic Clusters. Numerous investigations have been made of the colors and magnitudes of galactic clusters, notably by TEN BRUG-GRNCATE, DOIG, GRAFF, HERTZSPRUNG, PICKERING and PLEMING, RAAB, SEARES, SHAPLEY, TRUMPLER, and VON ZRIPEL and LINDGRENS. The HENRY DRAPER Catalogue contains spectral data for only the brightest clusters. The Harvard material is discussed first, followed by brief accounts of a few individual clusters and the spectral classification of clusters by TRUMPLER.
- a) Harvard Studies. Mrs. Flammed tabulated the spectra for seven galactic clusters, the Piciades, Praesope, Coma Berenices, I.C. 2602, N G C. 3532, Messier 6, and Messier 7. The stars for which spectra are classified are distributed over a larger area than that actually covered by the clusters, and foreground stars of course cannot generally be differentiated and excluded Some very faint stars, barely distinguishable on the plates, are included. The results are summarized for Class A in Table 6.

Table 6. Percentage of Class A Stars in Seven Galactic Cinsters.

	Clauter	Stem Classified	Stars in H.D.C.	Persont Class A
Pictados , Pracespo I C, 2602 , N G C 3532 Coma , Mossier 6 Messier 7		91 90 64 204 117 91 346	58 135 6 75	65 31 77 93 15 75 78

Limits indefinite.

Although the classification was crude, and for some stars quite uncertain, the existence is clearly shown of a different spectral distribution in Praesepe and Come from that in the other five clusters. It is the same distinction that is now recognized in the Pielades and Hyades types, or in TRUMPLER's types 1 and 24.

The frequency of A stars in galactic clusters has led to attempts to determine spectral parallaxes on the basis of the material of the HENRY DRAPER Catalogue"; but because of the wide dispersion in magnitude the attempts are not always happy.

b) Spectra in the Brighter Galactic Clusters. The Plaindes, the Hyades, and Come fall under the head of "very loose and irregular clusters",

Svenska Vet Akad Handl 61, No. 15, p. 126 (1921).

See bibliography in Hary Mon No. 2 (1930).

B. C. PICKERING, Hary Ann 26 (1897); see also Table 6.

Publ A S P 37, p 307 (1925). See note 1, p. 705, on his later work.
 Doto, J B A A 33, p 201 (1925); RAAB, Lund Medd, Série II, No. 28 (1922).
 HERTESPRUNG, M N 89, p. 660 (1929) See also Harv Bull 764 (1922)

division c in the classification of galactic clusters in ciph 5. Figure 10 shows for the Pleiades the spectrum-magnitude relation as compiled by Hertzsprung<sup>1</sup>. The spectral data on h and  $\chi$  Person, Messier 11, and two southern clusters may be summarized as follows

1 The Double Cluster in Perseus Sixty-six bright stars in the double cluster in Perseus, classified mainly by Trumpler<sup>2</sup>, range in spectrum from A0 to B9, and in magnitude from 5,5 to 10,9. Two matters of exceptional interest

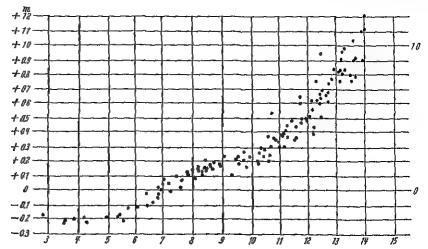


Fig 10 Relation of color to luminosity in the Pleiades Ordinates, color indices, abscissae, photographic magnitudes (From Herzeprung)

in this cluster are the fact that a large number of the brighter stars show the c-character, and that the numerous bright line stars are by no means the brightest members of the cluster

- 2 Messier 11. In supplementing my earlier work on the colors in Messier 11, I found a from plates made with the 100-inch reflector at Mount Wilson that the brighter spectra are chiefly of class A. This observation was later verified by Lindblad on other Mount Wilson spectrograms. The spectral classes of fifty-nine stars in and around the cluster have since been given by Trumpler.
- 3 NGC 3532 and NGC 3766 The distribution of spectra in two southern galactic clusters has been derived by BECKER from his own photographs made at La Paz<sup>8</sup> He finds percentages as tollows

	B0B7	B8A1	A 5A8	K0	K4	Number of Stars
NGC 3532 NGC 3766	3,8 44,2	86,3 39,5	1,5 4,7	8,4	11,6	131 13

4 Lick Bull 12, p 10 (1924) 5 A N 236, p 327 (1929)

Ihe magnitudes determined for this cluster are apparently in error, probably by a constant amount, notwithstanding the consistency of the Mount Wilson photometric plates [Mt Wilson Contr. 126 (1917)]. The color indices are systematically too great, as shown by my own spectrum plates (unpublished), and subsequently by the similar work of Lindblad and Inumpler. A correction of -0.4 to the photographic magnitudes is indicated by an unpublished Harvard plate, but even then the colors and spectra are inconsistent. There is a probability of differential light absorption within the cluster.

For N G C 3532 Mrs. FLEMING recorded ninety-three per cent of the 204 stars as Class  $A^1$ 

c) TRUMPLER'S Investigations The kinds of spectral distribution among the stars of a galactic cluster, first recognized in the early Harvard work, and amplified by all subsequent studies, are defined in some detail in TRUMPLER'S scheme of classification (ciph. 5 above), and a number of galactic clusters have now been assigned by him to the classes and their subdivisions. For fifty-two clusters the relative numbers in the various classes are as follows

Тура	Number	Тура	Number
1 b	24 6	2f Others	1
38	20		_

It will be seen that the Pleiades type preponderates among the systems bright enough to classify. This may, however, be an effect of selection, as Type 1b contains far brighter stars than any of the others. The bearing of this selection on estimates of distance is considered on page 748, footnote 1.

## d) Variable Stars in Star Clusters.

15. The Frequency and General Properties of Variable Stars in Clusters. Periods have been determined for 466 variable stars discovered in forty-five globular clusters; all but nineteen are found to be cluster type Cepheids. There is a slight correlation between frequency and galactic latitude, the rich clusters having a greater mean distance from the galactic plane than have the poor. The latter are distributed equally throughout all classes, while the rich clusters are confined to the intermediate classes. It seems unlikely that observational selection is responsible for this result; the affect, however, may be due in part to the decreased discovery chance in a very condensed cluster

The general properties of variable stars are discussed elsewhere. There is no evidence that the Cepheid variables in clusters, whether of short or long period, are different in their various characteristics from those in the Galaxy at large. The color changes and light curves are of the usual sort. The long period variables in 47 Tucanae are also normal in period, range, and form of light curve.

Certain features of cluster variables, however, are to be noted. The great majority are, on the average, 1,5 to 2,0 magnitudes fainter than the brightest stars in the cluster (see ciph 31 below). There is observed, particularly in  $\omega$  Centaurl, Messier 3, Messier 5, and Messier 13, a definite fainter limit to the magnitudes of Cepheids, similar to that found in Miss Leaverr's survey<sup>4</sup> of the Magellanic Clouds. The negative results of the searches for faint variables, and the form of the period-luminosity curve, which flattens conspicuously for periods less than a day, suggest that dwarf Cepheids do not occur. There is likewise no convincing evidence of eclipsing binaries in any globular cluster<sup>5</sup>; but the faintness of such stars would preclude their discovery on most of the existing plates.

The peculiarities of variables in clusters lie in the relative numbers of different types and subtypes as compared with those in the galactic system, galactic star clouds, or the Clouds of Magellan; but it is to be noted that very serious factors of incompleteness and selection affect the comparison of clusters

<sup>&</sup>lt;sup>1</sup> See Table 6 above. Previous to 1930

LUDENDORFF, volume VI, chapter 2. 4 Harv Circ 173 (1912).

But see Guttinger and Practic, Sitzber Prouss Akad Wise 1925, p. 508.

with the Galaxy, and also that there appear to be just as great differences in variable star content between clusters as there is, say between  $\omega$  Centaum of 47 Tucanae and the solar neighborhood

16. A Summary of Known Variables. Despite a careful search, few variable stars are definitely known to belong to galactic clusters, some that have been tentatively assigned to such systems are of unrecognized type, and probably he in the surrounding star fields. Many have been found, however, in globular clusters, as remarked above The history of their discovery is short Examining some of his earlier photographs, Di Common first noted the probable variability of some stars in Messier 5. Professor E C Pickering<sup>2</sup> in 1889 and Mr David PACKER<sup>8</sup> in 1890 also made some carly observations of the variables in globular clusters, which were independently confirmed by Barnard a few years later 4 But the whole development of this special branch of variable star astronomy is essentially due to Professor Bailey, whose extensive research on globular clusters, begun about thirty years ago, is the basis of much of our knowledge concerning cluster variable stars. Employing mainly the photographs made at Arequipa with various telescopes, BAILLY has found the majority of cluster variables now known, and has made by far the most important investigations of light curves and periods. Aside from BAILEY's work, the discovery and study of the variables has been almost exclusively the work of Miss Woods at Harvard, BAADE and LARINK at Bergedorf, and the writer and his collaborators at Mt Wilson and Harvard [see references in Harv Mon No 2 (1930)]. LARINK has made an extensive check of BAILEY's periods for cluster-type variable stars in Messier 3, finding that, after a twenty-year interval, 82 periods were unchanged and 29 probably had varied My similar check on 54 of Balley's variables in Messier 5 results in periods accurate to within a tenth of a second; in this cluster nearly all the periods are constant throughout an interval of thirty vears

The data at present available concerning the variable stars in globular clusters are summarized in Table 7 Clusters examined with care but without discovery of variable stars are also included in the table. Some stars suspected of variability are omitted in the absence of numerous or decisive observations. Three of these, for instance, are in the Hercules clusters, where my measures on a few plates can not be considered to furnish sufficient evidence of variability. In crowded regions and for close doubles the photographic development (Eber-HARD) effects may produce spurious variability, for it varies from plate to plate under ordinary working conditions Aside from this and similar uncertainties, which lead to the inclusion and exclusion of suspected variables, there is another element of incompleteness in these tabulated results because of the difficulty of thoroughly examining the centers of clusters, and also because of the small number of plates sometimes involved in the surveys In general it may be said that scarcely a cluster has been examined with the accuracy and thoroughness necessary to detect ordinary eclipsing stars of short range or narrow minimum, and to exhaust the possibility of Cepheids of small range

<sup>1</sup> M N 50, p 517 (1890), 51 p 226 (1891)

AN 123, p 207 (1889), Harv Circ 2 (1895)
Sid Mess 6, p 351 (1890), 10, 170 (1890), Engl Mech 51, p 378 (1890).

A N 147, p 243 (1898)
 SHAPLBY, Mt Wilson Contr 116, p 79 (1915)

EBERHARD, Zf Phys 13, p 288 (1912), Publ Astrophys Obs Potsdam No 84, p 1 (1926)

Table 7 Summary of Variables in Clusters

		150	10 7 10	umma	ry of	Varia	bles ir	ı Clus	ters,
n.g.c.	Y	A	Clam	Hillip- Liekty	Vari- ables	Por <14	  >14	Sur- proted	Helicusco
104	272°	~449	III	8	7		3		1, 2
288	214	-88	x	9	2			=	3 2
362	268	-46	ПП	8	14	_	l _	_	1
1851	211	-34	II	b	3	_		_	4,5
1904	195	28	v	Ŋ.	5	_	_		1
2419	148	+23	IIA	9	26	_	_		40
3201	244	+10	x	9	61	_	-		6. 7
4147	227	+78	IX	Ľ	4		_	8	8, 42
4590	268	+37	x	0	28	27	4	_	9, 10
4833	271	- 8	VIII	9	5	<u> </u>		=	5
5024	307	+79	v	o o	42	<u> </u>	_		11, 12, 41
5053	310	+77	XI	9	9	8	-	_	13
5139	277	+16	VIII	8	132	95			
5272		+77	VI	8	166	110	5		1, 14
5286	280	+10	v	9,5	100			79	1, 15, 16, 17, 18, 19
5466	8	+70	ΧП	913	14	12	_	_	20
5904	333	+45	v	9	84		_	8	12
5986	305	+13	VII			69	3		1, 21
6093	320	+18		10	4		-	_	11
6121	319	+15	ıχ				_	l -	1, 39
6205	26	+40	Ÿ	9	33	3		5	22
6229	41	+39	VΠ	9,5	7	1.	2	3	1, 17, 23, 24
6266	320		ΪV	_	4	_	-	-	8
6293	325	+ 7 + 8	ΪΫ	8	26		-		1
6333			VIII	9	3	_		-	25
6341	333	+10	IV	9	.1	_	-	-	3
6362	35	+34			14	-	~	-	17, 26
6397	293	-17	X	8	17	_	-	-	27, 28
5406	304	-12	IX	9	2	_	-	-	1.
6426	356	+15	IX.	9 9 9	2	_	-	-	40
0539	348	+ 6	X	9	4	_	-	_	29
6541	317	-12	m	9	1	_	-	_	30
6553	333	- 4	XI	9	_	_	<b>-</b> -	2	25
6584	310	-18	VIII	9	_	-	_	_	20
6626	336	- 7	IV	9	9		_		1
6656	338	- 9	AII	8	21	9	2	4	1, 31, 32, 33
6712	353	- 6	IX		1 1		_	-	8
6723	327	-18	ATT	9,5	17	16	_	_	1, 34
6752	303	-26	vi	_	1	_	-	-	1
6779	30	+ 7	X	8	4	-	-	2	25, 35
6809	335	<b>-24</b>	жі	9	2	_ ;	-	_	1
6864	348	-28	_I	9	11		-	5	25, 30
6981	3	-34	IX	_	29	29	-	5	8, 25, 36
7006	32	-20	I I		44	11	-	_	25, 37
7078	33	-19	IV	8	74	60	1 1	-	1, 21
7089	22	-37	II	9	11	-	1	-	1, 38
7099	356	-48	V	9	3	_	_	_	11
7492	23	-65	ХП	9	9		1	5	3

1 Balley, Hary Ann 38, p. 2 (1902) 2 Balley, Hary Bull 783 (1923). 3 Mt Wilson Observatory, unpublished. 4 Balley, Hary Bull 802 (1924). 5 Miss Sworz, unpublished. 6 Miss Woods, Hary Circ 216 (1919) 7 Balley, Hary Circ p. 234 (1922) 8 Miss Davis, Publ A S P 29, p. 260 (1917). 9 Shapley, Mt Wilson Contr 175 (1920). 10 Shapley, Publ A S P 31, p. 226 (1919). 11 Haade, Hamburg Mitt 5, No. 16 (1922) 12 Baade, Hamburg Mitt 6, No. 27 (1928). 13 Baade, Hamburg Mitt 6, No. 29 (1928). 14 Inness, Union Circ 59, 201 (1923). 15 Shapley, Mt Wilson Contr 91 (1914). 16 Shapley, Mt Wilson Contr 176 (1920). 17 Guthings and Praces, Sitzber Freuss Aland Wilss 1925, p. 508. 18 Lardyk, Bergedorf Abhandhungen 2, No. 5 (1921). 19 Bardyaed, A N 172, p. 345 (1906). 20 Barley, Hary Bull 801 (1924). 21 Barley, Hary Ann 78 (1917). 22 Miss Lardyk, Hary Circ 90 (1904). 23 R A J 1, p. 16 (1924). 24 Shapley, Mt Wilson Contr 116 (1917). 25 Shapley, Mt Wilson Contr 190 (1920). 26 Miss Woods, Hary Bull 773 (1922). 27 Miss Woods, Hary Circ 217 (1919). 28 Miss Woods, (Continued sext page holow.)

### e) The Distribution of Stars in Globular Clusters.

17. Are Cluster Stars Arranged Spirally? In order to determine whether the frequently described spiral structure in or near the center of globular clusters could be seen on large scale photographs, I made a series of exposures on bright northern globular clusters some years ago with the Mount Wilson reflectors The exposures varied in length. When only a few hundred stars were shown in a cluster, the spiral structure could almost invariably be traced, if the exposures were longer, the spiral arms became inconspicuous, or another set of arms, sometimes with different center and pitch, was found or imagined. The conclusion was reached that the phenomenon is wholly illusory The significance to be attached to chance groupings and chance vacancies decreases remarkably with increasing exposure time. Nebulous obscurations that are reported to conceal the brighter stars are found, upon deeper penetration, to be ineffective for the more numerous faint stars, and therefore they cannot be real

Spiral structure is the easiest form to visualize in centrally concentrated random groupings-especially when the number, pitch, thickness, origin, length, symmetry, and definiteness of the spiral arms are all arbitrary. Structural features other than flattening and central concentration may be present, but it is certainly madvisable to conclude definitely, from knowledge of only a small percentage of the total number of the stars, that such structure occurs Probably in only one globular cluster (Messier 22) have stars as faint as the sun been photographed, and in only a tew of those studied for stellar distribution have

stars other than giants or supergrants been thoroughly examined.

The a priori argument against the existence of spiial form in the images of globular clusters is, of course, simply that the clusters are three-dimensional Cleanly traceable spiral aims would mean a most remarkable and unbelievable arrangement of stars in systems that are always nearly spherical. The discussion in eigh. 22 of the ellipticity of globular clusters will show how little they are flattened Even the images of the much sparser galactic clusters are very rarely so elongated that we can assume them to be essentially two-dimensional

18. On the Laws of Distribution. The first detailed numerical consideration of the space arrangement of stars in globular clusters was made by Professor E. C Pickering who examined the distribution in ω Centauri, 47 Tucanae, and Messier 13, and proposed general empirical relations connecting surface

density, y, with the distance from the center, r, in the forms

$$y = \int (1 - r^2) \, dz$$

 $y = \int (1 - r)^n dz$ 

Subsequently much time has been devoted to studies of the laws of the distribution of stars in globular clusters. Various formulae relating the number of stars per unit volume, N, with distance from the center of the projected image

and

Hary Ann 26, Chap XI (1897)

unpublished. 29 HUBBLE, letter 30 Miss Woods, Harv Bull 764 (1922), see also A N 215, p 391 (1922) 31 Harv E 33 BALLEY, Pop Astr 28, p 518 (1920) 32 Zô-Sé Annals 10 (1918) 31 Harv Bull 848 (1927) 35 Mis 34 BAILBY, Harv Circ 266 (1924) DAVIS, Publ A S P 29, p 210 (1917) 37 Wash Na 36 Mt Wilson Contr 195 (1920) Ac Proc 7, p 152 (1921) 38 CHÈVREMONT, BSAF 12, pp 16, 90 (1898) 39 BAILEY Harv Bull 798 (1924) 40 BAADE, letter of June 8, 1932 41 GROSSE, A N 246, p 2 42 BAADE, AN 230, p 353 (1930).

 $\tau$ , or with  $\varrho$ , the distance from the cluster center, have been derived (or assumed) and applied to published counts of stars We have, for instance, from VON ZEIPHL,

$$N(\varrho) = \frac{1}{\pi} \int_{0}^{R} \sqrt{(r^{2} - \varrho^{2})} \frac{d}{dr} \left( \frac{1}{r} \frac{du}{dr} \right) dr$$

where R is the radius of the cluster and s is the number of stars in the corre-

sponding unit area of the projected image

The problem of finding a law of space distribution from the law of apparent distribution in a globular star system has been solved by von Zeipel, who has been the leader in the attempt to deduce the structure of clusters from observation of stellar distribution. He was the first to utilize in this problem the principles of the theory of gases. Analogies with the kinetic theory have encouraged a number of theoretical and observational researches, but as yet no completely satisfactory representation of the observations has been found

It seems unnecessary to treat in detail the history, methods, successes, and failures of these various investigations of distribution. No other phase of the study of globular clusters has been so frequently and thoroughly described. Special attention should be called, however, to the discussions by H. C. Plummer, ten Bruggencate, Strömeren, Eddington, Jeans, Parvulesco, and Martens<sup>1</sup> A further important step has been made by von Zeifel and Lindgren, who proceed, from the assumption that the stars of different masses are distributed in equilibrium in relation to surrounding stars, to the determination, from the observed distribution, of the mean masses for various color classes and absolute luminosities. They have used the method with success in the study of the rich galactic cluster Messier 37, and Wallenguist has further discussed their analysis and applied the method to his own study of the magnitudes in Messier 36. Freundlich and Heiskanen have provisionally applied it to the study of the distribution of stars in globular clusters, but the observational material is yet too uncertain for satisfactory results.

That the discussions of the adiabatic or isothermal distributions of stars in globular clusters have been unsatisfactory in practice is not surprising, since the data from which comparisons have been made are inherently faulty. The best chance for improvement and successful application of the theory lies in the few rich galactic clusters from which the foreground and background stars can be satisfactorily differentiated. For the globular clusters, however, the crowded centers and the attendant difficulties with EHERHARD effect and background contrast vitlate the counts, except for the outer parts. Furthermore, the available counts deal with only the few hundred or few thousand supergiant stars; tens or hundreds of thousands of fainter stars, which must play a major rôle in stellar distribution, have not yet appreciably entered the investigations. TEN BRUGGENCATE has recognized the importance of ellipticity in the distribution of stars in globular clusters, but otherwise all discussions of the problem have

ignored this lack of radial symmetry.

The star counts that have been used for the study of globular clusters are almost exclusively those of Bailey at Harvard and of Pease and Shapley at Mount Wilson Photographs on a larger scale are needed. Special attention should be given to the brighter and more open globular clusters ( $\omega$  Centauri, N.G.C. 3201, N.G.C 6397), and also to "giant-poor" anomalous systems and those clusters like N.G.C 2477 that are possibly intermediate between the globular

<sup>&</sup>lt;sup>1</sup> See references in Hery Mon No 2 (1930). See also the later papers by HEURMANN and STEDENTOFF, Z f Phys 54, p 183 (1929) and Z f Astrophys 1, p. 67 (1930).

and the galactic types Tables and figures of the distribution of the stars in globular clusters are given for several of the brighter clusters by Pickering, Plummer, von Zeipel, and Heckmann and Siedenforf

In conclusion, we must admit that the situation is not very hopeful. The frequency is (roughly) inversely proportional to the fourth power of the distance from the center, this holds only for giant stars in the typical globular clusters. The law of distribution of fainter stars is even less definitely known. We find them more widely dispersed than the giants, but we can say nothing of their distribution within the central sphere of ten parsecs diameter, where the crowding of brighter stars "burns out" the photographs

The distribution of brightness in a globular cluster as a function of distance from the center has been investigated by Hertzsprung for Messier 3, by Hogg

and by NABAKOV for Messiei 13, and by Schilt for & Centauri1

19. Luminosity Curves for Stars in Clusters Distribution in absolute brightness as well as in space can be satisfactorily studied as yet only for the giant and supergiant cluster stars. Although, as we have seen, the space distribution is not independent of the influence of dwarf stars, the fragmentary absolute luminosity curves have a meaning and a certainty that are essentially unimpaired by such forced neglect of the dwarfs. Moreover, with the use of more powerful telescopes, especially on the borders of bright southern clusters in high galactic latitude, we shall soon be able to extend both the general luminosity curves and the luminosity curves for specific color classes to stars as faint as the sun or fainter. In the near future we should therefore have for the globular clusters much more satisfactory data on the frequency of luminosities than we now have for stars of the general galactic system.

The labor of determining magnitudes and colors on a satisfactory photometric basis is so considerable that luminosity curves will come slowly, for only three globular clusters are the color and magnitude surveys at all extensive. It is necessary, therefore, to resort for the time being to general luminosity curves based on provisional magnitude scales, except for the giant stars in the three

systems for which results are herewith presented

a) Frequency Distribution of Giant Stars Observations of frequency distributions in Messier 3, Messier 13, and Messier 22 are combined to give Table 8. Results are tabulated for six intervals of color class redder than fo Stars redder than k5 are grouped together, since the data are insufficient for class m alone, for classes b and a the observational limits cut off the luminosity curves so quickly that the results are not significant. Probably the curve for class f is also affected both by the confluence of giant and dwaif series and by the magnitude limitations of the catalogues Distance moduli used for reduction from apparent to absolute photovisual magnitudes are taken from Appendix A The absolute photovisual magnitude limits of the catalogues are +0,4 for Messici 22, +0.5 for Messier 13, and +1.6 for Messier 3. The table is therefore of low weight for stars fainter than  $M_{pv} = +0.5$  The picliminary maximum at 0,0 for interval fo to f5 is probably related to the humps in the general luminosity curves of these three clusters (Figure 11), which are caused mainly by an abundance of blue stars and variables. The average dispersion of absolute magnitude for the various intervals of color is about half a magnitude, which is probably well in excess of the observational eriors

<sup>&</sup>lt;sup>1</sup> Hertzsprung, A N 207, p 89 (1918), Nabakov, R A J 1, p 109 (1924), Ilogg, Harv Bull 870 (1929), Schilt, A J 38, p. 109 (1928), Pop Astr 36, p 296 (1928) See also Hogg's recent discussion of the luminosity distribution in six globular clusters A J 42, p 77 (1932)

Table 8. Composite Luminosity Curve of Messier 3, Messier 13, Messier 22

Table 8. Compo	eite Lum	inosity (	Curve of	Messier	3, Monaid	Br 13, <b>M</b>	pealor 22
Absolute Photo- visual Magnitude	10 to 15	15 to g0	gQ to g5	Color Class g5 to k0	k0 to k5	>k5	All Calors
-4.0 to -3.5 -3.5 to -3.0 -3.0 to -2.5 -2.5 to -2.0 -2.0 to -1.5 -1.5 to -1.0 -1.0 to -0.5 -0.5 to 0.0 0.0 to +0.5	- 1 1 1 8 18 103	- 2 1 7 24 85 136 132	- 5 34 28 71 73	1 1 5 16 32 32 32 20 7 5	1 - 13 11 6 4 1	1 11 18 5 2 1 —	3 13 38 39 82 97 195 120 273
+0,5 to +1,0 +1,0 to +1,5	38 85	31 31	8				78 117
Totals	346	449	264	120	38	38	1255
H3 #8		/	_		7	,	KEEDIO
25		1					800
Mi s				-	$\perp$	<del> /-</del>	130 M 21
<b>10</b>	+			+		4	100
Ni so							50
						+/1	150 100
259		/			/	1/1	Na So
HS 199	-			1	1	1-1	
780	$\mathscr{U}$			<del>  </del>	-	+	W Na

Fig. 41 Luminosity curves for eight globular clusters. Ordinates are numbers of stars, abscisses are photographic absolute magnitudes (approximate).

Until we have obtained data from other clusters, there is little point in fitting the usual exponential curves to the observations. Some of the asymmetries

may be real in the curves representing magnitudes and practically disappear in the corresponding curves showing the distribution with respect to total radiation or mass

b) The Preliminary Maximum—General photographic luminosity curves based on provisional magnitude scales are given in Figure 11 for eight globular clusters. All the plotted material except that for NGC 5053 is derived from my work on Mount Wilson plates. The methods of estimating the magnitudes and some of the numerical data are published elsewhere. The curves suggest two general comments, which are followed below by a few special notes on the individual clusters.

i There is a considerable variety in form, an indication of the impropriety of using any method of parallax determinations that depends on the form of

only the brightest portion of the general luminosity curve

2 Without exception, all the globular clusters show preliminary maxima, which fall within half a magnitude of the median magnitude of cluster type variables, as indicated by the two heavy vertical lines in Figure 41. We have evidence in all of these globular clusters, though it is not shown graphically for NGC 5053 and Messier 22, that the general luminosity curve rises steeply and high for stars fainter than the critical absolute luminosity near absolute magnitude zero. The bunching of stars at this particular brightness is probably of considerable significance in the economy of globular clusters. The resultant hump in the luminosity curves has possibilities in the measurement of distance

3 Details concerning Figure 11

- a) The preliminary maximum for Messier 3 is partially due to the hundred and fifty known variable stars, when the cluster type variables are omitted from the diagram we have the milder and fainter hump shown by the broken line and small circles
- b) For Messier 2, Messier 5, and Messier 15 the variable stars have not been excluded, but they are not sufficiently numerous, even in Messier 5, to contribute much to the very conspicuous preliminary maxima

c) The somewhat fragmentary luminosity curve for NGC 5053 is derived

from data published by BAADE2, with variables excluded

d) The preliminary maximum for Messier 13 is built up largely by stars of small or negative color index; the cluster has no definitely recognized cluster type Cepheids

e) For Messier 68 the two luminosity curves result from stars in different selected areas, measured on two plates. The curves are in fair agreement, a

second preliminary maximum at M = +1.4 is suggested

f) The fragmentary luminosity curve for Messiei 22 is based on an unpublished catalogue, prepared at Haivard from my Mount Wilson photographs. The wide displacement of the maximum from absolute magnitude zero suggests that the correct distance may be ten to twenty per cent larger than that given in Appendix A; but further work on the magnitudes of the fainter stars is necessary before anomalies of the luminosity curve can be taken seriously.

#### f) The Forms of Clusters.

20. Definition and Difficulties. By the ellipticity of globular clusters we may choose to refer either to the symmetrical elongation of integrated images on photographs, or to the systematically greater number of stars along one axis of the projected image than along any other, as determined by detailed star

<sup>&</sup>lt;sup>1</sup> Mt Wilson Contr 155 (1917), 175 (1919) 
<sup>2</sup> Hamburg Mitt 6, No 29 (1928)

counts Both of these phenomena can be explained most naturally by assuming that the clusters are oblate — that is, that the gradient of the space density of the stars differs in different directions from the center and is usually symmetrical about a polar axis and an equatorial plane Probably the forms of the integrated photographic images are related as directly to star density as are the counts.

It is difficult, however, to determine the actual bounds of a globular cluster along various radii, or even the limits of the projected image, because of (1) the unknown and possibly peculiar density laws in different directions for a flattened stellar system, (2) the confusion with foreground stars, (3) the present lack, near the edges of individual clusters, of sufficiently long exposures made

with large reflectors

The detection of the planes of symmetry, moreover, depends on the degree, the orientation, and the nature of the ellipticity. Thus, if the ratio of minor to major axis is near unity, if the polar axis is nearly parallel to the line of sight, or if the property of concentration toward a plane is confined to the fainter unobserved stars in the cluster, the successful analysis of form is impossible

Early studies of globular clusters, such as BAILEY's star counts1, dealt with but one or two thousand stars in each cluster, while the underlying ellipticity usually becomes evident only when large numbers of stars are considered. Consequently, nothing very definite was known of the important fact of deformation until the systematic star counts on Mount Wilson photographs were analyzed. Later it was noted that the numerous faint stars frequently make their presence known on masse as well as in detailed counts, so that the diffuse integrated images of clusters photographed with small telescopes can be used to study cluster forms, even if few or no individual stars are shown. The counts, however, are sometimes more searching. For example, in Messier 13, described. below, the Harvard plates do not show, on inspection, the marked ellipticity revealed by the counts, they indicate, if anything, a slight clongation in a direction 45° from the major axis. The same is true of some other clusters. When an integrated image is clearly alliptical, the numerical ellipticity shown by star counts is very large. In a condensed cluster the EBERHARD effect and other difficulties may interfere seriously with the determination of the frequency of stars as a function of the distance from the center, but errors arising from such sources do not affect measures of the orientation of the major axis of the cluster image.

21. The Blongation of Messier 18. Among the globular clusters whose forms were investigated by the writer, partly in collaboration with Mr. Peaser, Mrs. Shapley, and Miss Sawyer, the Hercules cluster, Messier 13, best illustrates

the nature of the allipticity throughout a wide range in magnitude.

The stars in Messler 13 were counted on nine plates, and the results arranged for analysis in a framework of twelve equal radial sectors and a series of concentric rings. The plates are of various exposure times, ranging from one minute to five hours. The counts of the total number of stars in each of the twelve equal sectors show the amount of ellipticity and its change with magnitude. The counts for each of the zones between concentric circles show how the degree and direction of ellipticity varies with distance from the center of the cluster.

In Table 9 the numbers of stars are given for six different plates for each sector separately, but with the zones not differentiated. For the two photographs of longest exposure Table 10 again gives the number of stars in different sectors, but divides the material into four zones for each plate. The central regions are too much burned out to be included in the star counts,

<sup>1</sup> Harv Ann 76, No. 4 (1915).

PRASE and SHAPLEY, Mt Wilson Contr 129 (1917).

Table 9. Ellipticity for Different Exposures in Mossicr 13.

Duration	Total					Numb	er of S	tore In	Sectors				
of Exposure	Number of Stam	15°	45°	75*	105°	135°	165°	1950	2250	255°	285°	315*	343*
6 <sup>m</sup> 15 22 37.5 94 300	5890 7790 14150 16600 25000 30000	163 296 734 749 1261 1126	149 264 672 770 1340 1234	433 744 913 1475	396 859 1008 1590	1580	213 314 638 853 1431 1232	154 284 569 779 1338 1079	154 230 583 804 1343 1085	174 259 684 974 1486 1187	256 401 825 1011 1590 1300	235 309 852 963 1580 1368	108 305 738 763 1361 1258

Table 10. Ellipticity and Distance from Center in Messier 13. (Results from two plates.)

Distance					Numb	or of S	teurs in	Scotors				
from Center	15°	45°	75°	105°	135°	165°	195*	225°	255*	285°	315°	345°
2' to 4'	623	668	750	762	764	728	712	683	758	778	718	670
4' to 6'	358	361	423	464	476	386	330	352	402	438	479	394
6' to 8'	168	207	212	236	226	202	188	194	214	248	249	198
8' to 10'	112	104	90	128	114	115	108	114	112	126	134	99
3' to 5' 5' to 7' 7' to 9' 9' to 11'	560	640	624	684	788	642	586	597	629	658	712	662
	362	374	410	471	431	360	302	292	358	396	124	394
	204	220	220	261	244	230	191	196	200	246	232	202
	141	136	116	118	130	129	131	124	130	157	131	100

The ellipticity is illustrated in Figure 12, which shows the amount and position angle of the elongation at different distances from the center. The cluster is

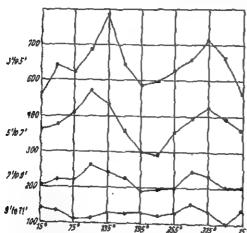


Fig. 12. Ellipticity of Messier 13 for different intervals of distance from the center. Ordinates are numbers of stars and abscissae are position angles.

seen, from these tables and from the figure, to be conspicuously clongated, showing approximately twenty-five per cent more stars in the direction of the major axis than in the direction perpendicular thereto. The ellipticity, which shows throughout the cluster from center to edge, appears in all magnitudes from the thirteenth to the twentleth and fainter, though it is relatively inconspicuous for the stars brighter than the fifteenth magnitude.

22. Ellipticity and Orientation of Globular Clusters. Over half a million stars have been counted in the course of the Mount Wilson and Harvard studies of the forms of globular clusters. By means of star counts the position angles of the major axes have been found for

twelve systems, and evidence of approximate circularity or asymmetry adduced for a few others. Direct estimates of the position angles for the integrated images of most of these clusters are found to agree closely with those determined from the laborious counts; hence further surveys of the forms have been made using only the direct estimates of ellipticity on small scale plates.

<sup>&</sup>lt;sup>1</sup> H. Shapley and Martha B. Shapley, Mt Wilson Contr 160 (1918).

a) Orientation of Major Axes The ellipticity and orientation given in columns 13 and 14 of Appendix A are based on a Harvard investigation. except for starred values which are taken from the earlier Mount Wilson counts. The ellipticity is expressed as ten times the ratio of the minor to the major axis. The orientations, with respect to the galactic circle, are given only for those thirty-nine clusters in which the ellipticity is 8 or less, or if 9, only when the orientation could be certainly determined. The orientation with respect to the galactic circle is reckened from the "galactic cast" (direction of mereasing longitude) through the "galactic south"; negative angles consequently indicate reckening from the east in the opposite direction

b) Inclination to Galactic Circle The data bearing on the relation of the elongation to the plane of the Galaxy are collected for thirty-seven globular clusters in Table 11 (N.G.C. 1866 and N.G.C. 1978, in the Large Magellanic

Cloud, are omitted from the table).

Table 44 Orientation of Globular Clusters

NGC	Clean	Geleciis Letitode	Distance from Galentio Piene lejes	Degree of Blongation	Inclination to Galactic Circle
104	ш	-45°	- 4,8	8	-55°
362	III	-47	- 9,4	8	+65:
1851	II	-34,5	- 8,1	9 9 8	-75
1904	V	-28	- 9,6	9	+ 5
2298	VI	-15	- 6,9	8	+39
2419	VII	+23	+11,9	9	<b>— 56</b>
2808	I	-11	- 3,1	8	+84
4833	VIII	- 8,5	- 2,2	8	-80,
5024	V	+79	+17.9	9	- 79
5053	XI	+78	+17,0		-61
5139	ΛÍΠ	+15	+ 1,8	6	+30
5272	VI	+77.5	+11,9	8	+54
5897	XI	+29	十 8,0	8	-441
5904	v	+46	+ 7.8	9 8	+16
6101	IX.	-16	- 5,7		+35
6121	Ξ	+15	+ 1.9	9 9 8	+72 -64
6139 6144	χï	+ 6 +15	+ 3.1 + 4.8	1 2	-07 -22.
6205	V	T 13	+ 6.6	9.5	-63
6235	×	+12	+ 5,9	8	+89
6266	ĪŸ	I I'7	+ 2,3	8	+16
6273	viii	1 76	+ 2.6	6	-28
6341	IV	+35	+ 6.4	6 8	+16:
6356	п	1 + 9	+ 7,8:	١٥	-14
6362	X		- 4.7	9 8	+78:
6397	TX.	-12,5	- 1.2	] 9	+73
6402	VIII	+14	+ 4,8	و	+76
6440	V	+ 2	+ 1,71	8	+ 10:
6441	III	- 6.5	- 2,2	8	+40
6517	IV	+ 6	+ 5,2	8	- 41
6626	IV	- 7	- 2,0	9	+18
663B	VI	- 7.5	- 3.9	8	-27
6652	VII	-13	- 5,3	8	-111
6656	AII	<b>–</b> 9	- 4,4	9 8 8 8 9 8 8 8	+18
6779	X	+ 8	+ 2,8	8	+121
7078	IV	-28	- 6,1	8	+11
7089	п	<b>—36</b>	- 8,2	9	<del>-8</del> 0

<sup>&</sup>lt;sup>1</sup> SHAPLEY and SAWYER, Harv Bull 852 (1928).

SHAPLEY, Mt Wilson Comm #5 (1917).

That is, position angles without a colon in Hary Bull 852 (1927).

Although the estimates here presented are probably better than any previously made, I feel that they are not of much significance except for the few clusters for which the ellipticity is conspicuous and the orientation angle is given without a colon. The average deviation of a position angle from the values previously determined from Franklin-Adams charts is about 30°, an indication of the inherent difficulty of the estimates. Some of the clusters are definitely asymmetrical. For most of those not listed in Table 11 the deviations from circularity are small, or the clusters are too faint or too involved in a star field for useful determinations of form. Notwithstanding the difficulties and uncertainties, for all but eighteen of the ninety-three clusters in Appendix A the degree of ellipticity is estimated.

Attention should be paid in the future not so much to small and difficult objects as to closer analyses of the distinctly asymmetrical systems and of the brighter clusters in which the degrees of ellipticity can be studied with respect to colors and magnitudes. From detailed investigations, as you ZEIPEL has shown, we may hope to get information on the masses of stars of different volors and luminosities, using as criteria of mass the distribution with respect to the

centers and to the hypothetical galactic planes within the clusters's

Although the estimates of orientation are admittedly uncertain, the measures show definitely that large and small values are scattered throughout all distances from the galactic plane. In order that the equatorial plane of a cluster be parallel to the plane of the Galaxy, parallelism of the major axis with the galactic circle is a necessary though not a sufficient condition. We need to know the true form, or an equivalent, and get another component of the inclination, before we can fix the plane of the cluster in space; at present there is little prospect of measuring the true oblateness. The equatorial planes in the clusters with low inclinations of course may or may not be parallel to the galactic plane; those with high inclinations are certainly not parallel. There is no good evidence as yet that the clusters are not inclined at random in space.

23. Some Peculiar Clusters. A few globular clusters that depart considerably from a spherical form have been studied. They are of interest in connection with the possible dissolution of clusters and also in considerations of the distribu-

tion laws.

a) Messier 3 (N.G.C. 5272), Messier 5 (N.G.C. 5904), and Messier 62 (N.G.C. 6266). It is difficult to account for such pronounced and deep-scated asymmetries in globular clusters as those of Messier 3, Messier 5, and Messier 62. For Messier 3 the distance from other stellar systems is now, and probably for hundreds of millions of years has been, extremely great; the galactic latitude is +77°,5. There is no evidence of occulting matter in the cluster or in front of it that might be responsible for a spurious appearance of irregularity. The measure of asymmetry is illustrated by the following data 4, based on the counts of two Mount Wilson plates, the numbers of stars being given for thirty degree intervals of position angle:

Position Angle. . . . . 15° 45° 75° 105° 135° 165° 195° 225° 285° 315° 345° Number of Stars . . . 244 234 246 220 198 242 222 282 292 321 303 263

Further work should be done on this cluster, as the counts on different plates

<sup>&</sup>lt;sup>1</sup> H. Shapley and Martha B. Shapley, Mt Wilson Contr 160 (1918).

FREUNDLICH and HRISRANEN, Z f Phys 44, p. 226 (1923).

See discussion by Ten Bruggencatz, Die Sternhaufen p. 72 (1927). Pease and Shapley, Mt Wilson Contr 129 (1917).

For Messier 5 we have comparable data from a long exposure plate showing 15000 stars, made by Prase and counted by Miss Davis<sup>1</sup>, the star numbers referring to a region between 3' and 15' from the cluster's center.

Position Angle 15° 45° 75° 105° 135° 165° 195° 225° 255° 285° 315° 345° Number of Stars . . . 924 1016 972 861 693 783 870 978 1037 955 907 952

The asymmetry of Messier 62 is shown numerically in the following counts based on a Mount Wilson photograph, a central burned-out area one minute in diameter being excluded

. 15° 45° 75° 105° 135° 165° 195° 225° 255° 285° 315° 345° Position Angle. Number of Stars . . . 67 56 67 45 35 42 49 56 68 79 72 72

When opposite sectors are combined, the position angle of the major axis appears to be about 75°, the values of the angle estimated from the integrated image are 70° and 55° for two independent determinutions

Messier 62 is the most irregular globular cluster. Does absorbing account asymmetry? Or has collision or encounter deformed it?

b) Messier 19 (N.G.C 6273). Figure 19 and the estimated ellipticities in Table 11 show that Messier 19 is the most elongated globular cluster so far studied. The circular coordinates of the diagram. are position angles; the radial coordinates are relative numbers of stars in each thirty-degree sector. The position angle of the major axis of the diagram. is 15°, and along this exis there are more than twice as many stars as along the minor axis Photographs show no evidence of a double nucleus. Since the galactic intitude is +9°, and the major aids is inclined less than thirty degrees to the galactic circle, the equatorial plane of the cluster is probably nearly parallel to the galactic plane.

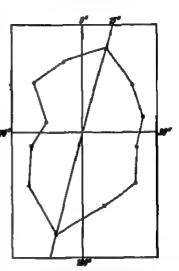


Fig 13. Diagram of star density in Messier 19

Considering this extreme example, we conclude that the flattening of a cluster is systematically of a lower order than that of spirals and the galactic system

c) Messier 22 (N G C 6656). The form of globular clusters near the galactic plane may have an important bearing on the relationship of the Galaxy and gulactic clusters to the globular systems, Messier 22, in galactic latitude -9° and one of the nearest globular clusters, is significantly situated for a test of deformation and of the orientation of its central plane. On a photograph which shows more than seventy thousand stars from the twelfth to the twentieth magnitude, most of which are undoubtedly members of the cluster though it is located in the direction of a rich galactic star cloud, a detailed count has been made .

The number of stars in the direction of the major axis is nearly thirty per cent greater than the number along the minor axis. The orientation of only 18° and the high ellipticity, which suggests that we see the cluster edgewise, indicate that it may lie nearly parallel to the galactic plane.

SHAPLEY and DAVIS, Publ ASP 30, p 164 (1918)

Mt Wilson Contr 160, p 7 (1918); Harv Bull 852, p. 25 (1927).

SHAPLEY and DUNCAN, Pop Astr 27, p. 100 (1919)

d)  $\omega$  Centaum (NGC 5139) The 128 cluster type variables in  $\omega$  Centaum appear to be preferentially along the equatomal plane of the system. Table 12 and Figure 14 illustrate this remarkable distribution. The data are obtained

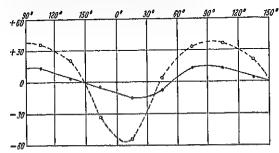


Fig 14 The distribution of stars in ω Centauri Ordinates are percentage excesses along the various radu indicated by the position angles (abscissae). The full line shows that the position angle of the major axis for all stars is about ninety degrees. For the variables alone (broken line) the axis is about the same, but the relative excess is three times as great

from Harvard plates, which show the ellipticity for all distances from the center.

Table 12 Distribution of 5000 Stars in ω Centauri (Results from two plates)

Width of		.*				Sec	tors			-			Mean
Zono	15°	45°	75°	105°	135°	165°	195°	225°	255°	285°	315°	345	
3' to 6' 6 to 9 9 to 12 12 to 15	148 84 66 44	129 89 81 54	151 151 96 61	182 142 74 61	165 139 64 57	159 113 79 57	164 105 64 40	173 119 68 59	203 153 88 57	182 163 97 59	198 125 74 51	163 117 68 45	168 125 77 54
3 to 9 9 to 15 3 to 15 Variables	232 110 342 8	218 135 353 6	302 157 459 17	324 135 459 12	304 121 425 9	272 136 408 5	269 104 373 2	292 127 419 16	356 145 501	345 156 501 17	323 125 448 16	280 113 393 9	293 130 423 11

The numbers of variables in opposite sectors are combined in making the diagram. The relative amplitudes of the two curves show that towards the supposed plane of symmetry the variables are three times as condensed as the stars in general, and the latter exhibit such strong ellipticity that  $\omega$  Centauri is easily seen to be elongated on all photographs

24. The Structure of Galactic Clusters. a) Orientations. Only for the comparatively rich and compact galactic clusters is it possible to estimate the orientation. The loose systems—classes a, b, and c—are generally of too indefinite size and membership to show significant boundaries. Eighty-one clusters are found sufficiently condensed for examination, of these, fifty-seven show measurable orientations. Taken as a whole, the clusters appear to be oriented at random, within the uncertainty of the determinations. In points of detail, however, we see that the average inclination to the Galaxy differs from place to place, so that in some regions the clusters appear to be mainly aligned with the galactic circle, in others they are oriented approximately at right angles to it. Tables 13 and 14, showing the mean inclination for intervals of galactic longitude and latitude respectively, indicate that there is no correlation of orientation with either longitude or distance from the galactic plane.

<sup>&</sup>lt;sup>1</sup> Mt Wilson Comm 45 (1917)

<sup>&</sup>lt;sup>2</sup> Harv Mon 2, sec 33 (1930), see also Collinder, I and Circ No 2 (1931).

Table 13 Longitude and Inclination

Morn Galantia Longitudo	Number of Clusters	Mean Indination	Moss Galectic Longitude	Number of Chaters	Megn Indination
82°,6	5	60°	242°,2	6	30
128 ,0	Š	55	279 .1	5 ]	62
156 ,5	1 5	33	302 ,3	5 (	53
183 ,5	5	42	322 ,3	5	31
201 .7	5	44	337 ,6	6	33
217 .9	5	50			

Table 14 Inclination and Distance from Galactic Plane

Mana Rain # (In passeos)	Number of Clusters	Morn Indication	Mean Inclination	Number of Clusters	Mean Rain A (in payment)
677	5	45°	80°	7	69
425	5	38	70	5	203
265	5	47	66	4	167
196	5	34	59	7	279
143	5	51	47	5	215
100	5	52	40	5	131
62	5	47	29	i a	281
30	3	39	18	5	175
17	6	53	12	4	222
6	6	47	4	1 4	108

b) The "shoulder" effect. A peculiarity in the distribution of stars has been observed in a number of galactic clusters, and leads to the conclusion that their dimensions are much larger than at first appears. Messier 67 plainly exhibits this unusual distribution. A summary of the average star density, photovisual magnitude, and color index is given in Table 15 for 232 stars of the cluster. There is no decrease of star density, or change of average magnitude or color outside a circle of 6',5 radius about the center of the cluster, but inside that circle the density, brightness, and redness of the stars increase towards the center.

Table 15. Average Star Density, Photovisual Magnitude, and Color Index in Messier 67

Distance from Conter	No. of	Area in Sq.	No. Stern per Square	Av Pv. Meg.	Average Color Index		of Stars
			Minute			Background	Claster
0',0- 2',5	35	19,6	1,78	12,49	+1,00	6	29
2,5-4,5	- 64	44,0	1,45	12,85	+1,00	13	51
4,5-6,5	49	69,1	0,71	12,52	十0,94	21	28
6,5-8,5	30	94,3	0,32	13,03	+0,81	28	2
8,5-10,5	34	119,5	0,28	13,06	+0,82	36	( <b>→2</b> )
10,5-11,5	20	69.1	0,29	13,11	+-0,80	21	(-1)
Total	232	-		_	_	125	107

If it is assumed that the constant density outside the circle of radius 6',5 refers to the background or foreground stars, the cluster appears to be composed of about one hundred stars scattered over an area of radius 6',5. Further study, however, indicates that the evidence is misleading. The background density of 0,3 stars per square minute is nearly ten times as large as would be expected for the galactic latitude and the photovisual magnitude concerned. This condition suggests that the cluster with radius 6',5 is merely a well-marked nucleus of brighter and redder stars in a much larger system. Further counts made on Wolf-Palies photographic charts of all stars within a degree of the center of the cluster show that the system extends far beyond the limits of the plates used

for the magnitude work. The real diameter may be as much as one degree. If Messier 67 is roughly spherical in form, the space occupied by the nucleus is about a hundredth of the total volume of the cluster. The total membership is approximately five hundred stars between photovisual magnitudes ten and fifteen, but only the central concentration of one hundred and fifty stars is noticeable in an ordinary survey

The "shoulder" effect has appeared in studies of Messiei 11, Messiei 37, and other galactic clusters Trumpler found it in Praesepe, the Pleiades, and h Persei<sup>1</sup> The change of radius with magnitude (outside the nucleus) is shown for h Persei in Figure 15, based on data accumulated by VAN MAANLN and

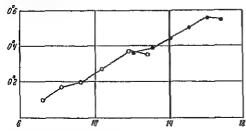


Fig 15 Relation of radius to magnitude for h Perser Ordinates are distances from the center in degrees, abscissae, photographic magnitudes (From Trumpler)

TRUMPLER, the effect is even more pronounced for the Pleiades and Praesepe

c) Additional Remarks on Galactic Clusters Various other studies have been made of the structure of galactic clusters. Of especial value is the work of von Zeipel and Lindgren on the magnitudes and distributions in Messiei 37 The luminosities tabulated by them (Table 16) illustrate the double maximum for class a stars, a phenomenon that may be of some value in estimating the distances of galactic clusters. From the space distribution for different ma-

gnitudes and colors they have determined, by the ingenious method devised by von Zeipel, the approximate mean masses of the stars of various spectral classes The method has been applied by Wallenguist to other galactic clusters

Limits of	1		Color	Classes		
Magnitude	ь	a	ſ	g	k	Н
] 11,0	0	2	0	0	0	0
11,0~11,5	0	4	1	1	0	C
11,5 - 12,0	0	12	0	5	0 [	C
12,0-12,5	7	21	0	10	0	C
12,513,0	8	18	0	1	0	C
13,0-13,5	20	16	3	0	1 1	(
13,5-14,0	5	37	2	0	0	C
14,0-14,5	3	29	7	1 1	0	(
14,5-15,0	1	19	16	3	1 1	(
[ 15,0	0	2	38	9	1	(

Table 16 Luminosity Curves for Various Color Classes in Messici 37

KUSTNER and CHEVALIER have made accurate modern catalogues of positions in several galactic clusters, which will be of importance for future analyses of proper motions Photographic and photovisual magnitudes of stars in Messier 35, Messier 36, and other northern clusters, as determined by Wallenguist, afford material for the discussion of bolometric magnitudes, luminosity curves, density laws, and probable mean masses, as well as star colors. The ratio of field stars to cluster stars for five thousand stars in the faint northern cluster N G C 7789 is shown in Table 472 It is well to observe from the first line that the rapidly decreasing ratio does not mean the total absence of dwarf stars from the cluster, or even their relative scarcity.

<sup>&</sup>lt;sup>1</sup> Allegheny Publ 6, No 4 (1922)

<sup>&</sup>lt;sup>2</sup> Mt Wilson Contr 190, p 7 (1920)

Tabel 17 Star counts for NGC 7789

Photographic Magnitude Interval	] 16	16—17	1718	18—19	19—20	Total
Clustor Stars Flok! Stars . Ratio	347 592 0,59	210 256 0,82	155 666 0,23	266 1178 0,23	126 1475 0,09	1104 4167

The structure of well known moving clusters and streams of stars, such us the groups in Taurus, Ursa Major, Scorpio, and Perseus, has been treated by numerous writers1. The group motions are essentially parallel to the galactic plane, though the clusters are flattened variously with respect to the direction of motion; the flattening of the Perseus and Ursa Major clusters is at right angles to the direction of motion, while the Scorpio group is flattened parallel to the gulactic plane, and the Hyades cluster is nearly spherical

## g) The Transparency of Space.

25. Early Investigations of Light Scattering In all researches on the structure of the stellar universe the possibility of the loss of light in its passage through interstellar space must be recognized. If the loss of visual light due to absorption or scattering in space should be as much as a millionth of one por cent in each hundred million miles, stars thirty-five hundred light years away would appear about two magnitudes too faint. Uncertainty in the coefficient of scattering is, therefore, very serious in studies of the distances of faint stars.

The early work on light scattering indicated high absorption in space KAPTHYN in 1914 derived a coefficient, expressed in stellar magnitudes per parsec, of 0,0003, corresponding to a change of a tenth of a magnitude in color index for each three hundred parsecs of distance. At the beginning of the work on star clusters at Mount Wilson (1915) the following values were on record for the increase of color index with each parsec of distance.

Observer	 Town	KAPTEYN	Kno	Turner	van Rhije
Coofficient	0.00047	0.00031	0.0019	0.0030	0,00015

In all work yielding positive results the stars of small proper motion have appeared to be redder In view of the fact that small proper motion is now recognized as characteristic of highly luminous stars, this excess of redness is to be regarded as merely a correlate of bright absolute magnitude, rather than as Indicative of light scattering. The work of SEARES and others has clearly shown differences in color for giants and dwarfs.

There remains, however, some evidence of a tenuous local cloud of absorbing matter, estimated by King4 as extending to a distance of thirty parsecs, reddening the stars at the rate of d = 0,0003 magnitudes per parsec, but affecting more distant stars only by a constant (and negligible) amount

A more declaive test of light scattering is to be found in the study of colors of objects at much greater distances, such as those of globular chisters

26. Blue Stars in Messler 13. After KAPTEYN's work on light scattering, and the contemporary results of KING, JONES, and VAN RHIJN, which independently confirmed it, the discovery in 1915 of stars with negative color indices in Messler 13 was unexpected. A critical examination of photovisual and photographic magnitude scales falled to assign the apparent blueness of the cluster

<sup>&</sup>lt;sup>1</sup> See references in Appendix D of Harv Mon No 2 (1930).

<sup>1</sup> See references in hiplingraphy of Harv Mon No 2 (1930)

8 Bee references in hiplingraphy of Harv Mon No 2 (1930)

8 Mt Wilson Contr 116 (1915)

stars to observational error. Out of 495 stars with well determined color indices, 86 were found to be of color class b, and 63 of class a

With a scattering coefficient of d=0.0003 (Kapienn's last value), and an assumed distance for the cluster of as little as a thousand paisees, practically no negative colors should appear if the stars are of usual spectral classes. With the obviously better parallax of 0",0001, the color index produced by Kapienn's scattering should be +3.0 for stars of spectral class A, and many color indices should be greater than +4 in a typical distribution of spectral classes. It was found from the Mount Wilson photometric work that the range of color index

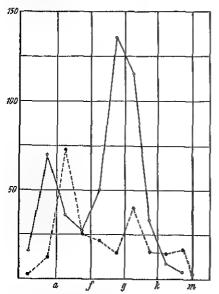


Fig 16 Frequency of color classes in Messier 13 (full line) and in the neighborhood of the sun (Yerkes Actinometry) Coordinates are relative numbers of stars and color classes

observed in Messiei 13 is the same as that found among nearby galactic stars, as illustrated in Figure 16 (The direct correspondence of color class with spectral class in this cluster has been verified by the spectrograms made by Pease<sup>1</sup>). There are no color indices in the cluster larger than - $\frac{1}{2}$ . The largest admissible color excess appears to be about  $0^{m}$ , 1, and, even if this excess is attributed entirely to light scattering, we derive d=0.00001, a thriftenth of the value derived by Kapieyn, and a fifteenth of the value found by van Rhijn from a consideration of the stars in the Yerkes Actinometry

The foregoing upper limit of scattering is so small as to be entirely negligible in dealing with nearby stars in high galactic latitudes, but a more accurate value is desirable, and fortunately it can be found from studies of external stellar systems

27 Faint Blue Stars in the Milky Way. The galactic latitude of Messier 13 is +40° fhat light scattering is absent in this direction is no proof that it does not occur elsewhere, especially in low ga-

lactic latitudes where stars and diffuse nebulosity are concentrated. To make the test more comprehensive with respect to galactic latitude and longitude, the search for negative color indices has been carried out in several distant cluster systems, on the assumption that a normal range of color index and the presence of numerous blue stars are strong evidence of the transparency of space in the directions and to the distances considered. The results are in Table 18, where the observed extremes of color are shown in the fourth and fifth columns, and, in the next two columns, the mean photovisual magnitude and mean color index for a group (usually ten) of the faintest blue stars. The distances in the last column are taken from the tables in Appendices A and B

Similar results have been obtained for faint stars in four Milky Way fields, and Seares has found faint blue stars in the Selected Areas that fall in low galactic latitude

Considering the relatively large distances of the tabulated objects, and their wide distribution, we appear justified in generalizing the results of the

See ciph 12 SHAPLEY, Mt Wilson Comm 44 (1917)

Table 18 Test for Space Transparency in Various Regions

Citatur	Galactic		Color Index		Moun Pv	Mars Cojor	Distance in
	Longituda Latitudo		Largest Smellest		Mag.	Todas	Kiloperace
Mossler 3	12° 27 33 139 142 154 189 332 338 355	+78° +40 -28 +1 +3 -1 +46 -9 -3	+1,77 +1,42 +1,50 +2,12 +1,50 +1,31 +2,00 +1,67 +2,05 +2,06	-0,39 -0,52 -0,21 -0,45 -0,30 -0,15 -0,04 -0,14 -0,16	15,1 16,54 16,0 13,5 12,5 11,5 12,3 14,6 14,34	-0,16 -0,34 -0,14 -0,16 -0,23 -0,07 -0,02 -0,10 -0,28 -0,08	12,2 10,3 13,1 1,1 1,2 0,8 0,8, 10,8 6,8

study of Messler 13, and in concluding that interstellar media, throughout the distances here concerned, have no serious effect on the color of light. This conclusion does not bear on obstruction of light by recognised diffuse nebulosity (dark and bright), nor on the colors of nebulous stars, nor on the absorption within galactic clusters which has been found lately by several investigators and sometimes interpreted, perhaps prematurely, as evidence of strong general anace absorption

28. Colors in Other Distant Objects. The magnitudes and color indices of thirty-eight supergiant red stars in NGC 7006 have been measured. Even at a distance more than five times that of Messier 13, no abnormal redness appears in this cluster, and there is no other peculiarity in its star colors, although its radiation has travelled through space for an interval of 480000 years. The mean color index of 1,10 for the brightest thirty-five stars, which is comparable with that of 1,15 for Messier 3 and 1,03 for Messier 13, shows that the reddening does not exceed a tenth of a magnitude. Therefore the absorption coefficient, expressed as change of color index for each parsec of distance, is d < 0.000002

This same coefficient of space absorption was found by LUNDMARK and LINDBLAD in a study of the Andromeda Nebula. Investigations at Harvard of the cloud of three hundred bright extra-galactic nebulae in Coma and Virgo4 have resulted in the determination of the coefficient, d < 0.00000007

29. Messier 5 and the Relative Speeds of Blue and Yellow Light. One significant consequence of the study of variables in Messier 5 has been a determinution of the relative speeds of light of different wave lengths. Periods ranging from six to twenty hours, with an average of thirteen hours, have been found for a large number of stars; many of them are known to within a fraction of a second. The steep rise to maximum brightness of a typical cluster type Cepheid variable makes the time of median magnitude on the ascending branch more accurately determinable than the times of maximum or minimum. It was found by WENDELL at Harvard and by the writer at Princeton that the time of median magnitude can be determined to within two or three minutes.

For the revision of the periods and for the test of the speed of light I made five special series of photographs of Messier 5 in 1917, using the 60-inch reflector of the Mount Wilson Observatory. The exposures of twenty to thirty minutes

<sup>&</sup>lt;sup>1</sup> SEARES and HUBBLE, Mt Wilson Contr 187 (1920)

SHAPLEY, Mt Wilson Contr 165, p 5 (1918); see also SHAPLEY and MAYRERRY, Mt Wilson Comm 74 (1921).

Ap J 50, p. 386 (1919) Through an error the value is printed ten times too small
Sharkey and Amss, Harv Circ 294 (1926)
Harv Ann 73, Part 2 (1917), Harv Bull 763 (1922), Harv Repr 5 (1923), Wash Nat Ac Proc 9, p 386 (1923); see also ciph 16 above

that were necessary to record the yellow light with an isochromatic plate and yellow filter were interrupted in the middle for an exposure of one or two minutes on an ordinary plate sensitive to blue light. In this manner the variable stars were photographic in two regions of the spectrum at essentially identical times. Photographic and photovisual observations were carried on throughout several hours of the night. Each run of plates gives fragments of the light curves of all the variables, but since the average period is thirteen hours, for only a few stars in each series was the light rising from minimum through median to maximum during a given night's run on the cluster.

The measurement of the plates yielded 6300 magnitudes, from which fourteen measures of the times of median magnitude both in blue and in yellow light were obtained for eleven different variables. The results appear in Table 19. The maximum effective wave length for blue light is approximately 4500 Å, and for yellow light, 5500 Å. The observed difference in the times, t, of rise to median magnitude,

$$\Delta t = t_{\rm pg} - t_{\rm pv}$$

is given in thousandths of a day in the fourth column. Thus a positive residual would indicate that the yellow light is measured as arriving first

Number of Variable	Photographic Range	Photovisual Range	14	Weight
1	1 <sup>m</sup> ,2	O <sup>in</sup> ,7	{ +0°,009	3 2
4	1 ,4	0 ,9	100,001	1
8	1.1	0,7	-0,012	l i
12	1 ,3	1,0	<b>−0,005</b>	2
i8	1 .5	1 ,05	- -0 ,001	1
20	0,9	7, 0	0,000	2
28	1,2	8, 0	-1-0 ,006	2
59	1,0	0 ,7	-0,003	1
63	1,2	0,9	-0,002	3
64	1,0	0,7	- 0 ,005	1
81	1,1	8, 0	100,001	3

Table 19 Differences in Times of Median Magnitudes

It is seen immediately that there is no measurable difference in velocity, the values of \$\alpha t\$ being of the order of the uncertainties of measurement, six are positive, seven are negative, and one is zero. The mean value of the difference in time required for the passage of blue and of yellow light over the distance from the cluster to the earth is

Blue—Yellow = 
$$-0^{d}$$
,00012  $\pm 0^{d}$ ,0007 =  $-10$  seconds  $\pm 60$  seconds.

We have determined in this experiment merely an upper limit to the difference in speed. We find that since the distance to the cluster is approximately 11000 parsecs, light of these two colors, which differ by twenty-five per cent in wave length, differs in time of arrival at the earth by no more than one minute after traversing space for more than thirty-five thousand years. In other words, the relative size of the probable error indicates that the chances are even that the speeds of blue and yellow light do not differ by more than one part in twenty thousand million; probably they do not differ at all

From eleven determinations of the maxima for nine variables in Messier 5, a similar equality in speed was found for blue and yellow light. In this result,

also, the probable error exceeds the observed average difference, but the determination has much less weight than the one based on median magnitudes

It is to be noted in conclusion, however, that the essential equality in speed does not necessarily indicate a perfectly transparent interstellar medium. As GROOSMULLER<sup>1</sup>, among others, has pointed out, a large amount of dust and gas can exist in space without measurably affecting the speed of light.

#### h) The Distances and Dimensions of Clusters.

30. The Photographic Period-Luminosity Curve. The correlation of absolute magnitude with period for Cepheid variables is discussed in detail olsewhere. But the importance of the period-luminosity curve in obtaining the distances of globular clusters is sufficiently great to justify a briof consideration here of some outstanding features. Because of their bearing on the investigations of cluster magnitudes and distances, it is well to mention the derivation of the adopted photographic period-luminosity curve, and the determination of its zero point.

a) The Photographic Period-Luminosity Curve The curve relating period to magnitude was obtained from variables in the Small Magellanic Cloud. The plot of the median apparent photographic magnitudes against logarithms of the periods for 106 variables is shown in Figure 17 Points of low weight are enclosed in circles, and the periods determined by Miss Leavitr are indicated by crosses. A few of the stars diverging most widely from the curve may not be actual members of the system, but the fairly high galactic latitude (-33°) makes rather unlikely the occurrence of typical Cephelds except as members of the Cloud.

The deviations from the curve in Figure 17 are not larger than might be expected in view of the difficulties of observation. The average deviation in magnitude of the thirty-two variables whose periods Miss Leavitt obtained is 0,19, for the seventy-four other stars it is 0,25, for all, 0,23. The systematic magnitude deviation from the curve is -0.063 for the Leavitt variables and +0.049 for the others, showing a negligible systematic difference between the earlier and the later work

Some of the dispersion in magnitude can be attributed to the thickness of the Cloud in the line of sight, but between the variables at the near and far edges this correction amounts to only 0,14 magnitudes. If  $\alpha$  is the angular radius of a sensibly spherical system, the maximum dispersion in magnitude arising from the thickness is given with sufficient approximation for remote systems by

$$\Delta m = 5 \log \left[ (1 + \sin \alpha)/(1 - \sin \alpha) \right]$$

The correction is thus independent of the distance and real thickness. The diameter of the Small Cloud is 3°,6 and the extreme correction to mean values is therefore less than a tenth of a magnitude.

Other factors contributing to residuals from the period-luminosity curve are the Emerican effect and obstruction by nebulosity. To these may be added actual deviations for the periods and magnitudes from average conditions—that is, a true scattering which may arise from differences in mass, structure, or other physical properties. We should also consider errors in the periods and the observational uncertainties for individual variables, which may easily amount to two tenths of a magnitude. Errors due to the failure to resolve double stars are not likely to be serious

<sup>&</sup>lt;sup>1</sup> HEMEL on DAMPHUM, 22, p 153 (1924)

LUDENDORFF, Volume VI, 2, chapter 2.

In Figure 17 only two stars with periods shorter than a day are included. There appear to be many others of this sort in the Cloud<sup>1</sup>, but they are not considered in the present discussion because of the relative weakness of the magnitude scale fainter than 17,0. These cluster type variables will soon be studied with a large reflector, when short exposure photographs and better magnitude sequences can be used.

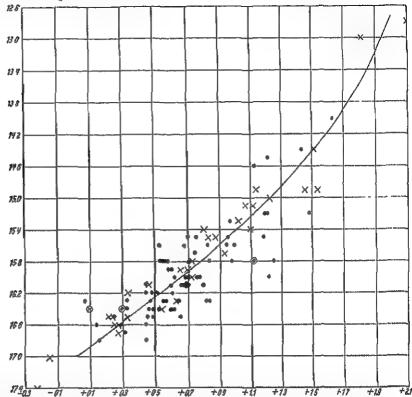


Fig. 17 Photographic period-lummosity curve Ordinates are apparent imagnitudes; abscissae are logarithms of the periods Crosses refer to periods determined by Miss Leavitt Circles enclose values of low weight

By grouping the points plotted in Figure 17, first in order of the logarithms of the period, and then in order of apparent magnitude, we get the two sets of means shown in Table 20. All magnitudes of Cepheids in this chapter are median values. that is, (max + min)/2

Table 20 Data for the Photographic Period-Luminosity Curve

Moan I og P	Mognitude	Number	Absolute Magnitude	Meaa Magnitudo	Mean Log P	Number	Absolute Magnitude
-0,194 +0,253 0,610 0,986 1,357 1,961	17,2 16,51 16,08 15,48 14,93 12,90	2 17 53 21 11 2	-0,12 -0,81 -1,24 -1,84 -2,39 -4,42	17,00 16,44 15,99 15,51 15,05 14,38 12,90	+0,054 0,437 0,677 0,871 1,267 1,380 1,961	4 33 36 17 9 5	-0,32 -0,88 -1,33 -1,81 -2,27 -2,94 -4,42

SHAPLEY, Wash Nat Ac Proc 8, p 69 (1922)

The distance modulus for the Small Magellanic Cloud (see crph 39) is 17,32, and the absolute magnitudes for variables in the Cloud are therefore given by M=m-17,32. In the fourth and eighth columns of Table 20 are the absolute magnitudes corresponding to mean values of  $\log P$ 

A by-product of work on the period-luminosity curve is a determination of the relation between period and spectral class, shown in Figure 18. The period-

Spectrum curve is discussed by Ludendorff, in Vol VI, Chapter 2, of this Handbuch. It may be noted here that the relation holds for long-pariod and RV Tauri variables, as well as for the cluster types.

b) The zero point. Me Although the form of the period-luminosity curve and the deviations from it are now fairly well known, we remain for the time being in a state of suspense with regard to the zero point Originally based on

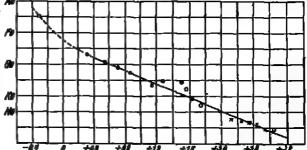


Fig 18. The relation of spectral class (ordinates) to logarithm of the period (abscissed) for variable stars. Open circles refer to RV Tauri variables, crosses to long period variables, dots to Copheid variables, and the open square to the mean cluster type Copheids.

the parallactic motions of the few bright Cepheld variables for which accurate Proper motions were available, the zero point has been the target of much discussion and suggested revision.

KAPTEYN and VAN RHIJN believed that the large observed proper motions of cluster type Cepheids in the Galaxy show them to be dwarfs and necessitate an enormous shift of the zero point I had adopted, with consequent disaster for my measures of galactic dimensions. Later discussions of the proper motions and radial velocities of these variable stars indicated, however, that they could not be used in the manner adopted by KAPTEYN and VAN RHIJN. Many of the stars of this subtype belong to the well known high velocity group, and when allowance is made for their high space velocities, the proper motion data are not in disagreement with the zero point indicated by the classical Copheids,

The most thorough study of the zero point is that by R E Wilson\* He concluded that the distances that I had based on the period-luminosity relation should be decreased by twenty or thirty per cent, but in view of the new generally accepted Kapteyn correction to Boss' proper motions, this change in the zero point by Wilson may be, as he himself pointed out, largely effected. In the most recent discussions of Cepheid motions Ookt gets 1,06 ± 0,26 (m. e) as the correction factor to my parallaxes, using Mount Wilson measures of radial velocity.

So far us they go, the trigonometric parallaxes in the Yale Catalogue and the Mount Wilson and Upsala spectroscopic parallaxes support the system based on the period-luminosity curve. van Maanun has found satisfactory agreement of his trigonometric parallaxes with the values from the period-luminosity relation.

<sup>&</sup>lt;sup>2</sup> BAN 1, p. 37 (1922). Hary Circ 237 (1922); R.H. Wilson, A J 35, p 35 (1923).

<sup>\*</sup> A J 35, p. 35 (1923). 
\* B A N 4, p. 91 (1927).

\* Schleringer, Catalogue of Parallaxes, Yale Univ. Obs. 1924; Shapery, Harv Circ.

237 (1922). Lindblad, Ap J 59, p. 37 (1924). 
\* Publ A S F 32, p. 62 (1921).

In view of Wilson's work, however, and of other indications that the nearer galactic Cepheids give too bright a zero point. I have made a provisional correction of +0,23 magnitudes, which reduces to 0,00 the absolute photographic magnitude of cluster type variables. The correction has been applied to the period-luminosity curves, and to all the computed distances appearing in this chapter. It amounts to a systematic decrease of eleven per cent in the distances computed from older period-luminosity curves.

Awaiting the completion in a few years of the McCormick and Mount Wilson investigations of the proper motions of a large number of galactic Cepheids, we adopt this corrected zero point and the scale of distances dependent on it

The resulting absolute magnitudes in clusters and Magellanic Clouds are accordant with a large body of astronomical observations, and compatible with recent astrophysical theory. There seems to be no serious inconsistency in the resulting luminosities, except that the revision has made the maximum hightness of stars in globular clusters surprisingly low. I am inclined to predict that the correction to the zero point now adopted will never exceed a quarter of a magnitude, and that it may be in either direction, but this prediction should be made with caution because of the increasing evidence of peculiar drifts and of heterogeneity in the star structure in the immediate vicinity of the sun

81. Distances of Globular Clusters Obtained from Cepheids and Bright Stars. From the period-luminosity curve distances can be determined directly for all the globular clusters in which the Cepheid variables have been studied and magnitude scales determined. In Table 21 are collected all the relevant observational data now available from my own studies<sup>2</sup>, and also, for N G C 5053 and N G C 5466, the magnitudes measured by BAADE with the Bergedon reflector For the sake of homogeneity, the magnitudes measured at Bonn by Kusiner

for three globular clusters (M3, M15, and M56) were not used

a) The Observations The new material represents a considerable expansion over that in hand twelve years ago. The determination, in 1917, of the parallaxes of sixty-eight globular clusters included only seven for which the variable stars had been studied, and for two of these the preliminary data could not be used quantitatively. As variable stars in clusters are fundamental in calibrating methods of determining distances, I have given considerable attention since 1917 to the discovery and observation of variable stars in clusters. Mount Wilson plates and various series in the Harvard collection have been used for this work. I am indebted to several assistants at Mount Wilson and Harvard for aiding in this laborious research, and especially to Miss Sawyer who has taken an active part in the recent revision of cluster distances.

There are now nineteen instead of five clusters in which variable stars have been measured sufficiently to enter the new determination of distances. Of the 730 variable stars in these nineteen clusters, 524 have been studied enough to be useful in fixing the "median magnitudes" for the clusters concerned. In 1917 the absolute magnitudes of the high luminosity stars had been measured for only twenty-eight clusters, we now have measures on the brighter stars in forty-eight systems.

b) The Methods For a new determination of distances and distribution, I have followed in principle, though not in detail, the methods developed and

<sup>&</sup>lt;sup>1</sup> See various papers by ten Bruggencate, Curtis, Doig, Kienle, Mai mouist, and Strömberg Since this chapter was written in 1930 there have been further discussions of the zero point by Gerasimovič [A J 41, p 17 (1931)], Nordsfröm [Lund Obs Circ 2 (1931)], and others

<sup>&</sup>lt;sup>3</sup> From Hary Bull 869 (1929)

<sup>&</sup>lt;sup>a</sup> Harv Bull 869 (1929)

Table 24 Magnitudes of Variables and Bright Stars

Table 21 Magnitudes of Variables and Bright Stars							
N G.C. C			hotograpkie Megalinde		Preliminary	Notes	
N G.L.		Variables	25 Br	6th Star	30th Star	Modulus	
404	ш		13,09	12,4	13,4	14,33	Note 1, 47 Tucanno
104 288	*** (		14,80	14,5	15,1	15,87	Note 2
362	în	15,5 (4)	14,12	13,5	14,8	15,49	
1904	v	ו נבו כיכי	15,29	15,01	15,72	16,61	Member 79
2808	ĭ		14.9	14,3	15,4	16,25	,,,
	$\hat{\mathbf{x}}$	14,52 (5)	13,52	13,3	13,8	14,57	Note 3
3201	ρÂ	16.8 (1)	16,58	16,23	16,93	16,99	GP, note 6
4147	X	10.0 (1)	14,80	14,31	15,08	15,87	Monder 68
4590	v	15,90 (6)		14.94	15,26	16,36	Mondor 53
5024	χĭ	16,19 (8)	15,07		16,0	16,15	GP
5053			15.65	15,1	13,1	14,22	a Contapri
5139	VIII	14,37 (5)	12,91	12.6		15,48	Meanler 3
5272	VI	15,50 (8)	14,23	13,92	14,45	16,16	GP
5466	XΠ	16,17 (6)	15.72	15.1	16,2	16,16	Ŭ.
5897	XI		15,15	14,9	15,4		Mondor 5
5904	v	15,26 (8)	13.97	13,74	14,27	15,26	arrena 3
6093	프		14,88	14,72	15.09	16,24	Note 4, GP, Mossier 4
6121	IX	14,27 (6)	13,88	13.3	14,4	14,29	GP
6144	IX	_	15,76	15,2	16,3	16,22	l GE
6171	ж	— !	15,46	15.2	15,9	16,57	Marrian 44 Main 8
6205	v	15,20 (4)	13,75	13.45	13,92	15,10	Mosaier 13, Noto 5
6218	IX	_	13,97	13,56	14,31	15,07	Mossier 12
6229	VΠ	_	16,18	15,90	16,37	17,36	ł
6235	X		16,17	15.7	16,8	17,28	16
6254	VΠ	_	14,06	13,35	14,38	15,17	Momier 10
6266	ΙV	16,40 (6)	15,87	15,6	16.1	16,37	irrog , Memior 62
6333	VIII	Page 1	15,61	15,08	15,88	16,70	Mondor 9
6341	IV	_	13,86	13,60	14,16	15,48	Mondor 93
6356	I	t –	17,16	16,86	17,44	18,51	
6397	IX	_	12,61	11,9	13,1	13,67	GP .
6402	AIII	ì –	15,44	14,85	15,86	16,56	Mosaler 14
6535t	XI:	_	15,9	15,3	16,4	16,89	l
6541	ш	14,42 (4)	13,35	12,7	13,8	14,53	Noto 3
6626	īv	- 1.7	14,87	14,49	15,11	16,14	Monior 28
6638	VI	l —	16,22	15,90	16,60	17,48	1
6656	VII	14,06 (5)	12,93	12,80	13,26	14,12	Mounter 22
6712	IX		16,10	15.65	16,36	17,17	J .
6723	VII	15.33 (6)	14,20	13,7	14,8	15.37	
6752	VΙ	- 1000	13,26	12.8	13,6	14,47	
6779	X	} _	15,31	14,98	15,70	16,39	Momier 56
6800	XI		13.58	12,9	14,2	14,58	Memler 55
6864	ī	} ~	17.06	16,76	17,35	18,43	Mossior 73
6934	VIII	_	15,78	15,33	16,11	16,91	
6981	IX	16,80 (8)	15,86	15.53	16,20	16,86	Messior 72
7006	Ī	18,96 (6)	17,50	16,99	17,89	18,91	
	ΙÝ	15,63 (7)	14,31	14,13	14,55	15,63	Mondor 15
7078	ř	15.71 (4)	14,61	14,25	14,76	15,81	Momier 2
7089	😾	131/1 (4)		13,77	15,04	15,80	Memior 30
7099	XII.		14,63	16,3	17,1	17,22	GP
7492	I with		16,82	10,3	1 ,,,,	1 1122	

<sup>4</sup> The long period variables in 47 Tucanae (Harv Bull 763) could not be safely used in measuring the distance.

2 The mean magnitude of the 25 brightest stars was determined at Mount Wilson to be 14,81, with a range of 14,38 to 15,04.

3 The magnitudes of N G C, 3204 and N G C, 6541 may be considerably in error due to unsatisfactory comparison sequences. They are not included in the determination of the reduction curves for apparent integrated magnitudes and diameters, though they are appropriately used in constructing Table 22.

4 For N G,C, 6124 the serve point of the magnitude scale depends on both Harvard and Mount Wilson measures of Mount Wilson plates.

5 The measures of 13,4 to 14,1

6 Baanz has recently studied this difficult system [A N 239, p. 353 (1930)] and his better results give a modulus 16°,52 ± 0°,05. He necrectly reassigns the cluster to a much earlier class (on the basis of new long exposure plates)

described in 1917. As before, the reasonable assumption is made that the median absolute magnitude of variables with periods less than a day is constant from cluster to cluster. The difference between the median magnitudes of the variables and the magnitudes of the brightest stars is again found, on the average, to be so definite a quantity that brighter star magnitudes themselves can be used as criteria for those clusters where variable stars are lacking or have not been analyzed. We go farther by taking measures of integrated apparent brightness (total magnitude) and angular diameter as criteria of relative distance, using these measures, after appropriate calibration, not only to strengthen the determination for the forty-eight clusters whose variables and bright stars have been studied in some detail (Table 21), but also for the other forty-five clusters now known in the galactic system for which we have as yet no measures of variables or of individual bright stars.

c) The Results A few of the essential details of Table 21 should be mentioned. The classes in the second column are those described in ciph 6 and listed for all globular clusters in Appendix A. The apparent median magnitude of cluster type variables is in the third column. When a cluster contains long period Cepheids, their magnitudes are reduced to the cluster type median by means of the period-luminosity relation and are then combined with

the magnitudes of the cluster type variables

Since we have adopted zero as the absolute photographic magnitude for cluster type Cepheids, the third column actually contains a direct determination for numeteen clusters of the distance modulus, m-M=5 ( $\log d-1$ ), where d is the distance in parsecs and m is the apparent median photographic magnitude.

The parenthetical numbers in the third column are the combining weights assigned to the mean median magnitudes of the variables in each cluster. These weights depend on the number of variables, on the detail with which periods and light curves are known, and on the estimated accuracy of the magnitudes. The means of the third column are used in conjunction with the distance moduli derivable from the next three columns to determine the preliminary modulus in the seventh column.

The fourth column contains the mean magnitude of the twenty-five brightest stars (after the exclusion of five of maximum brightness in order to avoid, or at least to diminish, the effect of optical doubles and of the chance superposition of bright field stars). A weakness in using this method lies in the dependence of the area in each cluster surveyed on the compactness or distance of the cluster, or on the richness of the foreground of galactic stars. Uniformity of selection was strenuously sought, and I am convinced that for most clusters the mean of the twenty-five brightest stars, as well as the magnitude of the thirtieth star, would not be appreciably disturbed by including or excluding too much of the dense central region.

In the following columns are given the apparent magnitudes of the sixth and thirtieth stars in each cluster, the sixth star is the brightest object and the thirtieth the faintest included in the mean of the twenty-five brightest

The difference between the median magnitudes of the cluster type variables (third column) and the magnitudes of the three succeeding columns are found to depend on the class of the cluster. Table 22 gives the readings from the smooth curves that represent the changes of the three sets of differences with class. In the earlier work a single constant value, 1,28, for the difference between the median and the twenty-five brightest, was used; the two other sets of differences were not then considered in obtaining distances. The range of variation now found for med.—25 br is from 0,92 (Class XII) to 1,34 (Class I).

The present method of using three different points in the sequence of apparent magnitudes is essentially equivalent to comparing, from one cluster to another, the general luminosity curves for giant stars. Its advantage over provious practice lies in the allowance it makes for abnormal distribution—or even small deviations from the average—in limited groups of stars. The extended method is obviously justified by the non-parallelism of the three curves representing the relation of reduction factors to class of cluster.

A comparison of the modulus from variable stars alone (third column of Table 21) with the preliminary modulus (seventh column) based on bright stars and variables together, indicates how satisfactorily the data for bright stars agree with the results from the variables. The agreement shows, in fact, to what extent one typical cluster is comparable with another inside the various classes.

d) Giant-poor Clusters. A number of the clusters of the more open classes (Classes IX.—XII) were found upon examinations for star frequency to be poor in giant stars. Their luminosity curves are abnormal. Such objects are indicated by the letters GP in the last column of Table 21. They were not used in deriving differences in Table 22 for normal clusters, and the irregular cluster Messler 62 (N.G.C 6266) was also excluded.

Table 22 Reduction to the Median Magnitude of Cluster Type Variable Stars.

		_	
Class of Chapter	Median — 25 Br	Median dib Star	Median—30th Star
1	1,34	1.77	1,04
II	1,33	1,74	1.01
ш	1,32	1,71	0,98
IV	1,30	1,68	0,95
V	1,28	1,64	0,92
VI	1,24	1,60	0,89
VII	1,20	1,56	0,86
VIII	1,15	1,51	0,83
TX.	1,10	1,46	0,80
×	1,05	1,40	0,77
XI	0,99 :	1,34	0,74
XII	0,92	1,29	0,71

The GP clusters with measured variables were used, however, to determine special reduction factors for all the "giant-poor" clusters. A study of these abnormal systems shows that the following mean values can be satisfactorily used in reducing the magnitude measures to the standard median magnitude of the cluster type variables.

e) The System of Weighting. For the typical clusters for which bright star magnitudes have been measured (Table 21) the reductions to "median magnitude" are made directly with the aid of Table 22, and the three resulting determinations for each cluster are combined with weights 2, 1, 1, for the mean of 25, 6th, and 30th, respectively, to get the preliminary distance modulus. The modulus from variable stars, when available, was, of course, included with appropriate weight in the mean value in the seventh column of Table 21. The final weight of each preliminary modulus is therefore the weight in the third column (from the variable stars) increased by four.

32 Distances of Globular Clusters Obtained from Diameters and Integrated Magnitudes. Further steps in deriving the distances of the clusters are now obvious and need only be summarized. Plotting the values of the preliminary modulus in Table 21 first against the angular diameter and then against integrated brightness, we get two empirical curves that may be used for the derivation of the distance modulus of any globular cluster for which the total magnitude and angular dimensions have been measured. The coordinates of these curves are given in Tables 23 and 24

Table 23 Modulus-Diameter Curve for Globular Clusters

Table 24 Modulus-Magnitude Curve for Typical Globular Clusters

		٠,			
Modulus	I og Diameter	Modulus	Integrated Magnitude		
14,0	1,30	14,0	3,1		
14,5	1,20	14,5	3.7		
15,0	1,05	15,0	1,5		
15,5	0,89	15,5	5,6		
16,0	0,67	16,0	6,7		
16,5	0,42	16,5	8,1		
17,0	0,24	17,0	0,4		
17.5	0,11	17.5	10,5		
18,0	0,02	18,0	11,4		
18,5	9,92	18,5	12,2		

a) Angular Diameters. The adopted diameters, which are given for all globular clusters in Appendix A, are based on measures made at Harvard on photographs of Series A (Bruce 24-inch refractor) and of Series AX and AY, which are made with short focus cameras, double weight is assigned to the large scale plates. It should be noted that the measured angular diameter of a cluster depends on exposure time, the recorded diameters, d, are therefore not exactly proportional to the parallaxes nor related by the normal formula d=k 100,2m to the integrated apparent magnitudes, m. This limitation, however, does not decrease their value as a measure of relative distances

In general the measures of diameter refer to the nucleus or the main body of the cluster. Plates of long exposure, made with large telescopes, when carefully counted and analyzed, show that the clusters are of considerably greater extent than is recorded in these "surface" measures of angular diameter. The distribution of cluster type variables also frequently indicates the wide dispersion of cluster stars. For example, Bailey notes the existence of variables 19' from the center of NGC 3201, though the "working diameter" in the catalogue is 7',7, in agreement with the value given in the NGC.

b) Integrated Appaient Magnitudes The photographic magnitudes for globular clusters are on a convenient but not the conventional scale. They were measured by Miss Sawyer on plates of the AX and AY scries. The scale in much more open than in the customary Pogson system and as a result the integrated brightness listed in Appendix A ranges from the third to nearly the thirteenth magnitude. It the scale were on the usual system of stellar magnitudes, this difference of ten magnitudes would indicate a range of one hundred in the relative distances, rather than the factor of ten which is actually found

The measures of brightness are, however, fairly accurate, since much care was taken in the selection of plates and of magnitude sequences. Photographic images of globular clusters depend on the lenses, plates, and photographic development, and for the brighter and larger clusters are necessarily uncertain

<sup>&</sup>lt;sup>1</sup> Harv Bull 852 (1927)

<sup>&</sup>lt;sup>2</sup> Harv Circ 234 (1922)

<sup>&</sup>lt;sup>3</sup> Harv Bull 848 (1927)

not only because of the size and texture of the photographic image, but also because of the scarcity of suitable comparison stars and the general weakness of photographic sequences for bright magnitudes. With the warning that these now measures of brightness cannot be used for the computation of absolute magnitudes or for comparison with visual integrated magnitudes for the determinations of color index, or, as DUFAY¹ has discovered, used directly for the derivation of relative distances, we can proceed to make important indirect use of them, whon properly calibrated, to get at the distances of clusters for which we have no data on individual bright stars or variables

c) The Distance Moduli and Their Weights Unit weight is assigned to each of the determinations of cluster distances based on magnitude and on angular diameter. When other values are available, as in forty-eight of the clusters, the weight four is assigned to the modulus depending on the hright stars, and the weight for the modulus from variable stars is that given in Table 24 above For instance, the four values of the modulus for Messier 3 (N G C. 5272) are 15,50 (variable stars), 15,45 (bright stars), 15,23 (diameter), and 15,0 (integrated magnitude) The corresponding weights are 8, 4, 1, 1 The adopted mean modulus is 15,43, corresponding to a mean distance of 12,2 kiloparsecs or about 40000 light years.

For the "giant-poor" clusters the modulus from the angular diameter is derived from the curve for normal systems, but the modulus from the integrated magnitude is derived from a smoothed curve based on only the clusters that are deficient in giant stars. Loose globular clusters, such as NGC 288 and NGC 3201, may approach the deficient condition, but the variable reduction factors of Table 22 largely correct for minor systematic deviations from average conditions of magnitude frequency.

The adopted mean modulus for each cluster is given in Appendix A, followed by a letter indicating the quality of the determination. The assumed quality depends on both the final weight of the modulus and the accordance of the various determinations. The letter "a" indicates the values of highest weight, the letter "e" refers to the most uncertain determinations, which are, unfortunately, still too numerous. The distribution among the qualities is. a 13, b 25, c 23, d 17, and e 15.

For clusters in which there is good material on variable stars, the determinations based on total magnitude and diameter contribute but slightly to the finally adopted modulus. The computed distances for nearly half of the clusters, however, depend entirely on the relatively low weight determinations of the apparent brightness and diameter. Efforts will be made within the next few years to extend the work on variables and magnitudes of individual stars. As a result, alterations in the distances of individual clusters can confidently be expected, but it is practically certain that the scale of the system of clusters and of the Galaxy will not be affected thereby. The zero point correction predicted above is the only agent likely to disturb the general scale of distances.

d) Comparison with Earlier Results. As previously noted, we have made a systematic correction of eleven per cent to the distances of globular clusters through making a provisional alteration in the zero point of the period-luminosity curve. On comparing the individual distances now given (Appendix A) with those previously obtained through my investigations at Mount Wilson<sup>2</sup>, the average difference is found to be twelve per cent (after allowing for the systematic change). The revision of the individual distances has therefore not

<sup>&</sup>lt;sup>1</sup> Lyon Bull 11, p 59 (1929)

Mt Wilson Contr 152 (1918).

been at all diastic, though in a few cases where the early material was unusually weak it has been more than thirty per cent. Because of the great increase in the basic photometric data and in the number of globular clusters whose Cepheid variable stars have been studied, the present values are much more secure than those formerly determined.

At times during the past twelve years the scale of distances has been challenged, and evidence or argument advanced to show that I had derived cluster distances and galactic dimensions that might be from five to one hundred times too large. It is madvisable to take space to reproduce here or even to summarize these many discussions, because the general order of distances, and consequent galactic arrangement, is now very generally accepted. It should suffice to mention Ten Bruggencate, Charlier, Crommelin, Curris, Doig, Hopmann, Kapilyn and van Rhijn, Lundmark, van Maanen, Malmquist, Oori, Parvullsco, Perrine, Schouren, Sfares, and R. E. Wilson as principal contributors on one side of the other of the discussion, and for the details refer to their papers which are listed in the general bibliography of star clusters in Harvard Observatory

Monograph No 2

of the number and distribution of galactic clusters in ciph 9 was based on a new and fairly homogeneous catalogue which is given in Appendix B. Although intentionally incomplete because of the adopted restrictions which exclude poor or indefinite groups, as well as the galactic clusters in the Magellanic Clouds, the catalogue is probably the most serviceable yet compiled for the general study of galactic clusters. Miss Payne is responsible for the classification of the individual clusters and for the estimates of magnitudes and of numbers of stars. The classifications (sixth column of the catalogue) are on the system proposed in ciph 5. The galactic coordinates are on the Harvard system (Pole at 12<sup>h</sup> 40<sup>m</sup>, +28°1). The angular diameter is from Melotic's catalogue, except when in heavy type, in which case the estimate was made by Miss Roper using Harvard photographs; it is necessarily approximate and generally refers to the obvious nucleus. Detailed star counts nearly always extend the diameter

The orientation, expressed as the position angle of the major axis of an elongated cluster with reference to the galactic equator, was estimated independently by Miss Payne and the writer on Harvard photographs for the more compact galactic clusters (Melotte's Class II), the results, which are very accordant, are discussed in ciph 24 above. The ninth column of the catalogue indicates the approximate number of stars that could be assigned to each cluster on plates whose fainter magnitude limits are as given in the tenth column. In the clusters for which this fainter limit is not given, the majority of the cluster

It is probable that many stars within the bounds of a cluster are superposed members of the intermediate galactic field, for these systems usually lie in rich regions in low galactic latitude. Obvious bright foreground stars were not considered in choosing the fifth star for each group and estimating its magnitude. It is probable, therefore, that nearly always the estimated magnitudes in the eleventh column actually refer to a star that is near the maximum luminosity in its cluster. How bright absolutely that object may be depends to some extent on whether it is a member of a Pleiades or a Hyades type of cluster, and also whether the cluster is poor or rich in stars. No claim to accuracy is made for these estimated magnitudes; they are given as rough indicators of the brighter

<sup>1</sup> Pickering, Harv Ann 56, p 1 (1912)

limit of apparent magnitude, and as a means of making prehumary estimates of the distances and space distribution of galactic clusters.

34. Parallaxes of Galactic Clusters. Direct trigonometric measures must necessarily full to give useful information on the distances of galactic clusters, even when they are as near as the Pleiades Measures of proper motions and fairly extensive studies of the spectral composition of some of the nearer galactic clusters have led to useful estimates of the approximate distances. For ten systems, including the Pleiades, the Hyades, Priesope, Messier 11, Messier 37, the double cluster in Perseus, and the bright cluster in Coma Borenices, the distance in kiloparsees has been determined through more or less detailed studies of motions, magnitudes, and spectra, and is entered between the twelfth and thirteenth columns of Appendix B. The sources are given in the notes at the end of the catalogue. The accuracy of these ten values is not high, except for the Hyades.

For other galactic clusters no equally dependable measures of the distances are yet available, though provisional photometric or spectral parallaxes have been published by various investigators. Doing and Raam in particular have analyzed the spectral data and derived useful preliminary estimates for many of the brighter groups. My own early values for a number of the galactic clusters are systematically too great; the published estimates were admittedly very provisional, and gave distances that now appear on the average to be two or three times too large because of the tentative assumption that the brighter stars were of exceptionally high luminosity

TRUMPLER's spectroscopic and photometric researches on galactic clusters, which have been in progress for some years, should eventually give fairly accurate values of the distances of many of the galactic clusters; his method involves the use of luminosity curves for various spectral classes in the clusters, or, what is essentially the same, the use of a Russell diagram for fixing the distance modulus. The final standardisation of his system of distances will probably await much serious work on the absolute luminosity dispersion for stars of Class A.

In 1931, P COLLINDER published an exhaustive study of galactic clusters, dealing with their structural properties and distribution in spaces,

Spectroscopic paraliaxes should eventually give the distances of a number of galactic clusters which contain late type stars; and with the development of dependable spectroscopic methods for early type stars, such as those for cahadowed by Miss Williams' in analyses of absorption lines in Class A spectra, the spectrum line method may turn out to be the most dependable one for measuring the distances of galactic groups. It will be a procedure much less time-consuming than the Russell diagram method

Since the accurate determination of the distances of galactic clusters is still mainly in the future, it seems worth while for the time being to tabulate direct photometric estimates. Assuming that the fifth star in order of brightness in a galactic cluster has the absolute magnitude of an average bright Class A star, +0,5, we derive the distances given in the twelfth column of Appendix B. In the thirteenth column are given the distances corresponding to an assumed absolute magnitude of -0,5. Since we are dealing with objects selected on

<sup>&</sup>lt;sup>1</sup> J B A A 35, p. 201 (1925). Lund Modd Série II, No. 28 (1922).

Mt Wilson Comm 62 (1949).
 Preliminary publication in Lick Bull 14, p. 154 (1930), after the completion of this manuscript.

Publ A 8 P 37, p. 307 (1925).
 Lund Obs Ann 2 (1931).
 Harv Circ p 348 (1929).
 Miss Ancier has extended the method and applied it to various galactic clusters. [Herv Circ 352 (1930); Herv Bull 882 and 883 (1931)].

account of high luminosity, these greater distances are probably more nearly correct. They have therefore been used in computing, in the next two columns, the linear diameter of each cluster in parsecs and the distance of the cluster from the galactic plane. The wide range in linear diameters, reflecting in part the difficulty of estimating the bounds of a galactic cluster, is a striking feature of these computed results. The smallest objects appear to be only a few light years in diameter, and the largest more than fifty. Not much weight can be put on individual values of the distance, but it is practically certain that these values are of the right order of magnitude and can serve to give a correct idea of the distribution of galactic clusters in space. The light they throw on galactic dimensions is considered in ciph 42.

85. Radial Velocities of Globular Clusters. The measured radial velocities of globular clusters range from -350 to +315 km/sec. From Table 25 it can be seen that there is no clear dependence of velocity on class of cluster, galactic latitude, angular diameter, total magnitude, or distance from the sun. The only appreciable correlation appears to be that of speed with distance from the solar apex, pointed out by Strömberg<sup>3</sup>. The dependence is in the sense of increasing velocity with increasing distance from the solar apex.

The simplest interpretation of the relation of speed to position in the sky is based on the assumption that the apparent systematic drift of the clusters is but the reflection of the motion of the local system in the Galaxy. When corrected for this motion, the average speed of globular clusters remains high—approximately a hundred kilometers a second, but as a group, the globular clusters are essentially at rest with respect to the whole galactic system, unlike the extra-galactic nebulae, which show a large K term apparently dependent on distance

The radial velocities of globular clusters have been measured mainly by Slipher at the Lowell Observatory. Except for two or three clusters, all measures refer to the integrated images and not to individual stars. The study of differential radial motions in a globular cluster is one of our important future problems. The successful measure of the proper motions in globular clusters, also, must await the photographs of the future. VAN MAANEN has shown that the proper motion of Messier 13 as a whole and its average internal proper motion are less than 0",001 annually, an amount to be expected from a consideration of the distance and the radial velocity. The values of the annual proper motions are slightly larger for Messier 2 and Messier 56, but are consistent, he finds, with my estimated distances and the average radial velocities.

<sup>&</sup>lt;sup>1</sup> The assumption that the fifth star in the cluster is not more luminous than -0.5 implies, in general, that the star is not earlier in spectral class than B8. For a cluster of the spectral constitution and richness of the Pleiades, this assumption would therefore give too small a distance. I rungler has found that about half the clusters he has classified are of the Pleiades type, but, as pointed out in eight 14, this proportion is probably too large because of observational selection. The clusters of the Pleiades type are apparently poor in highly luminous stars of early type, for of fifteen enumerated by RAAB, not one has a fifth star of class as early as B5. The adopted method, therefore, probably does not lead to serious systematic error.

<sup>&</sup>lt;sup>9</sup> Mt Wilson Contr 292, p 5 (1925) A suggestion of a dependence of velocity (corrected for solar motion) on galactic latitude and therefore on mass of the intervening star fields is discussed by ten Bruggencate [Wash Nat Ac Proc 16, p 111 (1930)], who seeks a trace of the red-shift, characteristic of the spectra of distant spiral nebulae. The material is myet insufficient to establish the correlation securely, or to discriminate among its possible interpretations.

Mt Wilson Cont. 284 (1925)
 Mt Wilson Cont. 338 (1927)

NGC	Cl	1808 25	Spectron	Ampular	Pg. Mag.	Distance (kpc.)	Ratio
				Diameter			Velocity
1851	11	—34°,5		5′.3	6,0	14.3	+315km/sec
1904	V	<b>⊢28</b>	1 - [	3,2	8,1	20,4	+235
5024	V	+79		3.3	6,9	18,2	180
5272	VI	+77.5	[ G [	8, 9	4,5	12,2	<b>⊢130</b>
5904	v	+46	G	12.7	3.6	10,8	+ 10
6093	II	+18	Ko	3.3	6,8	17.5	+ 70
6205	ν	+40	Go	10,0	4,0	10,3	-265
6218	ΙX	+25	-	9,3	6,0	11,0	+160
6229	VΠ	+40	1 - 1	1,2	9,7	29,8	- 100
6266	ΙV	+ 7	K0	4 ,3	7,0	18,6	+ 50
6273	AIII ,	+ 9	[ G5 [	4,3	6,8	16,3	+ 30
6333	ALLI	<b>∔10</b>	K?	2 ,4	7.4	20,8	+225
6341	ΙV	<b>∔3</b> 5	G5	8,3	5,1	11,2	<b>— 160</b>
6626	ŢV	- 7	G5 [	4 .7	6,8	16,6	lo
6934	VIII	-20	Go	1 ,5	9,4	24,9	350
7078	IV '	<b>-28</b>	[ F ]	7,4	5,2	13,1	<b>–</b> 94
7089	11	<b> 36</b>	F5	8,2	5,0	13,9	- 10
7099	v	-48,5	178	5 .7	6,4	14,6	<b>— 125</b>

Table 25 Radial Velocities of Globular Clusters

86. Dimensions and Star Densities of Ciusters. It is impossible to say how many stars constitute a typical globular cluster. Our photographs can reach only a little way down the main sequence towards the dwarfs. When we attempt to go farther, the high density of the central stars "burns out" the photograph and conceals the information we might otherwise obtain. From available counts on our most suitable photographs of the brightest clusters we estimate that in the average globular cluster there are more than twenty thousand stars brighter than absolute magnitude +5. To the same magnitude limits, the population of an average galactic cluster is less than two hundred stars.

The diameter of a globular cluster is also indeterminate. It is probable that the actual linear dimensions depend on the brightness of the stars involved, becoming greater for stars of lower luminosity and mass; the same dependence appears also in galactic clusters. From Table 23, which gives the relation of distance modulus to angular diameter for normal globular clusters, we can compute the following relation of linear diameter to distance.

Distance	Modulus 18—M	Angular Disanciar	I Javerr Diameter		
10 kpc	15,0	11/,2	33 pc		
20 [	16,5	2,6	16		
30	17,4	1,4	13		
40	18,0	1,02	12		
50	18,5	0,85	12		

The measured decrease of linear diameter with increasing distance is of course mainly photographic. The loss of light in space is here of minor significance. We under-measure the angular diameters of remote clusters because of the failure of outlying faint stars to rise to measurable prominence on the photographic plate. I think we can safely take the diameter of a typical globular cluster to exceed thirty-five parsecs, but the diameter of the nucleus, in which the brightest stars are concentrated, appears to be only one third as large.

The average linear diameter of the galactic clusters for which definite estimates can be made (Appendix B) is 6,24 parsecs. Few galactic clusters

<sup>&</sup>lt;sup>1</sup> See, for example, Pop Astr 27, p 104 (1919)

See Figure 15

exceed twenty parsecs in diameter Trumpler has determined preliminary distances from observations of magnitudes and spectral types for fifty-two systems. He finds a range in linear diameter from 3,5 to 25 parsecs, with the

great majority between 4,5 and 10 parsecs

The number of stars per cubic parsec in a typical globular cluster cannot be computed at present, except for the supergrant stars. It is obvious, when the dwarfs are taken into consideration, that the distances separating stars at the center of a rich globular cluster are on a planetary rather than a stellar scale. It seems probable that sooner or later we should have evidence of stellar encounters in such crowded regions; but only one nova in a globular cluster is now on record—the seventh magnitude object in Messier 80, which appeared in 1860.

The space density and the distances separating individual stars can be more readily computed for galactic clusters when rehable estimates of the parallaxes become available, and when we have made sufficient allowance for superposed stars. Trumpler's study of one of the richest of the galactic clusters, Messier 11, provides material that illustrates the conditions in these systems. He finds that the cluster is 1250 parsecs distant. It has in the rich Scutum star cloud, which has a star density nearly four times that of the average field of the galactic belt. The cluster itself is made up of about 480 stars brighter than magnitude 15.5, distributed over an area approximately a quarter of a degree in diameter. The bright stars are concentrated within a central area of less than 4' radius.

For stars brighter than absolute magnitude +4,5 the relation of density to distance in Messier 11 is found to be as follows

Distance from Center in Parsecs	Stars per Cubic Parses	Distance from Center in Parsecs	Stars per Cubic Parsec
0,27	83	1,68	4,9
0,60	80	2,04	2,2
0,96	33	2,40	0,5
1,32	9,5		

The central density of Messiei 11 is much higher than that of the average galactic cluster. In contrast with the density of 83 stars per cubic parsec for Messiei 11 is the density for Messiei 37 of only eighteen stars per cubic parsec for stars brighter than absolute magnitude +4,5. The corresponding number for Messiei 36 in twelve (Wallenguist), for the Pleiades, 2,8 (if the parallax is taken as 0",008), and, for the vicinity of the sun, 0,011. The average separation of stars at the center of Messiei 11 is one light year.

TRUMPLER points out that "an observer at the center of Messier 11 would find about forty stars with parallaxes of 2" or more and which would appear three to fifty times as brilliant as Snius shines in our sky". It is quite probable, however, that this display would be very dull compared with the show at the center of the Hercules cluster.

# i) Star Clusters in the Magellanic Clouds.

87. Types of Clusters and Nebulae. Both globular and galactic clusters appear in the Magellanic Clouds, the latter type exhibiting much variety in richness, dimensions, and nebulosity. In the New General Catalogue and the Index Catalogues 44 clusters and nebulae are listed within the limits of the

Later revised to 1340 parsecs Lick Bull 14, p 154 (1930)
 Lick Bull 12, p 10 (1925)

Small Cloud and 301 within the Large Cloud. The descriptions, however, are meager, and photographic plates reveal scores of clusters and nebulae that have not yet been catalogued and described. For the Small Cloud a catalogue by Shapley and Miss Wilson<sup>1</sup> gives 237 new objects, chiefly nebulous stars and groups of stars. A manuscript catalogue of the star clusters in the Large Cloud, recently prepared from Harvard plates, contains 410 new entries—nearly doubling the number known from Herschel's survey and subsequent investigations. A complete catalogue and analysis of the clusters in the Magellanic Clouds, however, must await future surveys with the reflectors, since the telescopes at present available do not permit adequate resolution of the small groups.

Among the great number of nebulae in both Clouds, none has been found which could be assigned safely to the spiral class. As would be expected from their total absolute magnitudes, mainly between -3 and -7, they are for the most part of the diffuse and irregular types, with a meager sprinkling of planetaries. Of the many diffuse nobulosities in the Large Cloud the greatest is the famous "Looped Nebula", 30 Doradus. Its absolute brightness probably exceeds magnitude -13, and its total diamster, including the fainter ways and loops of nebulosity, is thirty paraecs or more.

88. The Globular Star Clusters. Dunlor, Sir John Herschel, and others have described many of the compact star groups in both Clouds as globular. The N G.C. records sixteen globular clusters in the Large Cloud and two in the Small. On the basis of photographic material Balley, Melotte, and others have remarked that few if any of these objects are correctly assigned. In fact, none of them is now retained as truly globular. On the other hand, the accepted globular clusters, listed for both Clouds in Table 26, are not described as such in the N G.C., though they all appear in that catalogue. The existence of globular systems in the Magellanic Clouds affords a valuable opportunity for the comparative study of globular and galactic types, and for the examination of the relation of globular clusters to galaxies.

The first two clusters of Table 26 belong to the Small Magallanic Cloud; the eight others to the Large Cloud. The angular diameters and integrated magnitudes are given on the same basis as in Appendix A for globular clusters in general. The diameters, therefore, are not indicators of the extreme bounds of the clusters—they are rather measures of nuclei. N.G.C 416 in the Small Cloud is more uncertain than the others and later may be dropped

It is seen that the globular clusters in the Large Cloud range from the compact Class II to the fairly open Class VIII. In earlier considerations of clusters in the Large Cloud® seven objects were listed as possibly globular. DI these N G.C. 1654 has now been definitely dropped®, and N G.C. 1835 and N.G C 1856 have been added to the list. Later analysis may show that some of the following N.G C. objects are globular clusters4.

1711	1926	2056	2133
1789	1939	2058	2134
1852	1944	2065	2157
1872	1986	2107	2164
1903	2019	2108	
1916	2031		

<sup>1</sup> Harv Circ 275, 276 (1925)

Harv Bull 775 (1922); Harv Circ 271 (1925)

It was included in Herv Bull 848, 849, and 852 as a doubtful object.
In 1932 (two years after the completion of the manuscript) a dozen new globular clusters were found in the vicinity of the Large Cloud (Herv Bull 889).

Table 26 Globular Clusters in the Magellanic Clouds

NGC	R A 1900	Dec 1900	Galactic Angular Long I at Drameter		Angulai Drimeter	Integrated Magnitudo	Class	Adopted Modulus	Quality		
416 419 Mean 1783 1806 1831 1835 1846 1856 1866 1978 Means	1 5 1,0 1 5 ,4 4 58 ,8 5 2 ,4 5 5 ,8 5 5 ,8 5 5 7,7 5 10 ,1 5 13 ,6 5 28 ,1	-72° 53′,5 -73° 25,1 -66° 8,1 -68° 8,0 -65° 3,6 -69° 32,1 -67° 35,0 -69° 15,1 -65° 34,9 -66° 18,5	262° 262 — 242 245 242 247 245 247 245 247	- 13° - 42 - 37 - 36 - 35 - 34 - 34 - 34 - 34	0',9 1,4 1,4 0,9 1,3 1,2 1,2 2,1 2,2 1,0 1,5	11,3 10,2 — 10,1 10,6 10,0 9,9 10,4 8,8 8,0 10,2 9,61 1 0,24 (m e)	VI V	18,05 17,36 17,50 17,32 17,04 17,38 17,44 17,56 16,76 16,58 17,72 17,25 17,25	c d c c d		

In none of the globular clusters of the Magellanic Clouds have variable stars been found, nor have the brighter stars been measured individually. The final test as to whether the doubtful objects are typical globular systems, or merely open groups involved in nebulosity, will be in future examinations for variable stars, and in the study of density and luminosity laws.

Miss Cannon has thrown doubt on the globular nature of a number of bright objects in both clouds by showing that their integrated spectra are of early class; we have already seen that practically all typical clusters belong to Classes F and G. Thus she finds

NGC	Spectrum •	NGC	Spectrum
294	A?	2107	A?
1872	A3	2134	A
1903	A	2157	A2
2041	A3	2164	A5

The spectrum of NGC 419, in the Small Cloud, resembles Class K in its distribution of light and in the faint appearance of the G band and of lines H and K. The spectrum of NGC 416 is too diffuse and faint to classify. The spectral class<sup>2</sup> of NGC 1866, in the Large Cloud, is F8, that of NGC 1835 is possibly G5, though for it and the other compact clusters of the Large Cloud the spectral images on the Harvard objective prism plates are too difficult for classification.

89. Distances of the Clouds. Values of the distances of the Magellanc Clouds can be based on measures of the globular clusters, but from Cepheid variable stars more accurate results are obtained, which can then be used to determine the absolute magnitudes of the clusters. In the minth column of Table 26 the distance modulus is given for each cluster, derived from the measures of angular diameter and integrated photographic magnitude. In the use of these data we follow the principles developed in an earlier section on the distances of globular clusters of the galactic system. In getting mean values of the modulus for each cloud, weights were assigned as follows.

Quality	Weight
C	4
d	2
C	1

<sup>1</sup> See Appendix A

<sup>&</sup>lt;sup>2</sup> Haty Bull 868 (1929)

While clusters of quality c may be accepted as almost certainly globular, some

doubt still attaches to those qualified as d and o

The mean modulus derived for the Small Magellanic Cloud is nearly identical with the value 17,55, proviously derived from 107 Cepheid variable stars. With the adopted revision of the zero point of the period-luminosity curves the distance modulus from the variables becomes 17,32. Accepting this value we have for the Small Magellanic Cloud.

 $\pi = 0'',0000345$ Distance = 29 kiloparsecs = 95 000 light years
Linear Diameter = 6000 light years.

At this distance the integrated absolute magnitude is -7.42 for N G C. 419, the only object that appears definitely, from the survey of existing plates, to

be a globular cluster

For the Large Magellanic Cloud the mean distance modulus from eight globular clusters is 17,25, with a mean computed error of only one tenth of a magnitude. But the Cepheid variable stars should eventually give us a much more dependable value of the modulus. The modulus derived from a recent study of the variables is 17,10. Adopting this value, we obtain the following results for the Large Magellanic Cloud.

\pi = 0",000038

Distance = 26,2 kiloparsecs
= 86000 light years
Linear Diameter = 10800 light years

The corresponding mean absolute photographic magnitude of a globular cluster in the Large Magellanic Cloud is -7.46 (weighted mean). The absolute values range from -9.1 to -6.5, an indication of the degree of uncertainty involved in assuming a constant integrated absolute magnitude for globular clusters. The spread is considerably less if the cluster N G.C 1866 is assigned to the foreground rather than to the Magellanic Cloud, and it would be very small indeed (-7.2 to -6.5) if the newly admitted N G C 1856, when analyzed with a large telescope, proved to be a nebulous open group

40 On the Relation of the Clusters to the Magellanic Clouds. The angular diameters of the globular clusters in the Large Cloud are at most two or three minutes of arc; the angular diameter of the Cloud as a whole is slightly more than seven degrees. Enormous and rich as we know a typical globular cluster to be, it is obviously small compared with ordinary external galaxies. The clusters of the various sorts, however, are important in the general appearance of the Clouds, and especially in the make-up of the high luminosity population.

The distribution of the open clusters throughout the Clouds is much the same as the distribution of the Cepheid variable stars and of the general stellar population, on the other hand, the accepted globular clusters in the Large Cloud are almost exclusively to the north, and N.G.C. 1866 and N.G.C. 1831 lie quite outside the main structure of the Cloud. There are, however, a half dozen variable stars, apparently of the Cepheid class, in the same region as these clusters, and long exposures on short scale plates show that the outlying clusters and variables are within the observable bounds of the Cloud.

<sup>&</sup>lt;sup>1</sup> SHAPLEY, YAMAMOTO, and WILSON, Harv Circ 280 (1925), see also SHAPLEY, Herv Circ 255 (1924)

See ciph. 30. SHAPLEY, Harv Circ 268 (1924).

The asymmetrical distribution of the globular clusters in the Large Cloud has led some to surmise that the globular clusters of the galactic system may also be eccentrically arranged with respect to the general galactic structure, and therefore that they cannot be used as I have used them, in estimating minimum values of galactic dimensions. But this one-sided distribution of the globular clusters in the Large Cloud is modified by the inclusion of N G C 1835 and N G C 1856 in the list accepted at present, and it would be quite altered if a considerable proportion of the list of suspected globular clusters prove to be typical systems. The two clusters N G C 1789 and N G C 1944, both of which are strongly suspected as globular, he far from the center of the Cloud on the south—directly across from the outlying globular clusters of Table 26

It is of significance that the 1400 known variable stars in the Large Cloud and the 969 in the Small Cloud<sup>1</sup> avoid the numerous open clusters. In this respect the Clouds are like the galactic system, where open clusters are free of variable stars of all kinds. The globular systems in the Magellanic Clouds, are, of course,

too compact to have been scarched as yet for variables

Possibly the most striking fact arising from the study of globular clusters in the Magellanic Clouds is the low absolute magnitude of their brightest stars when compared with the brightest objects in the open and nebulous groups. If the new values of the distance moduli are correct, there is scarcely a star in the ten accepted globular systems of the two Clouds that exceeds —3 in absolute photographic magnitude. This result, however, is in complete agreement with the condition found in globular clusters of our own galactic system. In contrast, the individual stars in scores of the nebulous star groups in the Magellanic Clouds appear to exceed —3 in absolute photographic magnitude, and in many groups they attain the excessively high luminosities of —5 and —6. This again is in agreement with the data on absolute magnitudes in galactic clusters, especially in those large early spectrum groups in Orion, Scorpio, and elsewhere that are associated with bright nebulosity.

It may be remarked in conclusion that, notwithstanding their remoteness, isolation, and high galactic latitudes, the Magellanic Clouds may be more closely allied to our galactic system than we have heretofore supposed. It is probable that the observed high speed recession of the Clouds should be assigned almost wholly to the motion of our local system in the Galaxy. Apparently the Clouds are not in rapid motion with respect to the sum total of the galactic system, or

the system of globular clusters

### j) Dimensions of the Galaxy.

41. Membership in the Galaxy Our galactic system, as here defined, is composed of the aggregate of stars and nebulae whose distribution appears to be organized with respect to the galactic plane. Globular clusters are therefore included, with galactic stars and galactic clusters and nebulae, but the Magellanic Clouds and the extra-galactic nebulae (spiral nebula family) are outside the organization.

A final judgment, however, of galactic membership must await more information on speeds and masses, and on the phenomena of galactic rotation. Possibly some of the remote globular clusters (e.g. N.G.C. 7006, N.G.C. 4147, and Messier 75) are actually independent, being either fugitives from the Galaxy,

<sup>2</sup> Harv Rept 61 (1929)

<sup>&</sup>lt;sup>1</sup> LEAVITT, Harv Ann 60, No 4 (1908) Approximately 600 new variables have been found on Harvard plates of the Largo Cloud since 1930 (as yet unpublished)

or only chancing for the moment (cosmically speaking) to be moving in this part of space. On the other hand, the Magollanic Clouds may sometime be shown to be affiliated with our Galaxy, or, at least, with a local group of galaxies including the three Andromeda nebulae, Messier 33, and some others<sup>1</sup>.

In measuring the Galaxy we should at the start admit indefinite limits, and also striking irregularities, not only in the interior but probably also at the edges. The dimensions discussed below are therefore not to be taken too literally as marking the boundaries, or even as giving sharp limits of star density. At best we measure or estimate the distances of the remotest attainable stars, or groups of stars, which yield to present methods and which appear to be members of the galactic system.

- 42. The System of Galactic Clusters. Although the loose star groups contribute little to our knowledge of the dimensions of the Galaxy, their space distribution may be mentioned here as bearing on the structure of the nearer parts of the Milky Way. The catalogue of 249 galactic clusters in Appendix B contains galactic longitude, approximate distance, and R  $\sin \beta$  (distance from the galactic plane). Some features to be noted in the distribution of the galactic clusters are:
- 1 The contrast in galactic distribution of galactic and globular clusters (see Figure 6).
- 2. Close confinement of galactic clusters to the neighborhood of the galactic plane
- 3 The relative nearness of galactic clusters to the sun, which results in a distribution essentially free from effects of the obstructing clouds that contribute much to the anomalous distribution of the globular clusters. The galactic clusters are in large part members of our local system and the circumjacent star clouds.
- 48. The Higher Systems of Globular Clusters. To illustrate the space distribution of the ninety-three known globular clusters of the galactic system (Appendix A), the following rectangular coordinates have been computed for all

$$X = R \cos(\lambda - 327^{\circ}) \cos \beta,$$
  

$$Y = R \sin(\lambda - 327^{\circ}) \cos \beta,$$
  

$$Z = R \sin \beta,$$

where R is the distance in kiloparsecs,  $\beta$  is the galactic latitude, and  $(\lambda - 327^\circ)$  is the galactic longitude measured from the direction of the center of the cluster system. The latitude, longitude, distance, and  $R\sin\beta$  are given in Appendix A; the computed quantities X and Y are given in Table 27

a) Eccentric Position of the Solar System A diagram of the distribution of the globular clusters in the plane of the Galaxy (XY plane) is shown in Figure 19. Crosses indicate clusters lying on the north of the galactic plane, and dots those on the south; the smaller the symbol, the more distant is the object from the plane. The equality of the division by the galactic plane of the supersystem of clusters is remarkable—forty-seven clusters are on the north, forty-six on the south.

The direction to the center of the system, derived from the apparent positions of globular clusters, is seen to agree with the direction on the basis of space coordinates; in Figure 19 there are forty-six positive values of Y and forty-six negative values, with Y = 0 for one cluster. (The remote system N.G.C. 7006.

<sup>&</sup>lt;sup>1</sup> Shapley, Harv Repr 51 (1929).

Table 27 Cooldinates of Globular Clusters

	lable 2	7 Coordinate	s of Globu	lai Clusters	
NGC	R cos f × co-(1-327°)	R cos ft ≮ san (1−327°)	NGC	R cos // × cos (1 ~ 32/°)	R cos β Δ Siii (λ 327°)
104	+ 2.8	- 3,9	658‡	£18,6	- 5,0
288	- 0,5	~ 0,1	6024	- 21,7	1,2
362	+ 4,5	- 7,5	6626	16,3	1 2,3
1261	0	-13,7	6637	4 18,4	1 106
1851	- 5.0	-10,6	6638	<b>⊢29,0</b>	1 1,3
1904	-12,3	13,2	6205	4,0	1 6,8
2298	-10,4	-23,4	6218	4 9,5	2.9
2419	-28,0	- 0,5	6229	- 6,7	) -21 h
2808	+ 3,0	15,6	υ235	<b>⊢28,</b> 0	0
3201	+ 1,1	9,0	6254	F-10,0	2,9
4147	- 0,9	- 4,5	6266	- 18,3	1,6
4372	+ 5,0	- 8,0	6273	-  16,0	0,7
4590	+ 6,7	10,7	6281	F27,6	0,5
4833	+ 8,8	-13,0	6287	1 27,1	1 0,5
5021	十 3,2	<b> 1,3</b>	0293	22,8	- 0,8
5053	+ 3.5	- 1,0	0304	-  25,0	1,8
5139	+ 1,2	- 5,0	6316	31,5	- 0.8
5272	- 4 2,0	+ 1,7	6325	1 46,0	0,1
5286	<b>+16,0</b>	- 17,0	6333	20,3	2,1
5466	+ 3,8	+ 3,1	63   1	1 3.3	1 8,6
5634	- 19,8	5,8	6342	1 39,1	1 51
I 4499	+14,0	-18,0	6352	1 18.4	(5,0)
5824	- 1 24,4	-11,9	6356	+ 48,5	-1 6,0
5897	+15,0	4,0	6362	+12,0	8,0
5904	+ 7.4	+ 0,6	6366	26.3	1 9,1
5927	+16.8	J — H <sub>2</sub> 0	6388	1 16.6	4,2
5946	+27,2	17,0	6397	<b>1 5.1</b>	- 2,1
5986	4 15,4	- 6,2	6402	+ 17,7	1- 7,2
6093	+ 16,5	- 1,9	6652	1-23.0	1 0,6
6101	f-14,7	<b>−13,5</b>	6656	- 6,3	- 1,2
6121	+ 6,9	- 1,0	6681	+18.7	1 1.0
6139	+27.7	- 8,5	6712	23,2	1 11,6
6144	+ 17.3	2,4	6715	118,6	0,2
6171	+ 19,4	+ 1,7	6723	+11.7	3,0
6426	+31,3	+17,4	6752	+ 6,7	1 16.8
6440	+49.5	F 7,0	6760	23.1	17.8
6441	+21,0	- 0,2	6779	- 9,1  - 2,0	1,2
6453	+50,0	- 0,4	6809	+ 7.9	14.8
6496 6517	+21,2 +470	4,5	6864 6934	-F40,7	18.7
6522	-} 35,8	+17,1	6981	-[-15,6	1114
6528	44,0	+ 0,6 + 1,2	7006	4-22,4	1 48,0
6535	+23,0		7078		10,6
6539	+35.8	十12,3 十13,8	7089	-1 4,7  - 6,6	9,2
6541	4 8'6	- 1,5	7099	+ 8,6	4,6
6553	+ 26,6	+ 2,6	7492	-1 6,4	+ 9,1
6569	-29,1	+ 0,5	1774	1 1 11	1 3 20
0,007	1 ~//-	1 12	3	1	1

with coordinates X = +22,4, Y = +48,0, falls outside the limits of the diagram)

The origin of coordinates for Figure 19 — that is, the position of the observer — is on the border of the globular cluster system. The center of gravity of the system of clusters, indicated by an open square, has the coordinates X = +16.4, Y = -0.3 (or Y = +0.2 if the remote and isolated NGC 7006 is included)

Probably ten or twenty globular clusters, within the limits of space represented by the diagram, await discovery. Obscuring nebulosity possibly conceals most of these systems, of which the existence is intimated by the scarcity of

observed points in the right half of Figure 19. Of course we need not assume high regularity in distribution, or even approximate circularity in the projected array, but it is probably the observational difficulties caused by nebulosity and by the small dimensions and faunt magnitudes of remote clusters, and not

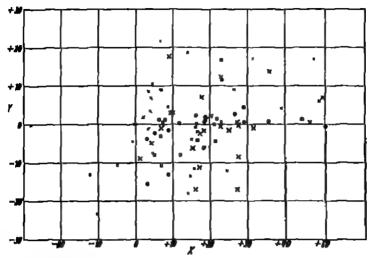
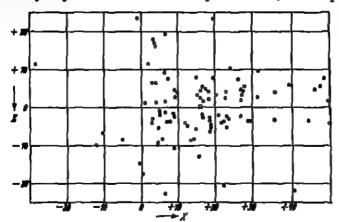


Fig 19 Distribution of globular clusters in the plane of the Galaxy The sun is at the origin of coordinates.

inherent irregularities, that have produced the apparent deficiency for X greater than +30 kiloparsecs. On the left side of the diagram, from X = 0 to X = -20, where the survey may be considered sufficiently exhaustive, the complete absence



Mg 20 Distribution of globular clusters in the XZ plane,

of chaters from one quadrant is even more striking and significant structurally than the scarcity of values of X greater than +30.

The cluster at the extreme left is N G.C. 2419—an object in a region far from other clusters, found through studies of the Lowell Observatory photographs<sup>1</sup>.

<sup>1</sup> Hary Bull 776 (1922)

b) The "Region of Avoidance" The same asymmetrical position of the sun with respect to the supersystem of globular clusters is shown in Figure 20, where all ninety-three systems are plotted on the XZ plane. The center of gravity, that is, the algebraic mean values of X and Z, indicated by an open square, is at  $X=\pm 16.4$ ,  $Z=\pm 0.4$  NGC 2419 again stands out on the extreme left.

The most interesting feature of Figure 20, which represents a section perpendicular to the galactic plane, is the "region of avoidance". The scarcity of globular clusters in low galactic latitudes is again in evidence. Here is a central section 2,5 kilopaisecs (8000 light years) in diameter, in which no globular cluster has been found. On the other hand there is only one galactic cluster out of the

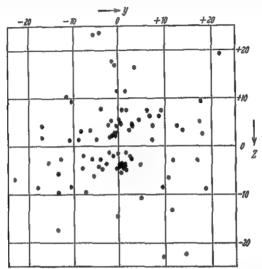


Fig 21 Distribution of globular clusters in the YZ plane

249 listed in Appendix B that does not fall well within this mid-galactic segment and that cluster, N G C 2243, is of doubtful nature and uncertain distance Practically all known galactic stars and nebulae also fall within this "region of avoidance"

- c) Projection on the YZ Plane. Figure 24 shows the distribution of globular clusters projected on the YZ plane, which is perpendicular to the line joining the sun and the center of the system at galactic longitude 327°, galactic latitude 0°. The "region of avoidance" is again clearly shown, and also the essential symmetry of the globular cluster system, for the numbers of clusters in the four quadrants are 23, 24, 22, and 24 Again N G C 7006 is outside the diagram, with coordinates  $Y=+48.0,\ Z=-20.4$
- 44. The Distance to the Galactic Center. It appears to be a tenable hypothesis that the supersystem of globular clusters is coextensive with the Galaxy itself. Researches on variable stars in the Milky Way¹ will eventually afford an instructive check on this hypothesis. Until we have such direct measures we can only assume that the galactic system is at least as large as the system of globular clusters. We have shown rather convincingly that the globular clusters are galactic members or associates.

<sup>1</sup> SHAPLRY, Harv Repr 51 (1928)

The algebraic mean of the values of  $R\cos{(2-327^\circ)}\cos{\beta}$  gives a preliminary indication of the distance to the center of the cluster system, and provisionally, therefore, of the distance to the center of the Galaxy. In so far as it depends on the globular clusters now known, the uncertainty of the distance does not exceed ten per cent. Further research on faint globular clusters, especially if now ones be found, will be more likely to extend the system than to reduce it; on the other hand, the distances of the more remote clusters are the least certainly determined and must be given low weight. We shall adopt as the distance to the center

 $R_g = 16 \text{ kiloparsecs}$ = 52000 light years

The galactic star clusters and the ordinary individual stars are too near the sun to contribute effectively to the determination of the distance to the center. But the direction to the center, as is well known, is confirmed by the counts of funt stars, and through the recent studies of galactic rotation by Lindrich, Oort, J. S. Plaskett, Schilt, and others; it is shown, though less definitely, by the distribution of Milky Way star clouds, planetary nebulae, Class O stars, and other objects of high luminosity. Practically all types of stars, however, with the possible exception of the novae and Copheid variables, are too faint absolutely and too infrequent in number to contribute to the current surveys of galactic regions that are near or beyond the center of the cluster system.

Studies of the cluster type Cephoids and the long period variable stars in the southern Milky Way have led the writer and Miss Swope to a value of the distance of the centrally located star clouds that is very much like the value given above. The variable star investigations of several observers at Harvard tend to support this suggestion that the heavy star clouds in Ophiuchus, Sagittarius, Scorpio, and neighboring constellations are parts of a massive stellar nucleus of the galactic system. The distribution of the cluster type Cepheids in these regions suggests that the nucleus extends perhaps half way from the center toward the sun. The speed of rotation about this nucleus is approximately 300 kilometers a second at the sun's distance from the center

One important feature of the galactic central region is that the center itself lies behind heavily obscuring nebulosity. The dark clouds at the center are apparently but a part of those causing the rift in the Milky Way that extends from Cygnus southward to Centaurus; they seem to be largely responsible for the apparent avoidance of the mid-galactic regions by globular clusters.

45. On the Size and Structure of the Galaxy. An inspection of Figures 19 and 20 gives only a rough idea of the total diameter of the flattened galactic system. The most remote globular clusters are the following:

N.G.C.	Distance kps	м.д.с.	Distance kps
6325 6342 6356 6440 6453	46 40 50. 50: 50	6517 652 <b>8</b> 6864 7006	50 44,4 48,5 56,8

NORT, Recharchee Ast Obs Utrecht 8, p. 113 (1917); SEARES, Mt Wilson Contr 347 (1927).
 SHAPLEY, Harv Repr. 52 (1928)

Some of these values are uncertain, the distances may be greater or less, but the superior distance of NGC 7006, a cluster in Vulpecula with  $R=56.8~\rm kpc$  = 185000 light years, seems to be well attested by observations on its individual stars and on its cluster type Cepheids<sup>1</sup>

The greatest distance separating two of the clusters is

NGC 7006 - NGC 2298 = 80 kilopai secs

Several other clusters are nearly as widely separated, N G C 2208 in Puppis is 71,3 kiloparsecs from N G C 6517 across the sky in Ophiuchus, and N G C 2419 in Lynx is 79 kiloparsecs from N G C 6453 in Scorpio. We may take such distances to indicate the extreme dimensions of the galactic system, for certainly most of these globular clusters, if not all, are integral parts of the Galaxy.

It does not follow from the wide dispersion of globular clusters that individual stars of the Galaxy are so widely dispersed, but it appears reasonable to maintain that the greatest diameter of the Galaxy in its plane is not less than seventy thousand parsecs, and it may be thirty per cent larger. The thickness of the system varies with distance from its center, being perhaps ten to fifteen thousand parsecs at the galactic nucleus, and one-half as much out where the solar system is located. Occasional isolated stars, however, and, of course, the globular clusters extend to twenty thousand parsecs and more from the galactic plane, lying well outside the relatively thin mid-galactic stratum.

The most remote individual stars known in the Galaxy are the novae and a few long period Cepheid variables, of faint apparent magnitude, studied by Gerasimovič, Miss Swope, Miss Harwood, and others, on Harvard and Nanticket plates. Some of these appear to be well beyond the galactic nucleus, with distances comparable with those of the remoter globular clusters and the Magellanic Clouds. Since progress is rapid in the discovery and study of faint variables, it will be advisable to postpone the discussion of the part they play in the measurement of the extent and orientation of the galactic system. It may be twenty years or more before the detailed picture of the structure of the galactic star clouds can be drawn.

It is of significance, however, to compare the picture of the Galaxy that grew out of the carlier work on clusters and the local star system<sup>2</sup> with that resulting from the more recent studies of galactic structure<sup>3</sup>. The earlier view vizualized the Galaxy as a unified discoidal stellar system, evolved from amalgamating star clouds and clusters. The local cloud was mapped out and described as one of the minor elements. The Galaxy was considered, not a single spiral nebula, but rather an organization of many half-digested star clouds and clusters, moving in an extensive stratum of stars and galactic nebulae.

It was suggested that the obvious dynamical equilibrium of a globular cluster, acquired originally at a great distance from external perturbing matter, results in a delicate adjustment that readily breaks down under stresses such as those prevailing in a large galactic system, further, that faint stars in a globular cluster, as in the galactic system, are of small mass and therefore of more than average velocity, so that in their motions in the cluster they frequently attain great distances from the center. When such globular systems approach or mingle with other clusters or the dense stellar fields in the mid-galactic segment, the dwarfs will preferentially become scattered through encounters. The massive

Mt Wilson Contr 157, Sect 7 (1918)

Harv Circ 350 (1930)

<sup>1</sup> Shapley and Mayberry, Mt Wilson Comm 74 (1921)

cluster stars, which are mostly of high luminosity, and which are concentrated to the center and endowed with low peculiar velocities, will retain their cluster organization longer in a disrupting neighborhood. A globular cluster thus becomes a galactic cluster which slowly dissolves into the galactic field. Flattening and distortion of galactic clusters and star clouds arise through the "encounter machinery" discussed by Jeans, and through rotation. Star streaming appears to be a complication of the various motions in and of the local system and general galactic field

The galactic system, it appears on this interpretation, is in an advanced stage of the survival of the most massive. In size the spiral nebulae are not comparable to it, ours is a Continent Universe if the average spirals are considered Island Universes

The relation of galactic and globular star clusters to each other, and their relation to star clouds and galactic systems, remains obscure in many respects. Yet the recent study of these structures brings increasing evidence that the above interpretation should be extended. Its modification is necessitated, in part, by difficulties such as the scarcity of clusters intorinediate between globular and galactic groups, and the slowness or even unpossibility of the amalgamation of clusters and star clouds with no more potent a resisting medium available than the galactic star field with its infrequent encounters. In view of these obstacles, and others related to the distribution of dark nobulosities and the anomalous position of the Galaxy among other systems, the amended hypothesis is advanced that our galactic system is neither a spiral, such as the Andromeda Nebula, nor a single unified discoidal star system, like a Magellanic Cloud on a grand scale. It is rather a super-galaxy—a flattened system of typical galaxies It is comparable, in mass and population, with the Coma-Virgo cloud of bright galaxies, rather than with one of its members. Within the galactic system are fairly distinct galaxies, such as the local system, the Scutum star cloud, and the great star fields in Sagittarius. The dark nebulosities are associated with the local system

Galactic star clusters, from the new point of view, are not evolved from globular systems. They are probably the results of a quite different developmental process. The test of the amended hypothesis has in future studies of star distribution and motions, faint variable stars, and the accurate determination of the space distribution and affiliations of galactic clusters.

## Appendix A. Catalogue of Globular Clusters.

The material on which is based the catalogue of globular clusters has been described in the text. For three clusters, N G C. 4372, N G.C. 6356, and N G.C. 6864, special notes appear at the end of the catalogue. Daggers after the N.G.C numbers in the first column indicate questionable objects (ciph. 4). Galactic coordinates are on the Harvard system (Pole 12<sup>h</sup> 40<sup>m</sup>, +28<sup>b</sup>). The values of the ellipticity and orientation are described in ciph. 22. Colons in the orientation column indicate less certain values, and asteriaks mark those derived from star counts on Mount Wilson plates. The magnitudes and diameters are explained in part h), and there and in part j) are described the derivation of the distances listed in the last three columns of the catalogue.

<sup>&</sup>lt;sup>1</sup> Harv Circ 350 (1930)
<sup>8</sup> See Addendum on p. 773.

Cf. footnote on N G C 4147 on page 741

Catalogue of Appendix A Integrat Galactic No of Succ Angidu Class ed Magni Dec 1900 Variables NGC Name RA 1900 trum Diameter I at tude Long 7 ш (75 272° -45° 23' -72°38′ 3 47 Tuc 0h 19m,6 104  $\mathbf{x}$ 2 --88 10,0 7,2 ,8 --27 8 157 0 47 288 Ш (15 14 268 -475,3 6,0 -71362 4 62 0 58 ,9 23 (; II 8,5 ,5 -5536 237 -51.52,0 9 1261 3 3  $\Pi$ ,8 -34.5 5.3 6,0 ₫ 508 5 -400 212 10 1851 V 5 -28 3,2 8,1 -24194 M79 5 20 1, 37 1904 VΙ 213 --15 1,8 10,1 2298 6 45 ,4 -3554 VII +23 +39 6 148 1.7 11.0 ,4 2419 7 31 K() ,0 6,3 I ---64 249 -11 5.7 9 10 27 2808  $\mathbf{x}$ 61 + 9 54 244 7.7 7,4 ,5 -453201 445 10 13 IX A7 5 б 226 十79 1.7 10.3 ,0 +19 4147 12 5 IIX7 269 -- 10 12,0 7,8 12 ,1 -724372n 20 28 +36 7,6 X ,2 269 2,9 M68 34 -26 12 4590 12 5 VIII - 8,5 4,7 6,8 52 ,7 -70 20271 4833 12 40 v M53 8 ,0 +18 42 305 十79 3.3 6.9 5024 13 十78 9 ,5 3,5 10,5 ΧI +18 13 309.5 5053 13 11 132 +15 3  $_{
m IIIV}$ ω Cen ,8 -4623 5139 13 20 47 277 VΙ ( T 160 37 ,6 +28十77.5 9,8 4,5 5272 M3 13 53 8 Go 8,5 V 0 5286 J 388 39 ,9 -5052 280 +10 1.6 13 8 5,0 XII 11 0 十72.5 10,0 5466 14 1 ,0|+29IV 310,5 +48,5 10,4 5634 ,4 - 5 32 1,3 14 24 Хľ -8149 -203,1 11,5 I4499 \_ 14 45 ,0 275 1:8 ,8 -3240301 +21 1,0 9,3 I 5824 14 57 - 29 XI 7,3 5897 15 11 .7 -- 20 39 312 7.3 V 84 + 2 +16 (r M5 12,7 3,6 5904 15 13 ,5 27 332 VIII 3,0 5927 15 20 ,8 -50 19294 + 4 8,8 M 40 28 295.5 + 3.5 IX 59461 15 ,2 -5019 1,3 10,6 VII 1.8 1 .1552 ,5 39 十12 3.7 5986 15 -3727 305 7,0 II Κo 4 6093 M80+18 6,8 16 11 ,1 -- 22 44 320.5 3,3 X 6101 16 14 ,4 -7158 284,5 -163,8 9,5 M4 ,5 IX 16 33 6121 16 17 -2617 319 十15 14,0 5,2 TI 16 -389,8 6139 21 ,0 36 310 + 6 1,3 ,1  $\mathbf{x}$ 16 21 6144 -2549 319 +15 3,3 10,3 ,9 6171 16 26 -1250 332 +22 2,2 8,9 X M113 V Go 7 16 38 10,0 6205 ,1 +36 39 27 +40 4,0 6218 M<sub>12</sub> 16 42 IX ,0 -146 344 十25 9,3 6,0 VII 6229 16 44 ,2 +47 42 40 +40 1,2 9.7 -1 6235 ,4 X 16 47 -220 327 +12 1,9 10,8 -M10 VII 6254 - 3 16 51 ,9 57 343 +22 8,2 5.4 -6266 M62 54 ,9 IV Kυ 26 16 -2958 322 + 7 4,3 7,0 M19 G5 6273 16 56 ,4 ~-26 7 324,5 + 9 4,3 6,8 VIII 6284 58 10 16 ,4 -2437 326 + 9 1,5 10.0 1X 6287 16 59 --22 +10 , 1 34 328 1,7 10.4 VII C+5 6293 3 -17 4 ,0 -26 26 325 7 1,9 8,8 ſΛ + 8 6304 \_ 17 ,2 -2920 323 + 5 1,6 9,2 VI Ţζ 6316 10 ,3 -28 G<sub>5</sub> -17 325,5 + 5 1,1 9,9 III 6325 11 ,9 17 -2338 327.5 + 6 0,7 IV 11,9 M o ,3 6333 17 13 -1825 333 +10 2,4 VIII 165 7,4 1192 6341 17 14 ,1 +43 15 36 +358,3 5,1 IV G5 14 6342 15 17 ,3 -1929 333 + 8 0,5 IV 11,4 63521 ---17 17 .5 -4822 309 --- 8 2,5 ΧI 7.9 ,8 6356 17 17 **-17** 43 334 + 9 1,7 8.6 II  $K_0$ 1 225 6362 17 21 .5 -6658 293 --- 18 6,7 X 7,1 17 6366 22 17 ,4 -- 4 59 346 4 XI +15 12,1 6388 29 17 ,0 -44 40313 — 8 3,4 7,1 III ĸ ---M14 6402 32 17 ,4 ~ 3 11 349 +14 3,0 7,4  $\mathbf{v}$ 6397 4 366 17 32 .7 -5337 304,5 -- 12,5 19,0 IX G? 4,7 2 6426 39 17 .9 + 3 13 356 十15 1,3 IX 12,2 6440 ,0 17 43 -20+ 2 0,7 20 335 11,4 ٧ 6441 17 43 6,5 ,4 -37 321 2,3 8,4 III Jζo 6453 17 44 .7 -34 36 322,5 5,5 0,7 IV 11,2

Globular Clusters

GIODE			P	e otom rephile	Negatind		Adopted	Quality	Distance	Reinß	R cos f
NGC	RHIpt	Orient.	Var	Bright	64h	30th	Modulus		kps	lipo	princ
104		—55°		13,09	12,4	13,4	14.17	b	6,8	<b>- 4,8</b>	4,8
288	9	- 1	1	14,80	14,5	15,1	15,81	b	14,5	-14.5	0,5 8,8
362	8	+65	15.5	14,12	13.5	14,8	15,55 16,72	Ъ	12,9	- 9.4 -17.2	13.7
1261   1851	9.5	-75	_	_ 1	_		15,78	G	14,3	- 8,1	11.7
1904	9	+35	_	15,29	15,01	15,72	16,54	Ъ	20,4	- 9.6	18,0
2298	ã	+39:		-	-	_	17,12	d	26.5	- 6,9	25,6
2419	9	-56	-	-			17,41	d	30,3	+11.9	28,0
2808	8	+84		14.9	14,3	15,4	16,05 14,81	b	16,3 9,2	- 3,1 + 1,4	16,0 9,1
3201	9		14,52 16,8	13,52 16,58	13.3 16,23	13,8 16,93	16,93	ь	24,2	+23.7	4,6
4147 4372	9	<u> </u>	10,0	10,30			14,91	0	9,6	- 1.7	9,5
4590	ó	- I	15,90	14,80	14,31	15,08	15,95		15,5	+ 9,1	12.0
4833	8	-80	-	-	-	144	16,01	- 6	15,9	- 2,2	15,7
5024	9	<b>-79</b> *		15,07	14.94	15,26	16,30	B.	18,2	+17.9	3,5 3,6
5053	8	-61	16,19	15,65	15,1	16,0 13,1	16,20	a. b	17,3 6,8	+17.0	6,6
5139	8	+30 +54	14.37 15,50	12,91	12,6 13,92	14,45	15,43	6	12,2	+11.9	2,6
5272 5286	9,5	T37	13,30	- 14,23	- 3,32	- 1713	16,89	ä	23,9	+ 42	23.5
5460	آو ا	-	16,17	15.72	15,1	16,2	16,16	b	17,0	+16.2	5,1
5634	9	-		-	_	_	17,49	C	31,4	+23.2	20,5
I4499	9	-	_	-	_	-	16,91	9	24,1	- 8,2 +10,4	22,7
5824	_	1 =		12.41	44.0	15,4	17,32	o b	29,1 16,4	+ 8,0	15.5
5897	8	-44' +16	15,26	15,15	14,9 13,74	14,27	15,17		10,8	+ 7.8	7.5
5904 5927	9	T10	13,20	13197	- 13,77	-	16,56	ā	20,5	+ 1,4	20.1
59461		_	_	_	_	-	17.54	d	32,2	+ 2,0	32,1
5986	_	-	_	- 1	_	_	16,14	G	16,9	-j- 3.5	16.6
6093	10	_	_ '	14,88	14,72	15.09	16,22	a.	17.5	+ 5.4	16,6
6101	8	+35	44.00	42.00	13,3	14,4	16,60	b	20,8	- 5.7 + 1.9	7,0
6121	9	+72* -64	14,27	13,88	1313	17/17	17,34	ď	29.3	3.1	29,1
6139 6144	8	-22:	_	15,76	15,2	16.3	16,29	b	18,1	+ 4.8	17.5
6171	9		_	15,46	15,2	15.9	16,63	Ъ	21,2	+ 7.9	19,6
6205	9,5	<b>−63</b> *	15,20	13.75	13.45	13,92	15,07	8,	10,3	+ 6,6	7.9
6218	<b>-</b>	-	-	13,97	13,56	14,31	15,21	b	11,0 20,8	+ 4.6	2,8
6229	-	+89	-	16,18	15,90	16,37	17,37 17,28	"	28,6	1- 5.9	28.0
6235 6254	8	7.07	I =	16,17	13.35	14,38	15.26	b	11,2	+ 42	10,4
6266	ã	+16	16,40	15,87	15,6	16,1	16,35	C	18,6	1 2.3	18,4
6273	6	-28	_		_	-	16,06		16,3	+ 2,6	16,1
G284	10	-	-	-	-	-	17,24	o d	28,0	1 1 11	27.7
6287	9	_	-	_	=		17,24	6	28,0 23,1	+ 4.9	
6293	9,5	=	1 =	_	=	_	17,02	٥	25.3	+ 22	
6304 6316	913	_	_	_	_	-	17,52	d	31,8	+ 2,8	
6325	1 -	_	_	<b>–</b>		-	18,3	0	461	1 4,8	
6333	9	_	_	15,61	16,76	15,08	16,61	b	20,8	+ 3,6	
6341	8	+16	1 -	13,86	13,60	14,16		b	11,2	+ 6,4	
6342		_		-	-	=	18,0: 16,48	0 d	19,7	T 3,0	
6352 6356		-14	_	17,16	16,86	17,44	18,51	0	50.	+ 7,8	
6362		十 <del>78</del>		''''		"-"	15,90	d	15,1	- 4.7	14,4
6366		, , , s	] -	-			17,34	8	29	+ 7.5	
6388	9,5			-	1		16,20		17.3	- 2,4	
6402		+76		15,44	14,85	15,86		8.	19,7 5,6		
6397	1 2	+73	~	12,61	11,9	13,1	13,76		37.1	+ 9.6	
6420		+10	<b>↓</b> = .	=	=	=	18,5		50	+ 1.7	
6440 6441		+40		_	l –	-	16,62		21,1	- 2,2	21,0
6453		'-"	_	-	-	-	18,5:	0	50	- 4,8	\$ 50

Catalogue of Globular

NGC	Name	RA 1900	Dec 1900	Gal-	retic Lat	Angulai Diameter	Integra ted Mag nitude	Class	Spec trum	No of Variables
							mende			
6496	_	17h 51m,8	-44° 14'	315°	-10°,5	2',2	9,7	$\Pi X$	_	
6517		17 56 ,4		347	+ 6	0,4	12,1	IV		
6522	l –	17 57 ,2		328	<b></b> 5	0,7	11,0	V1		
6528	_	17 58 ,4		328,5	5	0.5	11.8	V		
6535†	_	17 58 .7	<b>→ 0 18</b>	355	4 9 .5	1,3	11,9	Xl	-	
6539†		17 59 ,4		348	+ 5	1,3	12,6	X		1
6541	J 473	18 0 ,8	-43 44	317	-12	6,3	5,8	III	(,	l l
6553	_	18 3 ,2	-25 56	332,5	- 5	1,7	10,0	XI	9-11	0
6569	_	18 7 ,2	-31 51	328	ا5, 7	1,4	10,2	VIII	***	
6584	₫ 376	18 10 ,6	-52 15	309,5	-17	2,5	8,3	VIII	-	0
6624	-	18 17 ,3	-30 24	330	10	2,0	8,6	VI	Mo	-
6626	M28	18 18 ,4	-24 55	335	- 7	4,7	6,8	1V	(15	9
6637	M69	18 24 18		329	-11	2,8	7,5	V	1/2	
6638	! —	18 24 ,8	-25 34	335,5	7 ,5	1,4	9,2	VI	p.n	
6652	•	18 29 ,2	-33 4	328,5	-13	1,7	8,7	VI	IN 5	-
6656	M22	18 30 ,3	-24 0	337	- 9	17,3	3,6	VII	***	21
6681	M70	18 36 ,7	-32 23	330	i3 ,5	2.5	7.5	V	<b>←</b>	B==0
6712	l –	18 47 ,6	8 50	353,5	- 6	2,1	9,9	IX		1
6715	M54	18 48 ,7	-30 36	333	-15	2,1	7,1	III	I.8	-
6723	J 573	18 52 ,8		328	19	5,8	6,0	VII	(,5?	17
6752	리 295	19 2 ,0	-60 8	303	-26.5	13,3	4,6	VI	60	i
6760	_	19 6 ,1		3	5	1,9	10,9	IX		-
6779	M56	19 12 ,7		30	+ 8	1,8	8,8	X.	~	1
6809	M55	19 33 ,7		336	-25	10,0	4,4	XI	-	2
6864n	M75	20 0 ,2		347	-27	1,9	8,6	I	GO	11
6934		20 29 ,3		20	-20	1,5	9,4	VIII	60	
6981	M72	20 48 ,0		د	-34	2,0	8,6	1X		29
7006	35.4	20 56 ,8		32	-21	1,1	11.8	I	len.	11
7078	M15	21 25 ,2		33	-28	7,4	5,2	IV.	ŀ	74
7089	M 2	21 28 3		21	36	8,2	5,0	II	1.5	10
7099	V130	21 34 ,7		355	-48,5	5 ,7	6,4	v	1/8	
7492	****	23 3 ,1	-16 10	22	<b>-</b> 64	3 ,3	10,8	XII	-	3 9

Notes to Appendix A

NGC 4372 The distance depends only on the diameter measure. The cluster appears to be partially obscured by one of the streamers from the Coal Sack nebula. A special investigation of the magnitudes is being made on Harvard plates.

NGC 6356, 6864 The distance depends only on the magnitudes of the hight stars, since the integrated brightness and diameter appear to be abnormally large. There may be obscuring nebulosity in the field of NGC 6356

Clusters. (Continued.)

N.G.C.	Hillpt	Orlent	r	للرجيهمامة	o Magaliu	do	Adopted	Quality	Distance	R stb.∦	R cost
		OILL.	Ver	Bright	64	30lh	Modning	Quanty	kpc	kpe	lipo
6496	_	_	_	_	-	_	16,90	d	24.0	- 4,0	21,6
6517	8	4°:	_	_	~	_	18,5	0	50	+ 5,2	50
6522	-	-	_		~		17.78	0	36,0	- 3,2	35,8
6528	_	-	_	-		_	18,24	0	44,4	- 3.9	44,1
6535†	_	-	_	15.9	15.3	16,4	17,13	a l	26,7	+ 4,4	26,3
6539†	9	-	-		~	_	17,94	o	38,7	+ 3,4	38,4
6541	9		14,42	13,35	12,7	13,8	14,76	G	8,9	- 1,8	8,7
6553	9	-	-				17,14	G	26,8	- 2,3	26,7
6569	9,5	_	-	_	_	_	17,35	0	29.5	- 3,8	29,2
6584	9	-	- 1	-	~	-	16,56	C	20,5	- 6,0	19,6
6624	10	_	-		~	_	16,74	C	22,2	- 3,8	21,8
6626	9	+18	-	14,87	14,49	15,11	16,10	8.	16,6	- 2,0	16,4
6637	9	-	_	-		-	16,36	0	18,7	- 3,6	18,4
6638	8	-27		16,22	15,90	16,60	17,36	b	29,6	- 3,9	29,3
6652	8	-444	_	- '	~-	_	16,87	d	23,6	- 5,3	23,0
6656	8	+18	14,06	12,93	12,80	13,26	14,16	n.	6,8	- 1,1	6,7
6681	9,5	_	_	_		_	16,41	6	19,2	- 4.5	18,8
6712	_	_	-	16,10	15,65	16,36	17,10	d	26,2	- 2,7	26,0
6715	10	-	_	_	-	_	16,44	d	19,4	- 5.0	18,7
6723	9,5	_	15,33	14,20	13,7	14,8	15,44	( b	12,3	- 4,1	11,7
6752	_	_	_	13,26	12,8	13,6	14,62	b	8,4	- 3,8	7.4
6760		_	-		-	l —	17,28	0	28,6	- 2,5	28,5
6779	8	+12:	-	15,31	14,98	15.70	16,54	Ъ	20,3	+ 2,8	20,0
6809	9	] -	l —	13,58	12,9	14,2	14,74	l b	8,8	- 3.7	8,0
6864	9	_	_	17,06	16,76	17.35	18,43	[ d	48,5	-22,0	43,2
6934	9	_	_	15,78	15,33	16,11	16,98	l b	24,9	- 8,5	23,4
6981	_	_	16,80	15.86	15,53	16,20	16,84	a	23,3	-13,0	19,3
7006	l I	-	18,96	17.50	16,99	17,89	18,77	b	56,H	-20,4	53,0
7078	] 8	-11	15,63	14,31	14,13	14,55	15.60	J 6.	13.1	J 6,1	11.6
7089	9	-80*	15,71	14,61	14,25	14,76	15.72	R.	13.9	- 8,2	11,3
7099	9	_	-	14.63	13,77	15,04	15,82	ъ	14,6	-10,9	9,7
7492	9	-	-	16,82	16,3	17.1	17,01	a	25,2	-22,7	11,1

Appendix B

Catalogue of Galactic Clusters

	_	Notes		ا			 			1	_	1	1	l	N	1		'n	1	I	1	4	ļ	1		ìA	1	1	ı	9	I	ı	I	I	I	1
	Rsing	W=-0,5	47 -	10,7	+	- 1	+403	- 70	 	+	- 26	+ 63	+	1 40	9	-405	-136	-136	A+ 18	08	+	<	+166	669 -	-205	57	+169	- 46	+ 19	15	-288	+ 24	-161	-230	-486	 [2
	Linear	M = -0.5	44	4	9	10°	45.8	5	) O	2,0	1,7	5,	17	S,	2,5	13.8	J 26 3	26,3	V3,8	99	2,3	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	7,9	4	3,6	40	رن درز	160	6.3	10	128	83	13,1	3.2	91	የባ የታ
	8	W=-0 >	3.80	2.00	12.5	4 4	10.5	1,45	0,66	2.75	1.15	1 38	1 15	1,91		1 05			99 07	2,29	1,15	20 66	1,82	5.0	0,83		1.15	4,57	0,87		1,10	1,91	1 00	1 10	2,09	1 66
	Distance	M=+0,5 %	2.40	1 26	174	0.91	6 61	0,72	0,42	1,74	0,72	0.87	0 73	1,20	0,79	99'0	7.51	1,51		1,45						=	0 72	2,88	0,55	0 04	69 0	1 20	0,63	69 0	1 32	£.
Z.	- Meag	Sh Star					14 6																				8						9 35			
valactic Clusters	Approx	dag Lun of Plate	13m	13	13	13	16	12.8	12,8	128	12,8	12,8	12.8	12,8	12,8	12	<del></del>	1	12,8	12,8	12,8	12,8	12,8	ı	13.2	1	12,8	I	128	1	ļ	1	12,6	13	13	12.6
lactic	No Of	Stars	355	2	50	20	30	9	100	8	S	20	20	29	8	20	I	l	ଧ	40	11	80	8	40	40	ı	15	40	8	1	30	40	9	13	10	10
I O	Orient		 	ł	1	1	Ind	Ind	\$	1		1	1	1	~	Ind	63	\$	l	1	ì	ı	1	Ind	I	I	1	ì	71	ì	33	Ind	71	1	60	1
Jacalogue	Approx.	meter	13,	Ξ	<b>L</b> -1	9	45	4	10	7	'n	r\$	1A)	'n	11	45	36	36	8	2	7	18	15	30	Ţ	I	7	13	23	I	\$	15	45	2	17: 10:	0
18. L	į		44	U	U	به	o,	ರ	ø	ψ,	ָ ט	<del>ن</del> م	ישי	Ď	ø	d	44	49	ď	Φ	<b>י</b> טי	ゼ	ø	e	ں ت	ш	Φ	ď	ш	ပ	Ü	e U	e)	ų,	<b>ت</b> ،	ଅ
	Salactic	Lat	- Amil	d	Ô	0	+22 ,6	נח	n	4	q=	C	0	44	0	2	W	'n	44	0, 2	Ŋ	14	'n	co	14	ξ	ÇQ	0	ক্ৰ	읽	T.	0	Ò	-12 1	-11 7	N   N   N   N   N   N   N   N   N   N
	Cal	Long	88.	88,5	88 5	585 5	8	<u>x</u>	# 22	95	8	56,5	88	8	8	105	102,5	103	106,5	\$	103	111 5	105,5	114,5	123,5	134.5	110,5	120	120	147	148,5	129 5	147	153.54	154	130
	7000	Dec. 1400	•				十84 47																													
	6	0061 4.44	60 H	<u>4</u>	25, 6	27 5	35 ,1	9 4	51 8,	8 .	26 ,6	34 9	37 2	37 ,4	39	51.	12 0	15 ,4	25. Cí	26 ,4	35,0	35 6	w w	~	5 5	41	58	(J	7 o	14	40 2	43 ,9	57 ,6	4, 1 oř (	٥ : ۵ :	12
	, , , , , , , , , , , , , , , , , , ,	; 5 4	103	129	133	146	188	436	457	559	581	637	654	629	663	752	869	884	Mel 15	957	1027	1039	Ħ	1245	1342	Pleades	1502	1513	1528	Hyades	1647	1664	1746	1807	101/	102/

1 Described in ciph 33, above

		1	i																	_																		
	ş	<b>8</b>	<u> </u>	1	1		- 00	-	•	 	<u> </u>	<u> </u>	<b>-</b> -	1	 	1	١	<u> </u>	=	2	1	13	 	 	<del>-</del>	 	  -	15	1	<u> </u>	ا 	1	 	16	ı	  -	ا -	  -
	A THE	ı L	>536	+	1 59	33	+	+113	ı	8	1 2	+ 256	ક +	R 1	-248	8 ^	1330	1 62	-2585	V- 0.7	+993	<b>★</b> + <b>\$</b>	+466	+25	V-118	<b>8</b>	1	+ 1,9	+574	<b>%</b>	-216	ı			-		<b>28</b> +	
	I heart Demote		٨	1				8,4			L.																	3,7	18,1	5,5	15,9	!	E,E	1,7	6,5	4	8,4	9,01
	Ş	# 0.5	>4.17	0,73	20	1,10	9	40		2,19	2,19	5,0	6%	0,79	3,8	75,01	2,19	8, II,	9,12:	₹0,76	15.8	₹0,76	7 73	1,66	<0.76	0,76		80	6,92	0,95	2,19		0.95	0,95	32	0,95	1,15	द्ध
	Distance	50+-14 H		ار الأرا			-	1,4	'	1,38	1,38	3,2	0,50	0,50	1,91	>3,16	1,38	5,25	5,76-	<b>\$</b> 4,0 <b>\$</b>	10,0	\$4.6V	1,45	1,05	\$ \$	0 48		0,5	4.37	90,0	1,38	1	0,60	0,0	-04	090	0,72	1,15
	No.	ज्या शिक्र	9°±21]	0,	11 ,1	7. 6	7. 92	7. 6	ı		11 2		0, 6												6, 8[		ı		13 ,7		11 2	1	4. 6	4. 6	4		& &	
	Appear	of Plate	ı	12,0	5 6	ı	ı	5, 6,	1	ű	13,0	ı	13,0	1	14	ı	14	15 ,5	I	ı	١	#	13	13	I	14	I	ı	14	‡	13 .5	1	1	I	1	13 ,5	£0 %	13 %
	16 Of	Special Control	20	8	<b>\$</b>	8	8	150	ı	8	a	<del>우</del>	흕	92	B	8	a	몺	9	16	<b></b>	R	유	<u>유</u>	2	8	ı	8	_ 유	*	8	- 	- 강	- 왕	କ	닭	망	- 8
Communed	8	•	ı	ı	Ind	Ę	P	ı	1	ı	ı	\$	9	ı	ı	6	ı	I	9	I	ı	  -	2	47	0	ı	1	<u></u>	47	ı	ı	E	3	1	ጸ	Š	ı	I
	1		æ	#	'n	ล	ដ	R	٠,	-	*	*	\$	149	LQ.	•••	∞	149	+	\$	m	윢	<u>ب</u>	\$	8	12	*	9	٥	R	23	9	<u>-</u>	9	_	<b>\$</b>	2	8
	į	•	44	P	44	9	44	#	゙゙	Þ	Þ	100	0	7	•	0	7	₩.	44	U	Þ	U	44	•	0	<b>d</b>	7	0	•	ಠ	•	<b>20</b>	<b>14</b>	Þ	•	44	7	J
	Galactio	Ţ,	+ 70,4	4 0 4	9, 1 +	0, 4 +	+ 2 4	+ 4 .5	+14 ,4	+ 1.6	+ 2.7	+ 73.8	9 6 +	* 1 1	7,4-	0,1	7:8 -	4,01	5. 91-	9.0	9° E +	7. 6 -	1 +11 ,7	¥. 91-1	0, 6	ተ ሪ	+10 *	1.0	4 4 %	1 + 1 .7	9' 5	L +13 3	1.0 -	**	1, 15+	+ 1 5	9" + +	67 + +
	i.	Long.		141 ,5	5	140	143	145	131	121	151	Ţ		163 ,5	171			172 5					155 5			180		189 55			205		_	205	196	\$		198 ,5
	į	1900						+33 31																														
	96, 4	1900	18.5	19 2	7 77	S S	55	5 45 .8	55.	53.	<u>۲</u>	L.	7.	(J	œ,	80 CJ	16	£.	25 ,7	0,	e E	35	37 ,0	<u>ක</u>	42 .7	<b>4</b>	<b>3</b>	ri B	5 0 0	Q Q	1, 01	<u> </u>	<b>5</b>	7,	K rá	31,9	H o	พ์
	ę.		1883	1893	1907	191	8	2090	2126		I 2157	73 73	2168	2169	2186	7	ğ	238	ğ	Ŗ	253	ž	8	ž.	28	<u>2</u>	8 4	233	ă	2353	23,27	2355	236	2362	2430	2421	22	13

(Continued)

1	ង								١	7116	47	3	-		.,,	142	E 4.			D.			~.		Ç. W.	.,							•	1,1,	~ .		•		
	:	Notes	ı	1	ı	17	18	1	I	ı	1	1	1	1	1	l	ı	l	1	1	ı	1	I	:	4	I	I	1	İ	!	I	1	I	ı	જ	23	1	1	
	Rsmß	72 = -0,5	+ 184	+ 532	86 I			+ 261				10			+ 168			131	_	98	上25	124	+ 181	+ 331	유 수	+ 363	0,01	69 -	211	118	- 68	- 116	129	-152	-1002	- 807	- 156	- 31	
	Linear	M = -0.5	4,2	67	4 w	12,8	8,0	6,4	43.9	6 1	99	3 C	ነተ የባ	99	16	23 0	44	4 G	00 (1)	3.7	61	o, o	ių ių	60 LD	1	s, S	0	11,6	и ц	9,1	3	56	4,4	3,1	7,9	13	12.8	co (n	
	90	1/=-0,5 lepe	1,82	4,57	1,66	1,82	1,10	4,37	1 91	2 63	7 26	1,45	7 09	2,29	1 38	1,32	1 82	0,95	0 95	1,26	0 95	1 91	1 91	2,51		+ 37	90 0	3 98	2.0	3,47	1 32	2 19	20	151	1 82	5.0	2 19	2 19	
	Distance	V = -0,5	1.15	2.88	1 05	1,15	69'0	2,75	1,20	1 66	0 79	0 91	1,32	1 45	0.87	0,83	1 15	09'0	090	0 79	090	1 20	1 20	1 58	0,18	2 75	0 0	2,51	61 10	2,19	0,83	1,38	5. 6.	0,95	1,15	3.2	138	1 38	
	Mor	5th Star	r m					7: 21																	1	-			to.			11 ,2	13		10 8	13	11 2	11 2	
	Approx	Mag Lan of Plate	8	13 8				i i	יין מז			ı	13 5	S S	43.5	Ī		13 3							ı	13 5	ı	13,4	1	13 ,5	1	1	l	13 ,4	12 ,8	· I	12 5		
,		Stars	65	9	20.	150	9	28	300	4	20	8	30	00	4	200	150	0,11	80	20	22	30.	900	40	1	30	10	0	52	30	16	16	20	10	67	8	33	30	
1	Omono		2	J	98	11	7.5	. 1	15	1	ļ	1	Ind	Ind	15	1	89	1		16	1	1	1	%	1	ı	ļ	1	9	36	. 1	1	!	I	37	120	1	1	
	Approx.	Dia- me'er	య	1/1	0	24	25	100	147 (C)	90	128	l'=	·	10	7	. 09	27	1/1	30	101	90	Φ.	. 40	00	1	(4)	20	10	10	0	10	10	m	1	1	ا م	20	9	
		0200	b.c	Ö	М	44	b	ಾರ	ы	044	9	יט	bá	b	o b	o bu	04+1	ď	444	44	٥	ن د	ن	44	ď	ש	U	70	7	4-	به ا	שי	ه	9	4-	ە ،	ש	44	
	Calactac	Lat	ำก	9	(1	10	۲ -	1 20	) 1/	7.00	ren	i ei	0	7	-	1	1 4	1	46.		4	٠ 4	/	1 1-	· 12	; 4	. 40	•	6	1 4	7.	יז ר	•	17	16	ا ا ا ا ا ا	4	Q	
	Cala	Long	1070	100	214	200	253	2000	22.60	203 2	200	244	244		1 2 2 2	0 4 4 6	2002	2 10	100	7 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	7 60	11 10 10 10 10 10 10 10 10 10 10 10 10 1	747	210.5	A 44 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	32.50	200	1 000	233.4	2000	23.4	1 17 6	230	1,000	284	230	245.5	243	
		Dec. 1900	110 50/		75			3 6		100	74	1 10				0 0	3 5		) 14  -				0 0	10	ì	3 6	្ន				177 10			- 6	15		) (	52 28	
		R.A. 1900	2.23 B	) (4 ) (4	3 6	9 6	3	1 10	. 0	9 5	2 6	2 2	ត់ ជ	1 1	n 4	D Y	א מ	1 0	<b>~</b> 0	) z	† <del>?</del>		- 0	- c.	3 6	7 6	1 1	, ,	y 6	א ני א ני	υ . γ .	÷ 5	ļç	1 0	Į.	<del>5</del>	1 6	26 26 26 26	
		SON	Mel 74	7 10 12	3/30	7.07	707	7:7	200	247	× 6	1 4 6		V 00 1 0	0000	N 00 10 10 10 10 10 10 10 10 10 10 10 10	4570	1 A	701	0407	7007	1071	200	7007	/404	7077	1 4000	1,4341	7007	0007	2020	1 2393	20/07	1,0/1	1 6	2082	0107	2910	

1		•	1																																				
		-	1	ا 			·	I	1	ا _	1	ដ	 	I _	 	I	  -	 	! 	ا -	 	١	ا 	;	7	  -	ا _		  -	1	ا -	4	1	1_	1	1	1	1	
	A P		1	4 <del>1</del> 1	- I	1 405	٠ د د د	R +	0	* *	-238	- 17	+ 13	<del>რ</del>	 4	) 기	88 I	+	<b>8</b> 1	+552	- 47	+ 16	+ 395 +	∃ ; +-	+188	+ -	ን : ተ	55	629	+267	1	+ 11	22 1	<b>贸</b> 十	1.546	- 27	1	+	
	There	70 e	4 4	7	, ,		11,5	4	Q V	3,2	10,5	4,1	9,1	1,5	1,1	6,1	2,3	1,5	29	9,1	2,6	2,5	6,1	ģ	1	7.	7	4	13,5	41,4	1,1	6,0	7.7	, V	7.7	1,1	5,5	7.3	
ĺ	8	- A	47.4	8	2 6	3 5	1 8	4	\$,6 -	1,38	4, 3,	ä	0,52	1,05	8	1.74	8	S	99,0	5.25	2,63	0,95	5, 5,	1.51		1,05	3	£.	6,61	6.7	P,0	0,3	6,61	R	6,61	r,	1,58	0,83	
	Distance	#	ç	72.57	c	16	200	Į.	0 0 0 V	0,87	1,51	0,13	0,33	9,0	0,76	1,10	1, 24,	0,33	0,42	3,31	1,66	0,60	<b>4</b> .31	0,95		99,0	0,67	0,87	4,17	5,0	0.57	2,0	4,17	9,76	4,17	0,83	1,00	0,53	
	A Contract of the Contract of		408.7	2 2	;	, ,	בי מנ	11 .8	7.8	10 2	11 14	9	8,1	9, 6	<b>0,</b> 0	10 .7	11,0	1,	9, 8	13 ,1	11 ,6	4. 6	13 ,1	10 *	ı	9	10	40 22	13 ,6	#	ω, Ε,	7.	13 ,6.	6, 6	13 ,6	10 01	10 ,5	1, 6	
	Append	1 5 E	1 1 1 1	2		ı	1	ti ri	ı	1	1	ı	ı	13	13	13	13	13	13	1	13	13	13 .5	13 ,6	ı	13 ,6	13 ,6	13 ,6	ı	ı	13 .6	13 .6		9. 51	14	9, 61	13 6	2	
("DOU")	_		5	2 4	7 8	3 5	7		20	ĸ	\$	ŗ,	130	은 유	ĸ	150	S	8	K	S	20	ম	ล	<u>6</u>	1	8	9	8	75	8	R	2	8	3	152	8	R	K	
Continued.	1		1	ı	ij		ı	ı	Æ	ı	\$	1	g	1	ı	ı	1	ı	ı	Por	ı	ı	ı	2	١	1	ı	ı	1	1	1	67	1	1	ı	ı	ı	ı	
<b>)</b>	-	4		1		31	3	Leg	••	•0	15	2	8	1	m	ä	+	9	51	9	=	60	7	13	ı	7	r <b>-</b>	119	7	91	+	40	+	9	4	r	, ti	S	
		į	Ţ,	5 4	4	о.	н	₩	v	44	0	٥	74	Ų	44	•	44	ы	9 0	ы	0	Ď	44	bė	v	Þ	Ð	44	ø		0	6	-	7	***	ð	 -	~	
	Gelectio	I tal	000	ا در	)   	0 V	• • •	* o +	0,	0, 4 +	9,5	0, 4	+	4	ণ ০ 	1 1 5	1 2	+	0, 1	0 9 +	1,0	0, 1	L. 4 -	+ 0 ,7	1.85 .4	7,1 +	+ 7 4	ا ا	0,	4 1 9	40	7	4	4	14	1	14	112.0	
	3	Long	0000	5.5	()	251	248,5	252	253	27	257	257	257	258.5	259	260	90	17	262	262.5	265	265	192	267.5	200	267.5	88	368	8	2	ì	2.2	1,12	1	1	1 1	300	7	
		Dec. 1900																								8 4													
		<b>2.A.</b> 1900		E .	27	20	17	2	20	ì	1 00	<b>,</b> g	, 6	<b>'</b>	00	<u>.</u>	1 =	7	; 3	, 4	9			61	8	2 4	5	1	ε	ļ	3 %	3 5	7 2	: 3	ξ.	ş		7	
		366																								H													

_
ŭ
ă
Ħ
甘
ĮÖ.
9

•	, 0										-																											
	Notes	Saluka Saluka	1	1	1	I	1	I	1	1	I	1	1	1	ļ	1	1	ı	1		1	1	I	I	!	ļ	I	I	ì	J	I	ı	I	1	I	I	۲ ا	3
	$R \sin \beta$ $M = -0.5$	ed H	- 23	+ %	<del>1</del>	十104	- - - - -	+	+126	-186	1445	1 75	105	122	130	2+	1 50	145	1 36	4	+ 13	2	1 63	-475	105	- - V	+	o I V	V-637	1108	cı 	ナノナー	- <del>-</del>	- 97	- 79	1 - 227	 	
	Linear Diameter	V=-0,5	7.9	9 7	9,9	4 ò	27	4 8	ໝູ	4.	00 10	60	(O)	4,9	44 5	0 9	0 9	17,5	60 60	17	1,6	တ်	61 4.	6J -	<b>4</b> ,0	<1,7	7	<del>'</del>	V8,7	10,0	<del>기</del> 범	R	8,0	3,6	5	w.	9	  -
	93	M=-0,5 kpc	1 82	1 10	3,80	1 58	1 82	1,82	6 61	3 80	6 61	0,63	1,91	1,10	1,66	0 83	2,29	7 8	1,3	1 45	0 79	1,51	1,66	3 98	4 57	<0,38 <	0 57	0 V V	75,04	2,29	131	50	6,0	2,51	1,05	£.	2 63	
	Dist	M = +0,5 1 kpc																																		0.91		i <del>-</del>
	Mag	oth Star	104,8	6	51 4	10 10	10 8	ე. გ	13 ,6	4, 21	13 6	60 00	10 9	7, 6	10 %	9	11 ,3	11 ,0	10	10	0 0	4, 01	10 ,6	12	12	4, T.	eo (Ú	4		11 ,3		13	_			10,3		I
	Approx	of Plate		10	13 ,6	I	13 ,6		1	13 ,6		1n	13 6	13 6	13 ,5	13 5	4	13 5	13 5	1	13 ,6	ı	I	13	I	I	12	či ci	Ì	12, 21	1	13 S	1		CI CI	13	1	l
ned)	No of	Stars	50	30	30	16	120	200	30	100	30	30	120	35	30	120	9	8	8	9	20	9	50	20	ଧ	120	9	500	2	<b>3</b>	9	20	12	8	ନ	200	9	l
(Continued)	Orient		59	1	38	1	I	64	I	Ind	S,	1	- 46	J	I	Ind	Ind	I	1	!	72	1	1	I	1	1	4	I	4 10	49	ļ	I	I	39	: 1	I	I	l
	Approv.	meter	15,	00	9	<b>9</b>	40	σ	<b>ო</b>	4	ſŊ	10	£,	50	2	53	0	30	2	4	7	20	μņ	22	ເນ	10	Ç	40	9	14 10	10	13	Φ	173	12	14	2	-
	Clace		4-1	୯	ø	0	יט	44	•	44	4+1	יט	44	ק	ď	Φ	4−1	ø	שי	44	44	ø	44	ø	יס	υ	4-1	ပ	4-1	0	44	ש	יטי	þζ	o o	ø	44 l	
	Galactic	Lat	Ö	Ŋ	-	'n	e)	<b>q</b> e4	+	d	100	8 9	1 2	1 6 4	4 4	4 4	1	4 - 4	    -  -	+	+ 10	1 .	() ()	φ	7	4 0 +	0	Ŧ	<b>!~</b>			าก	0		4	0, 6 -	٠ دن ۽	ť
	Gal	Long	282°,5	285	285 5		289 5	289	293 5	293 5	263			295 .5			302			306				301				312 ,5		309 .5		307	316	316	100	307 5	317	327
	320, 5-0	Lee 1900	-60° 16′	-56 7	-57 7	-54 6	-53 57	12	-53 15	- 56 10	27.	-60 13	53 57	- 57 39	44																					149 30		
		R A- 1900	22 12 13	28	36 1	41 8	57 .9	00	26	4	47 8	ر د د	14	10.6	0	Š	5	1 4	10	íć	, tr	) (r	9 (	. 4	43	47	80	6	1/2	11	10	16	66	Ç	-	17 16 ,9	11	<u>;</u>
		් ජ ප	1																																	1 4651		

																																				•	_
, contract of		প্ল	ı	1	l	I	1	27	. 1	i	1	1	1	প্ল	ı	ম	I	ጽ	I	52	<b>2</b> 3	25	ı	I	31	ង	33	ສ አ	I	33	I	1	ī	ı	l	36	37
4 N	E	ı	+ 17	: Н	1	-53	\  -   <b>5</b>	8	-114	ନ୍ଧ 	+	1 76	+ 25	33	1	ا ۲	   	유 I	<b>‡</b>	ı	ı	I	1348	ا ه	-244	18	- 83	ઇ 1	4	ま 1	1	-207	-131	E E	+ 33-	1331	B
Den se	K=-0.5	ı	70	4	1.8	17	V0.9	4.1	3,0	3,3	4	2,5	10,1	6,6	3,0	10,0	1,0	7,	2,6	1	1	J	4	0,8	ν, œ	121	6,7	1	20	10,6	1	9,9	7.7	12,0	10.2	7.9	3.6
R	3		0.69	9	1.05	9	71.05	0.57	105	0,57	50	1,45	4 88	8	9,0	1,38	8,0	ድ	0,91				0,1	5,50	20,0	1,66	1,91	8	6,50	0,94		229	3,31	8	0,5	3,92	_
Metaor	M-+0.5 M0.5 Mrs Apr	I	770	0.38	99'0	4	>0.66	95.0	9	9,36	0,2:	0,91	<u>1</u>	40	0,44	0,87	4,0	0,57	0,57	1	1	1	er Er	3,47	3,16	1,05	<u>4</u>	1,05	0,32	0,57	1	1,45	200	1.45	0,3	1,91	1.25
,	St. Sherr	_	7.1	*	0	1	9	, r?	9 0	80 LJ	7-	ال 10	11 ,8	4	5,	6 6	8 .7	و ق	و. ب	5	[13	<u> </u>	13	13,2	13,0	9, 01	6, 01	10 ,6	0,	e, e,	1	£, 11	12 ,1	11 5	<b>\$</b>	6, 11	9
Append A	of Plate	100	- ! 1	1	1		1	12.2	1	, 1	<b>~</b>	1	- 	4	4	5, 21	ı	4 t	ı	1	ı	1	1	43.2	43.22	12 .5	ı	5, 41	9.6	43 22	ı	13.2	4.51	1	10 2	13	14.5
No.	100 S	100	i ¥	18	2	, K	78	9	8	33	2	R	\$	S	8	3	25.	옶	73	ı	١	ı	유	R	2	55	4	33	9	유	-	75	×		 2	8	Ş
1000		   1	1	ı	1			ø	ا د	ı	ı	R	20	Ę	ı	n	‡	ı	1	ı	8	ı	1	ı	50	ı	ı	ı	ι	F	7.	#	Fed	ı	1	1	
			è	i ii	4	· ·	) N	, L	?=	Ā	8	9	2	8	=	15	יא	10		=	ų.	0,75	1.5	40	4	10		ı	8	9	-	- 0	00	<u></u>	2	•	٠,
į	Į	•	•	•	•	7	5 6		7		U	•	•	•	7	0	-	שי		ы	) bó	120	by by	) <b>1</b> 4	- I	0	Ð	Ü	4	7	~		944	· •	יי פ	-	-
Gelectic	1	1 430 7	; ·	t c	2 0	1 3	t 4 c	10	1 12	1	+11.6	-       0	4	.	1	4.4	3.7	1	66	4	7. 6	1 2	4	10 -	12	9 0 -	17	7	1	9 9	1	27	10	10	4 1	7 7	
3	I bag		۲ د د		3 1	_	3,5	11	\$ 5	277	•	3,5	i i	7.52	-	1		1 6	15	334	100		1 %		3		77.	272	2 4	175	:	263			7	254 6	Ξ.
	Dec. 1900	200	5 Y	3 7	2 S	31	2 S	) 1	7 5	2 5	14	7 5	2 2	1	Y	30	3:	3;     	38	131	176	134 47	3 6	1 2	3 (5)	19	15.	146 43	3 2	2 0	12	1 8 2 4	 2	99	2 6	18	_ ጓ : እ '
	P.A. 1900	0 110	21.5	9	4	1	<b>1</b>	1;	5, 55	3 5	2 7		۲ بر د د	2 5	2 t	;	{ ·	1 2	2 6	3 6	1 4	, c.	2 0	٠ <del>-</del>	: 5	5 6	1 7	1 4		1 2	20	Q 0	9 6	Ž.		₹ %	٩ ٢
	FGC	1							3																						?;						

(Continued)

		Notes	ļ	1	I	ı	1	ı	I	!	I	13	Ŷ	ı	1	1	i	39	1	1	I	I	4	l	l	I	1	1	]	1	1	+1	1	]	I		ļ
	R sun B	M = -0,5	+ 46	-108	-272	12	+ 56	+663	18	4 4 2	13	ا ما	_ Z0Z	100	+275	102	+ 12	1	+1034	-406	135	10		+ 41	<del>↓</del>	-177	08 	- 183	133	+118	+	+ 11	+480		- 22	-362	S I
	Linear	M=-0 5 pc	2,8	, S	4,4	1	126	8,8	1,1	00	00 ( N)	2,5	2,5	1,7	7.3	6,7	Δ, S	en en	7.3	16,8	in N	67	61	0	1,7	7.2	4	4 4	2,13	ر و ر	1,6	4.	13,3	4,0	4,5	34.8	<del>4</del> δ
	93	M=−05 kpc	62'0	2,00	>5,01	5 01	2 88	50	0 79	0 79	5 01	0,79	8,	0,95	5,01	1,15	0,79	0 95	0	(5) (8)	9	2 88	0 25	00	N SS SS SS	1,32	0,79	5 01	0,79	5 01	2 73		4,57	2,73	2 00	3 98	2 75
	Distance	M=-0,5 M	0,50	1,26		3 16	1,82	3,16	0 50	0,50	3 16	0 50	1,26	09'0	3 16	0 72	0,50	0,60	in G	1,82	1,51	1 82	0.16	1,82	1 %5	0.83	0.20	3 16	0,50	3,16	1,74	1,17	2,88	1,74	1 26	2 51	1,74
	Mag	3th Star	0 10		[13		11 00						0,							11,8	11 ,4	11 ,8	9	11 8		10 1			o,	13		11 0		11 ,7	11 0	12 5	11 ,7
	Approx	Mag Lim of Plate	13"	13	ı	ı	ı	I	13	1	1	ŧ	1	13	1	l	!	1	ı	I	13	I	1	I	I	1	I	1	43	1	1	13	13	l	I	13	i
חבת /	No of	Stars	40	50	80	9	ဂ္ဂ	150	က္ထ	6	۳. ارد	ନ	9	20	30	50	40	20	80	9	30	20	25.	10	20	လ္တ	40	40	လ	52	27	120	70	3	18	200	25
Continued	Orrent	٠	ı	1		ı	ì	ı	i	I	ļ	]	Dur	I	I	1	1	ł	Ind	53	١	ı	ı	I	ļ	ı	ı	ı	1	1	ļ	20	1	1	I	Ind	l
	Approx.	Dia- meter	12	9	നു	ı	15	9	rů .	00	4.	3	d* 1	9	rts.	20	90	7	ነብ	50	ro	œ	30	-	N	8	200	m	2	~	~	12	10	ı	۲۵	30	٥
	Ę	Cass	Ą	·U	44	ψ	יטי	7	י טי	o	יטי	ರ	piQ.	U	0	ø	ש	ゎ	bю	-	ø	Φ	o	d	d	יט	יט	שי	ゎ	Ð	で	Ø	þ	ď	Φ	v '	7
	Galactic	Lat	+ 30,3	1.8.1	   	103	+11 2	1 7 6	**	<del>ر</del> ي	+	<u>ነሱ</u> ነ	'A'	9	+ 0 4	'n	۳	0	+11,9	¢0	 60 5	0 1	12,7	+ %	+ 0 ,	7,7 -	∞ 1⁄1 	Ŋ	<del>पूर्व</del>	판	0	0	0,9+	0	9, 0	10	0
	Gal	Long	10°	ð íú	***		47	41 5	27	27 5	10 20 20 20 20 20 20 20 20 20 20 20 20 20	47	24 2.	47, 5	35, 55	33	46 ,5	45		37 5	57 ,5	62	60 ,5	65	64 5	63	56 ,5	69		76,5			33.5			83	83
		Dec. 1900	+100 14																																	+56 10	
	-	RA 1900	18h 46m,8	cı	ŧ٩	36	30 17	37	<u>ښ</u>	46	\$	4 8	4	0	7	1	19	R	3	30	49	27	8	40	4	7	74	11	43	ဂ္ဂ	1	19	5.	\$	51	22	52
	(	7 C C	6209	6755	6756	6802	6811	6819	6823	6830	6834	H 20	6838	6866	1311	6885	6910	6913	6669	6940	7062	7086	7092	7127	7128	7209	7243	7245	7380	7419	7540	7654	7762	H24	7788	7789	7790

```
Notes to Appendix B
     1 Mossier 103
     2 Distance from Wallenguist, Upsale Medd 42 (1929)
     3 h and z Porsol, fifth star assumed of magnitude −2<sup>M</sup>,5 TRUMPLER [Publ ASP 38,
p 352 (1926)] gives a distance of 2,3 on the basis of the mean magnitude for Class Ao.
4 Measter 34
     5 Memier 45, the diameter from Russell, Dugan, and Stewart.
     6 Distance and diameter from RUSSELL, DUGAN, and STEWART corresponds to an angular
radius of nearly two degrees
     7 Mossier 38
     8 Messior 36, distance from Wallenguist, Upsale Medd 32 (1927)
     9 Mossier 37, distance from von Zerpel and Lindquen, Svenaka Vot Akad Handl 61.
No 15 (1921).
     10 Mossier 35
                                                 11 Scarcely resolved
     12 Ecceptric in an alliptical diffuse nebula.
     13 S Monocarotis in cluster,
                                                 14 Mouster 41
     15 Monator 50
                                                 16 r Canis Majoris in cluster.
     17 Memier 46, an important photographic catalogue by Chryalten
     18 Mossler 93
     19 Praceope, Mossier 44, distance from Ruberll, Dugan, and Stewart
     20 Messler 67
     21 Diffuse nebula in a coarse cluster
                                                 22 7 Caringo involved
     23 Coma Berenless, distance from Russell, Dugan, and Stewart
     24 w Crucis.
     25 Not resolved, a photograph of N G.C. 6540 appears in Pop Astr Tkisk 8, p 62 (1927).
     26 Mount Wilson plate.
                                                 27 Messler 6.
     28 Mossier 7
                                                 29 Mossier 23.
     30 Moraler 21.
                                                 31 Mossier 24
     32 Memior 16.
                                                 33 Mossier 18
     34 Mossier 17, nebulosity.
                                                 35 Monster 25
     36 Mossier 26, TRUMPLER finds a distance of 2,75 [Lick Bull 14, p 122 (1929)].
     37 Memier 11, distance from TRUMPLER.
                                                 38 Messier 71,
     39 Mossler 29.
                                                 40 Member 39
     41 Mossier 52, distance from Wallenguist, Upsale Modd 42 (1929).
```

Addendum Current work on problems of both our own and external systems, in progress since this section was written, contributes effectively to our view of galactic attracture and indicates the necessity for gathering much more evidence before any conclusive theory can be advanced. For instance, there have been important studies at Harvard, Mount Wilson (Strenging), and McCormick Observatories on the integrated magnitudes and colors of globular clusters. The absorption extending out from the "region of avoidance" appears to affect the magnitudes and distances of clusters in low latitudes, making uncartain and impractical the estimate of the dimensions of the Milky Way in its own plane, but, on the other hand, the Harvard studies of faint clusted type variables in high latitudes (Wash Nat. Ac. Proc in press, 1933) indicate a total galactic extent of the order of that given above.

#### Chapter 6

# The Nebulae.

Ву

#### Heber D. Curtis-Ann Arbor, Mich

With 58 illustrations in the text and on a plate

### a) Introduction.

1. Definition of Nebulae. In the early historical development of the field, any object that was non-stellar with the limited telescopic powers available, and that did not appertain to the solar system, was fermed a nebula. The earlier lists and even the more important later catalogues have in general made no complete or satisfactory distinction as to the character of the nebulous object, and the genetic influence of such reference media as the great catalogues of Dreyer have involved the subject in a number of contradictions through the inclusion of such non-nebular classes as the globular star-clusters and the spirals. These inconsistencies persist in all the modern bibliographical apparatus of the field, and doubtless can never be entirely removed. Further reference to these difficulties will be made in ciph 4 and 34

2. Historical Notes. As in most fields of astronomy, research on the nebulae

may be divided into three moderately well-marked periods

A. The period preceding 1782, marked by visual or sporadic telescopic observation, and now of little more than historical interest. A few brighter star-clusters and the Great Spiral in Andromeda, which can be made out by the unaided eye, were noted very early. Aratus (300? a d) mentions Praesepe; Al-Suff (ca. 960 a.d.) notes Andromeda, Hevelius (1690), Halley (1715), and La Caille (1755), catalogued a few of such brighter objects. Messier's lists of 103 bright nebulae and clusters appeared in 1771 and 1781—82 See Appendix No. 4 for the modern identification of these objects, for which Messier's numbers are still in frequent use.

B. From 1782 to 1898 To Sir William Herschel must be given the unchallenged rank of pioneer in the field of nebular discovery. For nearly a quarter of a century following 1782, with tremendous zeal, with instruments which would seem totally inadequate to the modern observer, with an acuity of vision which has perhaps never been surpassed and which is a constant source of amazement to those who review his work with the much more powerful instruments of the present day, he discovered and catalogued in eight classes (cf. Appendix No. 2) 2509 nebulae and clusters

Second only to the work of his famous father was the continuation made by Sir John Herschel, who observed 2307 nebulae at Slough, and 1708 southern

Ϊĺ

<sup>&</sup>lt;sup>1</sup> Herscher's numerous papers in the Phil Trans and other media are now most easily accessible in: Scientific Papers of Sir William Herschel, Published by the Royal Society and the Royal Astronomical Society 2 vols, quarto London (1912).

objects on his expedition to the Cape of Good Hope, in the years from 1830 to 1847 He collected his own and his father's discoveries in his General Catalogue of Nebulac1, containing 5079 entries, and referred to as GC in the older literature.

The importus which had been given to the work of nebular discovery by the HERSCHELS brought a large number of other workers into this field in the middle third of the nineteenth century Space prevents more than a mention of the names of Rosse, Lassell, Stephan, D'Arrest, Swift, Schönfeld, Bond, and Voger. To Rosse is due the first detection of the spiral form; he discovered perhaps twenty spirals with the 6-foot reflector. There were many observers in this period who concentrated solely upon the discovery of new objects, with little care for accuracy of position. Others, as D'ARREST, made careful determinations of position, which may conceivably serve as a point d'appui for

proper motion investigations of the distant future

C. 1898 and following. While there is no well-marked line of demarkation between the second and third chronological divisions, the year 1898 may be conveniently taken us the starting point of the modern epoch, even though the very first photographic and spectrographic results are considerably earlier in point of time. The discovery of bright lines in the spectra of gaseous nebulae was made by Sir WILLIAM HUGGINS in 18644, to whom also is due the first spectrogram (of the Orion Nebula) in 18828. The first nebular photograph (also of the Orion Nebula) was taken by DRAPER in 18804 The first extensive sories of nebular photographs is due to Sir Isaac Roberts, and was made in the years from 1885 to 1904. His photographs confirmed Rosse's discoveries of spirals, and increased the number of known spirals to about forty.

It now seems strange that an immediate wider application of photography did not at once follow the significant pioneer efforts of Roberts, Drafer, Com-MON, HUGGINS, JANSSEN, and others. During the two decades following 1870 a considerable amount of purely stellar photography was carried on, but the great value of the reflecting telescope was not fully appreciated until its spochmaking revivilication by KEELER, at Lick Observatory, in 1898-1900'. KEELER's results showed the following salient advances, which have formed the norm for

much subsequent nebular research®

1 Reflecting telescopes of moderately large focal ratios (1.5 to 1.6) are the most efficient instruments known for nebular research.

2. A wealth of structural detail was shown, impossible to secure visually or with refractors

3. A predominantly spiral form was shown to exist in a large proportion of the objects recorded. About 40 objects had been previously found to be spiral

Sidorum nebulosorum observationes Havnianaes (1867), 1942 entries.

CR 94, p 94 (1882).
Amer J Se (3) 20, p. 433 (1880).
Liek Publ 8 (1908).

Phil Trans (1864)

The first stellar photograph was taken with the 15-inch equatorial of Harvard College Discreatory on July 17, 1850, by Mr Whipper working under the direction of Professor Bown, An image of a Lyrae was obtained

4 Proc R S London 13, p. 492 (1864)

Perhaps the main reason for this neglect of the reflector came from purely mechanical considerations. With scarcely an exception, reflecting telescopes from the days of the older Herschell down were mounted and equipped most crudely, in comparison with the mechanical excellence developed in the mountings of refracting telescopes. Lassell reflector at Malts. utilized man-power for its "driving-clock", a workman gave one revolution per second to a heavy flywheel suitably geared to the tolescope. There was, in this period, searcely a single reflector possessing adequate rigidity, accurate clock-work, or convenience of manipulation.

4 Very large numbers of very small and faint objects were recorded "A conservative estimate places the number within reach of the Crossley reflector at about 120 000. The number of nebulae in our catalogues is but a small fraction

of this" See ciph 36

Keeler's piogram with the Ciossley reflector was continued and completed by Perrine (1901—1903), and extended by Curtis (1909—1918) Later, the magnificent 60-inch and 100-inch reflectors at Mt Wilson, in the hands of Ritchey, Hubble, Pease, Duncan, Humason, and others, have secured larger scale nebular photographs of the highest perfection. A vast amount of survey data has been accumulated by the Harvard workers and on the Franklin-Adams star charts. All work in the radial velocities and spectrographic rotations of the spirals goes back to the extensive pioneer contributions made by Slipher, at Lowell Observatory. In Europe, to mention but a few, notable investigations have been carried out by Wolf, Reinmuth, Wirtz, Holetschek, Hagen, and others. In the still comparatively neglected southern heavens, a beginning has been made by Perrine, at Córdoba, and by Knox-Shaw and associates, at Helwan. More complete details of the progress which has been made since 1900 in the nebular field should be sought in the separate sections.

8. Bibliographical Notes<sup>1</sup>. The culmination of a century of discovery, marked by some slight progress in delineation of form and classification, was marked in 1888 by Drever's collection and revision of all previous results in his New General Catalogue (NGC), which, with his two supplementary Index Catalogues (I, II), contains 13223 entries. These are still the most complete catalogues of nebular objects, and the indispensable basis for all succeeding surveys.

The older nebular literature refers frequently to nebulae by the Messier number M, by Su W Herschel's Classes and numbers, by the numbers in Sir J Herschel's lists (JII), or by the same author's General Catalogue number (GC). The bright spiral numbered 4303 in the New General Catalogue (NGC), may then possibly have also the designations M61, I 139, JII1202, or GC2878. This is a source of considerable confusion and loss of time in consulting references in the older literature. Appendices Nos 1, 2, 3, and 4, give finding lists for locating such references in the NGC, which is the only method that should be employed in designating such objects. Throughout this treatment, nebulae will accordingly be referred to solely in the forms 7619, I 562, II 2418 (i.e., their numbers in the NGC or in the First and Second Index Catalogues), and with the omission of the qualifying letters NGC.

While many faint nebulae have been photographed which are not given in the NGC (see Appendix No 7), to be found in various published lists, the most comprehensive and homogeneous photographic catalogue of such NGC objects as can be reached from northern latitudes is doubtless that due to REINMUTH, with 6251 entries of NGC objects, a summary of the photographic work at Konig-

stuhl by Wolf, Reinmuih, Wirtz, and others?

There are already many thousand small nebulae listed that are not included in the NGC, and Hubbie has estimated that there may exist as many as 3 · 10' small and faint objects in the great group of the spirals (see ciph 36). The labor of observation and subsequent cataloguing adequate to a really complete

<sup>2</sup> Die Herschel-Nebel nach Aufnahmen der Königstuhlsternwarte, Publ Sternw Heidel-

berg 9 (1926)

<sup>&</sup>lt;sup>1</sup> J L E DREYER, A New General Catalogue of Nebulae and Clusters of Stars Mem RAS 49 (1888), Index Catalogue of Nebulae found in the Years 1888 to 1894, ibid 51 (1895), Second Index Catalogue of Nebulae and Clusters of Stars, containing Objects found in the Years 1895 to 1907, ibid 59 (1908)

Durchmustering of all such objects brighter than magnitude ca. 20 is so tremendous that it will doubtless be necessary to leave its completion to the centuries following our own. Even the systematic study and classification of the 25000 ± objects of present lists, as suggested by the Committee on Nebulae and Star Clusters of the International Astronomical Union (1925), demands international co-operation Λ new General Catalogue of Nebulae in the form of a card catalogue is being prepared by Lundmark at Upsala¹ and will be available for consultation by investigators. About 16000 cards have been written out, and it is expected that the complete catalogue will enumerate 35000 objects, publication is planned within the next few years.

A card catalogue which the author has compiled of literature relating to the nebular and allied fields since 1890, with the inclusion of older works of importance but with the omission of minor notes and papers of a purely general or popular nature, contains over 2000 entries. It is manifestly impossible, therefore, to aim at completeness in the bibliographical references quoted in treating this subject. In general, only a few of the more important references can be cited, and the names of numerous investigators must perforce be omitted

4. Classification and Units. A descriptive summary of the present status of the subject of the nebulae manifestly requires a less complicated and detailed system of classification than might be deemed necessary for the purposes of a catalogue. For this reason, the field is treated in this paper under its larger outlines, as follows:

The Diffuse Nebulae

- 1 Dark Nebulge.
- 2. Comule Clouds
- 3 Luminous Diffuse Nebulne

The Planetary Nebulas.

The Spirals

- 4 True Spirals.
- Berred Spirals.
- 3. Elliptical and Globular Objects.
- 4. Magalianic Type Spirals

In Appendix No. 5 are collected a considerable number of systems of nebular classification which have been suggested or used by investigators of the field

There are some elements of inconsistency in all existing systems of classification, that of this treatment included. The genetic development of the field, largely through the influence of the Herschels and the NGC, which perforce combined in one catalogue all diffuse nobulae, planetaries, clusters, and spirals, has forced us into a somewhat illogical position as regards nomenclature and classification. There has never been any difficulty as to the sogregation of the clusters as a class, inasmuch as they are not nebulae at all. The spirals are likewise not nebulae, in the rigorous sense, yet these objects form the overwholming preponderance of all existing "nebular" catalogues. We are presented with the dilemma, on the one hand, of continuing to distort somewhat the true concept of bona-fide nebulous matter by calling them "spiral nebulae", "anagalactic nebulae", "extra-galactic nebulae", "non-galactic nebulae", "außergalaktische Nebel", and the like, or, on the other hand, of abandoning untiraly this lack of nomenclatural rigor forced upon us by the historical development of a field

<sup>1</sup> Publ ASP 42, p. 31 (1929)

<sup>&</sup>lt;sup>8</sup> The comparatively rare cases where emission lines have been detected in the spectra of spirals may doubtiess be adequately explained as due to the inclusion of true luminous nebulasity. See ciph, 48.

in which the substantiation of the non-nebular character of the spirals is less

than fifteen years old

The author would personally prefer to use the term "galaxies" or "external galaxies", rather than the word "spirals" in describing these objects1, thus avoiding the partial inconsistency that no spiral structure is discernible with present resolution in the small elliptical and globular members of the class. The name "spiral" may, however, be regarded as a more or less satisfactory com-

A unit frequently used for the distances and dimensions of spinals in recent research literature is the parsec, which is the distance corresponding to a parallax of i" This concept of distance is less familiar to investigators in allied fields of science, and the unit of distance employed throughout this treatment will be the light-year, abbreviated to Ly, and equal to 9,46 · 1012 km, or 5,87 1012 miles 1 parsec =  $3.26 \text{ ly} = 3.1 \text{ } 10^{13} \text{ km}.^2$ 

1 E g , H Shaplly, Note on a Remote Cloud of Galaxies in Centaurus, Harv Bull 871, The Coma-Virgo Galaxies, I-VI, ibid, 864 to 869 and 873 (1929)

With an error of ca 8%, which is entirely negligible in comparison with the uncertainties of present cosmic data, the transfer from light-years to parsecs, or vice versa, may be made through the simple relations

$$D_{13}$$
 3/10 =  $D_{\text{paraces}}$   
 $D_{\text{paraces}}$  10/3 =  $D_{13}$ 

Of the equivalent methods of expressing the distance of a spiral, all of which may be found in the literature of the past decade

$$\tau = 0'',000\,0007$$
 $D = 1.4 \cdot 10^6 \text{ parsecs}$ 
 $= 4.8 \cdot 10^8 \text{ l y}$ 
 $= 4.5 \text{ A}$ 

the value in light-years has some advantages on the score of casy visualization

The added "historical" element involved in the use of the light-year as a measure of galactic distances is of great interest and value. Though the light-year was not used as a formal unit in his time, attention was perhaps first called to this point by 5h WILLIAM

HERSCHEL (Coll Sc Papers 2, p 213)

a telescope with a power of penetrating into space, like my 40-feet one, has also, as it may be called, a power of penetrating into time past it may be proved, that when we look at Sirius, the rays which onter the eye cannot have been less than 6 years and 41/2 months coming from that star to the observer. Hence it follows, that when we see an object of the calculated distance at which one of the remote nebulae may still be perceived, the rays of light which convey its image to the eye, must have been more than nimeteen hundred and ten thousand, that is, almost two millions of years on thou way, and that, consequently, so many years ago, this object must already have had an existence in the sidereal heavens, in order to send out those rays by which we now perceive it"

The following short table gives a number of the units which have been used in ex-

pressing the enormous distances of other galaxies

```
= distance traversed by light in 1 year = 9,46 1017 cm
Light-year
                                  = distance for \pi = 1'' = 3.261 \text{ y} = 3.1 \cdot 10^{18} \text{ cm}
Parsec
Cubic parsec
                                 = 34,65 \text{ l.y}^3 = 2,9 10^{65} \text{ cm}^8
                                  = 108 parsecs = 3260 l.y
Kıloparsec
                                _{\circ} = 10^{6} \text{ parsecs} = 3.26 \cdot 10^{6} \text{ l y}
Megaparsec
Sternweite, Macron, Astron
                                  = parsec
Simometer
                                  = 10^6 astr units = 15.81 y
Siriuswelte
                                  = distance for \pi = 0'', 2 = 16,31 \text{ y}
                                  = distance of Great Spiral in Andromeda, supposed to be
Andromede
                                          of the order of 1000 ly at the time this unit was
                                          suggested by VERY!
```

Α

= an unnamed unit used by DE SITTER in recent papers  $= 1.06 \cdot 10^{0} \, l \, y = 10^{21} \, cm$ 

### b) The Diffuse Nebulae.

6. Definition. The diffuse nebulae, which are rightly to be regarded as par excellence the actual nebulous elements of the cosmos, are irregular cloud-like formations (ex Lat nebula = cloud) of tremendous extent, of random and incheate structure, of the utmost tenuity, and composed of finely divided matter or matter in the atomic or molecular state.

In apparent size, they vary from small irregular patches or detached wisps to complicated structures of enormous extent and volume. Several of Herschel's regions of diffuse nebulosity cover over 7 square degrees, while the "North America" in Cygnus (7000) has an area of about 10 square degrees. There are even larger areas at very faint diffuse nebulosity in Orion, Taurus and Perseus which must cover over 100 square degrees in their extreme dimensions

6. Number and Distribution. The diffuse nebulae are essentially and definitely galactic in distribution, and are rerely found at any considerable distance from the galactic plane. Save as possible constituents of other galaxies (see ciph. 48), all are apparently within the bounds of our own galactic system. They are, moreover, nearly always more or less closely associated with stars

While no accurate data are available as to the total number of the diffuse nebulae, it seems fairly certain that this total is not large, and that this class does not form 10% of existing nebular catalogues. One may conservatively estimate their number as roughly 1000.

CURTIS, in the Crossley Reflector program, sought to secure a photographic record of all NGC objects with the Horschellan characterization B or L; the program was otherwise at random. He photographed 56 diffuse nebulae, as against 513 spiral, from which may be deduced a total number of ca. 1000 objects in this class.

CHARLIER® plotted the galactic coördinates of 14 475 NGC entries (reproduced as Figure 29), excluding all objects known to be planetary, annular, clusters, or of stellar type. For the zone 30° in width between galactic latitudes +15° and -15°, he found that the number of nebulae per 25 square degrees was but 1,3, and the numbers in the zones at ±15° were twice as great as those at ±10°. As the diffuse nebulae are most frequently seen in low galactic latitudes, if the area of the Milky Way be taken at 10800 square degrees (probably excessive), one would expect only ca 560 such objects, to which total would be added the numbers of any diffuse nebulae lying farther from the galactic plane

HARDCASTLE'S counts of nobulae observed on the Franklin-Adams plates may be regarded as referring to the brighter objects of the entire sky. In this count there were tabulated:

Spiral or probably spiral	•			173
Riongated, spindle-shaped, oval		•		233
Dilluso , , ,				51
Small, just distinguishable from a	ter Imagos	•	٠,	327
Total				784

This proportion of 6,5% again points to the number of the diffuse nebulae as of the order of 1000. New objects of the class are occasionally discovered, and doubtless additions will be made in the future, but present photographic surveys of the Milky Way area are of such completeness that no large number of such accessions is to be expected.

4 M N 74, p. 699 (1914)

<sup>&</sup>lt;sup>1</sup> Cl. Ross, Ap J 67, p. 280, Plates VI and VII (1928)

Llok Publ 13 (1918) Lund Modd (I) No 98 (1921)

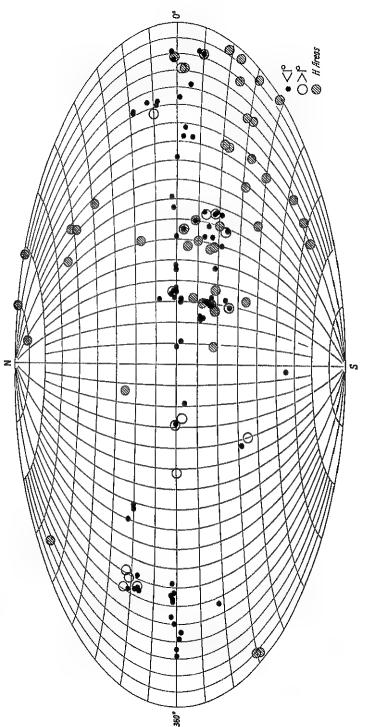


Fig 1 Galactic Distribution of Diffuse Nebulae

7. Physical Characteristics of Diffuse Nebulae. The spectral characteristics of nebulous matter will be treated later in ciph 15, 16 and 25, while reference will be made to the large body of theory based on quantum relationships as applied to the nebulosity of planetaries in ciph. 31 and 32 In the present section will be collected data referring more particularly to the mechanical attributes of such matter, even though it will occasionally be necessary to anticipate in part the conclusions of later sections.

The following subdivisions of the field seem clearly indicated

A Dark nobulae, see ciph 8.

B Coamic Clouds (??), see clph 9

C. Luminous diffuse nebulae

1 Showing emission spectra.

2. Exhibiting reflection or resonance effects

3 Variable in light

Not infrequently several of the sub-classes mentioned will occur in one and the same object. As to outward appearance, etc., the following characteristics may be noted:

- 1. Irregularity In general, there seems to be no such thing as a regular diffuse nebulosity, or one with clear-cut and sharp periphery. The pointed ends of certain fan-shaped nebulosities (see Figure 8; I 59) approach most closely in a definite boundary. In the great majority of cases, however, no sharp and clear-cut boundary can be made out in the random and irregular formations of the diffuse nebulae
- 2. An enormous variation in apparent luminosity. This range is very great; from objects like BARNARD 33 (see Figure 3), which are like a drop of ink by contrast with the brighter regions around, and which are non-luminous or, it best, very faintly luminous, to objects as bright as the Trapezium Region of the Great Nebula in Orion (see Figure 9), for which Wirtz<sup>1</sup> finds an areal brightness of magn. 7,76. His corresponding value for the central part of the Great Spiral in Andromeda is but 8,82.

3. Extreme tenuity. The really significant datum for any theory of the diffuse nebulae (and doubtless for the planetaries as well) is a density almost

vanishingly small (10° to 10°°)

The intimate alliance of luminous and dark matter in numerous diffuse nebulae leads one naturally to a theory postulating similar, or at least closely allied, constitution of the two sorts. Fluorescing or resonating molecules seem a reasonable hypothesis for the luminous diffuse nebulae, and this does not require the assumption of inordinate masses. If one postulates, however, a similar atomic or molecular condition for the matter in the dark diffuse nebulae, it is found that the density necessary to produce the amount of absorption observed requires "excessive" total masses.

While most of the evidence as to the extreme tenuity of diffuse nebulosity is of an indirect nature, it is somewhat surprising that one such line of evidence may be derived from a phenomenon within the solar system. As to the possible density of a swarm of fluorescing molecules, we have no very close analogies in other phenomena, yet the work of Schwarzschild and Kron<sup>a</sup> is very suggestive. In this brilliant piece of research, these authors determined the effective density of the matter within the tail of Halley's Comet on two assumptions, and from photographic data secured at Teneriffe with relatively small and inexpensive apparatus (two identical lenses of 2,5 cm. aperture, used extra-focally!). The

<sup>1</sup> Lund Medd (II) No 29 (1923).

<sup>&</sup>lt;sup>1</sup> Ap J 34, p. 342 (1911)

second of these postulates assumes that the light in the tail of this comet is given off by fluorescing molecules with a radius of the order of 10<sup>-8</sup> cm. Though there is evident danger in comparing fluorescing molecules so different as may be the s in a diffuse nebula and in a comet's tail, the analogy is illuminating and in not be rejected as an impossibility. For the density in the tail of HATLIY Comet, on this assumption, is 4 · 10-21.

Further induced evidence, pointing to densities vanishingly small, may be derived from mass limitations. We may assume for the distance of the torus Nebula in Otion a quantity of the order of 103 ly, a rough mean of the date minations of several investigators. The tremendous diffuse nebulosity which fills most of the central portion of the constellation of Orion, of which the will known Trapezium Nebula (1976) is but a bright minor part, can scarcely contain less than 105 cubic ly (1088 cm 3) if at the distance adopted With a density of 10-24, the mass of the entire structure would then be about 10 · O. a very moderate total If, however, the effective density were as great as 10<sup>-15</sup>, the mass involved (ca 1010 · O) would be so great as to dominate the gravitational motions of all

this portion of our galaxy

Allied with the subject of finely divided matter in a state of vanishing tenuity, the question of "stationary" or "inter-stellar" gaseous clouds should be briefly touched upon. There is manifestly a possible contradiction in any such correlation of two presumably different states of matter, even two different sorts of matter For the inter-stellar clouds of this type are detected through the behavior of the lines of ionized calcium or sodium, whereas these have not yet been discovered in the spectra of either the diffuse or the planetary tyre. of nebulosity Eddington, Gerasimovič and Struve, and others have postulated the existence of uniformly distributed diffuse matter in inter-stellar space, with densities of 10-24 (EDDINGTON), or 10-26 (GERASIMOVIČ and STRUVI), and temperatures of 10000° to 15000° abs, as defined by the molecular specife At such temperatures, while most of the Ca will be in the form Cani. there should be one part in 3000 of Carr, one part in 2 · 100 of Naz, and one part in 2 · 10° of Ca<sub>1</sub> It was calculated that this amount of Ca<sub>11</sub> should show absorption in a thickness of ca 3 1012 l.y This should theoretically show in all Main. though the strength of the stellar H and K lines of Ca makes it practically impossible to detect this in stars of types later than B5, unless the star is a linux of large range, or has a peculiar velocity of the order of 100 km /sec. There should also be a correlation between the distance of the star and the intensity of the absorption

PLASKETT and PEARCE in a series of brilliant papers, have studied the behavior of the Ca<sub>H</sub> lines in a list of 261 stars of types earlier than B5, marly all of which are close to the galactic plane and within the Milky Way structur. The results are tematkable The speed and direction of the solar motion comes

(1928)

2 If uniformly distributed at the first density named, the total mass within a spheroidal

Throughout this treatment, in the interests of uniformity, ionization will be represented by the Roman numeral subscripts alone, that is, the designation for the spectrum only will

be employed, and we shall write, for example, On instead of O+++

<sup>&</sup>lt;sup>1</sup> Proc R S London 111, p 424 (1926), Ap J 69, p 7 (1929), 65, p 163 (1927); 67, p 151

galaxy 10000 l.y thick and 60000 l y in diameter would be ca 6 · 1010 ©

Strictly speaking, Ca++ should be used for the state, and Cam for the spectrum corresponding to that state The subject is involved in a good deal of confusion at present on the nomenclatural side, there is a tendency on the part of some physicists to abandon the use of the + sign, and it seems probable that this will eventually be abandoned entirely. though there is as yet no international agreement on the subject

Publ Astroph Obs Victoria 2, p 335 (1924), M N 84, p 80 (1924), 90, p 243 (1930)

out practically the same as that determined from naked-eye stars in general, though the apex is displaced about 20° to the eastward. The K-term for these inter-stellar clouds is negligible. A rotational term, 1A, of 7,9 km /sec., seems indicated Assuming for the factor A the value 0,0052 km /sec per ly., a center of gravity is found for the inter-stellar clouds at a distance of 1400 ly and in longitude 335° This inter-stellar matter is found to be uniformly distributed, and the mean distance of the stars treated is twice that of the clouds.

For the dark clouds in Taurus, with apparent dimensions about 9° · 3°. PANNEKOEK1 derives a distance of 450 ly, giving an actual area covered about 20.60 ly. From probable assumptions as to the absorptive power of a gas, he finds that a gas would have to have a density of 10-15 to produce an absorption of 2 magn. But with this density the total mass of the Taurus dark clouds would be 4 · 10 · O, which would be expected to have a marked effect upon the motions in this portion of the galaxy Such a gaseous absorption would also be expected to exert some selective action on the spectra of stars observed through it, all of which leads PANNEKOEK to regard a cloud of material particles as the more probable state

C. SCHALÉN\* has investigated the dark nebulae in Cepheus through an analysis of the spectral types of the stars in this region. He derives three dark nebulae at different distances: 1 absorption 0,3 magn., distance 810 Ly., 2. absorption 0,6 magn, distance 1920 Ly; 3, absorption 1,5 magn., distance 2600 Ly The extended investigations of TRUMPLER and L. T. Slocum on ab-

scriptive matter in our galaxy should be mentioned here. Both authors find

a coefficient of absorption amounting to 0,0004 magn. per Ly

II, N. Russell has investigated the theory that the dark nebulae consist of finely divided matter, i c., fine "dust" In a cloud composed of spherical particles of radius r and density q, distributed at random so that the average quantity per unit volume is d, the extinction of a ray of light in passing through such a cloud will be a stellar magnitudes per unit of distance, where a is given by the equation:

 $s = 0.814 \frac{qd}{q\tau}.$ 

In this equation, q is a factor introduced to take care of the variation when the particles are of dimensions comparable with the wave-length. It is nearly unity for particles larger than 2 to 3 wave-lengths, and a maximum, 2,56, when the circumference of the particle is 1,12 times the wave-length. For visual light the maximum opacity occurs when the radius of the particles is 0,086  $\mu$ , and a cloud of rock particles of this size and density 2,7 will exert an absorption of 4 magn. if it contains but 0,0116 mg./cm. in cross-section, regardless of its thickness.

RUSSELL further suggests that this matter is repelled from the stars by radiation pressure, the giant stars being the main cause of such repulsion. The gravitational action of the cloud itself is regarded as the force which holds it together. An extinction of 10 magnitudes (quite sufficient for opacity) would

be produced by particles 144 \mu in diameter.

On Russell's highly reasonable theory, diffuse nebulae would be composed of two sorts of matter 1, actual minute particles which would provide for the opacity of the dark nebulae without the postulation of inordinately great masses, and, 2. Intermingled atomic or molecular matter which by reflection, resonance, or fluorescence produces the observed intrinsic luminosity. On this theory,

<sup>&</sup>lt;sup>1</sup> Amsterdam Proc 23, No. 5 (1920).

Lick Bull 14, p. 154 (1930).
 Wash Nat Ac Proc 8, p 115 (1922).

Ups Medd No. 50 (1930) 4 Liok Bull 15, p 123 (1931).

BARNARD's dark spot in Ophiuchus, if 500 ly distant, would need to have a total mass only about equal to that of the sun See further ciph 8 and 42

8 Dark Nebulae<sup>1</sup> A very considerable number of areas of dark nebulosity or occulting matter have been observed in our own and in neighboring galaxies

Such dark nebulae are of the following modes of occurrence, though it is not maintained that these are necessarily a manifestation of the same phenomenon

1 Dark spots seen against the luminous background of large diffuse nebulae;

type example 6523 (M8 Sagittain)

2 Similar isolated spots seen against the background of the stars type example, Barnard's Dark Nebula at 17<sup>h</sup> 57<sup>m</sup>, -27° 50′

3 Peripheral occulting matter surrounding masses of luminous diffuse nebulosity, as shown by diminution of star density, type examples, 7000 (America Nebula), the dark lanes extending from the nebulosity II 5146 about  $\varrho$  Ophruchi.

4 Larger areas of occulting matter as indicated by decreased density of

stellar distribution, of the references in the preceding Section

5 Calcium clouds in space, as evidenced by the behavior of the calcium lines in certain stellar spectia

6 In other galaxies, the evidences of peripheral occulting matter so frequently

seen in edgewise spirals, cf ciph 42

Whether any of the numerous dark or obscuring nebulae are entirely non-luminous is an open question. It is quite possible that we have, throughout the class of the diffuse nebulae, a regular progression from objects giving no light whatever to objects of the intrinsic brightness of the Nebula in Orion, and that a division of the group into bright and dark objects is superfluous. These dark nebulae are best seen by contrast, set off and accentuated by the luminous background of the Milky Way or of bright nebulosity. In some of these cases it is possible that the apparent lack of all luminosity is only subjective, rather than real. Certain it is that Barnard has recorded the detection of exceedingly faint luminosity in most of the so-called "dark" nebulae.

In distribution, the dark nebulae, like the luminous members of the class,

are definitely galactic, as may be seen from Figure 2

It seems certain also that we have to do with essentially the same sort of material in both cases, as is evidenced by the very frequent occurrence of the two sorts, luminous and non-luminous, in the same object

One of the most striking examples of this alliance is exhibited in the nebulosity south of & Orionis<sup>3</sup> This remarkable region contains the bright diffuse nebulae 2023, 2024, I 431, I 432, and I 434, and the dark nebula BARNARD 33, which projects into and seems to be nearer than I 434. The main feature of this remarkable region is the long wisp-like diffuse nebula I 434, which extends for

<sup>2</sup> J C Duncan, Bright and Dark Nebulae near & Orionis Photographed with the 100-inch Hooker Telescope Ap J 53, p 392 (1921) Cf also, W II Pickering, Harv Ann 32, p 66, and Plate III, Fig 3 (1895), I Roberts, Ap J 17, p 74, with Plate IV (1903), M Wolf, M N 63, p 304, Plate 11 (1903), J E Kerler, Lick Publ 8, Plate XIII (1908), E E Barnard, Ap J 38, p 500, Plate XX, Fig 1 (1913), H D Curtis, Lick Publ 13, p 23, and

Plate II, Fig. 5 (1928)

<sup>&</sup>lt;sup>1</sup> E E BARNARD, On the Dark Markings of the Sky with a Catalogue of 182 such Objects Ap J 49, p 1, 360 (1919), Catalogue of 349 Dark Objects in the Sky Carn Inst Publ No 247 (1928), Ap J 31, p 8 (1910), 38, p 496 (1913), Pop Astr 23, p 596 (1915), W S Franks, M N 65, p 160 (1905), 90, p 326 (1930), T E Espin, Dark Structures in the Milky Way R A S Can 6, p 225 (1912), 16, p 218 (1925), Investigation of Star Gaps with a Catalogue of 202 such Aleas, M Wolf, A N 161, p 130 (1903), 219, p 109 (1923), 223, p 89 (1925), M N 64, p 838 (1904), Seehger-Festschrift (1924), p 312; K Lundmark, Ups Medd 12 (1925), J G IIAGEN, A N 224, p 421 (1925) See also references under ciph 9, II Knox-Shaw, Obs 37, p 98 (1914)

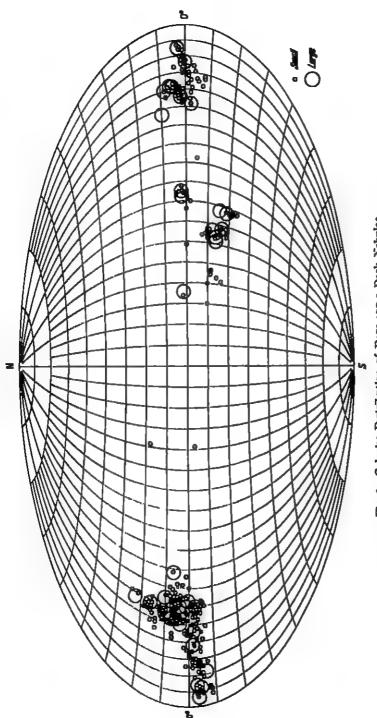
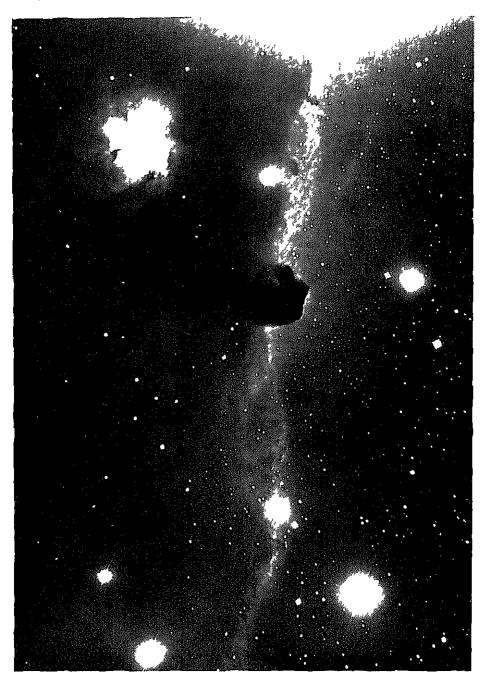


Fig 2. Galactic Distribution of BARNARD a Dark Nebulae.



Tig 3 Dark Nebula south of Zeta Oitonis (Barnard 33, near 1431) (Mt Wilson graph)

nearly 1° to the south of  $\zeta$  Orionis. To the west of this is very faint, tex diffuse nebulosity and numerous faint stars, to the east lies a large area

nebulosity, with very few stars showing. From this dark area a "bay" about  $4' \cdot 5'$  juts across I 434 at a point about 30' south of  $\zeta$ , this is quite clear-cut and dark except for a small wisp in its northern portion, while the transition from dark to luminous matter is very abrupt at the western and southern edges, resombling nothing so much as a blot of ink. Even at these western and southern edges, however, the largest scale photographs show a very narrow run of luminous nebulosity belonging to the dark "bay" rather than to I 434 beneath it

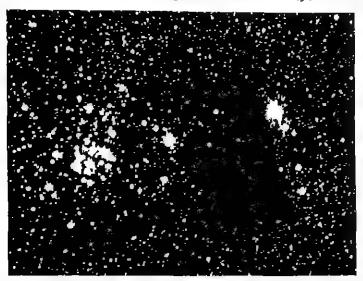


Fig. 4. The Dark Nebula Hannard 86 ( $\alpha = 17^{h} 57^{m}$ ,  $\delta = -27^{o} 50^{o}$ ) (Lick Photograph.)

Duncan suggests that four distinct types of diffuse nebulosity are exemplified here 1. the ropy, branching nebulosity of I 434, 2 the more compact nebulosity of 2024; 3. the nebulous stars 2023, I 431, 432 and 435; 4 dark nebulosity, best exemplified by Barnard 33 described above

Numerous larger areas are known where occulting nebulosity is more or less clearly indicated. Among these may be mentioned the Northern "Coal Sack" (20h 56m, +51°30'); BARNARD 144, described as a large, semi-vacant region 6°·3°, the area about 3° in diameter southeast of θ Ophiuchi (BARNARD 78), where an exposure of two hours with the Crossley Reflector shows almost a stellar desert, or the region at 18h 55m, -37°, of which Knox-Shaw says¹, "There are as many as twenty réseau spaces (each 5′ 5′) in which not a single star appears on a two hours' exposure with the reflector. These dark spaces are especially noteworthy as the region can not be said to be in the Milky Way, being 19° from the galactic plane and well away from the visible star clouds"

9. Cosmic Clouds. Vastly greater areas of alightly occulting dark matter or very feebly luminous nebulosity have been catalogued by HAGEN and his associates.

<sup>&</sup>lt;sup>1</sup> Holw Bull No 9 (1912)

<sup>2</sup> J G Hagen, A N 213, p 351, 214, p 449 (1921), 225, p 383 (1925), 227, p 391 (1926), A N Jub-Nr., p. 13 (1924), M N 81, p 449 (1924), Scientia (1922), p 185, Mem S A It (3) 1, p 9 (1920), Publ A S P 39, p. 167 (1925). Att Pont and Speo Vet persim (1922 and fl), G Aretti, Universo 9, No 4 (1928), shows that the Barnaed-Hagen idea of dark nebulae was anticipated by Seccili in 1877, F Breker, A N 223, p. 303 (1925), 225, p 129 (1925), 224, p. 113, 235 (1925), J. Hartmahn, ibid 229, p 61 (1927), J Hopmann, ibid 238, p 285 (1930), W 1' Rigge, I'up Arit 30, p. 203 (1924), J Stein, V J S 61, p 250 (1926), C. Wietz, A N 223, p 123 (1925); K Haidrich, ibid 241, p 397 (1931)

to which he has given the name cosmic clouds. These areas are often very large, 30 to 50 square degrees, and certain parts of the sky are held to be



Fig 5 The Dark Nebula BARNARD 72 (Yerkes Photograph)

almost completely covered by them Becker¹ gives in the final column of his General Catalogue the degrees of obscuration caused by obscure nebulae in the

<sup>1</sup> A Preparatory Catalogue for a Durchmusterung of Nebulae Spec Vat 13 (1928)

same field of view with the entry, on a scale of increasing density from I to VI There are apparently none of the 4100 NGC entries in the main catalogue which are not affected in this way! This is regarded as confirming the fact that the cosmic clouds are not a galactic phenomenon. If one will refer to HAGEN's chart<sup>1</sup>



1 kg 6. The Diffuse Nebula NGC 6514 (Trifid) (Lick Photograph)

it will be found that in the portion of the lune bounded by  $\delta = +45^{\circ}$  to  $\delta = +90^{\circ}$ , and  $\alpha = 130^{\circ}$  to 230°, the area which Hagen holds to be covered by cosmic clouds is at least 75%, or about 3000 square degrees. These clouds seem actually to aliun the Milky Way, Hagen locates comparatively few in the Milky Way structure (cf. in this connection the chart of distribution of Barnard's dark nebulae, Figure 2)

<sup>&</sup>lt;sup>1</sup> MN 71, p 434, Plate 9 (1921).

The status of the cosmic clouds postulated by HAGLER is still (1931) in doubt He has pointed out that Hirschill's large areas of diffuse nebulosity (52 suc were noted by Hirrschief, but the number is 45, as 7 regions were counted twice coincide with certain of the cosmic clouds he has observed1

On the other hand, attempts to corroborate Hagen's results by phote graphy seem to have been uniformly unsuccessful. Hormann has supporte these appearances by analogies drawn from the photography of faint nebulae coming to the conclusion that the eye, in observing extended areas, has sensitivity about five magnitudes fainter than can be detected with a large reflector photographically (?)

HARIMANN, from some indications that the cosmic clouds may be actuall faintly brownish or reddish in color, has suggested the use of extremely rapi lenses plus a color-filter as a possible means of securing a photographic recon-Wiriz holds that these appearances are subjective, rather than objective, an represent in reality the contrast with the apparent brightness of the varior celestial backgrounds2 Ivanov3 failed to photograph the cosmic clouds note by HAGEN and BLOKER in the regions of V and W Diaconis, and R and S lam

Haidrich describes in detail an extended series of aftempts to photograp the cosmic clouds by means of plates hypersensitized in the green. He record tailure in all attempts save one, taken with an 1 - 1-4,8 Zerss triplet of 104mm aperture, on which he believes he has secured a faint record. Numerous observe have felt that HAGIN's observations should be repeated by other investigator with other instruments, and in other climates. Some such corroboration scen indispensable before the cosmic clouds, of the number and extent assumed, G be regarded as completely substantiated

The Tartu counts of about 250000 stars to phot magn 14,5 on the Par Astrographic Charts<sup>6</sup> were at first thought to give a considerable measure of support to HAGEN's results. In a belt 2° wide at  $\delta = \{2\}$  Opin catalogue 196 obscured regions. From these counts it was estimated that the entire slwould show some 14000 similar patches and that, were this obstructing materi removed, about five times as many stars would be visible in low galactic latitude

SHAPLLY<sup>6</sup> has remyestigated this question with plates of longer exposu on twenty-two of the Paris regions which had been employed in the Lartii count taken with the 21-inch and 16-inch refractors, and showing stars from one three magnitudes fainter than the Paris Charts. A real obscuring nebulosi should conceal such fainter stars much more effectively. Than would be the ca for magn 14,5. While left Eukik's counts to that magnitude were in all cas verified, and her localized vacancies and clusterings complorated, it was four that the count to fainter stars in practically all cases obliterated such loc megularities. On the Harvard plates covering the same regions as the twenty-ty selected Paris charts, seven clusterings and twenty eight obscinations we surveyed, together with the surrounding unaffected areas. When laint sta alone were considered, all of the clusterings and all but four of the obscuratio disappeared

Shapti y<sup>7</sup> has secured similar negative results from the Harvard star cour on the region of X Cancii, reported by HAGLN\* to be surrounded by cosn clouds. Surprix concludes from these results, as did Wiriz, that Habit

<sup>&</sup>lt;sup>1</sup> M N S6 five papers (1926), 87, p 1 (1927) <sup>2</sup> A N 224 p 267 etc (1925) 
<sup>8</sup> M V B M No S, p 57 (1927)

M N 86 live papers (1920), 177 8 M V B M No 8, p 57 (1927)
 A N 224, p 267 etc (1925) 8 M V B M No 8, p 57 (1927)
 e g, I undmark, Publ A S P 34, p 191 (1922), Hagi n's reply, ibid, p 321
 b Opik and Ful M I ukk, Publ Lattu (Dorpat) 26, No 2 (1921)
 Harv Circ 281 (1925) 7 Harv Bull 831 (1926) 8 A N 225, p 383 (1926) 8 A N 225, p 383 (192

cosmic clouds are apparently observable phenomena, but are merely the effects, in general, of the uneven distribution of the stars brighter than the lifteenth magnitude, and that, except in well-known nebulous regions near the Milky



Fig 7 NGC II 5146 This object combines luminous and non-luminous diffuse nobulosity, shown clearly in its structure and in the marked falling off in the number of stars at its periphery (Mt Wilson Photograph )

Way, the obscurations suggested by the Tartu investigations are apparent rather than real.

10 Distances and Dimensions of Diffuse Nebulae Direct determinations of the distances of the diffuse nebulae by the parallax method are manifestly impossible because of the lack of sharp definition in the configurations of the



Fig 
The Diffuse Nebula NGC I 59 (Northeast of γ Cassiopeiae) (Lick Photograph)

two main classes seen, irregular and texturcless clouds, or tangled masses of wisps and streamers. It is evident that the distances of these objects can only be derived by indirect methods, and on the basis of more or less probable analogies or extrapolations. As the stars involved in such nebulosities have been found to be mainly of the earlier types, reasonable assumptions as to the average

distances of such stars of the given type and magnitude furnish an approximation to the distance of the nebula. Similar indirect evidence may be secured from star counts, in the case of dark nebulae, from the radial velocities and proper motions of involved stars, when available from involved variable stars<sup>1</sup>, etc.

Variables in Diffuse Nebulae.

NGC	Number	Magn.	Discoverer
2264	20	14 (max.)	Wolf, A N 221, p. 379 (1924)
6514	3		1.AMPLAND, Pop Astr 27, p. 32 (1919); Publ ASP 33, p. 267 (1921)
6727	1	8,6-10,5	INNES, Union Circ 33 (1916)
7023	2	<u> </u>	Perrine, Lick Bull 1, p. 187 (1902)
1 405	i	-	Harv Bull 786 (1923)

Table 1. Distances of Diffuse Nobulac.

NGC	٥	3	Туре	Distan <b>c</b> e la 1 y.	Ohs.
281	(jii 47 <sup>m</sup> ,4	+56° 3′	Diffuse ·	1 5- 1	L (Lundmark)
I 59	0 50 7	-1-60 11	Diffuse	250	L L
II 1805	2 24 ,5	-1-61 3	Diffuse		Gingricii
I 348	3 38 ,2	- -31 31	Diffuse	350 540	L
		1.01	Pleindes	350	L
-	3 41	- -24	Dark neb.	460	L
	3 25	- -28	Star + neb.	2300	Ĺ
I 405	5 9 7	-1-34 21	Neb. + cl. + lane	1500	Ĺ
I 410	5 16	+33 23	Neb. + cl.	3200	Ĺ
I 417	5 20	+34 12	Diffuse	large	L
2070	5 39 5	69 5	Orion	900	L
	5 30	- 5 <b>27</b>	CALION		BERGSTRAND
ì			}	600	KAPTEYN
				1800	TRUMPLER
		-[-20 31	Diffuse	3600	L
2175	6 3 7	- -20 31 - -10 32	Neb. star	3200	Ĺ
I 446	6 25 .3		Cl, - - diff. neb.	800	i.
2245	6 27 ,2	, -	Cl. + neb.	1500	Ĺ
2237	6 27	+ 5 0	Var. neb. + star	large	L
2261	6 33 .7 6 35 .5	+ 6 59	Br. + dark nob.	3300	L
	177	1 -12 11	Neb. star	1100	1.
12° 2771	7 0,6 40 41,2	- 59 9	n Carinae	2200	1.
	1	-65 28	Neb. + stars	1100	L
5189	13 26 A 16 14	-19 <b>5</b> 9	Dark neb. + star	550	1
	16 20	-25	ρ Oph. region	460	I.
6514	17 55 7	-23 2	Triffid neb.	550	L
0314	17 55 ,1	-27 50	Dark neb.	4000	L
6523	17 58 4	-24 20	Diff. M8	1600	L
(1343	18 11	-19 43	Dark neb. + star	3300	L
	18 9	18 15	Dark nob.	1600	L
6618	18 15	-16 14	Diffuse	3600	L
	18 55	-10 52	Dark nob. + star		L
-	18 55	-37 6	Neb, region	400	L
	19 14	+ 7 32	Dark nob.	650	L
	19 35	+10 20	Dark neb.	1300	L
_	19 54	+34 30	Dark neb.	1600	L.
7000	20 50	- -44 0	Diff. (America)	620	L
7000	} ~~~~	1	1	560	Buch-Anderson
	1	1		220	DUNCAN
7023	21 0 ,5	+67 46	Diff. + dark	650	L
-	21 35 0	+67 42	Ncb. star	360	L
	21 35 .9	+57 2	Br. + dark + cl.	3600	L
-	22	+59	Copheus, dark		O SCHALEN
7635	23 16 .5	+60 39	Nob. star	4100	L

<sup>1</sup> LUDENDORFF, Handbuch VI, Chap. 2, p. 243.



lig 9 The Diffuse Nebula NGC 1976 (The Great Nebula in Orion) (Lick Photograph)

The approximate distances of a number of typical diffuse nebulae, both luminous and non-himmous, are given in the preceding table. Nearly all the values have been derived by Lundmark<sup>1</sup> by various induced methods, a few

<sup>1</sup> Publ ASP 34, p 40 (1922)

ave been added from other sources. The majority of the values given must

regarded as subject to very large uncertainties.

The actual dimensions of many of the larger diffuse nebulae must be neasured in tens or even hundreds of light-years. On the basis of the estimated listances given in the table above, 6523 (M8) will be about 11 Ly. long; the america Nebula (7000) must extend over  $40 \pm {\rm Ly}$ .; the very large faint nebulosity in the constellation of Orion must be over 400 Ly. in diameter, etc.

11. Luminous Diffuse Nebulae. The salient characteristics of the diffuse achulae: indefinite and random structure; extreme tenuity; general association with stars; and galactic distribution, have been noted in the preceding sections. In proceeding from such more mechanical qualities of structure and form to the acts of their constitution as exhibited by their spectra, the peculiarity is at more met that the diffuse luminous nebulae show two sorts of spectrum; one howing emission lines, and another sort resembling the spectra of the involved tars, ascribed to reflection or to some sort of resonance effect. This will necessitate a separate treatment.

There seems, furthermore, no reason to doubt that the spectra of the plantary nebulae and those of the diffuse nebulae which show bright lines are caused by the excitation of the same sorts of matter, for the most part in similar conditions is to density and ionization. This similarity has been well put by W. Fl. WRIGHT!: The spectra of the planetary nebulae differ much more among themselves than one of them do from the spectrum of the Orion Nebula. Whether or not the spectral similarity which exists between the planetaries on the one hand and the Drion Nebula on the other indicates approximate equality of physical constitution lepends upon the sensitiveness of the nebular spectrum as an index of the state

of its source."

In spite of this similarity in the spectra of the two classes, however, it has been thought best, with the aim of segregating the pertinent data of each class, o treat the spectra of the diffuse nebulae and the planetaries separately. The mission spectra exhibited by certain of the diffuse nebulae will therefore be given in eight, 45, and this matter will be repeated, with the addition of the eries relationships and ionization potentials assigned by BOWEN, under the planetary nebulae in ciph, 25.

12. Proper Motions and Internal Motions (Visual). The older literature of the subject contains numerous references to researches attempting to show thanges or motions in the larger diffuse nebulae<sup>2</sup>. These attempts were based upon the often vague and inaccurate visual descriptions of earlier observers, and are now of value only as examples of energy and perseverance unfortunately

lirected.

Though the advent of the photographic process has given a far greater degree of attainable precision, the available time interval is still far too short to establish motions larger than the unavoidably gross errors of measurement of the ill-defined wisps, streamers, or other structural features of the diffuse nebulae. Aside from apparent changes due to light variations in a few variable diffuse nebulae, there seem to be no certain evidences of structural changes detected as yet. Lampland has pointed out that the intricate structure and

<sup>1</sup> Lick Publ +3, p. 262 (1918).

4 Publ A S P 28, p. 192 (1916).

<sup>2</sup> c. g. E. S. Holden, On the Proper Motion of the Trifid Nebula. Amer J Sc 34, p. 433 to 458 (1877)

The classification of the "Crab" Nobula, 1952, is somewhat uncertain. The changes which Duncan has noted in this object will be described later in ciph. 27.

definite character of some of the delicate filaments in the diffuse nebula 6992 [the beautiful "Net-work Nebula" in Cygnus, cf. Lick Publ 8, Plate 63 (1908)]

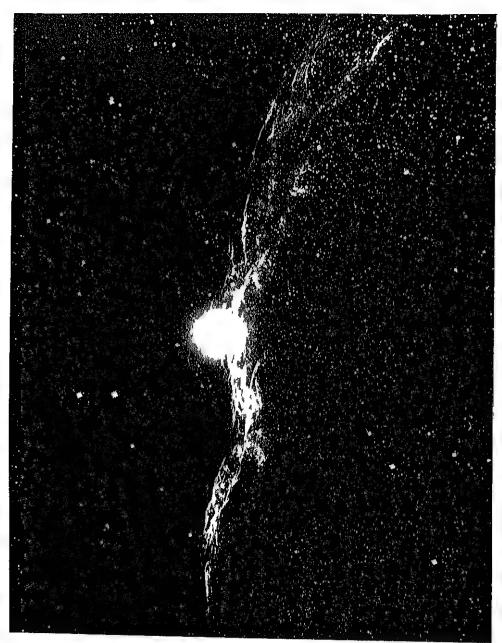


Fig 10 The Diffuse Nebula NGC 6990 in Cygnus (Mt Wilson Photograph)

should make it possible to detect comparatively small motions, and has studied two plates of this object separated by an interval of about 14 years. He states

that there are apparently elight displacements in small portions of some of the filaments in the southern part of this nebulosity. Duncan notes several new filaments found at the northern end of the "nebulous wreath in Cygnus" 1 CURTISE made measures of features in 10 large diffuse nebulae on Crossley plates with a time interval of about fifteen years, with the conclusion, "the most that can be said, both from the measures and from careful examination, is that there has pretty certainly been no change in the intricate formations of these enormous objects as large as one second of arc during the past fifteen years",

18 Radial Velocities of Diffuse Nebulae Such of the lummous diffuse nebulae as have an emission spectrum, with much of the light concentrated in a few bright lines, are suitable for radial velocity determinations, unless too faint. a condition which unfortunately prevails. Observing the Nebula of Orion in 1872, Huggins' determined the position of the chief nebular line as 5005 A. he attributed it to nitrogen, and ascribed its displacement as due to a recession of the Orion Nebula from the sun MAUNDER's attempts on the same nebulas

showed variations too large to permit any definite conclusion

It remained for KERLER® to secure the first definite radial velocity results on nebulae. He employed a grating spectrograph attached to the 36-luch refractor at Lick Observatory, using the third or fourth order. He determined the radial velocities of the Orion Nebula and of thirteen planetaries. When it is recalled that this was done visually, in the "prehistoric" days of the spectroscopic method, and that his values are in close accord with later spectrographic results. his achievements in this field must be regarded as an observational triumph (on Orion Kickler, -+17,7 km./sec , CAMPBELL and MOORE, -+17,5 km./sec )

Very few radial velocities are known for diffuse nebulae. From the descriptions, 5 nebulae in the Greater Mugellanic Cloud may possibly be of the diffuse type, these have the mean velocity of the Cloud, 4-276 km/sec. Others are

	=	•
	Object	l' (situ's motion removed)
Orlon		0,1 km /sec
3372	y Carinno	. —s
6514	(Irifid Nebula)	+21
6523	(MR Sagitturii) .	-1 8
664B	(Horacshop Nob )	4 20.7

14. Turbulence Effects in Diffuse Nebulae. Although radial velocities are known for but a few diffuse nebulae, in one case we possess fairly accurate knowledge of the relative motions of different portions of the same nebula, that of Orion KERLER (loc cit ) had earlier considered the question of relative radial velocity in different parts of the Orion Nebula, but obtained negative results He estimated that differential radial volocities as great as 8 km /sec, in the brighter parts of the nebula would have been detected. VOGEL and EBERHARD? found evidences of differential velocities in the Orion Nebula, indicating that the radial volocities of the material east of  $\theta_1$  Orionis was 5 or 6 km/sec larger in the positive sense than that of the material 0'.6 west of this star.

Mt Wilson Year Book No 29 (1930)

Proc R S London 20, p 383 (1872) Groenwich Spectr and Phot. Results (1884 and 1887)

H D CURTE, Proper Motions of the Nebulae Publ ASP 27, p 214 (1915) In all, CURTIB made measures on 150 objects of the various classes, based on Crossley negatives with time intervals averaging about 15 years. Curtis is since convinced that the probable errors of monsurement on such vague and diffuse elements or nebulous nuclei are vastly larger than the quantities sought. He therefore now regards the numerical results derived in his paper as meaningless, and relegates them in the status of the older visual comparisons

Lick Publ 3, p 165 (1894)
CAMPDELL and MOORE, Lick Publ 13, p 77 (1918) \* Ap J 15. p 307 (1902).

Our modern results on this nebula are due to the brilliant application of the interferometric method by Buisson, Fabry and Bourger and to the detailed and accurate spectrographic survey of the Orion Nebula by CAMPHELL and Moore 2.

The French investigators, with high technical skill, made use of an interferometer with a preliminary telescopic magnification (80  $\times$ ), so that the resulting interference rings formed a picture of the chosen region, an area about 4' square about the Trapezium. Measurement of the diameters of the interference rings will then give, first, the mean radial velocity of the nebula as a whole by using some known radiation as  $H_{\gamma}$ ; secondly, variations in different diameters of a given ring of known (or unknown) source give at once the relative radial velocities of the portions of the nebula covered by this ring; and, finally, certain assumed laws connecting the limiting order of interference with the atomic mass and the absolute temperature make an estimate possible as to the effective temperature of the nebular matter,

The authors measured 58 points on the interference rings, distributed in 12 directions from the Trapezium, and within a radius of about 2'; their resulting mean value for the radial velocity of the Orion Nebula was -1-15,5 km./sec.

As to the turbulence effects observed, they write: "The rings show local deformations in certain regions, indicating, in certain portions of the nebula covering a very small area, irregularities of speed which may amount to about 10 km./sec. Movements of this sort are manifested in the region to the southeast of the Trapezium in the direction of the star Bond 685. Moreover, there are great collective movements; with respect to the mean velocity, the northeast region is withdrawing at a speed of something like 5 km./sec., while the southwest region is approaching at pretty nearly the same speed. In general, the part of the nebula which we have studied has a sort of rotary movement about a line southeast-northwest, but with numerous irregularities."

15 plates were taken, with étalon separations ranging from 0,13 to 2,8 mm. The final values found for the wave-lengths of the chief violet nebular lines are:

> 3726,100 A 3728,838 A.

Next, by the use of the formula,

 $N=1.22\cdot 10^{6}\sqrt{m/T}$ 

where N is the limiting order of interference, m the atomic mass, and T the absolute temperatures, and through the use of étalons of gradually increasing separation, they set the limiting orders of interference as follows:

Hydrogen . . . . . . . . . . . . about 10000 "Nebulium"

This value of the interference limit was regarded as indicating a source of atomic mass about 3 as the origin of the "nebulium" lines. Also, by the use of the same formula, a high effective temperature, in the sense of molecular motions involved, was derived, amounting to 15000° abs.

B This empirical formula should not be taken too seriously, as is indicated by its failure in this case; the atomic mass of O is 8.

The formula in question was derived by Schönrock, Ann d Phys (4) 20, p. 995 (1906), and later, with a slightly different constant, by RAYLEIGH, Phil Mag (6) 29, p. 274 (1915). It involves, in the latter case, a postulated intensity difference of 1/40 (2,5%) as the minimum detectable in the formation of an interference ring. Though in no sense a rigorous formula, the temperatures found are probably of the right order.

<sup>&</sup>lt;sup>1</sup> Ap J 40, p. 241 (1914); cf. also ibid., 33, p. 406 (1911).

<sup>2</sup> Llck Publ 13, p. 96 (1918).

The researches of CAMPBELL and Moore confirmed the results secured by the interferometric method in most respects, but did not support the idea of a general rotation. In all, 86 spectrograms were taken, and the total of the exposures amounted to nearly 400 hours. In an area 2' square about the Trapezium they found a total velocity range of 13,5 km./sec., and interesting plates are given in the work quoted, tabulating the excess or deficiency of radial velocity at the numerous points observed in the nebula. "...a consideration of the charted velocities, especially those in the outer southwestern areas, seems to negative the suggestion of a rotation of the nebula. While the intermediate region from

I' to 4' northwest, west, and southwest of the Trapezium is a region of prevailingly low radial velocities, moderately low radial velocities are to he found also to the northeast, east, and south of the Trapezium . . . but when we consider all parts of the nebula covered by our observations, we are inclined to favor the hypothesis of great collective variations of velocity rather than a rotation as the prevailing factor," Widening of the lines in certain regions suggests that the radiations in such areas may be coming from widely different depths in the nebula, the different strata having different radial velocities. See further ciph, 46 and 28.

15. Luminosity of the Diffuse Nebulae: Gaseous Spectra. A considerable number of the diffuse nebulae exhibit an emission spectrum of the type associated with matter in a gaseous condition. The type example of this class is the Great Nebula in Orion: because of its intrin-

Table 2. Wave-lengths of Lines in the Orion Nebula (WRIGHT).

Nebula (Wright).					
( A 1) k	Intensity	Orlgia			
3704	2	#\$ 3703,9; He 3705			
3712,4	1	Hr 3712,0			
3722	2	Hμ 3721,0			
3726,16	40	O <sub>II</sub> ; B., F. & B., 3726,100			
3728,91	30	O <sub>IG</sub> B., F. & B., 3728,838			
3734	2	HD 3734,4			
3750	3	11x 3750,2			
3771	6	Hi 3770,6			
3798	10	$H\theta$ 3797,9			
3820	1	He <sub>t</sub> 3819,6			
3835,5	15	$H\eta = 3835.42$			
3868,74	40	Uniden tified			
3888,96	40	Πζ 3889,05; He 3888,64			
3964,8	10	11c <sub>1</sub> 3964.7			
3967,51	30	Unidoutified			
3970,08		IIs 3070,07			
4026,2	10	' Hett; flet 4026,2			
4068,62	5	Sit			
4076,22	2	$\mathbf{S}_{IC}$			
4101,74	60	ι Ηδ 4101.74			
4120,6	1 1	110, 4120,8			
4444,0	1	He, 4143.7			
4267.1	[ 1	C <sub>II</sub> 4267,14			
4340,46	100	Hy 4340,47			
4353	1	Unidentified			
4363,21	6	O <sub>III</sub>			
4388,0	4	Het 4388,0			
4471,54	20	11o <sub>1</sub> 4471,49			
4658,2	2	Unidentified			
4712,6	1	1Im, 4713.2			
4861,32	70	IIβ 4861,33			
4922,2	[ 1	11e <sub>1</sub> 4921,9			
4958,91	50	Ont			
5006,84	70	Ont			
5876	-	He			
6563		IIα			

sic brightness, the spectrum of this nebula has been more studied than any other, just as it was the first diffuse nebula in which bright lines were observed visually and later photographed.

In the preceding table are given the lines observed in the Orion Nebula by Wright, Additions to the identifications have been made from Bowen's papers.

<sup>&</sup>lt;sup>1</sup> The Wave-lengths of the Nebular Lines and General Observations of the Spectra of the Gaseous Nebulae. Lick Publ 13, p. 491—239, with many plates (4918). This monograph is the most complete collection of observational data on the gaseous nebular spectrum existing.

These lines will be found also, with the addition of numerous others found in the planetaries, and with screes relationships and ionization potentials, in Table 7. ciph 25

The lines at 5007 A and 4959 A have had a long and interesting history under then older designations,  $N_1$  and  $N_2$  for which the hypothetical source "nebulium" was postulated. The identification of these and other formerly unknown lines in the spectrum of the gaseous nebulae as multiply iomized  $\Theta$  and  $\tilde{N}$ is due to Bowing

It will be seen from the identifications in Table 2 that the more prominent features of the emission spectrum of gaseons diffuse nebulae are  $H_1$ ,  $He_1$ ,  $O_{H_2}$ and  $O_{HI}$ . A single weak line, 4267 Å, is ascribed to C, and two are possibly  $S_{II}$ . Although  $H\alpha$  is visible in Otion, the two lines of  $N_{\rm H}$ , 6548 and 6854 A, so prominent in many planetaires, as well as the weaker lines of  $N_{\rm HI}$  at 4634 A and 4641 A, are not found. The puzzle which had been presented for so many years' by "nebulum" has thus been almost completely solved by Bowen Of the stronger lines, only the two at 3869 A, intensity 40, and 3968 A, intensity 30. remain unidentified

HUBBIE<sup>2</sup> tabulates the following twenty-nine diffuse nebulae with emission spectrum, only thateen of which were known as such before

Table 3 Diffuse Nebulae with Emission Spectra (Hummi)

Number	Pv mag	Pv magn and spectrum of stars involved		n of	kemaks
281	8,6	10,2	Oc	5	4 components of BD 1 55 101
	10,3	11,6	Bo	1	3 stus
I 59	ĺ		(		ban nebulae neary Cass
1491	10,	6	[ Bo		,
1199	1		1		1
1621	13,0	14,0	j Oe	5	3 St., magnitudes estimated
T 405	5,	Ь	Bo	p	Boss 1249,   faint continuous
1952	ſ		[		Also strong continuous
1972	5.1	7.9	Ocs		Orion 4 St. in Trapezium
1982	6,	8	Bu	ը	Bond 734
I 131	1		ĺ		Bay neb near 4 Orionis
202	1		į		Also famt continuous
2175	7.		, Ou	-	BD   20' 1281
2237	7.1	8,2	l Oe	5	1 brightest st_of claster
	J		I ~		Union Circ No. 7 (1914)
2350	117	0	<sub>l</sub> Od		Magn estimated
3372	1		I		
5128	1		!		
6302	Į.		ļ		
6357	1				
6811	7,8	8,5	Oes		Trifid 2 comp of BD 23°338
6523	6.1	6,9	Oct		2 brightest st m M8
6611	8,3	9.2	0.5	Bo	3 brightest at in M46
6618	1				
6888	1,		Į.	1	
6960	13		ľ	ł	Fnormous loop in Cygnus
6922	jj.		]	)	
7000	}			ļ	America uch Cf also Worr Sitzb Heidelb Akad, Abt 27
7635					(1910)

<sup>&</sup>lt;sup>1</sup> J. S. HOWEN, Nature 120, p. 173 (1927), 123, p. 150 (1920), Publ A S P 39, p. 295

<sup>(1927),</sup> Ap J 67, p t (1928)

2 The Diffuse Galactic Nebulae Ap J 56, p 162 (1922), Mt Wilson Coult No 241 (1922). This is the most comprehensive monograph on the diffuse nebular which has appeared to date,

16. Emission Variations. The relative intensities of the lines in gaseous nebular spectra, whether of the diffuse or planetary types, vary in a very striking and puzzling manner, not only in different objects of the same class, but also in different portions of the same object. The Orion Nebula is the most striking example of this phenomenon among the diffuse nebulae.

This variation in the relative intensities of nebular emission lines is a problem which has yet received no entirely satisfactory explanation (see, however, ciph 28, 31, and 32). It is conceivably in some way connected with variations in the extremely low densities of these objects or of parts of the same object, as in Orlon. Modern physics can parallel the enormous temperatures of stars (Anderson's exploding wires), or temperatures near the absolute zero (ca. 1° K.), it can also deal with relatively high pressures. It is unfortunate that the greek occluded from the walls of our laboratory apparatus, as well as the great length of the mean free path, limit us to rarefactions whose ultimate tenuity in perhaps of the order of 40. We and that the presumably very fertile experimental field in densities less than this by factors of the order of 40. We seems forever closed to us. Our stellar and nebular laboratories will long remain our only source of ionization phenomenon in gases of densities vanishingly small.

CAMPBELL and MOORE (loc cit), in their work on Orion, have tabulated a great variety of ratios for the intensities of the  $N_1$ ,  $N_2$ , and  $H\beta$  lines, ranging from  $N_1$   $N_2$   $H\beta = 10$  3.5 for the center of the Trapezium region to 0.0.10 in the neighborhood of the detached nebulosity 1982 in the northeast quadrant, whereas the normal ratio in the planetaries is 10.3.4 CAMPBELL and MOORE, and Wilson, in the work quoted give also the values for the following five

XGC	$N_1$	$N_{\bullet}$	11/1	YIK	N <sub>1</sub>	N <sub>4</sub>	Hμ
1976	10	3	5	(1523	3	1	10
1372	10	1	5	6618	10	- 1	5
6514	3	1	10				

HUBBIE adds data for 12 others

objects

NGC	$N_1 \mid N_2$	IIβ	NGL	$N_1 \mid N_1$	ПĄ
1499	1	2	6611	- 1	1
L 423	i	1	6888	CI CI	2
1 414	0	5	6960 ]		
2024	1	3	6992	U	4
2175	i	1	7(XX)	0	2
2237	2	1	7635	U	5
E428	0	2			

Kerier took perhaps the earliest photographs of the Orion Nebula through a color screen, and found  $N_1$  and  $N_2$  concentrated in the Huygenian region Harthann, by a similar method, corroborated these results, and noted that 1727 A was of much greater extent Slipher worked spectrographically over a large part of the more distant nebulous regions in the constellation of Orion, in general confirmation of Campbell's earlier visual observations, and found that the emission lines decreased in strength till out at NGC 2068 the spectrum was continuous. ". then the variation in the spectrum may be said to begin

<sup>&</sup>lt;sup>1</sup> CAMPBELI'S discovery of this effect in different areas of the Orion Nobula, and Schrimer's attempts to disprove, formed an interesting and lively tilt of the earlier days of the spectroscopic method. Cf. J. Schrimer, V.J.S. (1897), p. 51, Ap. J. (1898), (... Runge, lbkl. 8, p. 32 (1899), Campbell, Whigher, Scharmerle, and Attern, lbkl. 6, p. 363 (1897), W. Campbell, lbkl. 8, p. 317 (1899), 9, p. 312 (1899).

Ap J 9, p 133 (1899) Ap J 21, p 389 (1905)

<sup>4</sup> Publ ASP 31, p 212 (1919)

in the center with the usual emission type which loses strength (different substances differently) with distance outward and ends finally, in the most distant masses, with a continuous spectrum of the normal stellar absorption type." Wright (1921, unpublished) using a quarz shifless spectrograph attached to the Crossley Reflector, found the relative sizes of the monochromatic images  $H\gamma$ ,  $H\beta > N_{1,2}$  The latest determination of variations of state or constitution of the Orion Nebula, made with powerful apparatus (a large objective prism), has been carried out by W. J. S. LOCKYFR<sup>1</sup>. The outstanding feature of Lockylr's plates is the great size of the image due to 3727 A, next in size are  $H\beta$  and  $H\gamma$ , following these in order of size come 5007 A, 1959 A, and 3869 A, which is the smallest of all. The radiation from the Huygeman region is found to be composed almost entirely of hydrogen and  $N_1$  and  $N_2$ , the Messierian branch contains these elements plus 3727 A, the outlying regions are composed almost entirely of 3727 A. Similar interesting variations are noted in the planetarics (see ciph 28), and have formed the basis of the quantum state theories of these objects

17. Luminosity of the Diffuse Nebulae Reflection or Resonance Effects. A relatively large proportion of the diffuse nebulae fail to show any emission lines whatever, or show them at best very faintly upon a background of relatively strong continuous and absorption spectrum. As nebulae with an emission spectrum are more easily identified than those with a continuous spectrum, if of the same surface brightness, Hubbit regards it as probable that diffuse nebulae with continuous spectrum are actually more numerous than those with bright lines. He catalogues 33 diffuse nebulae with continuous spectrum, of which but 8 were known earlier. See Table 4

Table 4 Diffuse Nebulae with Continuous Spectra (Hobbit)

Number	Py migh and spr lusely	etrum of stars ed	Remuks
1333 1 318 Pendes	10,6 8,4 9,8- 10,6	B8 B6 B8—A2 B5	BD   31°643 involved 9 stars Maia and Merope "The whole spectrum is a true copy of that of the brighter stars of the Pleiades" [Strem R, Lowell
	1		Bull 2, p 26 (1912))
	12,5	Iv8	$\alpha = \frac{1^{h} \cdot 1^{h \dot{a}}}{\alpha - 1^{h} \cdot 2^{h \dot{a}}},  \delta = \frac{1}{24^{h} \cdot 32^{h}} \cdot 5 \ln n$ probably a dwarf
1579	12,0 12,2	\n -B5	2 Stars
II 2087	_		
1788	10,0 13,0 <sup>†</sup>	B8	2 stars
11 2118		~	Great neb n p Rigel
1977	16	131	Boss 1361 Stipher [Publ A S P 31 p 214 (1919)] finds spectrum continuous, crossed by a few bright II lines, On absent
2023	7,8	B2	Neb around BD - 2 1345
2068	10,1 -10 8	B5B8	BD FO° 1177 STEPLER (L.C.) finds no bit lines. Spectrum continuous, crossed by II and He absorption, the formet series strong the latter weak, as in advanced B type stars.
-		~*	$ a = 5^h 45^m$ , $ a  + 1^o$ Bightest portion of great "spiral" in Otion

<sup>1</sup> M N 90, p 580 (1930)

(Continued.)

Number	Pv. magn. and spinyol		Remarks
2183	14,0	1 1 1 1 1 1 3	
-	13,5	B1	Bright uncatalogued "comet" neb.
1 - 446	163	' Bi	
1 447	8,1	. Bi	BD +10° 1159.
2215	10,7	131	Bright IIB suspected.
2247	8,8	B2p	Bright $H\beta$ and $H\gamma$ .
2261	var.	Peĉ.	Approximates a nova spectrum Cf. Stipmer, Lowell Bull 3, p. 63 (1918).
	8,2	BI	Uncatalogued neb. about BD 12" 1771.
	3,1	132	Nebulosity about $\pi$ Scorpil.
11 5502	4,2	132	Nebulosity about r Scorpii.
4601	7,1 8,4	B8A0	4 stars.
4603	7.8	132	Neb. about BD - 24° 12684.
4604 4605	5,2 - 5,0	B2- B3     	2 components of ρ Ophiuchi. Stipher, Lowell Bull 2, p. 155 (1916), finds spec- trum continuous and probably like that of ρ. Neb. about 22 Scorpli.
6726	4,9	123	Nep. anour 22 ocorpus
•	7,2 9,4	139	Neb. about BD 37° 13023 - 4.
6727 6729	var.	Gp	R Cor Austr; resembles T Tauri. St.t-
		}	PHER, LOWELT Bull 3, p. 66 (1918), finds weak emission on strong continuous.
6914	9,3 -9,9	B5	BD -  41"3731 and 3737.
7023	7.2	<b>132</b> p	Prase, Publ A S P 27, p. 240 (1915), finds strong continuous crossed by absorption lines. Stapmer, ibid. 30, p. 63 (1918), finds 11 and 11c absorption 4-H emission, which is strong in Hβ, and apparently identical with the star inteedded in the nebula.
7129	10,2 12,4	B3- B8	, 3 stars,
II 5146	10,0	B1	□ BD +46°3474.

The positions given in Tables 3 and 4 are for 1920,0. For data and deductions summarizing the character of the stars involved, see ciph. 19.

18. Variable Diffuse Nebulae. A few diffuse nebulae are definitely known to be variable.

These comparatively rare examples of variable nebulae are of great theoretical interest, and have certain characteristics in common:

- 4. Nearly all are fan-shaped, with a variable or suspected variable at the tip (in T Tauri the star is slightly removed from the tip of the fan).
- 2. All seem to lie in dark lanes or gaps, presumably filled with non-luminous matter.
- No certain correlation has yet been derived between the stellar and the nebular variation<sup>1</sup>.
- 4. The example most thoroughly studied, Hubble's variable nebula, shows no actual outward or other movement of formations.

The irregular and hap-hazard character of the variations in these objects, and the lack of correlation with variations in the involved stars, seem to negative any explanation involving the lighting up of successive regions outward by light pulses from the star. The dimming of the structural features by passing clouds

<sup>&</sup>lt;sup>1</sup> LAMPLAND, however, states in his last paper that 2261 is generally faint at times when the star is faintest.

Viriable Diffuse Schulac

Number	1	, s	Deruption
1555	fh tom,1	19 17'	HINDS VAILABLE REBUILTING the VALIBLE CO. I Long (Md.) bright line). Conspicion in 4570 the rebuil has been very funt since 1900. I arber object the discussed by BALKANAN ALN'S p. 442 (430.). A periodiscussed by BALKANAN ALN'S p. 442 (430.). A periodiscussed by BALKANAN ALN'S p. 442 (430.). The periodiscussed by BALKANAN ALN'S p. 442 (430.). So partially in the periodiscussion of the 100 millional Situated in valuation of the 100 millional Situated in valuation.
2215	6 37 ,2		Bright for shoped in issestingling to theorem upper controlled in the least stellar nucleu (5% 5% little structural detail. The in a drick lane. Variation suspected by Previo. Mt William Contr. No. 186 (1950).
2261	6 33 7	; 8 \$9   -   -   -   -     -	Humar s variable nebula a bright faut larged for a doubt 2' d'extending to the norf the variable R Monroce is (9,5-13'). Humar s plates how no variation in the nucleus, and be found strong containing perfrance Ap. L.H. p. 100 (1017). 48 p. 481 (1017). 28 mars.
3172	Jo 11 ,2	59 9	Nebulosity about y Catmae Tarly discussion with regard to suspected variability of thre object (from visual descriptions only) to be found parential in M.S. 31, 32, 34, and 36. Not confirmed by mobility photographs.
6511	17 56 ,3	21 2	The Trifid Nebula Artifolity suggested by Leaves
6720	16 55 ,2	37 6	Pop Astr 29, p. 631 (1920). Dark in their involved sethint's variable nebula discovered by him at Atlant in 1861, a fair shaped wisp with the varieble R Cor Angraf the tip, and lying in a pronounced dark region. The slat varies firegulary from ca magn. (1,5 fo. 1 y 8 (H av Bull 805 (1921)). Stripin R, Lowell Bull 3. p. 66 (1915). In a 20 hour exposure, found spectrum of noval type No certain correlation between variation of 4 or and of nebulosity. (I also, KNOV SHAW. Helix Bull 1 p. 111 (1915). It p. 182, with plates, (1920). No. 46 (1941). INMER, Dinon Cite No. 33, p. 260 (1916). No. 36, p. 285 (1916). LAMPTAND. Pop Astr 25, p. 650 (1917).

of occulting matter, quite heterogeneous as to density, has been suggested, and derives some measure of support from the location of these nebulae in dark lanes or gaps

A theory put forward with some hesitation by Lampland would ascribe the irregular variations in the nebular luminosity to a huminescence or fluorescence engendered by the passage of the body through clouds of non-luminous matter. This, also, is supported by the milion in which such nebulae are found. There are some very strong objections to such an explanation. 2261 seems to have remained unchanged in structure during all the period through which it has been observed. The theory would then require a density in such dark clouds vastly less than that of the luminous matter itself (10<sup>-24</sup>?), else this would be changed in configuration or even swept completely away by the passage of the non-luminous matter through its structure. Further work is urgently needed on the spectrum and light variation of the involved stars, as well as on changes in the nebulosity, before a satisfactory theory can be derived for these interesting objects.

19. Evolutionary Status of the Diffuse Nebulse. No definite decision can as yet be given as to the precise evolutionary position of the diffuse nebulae Without any precise formulation of the successive steps of the process, and by tacit analogy with early or later forms of the now discredited Kant-Laplace nebular hypothesis, it has long been customary to regard the diffuse nebulae as the first step in the evolutionary process which has formed the stars. Man's mind demands a logical sequence in such an evolutionary process, and it is possible that the insistence of this demand occasionally blands us to the fact that the "logic" of the process may have been injected from our own laws of thought, or by fallacious analogy with totally unalled developmental gamuts. Provided, however, that we cast aside all somewhat vague modern indications of an eternal or cyclically renowed universe, and that we assume an initial state of undifferentiated heterogeneity, it must be admitted that such a theory possesses a measure of sequential harmony, and is to that extent allaring

In roughest outlines, such a theory will run

4 An initial chaos of completely mixed or shuffled primordial elements, a tohu-wa-bohu

2 Gradual and irregular accretions into very rare and tenuous, non-luminous clouds, the axisible creation of matter by "cismic" rays from other already existing sources of radiation, the formation of "dark" nebulae.

3. Development under contraction of higher molecular speeds and "tomperatures", light emission, the luminous diffuse nebulae, containing only a few of the "earlier" forms of matter

4 (cravitational condensation of this luminous nebulosity into the "youngest" stars, the process is nearly finished in such cases as the Pleiades nebulosity, final development within the stars of the "later" and more complex forms of matter, etc.

It is said that ROWLAND jokingly laid down the dictum to a student that if a theory could not be right, the next best thing was for it to be exactly and diametrically wrong. It is not impossible that the rather attractive theory outlined above is exactly wrong. It is at least as probable, a priorl, that the nebulosity surrounding the Pleiades and other high temperature stars may be being emitted, rather than a residue of evolutionary contraction processes

<sup>1</sup> Cf I: W. BROWN, On the Passage of a Star through a Nebula Ap. ] 53, p. 169 (1921)

1

Our best summary of the facts that may bear on any theory of the diffuse nebulae is due to HUBBLE (l. c.). From the average spectral types of the stars involved in nebulosities of the emission and the absorption spectrum types, he has drawn the following important conclusions (cf. Tables 3 and 4 above):

- Stars involved in nebulae having continuous spectrum are nearly all of Class B1 or later.
- Stars involved in nebulae having emission spectrum nearly always have spectra earlier than Class B1, rarely showing any bright lines.

Hubble therefore holds that all nebulae of the diffuse type are intrinsically non-luminous, and that in every case the luminosity of nebulae showing an emission spectrum is excited by an involved hot star of earlier type, while the luminosity of those displaying a continuous spectrum is due to simple reflection or to some sort of resonance phenomenon, from similarly involved stars of later type. "A casual inspection of diffuse nebular structure and configurations of involved stars suggests that the association is for the most part temporary. This may be one fundamental distinction between diffuse nebulae and planetaries, for in the latter the central stars must be permanently associated with the surrounding nebulosity; otherwise their central positions could not in general be maintained."

These significant results introduce another difficulty in the long current assumption or theory that diffuse nebulosity forms the initial stage of stellar evolution. For most modern theories hold that the typical star begins its life as a red giant, of relatively low temperature, reaching the high temperature of the B stars only much later in its life history. If the primordial state of the stellar matter was nebular, and if this process is in some cases still incomplete, the fact that practically no red stars are involved in such nebulosities becomes a very serious objection to the older theory, and one that it seems impossible at present to remove.

There are, however, several very serious exceptions, as admitted by Hubble, to his theory that the light of the diffuse nebulae comes in every case from involved stars. Notable among such exceptions are the America (7000) and Network (6995) Nebulae: vast structures in which no bright stars whatever seem to be physically involved. If such objects are not intrinsically luminous, one can only make the assumption, on Hubble's theory, that the luminosity is in some way engendered from the stars of neighboring regions of the Milky Way.

## c) The Planetary Nebulae.

20. Definition of the Planetary Type. The term planetary has long been restricted to a limited class of relatively small and clearcut nebulae of emission spectrum, possessing a more or less definite spheroidal or annular symmetry with regard to a center which is nearly always stellar. Their apparent dimensions average less than 1', though this is greatly exceeded by some of the giants of the class (e. g., 7293 is 15'·12', and doubtless the largest planetary known); not a few of the genus are so small as to be apparently stellar in large telescopes. In apparent surface luminosity, they range from objects with the brightest nebular matter known (7009, 7027) to faint disks several hundred times less intense, which leave only a slight impression in an exposure of two hours (7139). While there are some exceptions to the rule, the typical planetary has a central star, whose apparent luminosities range from the 9th to the 19th magnitude, or fainter.

21. Number and Distribution of the Planetaries. In distribution, the planetary nebulae are definitely galactic, with a marked concentration in the Milky Way regions from  $\alpha=18^h$  to  $20^h$  See Figure 11

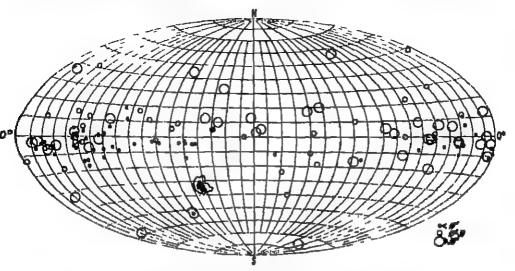


Fig 11 Calactic Distribution of the Planetary Nebulae. It will be noted that these distant from the galactic plane are in general the targer members of the group, which are presumably these. The smaller and more distant objects are closer to the galactic plane.

Pewer than 150 objects of this class are at present known, nor does it seem probable that future surveys will add greatly to this total. The most complete collection of data on the planetary nebulae yet published will be found in Volume 13





If 12a and b The Planetary Nebula NGC 6720 (Ring Nebula in Lyra) (Lick Photograph )

A photograph of the object is shown at the left, at the right is a sketch by Courts showing the intricate structure

About 135 are noted in the NGC lists as planetary or passibly planetary. A few have since been discovered by Humason, Humble, Prant, Innes, Jonekhere, Curtis, and others. At the time of publication of Vol. 13 of the Lick Publ. (1918), but 78 were known morth of declination.—34° The following considerations indicate that no great increase in the number of planetaries is probable.

1 To tost this point, Curris examined with a slittless spectroscope (filek Publ 13, p. 73) 79 small objects within 25" of the Milky Way which have the NGC descriptions, small, very

2 The rayion of the Drafter Catalogue increased the number of listed stellar spectra.

1 Troin 9(xx) to 227(xx) But one new object with a planetary spectrum was found.

of the Publications of the Lick Observatory, 1918, to be referred to henceforth as Lick Publ 13, with the omission of the date. It contains the following monographs:

Part III. The Planetary Nebulae, by II. D Curtis.

Part IV. The Spectrographic Velocities of the Bright-Line Nebulae, by W. W. C. von BELL and J. H. MOORE.

Part V. The Radial Velocity of the Greater Magellanic Cloud, by R. F. Wulson.
Part VI. The Wave-lengths of the Nebular Lines and General Observations of the
Spectra of the Gaseous Nebulae, by W. H. WRIGHT.

22. Forms Assumed by the Planetary Nebulac. Of the 78 planetaries worth of decl. -34°, depicted by Curtis in Lick Publ 13, 55 have a central star, as follows:

40	245	52 6572	6891
246	261	10 6578	6894
650	32-	12 6620	0005
II 1747	358	37 6629	7008
I 351	4.30	01 6720	7009
1504	11 350	58 6751	7036
1514	605	8 6772	7139
1535	II 459	0778	7293
J 320	621	0 6781	7.3.5-1
1 418	630	09 6803	7662
2022	636	90 6804	
II 2(4)	643	6818	
2371	(14)	5 6826	
2392	654	3 0853	
2438	656	6881	

8 very small planetaries, only 2" or 3" in diameter, may possibly possess a central star, though their small size makes it impossible to distinguish such. These are:

	6644		6807
!1	4732		-6833
11	4846	- 11	1997
	6790	11	5117

No central star can be made out in the following 13 objects:

1952	0.537	6886
II 2165	0505	7027
J 900	11 4776	11 5217
2440	6741	
II 4634	6884	

4 planetaries are binuclear, trinuclear, or too irregular to classify:

1952 J 900 2440 7027

From a consideration of the data given above, it seems evident that the typical planetary has a central star, of Class O.

The planetaries may be further classified as to apparent form:

A. Forms apparently helical.

6543 7294

B. Annular forms; main feature a circular or elliptical ring.

				-
	246	2438	6369	7662
	1535	2610	6720	,
Ţ	418	3242	6804	
	2022	3587	6894	
	2392	4361	7000	

C. Disks showing brighter edges; elliptical rings less perfect than those under (B), fading out at the extremities of the major axis, and giving the impression of ellipsoidal shells.

П	1717	6058	6751	6854
	1501	6563	6772	7009
	1514	6565	6781	7139
11	2165	6720	6804	7354
	2452	0741	6180	7662

1) Forms like those under ((), but with a more pronounced truncated effect, as though the ends at the terminations of the major axis of the shell had been out off, faint misue are generally seen at these extremities

40	6561	7026
650	6720	• • • • • • • • • • • • • • • • • • • •
2371	6778	
6058	6851	
(44.5	6905	

E Objects considerably funter along and at the ends of the major axis, this group contains some nebulae from all the first four classes

10	6445	7009
1501	6563	7026
1514	6565	7139
II 2165	6720	7293
J 9no	6741	7354
2372	6772	
2458	6778	
2152	6848	
0058	6853	
0369	6905	

It tircular or elliptical disks, fading out slightly at the periphery, and without discernible structure. Most of these are small, and the lack of structural details may be only apparent.

-1	151	6537	6629		6884
J	320	0572	LI 4776		6886
11	1568	6567	6803	11	5217
11	4644	6578	6879		
	0439	6620	GHR1		

II. Stellar planetaries. These are indistinguishable from a star on the scale of the Crossley negatives, but have been shown by visual observations to have a minute disk. In all probability they differ from the objects under (F) only in SIEC.

Mechanical and quantum theories of the forms assumed by planetaries will be treated in closs, 30, 31, and 32.

28. Proper Motions of the Planetary Nebulae. The almost stellar image presented by a planetary when observed with small apertures, as by a meridian circle, and the stellar nucleus exhibited in many of the group when higher powers are employed, have made these objects attractive subjects for position measures for over a century. The total number of measures on a few of these planetaries by filar micrometer, meridian circle, and photographic plates is quite large.

If any combination of position measures of three-quarters of a century ago with modern photographic positions has any chance of a trustworthy result in the nebular field, we should expect this from the almost stellar appearance of certain planetures. Lundhark has discussed all available older measures

<sup>&</sup>lt;sup>1</sup> Uрн Medd No 39 (1928)

(using recent plates for the final term) of six of the better determined planetaries, plotting the positions on charts and determining the proper motions graphically Reference to the "scatter" of these significant and illuminating diagrams (the

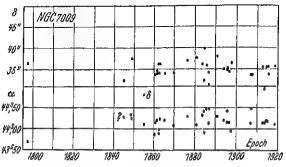


Fig 13 Positions of the Planetary Nebula NGC 7009, 1794 - 1920 (LUNDMARK) No certain proper motion 15 obscivable

contains van Maanen's latest values. These values of van Maanin are considerably more trustworthy, depending solely upon modern large scale photographic plates with an average time interval of 11 years. His probable cirous are

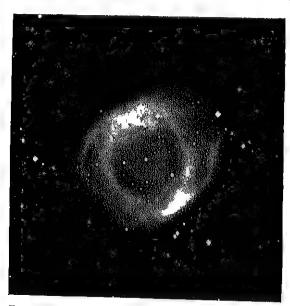


Fig 14 The Planetary Nebula NGC 7293 (luck Photo graph ) This beautiful object is the largest known planetary, and is about 15' 12' It appears to be two turns of a helix

given above, with that in declination below 24, Distances and Dimensions of the Planetary Nebulae While a number of investigators have discussed the parallaxes of the planetanes by various indi-

results by the trigonometri cal method are due to van Maanen His values, with some additions, have been collected by Lundmark and are given in Table 6, with the apparent and the derived absolute magnitudes of the central stars. To these values have been added

rect methods, practically all

1 Mt Wilson Conti No 406 (1930)

values for 7009 are reproduced m Figure 13) will convince anyone that absolutely nothing certain can be known of the proper motions of the plane taries (or other nebular types) through the support of the older visual observations, the only definite conclusion is that the proper motions of the planetaries must be very small

The following table gives I UNDMARK's values, together with those derived from nearly the same material by other m vestigators. The last column

0",0010 in a, and 0",0012 in  $\delta$ , the mean parallax resulting from his values in combination with the rotal tion results of Campbell Land Moore is 0",001, giving a mean mass of 180 · (·), and a mean absolute magnitude for the central stars of 14

In table 5 for LUND MARK, VM VAN MAANIN. WIRIZ, Ma MAKEM SON, NAC NICHOLSON (IC vision of Curris), Ly HN In each pair of values, the proper motion in a 18

the dimensions of the planetaries and their distances, the latter are mainfestly subject to large uncertainty

Table 5 Proper Motions of Planetary Nobulac

Object	Interv	ī.n	w	Ma	NAC	l <sub>a</sub> y	vM (11 y )
2371	45 y	-",040 + ,041			-",016 + ,074		
2392	65 y	800,	- ",004   - ",000	}	ı		
6058	11 y	,,,,,,,		Ì	!		- '000 - '000
6543	118 y	,013 ,007	,000   - ,014		1	[ ]	£00, + 600,
6572	91 y	+ ,012 - ,009	+ ,003 - ,004		- ,008 + ,024	+**,006 - ,017	- ,(X)4 + ,(X)7
6720	11 y		ì l				+00. +008.
6804	11 y				 		,(X)2 - ,(X)2
6905	11 y	ì	\ 		\ 		- ,006 (00),
70019	123 y	000€ + + 000€ +	009,    -  ,048		i [		,,,,,,
7662	121 y	+ ,012 + ,011		- ,024 + ,026	- ,005 + ,020		(  ,022) (-  ,004)

Table 6 Distances and Dimensions of the Planetary Nebulac

NGC	1 Mary		Mapp	Make	Itel	13fsL	Other values
	Are	ly			<i>a</i>	17	<del>-</del>
40	60"	0.12	11,6	+ 1,6	F ",003	1000	1
1501	56	,06	13,0	十8,7	16	200	
1514	120	,95	8,0	-0.5	2	1600	
1952	160	,96	15,5	1 9.2	G	600	
21122	28	,04	14,2	1	. 8	400	1
2371	60	,09	13.5	+8.3	11	3(11)	
2392	17	,04	[0,0	1 5,5	20	160	1 j-",006 S
3242	40	,(12	12,2	十7.8	31	100	1
1I 4593	15		10,0	-			, – ,007 S
(H)58	43	-	13.0	-	16		1
6210	43	-	11,7		. — з'	-	1
6543	22	,04	11,3	8,4	29	400	1
6572	16	,09	108	[-0,8	. 1	1000	
6 <b>72</b> 0	83	,66	14,7	8,5	2	1600	4 ,015 N
6778	25	,08	14,8	-1 6,3	5	640	
<b>GNOH</b>	63	,05	13,4	-1-9.7	1 20	160	[ ] - ,002.5
30°3639	5	,04	10,2	1 1.7	2 '	16(N)	L ono L
6826	27		9.5	_	' –		d 300,}
6853	480	.77	13.7	-  8,3	, 10	320	
6891	15	,02	12,1	8,0	17	190	l .
6905	44	,05	14.5	+9.7	13 1	250	
7008	86	.10	12,8	+8,2	14 -	230	1
7026	25	,04	15,1	<b>⊦9,9</b>	[ H	3(H)	1
7027	18	,04	10,9	- -4,9	8	400	
7293	SKK)	,38	13.3	F11,1	38 ,	86	T
7625	200	,20	8,5	-  4,2	16 !	20224	1
7662	32	1,02	12,9	+9,3	2t ¹	150	1

S = SWARTHMORE, N = NEWRIER, L = Lake

It seems fairly certain that the values given above are much too small as regards distances and diameters, and that these must be multiplied by some

as regards distances and diameters, and that that have as yet unknown factor, perhaps as large as 3 or 5. The mean absolute magnitude (about +8) is much lower than that derived from van Maanen's last determinations of proper motion (+3). Gerasmoviè has discussed this dilemma, deducing from van Maanen's (earlier) proper motions in combination with the Lick radial velocities a mean abs. phot. magn. for the nuclei of +5.9. By various indirect methods, using the angular galactic dip, galactic rotation, and novae at the planetary stage, he derives



+4,9 as the most satisfactory value of M, and points out: "None of the indirect methods used above has given so low an absolute magnitude (+8,1), or so large a mean absolute parallax (0",012) as derived from the Mt.Wilson parallax plates. No other case is yet known for which the discrepancy between trigonometrical parallax determinations and the results of indirect methods is as great as for the peculiar group under consideration. The explanation of this paradox seems therefore to be of much importants." As a result learner of the 150

portance," As a possible cause of the difference, he somewhat doubtfully assigns the existence of some sort of "sampling error" in the selection of the Mt. Wilson objects.



<sup>1</sup> Harv Bull No. 864 (1929).

25. Planetary Spectra; Spectrum of the Nebulous Matter. While the spectrum of the nebulous portions of the planetary nebulae is in most respects a duplicate of the emission spectra of the diffuse nebulae, there are a number of points of difference. In the case of the fainter lines, these differences may arise from the far greater areal luminosity of such an object as 7027 as compared with the Trapezium region of Orion. In other cases, it is possible that actual differences of state or constitution may be indicated. These differences do not seem, however, to be vital, or to indicate different sorts of component matter. There are also frequent differences among the planetaries themselves, as well as



Fig. 17. Objective Spectrogram of the Planetary NGC 7662. (Photograph by WRIGHT.)

in comparison with the diffuse nebulae, in the relative intensities of the lines, as noted for the diffuse nebulae in ciph. 16.

Table 7 is composite, in that it includes all the lines measured by Wright in various planetaries; for the peculiarities of individual objects, reference should be made to his monograph in Lick Publ 43. The series relationships and ionization potentials are as given by Bowen!. The intensities are mainly for 7027; in a few cases these are merely estimates.

Table 7. The Spectrum of the Planetary Nobulae.

7 LA.	Source	Series designation	Excitation potential, y.	Intens.	Notes
3313	O <sub>III</sub>	$3k^{8}P_{1} - 3m^{8}S$	36,72	1	1
3342	Om	$3k^3P_4 - 3m^3S$	36,72	-	5 2 3
3340	Oty?	$3m^{3}P^{-} \cdot 3n^{3}D$	51,76	- †	2
3420,2	N1/ 3	$3^{9}S_{-} - 3^{9}P_{-}$	47,	20	3
3445	On	$3m^3P_{\rm g} - 3n^3P_{\rm g}$	40,66	8	
3704	$H\tilde{\varepsilon}$ , He <sub>1</sub>	23 P 73 1)	13,49; 24,22	- '	4
3712	11br	-	13,49	l - 1	4
3722	$-H\mu$	-	13,48		4
3720,16	l On	$a^1S - a^2D_2$	3,31	50	4 5 5
3728,91	Oir	$a^4S$ - $a^3D_a^7$	3,31	30	5
3734	l ιιὰ .	-	13,47	l 1	4
3750	11x		13,45	] 3 ]	6
3759	$1 O_{11}$	$3k^{0}P_{a}$ - $3m^{0}D_{a}$	36,19	] 4	
3771	1 111"		13,43	1 4	
1798	110		13,44	5	
3820	I Her	$3^{9}P - 6^{9}D$	24,11	1 1	
3835.5	$111\eta$		13,38	8	
3810.2	1	-	i -	5	
3868,74	1 .			70	7
3888.96	112, 11e <sub>1</sub>	285 387	13,33; 22,92	10	8
3935	Catts	$4^{2}S - 4^{2}P_{2}$	3,14	1 - 1	
3964.8	He	$2^{1}S \cdot 4^{1}P$	23,65	5	9
3967.51			<b>→</b>	70	7
3970,08	lle	-	13,27	30	
4009	Her	$2^{1}I^{1} - 7^{1}II$	24,22	1- 1	
4026,2	Hen, Her	23 P -53 D	53,78; 23,95	1 1	
4064				1	}
4068,62	S <sub>R</sub>	$a^4S - a^2P_*$	_	20	10
4076,22	Sit	$a^{\dagger}S = a^{\dagger}P_1^{\dagger}$		2	10
4097,3	N <sub>ttt</sub>	$3h^2S - 3m^2P_2$	30,35	1	
4104,74	H8, Nm	$3k^2S - 3m^3P_1^2$		70	h

<sup>1</sup> Ар Ј 67, р. 1 (1928).

(Continued)

		(Continuou)	1	Inten	Niti
711	Source	Series designation	1 veit ition potential, v	1 1111111	
4120,6	Hε <sub>I</sub>	23 P-515	23 88	1	
11140	He	21P-61D	24,12		
•	Hun		53,76		
4200	C <sub>II</sub>	$3n^{3}D-4^{2}I$	20.87		
4267 1	$H_1$	_	13 00	43(1	
4310 16			I		1 [1
4353	O <sub>III</sub>	$a^{+}D - a^{+}S$	5,53	80	
4363 21	He	21 P= 51/)	23 95	5	
1306,0	0'''	$1b^2P_1 = 3m^2P_0$	26 18	, 1	
1416		$\frac{3k^2P_{1,2}}{2^3P-1^3D}$	23,61	۱ ۹	
1471 54	He <sub>I</sub>		53,54	1 2	
4541,4	Нєп		\ ,,,,,	· .	
4571 5		$ 3m^2P_1-3n^2D_2 $	33,611	1 2	
4654,1	N <sub>III</sub>	$3m^2P_2 - 3n^2D_3$	33,01	S .	
4040,9	N <sub>III</sub>	$3m^2 L_2 - 3m^2 D_3$	30,1	' 1	13
4649 2	CIII	3 3-3-1	1071	, 2	15
4658,2		_	EO 90	100	
4685 76	Hell	_	50,82	(0	
4711,4	] -	-	A 7 If s	111	
4712,6	He	23P-135	23,50	i	
4725 5	l –	-		20	1.1
4740,2			I [		1.
4861,32	IJβ	-	12,70	20	
4922.2	Hέ	2'P-4'D	23,61	2	
4958,91	O <sub>III</sub>	$a^3P_1-a^1D_3$	2,50	300	
5006 84	Om	$a^{3}P_{2} - a^{1}D_{2}$	2,50	500	
5017	He,	$2^{1}5 - 3^{1}P$	23,00	1	
5411,3	Hen	_	53,10	1	I
5655		_	1	1	
5737	} _	_		1	
5754.8	-	. ~	1	1 1	
5875 7	He	2 <sup>3</sup> P- 3 <sup>3</sup> D	22,98	8	
6302	1.0		1	5	
6313	_	<u> </u>	I	2	
6364	\ _	_		2	
6548 1	Nu	$a^3P_1-a^1D_2$	1,89	10	Ì
6562,79	$H_{\alpha}$	# 11 " Dg	12,04	100	1
6583 6	Nu	$ a^{\eta}P_{2}-a^{1}D_{2} $	1,89	30	{
	Her	$2^{1}P - 3^{1}D$	22,98	1	}
6677		$a^1 S - a^2 D_2$	شقريض ا	1 1	10
6730	SII	( 4- ) ~ u ~ 1J <sub>2</sub>	{	, ,	""
7009	750	23P-33S	22.62	1	
7065	He <sub>I</sub>	2-1-5-5	22,63	1	1.5
7138		$a^2D-a^2P$	If two	1	15
7325	OII	a"1)-a" l'	5,00		1.3

Notes to the table of wave-lengths

Note 1 The electron configurations in this table are indicated by Bowkin as follows. Terms arising from the most stable configurations, n being the number of valence electrons remaining in the atom.

(2) $2s$ , $(n-2)2p$ electrons	11
(2) 2s, $(n-3)$ 2p electrons and an excited selectron	I.
(2) 2s $(n-3)$ 2p elections and an excited p election	m
(2) 2s, $(n-3)$ 2p electrons and an excited d electron	11

The numeral preceding these letters indicates the total quantum number of the excited electron, these letters are omitted in one- and two valence electron systems, since for all the cases considered here the type of the term is the same as the type of the orbit of the excited electron.

Notes 2, and 3. These are the lines reported by Paimer at 337  $\{$  and 345  $\}$   $\mu\mu$  Note 4. Observed in Orion, but not in planetanes

Note 5 Buisson, Fabry and Bourger derived the wave-lengths 3/26,100, 3728,838 Note 6 Hz 3750,52

Note 7 The strong lines at 3868,74 and 3967,51 are still unidentified. Carbon has been suggested. 1. Bernan, reported in Pop Astr 39, p. 184 (1931), has studied the behavior of those lines, whose intensity ratio is constant in various planetary nebulae. He rejects the explanation of their origin as due to \$\epsilon\$\_{111}\$ and considers the availability of \$P\_{111}\$ or \$\epsilon\$\_{111}\$.

Note 8 Hζ 3889,051 He 3888,64

Note 9 Suspected with intensity 10 in BD  $+30^{\circ}3639$ 

Note 10 Cf Howay, Nat 123, p 450 (1929) Note 11 Suspected in Orion, not in planeturies

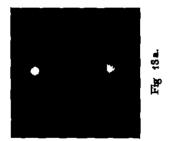
Note 12 See Note 7 Lines of C at 4647.4, 4650.7, 4651.6

Note 13 MERRILL finds this line in R Aquarii and Bi) -12°5145

Note 14 Unidentified

Note 15 MRRRII L gives 7135,6 and 7330,4

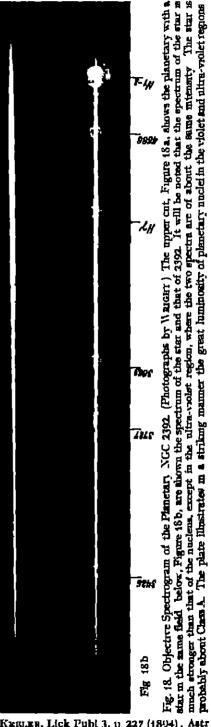
26 Planetary Spectra; Spectrum of Planetary Nuclei<sup>1</sup>. The resomblance of the spectrum of planetary nuclei to that



of the WOI F-RAYET stars, tentatively suggested by PICKERING, has been established beyond all doubt by the extensive researches of WRIGHT

The main characteristics of the spectrum of planetary nuclei are:

- 4 A marked and uniform extension of continuous spectrum into the ultraviolet
- 2 The occurrence of bright bands identical with those observed in the WOLF-RAYET sturs (Class O). The relative strength of these bright bands with respect to the continuous spectrum varies from object to object, in some, as 7026 and 6751, they occur almost without it, while in others they are barely visible against the strong continuous background.



<sup>&</sup>lt;sup>1</sup> В С Ріскевіма, А N 127, р 1 (1891), Ј В. Кикілев, Lick Publ 3, р 227 (1894), Astr and Astroph 13, р 497 (1894), W Н WRIGHT, Ap J 40, р. 466 (1914), Lick Publ 13 (1918)

Out of 30 planetary nuclei, WRIGHT finds that about one-half are Class O stars, and regards the evidence as unequivocal that the nuclei of all the planetary nebulae belong to the same stellar division as the Class O stars. The sequence will then be:

1. Nebulae without nuclei.

2. Nebulae with nuclei. These nuclei are in all cases stays of very high temperature, and in half the cases show the Wolfe-Rayer bands.

3. Class O stars, with no (observed) nebulous surroundings. Temperature

high.

The number of the WOLF-RAYET stars is about the same as that of the planetary nebulae. Miss Payne<sup>1</sup> enumerates a total of 238; of these 106 are of galactic occurrence, 39 are planetary nuclei, and 33 are in the Magellanic Clouds.

The spectral classifications of planetary nuclei have been tabulated by Missa PAYNE in tables VI, II, of the work quoted.

Table 8.

rapie 8.						
Object	Spectrum classification	thject	Spectrum classification			
40	W III	6629	Cont.			
246	O6	11 4776	W114			
II 1747	W	6720	Cont.			
I 351	W	6751	W114			
II 2003	Cont.?	6790	Cont.?			
1514	O8	6803	Cont. /			
1535	Cont.	30°3630	W111			
I 418	O7w	6826	Obw			
2022	Cont.	6833	Cont. /			
II 2149	O7	6879	Cont.			
2392	O8w	6891	Cont.			
3242	Cont.	11 4097	Cont.:			
4361	Cont.	6905	WHI			
II 3568	Cont.	7000	Cont.			
6058	Cont.	7026	WHI			
II 4593 6210 II 4634 6543 6572	O7 + Cont. W Cont. WI WI	II 5217 I 1470 7635 7002	W111 O O7 Cont.			

(The small w in the above Table indicates WOLF-RAYET lines in addition to continuous spectrum; WI has the line at 4686 A stronger than combined lines near 4.340 A; WIII has the 4686 A line weaker)

WRIGHT has suggested a classification of the planetaries based upon the relative intensity of characteristic lines, as follows:

Class I.	. 4686 A present in the nebula	Type object
	a) 3426 A stronger than 3445 A	7027
	VI JTTO A SUIGHREEF THEN 1476 A	Miles and a second
Clara II	or otto is and otto A absent.	-6884
C10.33 11	. 4686 A absent from nebula, 3869 A present	
	a) 3869 stronger than Hô	6572
Close II	of body if weaker thall Ho.	T O L Lis
Omas 11	I. 4686 A and 3869 A absent	. 1 .118

Further details as to the application of spectroscopic theory to the planeturies will be found under ciph. 28 and 31.

<sup>1</sup> The Stars of High Luminosity. Harv Monograph No. 3 (1930).

27 Radial Velocities of Planetary Nebulae; Rotation. Our knowledge of the radul velocities of the planetary nebulae north of declination —34° is very satisfactory and complete, thanks to the work of CAMPRELI and MOORE, south of this our results are due to Wilson (Lick Publ 13). Details as to the radul velocities of individual planetaries should be sought in the tabulation given on pages 168—9 of the papers quoted.

The more important results of CAMPBELL and MOORE, and Wilson may be

leagirammure

1 6 planetures show abnormally high velocities. These are

5871	- 127 km /sec	6644	-ի 2015 km./sex
6567	+133	11 473 <b>2</b>	L34
11 4699	- 117	II 4846	F 165

These values are excluded from the averages which follow

2 17 nebulae (12 probably of planetary type) in the Greater Magellanic Cloud show an average radial velocity of  $\pm 276\,\mathrm{km}$  /soc. The velocity spread is small, and there is no doubt that this represents the radial velocity of the Cloud as a whole

3 i planetary in the Smaller Magellanic Cloud has a radial velocity of  $\pm i68$  km/sec. With less certainty, this may be regarded as indicating the

approximate velocity of this Cloud

4 96 objects of planetary type yield a speed of -29,6 km/sec for the solar motion. The mean radial velocity of 31 of these with diameters less than 5" is 28 km/sec, while that of the 65 larger objects is 31 km/sec. Those velocities are about five times the average radial velocities of the B-type stars.

5 Of 46 planetaries examined, 25 showed internal motion effects, which may be interpreted as rotations about axes approximately perpendicular to the line of sight, while 4 are not so interpretable. The most elongated planetaries show the highest rotational speeds and, in general, the speed of rotation of outer

strata is less than that of strata nearor the center.

6 With some more or less probable assumptions, the mass of a planetary

seems in general to exceed that of the solar system

Physical change has been noted to date in but one object, and that is the "Crub Nebula", 1952 While it is somewhat doubtful whether it is a typical planetary, reference to its internal motions will be included at this point. Variations ascribed either to luminosity changes or to motion were first noted by Lampiano<sup>1</sup> and this nebula was intersubjected to careful investigation by Duncan<sup>2</sup>. His measures are based upon Mt. Wilson plates separated by an interval of 14.5 years. For twelve selected nebular points or configurations, radial motion outward from the center was definitely indicated, amounting to 1",54 in the interval. This displacement, if at a velocity of 25 km/sec., would correspond to a distance of 400 ly, and Duncan points out that it is necessary to assume neither an enormous distance not an extraordinary velocity in the nebular particles in order to believe that the observed motions are real

28. Spectroscopic Distribution Effects. The phenomenon of varying distribution of matter indicated by different spectral lines in the Nebula of

Orion has already been noted under clph 16 above.

Objective prism spectrograms likewise show more remarkable and equally definite evidence of differences in ionization distribution or constitution of

Publ A S P 33, p 79 (1921)

Wash Nat Ac Proc 7, p 179 (1921), with plate

different elements in the shells of many planetaries. Campbell 1 had already called attention in 1894 to the differences in the diameters of the spectroscopic images in I 418. This effect was perhaps first noted photographically by Woll 2 and corroborated by Burns for the Ring Nebula in Lyla 3. Wright has illustrated many cases in his monograph in Lick Publ 13, and most of the data in the following summary are derived from his researches.

Table 9 Distribution of Planetary Materials (Writh) Sizes of Rings of Formations

				ורזסינ	nations	
N	GC.	1 -	rgest —	> Siii?	llest	Notes
I 3 15 I 4	40 351 535 118 )22	II 3727	- 11 β	1171	1686 N <sub>1-2</sub>	No difference noted Slight difference Slight difference
24	165 192 110	3727 3727 — 3727	3967 N <sub>1-8</sub>	- 1686 - 4686	3420         3126	Differences in intensity but not in size large differences Slight differences
II 45 63 65 II 47	309 543	3727 3727 3727 3727 3727 3727	- N <sub>1-2</sub> N <sub>1 3</sub> N <sub>1 B</sub>	- - 11	1686 - 1686	Nearly equal  Some structural differences  Wort  Burns, Ho 3727  Whight
67 68 68 68 68	741 751 318 326 384	3727 3727 - 3727 3727	3869 II 3869	1686	$\begin{cases} & 3126 \\ & N_{1-3} \\ & 3426 \\ & 1686 \\ & & \\ & & 1686 \\ & & 3126 \end{cases}$	}Structural differences Structural differences
70 70 70	391 309 326 327 662 {	3727 3727 - 3869 3967	N <sub>1 0</sub>   N <sub>1-2</sub>	II  -  } 1542	1686 4686? 3126	Notable structural differences  About same size  Notable structural differences

It will be noted from the above compilation that the largest image in the majority of cases is given by 3727 Å,  $O_{\rm III}$ . The smallest ring is generally either 3426 Å ( $N_{\rm IV}$ ?), or 4686 Å,  $He_{\rm II}$ . Reference should be made at this point to the far more detailed results seemed by Berman, discussed in ciph 33. Berman determined isophotal contours for the various spectrographic images, and his diagrams show remarkable variations, not only in size, but in contour, so that the distribution due to a given state may be entirely unlike that given by another See Berman's diagrams, reproduced as Figures 25 and 26, a, b, c

<sup>&</sup>lt;sup>1</sup> Astı and Astroph 13, p 491 (1894)

<sup>&</sup>lt;sup>2</sup> V J S 43, p 283 (1908), also Goschichtete f michemission im Ringnebel Szb Heidelb Ak, Abh No 27 (1911), Die Spektia zweier planetarischer Nebel, ibid., Abh 35 (1911) Dei Ringnebel und der Dumbbellnebel, ibid., Abh 1 (1915), NGC 2438, ibid., Abh 2 (1916)

Lick Bull 6, p 92 (1910)

29. Turbulence Effects in the Planetaries. This name is chosen to designate one of the most remarkable characteristics of the spectra of some of the planetary

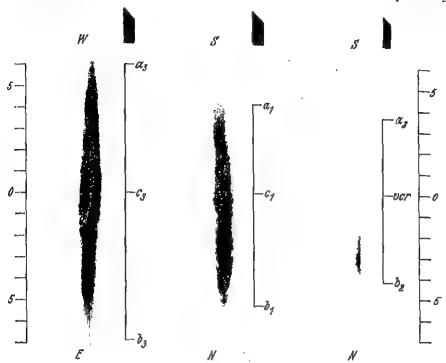


Fig. 10. Drawings of the  $N_1$  Line in NGC 6210. a minor axis; b and c major axis. (Moore.)

Table 40. Turbulence Effects in Planetary Nebulae.

	Titte the fullyfronge issued in I take eachy are but ac.
NGC	1) escriptions
40	The line $N_1$ is not straight, but a very flat, $S$ ,
2302	The line $N_1$ is single at its outer ends, with an irregularly doubled central portion.
3242	The nebular lines are tortuous, with a suspicion of doubling in the central part
	of $N_{y}$ .
6210	The N <sub>I</sub> line is tortuous and irregular, with a slight doubling in an exposure along
	the major axis.
6543	The $N_{\rm g}$ line is tortions, with several slight bends.
6572	The $N_1$ line is irregular and wavy.
0507	The nebular lines are S-shaped.
6720	The N <sub>1</sub> line is wavy, with a marked bowing toward the red in the contral portion
	along the minor axis.
6818	The N <sub>1</sub> line is tortions at the ends, and is slightly but clearly doubled, though
	irregularly, over the central portion of the planetary.
6891	N <sub>1</sub> irregular, and on some plates a very flat S.
7009	N <sub>1</sub> irregular; a very flat S.
7026	N <sub>1</sub> broad and very irregular, with marked minor effects of turbulence.
7027	N <sub>1</sub> shows numerous local irregularities and mottlings.
7662	$N_1$ is doubled in its central portion, with interesting differences between major,
	minor, and diagonal axis positions of the slit. On the major axis, the red com-
	ponent is stronger at one end of the doubling, while the violet component is the
	stronger at the other end. The contours of the line 4686 A show striking
	differences from those displayed by the chief nebular lines.
	See Figure 22.

WRIGHT and MOORE, Publ A S P 44, p. 307 (1929).

nebulac, a phenomenon so peculiar and so anomalous that no entirely satisfactory explanation seems as yet attainable. These phenomena differ from nebula to nebula, and the differences defy verbal description, so that reference should be made to the spectra exhibited pictorially in the papers of Wright and CMP-

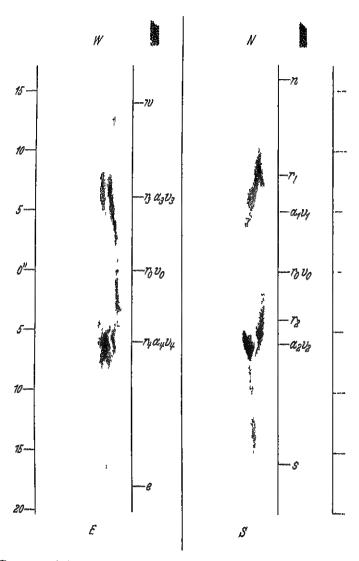


Fig 20. Drawings of the  $N_1$  Line in NGC 2592, a minor axis, b major axis. (Moore )

BLIT and MOORE in Lick Publ 13, and particularly in the sketches made by Moore, three of which are reproduced here as Figures 19, 20, and 21

While this phenomenon has some resemblance to the turbulence effects observed in the Orion Nebula, it is difficult to connect it with the distribution effects described in the preceding Section, and motions of the different elements or states of the same element seem to be involved. It is exhibited in the slit

spectrograms of a considerable proportion of the brighter planetaries, which show an astonishing complexity in the doubling, bowing, or distortion of the lines of the brighter radiations. There are, in addition, frequent minor differences between the appearances along the major and minor axes of the planetary disks.

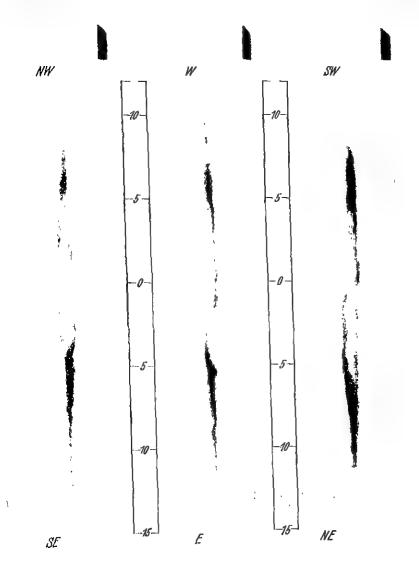
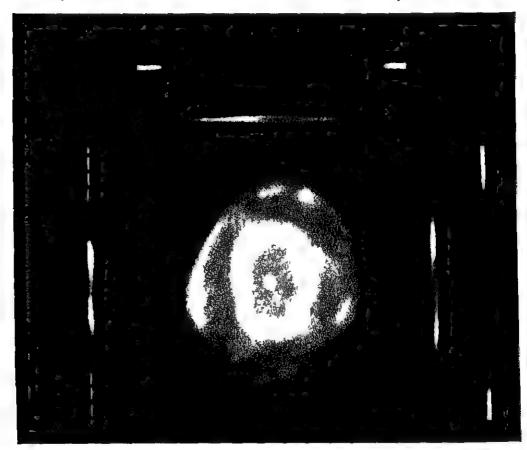


Fig. 21. Drawings of the  $N_1$  Line in NGC 7662. a minor axis; b diagonal axis; c major axis. (Moore.)

The radial velocities measured at different parts of the doubled lines in 2392 vary from +36 to +130 km./sec. The local irregularities in these spectral images are so masked by the process of photographic enlargement that they are best studied in Moore's drawings. Evidence for these turbulence effects is assembled in Table 40.

Polarization tests gave no support to the Zefman or Stark effects as possible causes of these irregularities and doublings, and relative radial motions seem an admissible explanation

CURT'S (Lick Publ 13, p 66tt), from his studies of planetary forms through direct photography, attempted to set up reasonable mechanical models for the production of these curious spectrographic phenomena. He found that most of the peculiarities in these bowed and doubled lines could be produced by the



The Planetary Nebula NGC 7662, and Imbulence Effects (Lick Photographs) The central figure is a drawing of the planetary by Curis. The spectra on each side and above are by Wright and Moore. At the left is the image of 5007 A (N<sub>1</sub>) with the slit along the major axis of the planetary, while the upper figure is the configuration of the same line with the slit along the minor axis. The line at the right is that due to 4686 A, with the slit along the major axis. It will be noted that there are striking differences in the images of 5007 A and 4686 A with a complete reversal of pattern. In their bearing on theories of planetary structure and ionization state distribution, these remarkable photographs are doubtless the most significant which have been secured to date

assumption of a planetary as a homogeneous, somewhat truncated spheroidal shell of gaseous matter, a form which seems to have numerous analogues in the photographic data. Matter falling in from the polar zones of such a shell, toward the nucleus, would, at various increasing inclinations of the equatorial plane of the rotating structure to our line of sight, produce through pure radial velocity

effects, first, shallow 5-shaped lines, next bifid lines, and finally, at 90°, lines which would be symmetrically doubled across the central portion of the planetary, while remaining single at the ends

This mechanical explanation, with the assumption of some degree of turbulence and irregularity in individual portions or features, would produce essentially all the line forms and anomalies exhibited (see Lick Publ 13, Plate XXVI, Ing 84). Yet it is probable that the matter is far from being so simple as this The varying sizes of the planetary shells produced by different alements, or even by different ionizations of the same element, together with the difference in the contours of 4686 A and 5007 A found by Wright and Moore, indicate that the planetary is a structure whose complexity may not be a problem of the grosser laws of matter, or of the deviaing of mechanical models, but rather a complexity whose source lies in temperature conditions and the quantum theory. In conclusion, it would seem that no satisfactory theory of the curious phenomena of these distorted and doubled planetary spectral lines exists as yet, a visit amount of further work is indicated on these objects with instruments of greater power, and the field will inovitably prove to be a very rich one,

80. Mechanical Theories of Planetary Structure. It has been noted in the proceeding for that, of all the various mechanical models set up by way of trial, ( trains found that the assumption of a homogeneous truncated spheroidal shell formed not only a close representation of observed profiles, but satisfied the parallel turbulence effects as exhibited by the spectrum line distortions

There are numerous planetaries which, in projection, give the effect of a shell of luminous matter apparently detached from the nucleus, and even with the regions between this shell and the nucleus nearly devoid of matter. Curris investigated this condition for available planetaries in Lick Publ 43. If the thickness of such a shell, supposed to be spherical, be expressed by d, with respect to the external radius, the brightness of the projected transparent ring should exceed that at the center of the planetary by the factor  $\sqrt{2/d}-1$ , giving the following values for various assumed shell thicknesses

libida in sentialdi	Melative brightness of sing	
0 004 ,01 ,1 ,3	44.7 14.1 4.4 2.3 1.7	

from 25 planetaries, with a mean brightness of the projected ring equal to 2,5 times that of the central areas, the mean thickness of the shell was estimated at 0,26 that of the external radius, and hence in good agreement with this conception of their structure. For ten other planetaries, however, the estimated brightness of the ring was far in excess of the value computed from the estimated thickness of the shell. The mean relative brightness of the ring was 32 times that of the central area, while the mean thickness of the shell was about 0,39, instead of the approximately 0,002 required by theory.

There is no very satisfactory explanation of such exceptional cases. That these exceptions are due to the fact that the objects are true rings, matead of shells, seems to be negatived by the fact that such rings would not be expected to be, in practically every case, arranged in space with the planes of the rings essentially perpendicular to our line of sight. This is not impossible, but almost infinitely improbable.

Also, the existence of peripheral rings of occulting matter in the equatorial planes of the planetaries, tentatively suggested by Campbell and Mooke as an explanation of the frequently fainter matter along and at the ends of the major axis, seems likewise to be negatived by probability considerations. There is practically a complete lack of planetaries showing an asymmetry in brightness on the two sides of the major axis, hence, it such peripheral rings exist, the equatorial planes of the planetaries must, practically without exception, pass through our position in space

GERASIMOVIČI has further considered the shell forms assumed by the planetaries. He has made a more accurate derivation of the relative optical thickness of such a shell and the central areas of a planetary through a some what complicated integral expression which takes account both of the direction of the emitted radiant energy and the curvature of the spherical shell. He thus derives the following values.

	Estimated relative thickness of shell					
Optical	n,t	osity of righ to	0,1 0.1			
thicl ness	Ratio of lumin		Out of the center			
2	1 8	t,4	1,1			
6	4 1	3,3	2,7			
10	7 5	5,6	4,1			

Using these values and (URITS' estimates of the thickness of the rings and the relative intensities, he derives a quantity, Im, for the absorption due to the nebular matter, and finds also the photographic magnitude of the nucleus, were the nebular veil removed. The average value of the photographic magnitude thus found for the nucleus 7,7, agreeng well with the value 6,7 found by Wilson for 83 O-type stats. Generally veil regards the mean parallax of 0",014 as determined by Van Mannen for 20 planetary nucleus as about 10 times too large, and with his revised values he finds that the absolute brightness of the nucleus is inversely proportional to the square of the linear diameter of the planetary. He further derives the mass of the shell of a normal planetary as of the order of 2.0, with an average density of 10.10, for the temperature over the sphere of maximal density he gives the abnormally low value of 8° abs.

There have been a number of attempts to explain the mechanism of such suspended and ocassionally apparently detached spheroidal shells. If ans a has treated the possible adequacy of radiation pressure in supporting such detached shells. Milne, however, after an extensive investigation of the theory of a chromospheric atmosphere, comes to the conclusion that any such detached shell of gas, e.g., Carl atoms, is an impossibility under the action of radiation pressure, or at least until it absorbs more radiation than it emits, and is thus in an unsteady thermal state. "An atmosphere partially supported by radiation pressure is so strongly condensed toward its base that it can hardly be distinguished from the reversing layer itself, either theoretically or observationally."

31 Quantum Theory and Planetary Structure In this and the following Sections there will be reviewed certain new tendencies in the theory of the diffuse and the planetary nebulae, that may be differentiated from those of the past by the factor of atomic constitution or molecular state, for these comparatively

<sup>&</sup>lt;sup>1</sup> A N 225, p 89 (1925) <sup>3</sup> M N 85, p 111 (1924)

<sup>&</sup>lt;sup>2</sup> M N 83, p 481 (1923)

recent developments, which must be regarded as still in the formative period. the name quantum theory seems most applicable, and can lead to no confusion1

32. The Theories of Zamstra, Bowen, Carroll and Berman Zanstra has employed HUBBIF's observational data for a theory of the luminosity of nebulous matter with involved stars. Compare also Russkii 's original suggestion of excitation in emission nebulae by radiation from a very hot body

Hubbick's results are re-summarized thus

1 The light from a patch of diffuse nebulosity having a continuous spectrum is the equivalent of the starlight interesphed (stars of classes By and later)

2 The light from a patch of diffuse nebulosity having an emission spectrum is the

equivalent of the startight intercepted (stellar classes mainly 140 and Oc5)

I The light from a patch of nebulosity in a planetary is, on the average, 4 to 5 magnitudes brighter than the equivalent of the starlight intercopted (stars of classes carlier than (Do5)

Assuming that the emitting star is a black body of temperature T, Zanstra first derives from the quantum theory the number,  $N_{r\bar{s}}$ , of "photographic quanta" intercepted per second by the given patch of nebulosity,

$$egin{aligned} N_{\mu h} &= \Omega \frac{2\pi}{c^4 h^3} I^3 \int \limits_{x_1}^{x_1} x_2^4 \ x_1 &= \frac{h_{1_1}}{hI} \ , & \qquad x_2 &= \frac{h_{7_1}}{kI} \ , \end{aligned}$$

where

 $\Omega$  ~ solid angle intercepted

6,54 : 10 97

1.372 10 14

The emitted light from the nebulosity may be due first to the mechanism of ordinary excitation, though this is regarded as too weak to cause the luminosity observed. The more important part is considered due to ionization and successive recombination. An atom in the normal state is capable of absorbing all the energy of a wave-length shorter than the head of the Lyman series, frequency  $= p_0 = 32.84 + 10^{14}$  The number of quanta thus absorbed will be

$$N_{nl} = D^{\frac{2}{r}} \frac{R^2 k^2}{e^2 k^2} T^2 \int_{x_0}^{\infty} e^{r^2} dx$$

1 Although his findings were not at all in accord with modern results based upon more accurate knowledge of wave-lengths, the detailed lavestigation of the problem of the nebular apactrum by J. W. Nicirolson should be mentioned here. The more important of his papers ara

The pressure of radiation on reflecting spherical particles. M.N. 70, p. 544 (1910).

The spectrum of nebullum MN 72, p 49 (1911) The constitution of the Ring Nobula in Lyra MN 72, p 476 (1912)

On the new nebular line 1 1353 MN 72, p 693 (1912)

Hydrogen and the primary constituents of nebulae MN 74, p 204 (1914)

The constitution of nebulae MN 74, p 486 (1914)

On the nebular line 1 3729 MN 74, p 623 (1914)

The atomic weights of the elements in nebulae M N 78, p 349 (1918)

Atoms with nucleus 2c were regarded by Nicholson as the origin of 3869 A, one with nuclous 3s produced \$187 A, while "nobuliam" was attributed to an atom with nuclous 4s His "protofluorine", postulated for the corona, was hold not to occur in nebulae. The atomic weight of nobulium was placed at 1,31

Ap ] 65, p 50 (1927)

Ohn 44, p 72 (1921); Wash Nat Ac Proc 8, p 115 (1922).

The free elections thus "knocked out" of the atom will recombine with the nuclei by falling back to one of the different levels, emitting the continuous spectrum at the head of the Lyman, Baimer Paschi n series etc. Subsequently the elections in the higher levels will return to the normal level either directly, under emission of the Lyman series, or in steps, emitting the other 11 lines. In this way a number of continuous spectra and line spectra will be produced (see Eddington's discussion below).

After a discussion of the quanta affecting the photographic plate,  $\angle$ ANSTAN derives the following ratio of the number of photographic quanta energing from patch of nebulosity,  $N'_{ph}$ , to the number of photographic quanta in the startight intercepted by the patch,  $N_{ph}$ 

$$\frac{N'_{ph}}{N^*_{ph}} \sim \frac{N_{nt}}{N_{ph}} = \frac{\int_{0}^{\infty} \tau^2}{\tau_0^2 - 1} \, d\tau \qquad \qquad \frac{\lambda}{\lambda} \frac{h\tau}{kT}, \\ \int_{0}^{\infty} \frac{\tau^2}{\tau_0^2} \frac{\tau^2}{\tau_0^2} \, d\tau \qquad \qquad \frac{p_0}{\tau_0} = \frac{32.84}{5.95} \cdot \frac{10^{11}}{10^{11}}, \\ \int_{0}^{\infty} \frac{\tau^2}{\tau_0^2} \frac{\tau^2}{\tau_0^2} \, d\tau \qquad \qquad \frac{p_1}{\tau_0^2} = \frac{5.95}{0.10} \cdot \frac{10^{11}}{10^{11}}.$$

Evaluating the integrals in this expression, the following actual ratios for different stellar temperatures are derived

T	Ratio $N'_{ph}/N_{ph}$	Ratio in magnitudes	1	Ratio $N_{RR}^2/N_{LR}$	k dlo m majnitud
15 000 ° 20 000 25 000 30 000 35 000	0,0075 ,006 ,271 72 1,41	5,51 2,95 1,11 0,36 0,37	10000 50090 100000 150000	2 50 5,1 58 101	() ())) {

In this table, a unit ratio occurs at about 35000", and the stellar temperatures, for the mechanism suggested, are

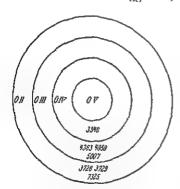


Fig 23 Bowen's Ionization Theory of Planetary Structure (After Bowln)

	Турс	Lat
B <sub>E</sub> Bo		21 000 28 000
()		31000

ZANSTRA's later values require a much higher temperature than this, because of similarity in the comparison with observation, however, his latest theory will be discussed along with Bric Man's below

Bown N<sup>1</sup>, following certain of Zanstra's conclusions, has set up an interesting and convincing mechanism for the planetaries, based upon the quantum theory and postulating exceedingly high temperatures for the central star. The resulting theory shows considerable resemblance to the observed data.

As a first approximation, he assumes a central star with a surface temperature of 150000° K, surrounded by an atmosphere of oxygen of very low density. At this temperature, from the strong photo-electric absorption of light of greater frequency than the ionization frequency of the atom or ion, oxygen in the inn-

<sup>1</sup> Ap J 67, p 1 (1928)

mediate neighborhood of the star could not exist in a state of ionization lower than  $O_V$  (author's  $O^{++++}$ ). Occasionally an electron will unite with such an  $O_V$  ion, emitting the  $O_W$  spectrum, to be immediately ejected by the radiation below

160 A. After traversing a distance represented by the inner circle in Figure 23, the radiation of wave-lengths below 160 A will have been so completely absorbed that now O<sub>IV</sub> can exist in the region outside, and by a similar process there will be a region farther out where O<sub>III</sub> may exist.

This mechanism gives a series of concentric shells whose diameters increase with the decrease of the ionization potentials of the ions present

within them. Bowen's theory thus furnishes a possible explanation of the relative sizes observed for the monochromatic images of the planetaries.

Bowen regards a temperature of at least 100000° necessary for the hottest planetary nuclei.

EDDINGTON<sup>1</sup> and WOLTJER<sup>2</sup> have discussed the difficulty of an adequate explanation of the great strength of such "forbidden" lines in comparison with the ordinary lines of the spectrum. EDDINGTON suggests that

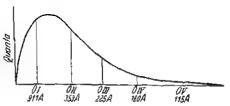


Fig. 24. Ionization Mechanism in Planetary Nebulae. (After Bowen.) The distribution in frequency of quanta emitted by a black body at a temperature of 150000° K.

λ	Source	Size
3426 A	N <sub>IV</sub>	Smallest
3346	O <sub>IV</sub> He <sub>II</sub>	11
4086	He <sub>11</sub>	Next in size
3313	[]	
3342	} O <sub>III</sub>	31
3444	)) <u> </u>	T
4859	Ou	Large
5007	$O^{11}$	
3726	On	Largest

this difficulty may be removed by a simple addition to Bowen's original condition, namely, that the stimulating radiation must be so weak that the atom is unlikely to absorb a quantum during the full duration of the metastable state. The strengthening of the forbidden emission is then merely relative to that of the ordinary emission. He gives the following illustration of this effect:

"Let (2) be a metastable state, the forbidden transition being  $2 \to 1$ . Let (3) be the state next above (2), from which there is an ordinary transition to (2). The full duration of (2) is taken as t sec., and that of (3)  $10^{-8}$  sec.

First let the radiation be moderately strong so that each atom . . . absorbs about once in 10  $^{3}$  sec. Then practically all the atoms arriving by any route from state (3) will forthwith emit, only about 1 in 10 $^{5}$  being arrested and jerked to some higher state by absorption. A fixed proportion will emit the line 3 > 2 and reach state (2). Of these, only 4 in 1000 will go on to state (1); the others are forestalled by absorption which diverts them to higher states. Accordingly the forbidden emission in  $2 \rightarrow 4$  is very much less than ordinary radiation.

Next let the radiation be so weak that each atom absorbs but once in 10 seconds. As before, the atoms arriving in state (3) will forthwith omit, a fixed proportion of them traveling to state (2). But now  $^{0}/_{10}$  of these will go on to state (1), because the chance of absorption (once in 10 seconds) is only  $^{1}/_{10}$  of the chance of emission (once in 1 second). There will be more quanta emitted in the forbidden line  $2 \rightarrow 1$  than in the ordinary line  $3 \rightarrow 2$ , because (2) is the end-point of other transitions besides  $3 \rightarrow 2$ , and  $^{0}/_{10}$  of all of them are followed

A forbidden line starting from state (2) becomes more or less equivalent to an ordinary line starting from state (3)."

<sup>1</sup> M N 88, p. 134 (1927).

A late and quite complete theory of such spectral excitation is due to CAR-ROLL<sup>1</sup>. His work is based largely on certain observational data of 11. II. PLAS-RETT<sup>2</sup> with the correction of certain of his conclusions attributed to errors in the equations employed<sup>3</sup>. The existence of the so-called forbidden lines is taken, as by most previous investigators, as an indication that the density must be very low, as otherwise the atoms would be disturbed by collisions. Also, as pointed out by Eddington, the stimulation by radiation is assumed to be very weak.

The processes postulated as affecting an atom of 11 are:

1. Capture of an electron by an ionized atom; effects small.

2. Excitation from the normal state by electron collision or by absorption of a line of the LYMAN series; effects small.

3. Ionization, photo-electric, or by electron collisions. The predominant

cause.

4. The numbers of atoms, electrons, or quanta of any particular specification

are assumed to be constant.

The mean density is taken as  $10^{-20}$ , giving a mean free path which lies between  $2.25 \cdot 10^{12}$  and  $2.25 \cdot 10^{13}$  cm, with an average duration of free path of the order  $40^7/T^{1/2}$  seconds. For all probable temperatures this is more than  $10^4$  seconds, while the life of excited H atoms is  $10^{-5}$  sec., or less. Collisions (and radiation as well) are accordingly regarded as insignificant in removing atoms from excited states.

CARROLL carries out extensive probability investigations as to the relative frequency of excited atoms in the various states and under different modes of excitation, and reaches the following general conclusions:

1. The H atoms are nearly all ionized.

2. The temperature is of the order of 10000°.

3. The Balmer emission lines are generated by electron captures by ionized atoms and their subsequent transitions.

4. The dilution; of the radiation is of the order of 1012.

5. The density is of the order 10-21.

6. While Lyman absorption must occur, indeed not much less nor more frequently than ionization, it has little effect in producing Balmer lines.

7. The mechanism of ionization is presumably photo-electric rather than

electron collision or line absorption,

A late and coherent theory of the nebular phenomena in the planetaries, based in large part upon investigations of intensity and isophotal contours of individual monochromatic images obtained with slitless spectrographs, is due to Berman and Zanstra<sup>4</sup>.

Zanstra's results are based upon slitless spectrograms taken with an ultraviolet spectrograph in the primary focus of the Victoria 72-inch reflector, while Berman's were obtained with two-prism quartz spectrograph in the primary focus of the Crossley Reflector at Lick. In both cases the monochromatic images were studied with registering microphotometers. Because of the brightness of

M N 90, p. 588 (1930).
 PLASKETT'S answer, Obs 54, p. 49 (1931).

<sup>&</sup>lt;sup>4</sup> D. H. Menzel, The planetary nebulae. Publ ASP 38, p. 295 (1926); The dilution of radiation in m nebula, ibid. 43, p. 70 (1931); Physical processes in gaseous nebulae, ibid. 43, p. 334 (1931); L. Berman, A spectrophotometric study of certain planetary nebulae. Lick Bull 15, p. 86 (1930); H. Zanstra, Untersuchungen über planetarische Nebel. Erster Teil. Die Leuchtprozesse planetarischer Nebel und die Temperatur der Zontralsterne. Z. I Astroph 2, p. 1 (1931); Publ Astroph Obs Victoria 4, p. 209 (1930). Earlier references quoted above.

these objects, most of the results were obtained on 6543 and 6572; Berman gives data also for 11 4593, 6826, 7009, 7027, and 7662.

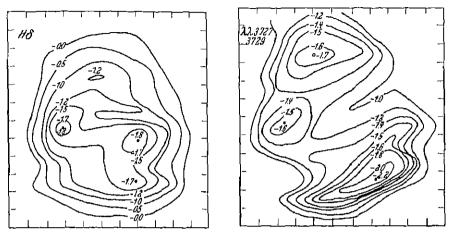


Fig. 25. Contour Diagrams of the H and  $O_{\rm H}$  Constituents of NGC 6543. (After Berman.) Note that the distribution of the two sorts of material is radically different within the same planetary.

Berman's isophotal contours are shown below in Figures 25 and 26, as an illustration of the power of the method. They give in compact form a mass of

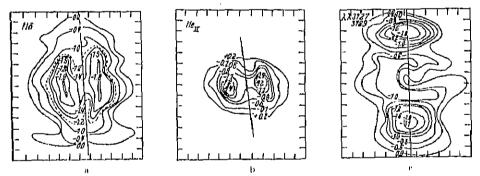


Fig. 26a, b, and c. Contour Diagrams of H,  ${\rm He_{H}}$ , and  ${\rm O_{H}}$  in the Planetary NGC 7009. (Berman.) The distribution of the three elements is entirely different;  ${\rm He_{H}}$  is smallest, and  ${\rm O_{H}}$  largest.

data as to the distribution of different elements or ionizations which is vastly more complete than earlier data. Berman's total integrated intensities of the different sources (from his Table VII) are given below in Table 41.

Taking the ratio of the intensity of  $O_{\rm HI}$  to  $O_{\rm H}$  as a rough measure of the degree of ionization, Berman determines the following percentages of ionized  $O_{\rm HI}$ :

Object	O <sub>HI</sub> /O <sub>H</sub>	Frantion of O <sub>[1]</sub> toulzed	Object	опт/оп	Fraction of O <sub>H</sub> louized
6543 6826 6572	1: 0,47 1: 0,13 1: 0,08	83% 87 92	7009 7027	1: 0,02 1: 0,02	98 98

Table 11. Total Integrated Intensities of Planetary Sources (BERMAN).

Source	λ	6543	6826	6572	7009	7027
Ont	5007	-1,54	- 1,67	-2,09	-2,52	-2,69
OIII	4959	0,48	-0,71	-1,03	-1,44	
$o_{nr}$	4363		+1,86	+1,84		-1,61
$\bar{\mathbf{O}}^{\mathbf{IH}}$	3445	_	'	1 -	. 1 40114	+1,58
$O^{11}$	3726, 3729	+0,03	+0,20	+0,27	+ +1,37	+ 1,47 + 1,30
$H\beta$	4861	0,00	0,00	. (),00	0,00	ì
$H_{\gamma}$	4340	+0,44	+0,61	+0,60	+0.57	+ 1.02
$H\delta$	4102	+0,86	+0,83	+1,16	+ 1.06	
$H_{\ell}$	3970	(+1,27)	(+1,20)	(+1,48)	(-1-1,51)	-1-1,68
$H\zeta$	3889	(+1,65)	(+1,50)	(+1,82)	(-[-1,98)	(+2,09)
$H\eta$	3835	+1.95	+1,71	+2.05	+2,42	(-+2,40)
$H\theta$	3798	+2,34	-	+2,49	7 2,12	+2,74
$H\iota$	3771	_	~-	+2,61		+3,03
H×	3750	_	~~	+2,79	i -	-1-3,43
He + 3867	_	+0,72	- -0,54	+0.61	+0.39	-
$H\zeta + \mathrm{He}_{\mathfrak{l}}$	-	十1,12	+0,96	1-1,43	+1,02	- -1,04
Hen	4686		1 -12	1 1773		-[-2,38
Hen	4542	_	_	_	1-2,18	+1,03
Holl	4200	_	_			-1-3,60
$He_{\mathbf{I}}$	4471	+2,47	_	_	_	- <b>⊢4,3</b>
$o_1(- -\hat{H}e_{11}\rangle)$	4026		+2,46	+2,61	+2,66	- - 3,04
Ho.	3889	+2.36	-	-[-2,69		3,54
•	- '-	(+2,15)	(十1.97)	(+2,74)	(- -1,60)	-[-4,()
$S_{II}$	4069, 4076	-	_	i –	_	
$N_{10}$	4634	ì				,
$N_{\rm HI}$	4641	-	_	l Í	i	1 - 40
CIII	4649	ĺ		_		+2,69
?	3967	(+1,72)	(+1,40)	(1400)		4
?	3869	+0.07	+0.05	(+1,26)	(-1-0,87)	(+i,56)
7	4571		7-0,03	-0,17	-0,56	- -0,04
? [	3426			_	~	4,15
,	3346	_	_			-0.09
,		1	-	-	-	-[-0,92

ZANSTRA considers two mechanisms of the luminous process:

- 1. The mechanism of re-combination.
- 2. The mechanism of electron impact, regarded as the cause of the "nebulium" lines.

Placing

$$x = \frac{hv}{kT}$$
,

he derives the following formulae for the determination of the temperatures of the central stars:

Mechanism 1, 
$$\int_{a_0}^{\infty} \frac{x^a}{e^x - 1} dx = x_0 \int_{a_0}^{\infty} \frac{x^a}{e^x - 1} A_r dx,$$

where  $A_r$  is the arbitrary measure of relative intensity derived from the observations. Similarly for

Mechanism 2, 
$$\int_{x_0}^{\infty} \frac{x^3}{e^x - 1} dx - x_0 \int_{x_0}^{\infty} \frac{x^3}{e^x - 1} dx = \sum \frac{x^4}{e^x - 1} A_x$$

where the original paper should be referred to for the derivation and for the measures.

A table is then derived for the temperature as a function of the difference in brightness between the nucleus and the nebular matter, and from this the temperature values are derived for 22 planetaries. These are given below in Table 12, with the addition of Berman's values, when available. The latter author determined the temperatures separately for H, He<sub>I</sub>, and He<sub>II</sub> on the hypothesis of ionization and electron capture, and according to the theory of impact excitation for the  $N_1$  and  $N_2$  images. Both authors note that the greater the difference in brightness between the nebula and the nucleus the higher should be the temperature. "Failure to observe nuclei in planetary nebulae with the above spectral characteristics may reasonably be attributed to the high temperature rather than to the non-existence of the nuclear stars (Berman)." The mean of Berman's values have in general been taken.

It will be noted from this table that there is a considerable measure of agreement in the values derived, and that the authors both attribute exceedingly high temperatures to planetary nuclei. Closely similar results as to a high average nuclear temperature have been obtained through a number of methods of analytical attack by Vorontsov-Velyaminov<sup>1</sup>.

Table 12. Approximate Temperatures of Planetary Nuclei, derived by Zanstra from Luminosity Differences, Nucleus-Nebulosity, with the Addition of Berman's Values.

		H <sub>Ithe</sub>	ı	Temper	ratures
Dbject	Marb .		ır _	ZANSTRA	Bernan
650	16,6	1),1)	6,7	85 000 b	
1535	11,6	8.8	2,8	38 000	
1952	15,0	8,4	7.5	100 000	
2438	16,6	9,8	6.8	85000	
2392	10,0	8,4	1,6	31 000	ı
3232	11,7	7,1	4,6	55000	i
1587	14.3	0,4	4,9	55000	
4361	12,8	10,1	2.7	37 000	
4593			-	-	25000°
6210	11,7	8,5	3,2	40 000	:
tel 4.5	19	10,4	8,6	140000	i
6309	14.5	10,7	3,8	45000	
6513	11,3	8,1	3,2	40000	33 000
6572	10.5	8,4	2,1	34000	43000
6720	14,7	8,8	5,9	70000	
6804	13.4	11,8	1,6	31000	i
6818	14,9	8,8	6,1	70000	
6826	10,8	8,4	2.4	35000	27 000
6853	13.6	7.3	6.3	75000	
6905	14.5	10,7	3,8	45000	
7008	12,8	12,2	0,6	28000	40000
7000	11,7	7,2	4.5	50000	: 40000 : 50000-
7027	1	1	·-	i	: 20000 <del>-1</del>
7062	12,7	8,4	4.3	T 50000 ±	I

33. Evolutionary Status of the Planetary Nebulae. There seems fittle doubt that the class of the planetary nebulae must be regarded as an exceptional, and doubtless very rare, branch of cosmical evolutionary development. We must consider them as presumably of catastrophic origin; lusus naturae impossible to fit in any orderly fashion within a reasonable gamut of stellar evolution.

т R А ј S, pp. 15, 122 (1931).

The arguments for such an exceptional status are two fold

t Theo earty of occurrence. Dewer than 150 are it present known. It is quite probable that the nucleus of a planetary is in all cases a Worr RAST. star These, too, are an exceptional class, and the number known at pre-emexcluding the planetary nuclei and those in the Magellanic Clouds, is 16b or about that of the planetaires. Because of this rarity, the planetaries can not wen be placed either at the beginning or the end of the general course of stell n evolution, except by making most improbable assumptions. There have been attempts, also, because of their small numbers, to link up the planetary clawith the novae, these attempts can not be said to have been very successful and meet with many difficulties as to spectrum and frequency

The planetaries are quite certainly fewer than 0.01% of the number of stars which may be assumed to be roughly within the apparent magnitude muniof the planetary nuclei. It thus appears impossible to postulate the planetary stage as one through which all stars pass, for it would then be necessary to assume that existence in the planetary stage can be but a negligible period in the his

history of a star, and only a lew thousand years in digitation

2. If the attempt is made to place the planetaries at any point in the stellar progression, then relationship with the Class B stars would seem most probable in fact, any connection whatever with red stars seems entirely out of the que stion Here we meet the almost insuperable difficulty caused by the observed lact that the average space velocity of the planetaries is live times that of the average Class B star

LUDENDORM, however, has assembled some data which partially remove this difficulty. For known double stars of Classes Oc to Bo, he assemble a the values of  $l = a/(1+a)^3 M \sin^4 t$ , where  $a = m_2/m_1$ , and M $m_3 \mid m_1$ far as is known,  $a/(1+a)^4$  is always less than 1, hence a large value of f will indicate a large value of M. Camphill and Mooki had already derived quite large values for the masses of certain planetaries. The radial velocities of the centers of mass of the systems were then feed from the effects of the solar motion and the K-term, giving a quantity  $\gamma_0$  . The available material was then grouped m the class subdivisions Oe to B5, and B8 and B9, following the values of / as follows

Value of /	10 lugar thin the ne Classes Oc to B5, proportion	on value 7 s km isci   Chisses 118 und 110,   proportion	
0,75	7 out of 12, 55%	2 Stars 100%	
0 10 to 0 75	5 out of 13, 38%	2 out of \$, 33%	
0,10	0 out of 12, 0%	0 out of \$ 0%	

There is thus indicated a marked increase of velocity with increasing mass, with the conclusion that the systems with largest mass possess velocities which approach those of the planetary nebulae, hence the deduction that large velocities may be expected for bodies with the masses attributed to the planetaries, and that their large velocity, on this assumption, is no bar to a connection between these objects and the O and B stars. There remain the difficulties as to the small frequency of these objects, in which respect they are still exceptional

Certain of the recent planetary theories of the quantum type postulate nuclei of tremendous temperatures, 50000° to 100000° abs, or more. If these high values are substantiated by luting observation and analysis, if will be mercly one more proof of their exceptional nature

<sup>&</sup>lt;sup>1</sup> Uber die Beziehungen der planetarischen Nebel zu den Heltum-Steinen A.N. 212, p 3 (1920) and 221 p 357 (1925)

## d) The Spirals.

84 Historical Note on the Spirals. In the cosmogonies of the eighteenth century, most nebulae were regarded as composed of stars, but too distant to be individually resolvable. Certain clusters and stellar aggregations which had appeared nebulous with lower powers had been found to be resolvable when higher powers or larger telescopes were employed. Hence by analogy, reasonable enough in the light of then existing data, all nebulous objects were believed to be similarly resolvable. Hungens wrote in 1682 in

"Num cacterae nobulezzo olim existimatae, atque ipsa Via Lactea, perspicillo inspectae aulias nobules habite comperiuntur, neque allud case quam plurium stellarum congeries et frequentia"

GATHEO, CASSINI and MICHELL regarded nebulae as thus resolvable; HALLEY, DERHAM, LAMBERT, KANT, and LACAILE maintained the existence of nebulous masses

Such was also Sir William Herschel's earlier bolief, namely, that all objects of a nebular texture could be resolved into stars if only sufficient power could be applied. Certain of his earlier papers contain references to other Milky Ways and to distances of the order of 10<sup>20</sup> km, which have striking resemblances to the conclusions of the island universe theory. These beliefs were abandoned by 1791 through the conviction that there were many objects which were intrinsically nebulous in character, and impossible to resolve into stars. The cosmogonical speculations of Kant, Lahbert, Michell, and others, may be dismissed as philosophical rather than observational deductions.

It is an interesting fact that the spiral nature of these objects seems completely to have excaped the Herschers. It is doubtful whether a single one of their objects contains this word in its description; it certainly is not given as an abbreviation, nor does the concept occur in any of their notes or papers describing the various types of nebulae observed. The spiral nature of these colestial objects was first discovered by the Earl of Rosse, with his 6-foot reflector. The spiral character of 5194 (M51) was first noted in 1845, and announcement was made in 4849.

Von Humbot pr's view at the time of the publication of his Kosmos (4845—50) was essentially the same as Hersener's later position. Cortain nobulous objects were regarded as truly gaseous, while others of different texture were thought to be composed of stars. For the latter objects you Humboldt coined the expressive plunes, "Weltinsel", which is perhaps the parent of the more modern "island universe".

A completely different phase was brought into the puzzling problem of the nebulae by the first spectroscopic observations. It was at once recognized that nebulae showing bright emission lines (the diffuse and planetary classes) must be truly guseous. Here, again, an insufficiently evidenced analogy was to impede unduly the final solution of the enigma. Because of the great numerical preponderance of the objects now known as spirals, it was found that the majority of the "nebulae" showed no bright lines, but a continuous spectrum, in which much later the more prominent Pranunderr lines were detected. These were frequently called "white nebulae", a name coined for them by Young. It was tacitly assumed that these objects also must be gaseous, premising some as yet unknown form of spectral excitation, or reflection effects from Milky Way stars.

Opera Varia (1784), p. 540.
 Kosmos 3, p. 187, ot passim.

Brit Am Report (1849), p. 53

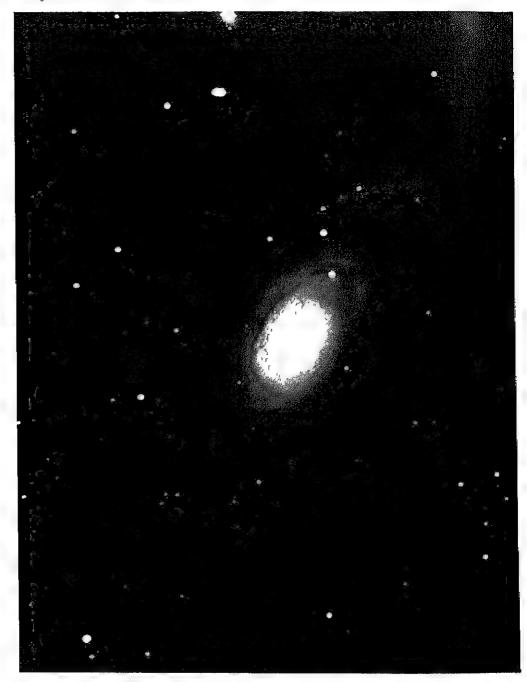


Fig 27 The Spiral NGC 3031 (M81) (Lick Photograph)

To this latter theory, the fact that the spectra of the white nebulae were later found apparently identical with those of solar type stars gave some measure of support

Note 7 The strong lines at 3868,74 and 3967,51 are still unidentified. Carbon has been suggested. 1. Bernan, reported in Pop Astr 39, p. 184 (1931), has studied the behavior of those lines, whose intensity ratio is constant in various planetary nebulae. He rejects the explanation of their origin as due to \$\epsilon\$\_{111}\$ and considers the availability of \$P\_{111}\$ or \$\epsilon\$\_{111}\$.

Note 8 Hζ 3889,051 He 3888,64

Note 9 Suspected with intensity 10 in BD  $+30^{\circ}3639$ 

Note 10 Cf Howay, Nat 123, p 450 (1929) Note 11 Suspected in Orion, not in planeturies

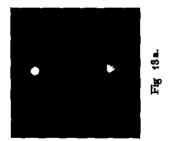
Note 12 See Note 7 Lines of C at 4647.4, 4650.7, 4651.6

Note 13 MERRILL finds this line in R Aquarii and Bi) -12°5145

Note 14 Unidentified

Note 15 MRRRII L gives 7135,6 and 7330,4

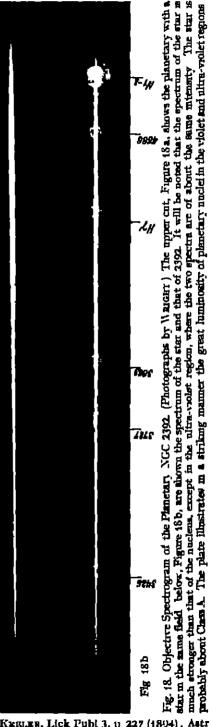
26 Planetary Spectra; Spectrum of Planetary Nuclei<sup>1</sup>. The resomblance of the spectrum of planetary nuclei to that



of the WOI F-RAYET stars, tentatively suggested by PICKERING, has been established beyond all doubt by the extensive researches of WRIGHT

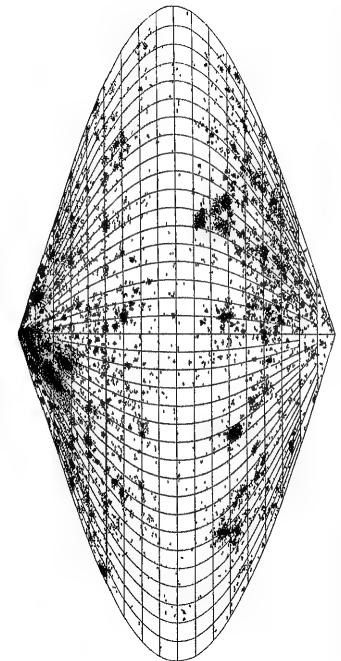
The main characteristics of the spectrum of planetary nuclei are:

- 4 A marked and uniform extension of continuous spectrum into the ultraviolet
- 2 The occurrence of bright bands identical with those observed in the WOLF-RAYET sturs (Class O). The relative strength of these bright bands with respect to the continuous spectrum varies from object to object, in some, as 7026 and 6751, they occur almost without it, while in others they are barely visible against the strong continuous background.



<sup>&</sup>lt;sup>1</sup> В С Ріскевіма, А N 127, р 1 (1891), Ј В. Кикілев, Lick Publ 3, р 227 (1894), Astr and Astroph 13, р 497 (1894), W Н WRIGHT, Ap J 40, р. 466 (1914), Lick Publ 13 (1918)

CHAMBERLIN and MOUITON'S planetcsimal hypothesis, which suggested the origin of the solar system from a relatively small spiral structure, and VANMA ANI N'S

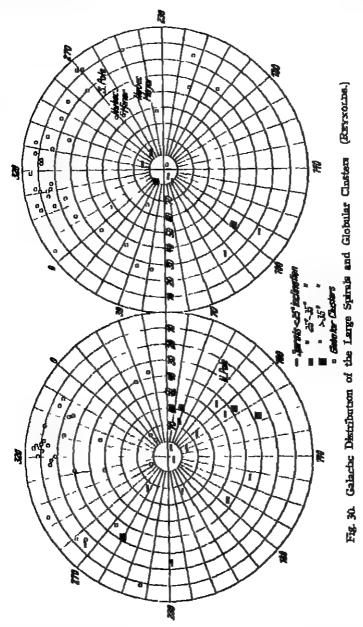


While the chart contains the diffuse nebulae these are comparatively few Clusters known annular and occur near the galactic plane. For all practical purposes, this is the most complete chart extant of spiral distribution (CHARLIER ) This chart contains 11475 NGC objects planetary nebulae, and stellar nebulae were excluded Galactic Distribution of Spirals

values of the internal motions in the spirals, secured in 1922 and following, for a time made full acceptance of the theory difficult to many. All doubts as to

the island universe character of the spirals were finally swopt away by Hubbles's discovery of Cepheid variables in these objects in 1924

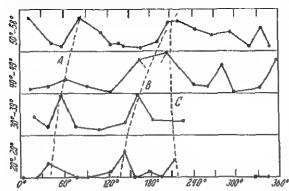
At present it may safely be said that the combination of the lines of evidence



secured from the peculiar space-distribution of the spirals, their enormous radial velocities, their star-like spectrum, and the occurrence of novae and Cepheld variables within their structures, has nullified all former objections. The theory that the spirals are conglomerations of stars, comparable in many cases with

our own galaxy in size and in number of component units, is now universally accepted 1.

35 Apparent Distribution of the Spirals, Super-Galaxies<sup>2</sup>. The fact that there is a marked concentration of "nebulae" about the galactic poles has long been known, and has been the subject of numerous papers. This tendency, first clearly indicated by Procior and Walers, is shown as well in all subsequent



lig 31 Variation of Nebular Distribution with Galactic Longitude (Searrs) Distribution of nebulae in the north galactic beinsphere according to galactic longitude (absessae) Four curves for the latitude intervals are noted in the margin A, B, C, are the more-or-less hypothetical lines of maximum frequency I and C correspond to the maximum in longitudes 50° and 220°.

studies of the smaller spuals. All agree in showing that the concentration about the north galactic pole is greater than about the southern, and in indicating a marked falling of in numbers as the galactic plane is approached. This diminution is clearly shown in Curits' counts of small objects (Lick Publ 13)

Calactic Intitudes	Number per square degree
+ 15° to + 90°	3 t
- 15° to - 90°	28
- 30° to - 15°	2 t
- 30° to 30°	7

Such variations in distribution have been more thoroughly studied by SLARLS,

who finds definite differences with galactic longitude. See his Figure reproduced as Figure 31

That our own galaxy should thus be situated about midway between two tremendous groups of several million galaxies each, and be, by such unique location, still more definitely an "island universe", is, of course, not an impossibility, whatever objections may be urged against this on the score of probability. This uniqueness of location and this exceptional isolation must be accepted, however, unless one prefers to assume a reasonable degree of uniformity of distribution for the 10° or so galaxies accessible to our telescopes, and to postulate, from the analogy of the phenomenon seen in so many spirals (see ciph 42), that a similar tremendous ring of occulting matter in our galactic plane and for the most part outside the Milky Way structure, cuts off from our view the spirals that would otherwise be seen in the zone between +15° and -15° galactic latitude

A recent development of the highest interest is the substantiation by IIumason of the arrangement of certain spirals in great groups, or "super-galaxies",

I his acceptance is not quite manimous, cf ciph 58 Also "La maneia de formaise de las nebulosas espirales es indudablemente la postulada poi Chamberlin y Moniton para explicar el origen del sistema solar, el paso de un cuerpo a poca distancia de otro, con la expulsion de materia en forma de dos comientes o brazos. Ahora se sabe que las espirales son sistemas mas pequeños y muy probablemente dependientes del sistema galáctico" C. D. Perrina, Asoc Cult de Conf. de Rosario (Argentina). No. 2 (1930)

<sup>2</sup> R A Proctor, M N 29, p 337 (1869), S Waters, ibid 33, p 406 (1873), 51, p 526 (1894), J II Riynoids, ibid 81, p 429 (1921), 83, p 447 (1923), 84, p 76 (1921), R F Santord Lick Bull 9, p 80 (1917), F Hertzsprung, A N 192, p 261 (1912), C Easton, ibid 166, p 130 (1904) C Abbe, M N 27, p 264 (1867), S I Bailey, Sc N S 25, p 565 (1909), A R Hinks, M N 71, p 588 (1911), E A Fath, Pop Asti 48, p 544 (1910), F Slaris, Ap J 62, p 168 (1915), P Doig, J B A A 33, p 238 (1923)

which possess contiguity of location and have, moreover, recently been found to possess radial velocities of nearly the same size for such of their component members as have been observed. Their special interest lies in the strong resemblance of such a structure of groups or super-galaxies to Charlier's theory of an infinite universe. As this characteristic grouping will be discussed in some

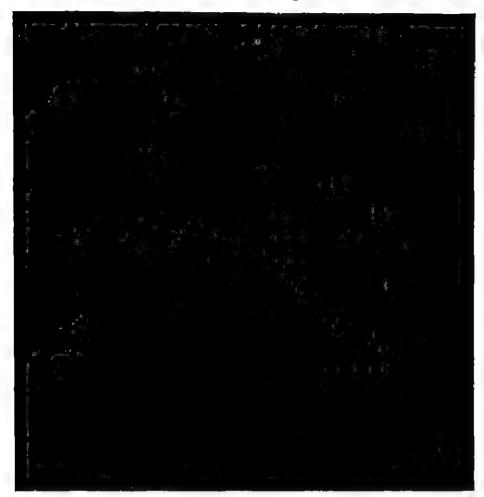


Fig 32 Cluster of Small Spirals (Link Photograph) This is a portion of the rich region at 12 55, | 28° 50′ It is 38′ 39′ in size, and shows 249 small spirals and elliptical objects

detail in ciph 56, 68, and 78, the details of such super-galaxies will be left for the Sections noted.

86. The Number of the Spirais. Early in his program of photography with the Crossley Reflector, and when the total number of regions observed was relatively small, KKKKKR discovered a very large number of very small and hitherto

<sup>&</sup>lt;sup>1</sup> J R. Kerler, A N 154, р 4 (1899), M N 60, р 128 (1899), I Jok Publ 8, Introduction (1908), С D Ренеим, Ар J 20, р 356 (1904), I Jok Bull 3, р 64 (1904), A J 29, р 79 (1945), H D Сияти, Publ A S P 30, р 159 (1913), Proc Amer Phil Soc 57, р 513 (1918), Lick Publ 13, р 12 ff. (1918), R J Path, A J 28, р 73 (1914), R P Sanford, Lick Bull 9, р 80 (1917), F H Skares, Aр J 62, р 168 (1925), R. Hurble, Science, Suppl 73, No. 1904 (1934)

unrecorded nebulous objects in all regions well removed from the Milky Way. At that time he estimated the total number accessible in the sky with the Crossley Reflector as 120000. When it is recalled that only about 11000 nebulae had been catalogued up to 1900, the increase of roughly 1000% made by Kristlek stands out as a contribution to cosmogony of the highest rank.

The question has since been investigated by Pirrini, (URIIS, PATH, SAN-LORD, SEARES, and Hubble The various estimates are given below in tabular form

Keller	1899	120 000		
PLRRINE	1904	500 000	(eventually	a million)
CURTIS	1913	700 000	,	
TATH .	1914	162000		
Curtis	1918	722000	(eventually	a million)
SLARES	1925	300 000	•	
Hubbll	1931	30 000 000		

There is little value in reviewing here the efforts which have been made to reconcile the smaller estimate of FATH (162000) and the larger ones of Perrini and Curtis (1000000  $\pm$ ), Curtis' support of these larger values may be found in Lick Publ 13. The great power of the 100-inch telescope has shown clearly that the number of small objects of the spiral class is very great.

As pointed out by W W CAMPBELL, there is less difference than appears at first sight between Hubble's value and those secured from the Crossley surveys, when one takes into account the larger volume of space accessible to the larger instruments. Hubble's estimate is for the entire number of such objects existing in the spherical volume of space whose radius is the distance of the most remote objects found on the Mt Wilson plates, without regard to those occulted in the Milky Way area. As, other things being equal, the 100-inch reflector should penetrate 2,83 times as far into space as the 36-meh (1055k) Reflector, the former should therefore command a volume of space about 22,0 times the volume accessible to the latter. Assuming that the distribution of these objects in space is roughly uniform, and making reasonable additions to the Perrine-Curies totals for those objects which are prevented from recording then images on the negatives by obstructing materials in our Milky Way system. it will be seen that there is a very satisfactory agreement in the two sets of estimates with regard to the density of distribution of the spirals. No one can predict, naturally, whether this observed density of distribution continues indefinitely See further ciph 77-79

- 37. Conspectus of Forms Assumed For the purposes of this treatment, the spirals are considered under the following main headings
- 1 True spirals, objects which show the spiral arms so characteristic of the class
- 2 Barred spirals, marked by a nearly straight band across the nuclear portion
  - 3 Elliptical objects, with no spiral structure discernible by present resolution
  - 4 Irregular and Magellanic type spirals

While the field is conveniently divided thus, there is a very wide difference in the forms assumed. The following examples, taken for the most part from the list and descriptions in Lick Publ 13, will give a partial illustration of such variation in details of structure. Edgewise or greatly elongated spirals have in general been omitted, as in such the essential features are masked by the inclination of the object to our line of sight.

There is no very large amount of agreement as to the relative proportions of the different types of spirals. The most important factor in the percentages found seems to be, as would be expected, in the aperture of the instrument used

HARDCASTLE'S counts of the brighter nobulae on the Franklin-Adams star charts, after the exclusion of objects evidently of the diffuse type, give 173 as spiral, 233 of the elliptical type, and 327 objects so small as to resemble star



Fig 31 The Magellank Lype Spiral NGC 4449 (Mt. Wilson Photograph)

images Shapley finds a very small proportion of spirals in the 2829 objects catalogued in Hary Ann 85, p 413 (1934)

Spheroklal			4			80%
Sphidle						12%
Oval .						7 %
Spiral	ï	,		<b>Jehn</b>	thar	L 1%

However, in his study of the Come-Virgo cluster of galaxies he reports a slight preponderance of the bona-fide spiral type, 30 to 27, and of 167 objects in the Coma A cloud, 48% are classified as spiral and 5% as irregular Shapley and Amss find much smaller proportions on the Bruce plates (8% spiral and 4% irregular), but admit that "obviously the recording of spiral structure is

<sup>&</sup>lt;sup>1</sup> M N 74, p 699 (1914).

Hary Bull 838 (1926)

Harv Bull 808 (1924)
 Harv Bull 876 (1930).

1 x montes

(near 1612), 5191, 7753

largely a matter of telescopic resolution." Doubtless the most trustworthy proportions are those found by HUBBLI in his detailed and valuable monograph, "The Extra-galactic Nebulae", in Ap J 64, p 321 (1926), as follows

Filiptical			23%
Normal and	barred	spirals	71%
Irregular		_	3 %

It is the belief of the writer that the proportion of true spirals may be exen larger because of instrumental limitations in recording the smallest objects of the

spual class, see ciph 40

38 True Spirals. These are the "normal" spirals of HUBBIE, and the term is self-explanatory, in these the characteristic spiral whorls are more or less clearly seen, nearly always making their start from a nuclear portion at points very closely 180° apart. They vary in size and in the distinctness with which the spiral arms are shown, from minute objects where faint traces of spiral character can just be made out, to enormous structures like 224 (Andromeda) and 598 (M33), where the spiral arms are clearly shown, and where the obtainable scale is such that many portions of the arms can be resolved into stars

The nuclear portion shows considerable variation in both the true spirals

and the barred variety

With satellite

Nucleat bortion		a vanjara					
Rather large	f 151,	221,	221,	2903,	4504		
reteries singe	l 4011,	1736,	5218				
	29,	200,	628,	173	3137		
Small and bright	3341.	3480,	3523,	3650	1720		
	3938,	1826,	5043,	501551	5 146		
Irinnelear?	7752						
Quite faint	253,	3556,	1321				
No nucleus apparent	1337.	2537,	7511				
There is also a wide variation in the c	haracter of	the w	iorls				
Deheate and very compact	,881	2775.	5055,	5800			
Rather compact	278,	1068,	2811,	1730			
Moderately open	221,	4826,	5191	5			
	598, 2532, 334 k	628,	697,	1637.	1042		
Open, generally with knots .	2532,	3147.	3181,	3108.	41144		
Open, generally with knots	1 334 6	3686,	3726.	3892	\$13.85		
	4321.	5320					
I wo branched or S-shape	[ 3025,	1051,	4236,	5217.	5 (10)		
t no branched or near the	6217,	6296,	7610				
Single whorl?	7393						

39. Barred Spirals The designation "barred spiral", introduced by HUHHII is far preferable to "q-type spirals", used earlier by Curris. These interesting objects have as their characteristic feature a straight or nearly straight bar of matter across a nucleus which is generally rather indistinct. Sometimes the whorls will apparently start from the ends of this bar, in other cases, the whorls may form nearly a perfect ring with the bar as a diameter. See Figure 34, where four of these objects are shown

Among the barred spirals are

Barred spirals	613, 2859, 4340,	1300, 3351,	1326, 3367,	1530), 3501,	1781 3691
Barred, Saturn-shaped	4340, 936,	4391, 1455	1725,	2021	7179

HUBBLE (1 c) lists 59 baired spirals, and it would seem that it is a by no means rare type See ciph 62-64 for references to its possible significance in theories of spual structure

40. Elliptical Spirals; the Provenance of the "Minute" Spirals. The type example of this class is 221, the bright oval companion south of the Great Spiral in Andromeda. Hubbi F lists 93 objects of this type, ranging from E0 (practically round) to E7 (considerably clongated), at which point the transition to the class of true spirals is held to occur. Strictly speaking, this class contains the overwhelming majority of the spiral class, simply because the smallest flecks are necessarily recorded without distinguishable structure.

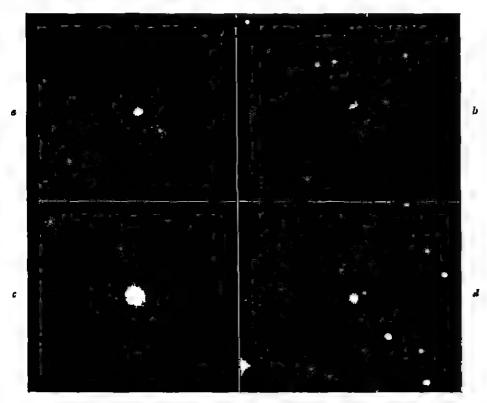


Fig. 34 Four Burrod Spirals a NGC 1300, b NGC 1530, a NGC 3351; d NGC 5921 (Lick Photographs)

Some doubts have been expressed as to the provenance of the countless very small round or elliptical objects, and their right to be classed with the genus of spirals. The writer in 1918 made the following generalization (Lick Publ 13, p. 12).

"It is my belief that all the many thousands of nebulae not definitely to be classed as diffuse or planetary are true spirals, and that the very minute spiral nebulae appear as textureless disks or evals solely because of their small size. Were the Great Nebula in Andromeda situated five hundred times as far away as at present, it would appear as a structureless eval about 0',2 long, with very bright center, and not to be distinguished from the thousands of very small, round or eval nebulae found wherever the spirals are found 'There is an unbroken progression from such minute objects up to the Great Nebula in Andromeda litelf, I see no reason its believe that these very small nebulae are of a different type from their larger neighbors."

Though this conclusion has been objected to as a "daring extrapolation", the writer feels that all the ovidence as to distribution, character, radial velocity,

etc, which has been obtained since 1918, serves only to strengthen this opinion, and were he re-writing it today, his only modifications would be minor changes in the phrasing so as to avoid the word "nebula" as far as possible. The writer finds no escape from the conclusion that all the objects of the spiral class, near or distant, 2° or 5" in diameter, with or without visible whorls, round, spindleshaped or elongated, are stellar aggregations of structures closely similar, and presumably of the same order of actual size. He places the smallest objects seen on the Crossley plates, 3" to 5" in diameter, at a probable distance of 1001 y, at this distance an object 3" in diameter would have a linear diameter of 14500 ly

There are doubtless a considerable number of objects like 221, whose projected outline is that of a slightly clongated ellipsoid, with any other exterior formations either non-existent or too faint to be recorded. As is well known, the type form of the spiral is a flat, discordal structure, roughly circular in plan, and with thicknesses 1/5 to 1/10 the diameter. When seen edgewise or nearly so, such objects will appear only as narrow spindles, with all evidences of spiral structure obliterated by the high inclination to the line of sight, whereas objects like 221 will present nearly the same cross-section from any point in space. These may

be regarded as, in effect, ellipsoidal star clusters of gigantic size

That the vast majority of the small round and elliptical objects are necessairly of the same type as 221 does not follow, though their precise nature, on any assumption, requires some measure of extrapolation. The detection of spiral structure is very markedly a function of the apparent size of the object, of the aperture of the telescope and its focal length, of plate grain and exposure time. Any of the considerable number of large spirals with somewhat accentuated central condensations or nuclear regions, if removed to several hundred times then present distance, would lose all details of spiral structure through the limits of the photographic process. The relatively very much brighter central portions of such objects as 224 and 598 require no excessive exposure times at their present distances, for many of these objects an exposure of a few minutes is adequate to obtain a legible record of the nuclear condensation, while an exposure of twenty times this length will be needed to show the whoils as strongly suming these objects iemoved to a distance 100 times as great, our present reflectors will still be able to obtain a record of the nuclear portions in an exposure of one to three hours. But, for the same object at the greater distance, any adequate record of the outlying whorls will now require an exposure of ten to twenty hours, if such were possible without undue sky blackening, even then, because of the minuteness of the structural features, these would be further obliterated by the factors of plate grain and telescopic resolution

41. Irregular and Magellanic Type Spirals There are a number of quite miegular objects of the spiral class, where the spiral structure is only faintly indicated, or entirely lacking, in some a looped or falcated structure made up

of patches is seen. Among such objects are

1 428, 1156, 2359, 2537, 2777 3077, 4214, 4401, II 2571 3034, 4618, 5144, 7309

Even more irregular are objects of the Magellanic type, of which our best examples are the Magellanic Clouds and such objects as 4449 (see Figure 3) and 35) While lacking the characteristic spiral formation, the Magellanic Clouds must be regarded as among our most "valuable" spirals because of their nearness (0,1 1061 y) with the consequent facility of study of individual components

42. Occulting Matter in the Spirals, and its Bearing on Observed Distribution. No description of the forms assumed by the spirals would be complete without a reference to the occurrence of non-luminous occulting matter, the evidence of the spirals seen edgewise or nearly so proves that these are relatively



Kig 35 The Large Magellanic Cloud. (Harvard Photograph.)

flat, round structures, and the occulting matter seems to occur in a peripheral band around the circumference. The characteristic has long been known, and was the source of some of the "blfid" and "double" objects noted by the Hen-

SCHLLS and ROSSE CURIS has treated this subject in Lick Publ 13, with illustrations showing the phenomenon in 77 spirals. This occulting matter may be

1 Irregular dark patches, generally in the central portions of the spiral, as in 147, 205, and 2655



log 36 The Edgewise Spiral NGC 1565 (Mt Wilson Photograph)

2 As manifested in spirals whose planes make a moderate angle with the line of sight, where one side is definitely fainter than the other, or seems to extend to a smaller distance on one side of the major axis. Isxamples, 2084; 2841, 4192, and 5033.

3 Dark lanes clearly in evidence on one side of the major axis in spirals

of small inclination to the line of sight, as in 3623, 4(29, and 3169)

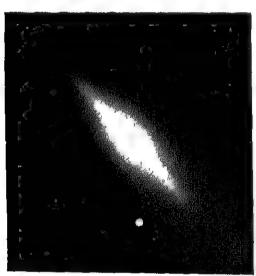


Fig 37 The Edgewise Elliptical Spiral NGC 3115 (Mit Wilson Photograph)

4 Spirals seen almost exactly edgewise, and showing indubitable evidence of a peripheral equatorial occulting ring, as in 4565 (finest example of the class), 891, 4591, and 5746

Though not observable in alledgewise spirals, the phenomenon is so frequent a one that it must be regarded as a very common characteristic of the spirals as a class. This cyidence, by analogy solely, may then be regarded as lending considerable support to the hypothesis that a similar peripheral band of occulting matter in the plane of our galaxy, and in large part presumably outside its structure, serves to cut off from our view the distant spirals which he near the projection of our galactic plane in space1

Indirectly, also, such a theory lends support to the belief that our galaxy is but one of many similar structures, as held by Easton and others, and more recently supported by Trumpler's investigations of the amount and localization of absorption within our galaxy. Though this theory is supported only by the

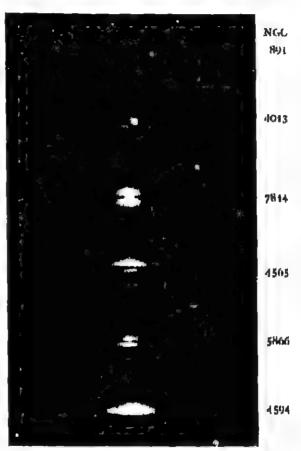
<sup>1</sup> Cf also R I SANFORD Lick Bull 9, p 80 (1917)

significant analogy of numerous external galaxies, it offers perhaps the best explanation of the curious fact presented by the peculiar distribution of the spirals, found in greatest numbers near the galactic poles, but almost never seen within the actual Milky Way structure, a phenomenon for which no other adequate explanation exists

48. Proper Motions of the Spirals. Regarded as an external galaxy, a relatively close spiral at a distance of 40°1y, and assumed to possess a motion

of 104 km /sec across our line of sight, would exhibit an annual proper motion of 0" 007. If we limit the velocity across the line of right to but 10" km /sec , a quantity of the order of the radial velocities of the larger and nearer spirals observed to date, the annual proper motion will be but 6",0007 Bearing in mind the very difficult character, from the standpoint of measurement, of even the last spiral nuclei and knots, together with the relatively short time interval vet available (ca. 30 -) years for photographic comparison and ca 75 years for visual), and the minuteness of the probable proper motions of these objects, the conclusion seems certain that the definite detection of proper motion in the spirals is far beyond existing methods and obtainable observational data

A very large amount of honest and painstaking effort has been expended on this problem, beginning with the carefully determined positions of such observers as



lig 18 Occulting Riffocts in Spirals. (Fick Photographs.) Photographed by II D Currus with the Crassley Reflector

D'ARREST three-quarters of a century ago, and extending to the photographic

<sup>1</sup> Van Maanen, Mt Wilson Contr No. 111 (1916), No. 136 (1917), No. 158 (1918), No. 182 (1920), No. 264 (1921), No. 237 (1922), No. 270 (1923), No. 290 (1925); No. 321 (1926), No. 356 (1928), No. 391 (1929), No. 405 - 8 (1930), C. Whete, Straigh Ann. 4, p. 112, 364 (1912), A N 263, p. 197, criticized by Kohold and Seriore, p. 299 and 305 (1917), 206, p. 109, 246 (1918), S. K. Kostinsky, Bull Acad St. Pátersb. (1916), p. 871, K. Reinnutt, Publ Heidelberg 7, p. 144 (1915), O. J. Lee, Pop Astr. 34, p. 492 (1916), J. M. Hawker, Pots Publ. 3, p. 135 (1921); C. O. Lameland, Pop Astr. 22, p. 631 (1914), 24, p. 658 (1916), Lowell Bull No. 73 (1916), F. R. Barnard, A. J. 30, p. 175 (1917), K. Luridmark, Pop Astr. 30, p. 623 (1922), Publ. A. S. J. 14, p. 408 (1922), M. Wolff, Publ. Heidelberg 3, p. 409 (1909), 6, p. 31 (1913), A. N. 190, p. 229 (1912), 202, p. 147 (1916)



Fig 39 The Spiral NGC 7217 (Mt Wilson Photograph) An excellent example of a spiral with compact and delicate whorls

measures and discussions of van Maanen, Lampland, Lundmank, and others, in recent years

With a full appreciation of the succee and careful investigation which has been devoted to this difficult problem, but with the conviction that any tabulation of the often contradictory results would only mulead and cause confusion, the



Fig 40. Inturnal Motions in NGC 3034 (MSI) as determined by VAN MAANES (VAN MAANES). This spiral has been chosen as a typical example of VAN MAANES's derived motions. It will be noted that the motions are provallingly outward along the spiral arms. The arrows indicate the magnitude and direction of the mean annual motions, and their scale (O".4) is indicated on the illustration. The comparison stars are inclosed in circles.

author profers to omit any discussion of past proper motion results on the spirals, and to refer the reader to the references quoted. VAN MAANEN'S values for several

will be found in ciph 45. We have as yet no certain knowledge of the proper

motion of any spiral

44. The Spirals as a System of Reference There is, however, a possible interesting by-product of the apparent total lack of a motion of translation in the spirals. Then tremendous distances, and then lack of detectable proper motion, give us a large number of essentially "stationary" points of reference, which should eventually prove to be of great importance in studies of the rotation of our own galaxy. The assumption of average fixedity seems amply justified, for small motus peculiares ought to be at random and to disappear in the mean. If then two sets of measures at a considerable time interval could be made of a large number of small and almost stellar spirals uniformly distributed in galactic longitude, preferably not more than 30° from the galactic plane, and referred to adjacent faint stars (magn 18+), it is conceivable that results of great value might be secured as to the rotation of the galaxy, local irregularities, etc Were our galaxy rotating in 108 years, stars in the peripheral regions would be expected to show tangential annual proper motions with reference to such points d'appur of the order of 0",01, which might be detectable with some certainty in 100 years

45. Internal Motions of the Spirals, Visual Determinations. At a distance of 1061 y, annual motions across our line of sight will correspond to

actual velocities as follows

Annual motion 0",0001 0",001 0",01 0",05 Velocity, km/sec 145 1450 14500 72500

These results indicate that, on the island universe hypothesis, internal motions in the spirals must be enormous to be detected by present methods. Such high velocities will also presuppose the existence of inordinate masses.

A vast amount of work has been done by VAN MAANEN in his investigations of spirals for internal motions. VAN MAANEN's more important results are given

below in Table 13

It will be noted from this tabulation that all eight objects agree in showing a stream motion outward along the spiral arms amounting to about 0",02 annually in the mean. The average distance of these spirals is 2,6 10<sup>8</sup> ly, so that this motion would correspond to an actual velocity of 79000 km/sec. In general, van Maanen's values indicate a quasi-rotation in the direction of the concave side of the spiral arms, which seems directly opposite to the spectrographic results of Stipher (see ciph 46). In his final paper 2 van Maanen investigates all possible sources of circuin the plates of in the methods of measurement which he employed, and concludes that the values he has given represent actual motions of roughly the order found. He has accordingly derived distances for the larger spirals ranging from 10<sup>8</sup> to 10<sup>1</sup> ly, with diameters ranging

<sup>1</sup> A VAN MAANLN, See the references under preceding section, K Lundmark, Internal motions of Messiei 33 Ap J 63, p 67 (1926), Mt Wilson Conti No 308 (1926), On the internal motions of spinals Publ A S P 34, p 108 (1922), J II Jeans, Internal motions in spiral nebulae M N 84, p 60 (1923), W II SMARF, The motions of spiral nebulae Ibid 84, p 333 (1924), W J A Schouten, Probable motions in the spiral nebulae Messier 51 Obs 42, p 441 (1919), D Parchomenko, Eine von den möglichen Interpretationen dei inneien Bewegung in den Spiralnebeln A N 222, p 369 (1924), B Meyermann, Die inneie Bewegung in den Spiralnebeln Ibid 221, p 239 (1924), J Jackson, On the influence of comparison stars on photographic proper motions MN 84, p 401 (1924), J II Jans, On the internal motions in spiral nebulae Obs 40, p 60 (1917) and 44, p 352 (1921), S Kostinsky, Motions in M 51 stereoscopically determined (Russian) Bull Acad St Pétersb (1916), p 871, M N 77, p 233 (1916)

Table 13 Internal Motion in Spirals, from van Maanen

Object	Proper motion		ninthra	Annual Internal motions		
	L	ð.	_ a	Vanwal rudwillin and come		
598 (M 33)	40	/ <sup>4</sup> ,003	0",00·	399 nobular points measured Mean stream motion outward along arms, +0",020, mean transverse, -0",003 Periods deduced from 60000 to 240000 years Lundmank's measures of same object gave mean stream motion  -0",002, mean transverse -0",0004		
<b>24</b> 03	+	,002	,00	Moan rotational, 0",015, mean radialoutward +0",014, with considerable differences with distance from center Periods deduced, 50000 to 120000 years		
3031 (M81)	i	,014	- ,00;	Stream motion outward along arms of 0",039, combined with alight transverse motion of +0",007 Deduced period, 58000 years		
4051	-	.003	J ,019	Radial motion outward 0",014		
4736 (AJ94)	-	,014	,00	Stream motion along arms of 0",021, plus transverse motion of 0",009		
5055	+	,005	,015	Stroum motion outward + 0",019, combined with transvence motion of - -0",004 Slight decrease with distance from center		
5195 (M51)	-	,001	J ,000	Mean stream outward, +0",(121, mean trans-		
5457 (M101)	-1	,005	- ,01:	Rotation of 0",022 at 5' from center Motions provailingly outward, with slight increase of rotation toward centur Deduced period, 85000 years.		

from a few light-years to several hundred. As noted later, both Jeans and Brown have published theories of spiral structure to fit the magnitude of the motions found by VAN MAANEN.

LUNDMARK has pointed out that the outward motions found by VAN MAANEN mean the comparatively rapid disintegration of the spiral, and that, with such motions, no spiral could exist longer than 3 • 10° years as a shiring body.

The measures of VAN MAANEN and the conception of the spirals as individual galaxies can not both be true, unless we are willing to assume velocities in the spiral arms which must occasionally amount to one-third the velocity of light. It seems impossible, moreover, to reconcile these values with the direction of the spectrographic velocity of rotation.

The intervals available for VAN MAANKN's measures were under twenty years. There seems at present no escape from the conclusion that these carefully made measures are subject to some instrumental error as yet undetected, and that they must be rejected until confirmation is secured by other observers and with materially increased time intervals. In view of the numerous other lines of evidence which now point so unequivocally to the adequacy of the island universe theory of the spirals, no other course is open

48. Rotation of the Spirals; Spectrographic 1. Spectrographic evidence of the rotation of a approximant was first secured by V. M. SLIPHER in 1914, and evidence

<sup>&</sup>lt;sup>1</sup> V M SLIPHER, The detection of nebular rotation. Lowell Bull 2, p.65 (1914), Spectrographic observations of nebulae Pop Astr 23, p 21 (1915); Spectrographic observations of nebulae said star clusters. Hid 25, p 36 (1917), Spectrographic observations of the rotation of spiral nebulae. Ibid 29, p 272 (1921), F G Prass, The rotation and radial velocity of the spiral nebula NGC 4594. Wash Nat Ac Proc 2, p. 517 (1916), Mt Wilson Comm No 32 (1916), Publ A S P 28, p 191 (1916), The rotation and radial velocity of the central part of the Andromeda Nebula. Wash Nat Ac Proc 4, p.21 (1918), Mt Wilson Comm No 51 (1918).

has since been obtained by Stiping and by Prisi for the rotations of a number of objects of the spiral class. Rotations have been definitely established by Stiping for six objects, and these effects are suspected in a number of others. Those definitely determined are

221, the well-known elliptical companion south of the Great Spiril in Andromeda 224, Andromeda (M31)

1068, (M77)

2683

3623, (M65)

159 F

On the assumption that the side of the spiral which shows the most prominent lanes or other occulting effects is the nearer to us, which seems a certainty, STIPHER states that all these spirals rotate in the same direction. "The direction is that in which the arbor of a spiral spiring turns when the spiring is being wound up." STIPHER found that the rotation in 224 was greater near the nucleus, the inclination of the lines of 4594 indicated a speed of 100 km/sec at 20" from the nucleus (PLISI, 330 km/sec at a distance of 2' from the nucleus)

The two papers by Prasi contain the most detailed as well as the most authoritative information yet available in this exceedingly difficult field (an exposure of 80 hours was necessary on 4594, and 79 hours on Andromedal). For 4594 he found that the velocities, as determined by a least squares solution, followed the linear relation.

$$y = -2.78 \text{ v} + 1180 \text{ km/sec}$$
.

and similarly he found for the Andromeda spiral (224)

$$v = -0.48 \text{ v} - 316 \text{ km/sec}$$

That is, in both spirals the angular speed of rotation is essentially the same for different distances from the nucleus. This relation gave a speed of 58 km/sec at a point 2' from the nucleus in 224. In this object also,

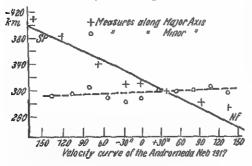


Fig 41 Rotational Velocity Diagram of NGC 221 (Andromeda) (Prase)

a plot derived from an exposure taken with the slit along the minor axis of the spiral likewise shows a linear relation, but with a much smaller slope than that derived from the spectrogram along the major axis

These rotational results of Pease, in their indication of a rotation obeying a linear instead of a quadratic law with varying distances from the nucleus, are of tremendous theoretical interest. They apparently require that we abandon

the dynamical models of every earlier theorist, in which the component elements move in orbits obeying the inverse square law. It would seem that the only theory which can satisfy these spectrographic results is one of the nature of the still uncompleted theory of Brown (see ciph 63), in which the particles are assumed to move in central ellipses, under a law of attraction of the form  $-n^2r$ 

47. Spectra of the Spirals, Stellar Type The great majority of objects in the spiral class show a continuous spectrum crossed, where the brightness of

the object permits the use of a sufficient scale for their detection, by the dark absorption lines characteristic of stellar spectra, and in all essential features a duplicate of the integrated spectrum of the Milky Way or of a star cluster It is this almost myarable continuous spectrum which earlier carned for them the name "white" nebulae. The descriptions of their spectrum will almost always he of the form solar type, like a Class G star, type GO or later, etc. Reference should be made here to the investigations of LUNDHARK and LINDRIAD1 on the effective spectra of celestial objects. They investigated 24 objects in all. and obtained the following mean values

Number	Close	Wase hangth maximum	liquivalent steller class
6	l'innutary	4130 Å	B±
4	Cluster	4190 Å	AB
14	Spiral	4290 Å	G2

See also clph, 49, 50

48. Spectra of the Spirals; Emission Lines There are some relatively rare and for that reason very passing exceptions to the almost universal rule that the spectrum of a spiral is such as would be obtained from a large congeries of stars. The total number of such exceptional cases in unknown, but it is probably not large. Among these may be noted.

1068

4051

4214

4449

Volcality |- 11(8) km /www Continuous spectrum with absorption lines, crossed by nobular emission lines. Strugg, Lowell Bull 3, p 59 (1917) reports that these lines are not images of the slit, but small disks.  $N_1$  and  $N_2$  were found strengly mellined, indicating a valuality of 300 km/sec. at 1' from the nucleus

Nucleus like a planetary nobula, showing bright H, 4686 A, and O lines (HUMASON) Continuous spenirum crossed by some absorption lines and by nebular emission

lines (Stripter)

This is a very irrequiar object of the Magolianic type, of Figure 33. Prace [Ap ] 46, p 24 (1917), Paris VIII, b)] notes the presence of 230 nebulous stars or patches (unto the numbers with the Large Magallante Cloud) Noted as continuous plus possible emission them by Wolf in Sitzber Holdelberg Ak, Abt A, Nr 15 (1912) Stippers describes an strong continuous spectrum crossed by the strong emission lines possible to the gustinuous spectrum crossed by the strong emission lines possible to the gustinuous spectrum crossed by the strong emission lines possible to the gustinuous spectrum crossed by the strong emission lines possible to the gustinuous spectrum crossed by the strong emission lines possible to the gustinuous spectrum crossed by the strong emission lines possible to the gustinuous spectrum crossed by the strong emission lines possible to the gustinuous spectrum crossed by the strong emission lines possible to the strong continuous spectrum crossed by the strong emission lines possible to the strong continuous spectrum crossed by the strong emission lines possible to the strong continuous spectrum crossed by the strong emission lines possible to the strong continuous spectrum crossed by the strong emission lines possible to the strong emission lines possible to the strong continuous spectrum crossed by the strong emission lines possible to the strong emission lines possible to the strong emission lines emission lines emission lines emission lines emission lines emission lines emission lines emission lines emission lines emission lines emission and derives a radial volocity of - 200 km /sec

A passible explanation for such exceptions to the almost universal absorption character of the spectrum of the spirals is doubtless to be found in the assumption of a large number of masses of the type of the diffuse or planetary nebulae intermingled in the prevailingly stellar composition of occasional spirals. 4449 contains 230 nebulous stars or patches, 278 patches of diffuse nebulosity (or planeturks) have been catalogued in the Greater Magellanic Cloud, a number of such diffuse patches have been noted in 224 (Andromeda) and other large spirals. Were the Cloud removed to 100 times its present distance, it would appart as an anre-colved patch not unlike 4449, and about 2',5 long

It is probable also that, in such a case, the emission lines are vastly easier to record thun the continuous spectrum of the background of stars. With the very keng exposures which are necessary to secure even a faint record of the continuous sixs trum of an integrated mass of stars in a cluster or spiral, and bearing in mind the advantage of concentration of the emission spectrum of such nebulous inclusions into a few hright lines, it would seem possible that such nebulous patches would easily be spectrographically recorded as emission

lines overlying the continuous background.

<sup>&</sup>lt;sup>1</sup> Photographic offective wave-lengths of nebulae and clusters. Ap J 46, p. 206 (1917), 50, p 176 (1920).

By way of illustration of this point using the ratio of speed between the spectrograph attached to the Lick Refractor and the quartz spectrograph of the Crossley Reflector, as given by Faih, = 1 25, Farir's instrument should have recorded easily in 30 initiates the bright lines of 6853 (the Dumb-bell Nebula), whose areal brightness is given as 10,8 by Wirlz Fath secured nothing at all of the continuous spectrum of the spiral 5194 in an exposure of 14,5 hours, although Wirlz' value for the areal brightness of this spiral is 10,9

49. Color Indices of the Spirals, the Results of Searcs Considerable work has been done by Searcs, Shapley, and others, on the color indices of objects

or different parts of objects of the spiral class

Taking two series of exposures, one on ordinary photographic plates and the other on isochromatic plates through a color screen which transmitted the light to the red of 4900 Å, Sharfs found notable differences in different parts of the spirals 4254, 4736, and 5194. The nuclear portions are strong on the "yellow" plates. On the other hand, the branches and especially the condensations found along the spiral arms are very blue "the knots of nebulosity are certainly bluer than the bluest of the neighboring stars", and are described as resembling in that respect the central star of the Ring Nebula in Lyra. For elliptical nebulae, however, Hubbit reports that plates exposed through a visual color filter show no difference between the nuclear and the outer regions.

SHAPLEA, using the Holdischik-Hopmann visual magnitudes for comparison with the photographic, has tabulated the color indices of 43 spirals, with the mean results

	Numbes	Color index
All elliptical objects All spirals	12 28	+0,33 +0,22
Triegilar	3	0,37

He points out for 7619 (not included in the tabulation) that this spiral, the faintest, fastest, and probably the most remote of those discussed, has the largest color index,  $M_{ph} - M_p = 2.8$  Hubble and Humason, however, (see ciph 55)

find a mean color index of +1,1 for the spirals they observed

Carpenter finds for 3034 (M82) no difference between the yellow and the blue images, although a photograph on a panchiomatic plate shows a substantially different distribution of brightness. For 5194 (M51), however, he corroborates the results obtained by Searls. The nucleus appears red, and has a color index of +1,6, there is a continuous increase in blueness in passing outward along the arms from their base, the color index varying from +0,6 near the nucleus to -0,3 at about one revolution from the nucleus. He suggests that such an effect might be due to the fact that younger stars are prevailingly near the nucleus, and older stars further out, most of the light in the latter case coming from the hotter stars of the giant sequence.

<sup>&</sup>lt;sup>1</sup> F II SEARTS, Prohomory results on the color of nebulae Wash Nat Ac Proc 2, p 553 (1916), Mt Wilson Comm No 36 (1916), Publ ASP 28, p 191 (1916), Distribution of color in certain spiral nebulae Pop Asti 25, p 34 (1917), The surface brightness of the galactic system as seen from a distant external point, and a comparison with spiral nebulae Ap J 52, p 162 (1920), Mt Wilson Contr No 191 (1920), II SHAPLEY, Note on the velocities and magnitudes of external galaxies Wash Nat Ac Proc 15, p 565 (1929), E b CARPINIER, I he distribution of color in two extra-galactic nebulae (abstract) Publ ASP 43, p 294 (1931)

<sup>&</sup>lt;sup>2</sup> Ap J 71, p 231 (1930)

50. The Radial Velocities of the Spirals<sup>1</sup>. The first radial velocity of a spiral (plates taken in 1914), the first spectrographic evidence of rotation of a spiral (1914), and the first spiral velocities of considerable magnitude, are due to V M STIPHER Very noteworthy extensions to our knowledge of the radial velocities of the spirals have been made at Mt. Wilson through the work of Humason, Prast, and others

Very rapid progress has been recently made in this difficult field at Mt Wilson, owing to the use of the new Rayron lens, which very materially shortens the exposure times meeded. 45 spiral velocities secured thus have recently been published?

This lens, of very short focal length and remarkable focal ratio, is an 8-fold calargement of a microscope objective, with an extra element added to provide for a source at an infinite distance. Its aperture is 50 mm, and its focal length is 32 mm, giving a focal ratio of 1 0,59, without doubt the highest ratio ever camployed for such purposes. The dispersion at 4500 A is 418 angstroms per mm with two prisms, and about 875 angstroms per mm with one prism, the total length of the spectrum from 3888 A to 5015 A is only 2,67 mm! A wide slit can be used, 0,2 to 0,6 mm. While the probable error of a spectrogram taken with this remarkable lons is estimated to be of the order of 400 km./sec, this is of little importance in comparison with the large radial velocities which are being obtained

Radius velocities are now (January, 1932) available for 90 objects, this total includes the two Magellanic Clouds. The radial velocities of the spirals have the following salient characteristics

1 They are provailingly velocities of recession (+)

4 Ap J 74, p 35 (1931)

2 They display an enormous range, from -300 km./sec to +19600 km /sec.

3 Remarkable groupings of spirals have been discovered by Humason, contiguous in apparent location in the sky, and with large radial velocities nearly identical in amount

V & Stepher, The resided volocity of the Andromode nobula. Lowell Bull 2, p. 56 (1914), Spectrographic observations of nobulae. Pop Astr 23, p. 21 (1915), Two nebulae with unparalloled vehiclies. Lowell Circ., January (1917), A.N. 243, p. 47 (1917), Spectrographic observations of nobulae and star clumbers. Pop Astr 25, p. 36 (1917), 30, p. 9 (1922), Nebulae Proc Anter Phil Soc. No. 5 (1917), R.A. 9 Can. 12, p. 72 (1917), M. Wolf, Reports in V.J.S. 49, p. 162 (1914), 50, p. 97 (1915), F. G. Parre, Radial velocities of nebulae. Publ A.S.P. 27, p. 133 (1915), The radial velocity of M33. Ibid. 28, p. 33 (1916); Radial velocities of NGC 3779 and 1700. Ibid. 30, p. 235 (1918), Ap.J. 51, p. 276 (1920), M.L. Humadon, Radial velocities of two nobulae. Publ A.S.P. 39, p. 317 (1927). The large radial velocity of NGC 7619 Wash Nat. A Proc. 15, p. 167 (1929), Radial velocity of one nobulae in the cluster of faint nebulae in Ursu Major described by Barde (A.N. 233, p. 65 (1928), Ap.J. 71, p. 356 (1930)], Radial velocity of two nobulae in the Porsons Cluster. Ibid. 71, p. 355 (1930), Apparent velocity-shifts in the spectra of faint nobulae. Ibid. 74, p. 35 (1934), R. F. Sarroup, Radial velocity of NGC 2681. Publ A.S.P. 34, p. 222 (1922), The radial velocity of the compenion of the Andromeda Nebulae. Ibid. 38, p. 44 (1926), G. H. Tauram, The motions of the spiral cellulae. Pop Astr 24, p. 111 (1916), H. N. Rumant, Radiation pressure and celestial motiona. Ap.J. 51, p. 111 (1916), H. N. Rumant, Radiation pressure and celestial motiona. Ap.J. 51, p. 111 (1916), H. N. Rumant, Radiation pressure and celestial motiona. Ap.J. 51, p. 111 (1916), H. N. Rumant, Radiation pressure and celestial motiona. Ap.J. 51, p. 111 (1916), H. N. Rumant, Radiation of spiral nebulae. Of the spiral nebulae. Rumantam and spiral nebulae in the atellae system. K.S. Vet Aland Handl. 60, No. 8 (1919), G. Steffmissure, Analysis of radial velocities of globular clusters and non-galactic nebulae. Ap.J. 61, p. 351 (1928), L. Courvoure, Bestimmong der absoluter

lable 14 Radial Velocities of the Spirals

NGC			km /sec		Spectial class	More to m	
205 221 224 278	63°,9 64',4 64',1 66',4	-22°,1 -23 ,1 -23 ,1 -18 ,2	- 300 185 220 + 650	Dum 5 5   5	G811	l ocal l ocal l so al l so al l ocal	
380 383 384 385 401 584	70 ,2 70 ,2 70 ,2 70 ,2 70 ,3 94 ,2	-31 ,4 -31 ,6 -31 ,6 -31 ,6 -28 ,1 -68 ,9	+ 1400 + 4500 + 4500 + 4900 - 25 + 1800	Hum Ifum Ifum Ifum Ifum Ifum	G3 G5 G5 G5	Proces Chater Proces Chater Proces Chater Local	
\$98 936 1023 1068	77 ,0 110 ,0 88 ,5 115 ,7	-32 ,6 -54 ,7 -20 ,2 -52 ,2 -14 ,3	70 + 1300 300 920 4800	P   S   S     S  -   Ilum	651 I	Local Local Tocal Local Poiseus Chistet	
1273 1275 1277 1700 2562	93 ,9 94 ,0 94 ,0 147 ,5 145 ,2	- 14 ,3 - 14 ,2 - 14 ,2 - 27 ,7 + 28 ,0	+ 5800 + 5200 + 5200 + 800 + 5100	Hum Hum Hum Llum P Hum	(14) (14)	Persons Chider Persons Chater Persons Chater Focal Cancer Cluster	
2563 2681 2683 2841 2859	145 ,2 110 ,0 132 ,9 109 ,7 132 ,6	+28,0 +38,4 +38,3 +43,0 +44,8	+ 4800 + 700 + 400 + 600 + 1500	Hum San S- - S Hum	(±)	Cancer Cluder   Local   Local   Local   Local?	
2950 3031 3034 3115 3193	98 ,0 85 ,2 84 ,3 190 ,1 154 ,7	+43 .7 +39 ,8 +39 ,4 +37 .7 +54 ,8	+ 1500 - 30 + 290 + 600 + 1300	Hum S S S Hum	G4 KLL K1 f,	Tocal? Tocal Tocal Tocal Tocal?	
3227 (i) 3368 3379 3489	158 ,7 170 ,3 176 ,3 175 ,1 176 ,0	+ 55 ,4 +48 ,5 +57 ,6 +58 ,0 +61 ,2	+ 1150 +19600 + 940 + 810 + 600	Hum Hum S S+ S+	G5	Focal? Leo Chister Focal Local Local	
3521 3610 3623 3627 4051	197 .7 86 ,4 181 ,4 181 ,9 104 ,5	+53 .5 +53 .5 +64 .7 +64 .7 +64 .6	+ 730 + 1850 + 800 + 650 + 650	S Hum S S	G2	local Isolated Focal Local Local Local	
(2) 4111 4151 1192 4214	83 ,4 92 ,1 97 ,1 207 ,0 102 ,1	+58,1 +71,2 +74,1 +75,9 +77,4	+11800 + 800 + 960 + 1150 + 300	Hum S S+ Hum S	G <sub>5</sub>	Ursa Maj Cluster Local Local? Local? (Virgo) Local?	
4258 4374 1382 4449 4472	80 ,8 220 ,1 206 ,2 79 ,4 229 ,4	+67,8 +74,6 +80,2 +71,5 +71,0	+ 500 + 1050 + 500 + 200 + 850	5 Hum 5 S	G4	Local Local? (Virgo) Local? (Virgo) Local Local? (Virgo)	
4486 4526 4565 4591 4649	225 ,9 232 ,7 166 ,0 241 ,8 238 ,0	+75 ,6 +70 ,9 +86 ,6 +52 ,8 +75 ,1	+ 800 + 580 + 1100 + 1140 + 1090	5 5 5 5+ 5		Local? (Vingo) Local? (Vingo) Tocal Local? (Vingo)	

(Continued )

	(continues)							
NG.	(wither	tin .	Rad. vol. km./vae	Anthor	Spectral clean	Allocation		
4736 4826 4853 4860 4865	71 .1 262 .6 21 .1 27 .7 26 .0	74 .7  -85 ,4   88 .1   87 .6  -87 .9	+ 290 + 150 -1 7600 + 7900 + 5000	S Hum Hum Hum	GLL GLL G1 G3 G3	Local Local Come Ber Chaster Come Ber Cluster Come Ber Chaster		
4872 4874 4881 4884 4895	24 ,d 24 ,d 15 ,6 26 ,6 26 ,4	87 .7   87 .7   86 .6   88 .2   86 .5	6900  - 7000  - 6900  - 6700  -  8500	Hum Hum Hum Hum Hum	G3 G4 G3 G3 G4	Coma Ber Cluster Coma Ber Cluster Coma Ber Cluster Coma Ber Cluster Coma Ber Cluster		
11 4045 5005 5055 5194 5236	26 ,0 46 ,4 49 ,0 49 ,0 261 ,4	86 ,5   78 ,1   73 ,1   67 ,5   42 ,9	6600  -  900  + 450  -  250     500	Hum S S S	GLL	ComaBer Cluster Local Local Local Local		
5457 5866 6350 6658 6661	45 ,0 36 ,0 34 ,9 355 ,4 355 ,6	59 .1   51 .3   13 .7   14 .6   14 .6	+ 300 + 650 -1 3000 -1 4100 -1 3900	Hum S Hum Hum Hum	G+P   G3   G3   G5	Local Local Local Local Local Located Located Located		
6702 6703 6710 6822 6824	18 ,5 18 ,6 0 ,2 327 ,8 32 ,0	18 .7   18 .6   11 .6   18 .3   14 .6	+ 2250 + 2000 + 5100 + 150 + 3200	Hum Hum Hum Hum Hum	G4 G3 G3 Pd G4	Isolated Isolated Isolated Local Isolated		
7217 7212 7331 7611 7616	29 ,6 34 ,8 36 ,8 30 ,3 40 ,1	20 ,6 17 ,0 21 ,7 48 ,8 -49 ,0	1050   15000   500   1400   1900	Hum Hum S Hom Hom	G4 G3 G2 G1	Local Isolated Local Pogasus Chuster Pogasus Chuster		
7619 7623 7626 L. Cl. S. Cl	10 , 1 30 , 3 30 , 5 224 244	49 ,2 49 ,1 49 ,2 32 43	3800   1800  - 3700   280  - 170	Hum Hum Hum Wis Wis	G2 G3	Pogasta Cluster Pegasta Cluster Pegasta Cluster Local Local		

Notes to Inble 14.

1 One of the brightest spirals in Characte's Cluster in Leo,  $\alpha=10^{h}~24^{m}.0$ ,  $\delta=1~10^{h}~50'~(1030,0)$ 2 Heightest object (No. 24) in Baane's Ursa Major Cluster,  $\alpha=11^{h}~43^{m}.3$ ,

These values are so exceptional in the respects mentioned that there is a tendency in recent literature to refer to them as "apparent" velocities. While it is not at present possible to render any decision as to the reality of these speeds, there is reason for the belief that they represent actual velocities, at least in greater part. For this reason, and for convenience, they will be referred to in the balance of this treatment simply as radial velocities. Because of their size and their prevailing characteristics of recession, they have formed the basis of numerous speculations and have, in particular, been regarded as the subject matter for various types of "relativity universes".

So intimately have they come to be connected with such questions and with one theory of the distances of the spirals, that the pertinent data concerning the radial voice ities of the spirals will be segregated, at the risk of some repetition. The values are given at this point, with spectral class where known, galactic

coordinates, and allocation into groups. They will be given again, with derived data as to dimensions and distances, in ciph 56. See also Appendix 8.

The successive columns in Table 14 are as follows

Column 1 The NGC number

Columns 2 and 3 The galactic coordinates These are taken from Emanuetli's excellent tables, where the origin of galactic longitudes is chosen so as to make the longitude of the solar apex = 0

Column 4 The radial velocity

Column 5 The authority for the velocity This is not always the observer, for example, the plates of 4192, 4374, 4853, 4860, 6702, 6703, 7217, 7242, and 7626 were obtained by Plase In this column, Hum = Humason, S = Stipher, S+ = Slipher and others, San = Sanford, Wil = Wilson

Column 6 The spectral class, when known, when standing alone, the values are as assigned by Humason, when followed by LL, they are from Lundmark and Lindblad

Column 7 Humason's allocation of objects to clusters of spirals. The term "isolated" is used for spirals of high velocity which may belong to similar clusters, not yet substantiated, while "local" is applied to objects which are presumably members of our own local system of galaxies.

- 51. Distances of the Spirals Parallaxes There have been numerous published values of duect parallaxes of the spirals in both the older and the more modern literature of the field. These give distances which are in diametrical contradiction with the values secured by other methods, and their range is wide. A tabulation of these conflicting and now almost universally discarded values could only cause confusion, and the writer prefers to omit all reference to them for this reason.
- 52. Distances of the Spirals from Novae Since 1917 a very large number of novae have been discovered in several spirals, among which the Great Spiral in Andromeda (224) leads the list. These are given in Table 15

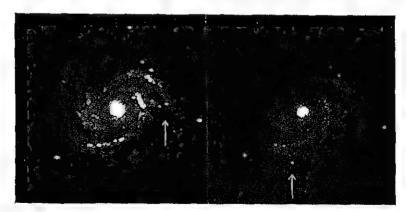
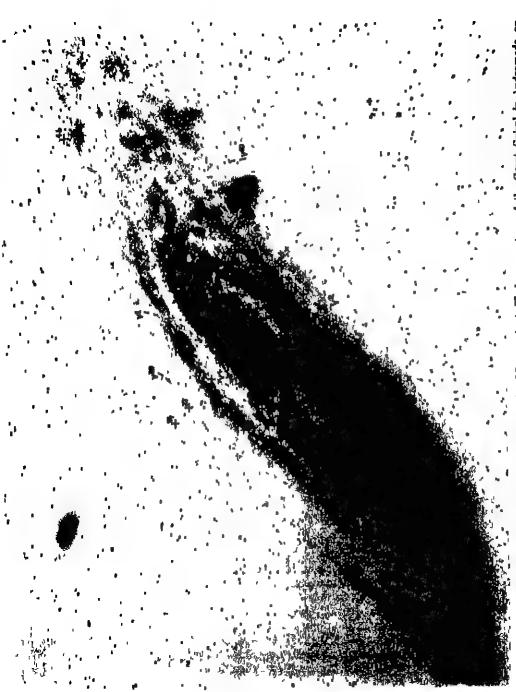


Fig 42 Two Novae in the Spiral NGC 4321 (Lick Photographs) Left taken April 19, 1901 Right taken March 2, 1914

The wealth of novae in the Andromeda spiral far exceeds the number of galactic novae (fewer than 40). As Hubble has well pointed out, aside from the uncertainty in the determination of the zero point, the mean absolute magnitudes are determined for the novae in 224 with much greater precision than for those in our galaxy.



tive of the Great Spiral in Andromeda on A number of variable stars are also shown Honner estimates that 30 novae appear in this spiral per year Prom HUERLE, Ap J 69, Plate II (1929) Novae and Variables in NGC 224 (Andromeda) shich are marked the novae which have app

Table 15 Novae in Spirals

No	Number of novae	Viern magn at maximum	Notes
221	87	17,2	Including S Andromedae, which appeared in 1885 (magn 7,2 at maximum), 87 novae hav been discovered in 221 (Andromeda). Nosto 22 were discovered in 1917 to 1922 by Ritches, Plast, Shapily, Santord, and Humason. Nos 23 to 86 were discovered by Hubbit of which he has since rejected Nos 26, 36, and 39 as possibly long period variables. Nos 8 to 90 were found by Duncan, Publ. A.S.P. 40 p. 347 (1928). Santomedae is not included in the maximum given. The magnitudes conditionates, dates of observation, etc., of these noval are assembled by Hubbit in, "A. Spiral Nebulas a. Stellar System, Messier 31.". Ap. 69 p. 103 (1929), Mt. Wilson (ontr. No. 376 (1929)
2103	!	16.5?	RECULY, Publ A S P 29, p 210 (1017)
2608 2841	1	11 7	Worl, AN 210, p 373 (1920)
3031	1	16	Prost, Publ A S P 29, p 213 (1917)
3147	i	14 ?	REACHLY, Publ A S P 29, p 210 (1917) Mrs Roberts, Publ A S P 29, p 211 (1917)
4303	i	14 5	REINMUTH and WOII, Harv Bull 836 (1926
4321	2	14	Curris, lick Bull 9, p 108 (1917)
4486	1	11,5	BATANOWSKY, A N 215, p 215 (1922).
4527	1	15	CURTIS, 1 c
5253	1	7,2	Mrs briming, Hary Cal. 1 (1805)
58578	2	18,5	RITCHI Y, 1 C
6946	1	14,6	RIICHLY, I c
598	4		ITUBBII, I c, p 119, footnote

The list attempts to determine the distance of the spirals by analogy with the galactic novae, made by  $Curis^1$  in 1947 were roughly of the right order, though rendered somewhat uncertain by the lack of accurate knowledge of the absolute magnitudes of galactic novae, an uncertainty which still persists Assuming tentatively that the galactic novae were at an average distance of 10000 ly, and with an average apparent magnitude at maximum of 5, he derived a difference of about 13 magnitudes between the galactic and spiral novae, indicating that the spirals were 400 times as far distant as the galactic novae. This gave a distance of the order of  $4 \cdot 10^6$  ly for the spirals "Correlations between the novae in spirals and those in our galaxy indicate distances ranging from perhaps 500000 ly in the case of Andromeda, to 10000000 or more lightyears for the more remote spirals"

A slightly greater amount of data on the galactic novae has since become available, and several similar and more accurate correlations have been made. There are few who would maintain, however, that it may not eventually be necessary to multiply or divide the distances of spirals found by the novae method, by a factor of from 2 to 5. Our knowledge of the absolute magnitude of galactic novae at maximum must be regarded as still highly uncertain Lundmark has placed this at -6,1, while Hubble, determining the distance of 224 from Cepheids, places the mean absolute magnitude of galactic novae at -5,7

There are, in addition, some other difficulties. The absolute magnitude of S Andromedae, in order to correspond with the values found for the familiar novae in that spiral, must have reached nearly -15. This is a truly enormous

Wash Nat Ac Proc 9, p 218 (1919), Lick Bull 9, p 108 (1917)

value, though as a parallel instance we have but to assume that Tycho's nown (which reached an apparent magnitude of about —5) was in reality as distant as 3300 ly. If the smaller spirals 3147, 4321, and 4527 are at a distance of 5 · 10° ly. (Hubble places 4321 at 4,6 · 10° ly), the absolute magnitude of the four 14th magnitude novae found in these objects must have been close to —12, the same is true for the nova found in 5253 by Mrs. Flexing. It would seem that we must assume two classes of novae to take care of all these discrepancies,—the one of roughly als magn —5 at maximum, and a class of comparatively rare exceptions 10(XX)-fold brighter.

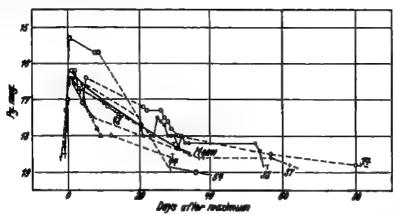


Fig 44 I light-curves of Six Novac in NGC 224 (Andromoda) (HURRER) Observed near maximum

There is no doubt that the majority of the objects in 224 attributed to this class are really novue. While for many of the objects the data are fragmentary, Hunna assembles the data for six which were observed over a longer interval (see Figure 44), and the composite light-curve of these has all the characteristics expected from novae in rapid rise, slow decline, and minor fluctuations

58. Distances of the Spirals: from Caphelds. The derivation of the distances of the spirals through the period-luminosity relation adduced for Capheld variables is due entirely to HUBBIE (1924). He has found 50 variables in 224, of which 40 are Caphelds, and 35 Caphelds in 598—9 have been discovered in 6822, none have thus far been reported from other spirals. The characteristics of these, together with 105 determined by Shapery in the Small Magellanic Cloud, and 6 from 6822, are shown in Hubbie's diagrams, reproduced below as Figures 45 and 46

Using SHAPLKY's values for the Cepholds in the Small Magellanic Cloud, for which he had derived the relation'

$$m - M = 17.55$$
.

the corresponding modulus for 598 (M33) was found to be,

m-M=22,1, or a distance of 850000 Ly

Similarly for 224 (Andromeda), the modulus is,

m - M = 22,2, or a distance of 9000001 y.

HUBBLE definitely calls attention to the fact that all these values are affected by any change of the zero-point of the Cephoid period-luminosity relation, and derived by Shapley.

There have been a number of revisions of Shapily's values, of which one of the latest and most authoritative is that due to Advans, Joy, and Humason's

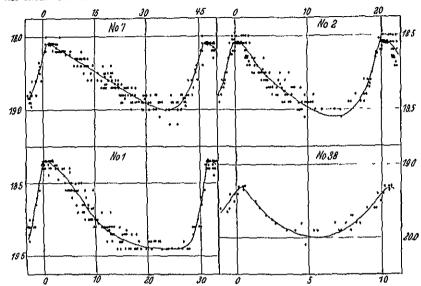


Fig 45 Light-curves of Four Cepheids in 224 (Andromeda) (Hubbi i ) the ordinates are photographic magnitudes, and the abscissae, days

These authors have determined the spectroscopic absolute magnitudes of 80 (e-pheids with periods between 1,6 and 45,2 days, using an extrapolation from the

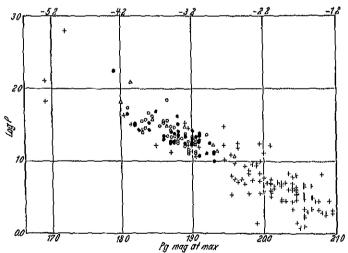


Fig. 46. Period-Luminosity Relation for Cepheids in Spirals. (Hubbil.) The crosses refer to 105 Cepheids observed by Shapley in the Small Magellanic Cloud, the black disks, to 40 Cepheids in 224 (Andromeda), the open circles, to 35 Cepheids in 598 (M33), the triangles, to 9 Cepheids in 6822. The apparent magnitudes at maxima have been reduced to the distance of 224 by adding 4,65 to those in the Small Magellanic Cl., 0,4 to those in 598, and 0,55 to those in 6822. The absolute photographic magnitudes at the top of the diagram are based upon Shapley's zero point (m-M=17,55) for the Small Magellanic Cl.)

<sup>&</sup>lt;sup>1</sup> Publ ASP 41, p 252 (1929, abstract)

reduction curves for ordinary grant stars, and with a comparison with trigonometric parallaxes for 16 mombers of the group. The derived mean of the spectroscopic absolute magnitudes in -1.74 As compared with Shapley's original value, these results show a displacement of the zero-point of about one magnitude, Shaplky's values being the higher. This would serve to bring objects determined by the period-luminosity relation about 37% closer. A Krppkk1 makes a somewhat similar investigation and changes Shaptily's zero-point by 1.1 magnitudes; he regards this as the minimum change required, this would mean a diminution of spiral distances of about 40% or more

A more precise determination of cosmic distances by all these methods must await the accumulation of more accurate data on the maximum brightness of novae, of the brightest stars, and the Copheid variable stars. While present values of spiral distances show a fairly satisfactory measure of agreement between the results of the different methods employed, it must be remembered that the corresponding values of the galactic data are likewise intimately interdependent

54. Distances of the Spirals: from a Distance-Velocity Correlation. Thu radial velocities of the spirals have, as noted above, such magnitude and range. as well as provailing positive character, that these features have long been noted as differentiating them most sharply from any other class of celestial body. There have been numerous attempts to determine from these velocities the speed and direction of motion of our own galaxy (see references under ciph 50 above, and also clph. 77). With the later enormous values of 4-3000 to +19600 km /sec. there has come in cortain quarters, however, the feeling that these can not bu actual speeds, and attempts have been made to explain the observed speeds as due to distance, or as necessary consequences of one or another type of limited, quasi-spherical relativity universes

The idea that there might be a correlation between the radial velocity and the distance of a spiral seems to have occurred nearly simultaneously to Wikiz, LUNDMARK, and RUSSELL (in a suggestion made to Silberstrin) in 1924. It has since been much more definitely treated, using a larger number of radial

velocities, by HUBBLE, DE SITTER, and CORT. Wirtz shows quite clearly from the velocities of the 42 spirals available at that time, that these velocities diminish with increasing diameter, i.e., increase

with increasing distance.

WINTS, Argument for Diameter

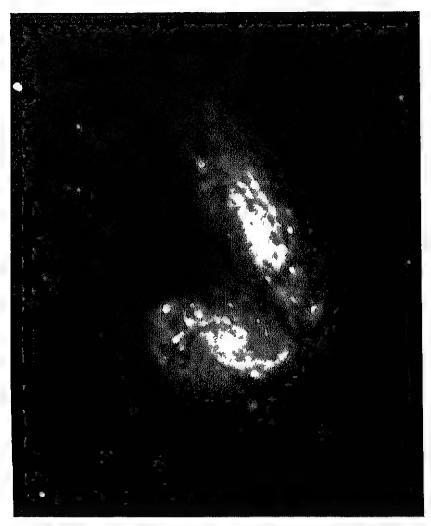
Log diam	Mean 1'	No.	Joy diam	Mean P	No.			
0,24 0,43 0,66	-827 km /mc,  -636  -512	9 7 8	0,88 1,07 1,71	+ 555 km /sec. + 334 - 20	10 5 1			

<sup>1</sup> A N 241, p. 249 (1931)
5 C. Wirtz, De Sittem Kosmologie und die Radialbewegung der Spiralnebel A N 222, p. 21 (1924), K LUNDMARK, The determination of the curvature of space-time in de Sitter's world. M N 84, p. 747 (1924), K Hunner, Extra-galactic nobulac. Ap J 64, p 321 (1926), A relation between the distance and radial velocity among extra-galactic nobulae. Wash Nat Ac Proc 15, p 168 (1929), Mt Wilson Comm No 105 (1929), E. HURHLE and M W HUMASON, The velocity-distance relation among extra-galactic nebulae Ap J 74, p 43 (1931), A Doax, Zur Statistik der nichtgalaktischen Nebel auf Grund der Künigstuhl-Nebellisten A N 229, 157 (1927), H. Shaprey, Note on the velocities and magnitudes of external galaxies Wash Not At Proc 15, p. 565 (1929). J. H. Cour, Note on the velocities of extra-galactic nebulae. BAN 5, p. 239 (1930); Some problems concurning the distribution of luminosities and peculiar velocities of extragalactic nebulae Ibid 6, p 155 (1930), W DE SITTER, On the magnitudes, diameters, and distances of the extra-galactic nebulae, and their apparent radial valocities Ibkl. 5, p 157 (1930), Wash Nat Ac Proc 16, p. 474 (1930), L SILBERSTEIN, Nat 113, p 602 (1924) See also references in ciph 69.

From these values he derived the relation

 $V(km/sec) = 914 - 479 \log diam$ 

LUNDMARK plotted the radial velocities against the distance, reproduced below as Figure 49. It will be seen from an inspection of this diagram that his scale of abscissae is greatly foreshortened by the scale he employed in lieu of



lig 47 The Spirals NGC 4567-8 (Mt Wilson Photograph)

more accurate distances, i.e., 50, 100, 150, etc., times the assumed distance of the Andromeda spiral, and that the relation indicated might have been more apparent with an expanded horizontal scale. He states "Plotting the radial velocities against the relative distances, we find that there may be a relation between the two quantities, although not a very definite one"

The results of Dose are based upon a statistical analysis of the Königstuhl nebular lists, with attempts to secure correlations as to brightness, etc. Taking

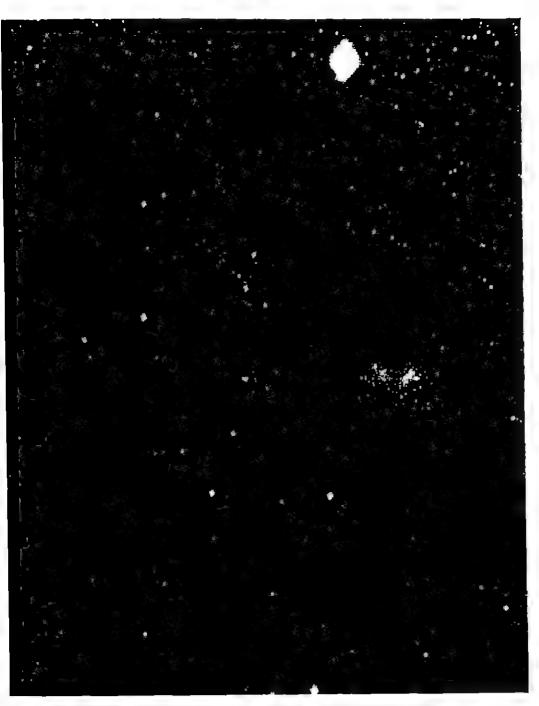
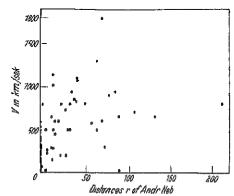


Fig 48 The Spiral New 224 (Andromoda) (Mt Wilson Photograph.) South preceding portion.

14

the radial velocities of the 44 spirals available, he first made a solution for the direction of motion and speed of our galaxy, linding



lig 49 Radial Velocity Distance Correlation for the Spirals (LUNDMARK) The unit of distance is that assumed for 224

1 -	299° 8′
D -	-  67° 32′
K =	765 - 110 km /sec

He then found, on correcting the individual values for this motion, that there is a slight but definite correlation between distance and radial velocity. No diagram is given, but he divides the spirals employed into three groups as regards size.

Croup	Dimeter	Rulid velochy			
Ţ	120' to 6'	1   631 km /sec			
11 111	6' to 3' 3' to 0',7	719        1880			

That is, the peculial radial velocity increases inversely as the diameter of the object, or directly as the distance. Both Wirrz and Dose, as is manifest, assume that the diameters are of the same order of magnitude

In his earlier paper, Hubbll took the distances of 22 spirals and the two Magellanic Clouds, estimated by various methods, as the basis, and introduced into the individual equations of condition for galactic motion a K-term varying as the distance, the equations taking the form

$$rK + X\cos\alpha\cos\delta + Y\sin\alpha\cos\delta + Z\sin\delta$$
 1'

I wo solutions were made, the first by using the 24 spirals individually, and the second by combining objects apparently contiguous as to direction and distance into 9 groups. The solutions gave

	24 spirils	9 groups		
Y	65 = 50	3 -1 70		
7	F226 ± 95	- -230 <del>L</del> 120		
La	- 195 ± 10	-133 <del>⊥</del> 70		
K	+465 ± 50	+513 ± 60 km /sec ]	pet	10 <sup>6</sup> pausces
A	286°	269°		
D	- 40°	33°		
$V_{\alpha}$	306 km /500	247 km /sec		

As a result of a more detailed analysis, and with the employment of a larger number of velocities, Hubbi E and Humason in their latest paper derive a value of 558 km/sec per 100 paisees, which corresponds to

The values for this red shift with distance as determined by DI SIIIIR, and in Oori's earlier paper, do not differ materially from this value (Oori, however, later derives a smaller value, ca 90 km/sec per 10g ly

This interesting relation, should it persist to the most remote spirals, may lead to some curious and rather bizarre consequences. If the faintest and smallest spirals at present observable are at a distance of 10° ly, such objects should show a radial velocity of about +170000 km/sec, corresponding to a shift to

the red of ca. 1500 A. Unless counterbalanced by radiation coming in from rich ultra-violet regions, one might even expect the most distant spirals to be

invisible on account of reduces

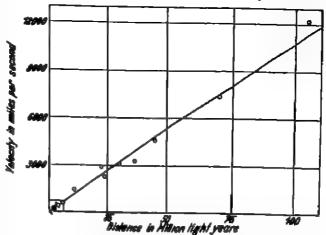
Except for the nearer spirals, whose distances have been determined by other methods, it should be mentioned that earlier diagrams were samply plots of one variable charted in two dimensions, and that there was thus no reason why all the plotted points should not fall precisely upon the line of the correlation

SHAPIFY, for exumple, criticized certain features of the velocity-distance cor-

a galactic motion toward the apex  $d = 277^{\circ}$ ,  $D = -136^{\circ}$ ; V = 280 km/sec. and using the Harvard photographic magnitudes of the objects,

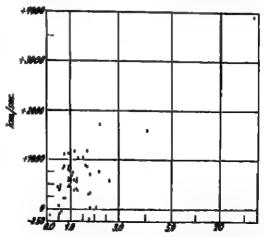
he plotted the resulting radial velocities against the function 10<sup>0,9 m 2,0</sup>. This corresponds to a plot of velocity against distance expressed in parsecs, provided space is assumed to be transparent, and provided that the absolute magnitude of the typical spiral is placed at 15

It will be noted from Shar-TRY's diagram reproduced as 14gare 51, that the internal agreement of the plotted velocities is fully as good as that for radial velocity alone Reference may also be made here to Lundmark's diagrain of the relation between areal brightness and the relative parallax of the spirals1



isig 50 Radial Velocity-Distance Correlation for the Spirale, (HUBBIER and HUMARON) The small black dots in the lower left hand corner represent the only available observations up to 1928. The open circles represent recent observations

relation, and pointed out that the total magnitude may equally well be regarded as a vital factor. Correcting the tabular radial velocities available for



llg 51 Radial Velocity-Magnitude Correlation for the Spirits (Shartey) This diagram shows the relation of the reduced radial volcoity to the quanfifth telegram are

The latest treatment of this relation, the brilliant paper by Hubber and HUMASON (I. c.), has removed, at least in part, the effect of such criticisms. They have here made use of parallel correlations through the factors of absolute

<sup>&</sup>lt;sup>1</sup> M N 86, p 877, Flg 7 (1925)

magnitude and apparent diameter, relations which may be more fittingly included with the matter of the Section following this one

55 Distances of the Spirals Photometric, the "Average" Galaxy<sup>1</sup> Under this heading will be assembled certain photometric data, and deductions as to the distances of the spirals which may be made from them. See also the last portion of ciph. 54, and luguies 50 and 51.

Two main classes of photometric data have been obtained, from which

eventually statistical results of great value may be secured. These are

1. Estimates of the total magnitude of the spiral. Knowing the distance  $D_{\rm IN}$  of selected typical objects, the mean absolute magnitude of these may be deduced through

$$M = m + 7.6 - 5 \log D_{1v}$$

or similar relations. Then, on the assumption that the "average" galaxy has a given absolute magnitude, the distances may be determined for other objects for which the total apparent magnitude is known. The method differs from that in which a mean diameter is assumed for the spirals in that the density of distribution within the spiral is a factor.

2 Estimates of the areal brightness, expressed in magnitudes per square second of arc, or in other luminosity units. Our data in this field are due mainly to Wiriz.

The valuable researches of Wirtz on the areal brightness of the spirals seem not to have received sufficient attention as yet, and certain of his numerous correlations may fittingly be repeated at this point, the comparisons are with his quantity Mg, an areal brightness or unit luminosity

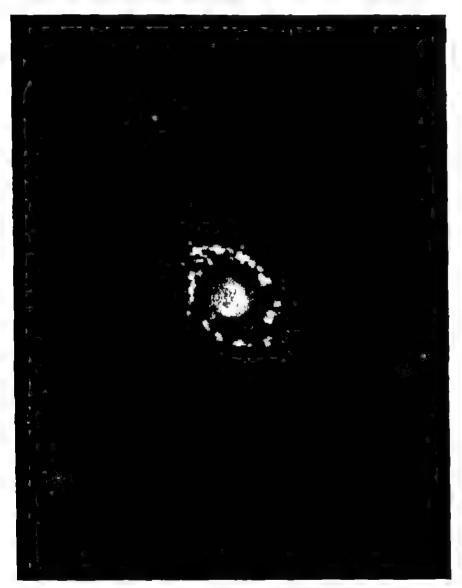
I Diameters There is a slight, but not very definitely established

tendency, for an increase of areal brightness with diameter

2 Gralactic Latitude. If the absence of the spirals near the galactic plane is due largely to occulting matter, as suggested by Curris and others, a falling off in areal brightness would be expected as this plane is approached. No such tendency is noted. The mean areal brightness of 547 spirals shows but slight variation between  $\pm 80^\circ$  and  $\pm 80^\circ$  of galactic latitude, and as a matter of fact those nearest to the galactic plane have slightly greater areal brightness.

<sup>&</sup>lt;sup>1</sup> C. Wirle, Flächenhelligkeiten von 566 Nebeltlecken und Steinligfen. Lund Medd (II) No. 29 (1923) While some values were found for the diffuse and planetary types, and clusters, he uses over 500 spirals in his correlations. Wirey tabulates the dimensions, both visual and photographic when available, the areal brightness Mg, and the total brightness,  $H_t$  expressed in mignitudes. This work forms one of the largest and most homogeneous body of data in this field. J. C. Picki ring, Hary Ann. 33, p. 135 (1900). Photometric areal brightness of 11 objects, 1 Hori rschi & Wich Ann 20 (1907) I otal brightness of 576 objects 1 Hori MANN, Revision of Hollischik's results for 88 objects. A N 211, p. 425 (1921), | H. Riy NOIDS, The light curve of the Andromeda Nebula, M. N. 72, p. 132 (1913), A. MARKOY, A. N. 231, p 329 (1929), correction ibid, 235, p 143 (1930). By methods somewhat analogous to those of Wiriz, he derives values of the surface brightness of 172 spirals (m per square second of aic), II Shapley, Note on the velocities and magnitudes of external galaxies Wash Nat At Proc 15 p 565 (1929), J S Parasklvopouros Integrated photographic mag nitude of the Small Magellanic Cloud Harv Bull No 840 (1926), E H Si aris, the surface brightness of the galactic system as seen from a distant external point, and a comparison with spiral nebulae Ap J 52, p 162 (1920), Mt Wilson Contr No 191 (1920), h Bickler, A preparatory catalogue for a Dirichmustering of nebulae, the General Catalogue Spec Val 13 (1928) For about 1100 objects the total magnitude is expressed in "grades" these may be converted into magnitudes on the scale of Wirlz by the formula,  $M=10^{\rm m}.86$  [  $0^{\rm m}.32$  (N=7), see his introduction, p  $\lambda$ II. See also the references under ciph 54

3 Orientation and Form 503 spirals are treated for a relationship between the ratio of the major and minor axes, A, and the areal brightness. The observed areal brightness shows no connection with this ratio, and also no



1dg 52 The Spiral New 4736. (Mt Wilson Photograph)

dependence upon from which side the spiral is observed. There is further no tendency to a parallelism between the planes of the spirals and the plane of the galaxy.

4 Radial Velocity. No adequate degree of corrolation is found between speed and areal brightness, though the radial velocities show a slight tendency

to increase with diminishing areal brightness.

There are patent an logies between the larg spuals and our own galar

more

(60 000 ly, Kapityn, a) others), see ciph 56 5113 11 Y's estimate of a diamet of 3 105 by allots our g laxy to a much more e ceptional position in C group - 224 (Andromeda) a pears likewise to be exce tional as regards luminosi distribution SLARIS four a wide difference between the areal bughtness of th Spiral and that of our galact system as seen from a dista point in space, magnitu 23 | per square second are for our galaxy, as again magn 17 18 as estimat for several spirals. Mariso however, in the derivation areal brightness for 172 sp rals, finds that 224 is 2

assumptions of

modera

115

5 Total Brightness and Radial Velocity See also ciph 54 A lan well-marked increase of speed with diminishing total brightness is indicate

6 Distance If the spirals are like galaxies, it would be expected th the areal brightness should be independent of the distance in the statistic mean Using Lundmark's estimates of the distances of 216 spirals (subject error in comparison with more recent results), Wiriz finds that there is a market decrease of areal brightness with increasing distance, the reverse is true for t diffuse nebulae

D+10513	100	10	20	13	9	1	6	\$	
Mg No	12 2 1 15	12,11	11 67 33	11,52	11 12 11	11 jo 6	10.89	10.70 7	10.58

The fact that areal brightness is found to diminish with increasing distan is regarded by Wirrz as an indication of the absorption of light in space



(Mt Wilson Photograph)

magn, or 12,2 times bright than the average spiral, ai Fig 53 The Spiral NGC 5194-5 (M51) 76 times brighter than o galaxy In other word 224 may be exceptional, and thus a portion of the lack of agreement betwee our galaxy and the (typical) spirals would be removed

A recent treatment of this question from the standpoint of absolute ma mtude, etc., is due to Lundmark<sup>1</sup> He now derives an abs magn of -5,7 f

Über die Bestimmung der Entfernungen, Dimensionen, Massen und Dichtigkeit für die nachstgelegenen anagalaktischen Steinsysteme VJS 65, p 275 (1930)

the galactic novae, in comparison with the value —5.5 found for those in 224 on the basis of Hubbi k's distance of that object derived from the Cepheids A relation is next derived for the mean abs magn of the 20 brightest objects in E spirals, in the form

$$-6^{3},8\pm0^{3},35+k\sigma_{M^{0}}=M_{so}$$

From this relation be derives the distances, total abs magn , and abs magn of the 20 brightest objects,  $M_{\rm 50}$ , as follows

Object	Object Distance		ΔE <sub>m</sub>	
Large Mag (I	0,1 × 10 <sup>8</sup> l y	-17.5	-6,5	
Small Mag Cl	0,1	- (7,4	-7.4	
224 (Andromeda)	0,9	-17,2	-7.1	
205	0,9	12,0	_	
59H (M 13)	1,1	15.8	- 6.5	
6822	0,7	- 17.2	7.2	

The latest and most authoritative investigations in this aspect of the subject, made as they are with the most powerful instruments, are due to Hubber and Hubbson (references under clph 54). While the primary purpose of their paper is the consideration of the velocity-distance correlation, it may be said that they have drawn upon all methods as yet known in the derivation of the distances of the spirals, the distances of nearer spirals forming a "zero point" rest upon the phenomena of novae and copheids in spirals, for the more distant objects, they have combined the velocity-distance correlation with correlations based upon total absolute magnitude, the magnitude of the brightest stars visible in individual spirals, and apparent diameter-distance comparisons. Whatever changes may be made in the future in their adopted zero-point, and whether or not a velocity-distance correlation may be proved untenable, their values certainly represent the last that astronomy is able to secure from present observational data

The basal data are derived from 40 objects, for which distances have been determined from stars of recognized types, novae, Cepheld variables, irregular variables, helium stars and P ( ygni stars.

These objects, with the adopted distances, are,

Glojert	Distagre	Total gbs wayn	Abs. muqu brightest stars	
Large Mag (1 Small Mag (1 6822 598 (M33) 224 (Andronwin)	0,095 10 <sup>6</sup> l y 0,085 0,61 0,77 0,8	16,6 15,8 12,0 14,9 - 17,0	5,8 -7,4 - 5,6 -6,3 5,8	
221	0,8 0,8 1,3 (2,1) (2,4)	13,2 12,7 13,1 15,3 16,0	~6,(t -6,(t)	

For 40 spirals investigation was made of the mean magnitude  $m_{\pi}$  of the brightest stars, and the difference between this and the magnitude of the object. The mean of all values is  $m_{\pi} - m_{\pi} = 8.88$  magn

From these were derived the following important values:

Moan phot also mage brightest stars			-6.0
Monn via alse mage of spirals.	•	• •	- 14.9
Mean plut six magn of spirals .			13.8
Moan color index	-		F 1d

In order to have one formula the following expression is adopted

$$M_{\rm bol} = \frac{1}{1} \log \frac{c_2}{T'} - \frac{2}{9} \log M + 0.90.$$

Here  $c_2/T'$  has to be selected in such a way that both the formulae are represented

The essential point in the theory of RABE is that M is considered to depend on the temperature much more than is the case in the theory of Eddington. The theory is of considerable interest and ought to be compared with the empirical data as soon as more observations have been collected.

The  $c_2/T$ -value in the above formulae corresponds to the surface temperature and is related to the effective temperature  $T_s$  in the following way

$$\log (c_2/T_s) = \frac{9}{2} \log \frac{c_2}{T} - \frac{1}{6} \log \mathfrak{M} - 0.134$$

The effective temperatures that result from the material of Rabe are in very good agreement with those computed according to the methods of Searls and of Brill. If the  $c_2/T$ -values are diminished by ten per cent they are in very good agreement with the corresponding values derived by M N Saha¹ on the basis of his theory of ionization. It is certainly very interesting that the theory of Rabe is able to explain most of the differences between the results of Brill and Saha.

Using the temperature-scale thus established RABE has computed the absolute magnitudes and the masses and derived the following mean errors

Spectral	Menn errors				
class	in M	in log M	11		
A0—F9 G0—G9 K0—Mdp	士0 <sup>11</sup> ,34 土0 ,48 土0 ,32	士0,19 士0,17 士0,11	22 23 20		

RABE then makes a revision of his system and finds from a discussion of the values of  $m_{\text{O}}$  and  $c_2/T_{\text{O}}$  a correction that should be added to the constants in his equation. He finds

$$\log \frac{c_2}{T} = \frac{1}{5} \log \varrho - \frac{1}{5} \log \mathfrak{M} + 0.342$$

For the application to binaries the equations giving the mass-luminosity relation are changed into the following forms:

Stars without atmosphere:

$$\log \pi = 9\log \frac{c_2}{T} - \frac{2}{3}\log \frac{\mathfrak{M}_A}{\mathfrak{M}_A + \mathfrak{M}_B} - 2\log a + \frac{4}{3}\log P - \frac{3}{5}(m+5+\Delta m_{\rm bol}) - 0.288.$$

Stars with atmosphere

$$\log \pi = -6\log \frac{c_2}{T} + \frac{5}{6}\log \frac{\mathfrak{M}_4}{\mathfrak{M}_A + \mathfrak{M}_B} + \frac{5}{2}\log \alpha - \frac{5}{3}\log P + \frac{3}{10}(m + 5 + \Delta m_{\text{bol}}) + 0.546.$$

Computing the parallexes and comparing with those actually determined RABE has found the mean error of one value to be  $\pm 0.295\pi$ .

The mass-ratio of stars where both the spectra have been observed but no orbital elements are known can be computed from the formula

$$\log\left(\frac{\mathfrak{M}_B}{\mathfrak{M}_A}\right) = \frac{9}{25} \left[ 20 \left( \log \frac{c_2}{T_B} - \log \frac{c_2}{T_A} \right) - (m_B - m_A) - (\Delta m_B - \Delta m_A) \right]$$

<sup>&</sup>lt;sup>1</sup> Zf Phys 6, p 40 (1921), Ap J 50, p 220 (1919), Phil Mag (6) 40, p 809 (1920), 41, p 267 (1921), London R S Proc (A) 99, p 135 (1921)

isolated spirals deviates widely from the one found in clusters of spirals, or else that the galactic system is surrounded by an extensive local agglomeration, the peculiar velocities of which are much smaller than those of outside objects.

56. Distances and Dimensions of the Spirals. Given fairly reliable estimates of the distances of the spirals, and the apparent diameter, it becomes possible to determine their real dimensions, at least approximately. In Table 16 are collected the dimensions of the spirals for which radial velocities are known, and, except for the larger and closer spirals, these depend in general upon values secured through the distance-velocity correlation. If the distance-velocity correlation be accepted, the values of the diameters are still subject to some uncertainty, and it may be that those given for the smallest and most distant objects are two or three times too small, 4, because of uncertainties in this relation,

Table 16. Distances and Dimensions of Spirals: Velocity-Distance.

1	2	1	-1	,	ú	7
No.	Deser.	Dimens	Mg	Rad. vel.   km./sec.	Dist. 10* Ly.	Diameter Ly.
205 221 224 278 380	Spir. Elf. Spir. Spir. Spir.	8' + 3' 2,6 + 1,8 120 + 30 1,2 + 0,3	11 <sup>16</sup> ,7 8 ,0 8 ,8	300 185 220 650   4400	0,8 H 0,8 H 0,8 HH 5,0 H 24,0 HH	3 500 1 000? 31 000 1 7 50 2 1 00
383 384 385 404 584	Spir.? Spir. Spir.? PH. Spir.?	0,3 0,25 0,25 1,3 2	11 ,1 10 ,6	4500  - 4500   1 4900   25  - 1800	24,0 HH 24,0 HH 24,0 HH 4,2 dS 41,4 H	2 100 1 700 1 700 4 50 6 500
598 936 1023 1068 1270	Spir. Barr. Spir. Spir. Spir.	55 40 3 2 6 1,3 2,5 1,7 0,5 0,2	12 ,1 11 ,1 10 ,2 0 ,8	70   1300   300   920   4800	0,7 dS 7,7 1L 3,4 dS 2,3 IL 36,0 HH	11000 6700 5900 2400 5200
1273 1275 1277 1700 2562	Spir.? Spir.? Spir. Spir.? Spir.	0.5 0.5 0.4 · 0.1 0.5 · 0.3 0.4 · 0.2	12 ,4 U ,1	5800  -1-5200  -1-5200  -1-5200  -800  -5400	36,0 HH 36,0 HH 36,0 HH 5,1 dS 29,5 HH	5 200 5 200 4 200 700 3 400
2563 2681 2683 2841 2859	Spir, Spir, Spir, Spir, Spir,	1.1 · 0.5 2.5 · 1.5 10 · 1 6 · 1.6 1.4 · 0.7	: 11 al 11 al	1 4800   1 700  -1 400   1 600  -1 1500	29,5 HH 5,8 dS 3,2 dS 5,1 dS 8,5	9400 4200 9300 8900 4100
2050 3031 3034 3115 3193	EH. t Spir. Trr. Spir. t Spir	1,0 · 0,4 10 · 10 7 · 1,5 4 · 1 1,0 · 0,8	0 ,8 11 ,0	1 1500 30 1 290 4 600 1 1300	8.5 2.4 HH 2.6 H 3.3 H 7.6	2900 13400 5300 3800 2500
3227  3368 3379 3489	Spir. Spir. / Spir. Ell. Spir.	3 + 1,2 0,5? 7 + 3,5 2 2,5 + 1	10 .7 10 .2 10 .3	-{ 1150   19600   940  - 810  - 600	8,1 dS 105 HH 5,7 H 4,8 H 3,6 H	7 100 15200 11400 2800 2600
3521 3610 3623 3627 4051	Spir. Spir.? Spir. Spir. Spir.	1,0 · 1,0 1,0 · 0,7 8 · 2 8 · 2,5 4 · 2	10 .3 11 .0 10 .9 10 .6 12 .0	730   - 1850  - - 800   650   650	4,1 H 1 5,0 H 4,3 dS 1 5,4 dS	4 700 3 500 4 1 600 10 000 6 200

(Continued.)

			(Continued.)			
No.	2 Descr.	Dimens	$M_{g}$	Rad, vol. km-/sec.	6 Dist. 10 <sup>4</sup> l.y.	7 Diameter 1.y.
4111 4151 4192 4214	Spir, Spir, Spir, Spir, Spir,	0',57 3,8 · 0',5 2,6 · 1,6 8 · 2 8 · 4	10 ,3 10 ,8 12 ,0 11 ,8	+11800 + 800 + 950 + 1150 + 300	150 B 5,8 H 7.3 dS 6,0 HH 2,8 dS	22000 6400 5500 13900 1 6500
4258 4374 4382 4449 4472	Spir, Ell, Spir, Mag, Spir,	20 · 6 2 · 1,8 4 · 2 3,5 · 2 2	10 .5 10 ,4 — 10 ,2	+ 500 + 1050 + 500 + 200 + 850	4,6 H 6,0 HH 3,7 dS 2,3 dS 5,7 dS	26800 3500 4300 2300 3300
4486 4526 4565 4594 4649	Ell. Spir. Spir. Spir. Ell.?	2 5 · 1 15 · 1,1 7 · 1,5	10 ,4 10 ,7 11 ,2 9 ,7 10 ,3	+ 800 + 580 + 1100 + 1140 + 1090	5.5 dS 3.9 H 7.6 H 7.2 H 7.5 dS	3 200 5 600 31 000 14 600 4400
4736 4826 4853 4860 4865	Spir. Spir. Eh.? Ell.? Ell.?	5 · 3.5 3 · 4 0.3 0.5 0.5	11 <sup>m</sup> ,0	+ 290 + 150 + 7600 + 7900 + 5000	3,0 dS 1,3 dS 45 HH 45 HH 45 HH	4400 3000 3000 6500 6500
4872 4874 4881 4884 4895	Spir.? Spir.? Ell.? Spir.? Spir.?	1,0 0,2 0,3 1,5 · 0,8 1 · 0,3		+ 6900 + 7000 + 6900 + 6700°  + 8500	45 HH 45 HH 45 HH 45 HH 45 HH	13 000 2 600 3 900 19 000 13 000
11 4045 5005 5055 5194 5236	Ell.? Spir. Spir. Spir. Spir.	0,5? 4,5° 1,5 8 3 12 6 10 8	10 ,9	+ 6600 - - 900 + 450 - - 250 - - 500	45 HII 6,6 H 3,6 H 3,0 dS 2,9 H	6 300 8 600 8 300 10 400 8 400
5457 5866 6359 6658 6661	Spir. Spir. Spir.? Spir. Spir.?	27 3 1 0,2 0,4 0,2 0,5	12 ,2 10 ,9	+ 300 + 650 + 3000 + 4100 + 3900	3,0 dS 6,0 dS 21,6 dS 24 23	23 400 5 200 1 200 3 100 3 800
6702 6703 6710 6822 6824	Spir. ? Spir. ? Spir. ? Mag. Spir. ?	0,2 0,3 0,2 20 0,9 · 0,5		+ 2000 + 2000 + 5100 - 150 + 3200	12 12 29 1,0 S	750 1 100 1 600 5 800 5 100
7217 7242 7331 7611 7617	Spir, Ell.? Spir. Spir. Ell.	2.5 · 2 0.5 9.5 · 2 0.7 · 0.3 0.2	11 ,4	+ 1050 + 5000 + 500 + 3400 + 3900	6 29 5,2 dS 23,5 HII 23,5 HH	1 000 4 600 14 600 4 760 1 400
7619 7623 7626 L. Cl. Sm. Cl.	Ell.? Ell.? Ell. Mng. Mng.	0,8 0,3 0,7 432 216	11 ,5  11 ,6 	+ 3800 + 3800 + 3700 + 280 + 170	23,5 HH 23,5 HH 23,5 HH 0,09 S 0,1 S	5 400 2 000 4 700 11 000 6 500

which has been determined from a relatively small number of moderately close objects, and, 2. because the observed diameters may not record the full extension of the spiral, for reasons noted in ciph. 40.

In the first column of the table will be found the NGC number, a brief characterization, when available, is given in column 2, in column 3 are given the apparent dimensions in minutes of arc, a single value indicating that the object is round, or nearly so, Wirtz' areal brightness, Mg, is given in column 4, column 5 contains the radial velocity, column 6 the distance, expressed in units of  $10^{\circ}$  Ly, in column 7 are given the computed diameters, given in Ly Abbreviations used are H = Hubbit R, HH = Hubbit and Humason, dS = Dr Sitter, S = Shapiry Where no letter follows a distance, it has been computed from the relation D = V/170, where D is in units of  $10^{\circ}$  Ly

The distances derived from the velocity-distance correlation are taken from Hubble and Hubble paper in Ap J 74, p 43 (1931), where the following data are assembled concerning super-galactic groups

Climiter	) ale ( munan	No. iq cL	No	Mean valuelty Rus/sec.	Mesu photo.	) Here. of cl.
Vinto	6,0 × 10 <sup>6</sup> Ly	(500)	7	+ 890	12,5	12"
Роданци	21.5	100	5	+ 3810	15.5	1
Pincon	24,0	20	4	F 4630	15,4	(1,5
Cancer	29.5	150	2	F 4820	16,0	1,5
Porsous	36,0	500	4	+ 5230	16,4	2 ,0
Coma Beronices	45,0	j 8un	3	+ 7500	17,0	1 ,7
Ursa Major	72,0	300	1 1	14800	18,0	0 ,7
Leo	105,0	400	1	4-196au	19,0	0.6

We may include here Shapery's results on the diameters of spirals in certain well-populated clusters of external galaxies?

1 HO CHILD A LING AND AND AND AND AND AND AND AND AND AND	
Number of galaxies in area	2775
Distance of Cloud A	10 <sub>1</sub> 5 10 <sup>4</sup> ( y
Diameter of Cloud A	2 · 10° l y.
Average diameter of companiont members	4500 ly
Larger members of Cloud A	
420H) (HIROW HIP)	. 15500 ly
42 कि स्पष्टिक अपूर्ण ।	. (8000
4304 open splr	. 48,600
4321 open spir	, (8900
4382 off	, . (53i##
4418 mple	24 000
4501 compact upin	18 000
4526 oll	(8.300
4535 ogen aptr .	19400
4569 compact splr	16 500
Distance of Cloud B .	
Distance of Cloud C	419 10 Ly
Distance of Cloud D	. 169 10 <sup>5</sup> l y
Largest members of C and D, Diameter	25000 ly
The Cuntaurus Group	
Number of galaxies in area.	, 1000
Distance of group .	146 40 <sup>4</sup> l y
Longth, 7 to ly	
Width, 1.8 10 1 y	
Diamoter of largest members	45000 ly
Average diameter of members, 15"	9700 ly
The Ursa Major Group	
	100 · 100 l y
Distance of group (MAI AQUIST) .	6,7 · 10 <sup>1</sup> 1.y 7
Moan distance spart	, 20000 ly
Diameter of largest members	- m.o.n 3
1 Ham Itali 962 864 874 (4020)	

<sup>&</sup>lt;sup>1</sup> Harv Bull 863, 864, 874 (1929)

The Come-Virgo Groups

By way of summary, assuming only the distances and diameters which have thus far been determined for spirals and groups of spirals, there appear to be two main classes as regards size the majority have more moderate dimensions of 2000 to 9000 Ly, with a class of grant spirals whose diameters range from 15000 Ly to 50000 Ly, or more. See also Hubbit's values, given in Ap. 1-64, p. 329 (1926).

Mention should be made here of the results derived by LUNDMARK in his extended paper, "The Relations of the Globulai Clusters and Spiral Nebulae to the Stellai System" [K Svenska Vet Ak Handl 60, No. 8 (1920)]. In this paper he has derived distances for 276 spirals, taking the mean of values seemed from their apparent magnitudes and their apparent diameters. These are distributed as follows.

No of spirals	Adopted distrince	Density   Per 10 ° cub Ly	No of spirits	Adopted distance	Density per to <sup>20</sup> cub fs
1	07 10 <sup>6</sup> l y	5 3	0	6,0 10 <sup>0</sup> 1 y	(), 3
1 [	1 3	1 1 1	10	7,2	0.2
4	2,2	0,5	18	9, 1	1.0
2	3 4	0,5	25	13	0,07
3	3,9	0.5	62	22	0.017
6	4 1	0,5	65	14	0,003
7	5,0	0,4	63	101	O,CCCIO3

Lundmark's distances from diameter and magnitude relations are in general larger than those found from the distance-velocity relation, as will be seen from the tabulation below comparing such objects as are common to the two methods

ACC Nº	Distance from dist vel corr	leib e ammanu l an ib bar agrac mod	NGC No	Distance from	TONOMARKS did from magn and disc
205 278 598 936 1023 1068 2681 2685 2841 3031	1.0 10 <sup>d</sup> l y 5 0 0 7 7 7 7 3.1 2 3 5.8 3.2 5.1 2.9	7.5 10 <sup>6</sup> l y 45 1 4 1 28 1 1 1.5 23 10 7.6 3 0	4371 1382 1410 4472 1186 1526 4565 1594 4736	0,0 10° f y 3 7 2 3 5,7 5,5 3,9 2 6 7,2 3,0	3,4 · to <sup>n</sup> 1 x 6,0 6,5 8,1 5,8 27 6,8 4 † 4 3,2
303   3115 3368 3521 3623	2,6 3,3 5 7 4 1 5,0	7,1 4,6 1 5,5 10 6,3	1826 5005 5055 5191 5236 5217	1,3 6 6 2 9 3,0 2 9 3 0	1,8 7
3627 4051 4192 4214 4258	4 3 5,4 6,0 2 8 4 6	5,2   20   8,2   10   5,3	5 † 57 72 † 7 7 3 3 1	3 () 7 () 5,2	10 27   11

57 Masses of the Spirals In general, the estimates of the total mass of typical spirals are roughly of the same order as that derived for our galaxy. The latter is a quantity still imperfectly known, and any derivation of spiral masses requires a large measure of hypothesis and extrapolation. Opin's method assumes that the luminous materials of the spirals have the same coefficient of

<sup>&</sup>lt;sup>1</sup> Ap J 55, p 406 (1922)

emission as those in our own galaxy, while Hubble (1 c) uses the spectrographic rotation. Lundmark assumes the mass-hubble law effective in all such systems, and starts from the total abs magn. (see the preceding Section). He points out that the total gravitational mass must be larger, and postulates largeration of dark material. The value derived from the total abs magn is styled the luminosity-mass, while that derived from spectrographic rotation values will be a gravitational mass. Lundmark assembles the following values, to which have been added determinations by Hubble (H), and Opik (O)

Object	Caravitation-mass	Ration in i dark to insummentar	Stems per	Authority
224	0,2 · 10 <sup>16</sup> O 3,5 · 10 <sup>8</sup> 1 6 · 10 <sup>8</sup>	20-1	0,006	' L II . O
1594	2,0 10 <sup>0</sup> 2,6 10 <sup>0</sup> 10 <sup>11</sup>			H O O C
3031	3 10 <sup>10</sup> 76 10 <sup>10</sup>	30 4 100 1	0,042	t. 1.
5194 Caluxy	0,1 10 <sup>10</sup> 10 10 <sup>10</sup>	10 l	0, <b>012</b> 0,08	

58. TEN BRUGGENCATE'S Theory of Elliptical Spirals. The investigations of Hubbic, fen Bruggencate, and others may fittingly be mentioned at this point

Hubbie's very thorough and detailed investigation is based upon observations made with a self-registering microphotometer, and he derived isophotal curves for the following 15 elliptical objects

221	1278	1472	\$115	4 122	4621
440	1281	1486	3179	4406	1749
584	4374	4552			

The isophotal contours are approximately circles for globular objects (Hubbi R's E0), except for the extremely clongated objects (E7), the deviations of the contours from symmetrical ellipses are slight. An interesting investigation is made of the projected densities of different types of structure, and he gives a comparison of the density distribution in the projected images of the mean elliptical spiral, an isothermal gas sphere, and a bounded gas sphere

REYNOLDS believed that he had detected evidences of polarization in the spiral 4826 (M64). Green and Meyer, however, were unable to substantiate any such effect in a number of nebulae of various types which they tested

Somewhat in contrast to these failures to detect polarization are two Bruggeroate's recent results. He investigates the spatial distribution laws of a nebula symmetrical through rotation, and extends the theory to the case where the isophotal surfaces within the object are concentric, coaxial, and similar ellipsoids of rotation. He finds a satisfactory agreement between his values and those observed by Hubble (supra). Based on Hubble's results, the Bruggeroate concludes that all elliptical objects have the same axial ratio, about 10.3, and in support of this, the probabilities of different degrees of ellipticity are investigated. To a first approximation, the brightness within the ellipsoid diminishes

<sup>1</sup> In Hubber 1 the distribution of luminosity in elliptical nebulae Ap J 74, p 234 (1930). P TREE BRUGGERGATE, Die Heligkeitsverfollung im Junern elliptischer Nebel / f Astroph 4, p 275 (1930), 2, p 83 (1931), J H Reynot de, Preliminary observations of spiral nebulae in polarized light M N 72, p 553 (1914). W K Green, An investigation of certain nebulae for evidence of polarized light Publ A 5 P 20, p. 108 (1917). W F Meyer, A study of certain nebulae for evidence of polarized light Publ A 5 P 20, p. 108 (1917). W F Meyer, A study of certain nebulae for evidence of polarization effects. Publ A 5 P 31, p 194 (1919)

as the inverse square of the distance from the center. He therefore interprets the elliptical objects as conglomerations of particles, rather than stars

"Die elliptischen Nebel dürften aus einem zentialen Kein bestehen, der als Lichtquelle dient, und dessen Licht in der ihn umgebenden Mateix nicht merklich absorbeit und remittiert, sondern gleichmäßig nach allen Seiten gestieut und reflektiert wird. Die von Hubbit emprisch gefunden: Beziehung, die Identität der Intensitätsverteilungen in den Projektionen allea elliptischen Nebel ausdruckt, bildet den Schlussel zum Verständnis des physikalischen Zustandes dieser kosmischen Objekte. daß elliptische Nebel keine durch ihre große Entfernung nicht aufzulosende Sternwolken sein konnen. (4)

The structure is postulated as transparent throughout the greater part, and the particles reflect and disperse the light from the nucleus in all directions Taking Hubbit's value of the radius, cal 1000 ly, the total average mass is placed at 108 O, and the effective density is of the order of 10 25 The diameter of the "nucleus" is of the order of 10 1 ly, with a mean density of about 10 10, the mean free path of the particles in the outer portions is of the order of 10 ly.

There are a number of very serious objections to this theory of 1EN BRUGGEN-

- I All existing evidence as to super-galactic groups indicates that the elliptical and the true spirals are inextricably intermingled as to arrangement and location. This theory assumes an entirely different constitution for these bodies, as contrasted with their immediate neighbors in space. This is most improbable.
- 2 From this contiguity in space with the spirals, and from the areal and apparent brightness of the elliptical objects, then total abs magn, must be of the same order as that of the spirals —15 to —17. This accordingly requires that the "nuclei" of the elliptical objects be sources of tremendous energy, equivalent to absolute magnitude—15 or higher. No such "sources" are known with certainty.
- 3 Furthermore, we should expect that the light from such central sources would be polarized, or that it would show selective reflection or absorption effects. None have been detected
- 59. Theories of Spiral Structure: Introductory! The structure of the spirals, showing as it does so frequently two well-marked spiral whorks starting
- 1 S ATEXANDER, 8 papers in A J 2 (1852), E J WITCZYNSKI, Outlines of a theory of spiral and planetary nebulae Ap J 4, p 97 (1896), Dynamics of a nebula A J 20, p 67 (1899), F C CHAMBIRIIN, On the possible function of disruptive approach in the formation of meteorites, comets, and nebulae Ap J 14, p 17 (1901), The origin of the earth Chicago (1916), E STRÖMGREN, Über die Bedeutung kleiner Massenänderung für die Newtonsche Zentralbewegung A N 163, p 130 (1903), J II JEANS, The stability of a spherical nebulae Proc R A S Lond 68, p 454 (1901), Problems of cosmogony and stellar dynamics. Cambridge (1919), Astronomy and cosmogony Cambridge (1928), M Woll Length of axes and position angles of 52 oval nebulae MN 68, p 626 (1908), H Knox Shaw, On the melinations of the planes of some spiral nebulae to the galaxy. MN 69, p 72 (1908), W Suthfraian, Bode's law and spiral structure in nebulae Ap J 34, p 251 (1911). L J J Sell, Evolution of the stellar systems, 2 (1910), E v d Pahlen, Über die Gestalten einiger Spiralnebel A N 188, p 240 (1911), h Norkl, Über die Entwicklung der kosmischen Nebel. A N 188, p 353 (1911), E Belot, Expérience reprodusant les spires des nebuleuses spirales. C R 154, p 1780 (1912), G W Watker, Some problems illustrating the forms of nebulae Proc R S Lond (A) 91, p 440 (1915), G F Breker A possible origin for some spiral nebulae. Wash Nat Ac Proc 2, p 1 (1918), B Hlerassimovitch, Sur les mouvements tourbillonaires dans les nébuleuses. A N 126, p 81 (1919), K Bottlinger, Zur Bildung der Spiralnebel. A N 210, p 5 (1919), C V L Charlier, Sur les nébuleuses spirales. C R 169 p 430 (1919), M Valier, Die Gestalt der Nebelflecke, insbesondere der Spiralnebel. A N 210, p 5 (1919), C V L Charlier, Sur les nébuleuses spirales. C R 169 p 430 (1919), M Valier, Die Gestalt der Nebelflecke, insbesondere der Spiralnebel. A N 210, p 5 (1919), C V L Charlier, Sur les nébuleuses spirales. C R 169 p 430 (1919), M Valier, Die Gestalt der Nebelflecke, insbesondere der Spiralnebel. A N 210, p 5 (1918), J Jans' answer,

from exactly opposite points on a nuclear portion, has long been a puzzle. No adequate, complete, and entirely satisfactory theory of the spirals as a result of classical dynamical laws has as yet (1932) been derived. A satisfactory theory of the forms assumed by the sorrals must then

A Furnish a reasonable dynamic explanation of the origin, shape, motions

within, and permanence of the spiral whorls

B It must explain why these take their origin at points 180° apart on a nuclear portion (very difficult))

( The component matter of the structure must be taken to be discrete

stars, rather than gas, or dust particles

The literature of the field is already very extensive, and additions are

constantly being made to it

60. Agreement of Spiral Arms with Mathematical Spirals A number of mathematical curves show more or less close approximation to the observed forms of the whorls of the spirals Some of these, with the law of attraction required in cuch case (SFR. I c.), are The gravitational sorral.

$$r^{\mathbf{g}}(\varphi - \varphi')^{\mathbf{g}} = c$$
,  $P = \frac{h^{\mathbf{g}}}{a^{\mathbf{g}}}$ 

The spiral of Archimedra,

$$r = a\theta$$
,  $P = \frac{h^4}{r^2} \left(1 + \frac{2a^2}{r^2}\right)$ 

The logarithmic spiral,

$$r = a^{\theta}$$
,  $P = \frac{k^{\eta}}{r^{\eta}} (1 + \log^{\eta} a)$ 

The litius.

$$r^{a}(l) = a^{a}, \qquad P = \frac{h^{a}}{r^{a}} \left(1 + \frac{4a^{a}}{r^{a}}\right)$$

The hyperbolic spiral.

$$r(l) = a, \qquad P = \frac{h^k}{r^k}.$$

The parabolic spiral,

$$(r-a)^a = 4 c a \theta$$
,  $P = \frac{h^a}{r^a} \left(1 + \frac{3 a^a (2o+1)^a}{r^a}\right)$ .

Spirals of other types show even more complex functions. It will be noted that only for the gravitational, logarithmic, and hyperbolic spiral is the law of force a relatively simple one, being as the inverse cube of the distance, for the other common types of spiral the law of force depends upon the third and fifth, or third and seventh power of the distances. It is unnecessary to emphasize that no cosmic forces are known whose action varies in this way

(1926). J II REVNOTON, The condonations in the spiral nebulae M N 85, p. 142 (1924). The forms and development of the spiral nebulae, ibid, 85, p. 1014 (1925). The spiral form and development of the Andromeda Nebula, ibid, 87, p. 112 (1926). F A. Leidemann, Note on the constitution of the spiral nebulae M N 83, p. 334 (1923). Approved by Reynolds, ibid, p. 182, criticized by Perrands and Chyrord, ibid, p. 272, 283, E. W. Brown, Gravitational forces in spiral nebulae. Pop Astr. 32, p. 545 (1924). Ap. J 61, p. 97 (1925) later views, Oles 51, p. 277 (1928). II Lindblad, Commogonic consequences of a theory of the stellar system. Ups Modd No. 13 (1926). On the spiral orbits in the plane of a spheroidal disk, with applications to some typical spiral nebulae, ibid. No. 31 (1927). On the nature of spiral nebulae M N 87, p. 420 (1927), H. Maris, The formation of spiral nebulae Phys Rev (2) 33, p. 1103 (1929), C. PARVUI ERCO, Sur la dynamique des nebuleuses spirales it A. J. 3, p. 157 (1927). J. C. Sollá, Algunas consideraciones sobre las nebuleuses apirales it A. J. 3, p. 157 (1927). J. C. Sollá, Algunas consideraciones sobre las nebuleuses apirales Roy Soc Astr Pap. 2, p. 149 (1929).

There is a general, though not entirely unanimous, agreement among those who have investigated the whorls of typical spirals, that, on the whole, these curves approximate most closely to those of the logarithmic (also called equiangular) spiral. In this curve, the angle between the tangent to the curve and the radius vector to the given point should be constant, and equal to are tan (1/log<sub>e</sub>a).

E V D PAHLIN made careful measures of the whorls of three large spirals 598 (M33), 5194—5 (M51), and 628 (M74). He found the agreement of all three with the logarithmic spiral relatively close (there are, in all such investigations, considerable variations in the density, width, or location of salient features in the whorls which can only be explained as chance inegularities, resulting doubtless from random differences of distribution in the original mass or aggregation). The spiral of Archim des was tested in 598, but did not give nearly so good a measure of agreement as the logarithmic spiral. It was impossible to substantiate any similarity with Wilczynski's gravitational spiral (see ciph. 61).

L BICKIR made measurements of the points in both whoils of 5194 5, with a least squares reduction. His measures result in an empirical spiral with characteristics as follows

- a) The two whoils are practically duplicates, and corresponding points stand diametrically opposite to each other, and equally far from a certain point near the middle of the central condensation
- b) Times of length  $r_p = a + bl^2$  may be drawn from the points of the real spiral to the line of sight which passes through the central point, and these lines, when displaced parallel to themselves to a point, all he in a plane. The longitude of the node of this plane is 160°, and its inclination 42°.

The essential duplication of the whorls is taken as an indication that the motion is outwards, for it is deemed unlikely that matter coming in from outside would arrange itself in two identical whorls 180° apart. The assumption is made that the increase in the longitude of the moving particles is proportional to the time. Such a relation is found possible with a certain spheroid whose equator coincides with the plane of the spiral, in which each particle acts according to the inverse square of the distance, and with a density varying from the center outward. The law of such a required density variation is investigated, and the resulting calculated curve shows a fair agreement with the observed contour of the whorls.

If Groot made an extended series of measures on the following eight large spirals (nine sets are given, on 17 individual spiral arms, but one spiral was measured twice) 5194 - 5 (M51), 4258, 3198, 4321, 4501, 4725, 3623, and 3031. The logarithmic spiral, the spiral of Archimedes, and the litius were all tested All the 17 arms investigated could be properly represented by the logarithmic spiral. Only 5 whorls (two each in 3623 and 3031, and one in 4321) could also be represented by the spiral of Archimedes of the litius, and it was thought that this was partially explained by the fact that the arms of these spirals could be investigated only over a very limited range. Equations were set up for each whorl investigated, and the two found for 4321 may be selected as examples

1321 whoil I 
$$\log r = 12011 - [8,9106] \varphi$$
  
1321, whoil II  $\log r = 11761 - [9,0327] \varphi$ 

The farrly close agreement of the constants of the equations for the two whorls in this and in practically all the other spirals studied indicates essential duplication for the whorls of individual spirals, and argues for an evolution proceeding from within outward. The total range in the value sof the angles

between the tangents to the whorls and the radii vectores is remarkably small (73° to 86°), the greatest range found for the two whorls of the same spiral was 4°, the mean value for all whorls measured is 79°. Some evidence was found for aksimes in the arms of 3031, the structure of all the others seems to be in one plane. Six other spirals were investigated by Groot in his accord paper, with essentially the same conclusions.

REYNOLDS has measured the configurations of a number of spirals and, in general, agrees with Groot as to their correspondence with the logarithmic spiral. The objects investigated were 5247, 2835, 4254, 4321, 1232, and 5457. He finds, however, a greater degree of irregularity in the run of the angles between the tangent and the radius vector. "The angle made by the tangent of the curve with the radius vector is usually between 50° to 70° in the carlier part of the curve, but in more advanced stages the angle may be anything between 40° and 80°. In many cases these extremes may be observed in the two arms and bifurcations of the same spiral" He regards both the filamentous and the massive spirals as in an advanced stage of development, and points out that spirals developed for less than half a revolution are rare, while spirals developed for more than two revolutions in an actual spiral form are unknown.

61. Whenever's Gravitational Spiral. Most earlier theories attempting to explain spiral structure are influenced by the hypothesis of gaseous constitution. The most general assumption has been that of a rotating gaseous spheroid, though dust-clouds which have been repelled from regions near the galactic plane have also been suggested Scharehle even proposed that the spirals were formed by matter ejected from volcanoes! Repulsive forces acting from the nuclsus outward have also been a favorite method (radiation pressure, etc.) giving rise to the "Dampistrahl" or "pin-wheel" theory of whorl formation,

The theory of the origin of the solar system from a (small) spiral in the planetesimal hypothesis of Chamberlin and Moulton is well known. This theory suggests that a spiral would be formed by the disruptive tidal action of two stars making a close approach. While this theory has been carefully and rigorously worked out by its authors, they admit that the enormous dimensions of the spirals make their origin in this way untenable (solar system: mass 1,001 ©; diameter, cs. 0,001 Ly.; Andromeda Nebula: mass 3,5 · 10° ©, diameter ca. 31000 ly!).

Among earlier attempts to identify the class of curve assumed, mention must be made of the gravitational spiral of Wilczynskii. His explanation is as suitable for a stallar composition as for other constitution. The component elements are assumed in his theory to revolve about a center of attraction under the action of gravitation, the inner components will manifestly rotate more rapidly than the components on the periphery, and initial irregularities as regards density of distribution will thus in course of time trail out into the whorls of a gravitational spiral. The number of whorl-turns will give an indication of the age of the spiral through the formula.

$$t = \frac{2\pi \pi}{\omega_1} \frac{1}{1 - (a/b)^{a/a}}$$
.

Here a and b are the radii of the circles between which the structure of the spiral lies,  $\omega_1$  is the angular velocity of rotation at the inner circle, u the number of turns, and t the clapsed time or age.

WILCZYNSER'S theory agrees with the observational data in the following respect: it gives a direction of rotation in the same direction as is indicated by SLIPHER's spectrographic determinations of rotation.

from the best observational data and the curve computed according to the theory is good, indeed. The average of the residuals is  $\pm 0^{M}$ , 56, most of which might fairly be attributed to errors in the observational data, and the maximum discordance is 1<sup>M</sup>.7 Certain refinements of the nature of a second approximation are suggested by Eddington, who derives the following relation between a change in the molecular weight and a change in the absolute magnitude1

$$-\Delta M = \frac{9\beta + 8}{4 - 3\beta} \log e^{\frac{\Delta \mu}{\mu}}$$

At the time this investigation was carried out the first approximation certainly sufficed. The accumulation of further data since then may invite us to make a second approximation

The masses of the Cepheids were computed on the basis of the pulsation theory. The method is that of successive approximations. A value of M is assumed From To (spectral class) the radius is deduced and then the mean density The central density  $\varrho_o$  is 54,25 times the mean density. The period Pis then obtained from the expression

$$P \varrho_{o}^{\frac{1}{2}} = 0.29 (\gamma \alpha)^{-\frac{1}{2}}$$

where  $(\gamma a)^{\frac{1}{2}}$  is taken from M N 79, p 15, table V with  $1-\beta$  as argument. The process is repeated until P stands. The highest value is 26,20 for Y Ophruchi and the lowest 4,14 @ for RR Ly1ae

EDDINGTON inquires if, assuming that the gas-laws hold good for ordinary stars, we then should expect that each star will have the precise luminosity deducible from its mass and effective temperature or, in other words, whether the theory is accurate individually or only statisfically. The sources of residual differences are principally abnormal composition and abnormal rotation. With regard to the first source an unduly large proportion of hydrogen would make the stai fainter. With regard to rotation it has been shown by E.A. Milne that a rapid iotation makes the star slightly fainter, but that the effect is very small until the speed is sufficient to deform the star considerably. What is to be feared, concludes Eddington, is that the observed spectrum misleads us concerning the true value of  $T_a$ . An unsuspected binary ought to betray itself by having a magnitude fainter than that predicted from a knowledge of its combined mass

The very interesting theoretical considerations as to whether it is physically likely that a dense star such as our Sun can obey the laws of a perfect gas cannot be given here The student is referred to § 9 in Eddington's paper

The high density of the white dwarfs is not abound. At a very low effective temperature smaller than that of a dwarf of spectral class M the star Sirius B is probably able to produce in some way "an imitation of leading features of the F spectrum sufficiently close to satisfy the expert observer" The deviation of this star from the mass-luminosity curve is not surprising if the density is 53,000  $\odot$  new considerations enter into the calculation of k, since the elections are in the capture zone of two or more nucler simultaneously. Also the deviation from the gas-laws may be considerable. On the other hand the star  $o^2$  Eridani B agrees quite well with the mass-luminosity relation.

In Kramers's theory the absorption coefficient k contains an additional factor  $\infty (1 + h r_1/RT)$  The effect of this factor was calculated and found to vary between +0,2 and -1,6 There are general reasons for accepting a correction factor of this form, which represents the ratio of the energy given up on capture

<sup>&</sup>lt;sup>1</sup> M N 84, p. 323 (1924)

The system of the spiral is supposed to originate in a lons-shaped aggregate of stars arranged in an ellipsoid of revolution. The distances between the component stars are very great in comparison with their diameters; the number of stars is postulated as very large. Furthermore, the number of stars in a given volume of the ellipsoid is assumed to be everywhere the same.

A field of force varying directly as the distance was chosen, this field permits circular motion, and deviations from circular motion which are symmetrical across the center, which is a vital factor in explaining the diametrical symmetry of the spiral whorls. The mathematical treatment is then made to depend upon two well-known gravitational phenomena. If such a particle or star be attracted toward a fixed center with a force  $-n^2r$ , it can move in a central ellipse with a mean angular velocity, n. Uniform distribution of the stars within the ellipsoid, if the flattening be considerable, will then cause the star to move under a force -Kr, in an ellipse whose center coincides with that of the ellipsoid, and every particle will be moving with nearly the same angular velocity about the polar axis of the flattened disk.

The initial requirement of constant density of distribution can be waived provided the amount of matter in a cylindrical volume standing on an element of area of the equatorial plane be proportional to  $(i - r_1^2/a^6)^{1/3}$ , where  $r_1$  is the distance of a particle (star) from the center, and a is the external radius. It is this function which admits of an observational test by counts of stars at different distances from the center. A dominating central mass is thus abandoned in favor of the action of the entire field upon the star.

A near (but not too near) approach and passage of a similar aggregate of the same order of total mess disturbs this field by a kind of "tidal" force which has several effects which can be separately considered. Actual distortions of the figure are small, and are bound to be subject to oscillations which are soon masked by other effects. There also arise variations of density which have a maximum along one axis in the equatorial plane and a minimum along an axis perpendicular to it, a change of density also occurs along any radius of this plane, the linear rate of change being proportional to the distance from the center This gives the appearance of a bar, nearly straight, across the plane of the object, (Compare a similar feature in LINDBLAD's theory, clph. 64, and note the great importance of this feature as an explanation of the relatively frequent barred spirals.) The altered gravitational field will eventually cause this bar to coil into a spiral, the "coiling" being produced by the radial variation of density. During the process the "arms" become denser, and the coiling (finally) becomes so close that the evidence of structure disappears. At this stage, the aggregate has reverted substantially to its original condition, and on Brown's theory the elliptical objects or close-packed and "compact" spirals may be "late" instead of "early".

Knots or subordinate aggregations in the arms are attributed (the least satisfactory of Brown's postulates) to the approach of another similar aggregate which starts a new set of arms, the intersection of the two sets producing the condensations (?).

Brown's theory may then be summarized as requiring an initial very populous aggregation of stars which by rotation has assumed the shape of a flattened ellipsoid of revolution. The start of the spiral arms requires an approach to another similar large aggregation. The postulate of this approach is the most difficult point in this or any similar theory, such approaches would seem to be of almost vanishing rarity. The theory has the following very notable points of merit:

Ì

- a) It provides for the symmetry of the two whorls from the nature of the central force adopted
  - b) It gives a possible explanation of the frequent occurrence of barred spirals
- c) Alone among existing theories, it offers a dynamical explanation of the rotational results secured by Pease (see ciph 46) in that the spiral rotates essentially as a whole

It does not, however, give any law for the curves observed in the spiral arms

64. Lindblad's Theory of Spiral Structure Lindblad has been almost the only modern theorist to make a comparison between theory and observation as regards the shape of the spiral arms. His theory rests upon a certain class of spiral orbits which are asymptotic to the peripheral edge of a flattened, rotating ellipsoid. The orbit of a material particle moving in a circular orbit outside the spheroid in the equatorial plane is derived in the form

$$\left(\frac{dy}{d\theta}\right)^2 = \varkappa \left[ \left(2 - \frac{1}{y^2}\right) \arcsin y + \frac{1}{y} \sqrt{1 - y^2} + \frac{4}{3} \mu y \right] + c_0, \tag{1}$$

where

$$\varkappa = \frac{e^4}{\arcsin e - e\sqrt{1 - e^3} + \frac{2}{3}\mu e^3},$$

and

$$c_0 = 2e^2 \frac{(1-e)^2 \arcsin e - e\sqrt{1-e^2} - \frac{1}{3}\mu e^3}{\arcsin e - e\sqrt{1-e^2} + \frac{2}{3}\mu e^3}$$

In the above

r and  $\theta$  are the polar coordinates in the equatorial plane,

u=1/r

y=e/r,

e = eccentricity of mendian section,

a = equatorial radius,

 $\mu = \text{ratio}$  of mass of nucleus to mass of spheroid

For (1) there is first substituted the symbolical expression  $\left(\frac{dy}{d\theta}\right)^2 = \psi(y)$ , and for a slightly disturbed motion, when the disturbance does not affect the value of the areal constant, h,

$$\left(\frac{dy}{d\theta}\right)^2 = \psi(y) + \Delta t \tag{2}$$

Since  $\psi(e) = 0$  and  $\psi'(e) = 0$ , for a value of y slightly less than e,

$$\left(\frac{dy}{d\theta}\right)^2 = \frac{1}{2} \psi''(e) (\delta y)^2 + \cdots \Delta c \tag{3}$$

The condition for the appearance of an asymptotic spiral orbit is then,

$$\psi''(e) > 0, \tag{4}$$

and this orbit possesses the characteristic feature that  $du/d\theta$ , or  $dy/d\theta$ , has a minimum value at y=e or u=1, and a maximum value for some smaller value of y, corresponding to a greater distance.

<sup>&</sup>lt;sup>1</sup> LINDBLAD's papers on the subject have appeared at intervals preceding 1928 in the Ark Mat Astr Fys of the K Svenska Vetensk Akad, and issued also as Ups Medd The more important papers are Ups Medd Nos 13, 19, and 31 No 31 is Series III, Vol IV, No 7 of Handl K Svenska Vetensk Akad, and contains a summary of his preceding investigations, and diagrams showing agreement with the whorls of known spirals

LINDBLAD then selects four values for  $\mu$ : 0,  $\frac{1}{2}$ , 1, and 2, which give for the ratios between the central mass and the total mass the values

0, 1/a, 1/a, and 1/a

With these values of  $\mu_i$  and with valuce of a equal to unity or very slightly less (e.g., for  $\mu = 0$  the values  $\theta = 1,000, 0.995$ . 0,980, 0,965, 0,950, and 0,920 were successively chosen), he then performed the numerical integration of equation (1) and tabulated the resulting values of & and n, and from these derived the corresponding curves Those for  $\mu = 0$  were found closest to Observed apiral whorls.

The equation was next integrated for  $\mu = 0$  and s = 0.995, with the assumption of a small but finite disturbance. For this purpose the square of the area constant,  $h^*$ . was assumed to be 10% amaller than in the first integration. The resulting curve gave better agreement and later, using  $\mu = 0$  and a = 0.965, a guite close agreement was found for the calculated spiral and the arms of 3034 (M81). See Figure 55 and 56

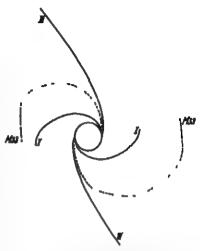


Fig 55 Theory of Spiral Structure. (LIMDRLAD) Theoretical curves for s - 0,99, compared with the spiral arms of 598 (M33)

The importus necessary to cause a star to pass from its orbit on the periphery of the rotating "mother system" over into the esymptotic spiral is assigned by LINDBLAD to one of two causes:

a) It is supposed that this may result from the tidal action of exterior systems, as in Brown's theory, producing a condensation along one axis of the system, and a corresponding rarefaction along

the axis at 90° from this.

b) In the absence of sufficiently atrong tidal forces, it is postulated as conceivable that the matter rotating most rapidly in the "mother system" may be ejected as a consequence of a certain type of sectorial harmonic waves analogous to that which renders the MacLaurin ollipsoid of a homogeneous liquid "ordinarily" unstable.

While it is pointed out that either of these postulated forces need be alight enough only to cause a star to pass over the boundary into an asymptotic apirul orbit, neither cause seems entiraly convincing.

Furthermore, there is a "turning point" in all of Linderad's spiral orbits at a finite distance, except for the case  $\mu = 0$ , s = 1,000, where it is at infinity This point marks the greatest distance from

Fig. 56 LINDBLAD'S Theory of Spiral Structure. The spiral arm of 3031 (M 81) compared with the theoretical curve for 🔊 🛏 0,97 (dotted curve) a 🖼 the apparentarm, b, the shape of the arm in the plane of the opiral, assuming an inclination of 60°

the nucleus which a star will reach in its asymptotic spiral orbit; after passing this point its distance will decrease. While there are slight inward bendings at the outer ends of the whorls of some spirals, the theory is scarcely supported by these random and infrequent irregularities, and it is legitimate to ask why this re-entrant portion of the curves is not a prominent feature of most spirals.

H Voct<sup>1</sup> has attempted to derive a theory which attributes the recession of the spirals and their internal mechanism to one and the same cause, a postulated "cosmic repulsion". This repulsion, from the results of Hubbel and Humason, is evaluated as

$$\frac{1}{R} \frac{dR}{dt} = \alpha = 1.8 \cdot 10^{-17} \text{ sec}^{-1}$$

The equations of motion are then written in the form.

$$\frac{d^2r}{dt^2} - r\left(\frac{d\theta}{dt}\right)^2 + \frac{GM}{r^2} - \alpha^2 r = 0,$$

$$\frac{d}{dt}\left(r^2\frac{d\theta}{dt}\right) = 0, \quad \text{or} \quad r^2\frac{d\theta}{dt} = h,$$

m which a is assumed not to vary with the time Integration of these equations gives

$$v^{2} = \frac{2GM}{r} + \alpha^{2}r^{2} + Ch^{2}$$

while the radius of curvature is given by

$$\varrho = \frac{v^3}{h \left[ \frac{GM}{t^3} - \alpha^2 \right]},$$

C and h are constants of integration

When  $\alpha^2$  is less than  $GM/r^3$  the orbit will be a spiral concave to the center of attraction, when  $\alpha^2$  is the greater, the curve will be of hyperbolic character and convex to the origin

Assembling the numerical data for 224 (Andromeda, outer portions),

$$M = 2 10^{42} \text{ g}$$
  
 $r = 2 10^{22} \text{ cm}$   
 $G = 6,66 10^{-8},$   
 $\alpha = 1,8 10^{-17},$ 

he finds that  $\alpha^2$  (GM/r<sup>3</sup>) = 0.02, approximately, 1 e , the spual is here concave to the origin

Vogt's theory assumes

- 1 A "cosmic" repulsion as the "Dampfstrahl" component.
- 2 Motion outward along the spiial aims

It gives no explanation of the diametrical symmetry of the two spiral whorls. Furthermore, there should come a time when the whorls will change from a form concave to the origin to one which is convex. In the numerical example given, this will take place when r increases to a value 3.7 times its present value  $(50^{1/3})$ . That no spirals are found with such hyperbolic outer whorls, in fact, none with more than two or three spiral circuits, is naively attributed to the present youth of the universe

65. Theories of Spiral Structure Summary. It will be noted that the "pin-wheel" theory of the spiral arms, Lindblad's asymptotic spirals, Jeans' hypothesis, and all theories which postulate the ejection of matter at diametrically opposite points from a rotating spheroid, as well as van Mannen's measures, seem to require motions proceeding mainly outward along the spiral arms. It is not easy to reconcile this feature of most theories with Slipher's direction

<sup>&</sup>lt;sup>1</sup> Zur Dynamik der Spiralnebel A N 243, p 405 (1931)

of rotation of the spirals "the motion is invariably that similar to a spiral spring when it is being wound up" Equally difficult is a comparison of such theories with Prace's rotational results. Brown's theory of stars in a spheroidal mass, all rotating with nearly the same angular velocity, comes closest to observation in this respect.

Though the present writer does not share the philosophy of despair voiced by Jeans<sup>1</sup> it is perhaps fitting to close this discussion of theories of the structure of the spiral arms, none as yet entirely adequate, with a few quotations giving some of his recent views.

"It seems almost impossible to explain pure rotation dynamically in terms of known forces, and we are led to the disconcerting, but almost inevitable conjecture, that the motions

in the spiral nebulae must be governed by forces unknown to us

The only result that seems to emerge with some clearness is that the spiral arms are permanent features of the nebulae. They appear to have been formed in the process of ahrinkage, two convolutions or thereabouts being formed by each nebula, and to have been perpetuated in static form ever since.

Their further interpretation forms one of the most puzzling, as well as disconcerting,

problems of cosmogony

Rach failure to explain the spiral arms makes it more and more difficult to resist a suspicion that the spiral pobulae are the seat of forces unknown to us, which may possibly express novel and unsuspected metrical properties of space."

66. Evolutionary Status of the Spirals. These considerations can be presented very briefly, in view of the length of the discussion to follow on the larger aspects of cosmogony raised by the spirals. There is a general agreement that the spirals are structures of a galactic nature. The larger members of the class, at least, seem to be vest congeries of suns, whose linear dimensions, masses, and total number of component stars are approximately of the same order as the similar relations in our galaxy. Our galaxy, in turn, is the most accessible spiral for study, just as our sun is the most accessible star.

Nothing is as yet definitely known as to the laws which govern the characteristic structure of the spirals, nor as to the direction of the evolutionary process exhibited in them as a class. We do not know certainly whether the process as now observed is one of formation, permanency, or disintegration. However, from the time which light takes to reach us from such enormous distances (10° to 10° or more light-years), and from the analogy of the present similar condition of that member of the class in which we are situated, the relative permanency and quasi-eternal duration of these great structures seems a certainty. It seems further self-evident that they represent the main, if not the only, course of evolution exhibited by the macroscopic cosmos as accessible to our investigation

- 67. Cosmogonical Deductions: Introduction. A large literature is rapidly assembling whose subject matter is the formulation of that larger cosmos of which the millions of other galaxies (the spirals) form the individual units. While the greater number of such speculations (for few would claim for these any other terminology in the present state of our knowledge) are attempts to include the spirals and their predominant characteristics of size, constitution, and tremendous velocities of recession, in some form of "relativity universe", emphasis should here be placed upon the fact that this, at present, is not the only alternative. There are still two alternatives, and may forever be two:
  - 1. An infinite Newtonian universe of the CHARLIER type.
  - 2. A closed universe, infinite only in the relativity sense.

<sup>&</sup>lt;sup>1</sup> Astronomy and Cosmogony, pp 351-2 (1928).

The Charlier Infinite Universe1. There have been several vague and somewhat inchoate cosmical structures postulated by philosophers which involve the assumption of system on system (e.g., LAMBERT), but these must be dismissed as hypotheses for which observational bases did not yet exist, and more or less common as a speculation among thinking men of all time

In all older astronomical treatises, and in some which are comparatively secent, we find the familial statement that an infinite universe is an impossibility, were it infinite, the night sky should be everywhere as bright as the sun. This objection can be shown to be mathematically true, granted only that a density of stellar distribution equal to that of our galaxy be assumed to extend outward without limit A more serious and equally cogent earlier objection to an infinite universe came from the dynamical dilemma arising from an infinite mass-total, here also it can be shown that a regularly distributed infinite universe must give rise at some point to an infinite attraction and corresponding infinite velocities

So far as is known to the writer, the first statement that these arguments against an infinite universe might be nullified by a particular and artificial arrangement of the component stars of systems is due to PROCTOR's

"But there is another way in which we may explain the darkness of the sky at night, without assuming either the extinction of light, or that occupied space is an infinitely inmute speck amidst an infinity of vacant space Assuming our system to form one of a finite number of such systems, separated from each other by distances bearing a very large ratio to the dimensions of each, and that thus a system of higher order is formed, which again forms one of a finite number of similar systems, and so on continually, the dimensions of each system of whatever order being always very small in comparison with the distance separating it from its neighbors, then there would no longer result m a necessary consequence even an appreciable illumination of the whole heavens "

OLBERS' criterion for the postulation of a uniformly luminous sky was as follows 3

"So wird also nicht bloß das ganze Himmelsgewölbe von den Sternen bedeckt, sonde in sie müssen noch hintereinander in unendlichen Reihen stehen, und sich untereinander wieder verdecken Es ist klar, daß derselbe Schluß stattfindet, wonn die Fivsteine nicht gleichförmig ım Raume, sondern in einzelne Systeme mit großen Zwischenzäumen verteilt sind "

Seeliger's treatment of the dilemma of infinite mass in the cosmos is contained in his paper, "Über das Newtonsche Gravitationsgesetz"4

"Es wird deshalb notwendigerweise zwischen den beiden Annahmen eine Wahl zu treffen sein, i die Gesamtmasse des Weltalls ist unei meßlich groß, dann kann das Niewronsche Gesetz nicht als mathematisch strenger Ausdruck für die herrschenden Anziehungskräfte gelten, 2 das Newronsche Gesetz ist absolut genau, dann muß die Gesamtmaterie des Weltalls endlich sein oder genauer ausgedrückt, es dürfen nicht unendlich große Teile des Rumnes mit Masse von endlicher Dichtigkeit erfüllt sein "

<sup>1</sup> To call this hypothesis the LAMBERT-CHARLIER system is norther fitting nor just The speculations of LAMBERT, KANT, and other earlier thinkers are guestes, nothing more, and too deficient in scientific character to warrant the annexing of their names A reference to the appropriate passages in Lamburr's Cosmologische Briefe, Augsburg (1761), with its assumptions of multitudes of comets, central "Regent" attracting masses, and the like, will confirm this conclusion

Eg, p 304

<sup>&</sup>quot;Wenn die Fresternsysteme solche Körpei zu Regenten haben, ob sie nicht wieder zusammen ein größeres System ausmachen, in dessen Mittelpunkt wieder ein Regent ist, der seinen Wirkungskreis durch dieses großere System ausbieftet? Die Systeme zusammen genommen machen bereits die Milchstraße aus Findet sich, daß jedes oder wenigstens nur emes derselben emen Regenten habe, so mag die Analogie sicher forigehen, und die Milchstraße hat auch einen der sie ganz beherrsche und herumlenke"

The Universe of Stars London (1878), p 67 <sup>3</sup> Bode's Jahrb 1826 <sup>4</sup> A N 137, p 129 (1895)

CHARLIER'S method of obviating the consequences of the criteria of OLBERS and SEELIGER may be described as a mathematical extension of the mystical speculations of early philosophers. He imagines the material elements of the cosmos arranged in a series of systems, with essential identity in the component elements of each system or stage

Let  $N_1$  stars, each of radius  $R_0$ , form a galaxy,  $G_1$ .

Let  $N_1$  galaxies, each of radius  $R_1$ , form a super-system of the second order,  $G_n$ 

Let  $N_2$  systems of the second order, of radius  $R_2$ , form a still higher system of the third order,  $G_2$ , etc., etc.

A distance  $r_i$  is then defined on the assumption that  $N_i$  spheres of radius  $r_i$  would be equivalent in volume to the system  $G_i$ , that is,  $r_i$  eatisfies the equation

$$N_t \frac{4\pi}{3} r_i^2 = \frac{4\pi}{3} R_i^2,$$

$$R_t = r_t \sqrt[4]{N_t}.$$
(1)

OT

Then  $2r_i =$  the distance of a component in  $G_i$  to the next component. The mass of any system will be.

$$M_{i} = N_{i} N_{i-1} N_{i-2} \cdot N_{2} N_{1} M_{0}, \tag{2}$$

where  $M_0$  is the mass of the initial element, a star.

Considering now a star  $G_0$  which lies on the boundary of a galaxy,  $G_1$ , and that each succeeding system in turn lies on the boundary of the next system above it, the total attraction of all such higher systems on the star  $G_0$  will take the form:

 $\frac{M_1}{R!} + \frac{M_2}{R!} + \frac{M_3}{R!} + \cdots$ 

The condition for the convergence of this series is that  $M_d/R_t^2$  shall be less than  $M_{t-1}/R_{t-1}^2$ , or, from equation (2):

$$\frac{R_i}{R_{i-1}} > \gamma \overline{N_i} \,. \tag{3}$$

This is CHARLIER's fundamental relation, and if this inequality between the radii of the successive systems is satisfied, the total attraction of a CHARLIER universe on the given star will not be infinite, but finite. Such an arrangement will then satisfy the criterion of SEELIGER.

By a similar analysis it is further found that the criterion of Olders reduces to the same relation between the radii and the number of components, i.e., if this same inequality is satisfied, the total luminosity of an infinite CHARLIER universe as seen from a star thus situated will be finite in amount.

A value is next found for the total luminosity received by a star situated at the center of the lowest system, this amount is found to be greater than for any other location, and in addition the inequality satisfying the two criteria remains unchanged; hence the relative position within a system has no effect in invalidating the inequality.

If instead of the respective radii of the systems and supersystems one employs the distances between the elements of a system,  $2\tau_i$ , there results from equations (1) and (2) the following inequality which must be satisfied for both Olders' and Skeliger's criteria.

$$\frac{r_i}{r_{i-1}} > N_{i-1}^{i/i} N_i^{i/i},$$
 (4)

<sup>&</sup>lt;sup>1</sup> C. V. L. Charler, How an infinite world may be built up. Ark Mat Astr Fye 16, No. 21 (1921), Lund Medd. No 98

and this in turn will reduce to

$$\frac{r_i}{r_{i-1}} > 1/\overline{N}_i , \qquad (5)$$

If the various systems are assumed to have each the same number of components. The velocity of a body at the limit of a system  $G_i$ , supposing that the velocity at infinity is zero, will be

$$v_i = \frac{h \sqrt{2M_i}}{\sqrt{R_i}},$$

whereas the velocity at the limit of the next sub-system below will be

$$v_{i-1} = \frac{k\sqrt{2M_{i-1}}}{\sqrt[i]{R_{i-1}}},$$

whence

$$v_i \quad v_{i-1} = \sqrt{N_i} / \frac{\widetilde{R}_{i-1}}{R_i}, \tag{6}$$

resulting in the following inequality as regards the velocity necessary to satisfy the two criteria

 $v_{i} < v_{i-1} \sqrt[3]{N_{i}} \tag{7}$ 

If a particle falls inward from the limit of a system, supposed spherical, and with initial velocity = 0, the velocity will be

$$v = \frac{k \sqrt[l]{M_t}}{\sqrt[l]{R_t}} \tag{8}$$

Now the interesting and highly significant fact in Charliller's theory of an infinite universe is that, so far as this is accessible at present, the arrangement of objects and systems is precisely what would be expected on such a theory. That is, we do have aggregations of 10<sup>10</sup> or more stars arranged in a galaxy, while at distances relatively very great compared with the distances between the stars or the diameters of the galaxies we observe a very large number, perhaps 3 · 10<sup>7</sup>, similar galactic structures

It is perhaps not necessary to assume that we see more than a part of the super-system  $G_2$ , and the existence of such higher arrangements as  $G_3$  and  $G_4$  must remain highly speculative. There is a natural tendency to regard the well-populated clusters of galaxies in the Coma-Virgo, Ursa Major, Centamins groups, etc., as distinct  $G_2$  systems. Their comparatively limited numbers (1017) might be against such a deduction, and lend support to the consideration of such groups as merely local regions of greater density of population within the system  $G_2$ . Their community of radial velocity is, however, rather a strong argument for their  $G_2$  character, forming separate units in the super-system  $G_3$ . See Appendix No. 8

While an effort to set up an extended Charlier arrangement must be regarded as merely an interesting speculation, the attempt is not without value. One needs only to be limited by approximations to the mass of a galaxy, by assumed bounds to the total number of galaxies within  $G_3$  systems, and by permissible upper limits of velocity

It is, of course, entirely possible to speculate upon radically different arrangements under the Charlier scheme, and still satisfy the inequalities which render nugatory the criteria of Olbers and Seeliger. As a matter of fact, the tentative scheme illustrated in Table 17, should doubtless be changed to smaller values of the number of unts in a  $G_2$  system, in view of data at hand for clusters of galaxies

System	G	G <sub>1</sub>	G <sub>n</sub>	G,	
Object	Blar	Spirel	fluper-galaxy	Super-system	
N <sub>i</sub> M <sub>i</sub> R <sub>i</sub> Vol; d <sub>i</sub> Abs. magn Mean V <sub>i</sub> . Av app. magn Av dist. apart . Diam at av dist.	1 2 · 10 <sup>30</sup> g 7 · 10 <sup>3</sup> km — -1-5 6,8 km./sec 30 l y	10 <sup>th</sup> stars 4 10 <sup>th</sup> g 3 · 10 <sup>th</sup> l y 3 10 <sup>th</sup> cm s 8 10 <sup>-14</sup> 15 168 km /sec. 12 10 <sup>th</sup> l y	10 <sup>6</sup> galaxies 4. 10 <sup>48</sup> g. 10 <sup>9</sup> l y 4. 10 <sup>81</sup> cm s 9 · 10 - 88 - 30? 1700 km /sec 25 3.5 10 <sup>18</sup> l y	10 <sup>8</sup> super-gul 4 · 10 <sup>M</sup> g 10 <sup>14</sup> Ly 3,6 · 10 <sup>M</sup> cm 9 · 10 <sup>-41</sup> -50?	

Table 17 Tentative Illustration of Charlier's Systems.

Note The mass of the galaxy has been multiplied by the factor 2 to provide for non-luminous matter. The average distance apart presupposes symmetrical cubical piling. The velocity and average distance apart are for the given system in the system  $\frac{7}{7}+1$ .

Using 10° for the number of the spirals, and 10° for the number of stars in a spiral, etc., Charles derives the following inequality for the limiting angular diameter of a spiral.

$$\alpha < \frac{1}{N^{1/\alpha}}$$

whence the nearest spiral to us should have an angular diameter less than 5°,7; 224 (Andromeda) is about 2°. Also, he finds that the apparent magn. of the nearest spiral should not be greater than ca. 4,5 (Andromeda, 4,6 magn.) He finds furthermore that the radius of the farthermost spiral in the super-galaxy (with the numerical data assumed) should be smaller than 3',4, and it should be fainter than the 15th app, magn. His estimate of the distance of the most remote spiral, on these assumptions, is 54 · 10° l.y., doubtless too small, but of the order of some recent estimates. With the same initial data, he finds that the velocity of a spiral should be less than 178 times the velocity of the stars in our galaxy, giving a value less than 5300 km./sec (present maximum, +19600 km/sec)

There seems no escape from the conclusion that it is possible to arrange an infinite universe on Charler's scheme, without causing infinite luminosities or infinite velocities, and the close parallelism of his plan with the observed arrangement of the accessible visible cosmos is cartainly startling. Any mean velocity for spirals or for super-galaxies composed of spirals may be provided for by the postulation of suitable values for the masses, number of units, and distances apart. It is to be noted, however, that while the Charler construction can be made to provide for any mean velocity of the spirals, it must be admitted that, in its original form, it offers no explanation of the preponderance of velocities of recession. See Appendix No 8 for further treatment

69. The Spirals and Relativity Universes: Introduction<sup>1</sup>. The very large amount of reference material, of which the more important treatments are given below<sup>1</sup>, on this aspect of the position of the spirals, together with the high standing

<sup>&</sup>lt;sup>1</sup> A. Rinstrin (with Grossmann), Entwurf einer veraligemeinerten Relativitätstheorie und einer Theorie der Gravitation. Z f Math Phys Jan. (1914), Die formale Grundlage der aligemeinem Relativitätstheorie. Szber Berl (1914), p. 1030; Zur nilgemeinen Relativitätstheorie, ibid. (1915), p. 778. Erkiärung der Periheibewegung des Merkur ans der aligemeinen Relativitätstheorie, ibid. (1915), p. 831; Die Feldgleichungen der Gravitation, ibid. (1915), p. 844; Die Grundlagen der aligemeinen Relativitätstheorie, Ann Phys 49, p. 769 (1916), also published separately by Bartn; Näherungsweise Integration der Foldgleichungen der

of the authors quoted, is a sufficient proof of the importance of this comparatively recent cosmological development, and warrants a somewhat detailed treatment

In roughest outline, the development of ideas postulating universes of the relativity type during the past thuty years has been about as follows

- 1 1900 Schwarzschild discusses the characteristics of non-Euclidean closed universes
- 2 1914-1918 EINSTEIN develops his general theory of relativity and postulates a closed cylindrical universe whose "radius" is a function of the amount of matter contained in it

Gravitation Szber Berl (1916), p 688, Kosmologische Betrachtungen zur allgemeinen Relativitätstheorie, ibid (1917), p 147, Kritisches zu einer von Herrn Dr Sitter gegebenen Lösung der Gravitationsgleichung, ibid (1918), p 270, Pimzipielles zur allgemeinen Relativitatistheorie Ann Phys 55, p 243 (1918), The new field theory Obs 52, p 82 (1929), Zum kosmologischen Problem der allgemeinen Relativitätistheorie 5/lier Beil (1931), p 235, W DE SITTER, On the relativity of mertia Amst Proc 19, No 9, 10 (1917), On the curvature of space, ibid 20, No 2 (1918), On Einstein's theory of gravitation and its astronomical consequences MN 76, p 699 (1916), 77, p 155 (1916), 78, p 1 (1917), 1hc expanding universe Discussion of Lemaîtie's solution of the equations of the mertial field BAN 5, p 211 (1930), Remarks on the astronomical consequences of the theory of the expanding universe, ibid, 5, p 274 (1930), On the distances and radial velocities of the extra-galactic nebulae and the explanation of the latter by the iclativity theory of incitia Wash Nat Ac Proc 16, p 474 (1930), Some further computations regarding non-static universes BAN 6, p 141 (1931), Do the galaxies expand with the universe? ibid . 6, p 146 (1931); R C Tolman, On the astronomical implications of the de Sitter line element for the universe Ap J 69, p 245 (1929), The effect of the annihilation of matter on the wave-length of light from the nebulae Wash Nat Ac Proc 16, p 320 (1930), On the estimation of distances in a curved universe with a non static line element, ibid , 16, p 409, 511 (1930), G LEMATER, Un univers homogène de masse constante et de rayon croissant, rendant compte de la vitesse radiale des nébuleuses extra-galactiques Ann Soc Sc Biux 47, p 49 (1927), translated into English in M N 91, p 483 (1931), On the random motion of material particles in the expanding universe Explanation of a paradox BAN 5, p 273 (1930), The expanding universe MN 91, p 490 (1931), On thermodynamic equilibrium in a non-static universe Wash Nat Ac Proc 17, p 153 (1931), McCrea and McVittie, On the contraction of the universe M N 91, p 128 (1930), Proc Edinb Math Soc (2) 2, part 3 (1931), G C McVIIIII., The problem of n bodies and the expansion of the universe MN 91, p 274 (1931), A S EDDINGION, On the mstability of Einstein's spherical world M N 90, p 668 (1930), cf Nat 125, p 850 (1930), On the significance of Einstein's gravitation equations in terms of the curvature of the world Phil Mag (6) 42, p 800 (1921), 43, p 174 (1922), K Schwarzschild, Über den zulässigen Krümmungsradus des Raumes V J S 35, p 337 (1900); H D Robertson, On the foundations of relativistic cosmogony Wash Nat Ac Proc 15, p 822 (1929), A FRIEDMAN, Z f l'hys 10, p 377 (1922), P HARZER, Übei die astronomischen Ergebnisse dei allgemeinen Relativitätstheorie AN 227, p 81 (1926), K Lanczos, Über eine stationäie Kosmologie im Sinne der Einsteinschen Gravitationstheorie Zf Phys 12, p 73 (1924), Über die Rotverschiebung in der de Sitterschen Welt, ibid , 17, p 168 (1923), V FREEDRRICHE U A SCHECH-TER, Notiz zur Frage nach der Berechnung der Aberration und Patallaxe in Einsteins, de Sitters und Friedmans Welten in der allgemeinen Relativitätstheoile ZIPhys 51, p 584 (1928), K Lundmark, The determination of the curvature of space-time in de Sitter's world M N 84, p 747 (1924), H Vogr, Die Instabilität der Welt A N 241, p 217 (1931), Die kosmologische Deutung der Spiralnebel, ibid , 242, p 181 (1931), J Chazx, Liffet Doppler-Fizeau dans l'univers de de Sitter CR 183, p 1093 (1926), C Wirtz, De Sitters Kosmologie und die Radialbewegungen der Spiralnebel AN 222, p 21 (1924), F SFLPTY, Beiträge zum kosmologischen Problem Ann Phys (4) 68, p 281 (1922), F Zwicky, On the red shift of spectral lines through interstellar space Wash Nat Ac Pioc 15, p 773 (1929), Phys Rov (2) 33, p 1077 (1929), L SILBERSTEIN, The determination of the curvature radius of spacetime M N 85, p 285 (1925), of ibid, 84, p 747 (1924). The curvature of de Sitter's spacetime derived from the globular clusters, ibid, 84, p 363 (1924), New determination of the radius of space-time Pop Astr 38, p 92 (1930), The radial velocities of globular clusters and de Sitters cosmology Phil Mag (6) 47, p 907 (1924), Nat 113, p 350, 602, 818 (1924), 114, p 347 (1925), 125, p 850 (1930), The size of the universe, attempts at a determination of the curvature radius of space time, Oxford Press, (1930), VIII +215 pp.

- 3. 1917—1929. DE SITTER, FRIEDMAN, TOLMAN, and others, develop further the idea of an Einstein closed, static universe, with excess of positive velocities among distant objects
- 4. 1927—1930 Lemaître finds a paradox in the static Einstein universe, and shows that it must be expanding. The latest papers of DE SITTER accept the idea of an expanding universe, and it is enthusiastically adopted by EDDINGTON

"Hence the radius of the universe has expanded by one part in 2000 in the last million years. The result is impressive. It indicates that the radius of space has doubled within ordinary geological time. We conclude that the radius of space was originally about 1,2 · 10 · 1 y. that it has since expanded considerably, but to an amount practically undeterminable, and that its present rate of expansion is 1 per cent in about 20 million years—a rate which will continue indefinitely. The universe is now doubling its radius every 1400 million years and this rate will, if anything, slightly increase in the future. In 10 is years the spiral nebulae will be to magnitudes fainter than they are now. With a time scale of billions in years, astronomers must count themselves extraordinarily fortunate that they are just in time to observe this interesting but evanescent feature of the sky." (i) [M.N.90, p. 677 (1930)]

5. 1929—1930. Tolman discusses the DE SITTER line element with rigor, and finds that the earlier conclusions as to uniform excess of velocities of recession are less inevitable than earlier held.

"The conclusion is drawn that the DE STYPE line element does not afford a simple and unmistakably evident explanation of our present knowledge of the distribution, distances, and Doppler effects for the extra-galactic nebulae" [Ap J 69, p 245 (1929)]

6 1930. Basing their investigation upon the line element of a universe containing matter scattered throughout and, in addition, with a concentration of matter around the origin, two Scotchmen, McCrra and McVrrre, come to the conclusion that a contraction process is as probable as one of expansion.

"It seems therefore that a condensation starting in an RIMSTRIM universe would cause this universe to contract .. We must conclude that if the actual universe started as an Rodinsorou universe and is now expanding, as the work of LEMATER and Rodinsorous suggests, this expansion can not have been caused by a radistribution of the matter into massive nuclei. Thus, as yet, no mechanism for setting up the expansion has been found."

Schwarzschild's initial paper on this general subject is an academic discussion of the possibility of various types of hyperspace rather than a treatment along relativity lines. By making estimates of the lowest limits of error in angular measurements now attainable, he derives the corresponding limiting dimensions for several forms of hyper-space. In the case of hyper-space, he shows that any radius of curvature larger than ca. 63 l.y. would be difficult to detect by present methods. In elliptical hyper-space the corresponding minimum detectable radius of curvature is found to be ca. 2500 l.y., with a "distance around the world",  $\pi R$ , of  $8 \cdot 10^{\circ}$  ly.

The EINSTEIN field equations are now available in many treatises (see references quoted). The general course of the historical development of these theories as relating to the excess of velocities of recession among the spirals has already been outlined. A complete study of this entire development would involve, first, a large amount of repetition in the treatment of the line element by the various investigators, combined with some measure of confusion due to occasional differences in mathematical nomenclature, and, secondly, such a treatment would in many cases, for completeness, be involved with discussions of the relativity effects adduced for the deflection of light in a gravitational field, and the shift of the Fraunhoffer lines to the red in such fields: questions which are of interest in other fields of astronomical investigation, but in no way germane to the present problem of the spirals.

For these and other reasons, the detailed treatment of the work done by the multitude of investigators will be greatly abridged, and will be replaced with a somewhat composite treatment drawn in the main from two or three of the latest workers in this subject a method which has some elements of the illogical, but also many advantages on the score of convenience and brevity.

The investigation chosen to represent the Einstein-De Sitter universe will be that of Tolman<sup>1</sup> Several reasons have motivated this choice 'Ioiman's paper is one of the latest in point of time, and is definitely restricted to the problem set by the large positive velocities of the spirals. Furthermore, it not only possesses great clarity of treatment, but it appears to the present writer to display a commendable and judicial sancness, in that no all-embracing inspiration is claimed, but difficulties are frankly emphasized

The subsequent theory of a necessarily expanding universe, as treated originally by Lemaître and Friedman, and also by Tolman on the theory of the annihilation of matter, will be drawn mainly from Limaître.'s original paper on the subject, and also from recent papers of Eddington and District Following a description of these methods of treatment, a summary will be given of the radu of various postulated relativity universes

70. Tolman's Critique of the DE SITTER Relativity Universe Tolman employs DE SITTER'S form of the line element, as derived from Einstein's generalized equation

$$-8\pi T = G_{\mu\nu} - \frac{1}{8}Gg_{\mu\nu} + \lambda g_{\mu\nu},$$

and the line element itself is an expression in angular variables of an element on the surface of a four-dimensional sphere of radius  ${\cal R}$ 

$$ds^2 = -R^2 [d\omega^2 + \sin^2\omega \{d\zeta^2 + \sin^2\zeta (d\theta^2 + \sin^2\theta d\phi^3)\}].$$

Substituting the variables  $\omega$  and  $\zeta$  by

$$\cos \omega = \cos \chi \cos \iota t,$$
$$\cot \zeta = \cot \chi \sin \iota t.$$

and placing further

$$\sin \chi = r/R$$
,

the equation of the line element is written in the form:

$$ds^2 = \frac{1}{1 - r^2/R^2} dr^2 - r^2 d\theta^2 - r^2 \sin^2 \theta d\phi^2 + (1 - r^2/R^2) dt^2.$$
 (1)

The geodesic equations will take the following forms from the norm form (after Eddington)

$$\frac{d^3x_\alpha}{ds^2} + (\mu\nu, \alpha)\frac{d\nu_\mu}{ds}\frac{d\nu_\nu}{ds} = 0, \qquad (2)$$

$$\frac{d^2r}{ds^2} + \frac{1}{2} \frac{dl}{dr} \left(\frac{dr}{ds}\right)^2 - re^{-\lambda} \left(\frac{d\varphi}{ds}\right)^2 + \frac{1}{2} e^{r-\lambda} \frac{dr}{dr} \left(\frac{dl}{ds}\right)^2 = 0.$$
 (3)

This is integrated best by substitution of the values found from (5) and (6), finding the equation

$$\frac{dr}{ds} = \pm \sqrt{k^2 - 1 + \frac{r^2}{R^2} - \frac{h^2}{r^2} + \frac{h^2}{R^2}}.$$
 (A)

<sup>&</sup>lt;sup>1</sup> Ap J 69, p 245 (1929)

With  $\alpha = 2$  the geodesic equation is that of a particle moving in the plane  $\theta = \pi/2$ , with  $d\theta/ds = 0$ , in accordance with the equations:

$$\frac{d\theta}{ds} = 0, \qquad \frac{d^n \theta}{ds^n} = 0, \qquad \theta = \frac{\pi}{2}, \tag{4, B}$$

$$\frac{d^2q}{ds^2} + \frac{2}{r} \frac{dr}{ds} \frac{d\varphi}{ds} = 0, (5)$$

the integral of which is:

$$\frac{d\,\eta}{ds} = \frac{h}{r^a}\,,\tag{C}$$

$$\frac{d^2t}{ds^2} + \frac{dr}{dr}\frac{dr}{ds}\frac{dt}{ds} = 0.$$
(6)

The integration of (6) gives:

$$\frac{dt}{ds} = ke^{-\nu} = \frac{k}{1 - r^2/R^2} \,. \tag{D}$$

In the above, h and k are the constants of integration; h can assume positive or negative values according to the direction of motion of the particle, while k, a time-like constant, can be only positive unless time is supposed reversible. For the special case of light, both h and h become infinite,

The form of the orbit is obtained by dividing (C) by (A), with rearrangement of terms:

$$d\varphi = \frac{h\,d\,r}{r^2 \left| \sqrt{\frac{r^2}{R^2} + \left(k^2 - 1 + \frac{h^2}{R^2}\right) - \frac{h^2}{r^2}} \right|}.$$
 (7)

This is the form of the relation, in Newtonian mechanics, applying to the shape of the orbit due to a central repulsive force proportional to the radius r. Hence in the DE SITTER universe the orbits of free particles are in general curved away from the origin.

Perihelion of the particle will be found by making  $dr/d\varphi = 0$ . Hence perihelion will be obtained by making the quantity under the radical sign in (7) equal to zero, or:

$$b^2 - 1 + \frac{r_n^2}{R^3} - \frac{h^2}{r_n^2} + \frac{h^2}{R^2} = 0.$$
 (8)

The velocity of motion of the particle in its orbit will be:

$$\frac{dr}{dt} = \pm \frac{(1 - r^2/R^2)}{h} \sqrt{k^2 - 1 + \frac{r^2}{R^2} - \frac{h^2}{r^2} + \frac{h^2}{R^2}}.$$
 (9)

From the equation of the original line element, putting  $ds^2 = 0$ , the purely radial velocity of light becomes:

$$dr/dt = \pm (1 - r^2/R^2). \tag{10}$$

In both the preceding expressions the velocity becomes zero at r = R. Hence all movement ceases at the radius R from the origin. Furthermore, since the integral of (10) shows that light would take an infinite time to travel over the radius R, we can never have any information of events happening at R or beyond, and hence may speak of a horizon to the universe at this distance.

TOLMAN determines the DOPPLER shift in two ways, with the origin at the observer, and with the origin at the source. In the first of these methods, the period of emission, from equation (E), will be:

$$dt_{\rm e} = \frac{k}{1 - r^2/R^2} ds$$
, (11)

during which the source will have moved the radial distance

$$\partial_t = \frac{dt}{dt} \partial t_0 = \frac{k}{1 - \mu t_0 m} \frac{dt}{dt} dt, \qquad (12)$$

and, by equation (10) for the velocity of light, the time taken by light to travers the distance will be

Hence the period of the light activing at the coupin will be

$$ds_{ij} = \frac{h}{1 - 1^{ij} R^{ij}} ds \pm (1 - p^{ij} R^{ij})^{ij} ds^{i}.$$
 (15)

where the plus ago applies to recoding object. As the provided in properturnal to the movelength observed at the origin and it to the models in it was heavily accepted in the local

$$\frac{dt}{1} = \frac{b}{1 - e^2/E^2} = \frac{b}{(1 - e^2/E^2)^2} \frac{d\tau}{dt} = \frac{1}{4}$$
(11)

Substituting from equation (v), the Dorrick shift is obtained in terms of the parameters of the orbit and the distance alone

For the Dorriza shift with the source at the name, (14) will take the form

By pating dr/dt = 0 in equation (i4), the Dorrect edited of the supple m at particular at the time of entrance m

$$\frac{d1}{T} = \frac{b}{1 - PDR} - 1, \tag{17}$$

where  $r_n$  is the distance from the origin to penhelion, and this equation, by the application of (6) can be rewritten in the form

$$\frac{dj}{dt} = \frac{1 - \frac{1}{2} + \frac{1}{2} - \frac{1}{20}}{1 - \frac{1}{2} \frac{1}{20}} - 1$$
(1H)

Since  $h^a$  are not be negative and  $R^a$  is larger than  $I^a$ , this may be written as the magnetity.

$$\frac{dI}{I} = \frac{1}{I(1 - 2L)R} - 1, \tag{(1y)}$$

or, expanding and neglecting higher order terms

whereas the Durrier effect at participes as positive, and would ordinarily be misspecied as a velocity of meeting.

Motoren it is not always positive, and the most valuable part of Torsian's analysis to be determination of the approximate relative durations of the positive and negative Dorrens edite to of the moving patitole in such a universe.

The equations of motion in a DE SITTER universe are completely reversible, as was first pointed out by Silherstein, and there seems no a priori reason why the number of positive and negative velocities among the spirals should not be approximately equal. Torman therefore next investigates the conditions for a reversed Dopplen effect, a.e., as a particle in a pe Street universe, though at rest at perihelion, will give the effect of a positive velocity of recession, over what range of its orbit will this positive velocity effect be of sufficient magnitude to cancel its negative velocity as it approaches perihebon?

In order to investigate the range of such a reversed Doppler effect, \$2/2 is set equal in zero in equation (15), giving as the condition for the radius r, at which reversal takes place.

$$\frac{r_t}{R^2}-\frac{h^2}{r_t^2}=2-2k,$$

while equation (8) gives as the condition for perhabon

$$\frac{r_1}{R^2} - \frac{h^2}{r_1} = 1 - h^2 - \frac{h^2}{R^2}$$

no that the reversed Doppler effect will be produced when an approaching source lies in the range between r, and ra. Since it is found later that k is of the order unity, and haiRs of the order zero, the range of such a reversed Doppler effect will be small Taking the radius re at which an oncoming source would come into observation as twice the distance to perihelion, which in its turn is taken as one-tenth of the distance to the horizon, which will give a DOPPLER shift at periludion, d1/2 = 0,005, the fraction of the time of approach to perihehon during which the particle would lie within the range which produces the reversed effect is only about 1/m (0,038)

As possible explanations of the facts observed in the spirals, Torman

considers in detail some four hypotheses.

A. The Hypothesis of Continuous Entry Here the uniform concentration of spirals within our observation would be produced by the continuous arrival of new objects to take the place of those which have passed perihelion and will never return. On this hypothesis, as the range of the reversed Dorpusa effect has been shown to be so small, there should be nearly an equality of the velocities of approach and recession. Only by making some rather radical assumptions as to the numbers of spirals which make perihelion at different distances from the origin, and making the assumption that the number of spirals which make perihedron at a given radius increase very rapidly with the radius, can the excess of velocities of recession be accounted for A linear increase of DOPPLER effect with distance is possible, but in no way inevitable. The radius of the observable universe must be at least ten times the range of distances at which spirals are now observed, as otherwise higher values would be expected than have been observed (order of 0,01) R would therefore not be less than 2 · 10 l.y.

B. The Hypothesis of Continuous Formation. The process of formation would be a continuing one, which will permanently maintain an approximately uniform concentration of the spirals. This idea is ahandoned as having little inherent probability. R on this hypothesis would be about 2 10° Ly

C. The Hypothesis of a Concentrating Fluctuation This assumes that the present concentration is the result of a finetuation from a smaller general concentration, which has occurred some time in the past. The chief demerit of this hypothesis is its appeal to some sort of special fluctuation in the concentration to account for the observed facts.

1 2

D The Hypothesis of Recent Formation, seems even more improbable than that of continuous formation, and for that reason may be abundoned at once

The conclusion which Tolman draws from his investigation is that the DE Sitter universe gives us no simple, adequate and, more than all, inevitable explanation of the facts exhibited by the spirals. In particular, he shows that only by rather drastic ad hoc specifications can this assemblage of data be explained at all. In detail, it can not be regarded as a satisfactory mechanism for the production of the present excess of large velocities of recession.

71 An Expanding Relativity Universe the Work of Lemaîtri, Eddington, McCrea, and McCitte. If the spherical universe is to be permanent and unchanging, the solutions of Einstein and de Sitter are both permissible. Robertson, and others, have shown that these are the only two possible solutions under such a condition. Lemaîtri has shown, however, that these universes are intrinsically unstable. That of Einstein has been described as containing "all the matter it can hold", while that of di Sitter is empty of matter. Eddington points out that there are an infinity of solutions for a spherical universe which is not in equilibrium, and that to every expanding solution there corresponds an individual contracting solution.

Lemaître places the pressure, p, equal to zero, while  $\varrho$  is the density of the total energy. The density of the radiant energy will be 3p, and the density of the energy concentrated in matter,  $\delta = \varrho - 3p$ .  $\delta$  is identified with T, while  $\varrho$  and -p are identified with the components  $T_1^1$  and  $T_1^1 = T_2^2 - T_1^1$  of the tensor of material energy. The components of the contracted Riemannian tensor are calculated for the interval:

$$ds^2 = -R^2 d\sigma^2 + dt^2 \tag{1}$$

Here  $d\sigma$  is the element of length in a space of radius unity, R is the radius of space, and is a function of the time. This feature is the essential advance of Lemaître's analysis, and has been followed in the latest papers of Tolman, Eddington, and de Sitter

The equations of the gravitational field are written

$$3\frac{1}{R^2}\left(\frac{dR}{dt}\right)^2 + \frac{1}{R^2} = \lambda + 8\pi\varrho\,, (2)$$

$$\frac{2}{R^2} \frac{d^2 R}{dt^2} + \frac{1}{R^2} \left(\frac{dR}{dt}\right)^2 + \frac{1}{R^2} = \lambda - 8\pi\varrho. \tag{3}$$

In the above,  $\lambda$  is a cosmological constant whose piecise value (or even its precise signification) is unknown, it is, however, very small  $8\pi$  is Einsti in's constant, which is written  $\varkappa$  by Lemaître.

A solution is then sought for the case where the mass of the universe remains constant while the radius increases. Calling this total mass  $M=V\delta$  and placing  $8\pi\delta=\alpha/R^3$ , where  $\alpha$  is a constant, and by aid of the relation  $\varrho=\delta+3\rho$ , the principle of the conservation of energy becomes

$$3d(pR^2) + 3pR^2dR = 0. (4)$$

Einstein's constant . 8 $\pi$  = 1.87 10<sup>-27</sup> c. g s. Unit mass . k = 6.675 10<sup>-8</sup> c. g s. Sun's radius in light-seconds . = 4.045 \cdot 10^{88} = 2.32 . = 1.48 km.

 $<sup>^{1}</sup>$   $8\pi$  is a constant in "natural" units. Some values in the natural and in the CG5 system which are frequently employed in such investigations are

Placing  $\beta$  as the constant of integration, this is integrated to

$$8\pi \dot{p} = \frac{\dot{\rho}}{R^4} \,, \tag{5}$$

and hence.

$$8\pi\varrho = \frac{\alpha}{R^6} + \frac{3\beta}{R^4}.$$
 (6)

Substituting these values in (2), he derives

$$\frac{1}{R^2} \left( \frac{dR}{dt} \right)^2 = \frac{\lambda}{3} - \frac{1}{R^2} + \frac{8\pi \varrho}{3} = \frac{\lambda}{3} - \frac{1}{R^2} + \frac{\alpha}{3R^2} + \frac{\beta}{R^4}, \tag{7}$$

where.

$$t = \int \frac{dR}{\sqrt{\frac{1}{3}R} - 1 + \frac{\alpha}{3R} + \frac{\beta}{R^2}}.$$
 (8)

Placing  $\alpha$  and  $\beta$  equal to zero and integrating, the solution of DE SITTER is found:

$$R = \sqrt{\frac{3}{\lambda}} \cosh \sqrt{\frac{\lambda}{3}} (i - i_0). \tag{9}$$

EINSTEIN'S solution will be found by making  $\beta = 0$  and R = a constant. Since dR/dt and  $d^2R/dt^2$  then become = 0 in (2) and (3), and

$$\frac{1}{R^2} = \lambda$$
,  $\frac{3}{R^2} = \lambda + 8\pi\varrho$ ;  $\varrho = \frac{2}{8\pi R^2}$ .

whence.

$$R = 1/\sqrt{\lambda}; \qquad 8\pi \delta = 2/R^4, \tag{10}$$

and, from (3)

$$\alpha = 8\pi \delta R^{a} = 2/\sqrt{\lambda}. \tag{11}$$

For Einstein's solution, (14) is not enough, the initial value of dR/dt must also be equated to zero. Putting

$$2 = 1/R_0^4$$
. (12)

and  $\beta = 0$  and  $\alpha = 2R_0$  in (8), there results:

$$t = R_0 \sqrt{3} \int \frac{dR}{R - R_0} \sqrt{\frac{R}{R + 2R_0}} \tag{13}$$

Writing:

$$8\pi\delta = 2/R_Z^4, \tag{14}$$

there results from (11) and (12).

$$R^0 = R^0_s R_0 \,. \tag{15}$$

The value of  $R_B$  the radius of the universe, deduced from the mean density on Einstein's formula (14), has been estimated at 8,8 10<sup>10</sup> Ly.

In order to find the DOPPLER effect for a universe of increasing radius, the equation of a ray of light from the line element (1) takes the form.

$$\sigma_{\rm s} - \sigma_{\rm 1} = \int_{1}^{L_{\rm o}} \frac{dt}{R} \,, \tag{16}$$

where  $\sigma_1$  and  $\sigma_2$  are coordinates characterizing the position in space,  $\sigma_2$  being the position of the observer and  $\sigma_1$  that of the source. A slightly later ray will leave  $\sigma_1$  at the time  $t_1 + \partial t_2$ , and arrive at  $\sigma_2$  at the time  $t_3 + \partial t_4$ . Whence:

$$\delta t_1/R_1 - \delta t_1/R_1 = 0$$
, and  $\delta t_2/\delta t_1 - 1 = R_2/R_1 - 1$ , (17)

where  $R_1$  and  $R_2$  are the values of R at the times  $t_1$  and  $t_2 - t$  is the proper time, if  $\delta t_1$  is the period of the emitted light,  $\delta t_2$  is the period of the light received. Thence

 $\frac{v}{c} = \frac{\delta t_2}{\delta t_1} - 1 = \frac{R_2}{R_1} - 1,\tag{18}$ 

which is the measure of the apparent Doppler effect due to the variation in the radius of the universe. It is equal to the excess over unity of the ratio of the radii of the universe at the time when the light is emitted and the time when it is received.

When r is placed for the distance of the source the approximate relation holds

 $\frac{1}{R}\frac{dR}{dt} = \frac{v}{cr} \tag{19}$ 

Utilizing the radial velocities of 42 spirals, and taking out a solar motion of 300 km/sec in the direction,  $\alpha = 315^{\circ}$ ,  $\delta = +62^{\circ}$ , Lemairri then derives a mean distance of 3.2  $\pm 10^6$  ly, and a variable radial velocity which amounts to 190 km/sec at  $\pm 10^6$  ly. Using equation (19), this gives

$$\frac{625 \cdot 10^{6}}{10^{6} \cdot 3,08 \cdot 10^{18} \cdot 3 \cdot 10^{10}} = 0,68 \cdot 10^{-27} \text{cm}^{-1}.$$

From this, by transformation and substitution in (13), (15), and (23), LI MAÎTRL derives the value

$$R_0 = 9 \cdot 10^8 1 \,\mathrm{y}$$

By substituting,

$$x^2 = \frac{R}{R + 2R_0},$$

the integral of (13) is transformed to

$$t = R_0 \sqrt{3} \int \frac{4 \, v^2 \, d \, v}{(1 - v^2) \, (3 \, v^2 - 1)} = R_0 \sqrt{3} \log \frac{1 + v}{1 - v} + R_0 \log \frac{\sqrt{3} \, v - 1}{\sqrt{3} \, v - 1} + C', \quad (20)$$

and designating by  $\sigma$  the fraction of the radius of the universe traversed by the light in the time t, and using (16):

$$\sigma = \frac{dt}{R} = \sqrt{3} \int \frac{2 dv}{3 x^2 - 1} = \log \frac{\sqrt{3} v - 1}{\sqrt{3} v + 1} + C', \tag{21}$$

from which Lemaître has derived the following table for  $\sigma$  and t as functions of  $R/R_0$ . The constants of integration in Table 18 were chosen so that  $\sigma$  and t

Table 18 DOPPLER Effect in Lumaitre's Expanding Universe

R/R <sub>b</sub>	$t/R_{o}$	e in degrees	v/o
1	00	-00°	19
2	4,31	<b> 51</b>	9
3	3,42	-30	5.7
4	-2,86	21	4
5	-2,45	15	3
10	1,21	- 5	1
15	0,50	- 1,7	0,33
20	Q	0	0
25	+0,39	1	
∞	∞	5	

should be zero for  $R/R_0 = 20$ The last column of the table gives the Doppler effects calculated from formula (19)

The shifts are seen to be excessive for all values of  $R/R_0$  less than 10, as Lemaitre well expresses it, there need be no speculation as to the formation of mirror or phantom images of the spirals or suns because, entirely aside from any questions of absorption of light in space, such

images, if received, would be displaced several octaves into the infra-red! These results of Lemaitre, obtained in 1927, have been the norm of most work in this field since that date, and his conclusions may be summarized

1 The mass of the universe is constant, and is connected with the cosmological constant, λ, through Εικετεικ's relation.

$$\sqrt{\lambda} = \frac{2\pi^2}{8\pi M} \approx \frac{\kappa}{4M} = \frac{1}{R_0}$$

2 The radius of the universe increases without limit from an asymptotic  $R_{\bullet}$  for  $t=-\infty$ .

3 The recession of the extra-galactic objects is a cosmical effect of the

expansion of space, and permits the derivation of a value for  $R_0$ .

4 The radius of the universe is of the same order as that deduced from the density by Einstein's formula

$$R = R_B \sqrt[3]{\frac{R_0}{R_B}} = \frac{1}{5} R_M$$

EDDINGTON transforms the foregoing formulae into:

$$\frac{dR}{dt} = \sqrt{\frac{R^4\lambda}{3} - 1 + \frac{4M}{3\pi R}},$$

and points out that there are three cases which may arise 1. If  $M>M_R$ , the system can expand continuously from a very small to a very large radius. 2. If  $M< M_R$ , the right-hand side of the equation vanishes for two positive values of R, and is imaginary between these values. Hence the world will either start with a finite velocity of expansion and expand to one of these values of R, or it will start with a finite velocity of contraction, and contract to the other of these values. 3. The limiting case is when  $M=M_R$  As  $R\to R_R$ ,  $dR/dt\to 0$  like  $(R-R_R)$ , hence the time that the radius remains in the neighborhood of  $R_R$  is logarithmically infinite.

EDDINGTON secures the spectral shift by the relation:

$$0 = \frac{\partial t}{R(t_0)} - \frac{\partial t}{R(t)},$$

where R(t) is the radius of the world at the time t, hence:

$$\frac{\delta t_0}{\delta t} = \frac{R(t_0)}{R(t)}$$

Taking the red-shift of the spirals as determined by Hubble as 153 km./sec. per  $10^4$  ly, he finds that this expansion amounts to about 1/2000 of the velocity of light. Hence  $\delta i_0/\delta i = 2001/2000$  for an interval  $i_0 - i = 10^6$  years. From this relation, the radius of the universe is considered to have expanded by 1 part in 2000 in the last million years. Eddington places the total mass of such a universe at

1,1 · 10<sup>20</sup> 
$$\odot = 2,3 \cdot 10^{54}$$
 g "Radius"  $= 1,2 \cdot 10^{9}$  l.y.

DE SETTER'S values of the "initial" and "present" radii of the universe are,

respectively, 0,8 and 4,6 · 10 ly.

That the universe is not only

That the universe is not only as likely to contract as expand (as admitted also by Eddington), but that it must in fact contract if there exists a single condensation at the origin, was maintained by McCrea and McVitte. If the start were made with an Einstein universe, and a condensation allowed to form, they maintained in their original paper that a process of contraction would be set up, which would persist indefinitely. They have since discovered an error in the analysis which led them to this theory, and now conclude that the total

L Obs 64, p 267 (1931)

volume of space is not altered to the first approximation by the change in the distribution of matter

In his latest paper Einstein has discussed non-static relativity universes, and has expressed a preference for a solution corresponding to a value  $\lambda=0$  for the "cosmological constant" DE Sitter shows that a family of oscillating universes result, and has investigated these in his most recent paper in the BAN 6, p. 141 (1931)

He makes the assumptions that the total mass of the universe, M, is constant and that the pressure is zero, from which the field equations reduce to the single

form'

$$\frac{1}{R^2} \left( \frac{dR}{e dl} \right)^2 + \frac{1}{R} = \frac{1}{3} \lambda + \frac{R_1}{R^3}$$

where  $R_1 = \alpha/3 = \varkappa M/3 \pi^2$  Placing

$$y = \frac{R}{R_1}$$
,  $t = \frac{ct}{R}$ , and  $\gamma = \frac{1}{3} R_1^2 \lambda$ ,

the equation becomes

$$\frac{dy^2}{dt} = \frac{1}{y} - 1 + \gamma y^2$$

The solutions of this equation are investigated graphically, with the aid of the relation

$$p = 1 - y + \gamma y^3$$

If  $\gamma$  is greater than 4/27, there is but one solution in which y increases from zero to infinity, i.e., an expanding universe

For  $0 = \gamma \le 4/27$ , there are two solutions, in one of which  $\gamma$  increases from  $\gamma_2$  to infinity, and oscillates between the limits 0 and  $\gamma_1$ ,  $\gamma_1$  and  $\gamma_2$  being the two points on the curve  $\rho = 0$  where  $\gamma$  has the prescribed value, and  $\gamma_1 < 1.5 < \gamma_2$ . There are then two families of solutions, a type of expanding universes, for positive values of  $\gamma$ , and the oscillating universes, for values of  $\gamma$  smaller than 4/27

Very significant are DE SITTER'S comments on the not very successful attempts to correlate the "expansion times" of such universes and present beliefs as to the time scale of stellar evolutionary processes.

". the time scale of the evolutionary processes can only be formally fitted into the scheme of the expanding universe by means of such a tremendous extrapolation as to deprive the theory of all real meaning. This is only another way of expressing the utter impossibility, which has already been repeatedly pointed out, of reconciling the short time scale of the expanding universe with our ideas regarding the evolution of stars and stellar systems. In the theory of relativity a year and a light-year are equivalent, whilst in astronomy 10° light-years is in very large distance, but 10° years is a short time."

DE SITTER also derives expressions which indicate that while there is a quasi-expansion effect within a galaxy, this is so very much slower than the expansion of the universe as a whole as to be practically entirely negligible

72. The Size of the Universe According to Sieberstein Radically different conclusions as to the dimensions of the curvature of space-time have been derived by Sieberstein in his book, "The Size of the Universe" (1930) In this work he has collected and revised his earlier articles in scientific periodicals, and it thus forms the most accessible summary of his views. The book contains one of the clearest and best introductions to the methods of tensor manipulation and analysis as yet available in English (see also the same author's article, Tensor, in the Encyc. Brit). Among the faults of the book are its marked polemic tendency, the apparent total rejection of modern results as to the distances of

the spirals, and the fact that most of the largest of the spiral velocities could not be included at the time the book went to press. It contains, however, valuable criticisms as to the validity of the EINSTEIN and DE SITTER universes, the author was the first to point out that negative velocities should be as apt to occur as positive ones; furthermore, Silberstein's method of attack differs from that of all other investigators in that he has applied his formulae to galactic objects

SILBERSTEIN'S development and method of attack is set forth in part V of the work referred to, to which reference should be made. His method consists essentially in the application of statistical methods for large groups of data, involving relations connecting the distance of perihelion, the speed which the object has in passing through perihelion, and the distance of the objects from the observer

For 20 clusters, he derives a value of the curvature radius,  $R = 40^8 \,\mathrm{ly}$ . For 38 spirals employed, he points out that R would be from 1 to 2,3 ·  $40^8 \,\mathrm{ly}$ , but is unwilling to accept From 29 Cephsids he secures  $R = 4.7 \, 40^8 \,\mathrm{ly}$ . Using 459 stars from Young and Harper's list<sup>1</sup>, he finds  $R = 6.4 \cdot 10^8 \,\mathrm{ly}$ . He finally adopts (p. 242, as of date of 1929)  $6.27 \cdot 10^8 \,\mathrm{ly}$ . This is roughly one-twentieth of the distances assigned by other investigators to the Coma-Virgo and Centaurus groups of external galaxies. The present writer feels that Silberstein's values for the "dimensions" of space are inordinately small, and that they will not stand the test of comparison with modern cosmical data, even if the inevitableness of some form of closed relativity universe be granted.

78. Various Determinations of the "Radius" of Space-Time.

Author	P, Ly.	Mans, g	Dale
DE SITTER SILBERSTEIN, HUBBLE LEMAÎTRE EDDINGTON, TOLMAN, INDIO THEE DE SITTER DE SITTER SILBERSTEIN, SILBERSTEIN	1,4 · 10 <sup>8</sup> 10 <sup>8</sup> 1,5 · 10 <sup>13</sup> 9 · 10 <sup>8</sup> 1,2 · 10 <sup>9</sup> 2 · 10 <sup>8</sup> 0,8 · 10 <sup>9</sup> 1,6 · 10 <sup>9</sup> 5,1 · 10 <sup>6</sup> 4,8 · 10 <sup>8</sup> 6,4 · 10 <sup>6</sup>	1,4 ° 10 <sup>86</sup> 9 ° 40 <sup>84</sup> 2,3 10 <sup>86</sup> 40 <sup>86</sup>	1917 1924 1926 1927, initial value 1930 1929 1930, initial value 1930, present value 1929, O-stars 1929, Cophoids 1929, 459 stars

Table 19 Values of Radius of Curvature of Space-Time

The values range from 4.8 · 10<sup>a</sup> Ly. (SILBERSTEIN) to 1.5 · 10<sup>11</sup> Ly (Hubble), though most investigators have postulated values of the order of 10<sup>a</sup> Ly. Were the present writer to accept some form of closed universe as inevitable, he would regard a radius of the order of 10<sup>12</sup> ly as the minimum admissible

74. Summary: the Dilemma of Choice between an Expanding Relativity Universe and the Distance-Velocity Correlation. The recent history of theories of relativity universes has passed through a stage of great confidence, perhaps over-confidence, in which considerable finality was thought to have been attained. As far as certainty is in consideration, its present condition does not appear quite so satisfactory. Omitting for the present other possible theories of Newtonian character, to be discussed later, there seems a partial dilemma, as individual hypotheses, between the two theories on which most recent work has been done. It would seem necessary to combine into one system the distance-

<sup>1</sup> Publ Astrophys Obs Victoria 3, No 1 (1924)

velocity correlation and the expanding universe, and no treatment has yet appeared showing in just what way the two are combined

It has been customary in some quarters to consider the velocities secured under the distance-velocity relation as apparent velocities (aside from individual motus peculiares, of course). This can not be so if the theory is to be allied with that of an expanding universe, for in such a structure the velocities must be real. If they are real, and if the present value of 170 km/sec per 10°1 y holds indefinitely, the outer parts at a distance of 2 10°1 y must be expanding with the velocity of light. Velocities nearly that of light in the region just this side of a finitely near horizon, do not appeal to the reason, this is, however, no argument against it, for in a domain beyond the scope of experience (a four-dimensional manifold in a continuum of six-fold curvature) it would be expected, perhaps, that the relations or seeming paradoxes which are the results of the basal hypotheses may also be beyond the domain of experience

The simplest explanation of a distance-velocity relation (Burns) is the manifest one that the objects with highest speeds would have reached greater distances from us. This presupposes, however, a universe without re-entires, and, like the theory of an expanding universe, meets with insuperable difficulties when the attempt is made to visualize the "initial" state. As a further alternative, it is perhaps reasonable to assume that the vibrations of the light-ray (not its speed) may be slowed up by minute amounts in passing through tremendous distances, were this so, the velocities of recession exhibited would be only apparent, and the most distant objects would be invisible, not from a horizon limitation, but from redness.

On the albed question of an expansion in a comparatively minute realm, one naturally recalls the K-term in stellar radial velocities. Such K-terms have been found by CAMPBELL, and others, particularly in the early type stars. They have given rise to a great deal of discussion, pro and con, of which one of the most recent and thorough investigations is that due to ROSENHAGEN¹. If existing, such effects may be regarded as giving support to a theory of expansion, as an expansion of spiral distances should be accompanied by corresponding expansion im kleinen. Vogt considers that the spiral arms are due to this same expansion effect. Assuming a star in our galaxy at a distance of 10¹ ly to be subject to this expansion effect of 1 part in 2000 per 10⁴ years, it should have a radial velocity, in this extreme case, of but 1,5 km/sec

75. Other Cosmogonical Deductions: an Aberration Effect Suggestions have been made that the high velocities of the spirals might produce an effect on the observed aberration Perrine<sup>2</sup> suggested that the aberration constant derived from a spiral of velocity 10<sup>1</sup> km /sec. should be 20",18 instead of the usual 20",47 Borčev<sup>3</sup> shows that Perrine's deduction is erroneous. "It should be remembered, however, that aberration can only be explained on the assumption that the observer moves relative to the other. The absence of the other drift necessitates, in turn, the constant velocity of light, whatever be the velocity of the source." VAN BIESBROECK has made careful position measures of the spiral in Ursa Major which has a radial velocity of +11700 km /sec (paper read at the September, 1931, meeting of the Amer Astr Soc), and has found no evidence whatever of a different value of the aberration constant for this object Courvoisier<sup>4</sup> has lately carried through some investigations of great interest,

A N 242, p 401 (1931)
 A N 240, p 319 (1930)
 A N 241, p 343 (1931)
 L Courvoisier, Zur Frage der Mitführung des Lichtätheis durch die Erde A N 213, p 281 (1921); Bestimmung der absoluten Translation der Erde aus säkulaier Aborration, ibid, 241, p 201 (1930), G v Gleich, Bemerkungen zur absoluten Translation unseies lokalen Fixsternsystems A N 242, p 265 (1931)

```
Notes to Appendix B
     1 Mossier 103
     2 Distance from Wallenguist, Upsale Medd 42 (1929)
     3 h and z Porsol, fifth star assumed of magnitude −2<sup>M</sup>,5 TRUMPLER [Publ ASP 38,
p 352 (1926)] gives a distance of 2,3 on the basis of the mean magnitude for Class Ao.
4 Measter 34
     5 Memier 45, the diameter from Russell, Dugan, and Stewart.
     6 Distance and diameter from RUSSELL, DUGAN, and STEWART corresponds to an angular
radius of nearly two degrees
     7 Mossier 38
     8 Messior 36, distance from Wallenguist, Upsale Medd 32 (1927)
     9 Mossier 37, distance from von Zerpel and Lindquen, Svenaka Vot Akad Handl 61.
No 15 (1921).
     10 Mossier 35
                                                 11 Scarcely resolved
     12 Ecceptric in an alliptical diffuse nebula.
     13 S Monocarotis in cluster,
                                                 14 Mossier 41
     15 Monator 50
                                                 16 r Canis Majoris in cluster.
     17 Memier 46, an important photographic catalogue by Chryalten
     18 Mossler 93
     19 Praceope, Mossier 44, distance from Ruberll, Dugan, and Stewart
     20 Messier 67
     21 Diffuse nebula in a coarse cluster
                                                 22 7 Caringo involved
     23 Coma Berenless, distance from Russell, Dugan, and Stewart
     24 w Crucis.
     25 Not resolved, a photograph of N G.C. 6540 appears in Pop Astr Tkisk 8, p 62 (1927).
     26 Mount Wilson plate.
                                                 27 Messler 6.
     28 Mossier 7
                                                 29 Mossier 23.
     30 Moraler 21.
                                                 31 Mossier 24
     32 Memior 16.
                                                 33 Mossier 18
     34 Mossier 17, nebulosity.
                                                 35 Monster 25
     36 Mossier 26, TRUMPLER finds a distance of 2,75 [Lick Bull 14, p 122 (1929)].
     37 Memier 11, distance from TRUMPLER.
                                                 38 Messier 71,
     39 Mossler 29.
                                                 40 Member 39
     41 Mossier 52, distance from WALLENGUIST, Upsale Modd 42 (1929).
```

Addendum Current work on problems of both our own and external systems, in progress since this section was written, contributes effectively to our view of galactic attracture and indicates the necessity for gathering much more evidence before any conclusive theory can be advanced. For instance, there have been important studies at Harvard, Mount Wilson (Straistins), and McCormick Observatories on the integrated magnitudes and colors of globular clusters. The absorption extending out from the "region of avoidance" appears to affect the magnitudes and distances of clusters in low latitudes, making uncartain and impractical the estimate of the dimensions of the Milky Way in its own plane, but, on the other hand, the Harvard studies of faint clusted type variables in high latitudes (Wash Nat. Ac. Proc in press, 1933) indicate a total galactic extent of the order of that given above.

A second uncertainty, which may eventually be turned into an advantage, tests upon the amount of random velocity, or average peculiar motion, which can be permitted a spiral or a group of galaxies. As to the variations within a group of galaxies, from the evidence of those determined at Mt. Wilson and given in Table 14, ciph 50, it would seem evident that this is 2000 km/sec, or more. If the cosmos be arranged on Charlier's scheme, in supergalactic groups, we may expect, also, an even higher variation in the velocities of such groups.

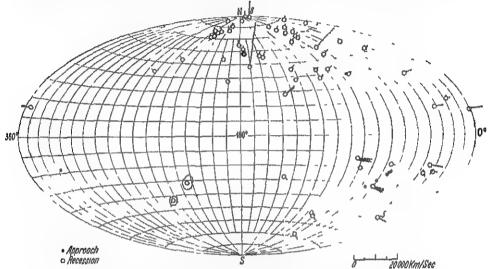


Fig 57 Galactic Distribution of Spirals of Determined Radial Velocity Positive velocities are indicated by lines extending away from the center of the diagram, and negative velocities by lines toward the center. The scale of the lines is indicated on the figure

77. Earlier Values of the Motion of our Galaxy in Space. A few of these values are collected in this Section, not because they are believed in any way to be a solution of the problem of the velocities of recession, but rather to indicate the past trend of research in this line. The distance-velocity values have been added. In this tabulation, A is the right ascension of the apex, D its declination,  $V_{\rm gal}$  the galactic motion, and K the "expansion" term common to all objects treated

Table 20 Values of the Apex and Motion of the Galaxy

Author	4	D	Pgal km /sec	km /sec	Reference
TRUMAN ,	300°	20°	670		Pop Asti 24, p 111 (1916)
Paddock	270	+30	200-	300-	Publ A S P 28, p 109 (1916)
Young and HARPER	300	-12	600	522	RAS Can 10, p 134 (1916)
Dose	299	+68	765		AN 229, p 157 (1927)
LUNDMARK	305	+75	651		Obs 47, p 279 (1924)
STROMBERG	310	+60	460	660	Ap J 61, p 353 (1925), mean of
		-	'		7 groupings of data,
Wirtz	195	+89	693	887	AN 215, p 349 (1922)
Hubble	286	+40	360	142/10 <sup>8</sup> 1 y	Wash Nat Ac Ploc 15, p 168
				,	(1929); 24 spu.
Hubble , ,	269	+33	306	157/10 <sup>6</sup> 1 y	ibid, 9 groups
HUBBLE ,	-	_	-	170/10 <sup>8</sup> l v	Ap J 74, p 43 (1931)
OORT .,	170	-64	360		BAN 5, p 239 (1930)
OORT , ,	_		_	90/10 <sup>8</sup> 1 y	BAN 6, P 155 (1931)
DE SITTER ,			-	146/10 <sup>6</sup> l y	BAN 5, P 157 (1930)

See further Appendix No 8

78. Moissard's Modification of the Dopping Formula. There have been several attempts to seek for other causes which might explain the recession of the spirals. Russell' shows that neither radiation pressure, nor gravitational or electrical forces can reasonably account for the high velocities of the spirals, to say nothing of their predominant positive sign

W. MICHILBON<sup>a</sup> pointed out that some of the assumptions in the derivation of DOITLER's principle are necessarily arbitrary; 1 that the period of vibration of the source is not affected by its motion along the line of sight, 2 that the

medium is at rest, and, 3 that its velocity is not changing

It is not impossible that a high "absolute" motion of our galaxy or our super-system of galaxies might contribute largely to the effect, as noted by DRUDIC

" In this case (both bodies moving) the rigorous calculation shows that the actual period T and the relative period observed at B stand to each other in the relation:

$$\frac{T}{T'} = \frac{c - u}{c \pm v},$$

(characters changed from original to conform with later nomenclature. H D C.) in which is is the absolute velocity of B, s that of A in the direction of the ray, and c that of the light in the medium between A and B . . Now we know nothing at all as to the absolute valcelities of the heavenly bodies, hence in the ultimate analysis the application of the usual equation representing Doffice's principle to the determination of the relative motion in the line of sight of the heavenly bodies with respect to the earth might lead to errors. Attention was first called to this point by Mosseard."

The Moissard-Drude suggestion that the ordinary formula for the Doppler shift is not rigorously accurate has not hitherto been considered, so far as the author knows. The great interest which attaches to the puszle exhibited by the great positive velocities of the spirals is sufficient warrant for the somewhat tentative illustration of this hypothesis given in Appendix No 8.

79. Conclusion. We must wait for many more velocities of spirals, with adequate representation near the south galactic pole and south of the galactic plane in the region from 180° to 360° galactic longitude, before any acceptable decision can be made between the various theories which have been advanced to explain the excess of valocities of recession exhibited by the spirals.

There are no theories of this very curious phenomenon which do not require the introduction of rather radical ad hoc hypotheses. In the velocity-distance correlation we need either to assume, with a considerable measure of observational support, that the vibration period of light is diminished by its passage through space, or that the universe is actually expanding, the outer parts more rapidly than the inner. If the cause is assumed a consequence of some form of expanding relativity universe, we find at once another basal assumption in the cosmological constant  $\lambda$ , which is inserted in the Einstein form of the gravitational equation.

$$G_{\mu\nu} = \lambda g_{\mu\nu}$$

"Finitude of space depends upon a "cosmical constant"  $\lambda$ . Except in so far as a value may be suggested by astronomical survey of the extra-galactic universe  $\lambda$  is unknown (EDDINGTON)." "The constant  $\lambda$ , which is a measure of the inherent expanding force of the universe, is still very mysterious, and it is difficult to see what its real meaning is. It might even be one constant too many, unless we may hope that it will ultimately be found to be in some way connected with Planck's constant h. Evidently the dynamical solution of Lemaitre is not

<sup>1</sup> Ap J 53, p 4 (1920). 
8 Ap J 13, p. 192 (1900)
8 Optics, English translation (1902), p 473, footnots 
4 C R 114, p, 1471 (1892)

the last word, but it can hardly be doubted that it represents an important step towards the true interpretation of nature (DE SITTER)" As noted earlier, the most recent solutions of Einstein and DE SITTER place  $\lambda=0$ . There is no theory yet advanced, in other words, which is free from somewhat drastic ad hoc hypotheses, all require a measure of extrapolation or speculation fat beyond the available range of observational data<sup>1</sup>

Whether one prefers to assume that light vibrations are slowed up by then passage through space (velocity-distance correlation, spiral velocities apparent), or to postulate a universe that is actually expanding (Lemaître's and other relativity universes, spiral velocities real), or to accept a universe of the CHARLIER type with the Molssard modification (spiral velocities in part real, in part apparent), is doubtless entirely a matter of individual choice and belief. The remarkably close parallelism between the structure of the suggested Charlier universe and the observed arrangement of the accessible exterior universe, is too exact and detailed to be cast lightly aside. Under assumptions which seem not more ad hoc than those which have been made for other theories tested, it would appear within the bounds of possibility to remove the excess of positive velocities which have formed the main obstacle to the acceptance of a universe of the Charlier type (see treatment in Appendix No. 8) For this and other reasons, therefore, the writer prefers, solely as a matter of personal choice and belief, to adhere, until more evidence may be gathered, to a cosmogony based on the scheme of CHARLIER, rather than to accept one or another of those which seem as yet somewhat nebulously based upon a fourdimensional frame of reference

It can not be too strongly emphasized, however, that many aspects of our present available observational evidence are so madequate and so incomplete that no final decision is possible, and that the field of speculation is still open as regards any of the theories which have been advanced in explanation of the excess of velocities of recession in the spiral class

# e) Appendices. Appendix No 1.

Finding List for Names frequently used in the older liferature

Namo	NGC	Mæssikr	Description		
America nebula	7000		Enormous diffuse neb		
Andromeda nebula	224	31	Largest spiial		
Crab nebula	1952	1	Planetary		
Dumb-bell nebula	6853	27	Planetary		
Hercules cluster	6295	13	Laige globular cluster		
Horse shoe nebula	6618	17	Bright diffuse nebula, of Omega		
Lagoon nebula	6523		Large diffuse nebula		
Network nebula	6995	1 —	Very large diffuse nebula		
Omega nebula	6618	17	Bught diffuse nebula, cf Ilorse- shoe neb		
Orion nebula, Great nebula in					
Orion	1976	42	Very bright diffuse neb		
Owl nebula	3587	97	Planetary		
Praesepe	2632	44	Bright open cluster		
Ring nebula (in Lyia)	6720	57	Planetary		
Swan nebula .	6618	17	Diffuse of Omega nebula		
Trifid nebula .	6514	20	Bright diffuse nebula		
Whirlpool nebula	5194	51	Fine spiral		

<sup>1</sup> Cf JEFFREYS' interesting and suggestive book, Scientific Inference, Cambridge (1931).

Finding List for MERSHER Numbers. (Abridged from SHAPLEY and DAVIS, Publ ASP 29, P. 178 (1917)

			78 (191	<del></del>	<del></del>
Meanite	NGC No.	Description	Ившия	NGC No.	Description
1	1952	Crab Nebula	51	5194	Spiral
2	7089	Globular cluster	52	7654	Cluster
3	5272	Globular cluster	53	5024	Globular cluster
4	6121	Globular cluster	54	6715	Globular cluster
5	5904	Giobular cluster	55	6809	Globular cluster
	6405	Open cluster	56	6779	Globular cluster
7	6475	Open cluster Diffuse nebula	57	6720	Plenetary (Ring nob lu Lyra)
Ą	6523 6333	Globular cluster	58	4579 4621	Spiral
9 10	6254	Globular cluster	59 60	4649	Spiral  Spiral (alli <del>ptical</del> )
11	6705	Open cluster	61	4303	Spiral
53	6218	Giobular cluster	62	6266	Globular cluster
13	6205	Heroules cluster	63	5055	Spirei
14	6402	Globular cluster	64	4826	Spirel
15	7078	Globular cluster	65	3623	Spiral
16	6611	Open cluster	66	3627	Spiral
17	6G18	Diffuse nobula (Horse-shoe		2682	Open chaster
***		or Omega nob )	68	4590	Globular cluster
10	6613	Open cluster	69	6637	Globular cluster Globular cluster
19 20	6273 6514	Globular cluster   Diffuse nebula (Trifid neb.)	70	6681 6838	1
21	6531	\`	71	6981	Open cluster Globular cluster
22	6656	Open cluster Globular cluster	72 73	6994	Open cluster
23	6494	Open cluster	74	628	Spiral
24	6603	Open cluster	75	6864	Globular cluster
35	I 4725	Open cluster	76	650	Planetary
26	6694	Open cluster	77	1068	Spiral
27	6853	Pianetary (Dumb-bell nob.)	78	2068	Diffuse nepula
28	6626	Globular citater	79	1904	Globular cluster
29	6913	Open aluster	80	6093	Globular cluster
30	7099	Globular cipator	81	3031	Spiral
31	224	Spirel (Andromeda neb.)	82	3034	Spiral
32	221	Spiral (elliptical)	83	5236	Spiral
33	598	Spiral	84	4374	Spiral (elliptical)
34	1039	Open cluster	85	4382	Spiral
35	2168	Open cluster	86	4406	Spiral (elliptical)
36	1960	Open chater	87	4486	Spiral (olliptical)
37	2099	Open cluster	88	4501	Spiral
38	1912	Open cluster	89 90	4552 4569	Spiral
39 40	7092	Open clustor Two faint stars		עטנד	Spiral
•		]	91	6341	Comet??   Globular chaler
41	2287	Open cluster	92 93	2447	Open cluster
42	1976	Dissume nebula (Great Ne- bula in Orion)	93 94	4736	Spiral
43	1982	Diffuse nebula	95	3351	Spiral
44	2632	Open cluster (Pruesepe)	96	3368	Spiral
45		Ploiades	97	3587	Planetary (Owl nebula)
46	2437	Open cluster	98	4192	Spiral
47	2478	Cluster	99	4254	Spiral
48	-170	Very open cluster	100	4321	Spiral
49	4472	Compact spiral	101		1.5
50	2323	Open cluster	101	5457 5866	Spiral   Spiral   identification
-	1	<b>\</b> -		, -	doubtful
	ſ	I	103	581	Open cluster

Appendix No 2
Finding Lists for Sir W Herschel's Classes and Numbers.
Herscher's Class I, 1-288

T. Land T. Co.	I 51 to I 100	I 101 to I 150	Tara to Took	Tent to Toro	7 074 40 7 099
I 1 to I 50	151 10 1100	1 101 to 1 150	I 151 to I 200	I 201 to I 250	I 251 to I 288
1055	6638	779	524	3877	3945
2775	7006	1022	821	3949	4041
3166	7331	6934	908	3938	4036
3169	393	7606	949	2639	4605
3655	7479	720	1453	2841	5308
5363	2903	1309	f023	4088	5322
4472	2905	1407	672	4096	1344
4698	1395	467	1600	4157	1491
4179	2784	1201	278	4220	3923
<b>4</b> 643	1332	7723	4546	4346	2880
4153	2974	7727	4159	4800	1931
1377	701	772	4866	4460	3682
3521	1052	2830	3115	4449	4128
4632	1084	2964	3294	5474	4250
4666	4361	3021	4151	5866	3182
4753	2781	3395	4369	2787	3206
3379	3962	3396	2782	1579	3445
3384	4856	3430	3184	2419	3458
4147	4902	4560	4145	3665	3488
3666	5634	3887	5290	3549	3610
3810	5812	4030	5739	3718	3613
4371	3254	1637	3432	3729	3332
4452	4150	4378	3941	4026	4589
4596	4245	4580	4062	4085	4648
4754	4274	4586	4203	4102	4291
<b>3</b> 345	4314	5746	4656	3631	4319
3412	4414	5813	4657	3780	4386
4438	2985	5846	4618	3898	4144
3593	3147	4699	4618	3998	4127
4365	3348	4958	5297	5422	6217
4526	3344	3672	5383	5473	613
4570	3900	2855	5713	5485	2977
4124	4494	2742	5750	3448	3183
5248	4725	4781	5728	4500	3329
4216	5012	4782	5633	5585	2976
4550	3245	4783	5195	5631	3077
4551	3486	2859	5377	5678	3735
4526	3504	5061	5689	5376	2655
4697	4251	4303	5676	5379	1
4941	4278	4713	5395	5389	
4731	4448	4808	5394	3621	1
4995	4559	4665	7008	2681	1
4594	4793	4900	651	4814	
6401	3813	5566	3675	3619	
6316	4214	5574	4111	3642	
6355	5005	5576	4138	3683	1
6712	5033	6304	4485	3690	
6356	5273	5921	4490	3894	1
6522	5557	6342	3198	2742	1
6624	584	6440	2683	2768	1

HERECHEL'S Class II, 4-350.

II 1 to II 50	II 51 to II 100	II 101 to II 150	II 151 to II 200	II 201 to II 250	II 251 to II 300	II 301 to 11 350
7184	3608	3489	6106	6569	7448	4984
7507	3626	3596	3692	6847	514	2481
157	3659	3800	3822	7013	660	2554
596	3691	3872	3825	6629	1134	2316
1032	4394	416B	4417	6642	7742	3110
1055	4450	4189	4443	6979	7743	5306
1580	2872	4208	4469	7217	95	5324
1587	2874	4212	4519	7741	1232	5343
1588	3070	4222	3681	214	2577	5426
7800	4124	4262	3686	315	2916	5427
4237	4294	4298	3804	972	7137	2986 5068
4651	4299	4302	3968	7457	1371	5084
3705	4313	4419	4193	7753	1385	
4119	4352	4473	4200	296	2139	5134
4578	4429	4477	4206	379	2196	2592
3462	4503	4479	4267	380	2613	2371
4235	4528	4474	4387	383	1415	2372 2608
4470	4564	4501	4388	392	3078	2619
4610	4608	4540	4413	407	3585	3106
4612	4638	4548	4425	410	718	
4795	4660	4458	4431	7367	741	4136
5106	4694	4461	4436	750	742	4278 4283
4420	4733	4476	4440	777	1070	4317
4772	4754	4478	4461	404	1153	4525
5147	4762	4639	4531	890	2967	4676
4453	5970	4654	4638	7678	4045	5089
5665	3338	4659	5600	7817	4073	5127
3226	3367	4689	5953	678	955	5623
3227	5669	5020	5954	680	1507 2695	5653
3626	2672	5936	4454	7769		
4592	3370	3423	4684	7771	2708	5607
3645	3455	3976	4691	7798	615	5832 3063
3640	4152	4180	4593	7332	636	3065
4412	4328	4197	4602	7339	1035 1208	3403
4457	4340	4215	4989	7556	1241	3516
4496	4350	4224	4775	7585	1299	3562
4527	4379	4223	4786	958 1003	1376	3629
4636	4405	4260	4951	1161	1886	3689
4664	4421	4261	4981	7814	1357	3798
2911	4450	4264	4928			3826
3389	4489	4326	4933	57	1421	3912
3547	4502	4333	5861	7681	3091	4555
3162	4515	4339	5077	57	3957	4747
3190	4540	4370	5548	7711	3957 4024	4789
3193	4710	4423	6287	234	4027	4819
3301	5962	4430	\$ <del>69</del> 4	877	5247	3248
3437	5996	4532	6544	7177 7280	4727	3327
2672	3041	4612	6540			3701
3599	3377	4623	6517	7454 7625	4877 4899	3710
3607	3485	5645	6528	7043	עעסד	31.10

HERSCHEL'S Class II, 351-700

II 351 to II 400	11 101 to 11450	II 451 to II 500	II 501 to II 550	II 558 to II 600	II 601 to II 650	II 651 to II 700
3728 3772 4162	5937 6118 3947	7444   210   7393	682 1172 1199	3637 3732 3892	1123 1129 1278	5930 6160 5129
4213 4455 5016	4032 4158 4336	7576 1417 + 1418	1209 2811 2907	2507 2889 2935	818 828 7231	5951 5980 5984
5637 3274 3277	4561 3897 4190	1065 1440 1452	3508 4033 4050	2718 '4658 '4759	1175 1193 252	6012 2691 4627
3380 3400	4534	521	5037 5044	4790 4939	661	4625 4655
3414 3418 3451 3510 3512	4711 4956 5014 5352 5440	533 550 1550 1090 1087	5049 5054 1620 1635 1713	3715 4825 2778 3381 5078	681 855 2274 2275 2435	4704 4963 5023 5103 5123
3713 4008 4017 4104	5444 5533 5544 5614	7562 7785 7284 1140	4904 4227 4229 2765	5 101 4270 4273 4277	691 695 1156 1169	5145 5289 5320 5336
4134 4173 4185 4196 4209 4275 4283 4310 4375 4556	5656 5675 5695 5347 5990 6962 6964 7311 7541 7537	137 255 599 873 1200 7310 7371 151 191 217	3611 1036 1646 1618 1638 1653 1682 1684 2721	4281 4300 4281 5668 5701 5770 4600 4701 5560 5638	259 428 3955 2990 4348 3604 2545 4342 4474 4468	5362 5410 5608 5630 5697 5784 5787 5893 5183 5184
4692 4798 4816 4827 4840 4839 4841 4869 4872 4892	7600 7724 337 357 788 881 883 895 7619 7626	681 833 835 838 838 839 851 945 1045 932 2770	4480 #630 5390 5364 4771 4845 4999 5740 5806 5831	5636 5690 6010 6235 5864 6445 6426 665 673 7458	4506 4595 1058 2563 3660 4597 5015 5253 3158 3163	5691 5719 5792 5865 5327 5345 5506 5301 5198 6155
4889 4911 4921 4923 4944 4952 4957 4961 5958 5910	7634 7364 7391 227 245 271 430 545 547 7443	2968   3067   3413   3424   2906   4233   4434   4470   4492   14535	\$839 \$838 \$850 \$854 \$869 2872 2874 4129 4818 3636	14 1024 1400 1442 7183 706 1441 7377 7197 7640	3334 4156 4662 4868 4914 5112 6158 5696 5704 5899	5448 5480 5481 5602 5660 5673 5351 5380 5406

HERSCHEL'S Class II, 701-909

HERBEITEL'S CIAMS II, 701 — 909								
II 701 to II 750	11 751 to 11 800	II 801 to 11 850	Il 851 to II 900	11 901 to 11 910				
6207	5857	5486	7773	6389				
7392	5859	4149	1435	6555				
259	6181	4161	29	30617				
1184	5582	4271	128	3523				
7354	5875	4290	132	3752				
7538	5820	4335	194	5949				
185	5879	5667	198	6646				
2798	5905	5687	200	2650				
3600	5907	5751	693	3063				
5311	5908	6125	196	46467				
5313	5963	6143	2320					
5326	5965	6338	2332					
5350	5894	4187	257					
5353	5982	4732	3904					
5354	5987	4987	4105					
5371	5985	5040	4106					
2998	6340	5250	4194					
3415	1569	5881	2814					
2543	2339	3571	2820					
3202	3687	2387	3259					
3205	4504	2415	3266					
3207	4626	2426	3394					
3891	4628	2693	6048					
3971	4671	3917	5928	1				
4020	3652	3924	6166	ļ				
2532	4487	5109	5 <del>49</del> 2					
2649	4813	5430	5513 6824	ĺ				
3583	4888	2756 2660	3622	}				
3614 3726	, 4925 5085	3669 3804	3654					
3769	4068			ļ				
3789 3782		3838	3879					
3762 4013	3656 3738	3895 3958	3225 3238	ł				
2326	3756	2726	3517					
2329	3888	3043	3625	1				
2340	3913	3725	3674	Į.				
3811	3916	3762	3435	ļ				
3893	3921	3770	3470	ł				
3896	1 3972	3796	5374	1				
3928	3977	3978	5491	<b>\</b>				
4047	3990	5216	5652	1				
4248	4172	5218	5661	1				
4381	4198	5370	5674	1				
4617	4644	5376	5679					
3320	4686	3668	5257					
5018	4695	4256	5258	J				
4144	5201	4332	7218					
4217	5278	4441	3107					
4389	5443	4524	5323	1				
, <del>116</del> 0	1 5475	4545	1247	i				

HERSCHET'S Class III, 1-350

III 1	III 51	III 101	III 151	III 201	III 251	III 301
to	to	to	to	to	to	to
III 50	III 100	III 150	III 200	III 250	III 300	III 350
1982	3020	5239	807	871	474	4495
867	3024	3833	1012	7168	488	4514
4028	3153	3876	266	7-197	520	4962
2939	3209	3874	421	251	3044	4966
3342	3300	4598	420	459	3156	5004
4698	5416	4779	495	473	2555	5056
2508	5146	3356	496	794	2618	5057
2894	5463	3425	499	803	4077	5065
5208	5482	3790	507	7042	850	5074
5209	2744	5587	508	7463	863	5672
5417 5570 4577 5621 3646 3649 4409 4505 2402 3433	2774 2802 2803 2843 3129 3303 3473 4126 4498 4758	3535 3679 3915 4422 5146 5885 5076 5079 5111 5605	987 1060 1066 1240 7186 7335 515 517 517 513	7165 7659 7691 774 781 7385 7386 7648 6956	941 1239 1409 2722 755 731 2076 1781 1993 2089	5808 5836 6011 6091 2963 3252 3343 3364 5620 3812
3491	5180	5597	536	7559	2283	3902
3506	5249	5595	552	7563	3052	3944
3524	6021	6267	553	171	3072	4015?
3088	6073	6278	614	907	3981	4021?
3177	3498	5396	679	2124	2763	4007?
4529	3616	5642	735	7671	2902	4101
3605	4037	5706	925	827	2992	4146
3686	4516	5709	1167	1044	2993	4670
3768	3559	5771	697	1046	4035	4673
3802	3731	5773	7316	7469	4724	3216
4344	3773	5798	7550?	7778	4756	3270
5490	4752	5635	7578	7779	5073	3475
6046	4880	5735	52	7782	5677	3615
2984	5136	5523	7506	2599	3818	3618
3848	5222	5594	7566	2628	5369	3651
3852	5221	5610	7592	2764	5468	3653
4067	5230	6372	7694	7321	5476	3670
4368	3401	5898	7701	7570	2566	3808
4390	3567	5903	7725	922	2983	3815
4482	3914	6064	7832	1979	3956	3832
4491	4246	6907	352	2073	2750	3911
4497	4296	6926	702	2815	2604	3951
4606	4297	6717	748	7436	3068	3983
4647	4343	6857	1266	216	2679	4002
5174	4341	7052	1287	1187	2783	4003
5175	4342	7720	1321	1353	2796	4979
5532	4366	23	1320	1401	2893	5559
5747	4588	108	1003	1426	2918	3196
2648	5210	233	1160	1439	4272	3265
2661	5235	604	213	470	4286	3527

HERSCHEL'S Class III, 351-700.

	ARRECHEL'S CHAM III, 351-700.							
III 351	III 401	JII 451	III gos	111 551 to	III <b>601</b>	III 651		
III 400	Ш 450	III 500	III 550	TII 600	111 650	III 700		
3550	4986	1393	1670	5546	3060	5157		
3552	5141	7156	1678	5549	4571	5187		
3714	5142	1762	1729	6070	4634	5433		
4004	5149	622	4591	5775	845	4985		
4080	5154	1073	5252	6548	2512	5003		
4131	5199	36	5356	532	2558	5214		
4132	5223	864	5203	990	2562	5730		
4169	5228	7252	5729	7492	2743	5731		
4174	5240	686	4599	1370	3791	5888		
4175	5265	723	2110	551	4705	5900		
4393	5399	24	5845	687	4720 3952	5922 4653		
4475	5401	1094	2513	703 704	4843	4668		
II 4051	5445	268	2914		4890	4690		
4927	5529	762	4703	705 706	3304	5334		
<del>498</del> 3	5579	7432	4739	797	3930	5392		
5000 5032	5589 5590	7794 154	4773	834	4025	5400		
5116	5533	773	4777 3145	1308	4774	5604		
5251	5616	1162	2948	1397	5107	5017		
5263	5654	7526	2863	898	5243	5047		
6001	5684	624	2979	910	5305	5716		
3883	5312	977	3411	980	6038	5173		
5768	5318	7647	4682	982	6120	5256		
5913	4719	924	4700	1293	6137	' 5500		
3805	5233	1036	4770	1294	27047	5714		
3821	7685	160	4784	7426	2755	5520		
3837	7750	280	2969	477	2838	1 5622		
3842	61	3099	2980	1207	2844	5797		
3926	274	2459	3591	7707	2852	5804		
3940	273	II 3115	3661	1138	2853	1 6154		
3954 4095	586 600	4356 4415	3667 3693	1030 1088	3237 3468	<sup>1</sup> 5303 5361		
4098	790	4464	4114	780	5093	5403		
4099	991	4488	4177	1056	5966	5407		
3862	7623	244	4265	1609	5992	+ 5515		
3860	7816	867	4714	1611	5993	5732		
3875	7751	1354	4748	1576	6058	5754		
3884	7665	2848	4794	1643	0146	6104		
3937	279	4763	5094	1659	61501	6255		
4049	450	1552	2719	1954	6173	5757		
4070	560	4014	2955	1242	6175	1 5791		
4069	564	4418	3074	426	5185,	7171		
4074	1248	4541	4688	429	5207	7180		
4061	1304	4642	4765	493	5522	1 1343		
4065	1324	4583	5019	193	5649	896		
4076	1358	4737	5382	3081	6018	7139		
4204	1924	3434	5386	2921		4183		
4685	2110	3495	4799	3509		5337		
4163	1114	1516	5329	2595	5025 5096	23355		
4097	1125	1779	5716	3053	1 3030	3319		

915

HERSCHLL'S Class III, 701 - 981

				<b>7</b> 01	
III 701	III 751	III 801	III 851	III 901	III 951
to III <b>75</b> 0	to III 800	to 111 850	to III 900	to III 950	to 111 98 t
3374 4253 2389 3192 3478 3595 3985 4117 2500 2541	2965 2530 2582 4087 4403 4404 4520 4878 4879 4928	4364 4547 5255 5526 5540 5777 4549 5113 5372 5402	4238 4391 3073 7760 7805 7806 1366 7016 7081 7680	2388 2578 4034 1120 3961 4693 4749 4857 5034 3188	6331 1633 1634 163 270 1284 6500 6501 1331 1362
2552 2684 2856 2854 3906 3922 4100 4218 4231 4232	4942 5478 5618 4462 4970 4993 3298 3657 3931 3594	5821 6088 6182 4142 4707 4801 4834 4932 4998 5009	39 7223 7248 7250 1985 13 7797 12 125 182	3220 3284 3408 3440 3530 3102 3286 3288 3407 3543	1377 1482 2938 3174? 3194? 3197? 3500? 3500? 3747? 3901?
4741 4708 3577 5087 4242 4288 6239 6283 4392 6186	3733 3737 3794 3824 3829 3850 4181 4675 4964 4977	5163 5225 5238 3497 2746 2780 2840 3885 2431 2474	173 192 201 2322 2329 180 2525 2805 4384 4566	3589 3671 5328 5592 5118 5224 5599 5331 7165	3939 3471 6068 6251 6252 5789 2908 3057 3210 3212
5536 5541 5598 5603 6241 5878 5902 5989 6015 6140	4973 4974 4967 5164 5294 5368 5447 5461 5462 5477	2692 2800 3870 4511 5526 2469 2488 2497 2505 2534	3392 5671 6071 6079 5760 5851 5852 6103 6089 6177	7230 7246 7251 3080 3734 7076 4972 4363 4572 3890	3215 2629 2641 7810
6434 6742 6781 6814 7423 2347 II 2133 2366 2810 2493	5484 3398 3499 4054 4141 4195 4199 4284 4358 4362	2710 3353 3757 3795 4154 2870 3740 5007 5342 4210	6129 6142 6195 5702 5710 5737 2290 2289 2333 2385	4159 4331 5909 5912 6324 5295 5452 5547 5640 5712	

Herse Class IV	CHEL'S , 1 — 79		веп <b>ки'я</b> V, 1—52	Here		MBCS VI, 1 VIII, 1—8	-42, VII,	167,
IV t	IV 51	ا ۷	V 51	VI I	VII I	VII 51	VIII 1	VIII SI
IV 50	IV 79	V 50	V 52	VI 42	VII 50	V1I 67	VIII 50	VIII aa
7009	6818	253	4236	2420	1662	7062	2509	2306
2261	7635	4536	3359	2304	2244	7082	2063	2413
2245	1501	4910	* ·	2269	1498	7209	2251	6507
3662	4143	4123		3055	1817	2253	1896	6561
4517	2537	4293		2194	2236	7762	2264	6596
3423	4051	5293		2355	2356	7790	2180	6910
3507	6301	3346	1	5053	6520	2192	1663	7024
4567	40	3628			6940	2479	1647	6997
4568	3658	6526		3466	6930	6866	2234	1664
3239	3310	6514		6144	2482	1513	2678	2311
6369	3992	6514		6284	2539	1528	2395	1778
6553	3982	6514		6293	2360	6756	6664	7708
6894	5204	6533		6451	2204	2627	6728	7234
6772	2440	6992		6802	2318	2567	6647	381
16	2346	6960		6678	2352	2401	6604	659
6905	2701	68		6839	2354	7143	6834	1027
1253	3963	598		2158	2362	2421	6938	7160
7662	2950	205		2309	6823	i	6837	2126
2170	1514	891		5897	6755		6840	7686
2185	5144	247		288	2215		6885	1582
1964	5856	2359		2266	1758		6800	2281
2467	6888	5170		2548	2254		6R82	6633
936	6826	3027		6645	2489		6950	6828
2023	7023	4565		7044	2112	1	2169	7031
2327	7129	246		1245	2186		2232	7243
1535	6946	3003		1605	2225		2129	6991
3242	1325	2264		2301	2349	ŀ	2367	7380
4038	4750	2024		2259	2423		2026	225
3456	3034	4395		7245	5998	1	7826	129
4861		1977		7789	6568		2627	1444
7302		1980	ŀ	663	6583		2286	6793
1700		1788		7086	752		2335	6989
1999		1908		869	1857		2343	6895
2022		1990		884	1883		2353	1348
2610				136	2224	]	2374	1545
2071	i	206		2132	2270	į	2396	6874
6543		7000		2506	2262		2414	2425
2182		1909		6804	2324		2422	1342
2438		3511		2571	1907	1	2302	
4804		3513		6171	7128		2331	
6514		4244		6412	7296		1802	
676		4631		6939	457	1	1996	
1186		4258			7419	1	1750	
2167		2403			7510	ł	2394	
2392		3953			436	1	2358	
5 <del>49</del> 3		3556		i	654	1	2430	
4915		3079			1502	1	2428	
3104		1097			559	1	2260	
5507	}	1624			637	1	2240	
6229	ţ	2997	ŀ	•	7067	1	2252	I

Appendix No 3
Finding List for General Catalogue Numbers

GC	NGC	GC	NGC	GC	NGC
100 200 300 400 500 600 700 800 900 1000 1100 1200 1300 1400 1500 1600 1700 2000 2100 2200 2300 2400 2500 2600 2700 2800 2900	196 376 516 676 812 1068 1370 1500 1653 1783 1892 1997 2102 2216 2436 2448 2666 2816 2969 3105 3240 3376 3319 3658 3812 3911 4209 1334	5057 58 59 60 5061 62 63 64 65 66 67 68 69 70 5071 72 73 74 75 78 80	7832 119 313 1251 1312 1767 1922 2189 2198 2515 3123 3229 3801 4270 4582 5200 5310 5366 5404 6634 7150 7285 7692	\$100 \$200 \$300 \$400 \$500 \$600 \$700 \$800 \$900 6000 6100 6200	113 751 1236 2487 2943 4031 4893 6041 6579 7085 7420 7670
3000 3100 3200 3300 3400 3500 3600 3700 3800 4000 4100 4200 4300 4400 4500 4600 4700 4800 4900 5000	4444 4556 4668 4793 4961 5095 5227 5361 5492 5634 5771 5925 6152 6362 6611 6805 6960 7127 7299 7507 7727				

Appendix No. 4

JН	NGC	J HL	NGC	ј н	NGC	J H.	NGC
1	12	1500	4864	3000	2150	4000	7713
50	224	50	5009	50	2231	4006	7764
100	477	1600	5142	3100	2452	4007	319
50	672	50	5248	50	2788	4008	322
200	835	1700	5352	3200	3053	4009	7796
50	1043	50	5475	50	3247	4010	7812
300	1343	1800	5603	3300	3447	4011	7823
50	1857	50	5696	50	3742	4012	368
400	2262	1900	5834	3400	4553	4013	7832
30	2392	50	6103	50	4903	4014	7
500	2562	2000	6572	3500	5126	4015	10
50	2742	50	6826	50	5393	4016	1905
600	2889	2100	7010	3600	5915	4017	2658
50	3032	50	7218	50	6222	4018	2973
700	3207	2200	7458	3700	6407	4019	3244
50	3370	50	7691	50	6653	4020	6404
800	3475	2300	7817	3800	6816	4021	6708
50	3514	50	264	50	7007		
900	3697	2400	461	3900	7154		
50	3819	50	754	50	7322		
1000	3930	2500	1140				
50	4036	50	1359		[ [	1	
1100	4123	2600	1493				
50	4221	50	1616	l			
1200	4299	2700	1759		[ ]		
50	4387	50	1816				
1300	4484	2800	1871	]			
50	4555	50	1943				
1400	4635	2900	2014		1	1	
50	4727	50	2080				

## Appendix No. 5

#### Systems of Nobular Classification.

- A Classification of Sir Wm HERECURL. This consisted of eight main classes,
  - I Bright nebulas.

  - II Paint nebulae. III. Vory faint nebulae
  - IV. Planetary nebulae Stars with burs, with milky chovalure, with short rays. romarkable shapes, etc.
  - V Vory large nebulae.
  - VI Very compressed and rich clusters of stars
- VII. Protty much compressed clusters of large or small stars,
- VIII Coarsely scattered clusters of stars.

As an amplification of those main classes, HERSCHEL used the abbreviations,

B Bright v. vary P. Punt c. considerably L. Large p. protty 9. Small e extremely,

the combination of which gave him sixteen available subdivisions in each class. A dozen or so other casily understood abbreviations gave a further description of the object in a very compact form, as,

"'. VBpLvgmbM — "very bright, pretty large, very gradually much brighter in the middle."

B Classification of Sir J Hirschill file introduced into his father's system five categories, each with five subdivisions

Sub class	Magnitude	Brightness	Roundness	Condensation	Resolvability
1 2 3 4	Great Large Middle-sized Small Minute	Lucid Bright Faint Dim Obscure	Circular Round Oval Elongate Linear	Stellate   Nuclear   Concentrated   Graduating   Discoid	Discrete Resolvable Granulate Mottled Milky

The object was then described by five numerals, 32255 would indicate "Middle sized, bright, round, discoid, milky". This system, with minor modifications, was employed by Schutzi, Nov Act Reg Ups 9 (1874). A somewhat similar system was employed by Broomsdan, CR 158, p. 1949 (1914), making use of nine sub classes under each of the categories, brightness, extension, form, condensation, and resolvability.

- C Bailey's Classification The merit of this classification is that the element of spectral type was included Harv Ann 60 (8), p 200 (1908)
  - A Vast, faint, irregular nebulosities, shown on photographs of long exposmo Examples, Nebula in Cygnus, Great Spiral about Orion
  - B Gaseous nebulae Objects having gaseous spectium
    - B1 Large, diffused, irregular Examples Orion, η Carmae
    - B2 Planetary, rmg, and other small, well-defined gaseous nebulae Examples 3587 (Plan), 6720 (Ring neb), 6618
    - B3 Nebulous stars Examples, 1514, 2003
  - C White nebulae and globular clusters Objects having continuous spectra
    - C1 Nebulae, small, round, unresolved, of somewhat definite term, generally round or elliptical
    - C2 Spiral nebulae
    - Examples 224 (Andromeda), 5194 C3 Globular clusters
    - Examples 5139 (\omega Centauri), 6205 (Hercules)
  - D Trregular clusters
    - D1 Fairly condensed, somewhat regular, stars of comparatively uniform magnitudes
      Examples 2437, 6494
    - D2 Fairly condensed, irregular, stars of different magnitudes Examples 869 and 884 (double cluster in Persons), 4755 (x (111115)
    - D3 Coarse, irregular, stars of different magnitudes Examples: Hyades, Pleiades
  - D Classification suggested by H Shapley [Harv Bull 849 (1928)]

Brightness,	Class A, brighter than 12 phg magn
•	,, B, 12-14 ,, ,,
	, C, 14-16 ,, ,,
	, D, 16-18 ,, ,,
	, E, 18-20 ,, ,,
Concentration,	a, least concentrated
	b,
	C,
	d,
	e,
	f, most concentrated
Degree of clouga	
Spiral form,	classification preceded by s
Irregular,	- • • · · · · · · · · · · · · · · · · ·
Tricknist,	Example: sAb9 = "a nearly round, bright spiral, very little
	Etample: SADy = a nearly lound, bright Spiral, very fithe

example: saby = "a nearly round, bright spiral, very little concentrated"

E Wolf's Classification Die Klassifizierung der kleinen Nebelflecken, mit Tafel, Heidelberg Astroph Inst 3, No 5 (1908), used also by Hubble, Yorkes Publ 4, part II (1917), with the addition of an extra type  $h_6$ 

An empirical system of classification, of 22 types indicated by the letters from s to s, with the emission of f, s, y, and s. The forms corresponding to these letters are given in a chart, to which reference must be made. See also Lundmark's allocation of Wolf's types under G below.

F Hunsle's Nobular Classification Mt Wilson Contr 324 (1926), of also ibid. 214 (1921) In this system it is assumed that the evolution of the spirals is from an earlier, closely arranged and compact form to an older form of more open arrangement

Cherecter	Gymbol		NGC Example
I Gelactic nebulac			
A Planotarica	P		7662
B. Diffuse			
1 Predominantly luminous	DL		6619
2 Predominantly obscure .	DO		Barnard 92
3 Conspicuously mixed	DLO		7023
II, Extra-galactic nebulae	1 1		
A. Rogular	1 1		
1 Klipticai	] En ]	Eo	3379
(a, omitting the decimal point = 1, 2,	1 1		
, 7, indicates the ellipticity of the	1 1	K2	221
object)	1	E5	4621
	1	E7	2117
2 Spirate	1 _ 1		1
a) Normal apirals	S		4404
Rarly .	Sa. Sb		4594 2841
2. Intermediate 3. Late	So		5457
b) Barred spirals	SB		3.57
i Barly.	SBn.		2859
2. Intermediate	SBb		7479
3. Late	SBc		3351
B. Irregular	l Irr		4449
Extra-galactic nebulae too faint to be			
classified	ا ي		l .

G LUNDMARK'S Nobular Classification. Studies of Anagalactic Nobulae, First Paper, Ups Modd 30 (1927) is perhaps the most detailed classification which has appeared to date. It is given below with a few verbal changes, and with LUNDMARK's allocation of Wolle's types.

	Character	Symbol	Example	Word
ī	Galactic Nobulae	G		
	4 Quasi-planetary nobulas	Gp		a, b, c
	a) No contral star	Gp0	6537	a, b,
	b) Hollooidal forms c) Central star and different gradations in the ratio of total light to light of	Gph	6543	•
	central star	Gp1—Gp10	40	c
	2. Irregular nebulae	GI GIb GId		
IT	Anagalactic nebulae	) A		1
	1. Anomalous nebulac	Δa	2537 5144	
	2. Globular, elliptical, elongated, ovate, or lentiquiar nebulae .	Λο		Ì
	a) Very little compressed toward center	ABO	4302	đ, h
	b) Siightly compressed toward center	Åe1 Åe2	2233 1600	9

	Character	Symbol	Γπιπρίο	Wolr
	d) Rather " " " e) Much " " " f) Very much " " " The letter a is added if absorption is present, e g	Ae3 Ae4 Ae5 Ao3a	1382 1278 4486	f, g, h, 1, k
7	Magellanic nebulae	Am		
•	a) Very little if at all compressed towards center b) Different degrees of compression	Λm0 Λm1 – Λm5	1449	p? q?
4	Spiral nebulac	As		
	a) Spiral structure barely seen b) Different degrees of compression to-	Aso	4 194	o
	wards center	As1-As5		
	Spiral arms continuous	Asic-Assc	3031	9, V
	Spiral arms broken	As1b-As5b	598	r, u, v
	c) One-branched spirals	As0	5278	
	d) Spual arms form a bright ring	Asr	4736	l t
	e) Doubtful connection of img with center (Saturn-shaped) f) Baired spirals g) Spiral arms have an appendix nebula	Ass Asp Asa	936 1326 5194 — 5	

## Appendix No 6.

### Published Reproductions of Nebulae

Introductory Any system of classification, however detailed, has serious limitations in the representation of objects which differ so greatly from individual to individual as do the diffuse and planetary types, and the spirals. For this purpose, there is nothing quite so satisfactory as a pictorial representation. The ideal NGC of the future would have a picture of the object at each entry!

Photographs and sketches of the various classes comprised under the term "nebulae" are for the most part widely scattered in the periodical literature. The following list is intended to give, in general, the best available representations that are available up to 1931. The list does not pretend to be complete, where there are very many representations available, as for an object like the Great Nebula in Orion, only a few of the better plates are mentioned. Reproductions in articles or books of a more popular nature are omitted, unless no other example occurs

The sketches of Rosse and Lassell have been included for their historical interest; these observers were the first to employ apertures adequate to recognize spiral character. Sketches will be indicated by asterisks\* \* It should be noted that the sketches made at Helwan and those of the planetaries made at Lick were carefully drawn from photographs and are nearly the equivalent of a photograph. The very large number of sketches in the older literature, made from visual observations, have been omitted, except as noted above.

References are given in the form Publication, volume, page preceding plate, number of figure on the plate if more than one is given, date Dates are omitted for Lick Publ 8 (1909), 11 (1913), 13 (1918), for Barnard's Atlas of Selected Regions of the Milky Way, Carnegie Institution, Washington, 1927 (abbreviated to 'Atlas').

Rosse's drawings appeared originally in Phil Trans 1850 and 1861, they are now most easily accessible in his Collected Scientific Papers, 1926. The plates retain the pagination of the Phil Trans, Plates XXXVI—XXXVIII

follow pages 112, 114, and 116 of the Collected Papers, and are from Phil Trans 1850; Plates XXV—XXXI follow page 150, and are from Phil Trans 1861. In citations of Rosse the page and date will be omitted.

LASSELL'S sketches (LAS) appeared in Mem RAS 36, pp. 82ff. (1866).

The plate only will be quoted, omitting the page and the date.

ROBERTS, Photographs of Stars, Star Clusters and Nebulae, London, 1893, 2 vols., will be referred to by ROB I and II. The dates given are those on which the respective plates were made, as for many objects the photographs of ROBERTS were the first taken. Other photographs published and discussed by Mrs. ISAAC ROBERTS in the M N are also headed ROB.

A large number of BARNARD's dark nebulae are best studied in the Atlas; entry is generally given for these objects only when taken individually. fr. = frontispicce; end = at end of volume, etc.

Most of the illustrations in the Ap J will be found also in Mt Wilson Contr

where the paper is repeated,

Number	Class	Reference
40	plan.	Lick Publ 13, p. 58, VIII, 1a and *L*; spectrum, ibld., p. 86, XXVII, 4, 5, 15; p. 240, XLIV, 3, 4, 5; L, 3.
68	nob, st.?	*ROSSB, XXV, 1*; *ROB, M N 73, VI, VII (1913)*.
131	ell,	*Helw Bull No. 9, II, 1 (1912)*.
134	spir.	*Helw Bull No. 9, II, 1 (1912)*.
150	barr, sp.?	*Helw Bull No. 9, II, 2 (1912)*.
151	spir.	Helw Bull No. 22, III (1921).
169	edgow, sp.	Lick Publ 13, p. 54, III, 20.
205	spir.	Ap J 46, p. 25, IX, a (1917).
221	oll,	Ap J 64, p. 324, XIV (1926).
224	spir,	ROB II, X (1894); Yerkes Publ 2, XXIV (1903); Lick Publ
(Andr.)	opari	8, I; 13, p. 54, VI, 76, 77, 78; Ap J 69, p. 158, I-VI, the
(		best direct, and also with novae and variables. Spectrum,
		Wolf, Szber Heidelb Akad Abh 27 (1910), 8.
246	plan,	ROB II, XVIII (1898); *M N 74, p. 712, XX (1914)*; *Helw
0	piun,	Bull No. 9, II (1912)*; Llck Publ 13, p. 58, VIII, 2.
247	spir.?	*Helw Bull No. 9, II, 4 (1912)*; *ROB, M N 75, p. 191, XV
-17	l abit'i	(1915)*.
253	spir.	Lick Publ 8, II; *LAS I, 1*.
255	spir.	Publ ASP 43, p. 352 (1931).
274 5	diff.	*Helw Bull No. 9, II, 6 (1912)*.
278	spir.	Ap J 46, p. 25, IX, b (1917); *ROB, M N 72, p. 408, III (1912)*.
281	diff.	ROB II, XXII (1896).
300	spir.	Helw Bull No. 22, I. (1921); *ibid., No. 9, II, 5 (1912)*.
578	spir.	Helw Bull No. 22, III (1921).
598	spir.	*Rosse, XXVI; XXXVI, 5*; ROB II, X (1895); Yerkes Publ
390	apit.	2, XXV (1903); Lick Publ 8, III.
613	barr, sp.	Holw Bull No. 9, I (1912).
628	spir.	ROB II, XI (1893); Lick Publ 8, IV.
650-1	plan.	Lick Publ 8, V; 13, p. 58, VIII, 3.
678	edgew, sp.	*Lick Publ 13, p. 54, III, 19*.
693	spindle	*Rosse, XXV, 2*.
697	spir.	Lick Publ 13, p. 54, IV, 45.
770	1 7	*Rosse, XXXVIII, 12*.
821	spir.	*ROB, M N 74, p. 238, X, 4 (1914)*.
828	spir.	*Lick Publ 13, p. 54, IV, 33*.
891	edgew, ap,	ROB I, VIII (1891); FRANKS, M N 65, p. 160, VIII, 1 (1904);
		Lick Publ 8, VI; 13, III, 1.
908	spir.	FRANKS, M N 65, p. 228, VIII (1904).
936	barr. sp.	*Holw Bull No. 9, III, 7 (1912)*,
972	spir,	*Rosse, XXV, 3*; Ap J 46, p. 25, IX, c (1917); Lick Publ 13, p. 54, V, 66.
1012	spir.?	P. 54, V, 66. *Rosse, XXV, 4*,
1023		*Roser, XXV, 5*.
1023	spir.?	L Troom's Try 1 2"

Number	Ciass	Reference
1068	spir	*Roser, XXV, 6*, *LAS I, 2*, ROB I, A (1892), Lick Publ 8, VII, Ap J 46, p 25, IX, c, d (1917)
1084	spir	*J AS I, 3*
1087	spir	Helw Bull No 22, III (1921)
1007	barr sp	Helw Bull No 22, I, III (1921), M N 85, p 1018, XX
1097	our p	(1925)
1186	spii	Ap J 51, p 279, XIII, d (1920)
	part sb	Helw Bull No 22, IV (1921), *ibid, No 9, III, 8 (1912)*
1187		Spectra taken with RAYION lens and photograph of region
1270	apir	ın Ap J 71, p 354 (1930)
1273	spir J	Publ ASP 24, p 227 (1912), I ick Publ 13, p 13, I, 2,
1300	bari sp	Helw Bull No 22, IV (1921)
1309	spir diff ?	*Helw Bull No 9, III, 9 (1912)*
1316		*Helw Bull No 9, III, 10 (1912)*
1350	Spir	*Helw Bull No 9, HI, 11 (1912)*
1365	ban sp?	Ap J 51, p 279, XIII, c (1920)
1491	ban sp	ROB II, XX (1897), Ap J 2, p 350, XI (1895)
1499	diff	Ap J 46, p 25, VI, a (1917), Lick Publ 13, p 58, IX, 6a, *6
1501	plan	*Rossr, XXV, 7*, *ROB, M N 71, p 234, VIII, 1 (1914)*
1514	plan	Lick Publ 13, p 58, IX, 7
	dan see	Holy Bull No. 22 TV (4024)
1518	игър	Hely Bull No 22, IV (1921)
1530	barı sp	Lick Publ 13, p 43, I, 2, b
1531	cll	*Hely Bull No 9, III, 42 (1912)*
1532	edgew sp	*Helw Bull No 9, III, 12 (1912)*
1535	plan	*LAS, I, 4*, Ap J 46, p 25, VI, b (1917), M N 60, p 42
		(1900), Lick Publ 13, p 58, IX, 8a and *8*
1555	vai diff	*Prase, Ap J 45, p 89, I, 1, a (1917)*
1579	diff	*Rosse, XXV, 8*, Ap J 46, p 25, VIII, a (1917)
1714	plan	*Lick Publ 13, p 90, fig 7*
1722	plan	*Lick Publ 13, p 92, fig 9*
1743	plan ?	*Lick Publ 13, p 92, fig 10*
1763	diff	*Lick Publ 13, p 92, fig 11*
1788	diff	Helw Bull No 22, II (1921)
1792	spn	*Helw Bull No 9, IV, 13 (1912)*
1888	odgow sp	Lick Publ 13, p 54, IV, 29
1935	plan	*Lick Publ 13, p 94, fig 14*
1952	plan?	*LAS, I, 6*, ROB I, XIV (1892), 1bid, II, XXVI (1895
(Crab)		I ick Publ 8, IX, ibid, 13, p 58, X, 11
1976	diff	ROB I, XVI (1888), ibid, II, XXVI (1896), Lick Publ
(Orion)		fi and XI, Pop Astr 31, p 376, XXV (1923), Yerkes Pu
, ,		2 (inner), XXI, (whole) XXIII (1903) Radial velociti
		Lick Publ 13, p 98, XXVIII, 18, 19, Spectrum, ibid
		XXIV, 20, 21, 22, XLIII, 4, Great outer portions at
		'loop' (II 2118), WOLF, MN 65, p 303, XI (1903), Szh
		Heidelb Akad 1, p 23 (1902), M N 65, p 528 (1925), Ap
		65, p 136, II (1927) (best)
1977	drif	Lick Publ 8, XII, Ap J 57, p 138, VI (1923)
1980	diff	*Rossr, XXXVIII, 16*
2022	plan	*LAS, I, 8*, Ap J 46, p 25, VI, c (1917), *I 1ck Publ
		p 58, X, 12*
2024	dıff	Lick Publ 8, XIII, Ap J 53, p 392, XI, XII (1921)
2029	plan?	*Lick Publ 13, p 108, fig 23*
2068	aiff	Lick Publ 8, XIV
2070	diff	*Lick Publ 13, p 108, fig 24*
2077	plan ?	*Lick Publ 13, p 109, fig 25*
2079	plan	*Lick Publ 13, p 109, fig 26*
2080	plan	*Lick Publ 13, p 109, fig 25*
2086	plan (2)	*Lick Publ 13, p 110, fig 27*
2146	edgew sp	Lick Publ 13, p 54, III, 14, Ap J 51, p 279, XIII, f (192
2175	diff	Atlas, IX
$\frac{2173}{2237} - 9$		ROB II, XXVII (1899), Lack Publ 41, XXVI, XXVII
31 /	4	
2245	diff !	*Rosse, XXVII, 11* Ap J 51, p 279, XIV, b (1920)

15 197

Number	Chass	Roference
2261	var, diff,	*Rosse, XXXVII, 10*; Helw Bull No. 22, VII, VIII (1921) Pop Astr 26, p. 248, XI (1918); Hubble, Ap J 44, p. 192
2264	diff.	· (1910); 45, p. 352, LX (1917).
1	(1111,	Lick Publ 8, XV; A N 221, p. 376 (1924).
2288		
2289	2 (4)	
2290 }	spir. (5)	Ap J 51, p. 279, XIII, a (1920).
2291		
2294 J		
2316	3	*Rosse, XXVII, 12*.
2359	diff.	*LAS, II, 9*; Ap J 51, p. 279, XVI, 1 (1920).
2371-2	plan.	(1917); Lick Publ 13, p. 58, XI, 16.
2392	plan.	*J.AS I, 11*; Ap J 46, p. 25, VI, d (1917); Lick Publ 43 p. 58, XI, 17a and *17*; Spectra; ibid., 13, p. 112, XXX 28; XXXI, 29; 240, XLIII, 1; XLVII, 1.
2403	apir.	ROB II, XI; Ap J 46, p. 25, X, c (1917); Lick Publ 8, XVII
2438	plan.	ROB II, XVIII; Lick Publ 13, p. 58, XII, 18a, and *18*
2440	plan.	Lick Publ 13, p. 58, XII, 19a, and *19*.
2452	plan.	*Lick Publ 13, p. 58, XII, 20*.
2537	spir.	*Lick Publ 13, p. 43, II, 6.
2610	plan.	*Lick Publ 13, p. 58, XII, 21*.
2655	barr, sp.	\$12(1)3 34 35 84 35 020 35 5 (4041)\$
2681	spir,	*ROB M N 74, p. 238, X, 5 (1914)*.
	-	Ap J 46, p. 25, IX, f (1917).
2683	spir.	Lick Publ 8, XVIII; 13, p. 54, III, 24,
2782	barr, sp.	*ROB M N 74, p. 238, X, 6 (1914)*.
2787	barr. sp.	*ROB M N 74, p. 238, X, 8 (1914)*.
2830	barr, sp.	*ROB M N 74, p. 238, X, 7 (1914)*.
2835	apir.	Holw Bull No. 22, II (1921).
2841	spir.	LickPubl 8, XIX; 13, p. 54, IV, 40; Ap J 46, p. 25, X, a (1917) 64, p. 326, XIII (1926).
2859	spir.	Ap J 64, p. 326, XIII (1926); *ROB M N 74, p. 234, XIII 2 (1914)*.
2880	sbir.	*ROB M N 74, p. 238, X, 3 (1914)*.
2903	spir,	*Rosse, XXXVI, 3*; *LAS, II, 12*; ROB I, XXV (1893) Lick Publ 8, XX; 13, p. 54, V, 57.
2868	spir.	Lick Publ 13, p. 54, III, 16,
2976	spir.	ROB II, XI (1895); Ap J 46, p. 25, X, b (1917).
3003	irr. sp.	Lick Publ 13, p. 54, VI, 72,
3031	apir.	ROB I, XXVI (1899); Lick Publ 8, XXI.
3034	irr. sp.	ROB I, XXVI (1899); Llek Publ 13, p. 54, V, 68; Ap J 6, p. 324, XII.
3079	lrr. sp.	ROB II, XVII (1895); Lick Publ 13, p. 54, V, 67.
3115	oll.	Lick Publ 8, XXII; Ap J 46, p. 25, XI, a (1917); 57, p. 27 XX (1923); 64, p. 324, XII (1926).
3132	plan.	*LAS, III, 13*; *Lick Publ 13, p. 118, flg. 35*.
3169	spir.	Lick Publ 13, p. 54, IV, 39.
3184	spir.	*ROSER, XXVII, 13*; ROB I, XXVII (1893).
3190	7	*Rosse, XXVII, 14*.
3198	spir.	ROB II, XI (1898); Lick Publ 8, XXIII.
32267	apir.	Lick Publ 8, XXIV.
3242	plan.	*LAS, III, 14*; Lick Publ 8, XXV; *13, p. 58, XII, 22 Spectrum, ibid., 13, p. 120, XXII, 38.
3351	barr, sp.	*Rosse, XXXVIII, 15*; Lick Publ 13, p. 43, I, 2, c.
3367	barr. sp.	*ROB M N 76, p. 647, XIV (1916)*; Ap J 51, p. 279, XIII, (1920).
3368	apir.	Publ A S P 25, p. 111 (1913); Lick Publ 13, p. 54, V, 52.
3372	diff.	*Lick Publ 13, p. 121, fig. 39*.
3379	ell.	Ap J 64, p. 324, XIV (1926); 51, p. 279, XV, a (1920).
3384	spir.?	Λp J 51, p. 279, XV, a (1920).
3389	apir.	Lick Publ 13, p. 54, V, 59; Ap J 51, p. 279, XV, u (1920
33956.	spir.	*Rosse, XXVII, 15*; Ap J 51, p. 279, XVI a (1920).
3404	edgew. ap.	Lick Publ 13, p. 54, V, 52.

Number	Class	Reference
3423	spir	ROB II, XII (1898)
3434	spn	*Rossr, XXXVIII, 13*
3556	spir	ROB II, XVII (1895), Lick Publ 8, XXVI, 13, p 54, III, 2
		*Dorar VVVVII (1* DOD II VIV (1000) T. 1. Tuble
3587	pian	*Rossi, XXXVII, 11*, ROB II, XIX (1895), Lick Publ
(Owl)		XXVII, 13, p 58, XIII, 23
3593	spir	Ap J 46, p 25, XI, b (1917)
3607	spir	*Lick Publ 13, p 54, IV, 34*
3621	spu	*Helw Bull No 9, IV, 18 (1912)*
3623	sbr.	*Rossr, XXXVII, 7*, *LAS, III, 15*, ROB II, XII (1898) Lick Publ 8, XXVIII, 13, p 54, III, 23,
3627	spir	*Rossf, XXVII, 16*, ROB II, XII (1898), Lick Publ (XXIX)
3628	edgew sp	ROB II, XX (1891), FRANKS, M N 65, p 180, VII, 4 (1904) Lick Publ 43, p 58, III, 8
3631	abit	ROB II, XII (1896)
3675	spir	Lick Publ 13, p 58, IV, 43
3718	edgew sp	Luck Dubl 12 o t0 TII 42
		Lick Publ 13, p 58, III, 13
3726	spir	ROB II, XIII (1898), Lick Publ 8, XXX
3786	spir (2)	An T 51, n 270 XIII h (4020)
3788∫	Free (m)	Ap J 51, p 279, XIII, b (1920)
3953	edgew sp?	*Rossc, XXVII, 17*
4013	edgew sp	Lick Publ 13, p 58, III, 2
		*Donn VVIII 10* A. T. c 100 3777 (1000)
4038-9	11.r	*Rossn, XXVII, 19*, Ap J 57, p 138, VII (1923)
4051	abn [	*ROSSE, AXVII, 19*, ROB II, XIII (1897)
4088	barı sp	ROB II, XIII (1896)
4151	7	*Rosse, XXVII, 20*
4156	spir ?	*Rossn, XXVII, 20*
4192	-	
	spir	Tick Publ 13, p 58, IV, 44
4206	cqdew sb	Lick Publ 13, p 58, V, 50
4212	Spir :	Lick Publ 13, p 58, V, 58
4214	nrsp	Ap J 64, p 328, XIV (1926)
4216	spn "	Ap J 46, p 25, XI, ■ (1917), Lick Publ 13, p 58, IV, 4
4220	spir	Lick Publ 13, p 58, IV, 48
4244	~_ 1	
4254	sbir	ROB II, XX (1897), Lick Publ 8, XXXI, 13, p 58, III, 1: *Rossr, end, XXXV, 2*, *LAS, IV, 46*, ROB II, XII (1896), Lick Publ 8, XXXII
4258	spir	Lick Publ 8, XXXIII, 13, p 58, V, 64
4266	edgew sp	Table Dubil 12 - 50 W 54
		Lick Publ 13, p 58, V, 51
4274	sbir	Lick Publ 13, p 58, V, 61
4282	edgow ap	*Lick Publ 13, p 58, III, 18*
4292	spir	*Rosse, XXVII, 21*
4303	spir	Lick Publ 8, XXXIV
4312	apır	*Lick Publ 13, p 58, IV, 32*
4321	spir	*LAS, III, 17*, Lick Publ 8, XXXV
1 1		
4361	plan	*Lick Publ 13, p 58, XIII, 24*, Helw Bull No 22, V (1921
4388	edgow sp	Lick Publ 13, p 58, III, 15
4389	edgew sp	*Rosse, XXVII, 22*
395-4401	spir	Ap J 51, p 279, XV, b (1920)
4402	edgew ap	Lick Publ 13, p 58, III, 11
4414	abit.	Lick Publ 13, p 58, VI, 70
		Link Dukl 42 m re TV 20
4429	spir	Lack Publ 13, p 58, IV, 38
4449	m sp	Ap J 46, p 25, VIII, b (1917), 64, p 324, XII (1926)
4476	ř	*LAS, IV, 18*
4477	7	*LAS, IV, 19*
448590	spir	*Rosse, XXVII, 23*
4486	ell	Ap J 56, p 166, III (1922), 57, p 276, XX (1923)
		Tack Dubl 42 to 50 VI at
	irr sp	Lick Publ 43, p 58, VI, 75
4490	spir.	*LAS, IV, 20*, Lick Publ 8, XXXVII
4501		
	edgew sp	Lick Publ 13, p 58, III, 9
4501		Lick Publ 13, p 58, III, 9
4501 4517 4526	edgew sp ell	Lick Publ 13, p 58, III, 9 Lick Publ 13, p 58, III, 7
4501 4517	edgew sp	Lick Publ 13, p 58, III, 9

Number	Clean	Reference
4559	spir	POR II VIV (1904) The Date of
4565	odgow an	ROB II, XIV (1894), Llok Publ 8, XXXIX  *LAS, V, 21*, ROB II, XX (1896), Llok Publ 8, XL, 13,
TOUT	erigon up	THE TI 4 An I for a cut TY (1990) MAY (1990)
		p 58, III, 4, Ap J 57, p 275, XX (1923), M N 65, p 180, VII, 2 (1904)
4567 — 8	apir (2)	Λp J 46, p 25, XI, d (1917)
4594	edgow sp	Ар J 46, p. 25, XI, с (1917) (bost), *LAS, V, 22*, ROB П,
		XX (1897), FRANKS, MN 65, p. 180, VII, 3 (1904),
		Lick Publ 13, p 58, III, 6, Ap J 64, p. 326, XIII (1926)
4618	spir ?	*ROSEE, XXVIII, 25*
4621	oti	*LAS V, 23*, Ap J 64, p 324, XII (1926)
4631	qs wagbe	*Roses, XXXVII, 9*, ROB II, XVIII (1894), Lick Publ II.
		XLI, 13, p 58, III, 22, REYNOLDS, M N 85, p. 1018, XXI
		(1925)
4634	odgow sp ?	*LAS V, 24*
4647	abir _	Ap J 56, p. 166, III (1922),
4649	वीL	Ap J 56, p. 166, III (1922)
<del>4</del> 656—7	aptr	*ROSSE, XXVIII, 26*, ROB II, XVIII (1894), Ap J 51,
		p. 279. XVI. 2 (4920)
4666	spir	Lick Publ 13, p. 58, IV, 47
4710	ell	Lick Publ 13, p. 58, IV, 47  *Rosas, XXVIII, 27*, Lick Publ 13, p. 58, IV, 28  ROM II, XIV (4804) Lick Publ 8, XIII
4725	spir	
4736	agár.	Ap J 46, p 25, XII (1917) (best), *LAS, V, 25*, ROB I,
150		XXVIII (1932), Lick Publ 8, XLIV
4781	apir	Holw Bull No 22, V (1921)
4826	BDIL	*LAS, VI, 26*, ROB II, XV (1896), Lick Publ 8, XLV, 13,
1000		p. 58, V, 54. ROB II, XIX (1894)
4900	aptr?	I KOD II, AIA (1894)
5005	apir	Lick Publ 43, p. 58, TV, 37
5033 5055	apir spir,	Lick Publ 13, p 58, IV, 36.  ROB II, XV (1896), Lick Publ 8, XLVI, 13, p 58, V, 56
5112	Spir ?	*Rosas, XXVIII, 28*
5128	gier,	Holw Bull No 22, V (1921).
5189	plan.?	*Lick Publ 13, p. 124, fig 45*
51945	apir,	*LAS, VI, 27*; *Roses, XXXV, 1*, ROB I, XXX (1889),
	-1	II, XV (1898), Yerkes Publ 2, XXIX (1903), Pop Astr 31,
		p. 374, XXIV (1923), Lick Publ 8, XLVII, 13, p 58, VI, 74
5236	apir	*LAS, VII, 28*; *Holw Bull No 9, IV, 17 (1912)*, REYNOLDS,
	l -	M N 85, p. 1018, XXI (1925), Lick Publ 13, p. 43, II, 7
5247	ephr.	*LAS, VII, 29*, Helw Bull No 9, I, *IV, 19* (1912)
<u> 5257 — 8</u>	aprir (2)	Ap J 51, p. 279, XVII, b (1919)
5278-9	spir	Ap J 51, p. 279, XVII, a (1919)
5378	oll.?	*Rosss, XXVIII, 30*
5383	barr sp.	Ap J 46, p 25, XIV, a, b (1917)
5394 - 5	erár	Idek Publ 43, p. 58, VI, 73
5427	apir	Holw Bull No 22, V (1921)  *Rosss, XXIX*; ROB I, XXXII (1892), Ap J 14, p. 34,
5457—8	abar.	II, 2 (1901), Lick Publ 8, KLIX, Pop Astr 27, p 496,
		XLII (1919), Ap J 64, p 326, XIII (1926)
5506	spir	*Lick Publ 13, p 58, IV, 31*
5529	edgow sp	Lick Publ 13, p. 58, IV, 25
5544-5	apir. (2)	Ap J 46, p. 25, XIII, a (1917), 51, p 279, XVIII, b (1920)
5746	edgow sp	Ap J 46, p. 25, XIII, d (1917), Lick Publ 13, p 58, III, 7.
5850	perr sp	M N 85, p 1018, XXI (1925), Ap J 64, p. 326, XIII (1926.)
5857-9	apdr	Lick Publ 8, L; *Roses, XXVIII, 31*
5866	odgew sp	*Rossa, XXXVII, 6*, Link Publ 8, LI, 13, p. 58, III, 5,
	-	Ap J 46, p. 25, XIII, a (1917).
5907	odgew sp	Lick Publ 13, p. 58, III, 10.
5921	barr, sp.	Publ ASP 24, p. 227 (1912), Link Publ 13, p. 43, I, 2, d.
3981	edgew. sp.	Lick Publ 13, p. 58, IV, 25.
6058	plan.	*Roses, XXVIII, 32*; *Lick Publ 13, p 58, XIII, 26.
6070	aptr	Ap J 46, p. 25, XIV, a (1917)
6205	dff.7	*Rosse, XXVIII, 33*
6210	blan	*Llak Publ 13, p 58, XIV, 28*; Spectrum, ibid., XXXIII, 52.

Number	Class	Reference
6302	plan ?	*Helw Bull No 9, IV, 14 (1912)*
6309	plan	Ap J 46, p 25, VII, a (1917), *Lick Publ 13, p 58, XIV, 30
6337	plan	*LAS, VII, 30*, Helw Bull No 22, VI (1921)
6369	plan (	*Lick Publ 13, p 58, XIV, 31*
6439	plan	*Lick Publ 13, p 58, XIV, 32*
	plan	Lick Publ 13, p 58, XV, 33a, and *33?
6445		
6482	3	*LAS, VII, 31*
6503	spir	Lack Publ 13, VI, 71
6514	diff	*LAS, VIII, 32*, Lick Publ 8, LV, Pop Asti 27, p 404, X
(Trifid)	7.00	(1919), Ap J 57, p 143, IX (1923)
6523	diff	Ap J 51, p 5, III (1920) (best), Lick Publ 8, LVI, 11, I I 13, p 58, VII, 81, Atlas XXX
6537	plan	*Lack Publ 13, p 58, XV, 35*
		Ap J 46, p 25, VII, b (1917) (best), Lick Publ 8, LVII, *1
6543	<b>P</b> lan	
		p 58, XV, 34*, Spectrum, ibid, 138, XXXIV, 53, 24
		XLIII, 2, XLIX, 1, 2, 3, Lick Bull 15, p 95, III, m (1930
Gree	Ciotie	
6555	spir	Ap J 46, p 25, XIV, b (1917)
6563	blan	*Lick Publ 13, p 58, XV, 36*
6565	plan	*Lick Publ 13, p 58, XV, 37*
6567	plan	*Lick Publ 13, p 58, XVI, 39*
		Tion 1 (1), p 30, 1211, 39
6572	plan	*Lick Publ 43, p 58, XVI, 38, Spectrum, ibid, 138, XXXI
		54; 240, XIJII, 3, XLVII, 3, Lick Bull 15, p 95, I
		d, e, f (1930)
1 400 2620	mlan	The The Land of the State of th
+30°3639	plan	Lick Publ 13, p 240, XLIV, 1, 2, L, 2 (spectrum only)
6578	plan	*Lick Publ 13, p 58, XVI, 40*
6393	diff	Holw Bull No 9, I (1912)
6611	diff	POR II XXIII /1905 An I 61 m 7 TV /4030)
		ROB II, XXIII (1897), Ap J 51, p 7, IV (1920)
6618	diff	*LAS, VII, 33*, ROB I, XXXVIII (1893), Lick Publ
		I.VIII, Ap J 51, p 9, V (1920)
6620	plan	*Lick Publ 13, p 58, XVI, 41*
		1 1 1 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
6629	plan	*Lick Publ 13, p 58, XVI, 42*
6644	plan	Lick Publ 43, p 58, XVII, 43
6690	spir .	Lick Publ 13, p 58, IV, 35
6720		
A Seedle St.	l ไวโซม	ROB I, XLI (1891), II, XIX (1898), Lick Publ 8, LI
(Ring)	1	13, p 58, XVII, 46a, and *46*, Spectrum, ibid, 14
	)	XXXV, 55, 146, XXXVI, 56, 240, XLII, 4, XLVIII,
6729	van diff	KNOY-SHAW, M N 76, p 646, XIII (1916), Helw Bull No :
0/29	A res Cives	
	,	I, II, III (1920)
6741	plan	*Lick Publ 13, p 58, XVII, 47*
6751	plan	*Lick Publ 13, p 58, XVIII, 48*
	i	
6772	plan	*Lick Publ 43, p 58, XVIII, 49*
6778	plan	*Lick Publ 13, p 58, XVIII, 51*
6781	plan	*LAS, IX, 34*, *Lack Publ 13, p 58, XVIII, 52*
6790	plan	Lick Publ 43, p 58, XIX, 53
6803	plan	*Lick Publ 43, p 58, XIX, 54*
6804	plan	Lack Publ 13, p 58, XIX, 55a, and *55*
6807	plan	Lick Publ 13, p 58, XIX, 56
6818	) ^ _	
0040	plan	*Lick Publ 13, XIX, 57*, Spectrum, ibid, 146, XXXVI,
		240, XLVIII, 1, Ap J 46, p 25, VII, c (1917)
6822	Mag type	Ap J 52, p 408, XIV (1925)
6826	plan	*Lick Publ 13, p 58, XX, 58*, Spectrum, ibid , 158, XXXV
0010	Private	
		58, 240, L, 1
6833	plan	Lick Publ 43, p 58, XX, 59
6853	plan	*ROSSE, XXXVIII, 17*, XXXI*, ROB I, XLIV (188
	Transit	Tiol-Dubl C TV 42 a 20 VV CA
		Lick Publ 8, LX, 13, p 58, XX, 60
6879	plan	*Lick Publ 13, p 58, XX, 61*
6881	plan	*Lick Publ 13, p 58, XXI, 62*
6884		*Link Dubl 42 m cg VVI 42*
	plan	*Lick Publ 13, p 58, XXI, 63*
6886	plan	*Lick Publ 13, p 58, XXI, 64*
6888	diff	ROB II, XXI (1897); Ap J 51, p 279, XVIII, c (1920)
6891	plan	*Lick Publ 13, p 58, XXI, 65*
		HOD TO STITE (1001) Tall TO SIA TOTAL
6894	plan	ROB II, XIX (1897), Lick Publ 8, LXI, *13, p. 58, XXI, 6
6905	plan	*Rosse, XXVIII, 34*; *LAS, IX, 36*.

Number	Class	Belizence
6907	рагт вр	*Helw Bull No 9, IV, 15 (1912)*
6925	spir	*Holw Bull No 9, IV, 16 (1912)*
6928	ирlт	Lick Puhl 13, p. 54, IV, 27
6946	spir	*ROSSE, XXX, 36*, ROB II, XV (1896), Lick Publ 8, LXII
6960	din	ROB I, XLV (1891), Pop Astr 10, II 392, XIV (1902), Yerkes Publ 2, XXVII (1903), Lick Publ 11, LXXIX,
6992	diff	LXXX, Ap J 57, p 146, XIII (1923) ROB II, XXI (1896), Publ A S P, fr, 16 (1904), Yorkes Publ
(Notw'k)	,,,,	2, XXVIII (1903)
6995	ditt	Lick Publ N, LXIII, 11, LXXIX, LXXX
7000 (Amer )		Work, Publ Heldalb 1, fr Atlas, XLVI (best for full extension), ROB II, XXIV (1896), M N 63, p 32, II (1903), Lick Publ 11, LXXVII, LXXVIII, Ap j 57, p 147, XIV—XVI (1923).
7008	plan	*ROSSE, XXX, 37*, ROB I, XLVI (1892), Ap J 46, p 25, VII, v (1917), Lick Publ 13, p 58, XXII, 69
7009	plan	*Rosam, XXXVIII, 15*, *LAS, X, 37*, Ap J 46, p 25, VII, o (1917), Lick Publ R, LXIV, *13, p 58, XXII, 70*, Spectrum, lbid, 148, XXXVII, 59, 240, XLII, 3, XI, VIII, 4, 5, Lick Bull 15, p 95, III, h (1930)
7023	qift	Worr, M N 68, p 30, IV, 1, 2 (1907), ROB II, XXIV (1898), Lick Publ 8, LXV
7026	plan	*Lick Publ 13, p 58, XXII, 71*, Spectrum, ibid, 158, XXXVII, 60, 61, 240, XLVII, 2
7027	nakq	*I.lek Publ 13, p 58, XXIII, 72*, Spectrum, lbld, 160, XXXVIII, 62, XXXIX, 65, a, b, c, 240, XIII, 1, XLVI, 1, 2
7129	aucr i	ROB II, IX (1895)
7139	plan	*Lick Publ 13, p 58, XXIII, 74*
7177	őll	*Rosse, XXX, 38*
7184	apir	Lick Publ 13, p. 54, V, 53
7217	apir	Lick Publ 8, LXVI, Ap J 46, p 25, XIV, = (1917)
7293	plan	Publ A S P 24, p 211 (1912), Helw Bull No 9, I (1912), Lick Publ 13, p 58, XXIV, 76
7309	upir	Helw Bull No 22, VI (1921)
7331	spir	*Rossa, XXX, 39*, Lick Publ 8, LXVII, 13, p 58, IV, 42
735 <del>4</del>	plan	*Llok Publ 13, p 58, XXIV, 77*
7418	spir	Helw Bull No 9, IV, 20 (1912)*
7421	apir	*Holw Bull No 9, IV, 20 (1912)*
7457	нріг	Publ ASP 25, p 111 (1913)
7479	spir	*Rosan, XXXVI, 4*, ROB I, L (1892), Lick Publ 8, LXVIII, Ap J 64, p. 326, XIII (1926)
7537	spir	Lick Publ 13, p 54, V, 55
7640	apir	Lick Publ 13, p 54, V, 65
7662	plas	*Rosse, XXX, 40*, *I.AS, X, 38*, I.I.k Publ 8, I.X1 Ap J 46, p 25, VII, f (1917), *I.Ick Publ 13, p 58, XXIV, 78*, Spectrum, Ibid, 164, XL, 64, 240, XI.II, 2, XI.VI, 3, 4, 5
7678	apir	*Rosse, XXX, 41*
7814	odgow sp	*Rosex, XXX, 42*, ROB I, LHI (1891), Lick Publ S, LXX, 13, p 54, III, 3
7817	spir	Lick Publ 13, p 54, IV, 49
		First Indox Catalogue
I 59	diff.	ROB II, XXV (1895), Lick Publ 13, p 43, II, 4
I 351	plan	*Lick Publ 13, p 58, IX, 5*
I 405	gitt	Knowl 26, p. 81 (1903), Strius 38, p 288, XIII (1906)
I 418	plan	*Lick Publ 13, p 58, X, 10*, Spectrum, ibid , 240, XLIX, 4
I 434	diii +dark	I 431, 433, 434, near & Orlonin, ROB M N 63, p 32, I (1902), Ap J 53, p 392, XI (1921), Lick Publ 13, p. 42, II, 5, Harv Ann 32, III, 3 (1895), Ap J 38, p 500, XX, 1 (1913)
I 1029 I 1470	spir diff	*Lick Publ 13, p 54, IV, 30* Ap J 51, p 279, XVIII, a (1920)

\umber   Class	Reference
II 1747	Second Index Catalogue  *Lick Publ 13, p 58 VIII 1*  *Jick Publ 13 p 92 fig 12*  Sec 1976 Onon  *Lick Publ 13 p 58 XI 11*  Lick Publ 13 p 58 XI 11*  Lick Publ 13 p 58 V 60  *Lick Publ 13, p 58, XIII, 25*  *Iick Publ 13, p 58, XIII 27*  *Lick Publ 13, p 58 XII 27*  *Lick Publ 13, p 58, XIV 29*  Lick Publ 13, p 58 XVII, 11  *Tick Publ 13, p 58 XVII, 11  *Tick Publ 13, p 58, XVIII 50  Lick Publ 13, p 58, XXIII 70  Lick Publ 13, p 58, XXIII 73  Lick Publ 13, p 58, XXIII 73  Lick Publ 13, p 58, XXIII 75  *Lick Publ 13, p 58, XXIII 75*
JONCKHELRI  320 plan  JONCKHERRE  900 plan  249 galaxies at 12h 55m + 28°30'  Cluster of galaxies in Ursa  Maj (Bande)  Christies Cluster in I eo  Large Magellanic Cloud	*Lick Publ 13, p 58 IX, 9*  *Lick Publ 13, p 58 XI, 15*  Lick Publ 13, p 13 I, 3  A N 233 p 71, II (1928)  Publ A S P 13, p 350 (1931)  Harv Ann 20, cud, IV, 2 (1891), 60 p 108 II (1908), Mem  R A S 60, p 144 V (1903), Harv Bull No 881, II (1931)
Small Magellanic Cloud	Huy Ann 26, end, IV (1891), 60, p 108, I (1908)

The largest of the diffuse nebulae are best seen in plates taken with instruments of shorter focus. Many such, frequently combining luminous and dark nebulosity, can be found in BARNARD'S Atlas, passim. Others are

Very large diffuse neb in luriga About η Carinae

Detached diff neb m Cygnus Near y Cygni

Very large, near w Eridam
Diff, in Monoceros
Bright and dark neb near
g Ophnichi
Very large diffuse near
£ Persei
Large diff + dark near
o Persei
Pleiades diffuse neb

Outer nebulosity of Pleiades

Very large diff near i Scorpu Verv large diff near i Scorpu Several diff neb in Vela Preceding 7000 Enormous diff in Taurus and Perseus 'Cave' neb in Cepheus

```
Near I 405 Wort, M N 63, p 506 && (1903)
Harv Ann 26, end, V, I, 2 3, VII 2 (1891) 60 p 229, IV (1908) (best), Mem R A 5 60, p 111, VI (1910)
```

FRANKS M N 65 p 158, VI (1901)
Lick Publ 11, I XXVI, Ap J 63, p 121, VIII, 126, IX (1926),
Atlas XLIV, ROB II, XXIII (1895)
WOLF, M N 65, p 528 AV (1905)
Lick Publ 8 XVI

Atlas, XIII, Lick Publ 41 XXXVI

Lick Publ 11, XVI, XVII

Atlas III

Lick Publ 8, IX, Yerkes Publ 2, XXVI (1963), ROB 1, XI (1888), II, XXV (1897)

BARNARD, MIN 60 p 258 IX, X (1900), Ross, Ap J 64, p 294, VIII (1928), lick Publ 11 XV

Atlas, XII

Atlas, XI

Millotte, MIN 86, p 636 XV (1926)

MELOITE, M.N. 86, p. 636 A.V. (1926) Ap.J. 63 p. 122 VII. (1926) Ross, Ap.J. 67, p. 280, VI. (1928)

Ross, Ap J 67, p 292, VII (1928) Worr, M N 69, p 117 VI (1908)

### Dark Nebulae

Most of the dark nebulae which BARNARD has catalogued will be found noted in the descriptive matter accompanying the plates of his Atlas, without doubt the most wonderful Milky Way photographs which have ever been made Some of the smaller spots which have been observed with instruments of greater focal length are given below

BARKARD No	m (875,0	å 1875,0	Reference
13	5h 74m,6	- 2° 32′	Ap J 53, p 392, VI (1921), Lick Publ 13, p 43,
63	17 0	21 20	Ap J 49 p to, 111, a (1919)
(14	17 10	-18 21	Ap J 49, p 10, IV, d (1919)
72	17 l6 l	- <b>23 3</b> 0	Ap J 49, p 10, III, b (1919), 57, p 143, VIII (1923)
75	17 18 1	-21 55	Ap J 49, p 8, II, b (1918)
84 :	17 39	20 12	Ap J 49, p 8, II, a (1919)
86	17 55	-27 52	Lick Publ 13, p. 54 VII, 80, Ap J 63, p. 122,   VI (1926)
92-93	18 9	~18 10	Ap ] 57, p 143, X, XI (1923)
98	18 25	- <b>2</b> 6 9	Ap ] 49. p 10, IV, c (1919)
127	18 55	- 5 17	Ap [ 49, p. 10, IV, a. (1919)
129	18 55	- 5 29	Ap ] 49, p 10, IV, a (1919)
133	19 00	- 7 5	Ap j 57, p. 144, XII (1923), 49, p 10, IV, b (1919)

## Appendix No. 7

### Abridged Nebular Bibliographical Apparatus

### 1 Lists of Nebulae Vinual Micrometric Positions.

W HERRITER, Scientific Papers of, published by the Royal Society and the Royal Astronomical Society, London (1912), 2 vols. Collects his papers scattered in the Phil Trans and other media 2500 entries, J HERECHEL, General Catalogue of Nebulae, Phil Trans (1864) 5079 ontiles, Rosss, Phil 7 mas (1853) and (1861), observations assembled in Trans Roy Dublin Sec 2 (1880), now most easily accordible in his Collected Scientific Papers, London (1926), LABRELI, MARTH'S CHEARING OF 600 objects found at Malta, Mem RAS 36 (1866), D'ARREST, Siderum nobulosorum observationes Havniouses Copenhagen (1867) 1942 entries. Micrometer, RUMKER, A N 63 to 68, New 1508, 1531, 1566, 1599, 1631 (1863 to 1866) Ring micromoter 135 objects, Schöner D. Astr Boob Mannholm 1, 2 (1862-1875) Ring micrometer 489 ob-Joets, Schul Tz, Nov Acta Reg Upr D (1874) Micrometer 500 objects, General catalogue of nebulae observed at Strassburg, by various observers, 1881 to 1910, Ann Sternw Strassb 4, 1257 NGC objects Micrometer, Winnecks, Bearbeltot von E Becker, Ann Sternw Stramb 3, p 1 (1909) Micromotor 406 NGC objects, Wirtz, Boobachtung von Nobelflecken, nungeführt in den Jahren 1880-1902, von H Kobold, A WINNECKE und W Schurt Micrometer 619 objects Ann Sternw Strassb 3, JAVELLE, Catalogue de nobulcuses, Ann Nico 4 (1895), 6 (1897), 11 (1908) Micromoter 1469 objects, Bigourdan, Ann Paris (1884ff.) I hour in a per volume Since published by Cauthler-Villars. Micrometer Bidoux-DAN sot out to observe every NGC object visible from the latitude of Paris, STEPHAN, Muny references in periodical literature, collected in the introduction to the NGC, p. 9, DREYER, A New General Catalogue of Nebulae and Clusters of Stars, being the Catalogue of the late Sir John 1. W. Herschel, rovised, corrected, and enlarged. Mem R A S Lond 49, p 1 (1888) lucludes all results known to the end of 1887 7840 entries + 88 objects found by Swift The Introduction contains references to the work of all earlier investigators. See also WIRTS' comparisons in Ann Stornw Strassh 4, Index Catalogue of Nebulae found in the Years 1888 to 1894, with Notes and Corrections to the New General Catalogue Mem R A S Lond 51, p 185 (1895) 1529 entries, Second Index Catalogue of Nobulae and Clusters of Stars, containing these found in the years 1895 to 1897, etc. Mom R A S Lond 59 (1908) 3857 entries, continuing from First Index Catalogue to No 5386, here, for the first time, photography bogins to overwhelm the cataloguer, of the 2800 Worr nebulae known at that time, the 1500 in the the future great catalogues of nebulae will certainly have to be third list are emitted 🦈 arranged in zones of one degree " Anwars, Verzeichnis der Orter von vierzig Nebelijecken AN 58, p 369 (1862) Hollomotor 40 objects, ROMER, Beobachtungen von Arkumpolar Nebeln

1

ı

auf der Hamburger Steinwarte. A. N. 63, p. 305 (1865). 64, p. 289 (1865). 66, p. 81 (1866). 67, p. 225 (1866). 68, p. 353 (1867). 437 entries. Ring milliometer. Vogi I., Beobachtungen von Nebelflecken. Leipzig (1867). Micrometer. 100 objects. Publ. Leipzig (1. p. 3. (1882). Micrometer. 132 nebulae. Engethann, Mehdian-Beobachtungen von Nebelflecken. A. N. (63, p. 193 (1883). Mehdan einele. 124 nebulae. Klamt, Publ. Astroph. Potsdam 7. p. 115 (1892). Micrometer. 82 objects. Porti R., Publ. Cine. 11. (1891). Micrometer. 105 nebulae. D'Encit. Hardt, Observations estionomiques failes a Diesde. 3, p. 96 (1895). Micrometer. 590 nebulae, Biecki R., Ann. Obs. I. dinb. 1, p. 1. (1902). 217 objects. Mehdan einele. Monniehmi yle. Veröft Steinw. Bonn. 1. (1895). Ring micrometer. 236 objects. Spitali R., A. N. 132, p. 369 (1893). Ring micrometer. 136 entites, Mlri eki, Observations micrometriques de in buleuses, I., Wusaw. (1903). 72 objects. Micrometer, Hagi N., A. preputatory catalogue for a Durch mustering of nebulae. The zone catalogue. Spec. Vat. 10. (1922—1927). I. Biecki R. A. preputatory catalogue for a Durch mustering of nebulae. The general catalogue. Spec. Vat. 13. (1928). About. 4100 entities, 4,705 with designation st. (stellar), and 700 unconfirmed objects.

#### 2 Lists of Nebulae Photographic

```
Wort (and colleagues) Königstuhl Nebel-Listen Publ Heidelb (Konigstuhl)
List No 1
              i, p 11
                       (1902)
                                151 entires
                                              List No 9, 3, p 149 (1909)
                                                                                102 entrics
                                                    No 10, 6 p 1 (1909)
No 11, 6, No 2 (1909)
     No 2,
              1, p 17
                        (1902)
                                301
                                                                                62
     No 3,
              i, p 125 (1902) 1528
                                                                                 91
                                                                                       11
                                                                    3 (1911)
     No 4
             2 p 57
                                                     No 12, 6, No
                        (1904)
                                272
                                                                               279
                                        12
                                                     No 13 6, No 8 (1912)
No 11 6 No 10 (1913)
     No 5
              2, p 77
                        (1904)
                                 239
                                                                               111
     No 6
              2, p 89
                        (1905)
                                 204
                                                                                511
     No 7,
                                                     No 15, 7, No 7 (1916)
              3 p 77
                        (1907)
                                 310
                                                                                189
                                        21
     No 8
                                                     No 16, 8, No 11 (1928)
              3, p 87
                        (1908)
                                 770
                                                                               678
```

Worr and Kaiser, Positionsbestimming von 124 Nebelficeken im Perseus-Nebelhaufen Publ Heidelb 6, No 11 (1913), Jorenz, Positionsbestimming von 178 Nebelflecken Publ Heidelb 6 No 3 (1911) Nearly all NGC objects Reinmurii, Photographische Positionsbestimming von Nebelflecken (Winnocke-Nebel) Publ Heidelb 8 No 2 (1927) 321 entires, 111 photographische Nebelpositionen, ibid 7, No 8 (1916) 111 objects, mostly new, ibid 8, No 14 (1929) 351 entries, Photographische Positionsbestimmung von 356 Schultzschen Nebelflecken ibid 7 No 6 (1916) 356 entries, all NGC, Photographische Positionsbestimmung von Nebelflecken in Virgo, ibid 8, No 7 (1927) 331 entries, ibid 8 No 11 (1928) 317 entries, mostly new Die Heischel-Nebel nach Aufnahmen der Königstuhl-Steinwarte, Heidelb 9 (1926) This work contains 6251 NGC objects and is the largest single photographic nebular catalogue in existence. It assembles all the previous Königstuhl work by Wirtz, Rilingutir, and others. It gives a, b, L, B, the diameters along major and minor axes and brief description, Pr Asc, Photographs of achulae with the 60 meh reflector, 1917—1919, Ap J 51, p 276 (1920) Descriptions of 330 objects, Curits, Descriptions of 762 Nebulae and Clusters photographed with the Crossley Reflector Lick Publ 13 KNOX-SHAW, Hely Bull No 9, p 69 (1912) 112 NGC and 48 new, ibid No 15, p 129 (1915) ca 195 NGC and 31 new, ibid No 30, p 71 (1924) 70 entries GRI GORY, Helw Bull No 21, p 201 (1921) 168 NGC, 177 new, ibid No 22, p 219 (1921) 183 NGC 60 new, Balli v Nebulae discovered at the Haivard College Observatory Harv Ann 60, p 147 (1908) 1238 new objects 1659 new nebulae, ibid 72, p 17 (1913), Smartly, Menzel, and Campbell, Descrip tions and positions of 2829 new nebulae Harv Ann 85 p 113 (1924), Mi Nzi i, Harv Bull No 773 ca 2000 new objects, mostly south of -45°, Hubbit, Extra galactic nebulac Ap J 64, p 321 (1926) Classifies 400 objects of the spiral type, Duncan, Photographic studies of nebulae Ap J 51, p 4 (1920), 53 p 392 (1921) 57, p 137 (1923), Killia, 744 nebulae (small) discovered on the plates of the Crossley program Lick Publ 8, p 31 (1908), SH BLRNAGE, Positionsmessing von Nebelflecken A N 230, p 305, 441 (1927) 189 entires

References to other phenomena of the nebulae will be found in the separate sections.

## Appendix No 8

A lost of the Moissard Modification of the Doppier Formula in a Universe of the Charlier Type

The Morssard hypothesis (see ciph 78) requires that we take into account the absolute velocity of the observer's system through the medium, as well as the relative motion of source and observer in the line of sight. In applying this theory to the observed data, it does not seem at all essential that we hold to the word "absolute", for we know nothing

of our absolute speed in space, and apparently must remain forever ignorant of its direction and amount. We may think, however, of various frames of reference to which our motion is relative e.g., the motion of our galaxy within the frame of reference given by the totality of members of our particular chaster of galaxies. We may even continue the analysis and consider the motion of this cluster of galaxies with regard to a reference frame composed of other similar groups of galaxies. We shall accordingly use the phrase "botal motion" to describe such motions through various systems of reference, and thus avoid the anathema

Relatively to such reference frames, Morsaarp's modification of the customary Doppler formula, requires that the total motion of the observer be taken into account. Following Morsaarp, we may make the postulate on classical grounds and replace  $c/(c\pm s)$  in the usual formula for the Doppler shift by  $(s-n)/(c\pm s)$ , where s is the velocity of the source relative to the observer in the line of sight, and s the total motion of the observer's system through the modium. This is equivalent to the assumption that our total motion through car reference frame "speeds up" our own wave vibrations and standards, so that vibrations from far distant sources at rest, or moving more slowly within this frame at random, would seem to be slower than our own. An observer in a system moving more rapidly than the mean total motion of the other morehors of the system would than observe an apparent excess of positive velocities. That we happen to be situated in a system of higher velocity than the everage may be assumed to be but a happy accident, similar to that by which the universe has not expanded sufficiently to render the beautiful spirals invisible. Like abstration, this effect would apparently not act Im kleinen.

The very large scatter of our velocity data on the spirals, together with the limited number of velocities known, proclude any need for rigor in the treatment. Placing X, Y, and Z as the components of such a total motion, the assumed effect of the total motion will then be two-fold

! It will be assumed to act with its full value as expressing the amount by which the observed radial velocity of a distant object tends to appear more positive

 In addition to the above effect, the component of such a motion in the line of sight will be manifested as the customary Dopples effect.

Then the total effect to be removed from the velocities of distant sources will be

$$X(1 + \cos \alpha \cos \delta) + Y(1 + \sin \alpha \cos \delta) + Z(1 + \sin \delta) = V$$
.

where Y in the observed radial velocity of the source

The scheme of Morsaard, applied as above, may be regarded as of the nature of a "directed" K-term, placing discrepancies of excess upon our own galaxy, rather than upon ALL other galaxies

The automishing degree of similarity between the Charlier theory and data thus far observed has been noted above. Humason's brilliant work at Mt. Wilson has shown clearly the existence of clusters of galaxies, localized as to grouping, and with radial velocities nearly the same.

While such clusters of external galaxies are for the most part very definitely indicated, it is, as yet, considerably more difficult to select with certainty those spirals which may be assumed to be members of our own local cluster of galaxies. It was finally decided to segregate as members of our local cluster all objects with an observed velocity less than 2000 km /sec , while all objects with velocities  $2000 \, \mathrm{km}$  /sec. or greater were assumed to be members of other  $G_0$  systems. This selection may have introduced some error, though approximate tests of the available material in different ways indicated that any over-precise refinement or grouping of the limited data is superfluous. This process, in particular, allocates to our local group the 7 objects assigned by Humason to the Virgo cluster.

The procedure employed in the application of the Moranano formula was then as fol-

1 Using the formula given above, the total motion of our galaxy was first computed with reference to our assumed local reference frame, or  $G_{a}$ , composed of 56 objects

2. The 34 remaining objects, belonging to well determined clusters of spirals, or "boluted" objects of high velocity, were formed into 13 groups, on the assumption that they represented other  $G_0$  systems in a Charler universe. The effect of the total motion of our own galaxy having been first removed, a second solution was made for the total motion if our local system of galaxies within the reference frame formed by the 13 other  $G_0$  systems. The locations of these are plotted in Figure 58.

The results of the two least square solutions are as follows

1 Total motion of our Galaxy within its local reference frame of 56 Spirals

770 
$$\pm$$
 100 km /sec , toward,  
 $\alpha = 288^{\circ}$ ,  $l = 339^{\circ}$   
 $\delta = -1^{\circ}$ ,  $b = -7^{\circ}$ 

2. Lotal motion of  $G_2$  cluster of 50 spirits within reference frame of (1) galactic clusters and isolated spirals of high velocity

$$5670 \pm 1500 \text{ km/sc}$$
 toward  
 $3 = 507$   $I = 308$   
 $\delta = -58$   $b = 55$ 

The residual velocities obtained from these two solutions are given in the subjoured table these have been rounded off to tens of kilometers for the first solution, and to hundreds for our local  $G_2$  in  $G_3$ . The column headings in this table, we self explanatory

Residual Velocities of Spirals on a Molssako Crakiti k Scheme

R	esidual Velociti	us of Spirals of	n a Molssakd Cr	Aki ti k. Scheme
700	Ob vel kin sec	Residud within ()	Residud, Gent G	Alloration
205	- 300	- 710	1	Local
221	3()()	600	ļ	Local
224	- 220	- 640		Local
275	<del>-,</del> 650	+ 200		Local
25(1	1 1400	- ]		
361	ł 4500	- }	000	Pisces Chister
354	4 500	<b>→</b>		
<u> 185</u>	F 4900	- J i	1	
404	- 25	610		Focal
554	F 1800	ł 1260		1 ocal
598	- 70	- 620	1	Local
936	+ 1300	580		Local
1025	† 30o	420	-	Local
1065	+ 920	+ 150		Lucat
1270	F 4800	- ]		
1273	<b>→ 5800</b>		2800	Deres of L. C.
1275	÷ 5200		2 mil	Persons Chister
1277	± 5200	] 1		
17(a)	⊰ \$00	~ 120		Local
2562	+ 5100	- ) !	15.5.015	
2563	F 4800	_ } !	0 1(x)	Cinca Cluster
2681	+ 700	- 250°		Local
2653	400	- 700	_	Local
2541	+ 60o	— 3 <sub>1</sub> 0		local
2859	+ 1500	+ 450		Linat
2950	+ 1500	+ 660	Ì	[ oca]
5031	- 30	- 760	İ	local
3034	- 290	- 130	ľ	local
3115	-  600	<b>– 4</b> 70		lacal
3193	+ 1300	+ 280	-	Local
3227	-F 1150	+ 140		Local
2261	$\pm 19600$	_	1 9500	Leo Cluster
3368	+ 940	- 30	-	Local
3379 3489	+ \$10	- 170		local
	.– <b>ნი</b> თ	- 330		Local
3521	÷ 730	- 300		t as at
3610	- 1850	+ 1130	_	I ocal
3623	+ 800	- 80		Local
3627	+ 650	- 230	_	l ocal
1051	+ 650	- 40		l otal Local
	+11800	_	+2100	
4111	- 800	+ 110	1.21/10	Ursa Major Cluster
#151 #192	+ 960	+ 270	-	l ocal l ocal
4214	- 1150	+ 410	- !	local? (Virgo)
- 1-1	+ 300	- 380		l ocal
		•		i crossi

(Continued )

		(Continuo	u)	
1	ļ <u>2</u>		3	Allonation
NGC	Olas, vel kut/ser.	Reskins within G	Reskhool, (I <sub>1</sub> in (I <sub>2</sub>	Viluoemed
4258	- - 500	- 150		Local
4374	F 1050	+ 360		Local? (Virgo)
4382	+ 500	- 180	-	Local? (Virgo)
1449	<b>2</b> 00	- 480	¦	Local
4472	+ 850	+ 180	-	Local? (Virgo)
4486	+ 800	4- 130	- (	Local? (Virgo)
4526	F 580	— 80	-	Local? (Virgo)
4565	-   1100	+ 460	-	Local
4594	-  1140	+ 540	-	Tane Bl
4649	+ 1190	ı 460	' -	Local? (Virgo)
4736	+ 290	- 300	i ~ Ì	Local
4826	- 150	- 390	ļ <i>-</i>	Local
4853	+ 7600	- <u> </u>		
4860	+ 7900	~		
4865	+ 5000	-		
4872	+ 6900	-		Coma Berenicas
4874	- - 7(KX)	<del>-</del> }	1200	Chaster
4881	- - 6900	- I		
4884	+ 67(n)	- <b>(</b>	l l	
4895	+ 8500	- [		
II 4045	- - 6600	]		
50x)5	900	F 360	i	Local
5055	+ 450	- 80	-	Local
5194	1 250	- 240	-	Local
5236	-J 500	-  50		
5457	- - 7(00)	- 130	-	Local
5866	+ 650	- - 330		l.cx.nl
6359	3 (K)()	i	-3200	Licolated
6658	J- 4 t00	-	2200	Incluted
6661	[ 3900	-	+2000	Inclated
6702	+ 2000		-1900	Incluted
6703	2000	_	~1900	Incluted
6710	-[ 5100	,	- <b> - 2</b> 900	Isolated
6822	- 150	- 4 90		I ax al
6824	F 3200	_	~ 1200	Inclated
7217	F 1050	4-1040	-	Local
7242	-  50au	-	F-1800	Incluted
7331	- 500	+ 400	]	Local
7611	-  3400	<b>-</b> }		
7617	- 1900	1 - I		
7619	-  38cm	1 . }	+2200	Родания Clustor
7623	-1 3800	-		
7626	+ 3700	- I		
LMC	+ 280	- 390		Local
SMC	-i 170	- 310	-	Local

The results from both solutions may be regarded as on the whole satisfactory, and perhaps significant. These found for the motion of our own galaxy within its  $G_k$  are in general "reasonable". We know so little as to a possible upper limit to the speed of a cluster of galaxies that the larger residuals found for our  $G_k$  moving in k k system do not seem impossible. The total motion of our own  $G_k$  cluster, as 5700 km/sec, is of the order of the larger residuals in the second solution.

A study of the reskiusis from the two solutions will indicate that the excess of positive velocities has been almost completely removed. It is unnecessary to reliterate that a slightly different grouping of the objects in the two classes treated, or the acquisition of a number

or velocities of spirals in the regions adjacent to the south galactic pole, would be expected to make significant changes in the magnitudes and directions of the total motions resulting

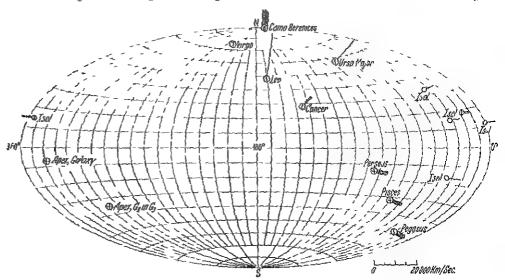


Fig 58 Distribution of Clusters of Galaxie.

from this method of treatment. The data are manifestly too limited in amount and in distribution to warrant any further refinement m the analysis

## Kapitel 7.

# Die Milchstraße.

Von

#### B. LINDBLAD-Stockholm.

Mit 28 Abbildungen und 1 Tafel.

## a) Einleitung.

1. Die Milchstraße als Objekt der Forschung. Das schwach leuchtende, diffuse und komplizierte, aber doch in einem gewissen Sinne sehr regelmäßige Gebilde unseres Nachthimmels, das den Namen Milchstraße (Voie lactée, Milky Way, griech. γαλαξίας, lat. Via lactea) trägt, ist in seiner Gesamtheit, der scheinbaren Ausdehnung nach, das gewaltigste aller Himmelsobjekte. In der Forschung haben wir zuerst die Milchstraße als scheinbares Gebilde, das "Phänomen der Milchstraße", zu betrachten. Es gilt hier, soweit möglich, persönliche Differenzen verschiedener Beobachter auszugleichen und ein mittleres Bild der Milchstraße, wie sie einem normalen menschlichen Auge erscheint, zu geben. Dieses Bild wird durch photometrische Schätzungen und Messungen in systematischer Weise ergänzt. Endlich greift hier auch die Photographie in bedeutungsvoller Weise ein. Doch muß immer daran erinnert werden, daß das visuelle und das photographische Milchstraßenbild in vielen Beziehungen prinzipiell streng zu unterscheiden sind.

Diese Festlegung des scheinbaren Phänomens hat aber nur einen Sinn, wenn sie für eine tiefer gehende Forschung die Grundlage bildet. Die Stellarastronomie sieht in der Milchstraße den Effekt einer Konzentration der Sterne unseres Systems gegen eine Fundamentalebene, die als Milchstraßenebene oder galaktische Ebene bezeichnet wird. Diese Konzentration gegen eine Ebene ist sogar in ihrer offenbaren Gesetzmäßigkeit das unmittelbarste Zeichen dafür, daß wirklich die uns umgebenden Sterne in ein gewaltiges System eingeordnet sind. In der Stellarastronomie wird das Wort Milchstraße bisweilen als ein Synonym für das Sternsystem verwendet. Es wird schließlich eine Aufgabe der Astronomie, die Erscheinung der Milchstraße in ihrer stellarastronomischen Bedeutung dynamisch zu erklären, welche Aufgabe es bedingt, eine statistische Mechanik des Sternsystems zu entwickeln. Die Methoden einer solchen statistischen Mechanik haben mehrere Berührungspunkte mit den statistisch-mechanischen Methoden der allgemeinen theoretischen Physik, wenn auch keineswegs die Theorien der kontinuierlichen Medien, der Gase und Flüssigkeiten, unmittelbar auf das Sternsystem angewandt werden können.

2. Übersichtliche Darstellungen und Monographien. Von Übersichtswerken über die Ergebnisse und Methoden der Milchstraßenforschung sollen hier nur einige erwähnt werden, welche, ohne neues Primärmaterial zu geben, durch selbständige zusammenfassende Gesichtspunkte gekennzeichnet sind. Unter

den alteren Werken dieser Art sind zu nennen F. G. W. Struve, Etudes d'Astronomic stellane<sup>1</sup>, J. Hirschill, Outlines of Astronomy<sup>2</sup>, H. J. Killin, Der Paxsteinhimmel usw<sup>3</sup>, R A Procior, The Universe and the Coming Transits<sup>1</sup> Einer spateren Zeit gehoren z.B. die Übersichtswerke von Miss Clarkki, und S NI WCOMB® an F RISH NPARI gibt unter dem Wort "Universum" in V VII N-Handbuch? eine eingehende Bespiechung der damaligen Resultate der Milchstraßenbeobachtungen und der Stellarstatistik. Etwas spater erschemt H Kobold. Der Bau des Fixsteinsystems\* Aus der Zeit der zwei letzten Jahrzehnte sind besonders zu erwähnen A.S. Eddington, Stellar Movements and the Structure of the Universes, and H KOBOLD, Das Steinsystem in und Stellarastronomie<sup>11</sup> K Graff gibt in R Henselings "Astronomisches Handbuch, herausgegeben vom Bund der Steinfreunde"13, eine Darstellung der Resultate der visuellen und photometrischen Milchstraßenbeobachtungen. J. Pr. issmann<sup>11</sup> hat eine sehr verdienstvolle Monographie, "Die Milchstraße" herausgegeben, die auch emen Zusatz von J. Hagin über "Die Nebelstraße" enthalt. A. Kopit gibt in MULTIR-POULITIES Tehrbuch der Physik 11 eine inhaltreiche Übersicht über den Bau des Sternsystems nach den modernen Untersuchungen. Eine zusammentassende Daistellung über den Bau des Kosmos ist von W Bernhi im r im Handbuch der Physik 15 gegeben worden

# b) Das visuelle Milchstraßenbild.

3 Die Beschreibung und zeichnerische Darstellung der Milchstraße Die Milchstraße ist schon für eine fluchtige Beobachtung ein auffalliges Phanomen des gestilnten Himmels und ist doch nicht leicht durch wissenschaftliche Vermessung quantitativ zu erfassen und darzustellen. Selbst eine genaue qualitative Beschierbung der Milchstraßenstruktur in ihren Einzelheiten und eine detaillierte zeichnerische Darstellung derselben ist erst in der Mitte des vorigen Jahrhunderts ernstlich angefangen worden. Hindernisse der exakten Beobachtung sind die mit der Hohe über dem Horizont wechselnde atmospharische Absorption und auch allerler Trubungen durch fremdes Licht, die den Eindruck des schwach leuchtenden Gebildes verfalschen konnen. Zu bemerken ist, daß die Milchstraße mir in geringem Kontrast gegen das allgemeine schwäche Himmelslicht leuchtet Die Schwierigkeiten sind naturlich mit der komplizierten Natur des Phanomens verbunden, mit der saniten und doch in einem Gewebe unendlich reicher Struktur vor sich gehenden Abstufung der Lichtstarke von den verhaltnismaßig hellen Wolken bis zu den kaum wahrnehmbaren femen Lichtschleiern, die dunklere Partien umgeben oder allmählich in den dunklen Hummelsgrund der außergalaktischen Regionen übergehen

Die Schwieugkeiten, ein einheitliches Bild des ganzen Milchstraßengurtels zu schaffen, sind weiterhin eine Folge dei Ausdehnung des Phanomens langs eines großten Kreises des Himmels, der um etwa 60 Grad gegen den Aquator geneigt erschemt. Nur in den Tropen kommt die ganze Milehstraße während

<sup>1</sup> St -Petersbourg Imprim de l'Acad Impér des Sc (1847)

<sup>&</sup>lt;sup>2</sup> London Longman, Brown etc (1849, mit spateren Auflagen)

<sup>&</sup>lt;sup>3</sup> Handb der allgemeinen Himmelsbeschreibung II Braunschweig (1872)

London Longmans, Giern, and Co (1874)
 Lhe System of the Stats Tondon Black (1890, 2 Aufl 1905)

<sup>6</sup> The Stars London Murray (1902) 7 IV, S 65 Leipzig Baith (1902)

<sup>&</sup>lt;sup>9</sup> London Macmillan (1914) Braunschweig Vieweg u Sohn (1906)

<sup>16</sup> Kultur der Gegenwart III (Astronomie) S 511 Leipzig und Berlin Teubner (1912)

<sup>11</sup> Encyklopadie der math Wiss VI 2 B, Heft 2 Teipzig Loubner (1926)

 <sup>&</sup>lt;sup>12</sup> S 183 Stuttgart Franckische Verl (1921)
 <sup>13</sup> Probleme der Kosmischen Physik IV Hamburg Grund (1924) 11 11 Auft, V, 2 Hälfte, S 429 (1928) 16 IV, S 577 (1929)

eines Jahreslaufs über den nächtlichen Horizont. Die gegenwärtig in den Einzelheiten genauesten Darstellungen des visuellen Milchstraßenbildes sind hauptsächlich über den nördlichen Teil der Milchstraße ausgedelnit, während zur Zeit der Vollendung der Uranometria Argentina der südliche Teil der Milchstraße der durch gute Darstellung begünstigte war

Aus dem Altertum sind zwei Beschreibungen der Milchstraße aufbewahrt worden, von Aristotri Est und von Ptolemaus Die letztere ist ziemlich eingehend und ist wahrscheinlich erst im 19 Jahrhundert übertroffen worden Fine deutsche Übertragung des Almagest mit der heutigen Sternbenennung gibt K MARITIUS3 PTOLEMAUS' Milchstraßenbeschreibung ist von Eastons nach Hal Mas Übersetzung mit Erklärungen wiedergegeben worden. Ein Bruchstück in freier Übersetzung mit Bemerkungen hat Pannekork in seinem unten besprochenen Werke "Die stidliche Milchstratte" gegeben. Eine nur wonig in Einzelheiten gehende Beschreibung der Milchstraße hat Thomas Wright in seinem seltenen Werke "Theory of the Universe" (London 1750) geliefert Die Sternkarten des 17 und des 18 Jahrhunderts behandeln die Milchstraße nur sehr dürftig Noch auf Bodks Karten ist nur eine schematische Milchstraßenkontur grob gezogen worden J K HORNER hat als erster nebst einer Milchstraßenbaschreibung eine elementare Photometrie der Magkllanschen Wolken und hellerer Partien der südlichen Milchstraße mit Hilfe von farbigen Glüsern verschiedener Dicke versucht W Herschfif gibt ein kurzes Verzeichnis von hellen und dunklen Partien der Milchatraße zwischen Sagittarius und Perseus. Emige Fortschritte in bildlicher Darstellung sind wohl in den Karten von W H WOLLASTONS, J W. LUBBOCKS und J DUNLOPIS zu registrioren

F W A ARGRIANDER fordert in Schumachers Jahrbuch, 4844, die Freunde der Astronomie zu Beobachtungen der Milchstraße auf In den 40er Jahren erscheint J Highschrißt verdienstvolle Zeichnung der sädlichen Milchstraße mit eingehender Beschreibung. A v Humbolder gibt im dritten Bande des "Kosmos" hauptsächlich nach den Arbeiten von J Herscher eine Beschreibung des Zuges der Milchstraße unter den Sternen

Ein Bruchstück einer detailieiten wörtlichen Beschreibung wurde im Jahre 1867 von H. J. Kifin in Hris', "Wochenschrift für Astronomie" veröffentlicht, und einige Jahre später gab endlich E. Hris's seine Zeichnungen der Milchstraße hernus. Sie gehen sädlich bis zur Deklination —35° Hris unterscheidet fünf I ichtstufen, die als Schattierungen verschiedener Tiefe in den Zeichnungen wiedergegeben sind. Some Darstellung steht daher mit den isophotischen Karten späterer Beobachter in Verwandtschaft. Die feineren Einzelheiten werden in dieser Weise nicht berücksichtigt, sondern in Lichtslecken einfacherer Kontur nusgeglichen. Die medrigste Stufe bei Heis entspricht dem schwachen Schimmer, in den die Milchstraße einem Beobachter mit scharfen Augen unter guten atmosphärischen Verhältnissen eingehüllt erscheint

- <sup>1</sup> Metourologica, Lib I, Cap 8 <sup>2</sup> Almagest, Lib VIII, Cap. 2
- Loipsig Tenhner (1912)
   La voie lactée dans l'hémisphère boréal Paris Gauthier Villars (1893)
- Uranographia siye astrorum descriptio Berlin (1801)
- Monatliche Correspondenz 10, S 220 (1804)
- <sup>7</sup> Phil Trans 1817, S. 302, Coll Scient Papers II, S 586.
- A Portraiture of the Heavens as they appear to the Naked Lye London (1811)
- The Stars in six Maps, etc. London (1830, mit spateren Aufl.)
- Phil Trans 1828, S 152
   Results of Astronomical Observations, etc., p 383 London Smith, Elder (1847);
   Beschreibung auch in Outlines of Astronomy (5 Edition, S 527)
  - Atlas cocleatis novus Köln (1872)

Die sudliche Milchstraße wurde in der großartigen Uranometria Argentina von B A Gould nach Zeichnungen von W M Davis und J M I nom in genauer Weise wiedergegeben. Die Art der Reproduktion der Zeichnungen war eine photolithographische, die Wiedergabe der Einzelheiten ist weiniger durch vereinfachende Ausgleichung gebunden als in den Karten von 11 is



Durch die Arbeiten von Heis und Gould war somit eine eingehende und wissenschaftlich einigermaßen brauchbare Darstellung des ganzen Milchstraßengurtels geschaffen worden. Die bisweilen erheblichen Unterschiede der zwei Bilder in den gemeinsamen Teilen lassen jedoch die Subjektivität der Auffassung selbst in den zeichnerischen Arbeiten hochster Klasse deutlich erkennen

Resultados del Observatorio Nacional Argentino I (1879) Mit Atlas

Inzwischen war eine Reproduktion der ganzen Milchstraße erschienen, die zwar eine noch schematischere Darstellung als die Hrissche bot, aber auf eine neue methodische Schützung der Lichtstufen gegründet war Dieses Werk ist in der "Umnométrio générale" von J C Houzikau1 enthalten. Die Beobachtungen wurden auf Jamaika angestellt Houzkau hat einen Versuch gemacht, die Linien konstanter Lichtstürke, die Isophoten, zu zeichnen. Er ordnet die Helligkeiten verschiedener Partien in eine Skala von Größenklassen, die eine Art Anschluß an die Größenskala der Sterne dadurch gewinnt, daß man das Hervortreten oder Verschwinden der Lichtflecken in der Däminerung oder in der Himmelsbeleuchtung durch den Mond zur salben Zeit wie das Hervortreten oder Verschwinden benachbarter Sterne einer gewissen Größe beobachtet Houzhau gibt in omer Tabelle die Intensitäten für 33 Punkte maximaler Holligkeit Um diese Maxima sind die isophotischen Linien in memlich schematischer Weise gozeichnet, oftmals als regelmäßig abgerundete Oyale Durch diese schomatische Regelmäßigkeit steht Houzeaus Darstellung in einer Sondorklasso unter den visuellen Milchstrußenbildern Die größten Intensitäten (Größen 4,5 und 5) notiert Houznau für die Gegenden, die in Tabelle i zusammengestellt sind (Koordinaton für Aqu 1880)

In schärfstem Gegensatz zu Houzeaus Methode steht die Art der Milchstraßendarstellung, die von O Bonddickers zu Birr Castle in Irland praktiziert wurde Die Milchstraße ist hier in eine komphisierte Struktur von feinen Strömungen mit oftmals ziem-

Tabelle 4

	- 4-5		
A.R	Dekl	Größe	Sterabild
16 <sup>h</sup> 4 <sup>m</sup> 17 46 18 () 18 8 18 8 18 23 18 41 21 2	- 54°,3 - 34 ,7 - 28 ,5 - 18 ,7 - 14 ,4 - 7 ,0 + 45 ,5	5 5 5 4,5 5 4,5	Norma Scorpius (M7) <sup>6</sup> Sagitterius Sagitterius Scutum Scutum Cygnus

lich scharfen Begrenzungen aufgelöst. Die Subjektivität dieser schönen und technisch vollendeten Darstellung ist offenbar Pannekork, der die Gelegenheit hatte, die Originalzeichnungen zu untersuchen und zu benutzen, macht jedoch die Bemerkung, daß diese Bilder viel mehr als die Reproduktionen alch dem wirklichen Anblick der Milchstraße nähern, und daß also der lithographische Prozeß, trotz größter Sorgfalt, viele schwache Nuancen modifiziert hat Eine Beschreibung seiner Arbeitsmethode hat BORDDICKER selbst in einer Notize gegeben

Unter den Zeichnungen dieser Zeit ist auch eine Chromolithographie von L. TROUVELOT<sup>®</sup> von der Milchstraße zwischen Casalopeia und Scorpius zu nennen Die Originale befinden sich nach Easten in Meuden

Zu den schönsten Zeichnungen der Milchstraße gehören wehl die von Julius Schmidt, die in den Jahren 1864—1867 zu Athen hergestellt worden sind und die erst kürzlich in phototypischer Reproduktion von der Sternwarte zu Leidens publiziert wurden. Die Zeichnungen erstrecken sich im Süden bis zur Deklination—45° Besonders die südlichen Partien, von Scorpius bis Aquila, sind mit erstaunlicher Fülle von Einzelheiten mit größter Sorgfalt ausgearbeitet worden

Annales de l'Observatoire de Bruxelles, N S , I (1878)

The Milky Way from the North Pole to 10° South Declination I ondou (1892)
 Die Größe der Gegend um M7 ist in HOUZEAUE Tabelle als 4, auf der Karte aber als 5
 bezeichnet Die letztere Zahl ist von Easton (i c) aufgenommen worden

<sup>4</sup> M N 50, S 12 (1889)

The Trouvelot Astronomical Drawings New York Scribner (1882)

Annalen van de Sturrewacht II Leiden XIV. Tweede Stuk (1923)

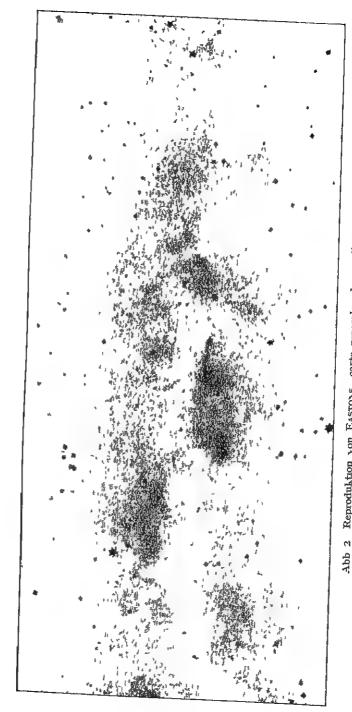
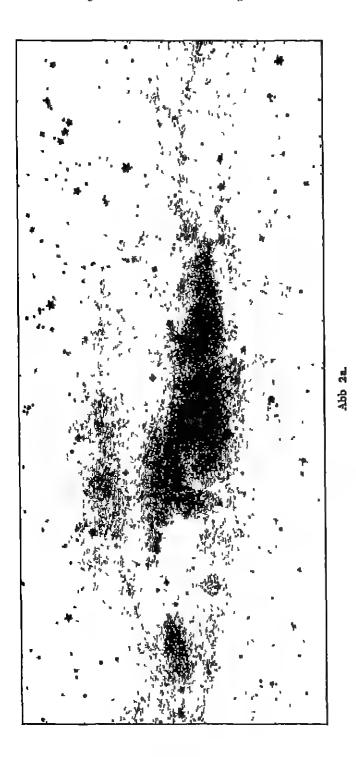


Abb 2 Reproduktion von Eastons "carte generale der nordlichen Milchstraße



Nach J Hopmann<sup>1</sup> befindet sich auf der Bonner Steinwarte im Manuskript eine Reihe von Schmidts Milchstraßenbeobachtungen, Beschreibungen und Helligkeitsschatzungen, beginnend 1859 in Athen, die nur terlweise in direktem Zusammenhang mit seiner Karte stehen

Die Milchstraße nordlich der Deklination -10° ist in sehr eingehender Weise von den zwei holkindischen Astionomen, C. Easton und A. Pannlkoi k. behandelt worden Eastons volher erwahnte, 1893 erschienene Arbeit, "La voie lactée dans l'hemisphere boréal", bildet einen sehr merklichen Fortschritt in der bildlichen Darstellung der Milchstraße. Easton hat seine Karten ganz unabhangig von anderen Daistellungen gezeichnet. Die Reproduktion ist auf lithographischem Wege ausgeführt worden, wobei der Zeichner selbst die zur Vorbeiertung notige Kopierarbeit sowie eine Retusche der gedrückten Karten ausgeführt hat Easton betont besonders die großen Schwierigkeiten, durch Zeichnung ein exaktes Bild der Milchstraße, wie sie dem Auge erscheint, wieder-Das Milchstraßenlicht ist so schwach und die Helligkeitschifferenzen der verschiedenen Partien sind so sanft akzentuiert, daß die Wiedergabe immer em wenig übertrieben werden muß Easton gibt eine Hauptkarte (carte genérale), welche die Gradation des Milchstiaßenlichts und die ielative Helligkeit der Milchstraßenpartien wiedergeben soll, wahrend dier "cartes explicatives" in etwas femere Einzelheiten gehen. Die Hauptkarte, welche ein bemerkensweites, vorzugliches Stuck Arbeit ist, wird hier in Abb 2 ieproduziert. Der Text enthalt eine ausführliche geschichtliche Übersicht über das Problem der Milchstraßenbeschierbung. Zuletzt gibt Easton hier eine eigene, sehr eingehende Beschierbung der nordlichen Milchstraße nebst einem Katalog, der die Randkoordmaten von 164 hellen Flecken und Stromungen und von 47 dunklen Partien enthalt. In emer spateren Arbeit<sup>2</sup> hat EASTON auch eine Karte mit isophotischen Linien gegeben

PANNLKOLK scheint der eiste zu sein, der die Mahnung Argi LANDERs in semer "Aufforderung", eme feste Skala relativer Helligkerten durch wiederholte Vergleichungen verschiedener Leile der Milchstraßenstruktur auszubilden, beheizigt hat In seinem Weike' "Die nordliche Milchstraße" gibt er die Resultate seiner umfangreichen Helligkeitsschatzungen. Die Helligkeiten wurden zuerst in einer willkuilichen Skala ausgedruckt, nachher wurde eine Zahl von Normalstellen ausgesucht, diese wiederholt aneinander angeschlossen und damit alle anderen zu beobachtenden Stellen verglichen. Die relativen Helligkerten wurden nach der Stufenmethode Argelanders geschätzt, und die Ausgleichung für die Normalstellen in einer zusammenhängenden Skala mit der Stufe als Einheit geschah auf dem Wege wiederholter Annaherung. In dieser Skala wurden die Helligkeiten von 128 Stellen der Milchstraße ausgedruckt. Der Stufenweit wurde zunächst unter Benutzung der atmosphauschen Absorption durch Vergleichung hellei Flecken, wenn sie in geringer Hohe stehen, mit hochliegenden Stellen der Milchstraße und auch nach Houzeaus Methode aus Beobachtungen in dei Dammeiung bestimmt. Eine bessere Bestimmung ergab sich spatei 1 aus einer Vergleichung mit den Helligkeitsmessungen von Van Riffin (Ziff 5) Der Stufenwert der Gesamthelligkeit des Himmelsgrundes ("Eidlicht" in weiterem Sinne + Milchstraßenlicht) eigibt sich hier zu 0,11 Gioßenklassen, was abei, wenn das "Eidlicht" eliminiert wird, im Mittel für das Milchstraßenlicht 0.3 Großenklassen bedeutet

<sup>&</sup>lt;sup>1</sup> V J S 64, S 320 (1929)

<sup>&</sup>lt;sup>2</sup> Verh der K Akademie van Wetenschappen, Amsteidam, VIII, Nr 3 (1903)

Annalen van de Steirewacht te Leiden XI Derde Stuk (1920)
 AN 214, S 389 (1921)

Pannekoek gibt seine Resultate teils in einer sehr ausführlichen wörtlichen Beschreibung der Einzelheiten, teils als Zeichnungen, die auf den zahlenmäßigen Resultaten füßen und durch ein photographisches Roproduktionsvorsahren vervielfältigt wurden, teils endlich als Karten mit isophotischen Linien, die direkt die Zahlenergebnisse zum Ausdruck bringen. Weiter folgen der sehr eingehenden Beschreibung der nördlichen Milchstraßenstruktur ausführliche Vergleichungen mit anderen Darstellungen (Easton, Schnidt, Boeddicker, Klein, Backhouse<sup>1</sup>, Uranometria Argentina). Schließlich werden die Isophotendarstellungen von Pannekoek und von Easton mit den Zeichnungen von Schmidt und von Boeddicker in ein "mittleres Milchstraßenbild" von zuhlenmäßiger Form zusammengefaßt, das auch in Isophotenkarten wiedergegeben wird. Der mittlere Stufenwert wird für die Eckpunkte und für das Zentrum jedes Quadratgrades des galaktischen Gürtels gegeben. Dieses Zahlensystem sollte als "das beste Gesamtresultat zu betrachten sein, das sich aus den bisherigen Arbeiten über die Milchstraße ableiten läßt"

Ganz kürzlich hat Pannekoeks nach demselben Plan seine Arbeit auch über die südliche Michstraße ausgedehnt. Die Beobachtungen wurden gelegentlich einer Expedition, die von der K Akademie der Wissenschaften in Amsterdam zur Beobachtung der am 14. Januar 1926 stattfindenden totalen Sonnenfinsternis nach Indien geschickt wurde, ausgeführt, und zwar sowohl auf der Bosscha-Sternwarte in Lembang auf Java, als auf dem Dampfer während der Reise. Die Witterungsverhältnisse waren durchgehend ziemlich ungünstig. Nichtsdestoweniger ist es dem unermüdlichen Astronomen gelungen, sein Programm durchzuführen und die südliche Milchstraße in ihren Einzelheiten auf photometrischer Grundlage darzustellen.

Eine Anzahl Normalpunkte wurde ausgewählt und durch wiederholte Vergleichungen untereinander in eine "siciliche Skala" eingeordnet, welche sowohl an der Aquilaseite als an der Monoceresseite mit der nördlichen verglichen und auf diese reduziert werden konnte Die Helligkeiten anderer Punkte wurden mit Hilfe der Normalsteilen geschätzt Pannekork gibt einen Katalog über die Beobachtungsresultate für 189 Stollen der südlichen Milchstralie.

Wie für die nördliche Partie der Milchstraße hat PANNEKOEK unch in dieser Arbeit auf Grund seiner Resultate Zeichnungen und Isophotenkarten ausgearbeitet und gibt auch eine in die feinsten Einzelheiten gehende wörtliche Beschreibung, der er die Beschreibungen von Prolemäus und von J Herschelle, folgen läßt

Der große Reichtum der südlichen Milchstraße wird besonders von Pannekoek hervorgeholen:

"Wer nur die Teile des Sternhimmels kennt, die in den mittleren Breiten Europas sichtbar sind, kann sich kome Vorstellung von der wundervollen Schönheit der südlichen Mitchstraße machen Gewiß gehört eine dunkle Augustnacht in Europa mit den großen hellen Lichtwolken im Schwan und dem anschließenden buchtigen Fleckenband im Adler und in der Cassiopela zu den schönsten Natureindrücken in unserem Welttell. Aber die Pracht des Südhimmels ist doch ganz anderer Ordnung, man möchte ihre höhere Potenz nach einer unrichtigen, aber verstündlichen Gedankennssoziation mit dem üppigen Reichtum aller Tropennatur in Zusammenhang bringen Es ist zuerst die viel größere Holligkeit, die die Milchstraße in ihrer südlichen Hälfte erreicht. Ihr Licht wüchst von dem schwachen, einförmigen Schimmer des Januarhimmels bei Orien und Sirius allmählich an und erreicht in Carina, in 250° Lünge, eine Helligkeit, die schon

<sup>&</sup>lt;sup>1</sup> The Structure of the Universe Publ of West-Hendon House Observatory I, II <sup>8</sup> "Die südliche Milchetraße", Annalen v d Bosscha-Sterrewacht Lombung (Java) II, 1ste Gedeelte (1929)

die hellsten Stellen am Nordhimmel übertrifft. Hier wirken die Anhaufung der schonsten Steine und Steinbilder, die dichtgestieuten Gruppen im Schiff, das Sudliche Kreuz und die hellen Centaurussteine mit den umegelmaßigen Buchten der scharf begrenzten Lichtpartien des Milchstraßenbandes zusammen, um ein



eindrucksvolles Ganzes zu schaffen Etwas weiter fangt eine reichgegliederte Reihe von Stromen und Wolken an, die stets heller werden, bis sie in dem Schutzen einen Hohepunkt erreichen, von dieser Reihe erblicken wir in Europa noch das letzte Glied in dem Lichtfleck im Schild Dei Glanz dieser hellen Schutzenflecken

PANNEROEKS Isophotenkarte für die südliche Milchstraße zwischen den galaktischen

Abb

fibertrifft weitaus alle anderen Gebilde der Milchstraße, die Eigentsmilchkeit des Eindrucks wird noch gesteigert durch die Armut dieser Gegenden an für das bloße Auge sichtbaren Sternen Bei jedem Vergleich füllt der Gegensatz auf, wie die Milchstruße im Schwan und in Lacerta mit szintilherendem Sternstaub dicht besät ist, wührend die hellen Schützenwolken wie mit ruhiger Leuchtfarbe auf einen sternenleeren Himmelsgrund gemalt erscheinen "

Als ein Beispiel der Pannekorkschen Milchstrißendarstellung wird in Abb 3 die Isophotenkarte der kontrastreichen Carina-Crux-Centaurus-Region des Südhimmels wiedergegoben

4. Photometrische Eichung der Isophoten Eine wichtige Ergünzung zu dem rein visuellen Milchstraßenbild, wie es nach den Beobachtungen mit bloßem Auge erschemt, liegt in den Resultaten photometrischer Messungen des Milchstraßenlichts In dem Universalphotometer von K. GRAFF1 wird ein Bild der beobachteten Himmelsgegend durch ein kleines Mikroskopobjektiv in der Kontaktiffiche eines Lummer-Brodhunschen Prismas erzeugt. Von der Seite her wird das Bild einer beleuchteten Milchglasscholbe nach dem Okular zu total roflektiert, so daß man den eingestellten Teil des Himmels als einen runden Fleck inmitten eines gleichmäßig erhollten Feldes sieht, das durch einen Photometerkeil vor der Milchglasscheibe auf die Lichtstürke des Fleckes abgeschwächt wird Als Anschlußheiligkeit für Graffs Messungen diente der Hintergrund in Ursa minor bei R A. 0h 0m und Dekl +85°, dem willkürlich die Größe 2m,0 beigelegt wurde. Als zweiter Anhaltspunkt diente die Cygnuswolke zwischen y und & Cygni, für die der Wert 1m,30 photometrisch erhalten wurde Graffs Beobachtungen verteilen sich auf 32 Stellen des Himmels, in Verbindung mit Stufenschätzungen wurden 47 Punkte der nördlichen Milchetraße von Sagittarius bis Canis major in ihrer relativen Helligkeit photometrisch festgelegt

J. Hopmann<sup>a</sup> hat als eine Nebenaufgabe bei der Sonnenfinsternisexpedition 1922 nuch Christmas Island mit Anschluß an Graffes Messungen übrliche Beobachtungen für einige Punkte der südlichen Milchstraße ausgeführt und auch und Menge Stufenschätzungen relativer Intensitäten in dieser Gegend gemacht Unter Benutzung der Pannkkokkschan Isophoton der nördlichen Milchstraße und Zuhilfenahme von Goulds Darstellung der südlichen Milchstraße in der Uranometria Argentina zur Ergänzung sonner Stufenschätzungen hat Hopmann dann eine Isophotonkarte der ganzen Milchstraße konstruiert Für Pannkkokks Stufenwert findet Hopmann aus Graffs Messungen 0<sup>m</sup>,138, für seinen eigenen findet er 0<sup>m</sup>,0996. Es sollte hervorgehoben werden, daß die Stufenmethode erheblich genauer ist als die photometrischen Messungen, deren w. F einer Beobachtung etwa 0<sup>m</sup>,1 beträgt Die im Photometer gemessene Fläche ist auch größer als die mit dem Auge vorglichenen Gebiete. Der Vorteil des Photometers besteht also wesentlich in der Einführung einer unpersönlichen Skala.

PANNEKOER® hat der Hopmannschen Darstellung einige kritische Beinerkungen gewidmet Es scheint sehr möglich, daß infolge unzulänglicher Verbindung der zwei Hälften der südlichen Milchstraße, Centaurus- und Curinaseite, in den Stufenschätzungen Hopmanns die Gegend um 6h R A (Monocoros) zu schwach, verglichen init der Gegend um 18h (Sagittarlus), ausgefallen ist Pannekoek hebt auch hervor, daß infolge variablen "Erdlichts" das Helligkeitsverhältnis zwischen Normalstelle und Milchstraßengegend veränderlich sein muß, und daß

<sup>&</sup>lt;sup>1</sup> Abhandl, der Hamburger Sternw zu Bergedorf II, Nr 5 (1920)

AN 219, S 189 (1923)

<sup>&</sup>lt;sup>8</sup> В A N 3, S 44 (1925), Die südliche Milchstraße (1929)

die Graffsche Methode daher kaum geeignet ist, eine ganz zuverlassige absolute Skala zu geben. In einer eingehenden Rezension der Panneroekschen Werke über die Milchstraßenstruktur macht Hopmann<sup>1</sup> auch einige Bemerkungen zu Panneroeks Kritik. Es ware noch zu früh, mit Sicherheit über das wahre Intensitätsverhaltnis zwischen den zwei Milchstraßengebieten zu uiteilen. Es scheint, als ob man vielleicht bei Pannerolk mit einer kleinen Variation der Stufe zwischen Nord- und Sudhimmel zu rechnen hat (vgl. Ziff. 5)

5 Die absolute Heligkeit des Himmelsgrundes. Zur Einstitlung der wahren Intensitatsverteilung des Milchstraßenlichts oder des allgemeinen Sternenlichts aus den Resultaten der photometrischen Stufenschätzungen und Messungen ist es notwendig, die beobachteten Heligkeiten von dem Einfluß der allgemeinen zerstreuten Strahlung des Himmels, die als "Erdlicht" im werteren Sinne bezeichnet werden kann, zu befreien Diese Strahlung ruhrt großenteils von Nordlichtern und vom Zodiakallicht her Die Scheidung der zwei Strahlungsarten, Steinlicht und "Erdlicht", ist dadurch möglich, daß die Steinstrahlung fur höhe galaktische Breiten aus den Steinzahlen mit genugender Approximation berechnet werden kann

Nach Pionierarbeiten von S Newcomb<sup>2</sup>, C J Burns<sup>3</sup>, S D Townley<sup>4</sup> und J C Kapteyn<sup>5</sup> haben besonders L Yntema<sup>6</sup> und P J van Rihjn<sup>7</sup> das Problem schr eingehend behandelt. Das benutzte Flachenphotometer besteht im Prinzip aus einer kleinen beleuchteten Scheibe, die gegen den Himmel gerichtet wird, und deren Helligkeit durch Anderung der Beleuchtung in meßbarer Weise gleich der Helligkeit durch Anderung der Beleuchtung in meßbarer Weise gleich der Helligkeit des Himmels an der betrachteten Stelle gemacht werden kann van Rihjn findet aus seinen auf Mount Wilson angestellten Beobachtungen die totale Helligkeit der direkten Steinstrahlung aquivalent mit 1440 Steinen der Große 1<sup>m</sup>,0, was in guter Übereinstimmung mit Yntemas Resultat, 1350 Steinen derselben Große, ist. Die beobachtete Steinstrahlung für miedere galaktische Breiten begt zwischen den aus den Steinzahlen in den Groninger Publikationen Ni. 18 und 27 berechneten Weiten, ist aber in besserer Übereinstimmung mit den letzteren Daten

van Riijn gibt für den mittleren Anteil der verschiedenen Strahlungsarten in der diekt gemessenen nachtlichen Strahlung folgende Weite. Die Einheit der Helligkeit ist ein Stein von der Große 1,0 im Harvardsystem per Quadratgrad. Die Steingroße 1,0 entspricht 0,94 10<sup>-6</sup> Meterkerzen (Hefner)<sup>8</sup> Die benutzte Einheit der Flächenhelligkeit des Himmelsgrundes entspricht daher etwa 0,78 10<sup>-6</sup> der Flächenhelligkeit des Vollmondes

Zodiakallicht	0.071
Ducktes Sternenhoht	0,029
Amora boreglis	0.024
Gestreutes Erdlicht	0,032
Gestreutes Stanenlicht	0,009

C Hoffmlister macht jedoch wahrscheinlich, daß van Rhijn den Anteil des Zodiakallichts zu hoch geschatzt hat Er findet überhaupt einen viel kleineren Betrag für das "Erdlicht", nur etwa ein Funftel von Yntemas und van Rhijns Wert

<sup>&</sup>lt;sup>1</sup> V J S 64, S 327 (1929) <sup>2</sup> Ap J 14, S 297 (1901) <sup>3</sup> Ap J 10 S 166 (1902) <sup>1</sup> Ptbl A S P 15 S 13 (1903) <sup>5</sup> Plan of Selected Ateas, S 11 (1906)

Publ Astron Lab Groningen Nr 22 (1909)
Publ Astron Lab Groningen Nr 31 (1921)

Vgl Russett, Ap J 43, S 128 (1916)
 Verdif d Sternw Berlin-Bibelsb 8, H 2 (1930)

VAN RHIJNA Resultate wurden von Pannekoek zur Ermittlung seines Stufenwerts benutzt (Zilf 3) In ühnlicher Weise hat Hopmann<sup>1</sup> seine scheinbaren Flüchenhelligkeiten der Milchstraße durch eine summarische Korrektion in wahre Intensitäten vorwandelt Das Resultat, die mittlere Intensität, pro Quadratgrad gerechnet, für aukzessive Areale in dem galaktischen Koordinatennetze (galaktische Länge und Broite), wird hier in Tabelle 2 wiedergegeben.

Tabelle 2 Die mittlere Verteilung des galaktischen Lichts nach Hormann,

· II3	o= - a	5° —1	s* -	5" +:	5° +1	5° +1	5° +30°
0.0	37 <sup>8</sup>	408	62 <sup>k</sup>	SSR	498	409	36 <sup>th</sup>
40	36	43	71	56	51 1	37	36
20	36	40	76	53	49	36	36
30	36	41	74	100	56	36	36
40	36	46	62	77	51	36	36
50	36	45	65	63	56	36	36
60	36	46	74	60	46	36	36
70	36	48	73	63	45	36	36
80	36	45	62	62	46	36	36
90	16	45	57	49	42	36	36
100	16	45	51	51	39	36	36
110	36	41	49	46	46	36	36
120	26	44	49	45	43	36	36
130	1 '	49	46	54	47	37	36
140		45	47	59	51	39	36
150	36		53	63	51	45	36
160	16	49	51	62	51	45	36
170		1 49	51	65	56	45	36
180	1 22	43	56	68	68	45	36
190	36		44	68	58	44	36
2(H)	36	42	57	83	60	48	36
210	36		57	79	66	48	37
220	16	46	71	79	73	51	40
230	36	42	64	73	66	51	39
240	36	37	57	80	61	48	36
250	36	36	50	89	62	41	36
260		36	44	95	51	39	36
270	36	39	44.4	116	90	42	36
280	36	45	106	117	105	49	36
200	16		F	117	116	57	39
3(N)	36	53	106	118	113	73	46
310	36	57	109	109	126	89	51
320	36	56		125	136	83	46
330	16	56	133 83	123	95	60	36
340	36	53			54	36	36
350	39	53	76	99 76	46	37	36
360	40	54	E8	1 70	100	3/	

Die Einheit der Helligkeit ist so gewählt worden, daß ein Stern von der Größe 1,00 im visuellen Harvardsystem gleich 1000 gesetzt wird. Es ist klar, daß die Resultate nicht als endgültig angesohen werden können, sondern einer sorgfältigen, Prüfung durch wiederholte Messungen und Vergleichungen verschiedener Teile der Milchstraße unterworfen worden müssen. Sehr auffallend ist die relativ große Intensität des Milchstraßenlichts im Intervalle L 270°—360°, die jedoch nach Pannekoik (Ziff 4) etwas übertrieben sein kann. Hopmann gibt in einer Pigur einen Vergleich der Vorteilung des Milchstraßenlichts nach galaktischer Länge mit den in analoger Welse behandelten Sternzahlen für die Grenzgrößen 8-,25 und 11m,0 (vgl. Ziff 16). Die Maxima der Sternzahlen sind in galak-

LAN 222, S 81 (1924)

tischer Lange betrachtlich gegen die Richtung zur Sagittarinsregion, wo das Milchstraßenlicht sein Maximum hat, gedicht

In C Hoffmeisters obenerwahnter Arbeit wurden auch die Pannikofkschen Normalstellen der Milchstraße mit dem Flachenphotometer, dessen Konstruktion im Prinzip mit dem von Yntema und van Riijn benutzten analog ist, ausgemessen Tabelle 3 gibt die Normalstellen mit den von Hoffmeister angenommenen Koordinaten Die Tabelle enthalt die Stufenschatzungen von Pannekofk und Hoffmann und weiter die gemessenen, auf das Zenith ieduzierten

L		be	1 1	١.	-
L	1.	De.	Ш	e	- 4

L thelle 3										
Stelle	a	5	Sternbild	L	P (NN	Норч	J,		$J_{ m abs}$	Graße
ψ	[2 °	- 32 °	Риррь	219,5	3,1		0,321 +	0,042	0,316	3 <sup>m</sup> ,71
- 1	105	-16	"	195 .5		) - i	279	·	,261	3 ,91
$\gamma$	107	- 4	Monoccios	186 ,3	28	1.7	,313	,032	,306	3 ,75
2	109	15	Cams major	197,0	2,7	3.7	300	,021	290	3 ,80
y V Y	100	- 5	Monoccios	183 ,8	1,8		,219	,002	,189	4 ,20
Y	117	-31	Puppis	217,6	1 }		.259	,053	,239	10,1
U [	91 L	19	Lepus	193 ,0	0.5	2.3	186	,03L	,18‡	1,53
A ]	166	60	Caima	257 4	65	7.3	,868	,026	1,000	2 ,16
Λ' C	178	62	Centaurus	263 .3	5,8		,608	,043	0,675	2,80
c [	114	53	Vela	213.8	3,0	-	321	,035	, 320	3 ,70
D [	141	16	Vela	237 ,5	1.7	63	,233	,051	,206	F .JS
D' ]	131	57	Caima	2 2 ,2	1.9	3,1	,196	,018	,160	1 , 15
Ľ	138	50	Vela	238,3	0,9	! -	184	023	,115	1 ,56
E'	160	44	Vela	247 ,7	10		691,	,015	,126	¹↓ ,7 I
F	200	63	Centaurus	271,0	1,0		.543	,077	,591	3 ,02
G	219	-63	Centamus	282 ,6	2.7	71	,423	,032	,441	
G′	201	- 58	Centaurus	275 ,2	2,9		,471	,037	,508	13,19
Н	196	-51	Centaurus	273 ,5	1 5	7.9	,208	014	,175	1 .35
K	191	-63	Cruy	269,9	0,0	7.9	,233	009	,206	81, 1
Ļ.	232	50	Noi ma	295 ,1	3,1	7.6	133		156	3 ,31
7	270	-28	Sagittarius	330 ,3	9,8	12,2	1,367	,060	1,624	1 .93
L	280	- 8	Scutum	353 ,0	7,2	9,5	0.845	, 104	0,971	2 ,12
Nordpol		- 90			t	l	,130	,009		5 ,13
	84	<u></u>					,202	,013	801,	4 ,40
	175	<b>+60</b>		l			,109	,003		

Intensitaten  $J_z$ , die auf den leei en Raum und tur Eidheht reduzierten "absoluten" Intensitaten  $J_{abs}$  und deren Aquivalente in Steingroßen per Quadratgrad. Die Einheit der Intensitaten entspricht einem Stein von der Große 2,22 per Quadratgrad und ist also im Verhaltnis 1 3,076 kleiner als die van Riijnsche Einheit Die Tabelle enthalt auch einige Stellen außerhalb der Milchstraßenstruktur

Der Vollstandigkeit halbei werden hier in Tabelle 4 auch Pannekoeks Stufenwerte fur die Normalstellen der nordlichen Milchstraße, wie sie in Panne-koeks erstem großen Werke angegeben worden sind, aufgefuhrt. Die galaktischen Koordinaten sind nach dem Martischen Pol ( $\alpha=12^{\rm h}$  40<sup>m</sup>,  $\delta=+30^{\circ}$ , 1880) gerechnet worden

Der Anschluß zwischen Hoffmeisters photometrisch bestimmten Intensitaten und Pannekoeks Stufenwerten in Tabelle 3 ist sehr gut und entspricht im Mittel der Gleichung

$$J_z = 0.100 + 0.086 S + 0.00045 S^3$$

wo S Pannekoeks Stufenweit ist Daß systematische Fehlei bei den Stufenschatzungen auftreten mussen, ist von vornheiem fast schstverstandlich (vgl Zift 4) Die Messungen scheinen zu zeigen, daß bei Pannekoek die Gegend von 200° bis 250° galaktischei Lange etwas zu hell, die Fortsetzung bis etwa 300° etwas zu schwach beobachtet ist, wobei die Angaben ielativ zum mittleien

Nullpunkt jenes Teils der Milchstraße bei Pannekoek zu verstehen sind Man kann dann nach Hoffmeister folgende Berichtigungen zu den Stufenwerten annehmen

(sal. J.Ango	mi.	Gal. Lilege	al.
200°	-0,2	260°	0.0
220	-0,3	280	+0.8
240	-0,3	300	+0.6

Die systematischen Fehler bei Pannekoek sind also jedenfalls sehr klein und erreichen kaum den Betrag von 4 st. Eine der obigen ähnliche Relation gibt der Vergleich mit Hopmanns Stufenwerten. Hier sind einige größere Differenzen zu bemerken, besonders für die südlichen Normalstellen H und K, die in Hopmanns Arbeit auffallend hell geschätzt worden sind

State	Bezelchenung	I	Н	Statement
1	3 II Scuti I A Aquilee	353°,0	- 3°,0	6,4
P M	& Aguillae — 110 Hore	16 ,1	+ 6,3	2,2
M	7 Aquilae # 110 Flore	16 .7	5.4	4.3
	6 Vulpec - 113 Here.	23 ,6	+62	1,4
Ñ	7 Sagittae - 12 Vulpec	26,6	1 - 3.8	3.3
N V Q	57 Cypul & 60 Cygnl	53 ,1	+ 0.9	5,1
В	a Cuphoi 3 Lacortao	69 .7	- 0.3	1 4,5
	7 Lucertan — 2 Cam	73 .5	- 2.0	3.7
N C	A Cophel & Cophel	! 74 /2	+ 3 7	0,4
ñ	β Cum — 7 Androin	79 9	- 4 i9	2,3
ĬŠ	и Androm – t Cass	83 ,2	-10 .8	1,5
	(# Cam, to Cophei)	113 12	_10 ,0	413
V	B Crust 1 Cophet	83 ,9	+ 1,4	3,6
				1
S	Sto Cass I y Cass.	94 ,8	+10 ,1	1,6
m	\$1) Cuiss & Causi.			1
T X H	# Cam - o Pornel	96 ,3	- 7 .1	1.1
X	d Cruss g Pornol	97 .8	- 2 .3	2.6
H	R Tourist Tourist + Aurigen	449 4	1 - 6.4	1.0

Tabolle 4.

J Duray hat in seiner eingehonden Arbeit "Recherches sur la lumière du ciol nocturne" die Intonsitäten einiger Milchstraßengegenden mit der Intensität des Himmels am Pol, wie auch mit den Intensitäten an Punkten in dersolben Zanitdistung oben außerhalb der Milchstraße verglichen. Er findet die dichtesten galaktischen Wolken etwa 2,5 mal so hell wie den Himmel am Pol, während für die meisten Milchstraßengegenden das Heiligkeitsverhältnis den Wert 2,0 nicht erreicht Die Messungen wurden teils mit einem visuellen Photomotor, einer für die Aufgabe geelgneten Form des Photometers von FARRY-Buisson, tolls photographisch ausgeführt. Duray findet, daß, nachdem die Strahlung des Himmels für die Diffusion des Lichts in der Atmosphäre korrigiert worden ist, etwa 1/10 der Strahlung von den schwachen Sternen herrührt Das Zodiakallicht entspricht in einer Sonnenentfernung von 60° etwa einem Sechstel der totalen Helligkeit Der Rest der Strahlung, von Nordlichtern abgesehen, stammt vielleicht aus einer Diffusion des Sonnenlichts durch Meteoriten außerhalb der Atmosphäre Die Strahlung des Nachthimmels ist nur in geringem Maßo polarisiert, erscheint auch nicht besonders reich an blauem Licht

f Tauri w Aurigae .

H Comin - s Comin - s Comin

Lyon Bull 10, Nr 9, S 70 (1928).

## c) Die Photographie der Milchstraße.

6 Die prinzipiellen Verschiedenheiten der visuellen und photographischen Beobachtungen. Wahrend schon Steine 7 Große einzeln dem normalen Auge unsichtbar bleiben, wachst die Zahl schwacherer Steine in den Milchstraßenzonen so gewaltig, daß ihr Gesamtlicht über ein kleines Areal einen merklichen Reiz auf die Stabchen der Netzhaut des Auges ausubt. In dieser Weise entsteht die optische Illusion, die wir als das Phanomen der Milchstraße wahrnehmen.

Der photographischen Platte gegenüber hegt die Sache merklich anders Die Empfindung des Auges ist vom Lichteffekt der pro Zeiteinheit aufgenommenen Energiemenge abhangig, wahrend die Platte in der Expositionszeit Belichtungsenergie akkumuliert. Die Steine sehr geringer Helligkeit drangen sich zwar auf der Platte so dicht anemander, daß ihre Scheibehen nicht mehr als distinkt anzuschen sind, aber Steine, die noch viel schwacher als die visuelle Sichtbarkeitsgienze (Große etwa 6m,5) sind, werden wesentlich unabhangig voneinander als mit der Belichtungsdauer wachsende runde Flecke abgebildet. Die Flache eines Scheibehens wachst jedoch nicht proportional zu der totalen wirksamen Belichtungseneigie, sondern langsamer Dei Einfluß der helleren Steine wird somit in der Photographie relativ zurückgehalten, wenn wir mit den Verhaltnissen bei der visuellen Beobachtung vergleichen Pannekokk<sup>2</sup>, der diese Tatsachen besonders ausemandergeset/t hat, hebt hervor, daß die visuellen Beobachtungen und die photographischen Aufnahmen zwei verschiedenartige Darstellungen der Milchstiaße bieten "Die Photographie zeigt die kleinsten Einzelheiten und Umegelmaßigkeiten, abei hauptsachlich in Steinpunktehen aufgelöst, nur mitunter von einer Flachentonung erganzt, und daher ist die richtige Gesamthelligkeit nur schwierig zu ermitteln. Das visuelle Bild erfaßt sofort die Gesamthelligkeit als solche, abei es gibt nur die grobere Struktur des Milchstraßenlichts wieder, in subjektiv abgerundeten Formen "

Eine andere Grundverschiedenheit der zwei Beobachtungsmeihoden liegt in dei Beweglichkeit des Auges, die es gestattet, in kurzei Zeit ein großes Areal an uberblicken und weit entfernte Punkte des Himmels unmittelbar nacheinander zu betrachten. Das bedeutet zwar in erster Linie eine Überlegenheit gegenübet det photographischen Kamera und ein notwendiges Mittel zur Überwindung der Unvollkommenheiten des Auges als optischen Instruments, aber es liegt doch in dei schnellen Diehung des Auges eine Quelle zur subjektiven Umforming des wahigenommenen diffusen Objektes Pannekoek schießt über diesen Umstand folgendes "In ausgedehnten Gebieten mit schwachen oder gleichmaßigen Lichtfluktuationen sucht das Auge Anhaltspunkte, um überhaupt etwas zeichnen und beschreiben zu konnen es sucht helle und dunkle Gebilde zu eikennen und findet sie oft in vollig zufalliger und peisonlicher Weise Reihen schwacher Steine 5 und 6 Große, die bei dem irrenden Herumtasten des Blickes die vorhandenen Lichteindrucke verstarken, rufen immer wieder das Bild deuthicher Lichtstreifen hervor, wo sich vielleicht gar keine großere Lichtmasse der wirklich teleskopischen Steine befindet Lichtstreifen, die Reihen sichtbarei Sterne folgen, finden sich ber allen Beobachtern, ohne daß es deshalb sicher ist, daß dem etwas Reales der Milchstraße selbst entspricht "Die photometrischen Messungen aber, die mit einem visuellen Flachenphotometei gemacht weiden, sind naturlich fier von Fehlern dieser Art. Die Vergleichung verschiedener Gegenden geschieht hier durch Anschluß an eine kunstliche Lichtquelle, die in

<sup>2</sup> Die nördliche Milchstraße, S 110

Ygl J Plassmann, Die Milchstraße als Gegenstand der Sinneswahrnehmung Z f Psychol (I) 88, S 120 (1921)

meßbarer Weise abgeschwächt oder verstürkt wird. Wir haben hier ein Mittel, ein objektives visuelles Bild der Milchstraße zu erhalten, das außerdem auf quantitativen Messungen der Helligkeit beruht. Wie vorher hervorgehoben ist, besteht jedoch noch die Schwierigkeit, den Eufluß der von Zeit zu Zeit variablen allgemeinen Himnelsbeleuchtung zu ehminieren

Wenn wir die Gesamtleistung der visuellen Methoden betrachten, müssen wir anerkennen, daß es schwer ist, auf photographischem Wege etwas Ähnliches zu erreichen. Wir haben oben von der Tendenz der photographischen Abbildung, die Struktur in Sternscheibehen aufzulösen, gesprochen Schon die Körnigkeit der lichtempfindlichen Substanz der Platten muß abei bewirken, daß bei genügend kleiner Fokaldistanz und also genügend kleiner Skala des Bildes die schwachen Sterne einer Milchstrußenregion in derselben Weise wie eine kontinuierlich leuchtende Flüche auf die Platte wirken. Um eine Schwärzung auf der Platte hervorzurufen, muß dann die gesammelte Intensität pro Efficheneinheit der Platte einen Minimumwert erreichen, was durch ein großes Öffnungsverhältnis des Objektivs befördert wird. Der in Winkelmaß ausgedrückte Durchmesser der Sternschelbehen, welcher bei vollkommener Abbildung dem Obiektivdurchmesser umgekehrt proportional sein sollte, wichst in der Regel mit dem Öffnungsverhältnis als ome Folge der unvermeidlichen Abblidungsfohler, die wesentlich Form und Größe der einzelnen Bilder bestimmen. Eine große Objektivöffnung bei kleiner Fokaldutanz bewirkt daher auch ein vollständigeres Zusammenfließen der Sternscheibehen einer gowissen Größenklasse, so daß man den Verhültnissen einer wirklichen Flächenabbildung nahekomint. Das Gebiet kontinulerlicher Schwärzung, welches durch das Zusammenwirken der Sterne entsteht, und seine Umgebung auf der Platte sind aber immer von uner mehr oder weniger lockeren Ansammlung von einzelnen oder in kleinen Gruppen zusammenfließenden Sternscheibehen besit. Die Begrenzung der kontinulerlichen Schwärzung wird daher wesentlich von der Optik des Linsensystems und von der Expositionszeit abhängig. Natürlich soll das Objektiv außer einem großen Öffnungsverhältnis auch ein großes nutzbares Bildfeld haben, um gleichzeitige Abhildung eines großen Areals des Himmels auf der Platte zu geben. Die optischen Abbildungsfehler des Linsensystems und die Vignettierung für schräg gegen die Achse verlaufende Strahlenbändel, deren Einfluß mit dem Abstande vom Plattenzentrum varnort, lasson aber eine Beartellung der relativon Intensitäten nur für ein ziemlich kleines Gebiet auf ein und derseiben Platte zu

Nichtsdestoweniger ist die Photographie für ein Studium der Einzelheiten des Milchstraßenbildes unentbehrlich. Durch das Zusammenfließen der Schelbchen an den dichten Stellen wird gegenüber den leeren eine starke Kontrastwirkung erzeugt. Wo das Auge nur strukturlese Lichtflecke wahrnlimmt, enthüllt die Photographie oftmals ein reiches, unendlich kompliziertes Spiel von Sternanhäufungen, leuchtenden Nebelmussen, wirklichen oder durch absorbierende Materie hervorgerufenen scheinbaren Sternleeren. Unsere jetzige Auffassung von der Struktur des Milchstraßenphänomens beruht daher in stärkstem Grade auf den photographischen Aufnahmen.

7. Die photographischen Arbeiten einzelner Forscher. Der Beginn der photographischen Milchstraßenforschung erfolgte durch E E Barnards erste Versuche im Jahre 1889 mit der "Willard Lense", einem Petzvalobjektiv von 15 cm Ölfnung und 78 cm Pokullänge, das später nach Umschleifung von Brashrar am "Crocker-Teleskop" der Lieksternwarte montiert wurde Einige der früheren von Barnard aufgenommenen Bilder sind in den orsten Bänden der

<sup>1</sup> MN 50, 5 310 (1890); Publ A S P 2, S, 240 (1890)

Zeitschriften "Astrophysical Journal" und "Populai Astronomy" ieproduziert worden. In dei letztgenannten Zeitschrift hat auch II C. Wilson¹ seine frühen Milchstraßenphotographien, die hauptsachlich mit einer der Barnardschen ahnlichen Linse aufgenommen sind, wiedergegeben. Eine großere Sammlung ausgezeichneter Reproduktionen hat Barnard erst im Jahre 1913 als eine Publikation der Licksteinwarte² herausgegeben. Die Reproduktion der Negative geschah nach der "Photogelatin"-Methode. Von hervorragender Schonheit sind besonders die Aufnahmen der steinreichen Sagittatus-Ophrüchus-Scorpius-Regionen. Die Bilder sind von Erlauterungen begleitet, die auf einer Analyse

det Originalnegative berühen Als em Beispiel soll die folgende sehr interessante Bemerkung zur Tafel N1 42, one Partie des westlichen Astes der Milchstraße um den Stein 58 Ophrucht (galaktische Lange 334°, Bieite +5°), mitgeteilt weiden "The very singular mass of aregular clouds that occupies the middle of the plate looks strange or out of place. It is quite unique in the milky way and does not give the impression of being clouds either of stars or of nebulous matter in its general makeup. In some respects these clouds have the appearance of being quite separate from the background of small stars, as if the masses were nearer to us. One would hesitate in passing on these as to their being nebulous, and yet the appearance does not suggest star masses. It, however, we examine the two small tufts at the left of the general mass, it will be seen that they are clearly made up of small stars which spread out in a scattering manner to the southeast from both masses, almost like coarse dust" In seinem untenerwahnten neuen photographischen Atlas Sagt Barnard von denselben Wolkenbildungen (Tafel 23) "They are probably entirely stellar, though this does not seem altogether certain. If stellar they probably are relatively very far away, though from their brightness this does not seem to be the case. Between us and these stars is a generous sprinkling of considerably larger stars , they are doubtless much nearer to us than the clouds" Die Lage dieser Wolke in einer Gegend, die wahrscheinlich nahezu emei Richtung gegen das Zentium des Milchstraßensystems entspricht, macht es moglich, anzunehmen, daß diese Wolke ein sehr entferntes Gebilde ist, dessen Platz im Raume vielleicht nahe am Zentrum oder vielleicht sogar in einer noch weiteren Entfeinung gelegen ist

Nach seiner Übersiedlung an die Yerkes-Sternwarte setzte Barnard mit dem 10/olligen Bruce-Teleskop, das er auf einige Zeit (1905) auch nach Mount Wilson brachte, seine Michstraßenaufnahmen fort. Seine Arbeit findet ihren Abschluß in der großartigen posthumen Publikation "A Photographic Atlas of Selected Regions of the Milky Way", die im Jahre 1927 von der Carnegie-Institution unter Redaktion der Yerkes-Sternwarte herausgegeben wurde. Die Karten sind photographische Kopien von sekundaren Negativen, die besonders hergestellt wurden, um einen größeren Kontrast oder größere Starke als die Originalnegative zu geben. Ein zweiter Teil des Werkes dient als Schlussel une enthält für jede Karte ein gleich großes Blatt, wo die helleren Steine der Bonner oder Cordobaer Durchmusterung eingezeichnet und alle bemerkenswerten. Ob jekte aufgenommen und numeriert sind. Jedes Blatt enthalt auch die Eckpunkte

emes aquatonalen Koordinatennetzes

Die Einleitung zum eisten Teil gibt eine ausführliche Bibliographie übe die Aibeiten von Barnard, die in irgendemei Weise die Photographie von Michstraßenobjekten berühren

Ungefahr gleichzeitig mit Barnards ersten Versuchen hat H C Russell auf der Sidney-Sternwarte mit einem Dallmeyerschen Objektiv von 6 Zol

<sup>&</sup>lt;sup>1</sup> Pop Astr 3, S 58 (1895) <sup>2</sup> Publ Lick Obs 41 (1913) <sup>3</sup> M N 54, S 39 (1890

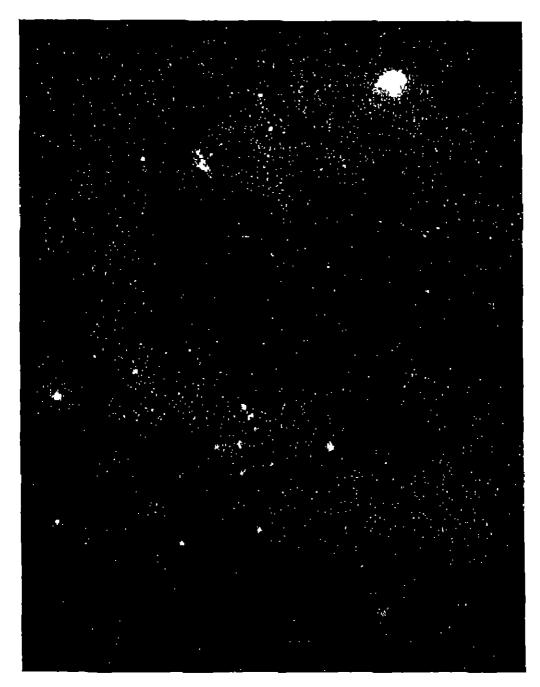


Abb 4 Milchstraße in Taurus, Auriga und Persons. Aufnahme von M Wolf mit Zoks-Tessar (31/145 mm) Belichtung 5 Stunden 2 Minuten

Öffnung Aufnahmen der sudlichen Milchstraße und der Magellanschen Wolken gemacht. Unter den interessanten Bemerkungen, die er an seine Aufnahmen



Abb 5 Umgebung von 8 Monocerotis Aufnahme von M Wolf mit dem 1620ligen Blucc-Refraktor (40/202 cm) Belichtung 5 Stunden 18 Minuten

knupft, kann ei wahnt weiden, daß er als erstei eine vei wischte Spiialstiuktui in dei Nubecula Majoi zu schen behauptet

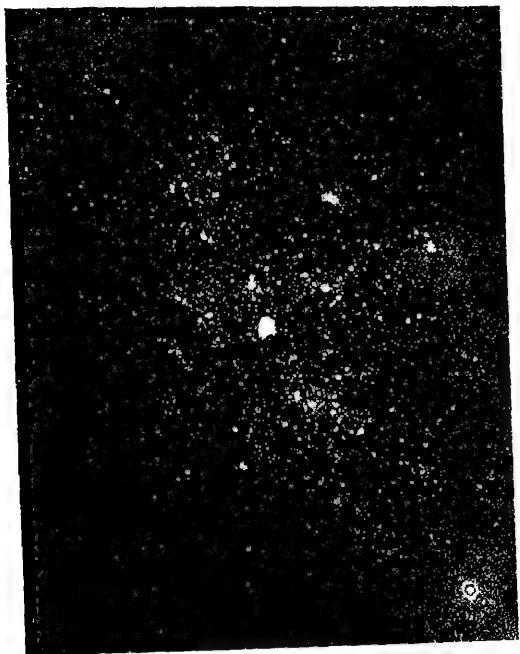


Abb 6. Umgobung von y Cygni Aufnahme von M Wolly mit dem Bruce-Refraktor Belichtung 6 Standen 50 Minuten

M Work ist nebst Barnard einer der erfolgreichsten auf dem Gebiete der Milchstrußenphotographie. Auf der Sternwarte Königstuhl, Heidelberg, hat Work mit dem 16kbilligen "Bruce-Refraktor" und auch mit kurzbrennweitigen Objektiven (besonders zwei Zeiss-Lessaten von 31 mm Offnung und 145 mm Biennweite) in großem Umfang verschiedene, und zwai meistens nordliche Gegenden der Milchstraße photographisch aufgenommen. Mehrere der Wollschen Aufnahmen sind oft in Lehrbuchern und Monographien als Illustrationsmaterial reproduziert worden. Vollständigere Sammlungen hat Wolf in den Werken "Die Milchstraße" (Leipzig 1908) und "Die Milchstraße und die Kosmischen Nebel" (Verlag Die Steine, Potsdam 1925) herausgegeben. Das letzteie Werk enthalt 16 ausgezeichnete Lichtdrucke von Milchstraßenpartien und Nebeln

Einige Prachtstucke dei Wolfschen Aufnahmen beziehen sich auf die Milchstraße im Sternbilde (ygnus, speziell auf die große (ygnuswolke, die viele Einzelheiten von großem Interesse zeigt. Einige bemeikensweite Erscheimungen, z. B. der "Amerikanebel" und der "Kokonnebel", sind besonders durch Wolfs Aufnahmen in ihren Einzelheiten klargelegt worden. Im ganzen hat Wolfsbewundernsweite Aufnahmen aller Gegenden der Milchstraße von Scutum bis Monoceros gemacht. Durch Geheimrat Wolfs freundliches Entgegenkommen werden hier einige von seinen Aufnahmen in Abb 4 bis 6 reproduziert.

Die Milchstraßenzeichnung von Goos, die nach Worrs Aufnahmen hergestellt ist, wird unten in Ziff 8 besprochen

Unter den wichtigsten Milchstraßenaufnahmen sind weiter die sehr schonen Photographien der sudlichen Milchstraße zu nennen, die von S. I. Balli v. Hanover in der Kapkolome mit einem Cooke-Objektiv von 1½ Zoll Öffnung und 13 Zoll Breinweite aufgenommen worden sind. Diese Aufnahmen bilden eine wertvolle Erganzung zu den Barnardschen und Wolfschen Aufnahmen der nordlicheren Gegenden. Die strukturieiche Zeisplitterung der Milchstraße von A. Centann aus nach wichsender galaktischer I ange hin und die große Machtigkeit der Wolkenbildungen in den Langen 300° bis 360° treten hier in imposanter Weise hervor

Die Arbeit winde spater in der nordlichen Milchstraßes fortgesetzt die zur Umspannung des ganzen Milchstraßengurtels erforderlichen Photographien wurden von W. H. Pickering auf Jamarka und von Barrey in Cambridge, Massachusetts, hergestellt

Ein interessanter Versuch, aus einem Material von Harvard-Platten ein photographisches Bild der Milchstraße in den Regionen zwischen Crux und Aquila zusammenzusetzen, ist von H Sitapier gemacht worden und wird hier durch Herrin Shapiers Enigegenkommen in Abb 7 ieproduziert. Interessant ist ein Vergleich zwischen diesem Bild und der Herscherischen Zeichnung in Abb 1

Von großtei Bedeutung als photographische Darstellung der Milchstraße, besonders in ihrem sudlichen Verlauf, ist die über den ganzen Himmel sich erstreckende Franklin-Adams-Karte³ Die Aufnahmen wurden von J Franklin-Adams mit einem Taylor-Objektiv von 40 Zoll Öffnung und 45 Zoll Breinweite zu Mei vel Hill, Godalming, in England in den Jahren 1905 bis 1909 und spater zu Johannesburg in Sudafrika gemacht. Da die Fokallange bedeutend großer ist als bei Bailleys Instrument, erscheinen die Steinwolken hier weit inehr aufgelost. Viele Gegenden der sudlichen Milchstraße, in Grux und Sagittarius, zeigen jedoch die komplizierte Struktur der ungeheuer dichten Steinwolken in außerordentlich auffalligem Kontrast gegen die benachbarten Steinleeren und gegen die gleichförmigeren steinarmeren Gegenden hoherer galaktischer

I Harv Ann 72, Ni 3 (1913)
 I Harv Ann 80, Ni 4 (1917)
 Franklin-Adaus-Chart, R Astronomical Soc (London 1921)

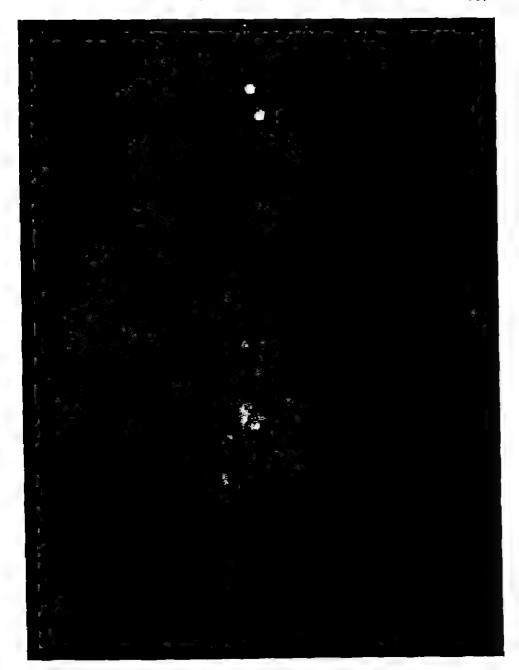


Abb 7 Zusammengesetztes Blid der zentralen Mijchstraßengegend swischen Crux und Aquila nach mit einem Ross-Tessar-Objektiv zu Arequipa aufgenommenen Platten

Breite Die Reproduktionen (Franklin-Adams-Karten) wie die Originalplatten selbst, die zu Greenwich aufbewahrt werden, sind schon von großer Bedeutung für mehrere Arbeiten in der Stellarastronomie gewesen

Unter neueren Milchstraßenaufnahmen sind / B die von E II Collinson<sup>1</sup> mit einem Anastigmaten 1 3, mit 6 Zoll Brennweite, gemachten zu erwähnen

Eine hohe Entwicklung der photographischen Technik ist aber besonders in den Aufnahmen von F E Ross² eitericht worden Mit einem Objektiv seiner eigenen Konstruktion (3 Zoll Offnung, 21 Zoll Brennweite) hat ei mit vielstundigen Expositionszeiten überaus schwache Nebelschleier in Orion, Monoceros, Lamus und Perseus photographieit. Bei solchen Objekten hangt der Erfolg, außei von dei Empfindlichkeit der Platten, sehr stark von einer kontrastreichen Reproduktion der Originalnegative ab. In dem Reproduktionsprozeß benutzt Ross panchromatische Platten mit Rotfilter. Er macht auch wichtige Bemeikungen über die Gienzglößen verschiedener Instrumente, wenn es sich um die Aufnahme von Sternen handelt. Es zeigt sich, daß für schwache Sterne gewissermaßen ein langbrennweitiger Refraktor einem Reflektor gegenüber an Wirksamkeit gewinnt infolge der kleineren Dimensionen der Sternscheibehen und der größeren Reduktion der Himmelshelbigkeit.

8 Milchstraßenzeichnungen auf Grund photographischer Aufnahmen. Photographische Photometrie der Milchstraße Eine Zeichnung dei Milchstraße auf Grund photographischer Reproduktionen ist zueist von Easton³ publiziert worden Sein Material war eine Kompilation der Aufnahmen verschiedener Milchstraßenregionen von Barnard, Wolf, Pickering, Russell, Bairey und anderen Die Zeichnung gibt in einer "zurkularen" Projektion die Milchstraße zwischen den galaktischen Breiten +20° und -20° In einer spateren Arbeit hat er eine in außerst feine Einzelheiten ausgearbeitete Karte der nordlichen Milchstraße gegeben

Die Wolfsche Sammlung von Milchstraßenaufnahmen ist im besonders genauer Weise von F. Goos zu einer zeichnerischen Konstruktion des nördlichen Milchstraßenverlaufs benutzt worden. Die mit den Zeiss-Tessaren aufgenommenen Milchstraßenbilder wurden in ein einheitliches Kartennetz eingezeichnet. Die vielen Steinhaufen, Nebel und Kanale wurden mit großter Sorgfalt wiedergegeben, wober der Zeichner sich bemuht hat, alles subjektive Vormterl auszuschalten, und nur zu zeichnen, was die photographische Platte zeigt. Die Helligkeitsverhaltnisse im großen wurden durch diekte Beobachtung am Himmel und durch Anlehnung an altere diekte Zeichnungen, besonders die von Easton, moglichst wahrheitsgetieu wiedergegeben. So ist eine Zeichnung entstanden, mit der an Darstellung der Einzelheiten keine durch diekte Augenbeobachtung erhaltene verglichen werden kann

Goos hat auch in verdienstvoller Weise die Zeichnungen von Heis, der Uranometria Argentina, von Easton, Boeddicker und Houzeau in dieselbe Kartenprojektion umgezeichnet, was für die Kenntnis der zur Zeit teilweise schwer zuganglichen alteren Zeichnungen von Bedeutung ist

Eine sehr bemerkenswerte Zeichnung der ganzen Milchstraße auf Grund von Reproduktionen der Baileyschen Platten und von eiganzendem photographischen Material hat kuizlich K. Lundmark unter technischer Mithilfe von O Jahnke heigestellt und in Druck vervielfaltigt. Durch Heirn Lundmarks Entgegenkommen und diese Karte hier in einer Tafel reproduziert. Sie findet sich auch in Reproduktion in Lundmarks Neubearbeitung eines Werkes von Arrhenius<sup>6</sup> und im Handbuch der Physik<sup>7</sup>

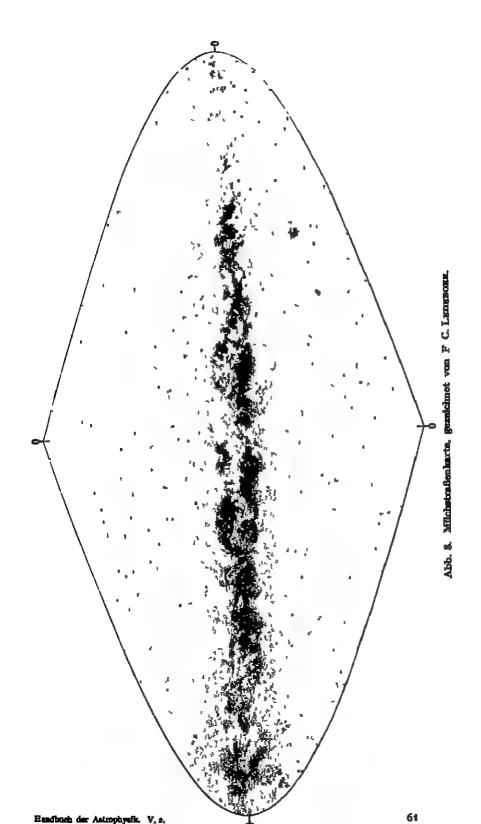
<sup>&</sup>lt;sup>1</sup> JBAA 37, S 132 (1927)

<sup>2</sup> Ap J 65, S 137 (1927), 67, S 281 (1928)

<sup>3</sup> Ap J 37, S 105 (1913)

<sup>4</sup> MN 89, S 207 (1928)

Die Milchstraße, mit einem Geleitwort von Professor Max Wori Hamburg 1921
 Världarnas utveckling Stockholm 1929
 IV (1929), Tafel



Auf der Stockholmei Steinwalte hat F.C. Lldebolk eine Zeichnung über den Verlauf der Milchstiaße in Flamstelds Piojektion nach galaktischen Kooldinaten ausgeführt (Abb. 8). Von dieser Kaite ist auch eine kleine Auflage im Druck herausgegeben worden. Als Vorbild dienten zum Teil die Zeichnung von Goos, besonders aber Reproduktionen der Bahleyschen und anderen Harvard-Photographien, die von Heim Shapley wohlwollend zur Verfugung gestellt worden sind, weiter auch für die Beurteilung der ielativen Intensitaten verschiedener Partien die Karten von Pannekopk

Unseie durch die Photographie erlangte Kenntnis der allgemeinen Lichtverteilung im Milchstraßengebilde ist bisher wesentlich nur von qualifativer Art geblieben Eine wichtige Arbeit, in der eine quantitative photographische Photometrie dei nordlichen Milchstiaße begründet wird, hat abei Panni korka ausgeführt, unter Benutzung eines von M Wolf auf der Sternwarte Heidelbeig angesammelten Plattenmaterials Die Platten wurden mit einem kleinen Tessarobjektiv von 33 mm Offnung und 145 mm Biennweite extialokal aufgenommen, und die Ausmessung geschah mit einem Harimannschen Mikrophotometer des Astronomischen Institutes zu Amsteidam Die Gradation der Platten für schwäche Intensitäten wurde aus den extrafokalen Sternscheiben dadurch ermittelt, daß die Differenz zwischen der Schwätzung eines Scheibehens und der kontinuterlichen Schwärzung der unmittelbaren Umgebung auf der Platte als Funktion der bekannten Helligkeit des Steins angesetzt wurde, wobei Koriektionen fur wechselnde Größe der Scheibehen auf der Platte, Unregelmäßigkeiten in der Lichtverteilung m den Scheibehen usw angebracht wurden. Die photographische Himmelshelligkeit eines Punktes winde dann aus der Differenz zwischen der Schwärzung ım betreffenden Punkt auf dei Platte und im unbelichteten Teil dei Platte berechnet Nach Berucksichtigung von Mittelpunktskorrektion und Nullpunktskonektion für die einander in großem Umfange überdeckenden Platten sind endlich die Intensitaten, wie sie auf jeder der 35 Platten für die Eckpunkte eines engmaschigen Netzes gefunden worden sind, auf 35 Kaiten wiedergegeben Einheit der Intensität ist die Helligkeit eines Steins 10 Große pio Quadratgrad Die Karten sind auch in einem Gesamtbilde zusammengefugt worden -- Die Beseitigung der systematischen Fehlerquellen hat in der Arbeit viel Schwierigkeit gemacht, und unerklärte Differenzen zwischen einander teilweise überdeckenden Platten treten auf Sie entstehen teils durch unberechenbare Einstitsse von Extinktion und von fremdei Erhellung des Himmelsgrundes Es ist auch nicht möglich, exakt anzugeben, für welche Große die Sterne auf den Platten noch einzeln als Scheiben sichtbar sind. Eine ähnliche Unbestimmtheit besteht abei auch, wie wir oben geschen haben, für visuelle Beobachtungen — Auf dei Bosschu-Sternwarte zu Lembang werden gegenwartig extiafokale Aufnahmen dei Südlichen Milchstraße für eine ahnliche Arbeit gemacht

## d) Das allgemeine Bild der Milchstraße nach den visuellen und photographischen Beobachtungen,

9. Der Verlauf der Milchstraße am Himmel in großen Zugen. Als hellste Flecke der Milchstraße können zwei in Sagittatius und Scutum gelegene I ezeichnet werden. Der erste und großere erstreckt sich südlich von  $\mu$  Sagittatit gegen  $\gamma$ ,  $\delta$  und  $\lambda$  desselben Sternbildes. An diesen Fleck schließt sich im Süc en eine nur weing schwächere Masse gegen z und  $\eta$  Sagittatit und gegen die charakte-

<sup>&</sup>lt;sup>1</sup> Eine Reproduktion dieses Druckes findet sich in K Svenska Vetenskapsakademichs Arsbok 1930.

<sup>&</sup>lt;sup>2</sup> Publ Astr Inst Univ Amst, Nr 3 (1932)

ristische Sterngruppe in der Schwanzsputze des Skorpions (G, i, x, i Scorpii) an, sie erscheint besonders hell um den Sternhaufen M7 herum. Diese ganze Partie der Milchetraße ist als die große Sagittariuswolke wohlbekannt und bildet den hervorragendsten Teil des östlichen Milchstraßenastes oder Hauptastes. Das Intensitätsmaximum der Wolke, wenn wir vom hollen Fleck um M7 herum abschon, liegt nördlich von y Sagattarii und südlich von dem Nebel M8 und dem Trifldnelzel, die als helle Knoten am Rande des dunklen Zentralgebiets, das hier die Milchstralie in zwei gewaltige Aste teilt, erscheinen Gegen dieses Zentralgebiet füllt die Intensität der Wolke sehr schnell und in einer sehr verwickelten Struktur ab

Vom südlichsten Gobiet der Wolke bei M7 geht fiber den Sternhaufen M6 eine schwache Lichtbrücke gerade bls zum westlichen Ast hinfiber, der sich hier in der weitgestreckten hellen Lichtmasse zwischen a Scorpii, a Scorpii und Ophluchi ausbreitet. Nördlich von dieser Masse wird der westliche Ast durch cinon dunklen Kanal durchquert, der von dem o Ophluchi-Nebel ausgeht und der sich über die Milchstraße nördlich und östlich von & Ophinchi in der Form eines gewaltigen Ankers ausbreitet. In der Nähe von Ø Ophsuchi sind in dieser Formation einige schr dunkle Partien zu finden. Auf der anderen Seite des Kanuls, von Ø Ophinchi aus, finden wir einige weniger helle, aber doch machtig erscheinende Wolken, die zum Teil ihrer "Fernkörugkeit" wegen sehr merkwirdig sind (vgi BARNARI), Ziff 7), und die ihrerseits gegen Norden hin von einem müchtigen dunklen Goblet begrenst and, das wie ein etwas gebogener Keil von Südwest her in die Milchstraße einsetzt, seine Spitze ungefähr in der galaktischen Länge von Altuir hat und den westlichen Ast in Ophiuchus in zwei weit getrennte Portien teilt. Die Spitze des Keils bildet auch die stellenweise schr dunkle Trennungsreglen zwischen dem östlichen und dem westlichen Ast der Milchstrate in den Sternbildern Serpens und Aquila. Die Trennung ist hier welt stärker markiert als in den Regionen von Sagittarius und Scorpius, wo die Trennung der zwei Aste überhaupt sehr uregulär und aft von hellen Brücken unterbrochen erschelnt.

In dem Ostlichen Ast ist die helle Verbindung zwischen Sagittarius- und Scutumwolke durch mehrere durchquerendo dunkle Kanale gestert, vor allem durch den zwischen & und y Scuti gelegenen, der an einigen Stellen sehr dunkle Gebiete ausweist. Sehr helle Flecken finden sich nördlich von  $\mu$  Sagittarii, ziemlich in der Zentrulimie der Milchstraße (kleine Sagittariuswolke) und um y Scuti herum. Die große Wolke in Scutum ist nach Barnard "the gem of the Milky Way, the finest of the star clouds" Der hellste Fleck befindet sich südlich von β Scutl In östlicher Richtung verbreitert sich die Wolke und nimmt das Licht sanft ah; das schwächste Milchstraßenlicht ist hier weit in südliche galaktische Breite zu verfolgen Die Wolke zeigt nach BARNARD eine gleichförmigere Fläche, als die Milchstrationwolken im allgemeinen Eme Anzahl sehr dunkler Flecke zeichnet sich außerordentlich schart gegen die nördliche Partie der Wolke ab, besonders unmittelbar nördlich vom Sternhaufen M11

Nördlich von der Scutumwolke wird der östliche Ast durch das Sternbild Aquila hindurch fortgesetzt. Von der dunklen Durchquerung bei A Aquilae an der Grenze der Scutumwolke aus geht der Lichtstrom weiter gegen Norden und bildet nach einer dunklon Durchquerung bei d Aquilae den hellen Fleck unmittelbar westlich von y Aquilae, der sich weiter nördlich in der hellen Partie im kleinen Sternbild Sogitta fortsetzt.

Der woniger ausgeprägte westliche Ast geht der nördlichen Seite des dunklen Gebletes in Ophluchus entlang in nordöstlicher Richtung und bildet zwischen β Ophluchi und & Aquilae eine langliche Wolke Dann folgt wieder eine weite dunkle Region Schwache Verbindungsstiome gehen von der eben genannten Wolke nach Sagitta und in einem Bogen gegen die sudwestlichen Auslaufer der großen Cygnuswolke. Die dunkle Trennungsregion zwischen dieser westlichen Ophruchus-Aquilawolke und der Cygnuswolke setzt in ahnlicher Weise wie das sudlichere dunkle Gebiet in Ophruchus in die Milchstraße ein. In der Form eines gebeugten Armes geht sie von den Sternbildern Lyra und Hercules gegen Sagitta, wo sie umbiegt, und von hier aus der Zentrallinie der Milchstraße entlang zwischen  $\varepsilon$  und  $\gamma$  Cygni gegen  $\alpha$  Cygni. Die Region zwischen  $\alpha,\gamma$  und  $\lambda$  Cygni, welche die geballte Hand des "Armes" darstellt, ist sehr dunkel. Dieses Gebiet ist zum Teil von den machtigen unregelmaßigen Nebeln nahe  $\gamma$  Cygni und  $\alpha$  Cygni ("Amerikanebel") begrenzt. Von hier aus geht weiter ein bierter dunkler Kanal in westlicher Richtung, der die nordliche Begrenzung der großen Cygnuswolke bildet

Die große Cygnuswolke steht mit der Paitie des östlichen Astes in Sagitta mittels einer schwachen Lichtbrucke zwischen  $\gamma$  Sagittae und  $\beta$  Cygni in Verbindung Diese Wolke hat einen fast ellipsenformigen Umiiß, mit der größeren Achse zwischen den Steinen  $\beta$  und  $\gamma$  Cygni, und bildet unzweifelhaft mit ihrei nachsten Umgebung eine der interessantesten Partien der ganzen Milchstraße Gegen die dunkle Trennungsregion im Osten fallt die Intensität ziemlich steil ab, wahrend gegen das Sternbild Lyra hin die Lichtstarke in sanfter Weise abnimmt. In der Mitte der Wolke, um  $\eta$  Cygni herum, liegt eine dunklere Region

Vom Sternbilde Sagitta geht als eine Fortsetzung des ostlichen Astes ein schwacher Lichtstrom gegen s und & Cygnt, der notdlich von diesen Sternen an Intensitat gewinnt und dann in stetiger Konvergenz gegen die zenitale Milchstraßenlime über o und 7 Cygni duich die Sternbilder Lacerta und Cassiopeia lauft, um in der dunklen Region um y Persei herum seinen Endpunkt zu finden Dieser Strom kann als Hauptstrom bezeichnet werden. Am nördlichen Rande dieses Stromes eischeinen einige Wolkenbildungen, die vielleicht als eine Foitsetzung des westlichen Milchstraßenastes angesehen werden konnen So erscheint ostlich von a Cygni die helle und sehr konzentiierte kleine Cygnuswolke, die m einem Bogen über α, o<sub>1</sub>, o<sub>2</sub> und δ Cygni mit der großen Cygnuswolke in schwacher Verbindung steht Nordlich von der kleinen Wolke liegt das tiefdunkle Gebiet, das als "nordlicher Kohlensack" bezeichnet wird. Von diesem erstreckt sich in sudostlicher Richtung ein dunklei Kanal, der schließlich nahe den Sternen A und o Cygni den Hauptstrom durchquert und damit die kleine Cygnuswolke von dem kleinen hellen Gebiet um  $\pi_1, \pi_2$  und g Cygni trennt Ziemlich weit nach Norden hin vom Hauptstrome aus erstieckt sich die schwache Cepheuswolke zwischen a, & und i Cephei Gegen Cassiopeia hin teilt sich der Hauptstrom gewissermaßen in Lichtstreifen, die von dunklen Gebieten (& Cophei bis 4 Cassiopeiae, 1 H bis \( \beta \) Cassiopeiae) getiennt sind. Nordlich von einer Verbindungslime zwischen  $\beta$  und  $\varkappa$  Cassiopeiae liegt ein Lichtmaximum, das sich m sudlicher Richtung über α Cassiopeiae in schwächeren Lichtmassen fortsetzt. Die Gegend bei  $\delta$  Cassiopeiae vereint sich mit den Perseushaufen h und  $\chi$  in einem langgestreckten hellen Fleck auf der Zentrallinie, der sich schließlich in das weitgestreckte Dunkelgebiet um y Persei herum verliert. Eine schwache, bogenformige Lichtbrucke über 9 Persei vereint die erwähnte helle Partic mit einem kleinen Lichtmaximum unmittelbar sudlich von a Persei. Auf der Nordseite geht ein mit der Zentrallinie paralleler Lichtstreifen über e Cassiopeiae zum Dunkelgebiet in Perseus

In der Perseus-Camelopardalis-Region ist die Milchstraße nur sehr schwach markiert, gewinnt aber in Auriga wieder an Intensität. In der Gegend um  $\eta$  Geminorum herum hat die Milchstraße eine eigentumliche Struktur, von hier

aus gehen nach allen Seiten helle und dunkle Streifen wie von einem Zentrum<sup>1</sup> BARNARD<sup>a</sup> macht die wichtige Bemerkung, daß in dieser Himmelsregion auf der nördlichen Seite der Milchstraße ein allgemeiner schwicher Lichtschimmer viel weiter zu verfolgen ist als auf der südlichen, gegen Orion hin, während in der diametral entgegengesetzten Sagittarmsregion der Lichtschimmer auf der Südseite der Milchstraße weiter ausgedehnt als auf der Nordseite erscheint. Von dem genannten Punkto in Gemini weiter südlich verläuft die Milchstraße als ein memlich emholtliches, schwaches, aber an Intensität wachsendes Lichtband durch die Sternbilder Monocoros und Canis major hindurch, um im Sternbilde Puppis eine etwas verwickeltere Natur zu zeigen. In stidestlicher Richtung von m Puppis, mit & Puppis nahe auf der Westseite, zieht ein langgestrecktes, von der Zontrallinie gegon Süden divergierendes dunkles Gebiet. Dieses wird von einer hellen Partie östlich von y Valorum im wesentlichen überbrückt und geschlossen Bel a—b Velorum zeigt diese Partie ein kleines Gebiet von betrüchtlicher Halligkeit Stidlich von dieser Stelle erweitert sich aber eine dunkle Region gegon beide Selten der Milchairaße, so daß zwischen y und d Volorum eine breite dunkle Durchquerung, auf die wohl zoerst J HERSCHEL! aufmerksam gemacht hat, zustande kommt Von hier aus wächst die allgemeine Intensität der Milchstraße schr schnell und verfüngt sich gleichseitig der Lichtstrom, um in die schmale, aber sehr helle Muchstraßenpartie in Carina überzugehen

Die Carinawolke zeigt gegen den Südpol hin einen sehr schnellen Intensitätsabfall; nach onem sehr konzentrierten Helligkeitsmaximum um n Carinac herum bildet sich gegen A Centauri eine sehr merkierte dunkle Embiegung in der intensiv leuchtenden Masse. In Crux wird der Strom breiter und umschließt den großen, dunklen, zentral gelegenen "Kohlensack" östlich von & Crucis. Diesos birnenförmige Oval hat eine größte Länge von etwa 8° und eine größte Breite von etwa 5° Dor helle Lichtstrom wird dann immer hrenter, bei & Centaurl wird durch eine langgestreckte, im Stornbilde Norma gegen Norden hin umgebengte dunkle Masse ein westlicher Ast abgesondert, der in wachsendem Abstand von der Zentrallinie der Milchstraße und mit abnehmender Intensität sich schließlich mit der hellen Partie des westlichen Milchstraßenastes in Scorpius vereint.

Der östliche Hauptstrom hat ein starkes Intensitätsmaxinum in Norma und sondert dort noch einen Strom gegen die westliche Scorpiuspartie ab. Der hier abgesonderte Strom wird jedoch in mohreren Punkten, bei y Normae, bei ζ Scorpii und zwischen μ und e Scorpii, durch dunkle Risse durchquert. Der östliche Hauptstrom wird durch die Spaltung nach Süden gedrückt und verliert zuerst bedoutend an Intensität, gewinnt aber in Scotplus und Sagittarius wieder an Stärke und trifft endlich über die Schwanzsterne des Skorpions mit der großen Sagittariuswolke zusammen. Bel den eben erwähnten Sternen erweltert sich die Lichtmasse gegen den westlichen Ast hin, so daß hier von & bis \( \mu \) Scorpii eine weite Überbrückung zwischen den zwei Hauptästen entsteht Zwischen dieser Lichtbrücke und der vorher erwähnten, über die Sternhaufen M7 und M6 gehenden liegt bel 1 und v Scorpii eine welte dunkle Höhle.

10. Die Magellanschen Wolken. Die zwei Gebilde des Stidhimmels, die als die Magellanschen Wolken (auch die Kapwolken oder die zwei Nubeculae, (N major und N. minor) bezeichnet werden, aind oftmals als "versprengte Stücke der Milchstraße" bezeichnet worden, wenngleich ihre vollkommene Abgeschlossenheit von der Milchsträße selbst schon von J Herschel ausdrücklich betont

PANNERGER, Die nördliche Milchetraße, S. 76.

Photographic Atlas I, S. 10.

Results of Astronomical Observations, S. 384 and Pl XIII (in Abb 4 oben reprodu-

from the best observational data and the curve computed according to the theory is good, indeed. The average of the residuals is  $\pm 0^{M}$ , 56, most of which might fairly be attributed to errors in the observational data, and the maximum discordance is 1<sup>M</sup>.7 Certain refinements of the nature of a second approximation are suggested by Eddington, who derives the following relation between a change in the molecular weight and a change in the absolute magnitude1

$$-\Delta M = \frac{9\beta + 8}{4 - 3\beta} \log e^{\frac{\Delta \mu}{\mu}}$$

At the time this investigation was carried out the first approximation certainly sufficed. The accumulation of further data since then may invite us to make a second approximation

The masses of the Cepheids were computed on the basis of the pulsation theory The method is that of successive approximations. A value of M is assumed From To (spectral class) the radius is deduced and then the mean density The central density  $\varrho_o$  is 54,25 times the mean density. The period Pis then obtained from the expression

$$P \varrho_{o}^{\frac{1}{2}} = 0.29 (\gamma \alpha)^{-\frac{1}{2}}$$

where  $(\gamma a)^{\frac{1}{2}}$  is taken from M N 79, p 15, table V with  $1-\beta$  as argument. The process is repeated until P stands. The highest value is 26,20 for Y Ophruchi and the lowest 4,14 @ for RR Ly1ae

EDDINGTON inquires if, assuming that the gas-laws hold good for ordinary stars, we then should expect that each star will have the precise luminosity deducible from its mass and effective temperature or, in other words, whether the theory is accurate individually or only statisfically. The sources of residual differences are principally abnormal composition and abnormal rotation. With regard to the first source an unduly large proportion of hydrogen would make the stai fainter. With regard to rotation it has been shown by E.A. Milne that a rapid iotation makes the star slightly fainter, but that the effect is very small until the speed is sufficient to deform the star considerably. What is to be feared, concludes Eddington, is that the observed spectrum misleads us concerning the true value of  $T_a$ . An unsuspected binary ought to betray itself by having a magnitude fainter than that predicted from a knowledge of its combined mass

The very interesting theoretical considerations as to whether it is physically likely that a dense star such as our Sun can obey the laws of a perfect gas cannot be given here The student is referred to § 9 in Eddington's paper

The high density of the white dwarfs is not abound. At a very low effective temperature smaller than that of a dwarf of spectral class M the star Sirius B is probably able to produce in some way "an imitation of leading features of the F spectrum sufficiently close to satisfy the expert observer" The deviation of this star from the mass-luminosity curve is not surprising if the density is 53,000  $\odot$  new considerations enter into the calculation of k, since the elections are in the capture zone of two or more nucler simultaneously. Also the deviation from the gas-laws may be considerable. On the other hand the star  $o^2$  Eridani B agrees quite well with the mass-luminosity relation.

In Kramers's theory the absorption coefficient k contains an additional factor  $\infty (1 + h r_1/RT)$  The effect of this factor was calculated and found to vary between +0,2 and -1,6 There are general reasons for accepting a correction factor of this form, which represents the ratio of the energy given up on capture

<sup>&</sup>lt;sup>1</sup> M N 84, p. 323 (1924)

VAN HERK findet durch Vergleich mit PANNEKOERS Resultaten, daß die hellste Partie der Scutumwolke erheblich heller als die hellsten Stellen der Magellanschen Wolken ist. Für die integrierte photographische Gräße in der gewähnlichen Skula findet er für zwei Platten

Pür die kleinere Wolke hat Shapley eine photographische Größe zwischen 4-2m und | 3m und J 5 PARASKEVOPOULOS +1m,8 angegeben Hertzsprungs obenerwähnte visuelle Flächenholligkeit entspricht 424 Sternen der Größe 10m pro Quadratgrad Man muß wohl hier aber bei dem Vergleich mit van Herks klemerem Wort in Betracht ziehen, daß wir wahrscheinlich mit einem Farbenindex der Wolken von etwa +0m,5 zu rechnen haben

11. Die Lage der Milchstraße. Die zentrale Linie des Milchstraßengürtels folgt sehr nahe einem größten Krais am Himmel Für den Pol dieses Kreises sind mehrere Bestimmungen gemacht worden W Herschelß gibt die Koordinaten RA = 186°, Deki = +32° für das Aquinoktium 1785 Die Werte von ARGKLANDER<sup>4</sup>, mus Bones Darstellung der Milchstraße in seinem Atlas bestimmt, und von F W. STRUVE haben nur historisches Interesse, sind aber schon mit den heutigen Werten nahe übereinstimmend. Houzeau benutzte die Koordinaten sciner 33 Punkte maximaler Helligkeit und berechnete, von Stroves Pol ausgehend, in einer Ausgleichung nach der Methode der kleinsten Quadrate den Pol des größten Kreises, der sich diesen Punkten am besten anschmiegt. Einmal rechnet er mit gleichem Gowichte für alle Punkte, ein zweites Mal mit Gewichten nuch den Helligkeiten. Eine Ausgleichung desselben Materials unter Einführung der Nordpoldistanz  $\sigma$  des Kreises als unbakannte Größe in die Gleichungen haben RISTRAPART und KOROLD unternommen Das Resultat von Kobold ist in der ersten Zeile der Tubello 5 aufgeführt. Die Tabelle gibt auf das Äquinoktium 1900 reduzierte Werte (außer für Newcomb, der sein Aquinoktium nicht angibt) der zur Zeit besten Bestimmungen, die auf Zeichnungen und photomstrischen Beobachtungen der Milchstruße beruhen

Huiss lint eine Bestimmung aus seinen Milchstraßenzeichnungen im Atlas Covlestis Novus gemacht, die nicht sehr von Goulds und Newcomes<sup>10</sup> Resultaten abwelcht, die aus Bearbeltungen der Milchstraßenzelchnungen um Atlas Coelestis Novus und in der Urunometria Argentina herrühren Besonders Gouldes Resultat

lst sehr viel benutzt worden

Rine Bestimmung auf Grund der Goosschen Darstellung der nördlichen Milchstralio ist von C. Wirtz<sup>11</sup> gemacht worden Diese Bestimmung behandelt aber die belden Arme der Milchstraße getrennt (vgl. wester unten). Graffia und Hopmann 18 haben weiter ihre photometrischen Messungen zur Lösung der Aufgabo benutzt

Hinsichtlich der Daten, die man zur Bestimmung der Symmetrieebene hernnziehen kann, sind in Anschluß an Pannekoeks Ausführungen die folgenden

Typen zu unterscheiden.

```
Harv Circ 260 (1924)

Harv Bull 840 (1926).

Phil Trans 75, S. 253 (1785), Collected Scientific Papers I, S. 251

Bonner Boobschtungen V. 3 (1862).

Btudes d'Astronomic Stellaire, S. 62 (1847)
                                                                                   Herv Bull 840 (1926).
```

Untermohungen über die Constants der Pracession, S 63 Karlaruhe 1892

Dor Hau des Tixsternsystems, S 184 (1906).

Vorrede zum Atlas, vgl Hauen, A N 217, S. 291 (1922).

Uranometria Argentina, S. 371.

Publications of the Carnegle Inst. of Wushington, No 10 (1904)

V J S 57, S. 22 (1922)

II A N 213, S. 27 (1921).

J A N 222, S. 92 (1924)

a) Man kann von den Randern ausgehen und tiberall die Mittellime möglichst

an die Mitte zwischen Nord- und Sudrand anschmiegen

Eine größere Sicherheit gewinnt man, wenn man die helleren Gebilde der Milchstraße als ihre Hauptobjekte ansieht und hellere isophotische I mien als Begrenzung ihres wesentlichen Teiles betrachtet. Dies führt zum entgegengesetzten Gienzfall

b) Man sucht alle hervortretenden hellsten Stellen Zentren der Lichtwolken und Maxima der Strome auf und legt die Mittellinie durch sie hindurch Will-kurlichkeiten in der Auswahl solcher Stellen lassen sich dann schwer vermeiden

Die Festlegung der Helligkeitsveiteilung in Zahlen bietet die Möglichkeit,

diese Willkurlichkeiten zu vermeiden, indem man entweder

c) für jeden Querschnitt die Lage des Lichtschwei punktes bestimmt, also  $\sum h \ b(N)$  gleich  $\sum h \ b(S)$  macht, wo h Helligkeit, b Breite im Koordmatensystem der Karte ist,

d) oder es wird für jeden Querschmitt die "Lichtmitte", also  $\sum h(N) = \sum h(S)$ .

berechnet

In der Tabelle 5 sind die Bestimmungen nach diesem Schema klassifiziett worden Nach Hopmann kann man konstatieren, daß die Ausatze a) und c), die Wert auf die mittlere Helligkeitsveiteilung legen, die Milchstraße als genau in einem Großkreis verlaufend hinstellen Dagegen hegt dei Zug dei hellen Wolken [Ansatz b) und d] in einem Kleinkreise, dessen Pol nordöstlich von dem der anderen Methoden hegt Newcombs Behandlungsweise muß als ein Kompromiß zwischen a) und b) bezeichnet werden, da ei 42 Punkte teils auf dei Mittellinie, teils an Stellen maximalei Intensität, in ziemlich gleichmäßiger Verteilung nach galaktischer Lange, benutzt hat Das in die Tabelle aufgenommene Resultat von Wirtz ist in ahnlicher Weise zu bezeichnen, bezieht sich aber auf den "Hauptzweig" der Milchstraße

Besonders großes Vertrauen verdient ohne Zweifel Pannekofks Bestimmung der Mittellinie der Milehstraße und die daraus folgende Lage des Pols in seiner oben (Ziff 3) erwähnten Arbeit über die sudliche Milehstraße Für jeden (nach der galaktischen Lange am Nord- und Sudhimmel wurde die Summe der Helligkeiten in dem entsprechenden Querschmtt der Milehstraße gebildet, und die Breite der Mitte, welche die Totalhelbigkeit in zwei gleiche Hälften teilt, bestimmt Die schwachsten Helligkeiten wurden vor der Summenbildung ausgeschlossen (die gegebenen Helligkeitszahlen wurden um eine Einheit vermindert und negative Zahlen durch 0 ersetzt) Die erhaltenen Werte sind in einer Tabelle in der erwähnten Arbeit aufgeführt Pannekoek hebt hervor, daß eine sich an die erhaltene Mittellinie schmiegende Ebene vielleicht noch nicht die wahre Symmetrieebene des galaktischen Systems darstellt, da die absorbierenden Nebelmassen in Taurus die Mittellinie nach Norden und in Ophiuchus nach Stielen drangen und daher der Pol scheinbar in der Richtung nach 330° Länge verschoben wird, seine R A hierdurch zu groß und seine Deklination ein wenig zu klein wird

Die Gesamthelligkeit als Funktion der galaktischen Lange zeigt nach Panniskoeks Zahlen ein hohes, schaifes Maximum in Sagittarius Die Daistellung der Helligkeit durch eine einfache gomometrische Formel ergab

$$h = 319 + 179 \cos(L - 323^\circ)$$

Die Abweichungen gegen diese Formel zeigen noch vier Maxima bei 325° in Sagiftarius, 50° in Cygnus-Lacerta, 170° in Gemini, 260° in Carina Minima dazwischen bei 10° in Aquila, 110° in Perseus, 230° in Vela, 290° in Cucinus-Lupus

Tabelle 5

Autorität		4	D	
Hourhau-Kobold Gould . Newcome Goos-Wirtz <sup>1</sup> Chapp Hophann Panneroek	(b) (a, b) (a, b) (a, c) (c) (d)	191° 26′ 190 38 191 6 195 8 192 16 189 44 194 0	+27° 56′ 27 13 26 48 29 8 26 48 26 0 27 43	91° 14',5 ± 50' (m F) 90 0 ± 6' 90 59 90 31 ± 23' 90 1 90 14,2 ± 6' 91 5

Aus den Zahlenangaben für  $\sigma$  ersicht man, daß die Sonne wahrscheinlich ein wenig nördlich von der zentralen Ebene der Milchstraße gelegen ist. Der Beitrug der Abweichung ist jedenfalls nach diesen Resultaten sehr gering, aber noch ziemlich unsicher bestimmt

Rine Neulerechnung des Pols der photographischen Milchstraße (Goos-Wolf) von Wirtz unter Berücksichtigung von Haupt- und Nebenzweig zusammen gibt  $A = 191^{\circ}, 9$ ,  $D = +31^{\circ}, 0$  (1900),  $\sigma = 87^{\circ}, 9$  Eine Auflösung für die photographische Milchstraße nach Barnards Atlas gibt  $A = 194^{\circ}, 2$ ,  $D = +28^{\circ}, 7$  (1900),  $\sigma = 88^{\circ}, 0$ . Die Sonne stände also etwas südlich von der Hauptebene der "aktinischen" Milchstraße Die wahre Bedeutung dieses Phänomens ist wohl aber noch ganz unklar

Über die zur Bestimmung des Pols benutzten mathematischen Methoden mag folgendes gesagt werden.

1. Houzeau berechnet den sphärischen Radius der Milchstraßenpunkte von Struves Pol aus. Die Abweichung von 90° für einen Punkt wird als eine kleine Verschiebung des wahren Pols gedeutet. RISTENPART und KOBOLD geben der etwas veruligemeinerten Methode von Houzeau die folgende Form. Seien  $\alpha$ ,  $\delta$  die Koordinaten einzelner beobachteter Punkte (etwa Punkte größter Dichtigkeit), A, D die Koordinaten des Pols, für welche man die Näherungswerte  $A_0$ ,  $D_0$  hut. Von diesem genäherten Pol aus berechnet man den Abstand  $\sigma_0$  eines bereichteten Maximums folgendermaßen.

$$\cos \sigma_0 = \sin \delta \sin D_0 + \cos \delta \cos D_0 \cos (\alpha - A_0)$$

$$\sin \sigma_0 \sin P = \cos \delta \sin (\alpha - A_0)$$

$$\sin \sigma_0 \cos P = \sin \delta \cos D_0 - \cos \delta \sin D_0 \cos (\alpha - A_0)$$
(i)

Die Hedingungsgielchungen zur Bestimmung der Korrektionen dA und dD des provisorischen Poles und der Größe  $\sigma$  sind dann von der Form

$$\sin P \cos D_{\bullet} \cdot dA + \cos P \cdot dD + \sigma = \sigma_{\bullet}. \tag{2}$$

2. Wenn wir die beobachteten Punkte des Milchstraßengürtels in einem provisorischen galaktischen System mit l,b bezeichnen und die Koordinaten des wuhren Pols in demselben System mit L,B, so haben wir unmittelbar die Relation

$$\cos b \cos l \cos B \cos L + \cos b \sin l \cos B \sin L + \sin b \sin B + \cos \sigma = 0$$
 (3)

Da wir voraussetzen können, daß der provisorische Pol nahe dem richtigen liegt, m kann  $\sin B = 1$  gesetzt werden, und wir können eine direkte Auflösung nach der Methode der kleinsten Quadrate mit den Unbekannten  $\cos B \cos L$ ,  $\cos B \sin L$ ,  $\sigma$  vornehmen Für  $\sigma$  kann man  $90^{\circ} + p$ , wo p die Tiefe ("dip") der Milchstraßenlinie bedeutet, einführen.

3. Newcomb sucht die Ebene durch unseren Beobachtungsort zu bestimmen, für welche die Summe S der Quadrate  $p^a$  ein Minimum ist, wo p den Sinus

<sup>&</sup>lt;sup>1</sup> Hauptrweig der Milchstraße.

der Winkeldistanz der Objekte von der Ebene bezeichnet Wenn wir die folgenden Bezeichnungen für die Richtungskosinusse einfuhren

$$a = \cos \delta \cos \alpha$$
,  $b = \cos \delta \sin \alpha$ ,  $c = \sin \delta$ ,  
 $v = \cos D \cos A$ ,  $y = \cos D \sin A$ ,  $z = \sin D$ ,

so ergibt sich

$$p = ax + by + cz$$

Wir bekommen dann die Summenformel

$$S = [aa] x^2 + 2[ab] xy + [bb] y^2 + 2[ac] xz + 2[bc] yz + [cc] z^2$$

Außerdem haben wir

$$x^2 + y^2 + z^2 = 1$$

Die Differentiation dieser Ausdrucke gibt, wenn wir die Bedingung  $d^5 = 0$  einfuhren, fur v, y, z die Gleichungen

$$([aa] - \lambda)x + [ab]y + [ac]z = 0, [ab]x + ([bb] - \lambda)y + [ba]z = 0, [ac]x + [bc]y + ([cc] - \lambda)z = 0,$$

wo I also durch die folgende Gleichung bestimmt weiden muß

$$\begin{vmatrix} [aa] - \lambda & [ab] & [ac] \\ [ab] & [bb] - \lambda & [bc] \\ [ac] & [bc] & [cc] - \lambda \end{vmatrix} = 0$$
(4)

Die Wurzeln dieser Gleichung sind reell und positiv. Sie bestimmen die diei Hauptebenen des Systems Newcomb zeigt, daß die Kondensationsebene durch die kleinste Wuizel & definiert wird Eine ausführliche Daistellung der Niew-COMBschen Methode hat Philippot<sup>1</sup> gegeben

Da die Milchstraße als der Kreis maximalei scheinbaiei Steindichtigkeit am Himmel definiert werden kann, so ist es klai, daß auch die Resultate dei Sternzahlungen zur Bestimmung der Lage dieses Kreises benutzt werden können Die fruhen Sternzahlungen beruhten im wesentlichen auf dem Material der Bonner Durchmusterung und ihrer stidlichen Fortsetzung Nach den Arbeiten von Ristenpart<sup>2</sup> und Prey<sup>8</sup> folgen die Dichtigkeitsmaxima der Steine heller als 9m,5 zwei etwas gegeneinander geneigten Ebenen. Die Lage der wenigei ausgepragten sekundaren Ebene fallt jedoch fur die beiden Autoren sehr verschieden aus

Aus der Verteilung der Sterne bis zur photographischen Größe 11,0 (Statistik der Zahlungen von H Henie nach der "Harvard Map") hat H Nori unter der Annahme A=191", D=+27" für die Lage des Pols die Tiefe  $\phi=+1$ ° 38′ 土 70' (m F) erhalten

Die die schwachsten Sterne bei ucksichtigenden Bestimmungen dei Symmetrieebene sind erst kurzlich von F H Searcs und P J van Riijn gemacht worden Seares Resultate wurden aus einer Statistik der Selected Arcas bis zur 18 photographischen Größe, zusammen mit einigen Zonen dei photographischen Himmelskarte, erhalten Er untersucht die systematischen Ab-

<sup>&</sup>lt;sup>1</sup> Annuaire de l'Observatoire Royal de Belgique, 1923, S 195 <sup>2</sup> Unters über die Konstante der Präzession (1892)

Denkschriften der math -naturw Klasse der K Akad dei Wiss, Wien, Bd 43 (1896). 4 Lund Medd, Serie II, Nr 10 (1913)

<sup>&</sup>lt;sup>5</sup> Recherches astron de l'Observatoire d'Utrecht VII, S 115 (1917) 6 Mt Wilson Contr 347, S 19, Ap J 67, S 141 (1928)

<sup>7</sup> Groningen Publications, Nr 43 (1930)

weichungen A der Logarithmen der Sternzahlen von einem rotationssymmetrischen Verlauf in gulaktischer Länge und bestimmt die Konstanten a, b und L'der Formel  $\Delta = a + b \cos(L - L')$ 

sowohl für verschiedene Größen als auch für verschiedene Zonen der galaktischen Breite Die Abhängigkeit von der galaktischen Länge wird als Folge dieser Verschiebung des gulaktischen Pols wie auch einer exzentrischen Lage der Sonne Im System gedeutet (Zilf 18) Aus den Werten von a, b und L' für verschiedene Zonen werden also der Betrag der Polverschiebung und die Länge des Zentrums ermittelt.

VAN RIIIINS Muterial sind für schwächere Sterne die Selected Areas (Haryard Durchmusterung und Mount Wilson-Katalog, wie oben bei SEARES) zur Gronzgröße 14 verwendet er die Franklin-Adams-Karten, bis zur Größe 10 die Bonner und Cordoba Durchmusterungen und für Sterne heller als 6m die Harvard Revised Photometry Beide Verfasser gehen von dem Gouldschen Pol aus und bestlimmen Länge und Breite des wahren Pols für die in Frage kommenden Sterne. Die Resultate sind in Tabelle 6 zusammengefaßt worden L und B sind die galaktischen Koordinaten des wahren Pols in Goulos System Die Gronzgrößen in sind photographisch van Rhijn gibt auch den "dip" p des Symmetriekreises

Tabelle 6

Searce						Van Reij	T
<b>P</b>	Ĺ	H		L	В	•	
9 11 13.5 16 18	275° 296 319 357 350	81°,9 83 ,2 82 ,0 85 ,9 87 ,3	4 5 6 8 10 14 14 16	152° 166 213 290 293 347 354 359	69°,0 88 ,4 87 ,3 88 ,7 87 ,2 85 ,0 87 ,6 86 ,1	-0°.7 +2.1 1.2 1.8 1.6 3.0 0.5	(Franklin-Adams-K ) (Selected Areas)

Den wahrscheinlichen Fehler in B, L con B und p schätzt van Rhijn zu etwa 1°

Für die Storne zwischen 9m und 14m zeigen die Resultate der zwei Verfasser sehr erhebliche Differenzen in der Breite B Es ist bemerkenswert, daß nach van Rhijn für Sterne schwächer als 8m praktisch dieselbe Lage des Pols für alle Klassen wiedergefunden wird Die große Bedeutung diesbezüglicher Fragen wird In den folgenden Abschnitten ersichtlich.

Für die Größen 8 bis 16 geben van Rhijns Resultate im Mittel  $L=330^{\circ}$ , B = 86°,6, p = +1°,9, und in Equatorialen Koordinaten für das Äquinoktium A = 193°54', D = +25°29', $\sigma = 91^{\circ},9$ 1900.

Wenn wir mit diesem Pol als Grundlage galaktische Koordinaten berechnen und diese mit  $L_1$ ,  $B_1$  bezeichnen, bekommt man nach van Rhijn für sukzessive Grenzgrößen die Werte in Tabelle7.

Die Verschlebung des Pols für die

 $B_1$  $L_1$ • 00,0 150°,2 65°,6 +1 .5 167 ,2 84 .7 5-6 87 ,3 167 ,2 90,0

Tabelle 7

hellsten Grenzgrößen ist ein Phänomen, das schon in großen Zügen von J Herschell und von Gould's beobachtet wurde. Gould fand, dall von den 527 Sternen bis zur 4 Größe 306 sich der

<sup>1</sup> Results of Observations, etc., p 385 Proc Amer Assoc for Adv Science, S 115 (1874), Uranometria Argentina, S. 354

Milchstraße, aber 330 sich einer anderen Symmetrieebene (dem "Gournschen Kreise") innerhalb 30° anlehnen. Fur den Pol seines Kreises fand Gould etwa  $A=171^{\circ},\ D=+30^{\circ},$  oder im galaktischen System der Tabelle 7  $L_1=162^{\circ},$  $B_1 = 69^{\circ}$  Dieselbe Verschiebung erscheint auch in Newcombs<sup>1</sup> Resultaten über die Lage des Pols für verschiedene hellere Großenklassen, verglichen mit dem Milchstraßenpol Nach van Rhijns Resultaten ist das Phanomen noch bis zui 7 Große schwach zu spuren VAN DE LINDE2 findet fur Sterne heller als 6m,25 den Pol  $A = 183^{\circ}$ ,  $D = +28^{\circ}$  Über die Bedeutung dieser Eischemung zu sprechen werden wir im folgenden mehrfach die Gelegenheit haben. Unter anderem wird es hervortreten, daß die Eischeinung auch besonders ausgepragt für die Heliumsterne und die Gasnebel in unserei nachsten Umgebung 15t (Zifi 13 und 19)

Zu erwahnen ist noch, daß J BAILLAUD für die Zone -[-22° der photographischen Himmelskaite, Grenzgioße etwa 12,5, eine sehr eiliebliche galaktische Konzentiation gefunden hat, eine Lage des Pols  $A = 200^{\circ}, 5, II = -1-27^{\circ}, 2 (1900)$ und eine Tiefe von 3° Spater hat er1 aus SEARES' Beobachtungsmaterial, aber nach einer allgemeineren und einfacheren Methode als der von Sparks benutzten, fui die Polkooidinaten

 $A = 193^{\circ}.7$ ,  $D = +27^{\circ}.1$ 

berechnet, mit einer Unsicherheit von etwa 2° Diese Lage des Pols stimmt sein wohl mit dem Pannekoekschen Weit in Tabelle 5 und ist auch mit van Riijns oben angeführten, aus analogem Material bestimmten in leidlicher Übereinstimmung

Von großem Interesse ist die galaktische Verteilung für Objekte von großer absoluter Leuchtkraft und dahei großer mittlerer Entsernung, da wir hier heurteilen konnen, in welcher Weise die raumliche Anordnung dieser Objekte sich der galaktischen Ebene anschmiegt Diesbezugliche Fragen werden in Ziff 19 und 20 naher diskutiert

12. Galaktische Koordinaten. Die Fundamentalebene der galaktischen Koordinaten wird durch den zum Milchstraßenpol gehörigen großten Kreis festgelegt Die galaktische Lange wird langs diesem giößten Kiels, gewöhnlich vom aufsteigenden Knoten des Kreises auf dem Aquator, gerählt Die galaktische Breite ist das Komplement der Distanz vom Nordpol dei Milchstraße Die Formeln zur Übertragung der aquatorealen Koordinaten α, δ in galaktische sind dann, wenn wir wie vorhei galaktische Lange und Bierte mit L und B, R A und Dekl des galaktischen Pols mit A und  $\bar{D}$  bezeichnen

$$\cos B \cos L = \cos \delta \sin(\alpha - A)$$

$$\cos B \sin L = \sin \delta \cos D - \cos \delta \sin D \cos(\alpha - A)$$

$$\sin B = \sin \delta \sin D + \cos \delta \cos D \cos(\alpha - A)$$
(5)

Nach der gegebenen Definition hegt die galaktische Länge 0° auf dem galaktischen großten Kreis im Sternbilde Aquila, die Länge 90° in Cassiopeia, 180° in Monoceros, 270° in Crux. Die über ein großeres Areal hellsten Partien der Milchstraße befinden sich in den galaktischen Langen 315° bis 335°, in den Steinbildern Sagittarius, Scorpius und Ophiuchus

Andere Vorschlage zur Annahme des Anfangspunktes in galaktischer Lange sind gemacht worden Man hat zuweilen als Nullpunkt den Sonnenapex benutzt (vgl unten) oder einen hellen Stern mit sehr klemer Eigenbewegung wic α Cygni<sup>6</sup> Keine von diesen Zahlungen ist bisher allgemein angenommen worden

Publ of the Carnegie Inst, No 10 (1904)

Publ of the Carnegie Inst, No 10 (1904)

De Verdeeling der heldere Sterren, S 59 Rotterdam Wyt & Zonen 1921

C 2 107 S 144 u 256 (1922)

4 C R 188, S 377 (1929),

Von dieser Willkürlichkeit des Anfangspunktes der galaktischen Länge abgesehen, gibt es ebenso viele Systeme galaktischer Koordinaten wie Bestimmungen der Lage des Milchstraßenpols. Da vurschiedene Bestimmungen oft ziemlich stark voneinander abweichen und es überdies nie darauf ankommt, eine galaktische Position mit äußerster Genaugkeit anzugeben, so wäre es natürlich am zweckniäßigsten, durch eine allgemeine Konvention unter Berticksichtigung der besten Bestimmungen eine gewisse Lage des Pols für allgemeine Zwecke zu fixieren. Hier herrscht gegenwärtig noch eine gewisse Verwirrung Oft werden abgerundete Ziffern, wie  $\mathbb{R}$  B  $A=190^\circ$ ,  $D=+30^\circ$ , benutzt, in anderen Fällen z B der Gouldsche Pol

A MARTH¹ hat zur Benutzung bei Milchstraßenbeobachtungen die galaktischen Koordinaten für die sichtbaren Sterne innerhalb der galaktischen Breiten  $\pm 20^{\circ}$  gegeben. Für den Pol der Milchstraße wurde dabei  $A=190^{\circ}, D=\pm 30^{\circ}$  (Äqu 1880) angenommen Der Marthsche Katalog ist speziell als Hilfe für die Konstruktion einer Karte aufgestellt und ist auch in dieser Weise vielfach benutzt worden. Panneroer, Easton und Plassmann haben z B. Reproduktionen solcher Karten unter Astronomen und Liebhabern verteilt, um die Praxis des Milchstraßenzeichnens allgemeiner zu verbreiten.

J C. KAPTEYN<sup>8</sup> hat eine Tafel für Berechnung der gelaktischen Breite unter Benutzung des Gouldschen Pols ausgearbeitet. Die Intervalle der Argumente sind 1<sup>h</sup> in α und 1° in δ. Eine Spezialtabeile für die Umgebung des gelak-

tuschen Pols wird auch gegeben

E. C. PICKERING<sup>4</sup> gibt nach A. SHARLE oine Tafel für galaktische Länge und Breite gamäß der Lage des Pols  $A = 190^{\circ}$ ,  $D = +28^{\circ}$  (1900) Die Intervalle sind  $40^{\circ}$  in  $\alpha$  und  $10^{\circ}$  in  $\delta$ 

O. R WALKEY hat cine Tafol für die Lage des Pols A = 12h 47m, D = +27°

und mit den Intervalien 1h und 10° gegeben

E. L. Johnson<sup>6</sup> hat unter Verwendung des Newcombschen Pols,  $A = 191^{\circ}, 1$ ,  $D = +26^{\circ}, 8$ , eine Tafel mit Intervallen 20<sup>m</sup> in  $\alpha$  und 5° in  $\delta$  berechnet.

A PANNEKOEK gibt in seinem oben reierierten Werke "Die nördliche Milchstraße" eine Tafel gemäß dem MARTHSchen Pol und mit denselben Intervallen

wie in Johnsons Arbeit.

J. Plassmann gibt in seinem Werke "Die Milchstraße" Tufeln mit den Argumenten  $\alpha - \Omega$  und  $\delta$  in Intervallen von  $6^\circ$ , wo  $\Omega$  die  $\Lambda$  R. des aufstelgenden Knotens der Milchstraße ist Kin paar Differentialtsfeln lassen die Korrektionen in L und B für eine andere Deklination des Pols als die zur Konstruktion der

Haupttafeln gewählte +27° 26' berechnen.

<sup>7</sup> Lund Obs Ann 3 (1932).

Eine Tafel, die nach Intervallen von 1° in  $\alpha$  und  $\delta$  fortschreitet, ist von C. V. L. Charlier auf der Sternwarte Lund ausgearbeitet worden. Die angenommene Lage des Pols ist hier  $A \approx 190^{\circ}$ ,  $D = +28^{\circ}$  (1900) Die genauesten gegenwärtig existierenden Tafeln sind später von derselben Sternwarte veröffentilcht worden. Die Arbeit geschah unter Leitung von J. Ohlsson, der auch ein Vorwort zu den Tafeln geschrieben hat. Für jeden ganzen Grad in  $\alpha$  und  $\delta$  werden L und B auf ein Hundertstel des Grades gegeben. Außerdem wird der Winkel  $\varphi$  zwischen Doklinationskreis und galaktischem Breitenkreis gegeben, um die Berechnung der Eigenbewegungskomponente längs der galaktischen Koordinatenkreise zu erleichtern. Die Lage des Pols ist die oben er-

<sup>1</sup> M N 33, S. 1 u. 517 (1872), 34, S. 77 (1873), 53, S. 74 u 384 (1893)

Vgl. PAMMEROER, Pop Artr 5, 8, 395, 485 u 524 (1898)
Groningen Publ Nr 18 (1908)
Harv Ann 56, S. 5 (1912)
MN 74, B. 201 (1913)
Union Circ 29, S. 226 (1915)

wahnte, aber ausführliche Reduktionstafeln zur Erleichterung des Übergangs

auf einen anderen Pol werden auch gegeben

P EMANUELLI hat ausfuhrliche Tafeln mit Angabe der Zehntelgrade in L und B gegeben Die Tafel schneitet nach Intervallen von  $10^{\rm m}$  in  $\alpha$  und 1° in  $\delta$  fort und 1st gemaß dem Newcombschen Pol  $A=12^{\rm h}$  44m,  $D=+20^{\circ}$ ,8 (fur das Jahr 1900 gultig angenommen) konstruiert worden. Die galaktische Lange wird hier vom Sonnenapev ( $\alpha = 270^{\circ}$ ,  $\delta = +30^{\circ}$ ) gerechnet. Der Verfasser gibt in der Emleitung eine ausführliche Bibliographie über Tafeln zur Berechnung galaktischer Koordinaten und über die verschiedenen Bestimmungen der Lage des Milchstraßenpols

P  $\check{J}$  van Rhijn² gibt fin jede Stunde in a und jeden Grad in  $\delta$  die galaktischen Koordinaten in einem System, dessen Pol mit dem Pol der schwachen Sterne (m > 8),  $A = 194^{\circ}$ ,  $D = +25^{\circ}$ ,5 (1900), ubereinstimmt Eine Spezialtabelle gilt fur die Umgebung des galaktischen Pols Außerdem werden Differentialtafeln entspiechend Verschiebungen des Pols in Übereinstimmung mit den Resultaten fur die helleren Steine (heller als m = 4, 5, 6, 7 resp.) gegeben

Graphische Verwandlungstafeln sind von H Selligle, P Stroobant, H NORTE, J. A PEARCE und S N HILLE publiziert worden. Zu diesen kommen auch ein paar Karten von O SEYDL, "Maps of the Boundaries of the Constellations in the Galactic System of Coordinates "7, gerechnet werden

R INNES<sup>8</sup> und nach ihm H Philippor<sup>8</sup> entwickeln die Vorteile, an Stelle der "mittleren" Örter der Gestirne die galaktischen einzustühren. Innis gibt Formeln und Tafeln zur genauen Übertragung mittlerer Orter der Jahresanfange zwischen 1750 und 1950 in galaktische Koordinaten unter Zugrundelegung de-Newcombschen Pols der Milchstraße Die galaktischen Längen werden vom Sonnenaper  $\alpha = 270^{\circ}$ ,  $\delta = +30^{\circ}$  (1900) getablt. Et gibt auch eine Spetialtafel zur duekten Verwandlung der schembaren Orter für das Jahr 1913 in "mittlere" galaktische Mehrere Beispiele, unter anderem fur Polaris und Polarissima, sind gerechnet worden Eine neue Bezeichnung der Steine schlägt Inni s auch voi Es sollten also an Stelle etwa der Benennung nach BD die helleren Sterne in den Vierecken sukzessiver Grade der galaktischen Lange und Biette nach der Lange numeriert weiden. Eine Bezeichnung

## 325°8°8 oder 325,8,8

bezeichnet also den achten Stern im Viereck zwischen Lange 325° und 326°, Breite +8° und +9° Negative Breiten sollten etwa durch Kursivstil ausgezeichnet werden

Eine Konsequenz der Benutzung galaktischer Kooldinaten ist natuigemäll. daß auch die Bewegungskomponenten der Sterne im galaktischen Koordinatensystem Ausdruck finden Formeln und Tafeln zur Beiechnung von galaktischen rechtwinkligen Bewegungskoordinaten, wenn Parallaxe, Eigenbewegung in RA und Dekl samt Geschwindigkeit im Visionsradius gegeben sind, hat kürzlich A Kohlschutter<sup>10</sup> veroffentlicht Die Lage des Pols wurde zu R A 190°. Dekl +27° angenommen In einer Spezialtafel weiden aber auch Verbesserungen

<sup>2</sup> Groningen Publ Nr 43 (1929)

Pubblicazioni della Specola Vaticana, Ni XIV, Appendice prima (1929)

<sup>&</sup>lt;sup>8</sup> Sitzber d K Bayer Akad d Wiss, Math-Phys Kl 16, S 220 (1886) <sup>4</sup> Annales Obs Roy de Belg 11, S 97 (1908)

<sup>&</sup>lt;sup>5</sup> Recherches astron de l'Observatoire d'Utrecht VII (1917)

Publ Astroph Obs Victoria 4, Nr. 4 (1927)
 Publ Obs Nat de Prague Ni 5 (1928)
 Union Circ 2 (1912)
 5, 6 (1913)
 Annuaire de l'Obs Roy de Belg 1923
 5 155 10 Veröff Univ-Sternw Bonn Nr 22 (1930)

zu den neun Übertragungskoeffizienten der Geschwindigkeitskomponente bei Ubergang zu einem anderen galaktischen Pol gegeben. Eine Sterntafel enthält die Koeffizienten für alle Sterne, deren Radialgeschwindigkeit zur Zeit bekannt war

## e) Der Einfluß der diffusen Nebel auf das Milchstraßenbild.

18, Die galaktischen Nebelfelder. Die Photographie hat uns in unverkennburer Welse gezeigt, daß der Milchstraßengürtel nicht nur eine von Sternen by yorkingto Region des Himmels ist, sondern auch reichlich leuchtende und dunkle, unregelniding begrenzte Nebelmassen enthält. Die Felder der leuchtenden Nobel sind in der Rogel als Gebiete eigenartiger Struktur der Milchstraße ausgezeichnet Die helle Nebelmasse selbst ist oft dicht mit Sternen, bisweilen von beträchtlicher Holligkeit, besät. Gebiete auffallend kleiner Sternanzahl erstrecken sich gewöhnlich in unregelmäßiger Weise um die hellen Partien herum Lis ist offenbar, dail man diese Reduktion der Sternfülle am emfachsten als einen Absorptionseffekt dunkler nobliger oder staubförmiger Massen auf das Licht entfernterer Sterne erklären kann, da wir andernfalls sehr langgestreckte, von uns aus radial gerichtete Lücken durch das Sternsystem hindurch in der Umgebung der hellen Nebel annehmen müßten, und das würde eine sehr unwahrschemliche Anordnung bedeuten1 Damit haben wir auf die Existenz mächtiger, nichtleuchtender Mussen geschlossen, die imstande sind, allgemeine Absorption oder Diffusion des Lichtes auszuüben. Solche Massen sind aber nicht notwendig nur in Verbindung mit leuchtenden Nobeln vorhanden, sondern verraten oft ihre Existenz nur durch ihre Absorptionswirkung als dunkle, an Sternen auffallend urme Gebiete, die gegen den hellen Hintergrund der Milchstraße kontrastieren

In diesem Zusammenhang mag erwähnt werden, daß die Luminiszenz der hellen Nebelpartlen wahrschemhelt von der Einstrahlung naheltegender Sterne lacilingt ist. V. M SLIPHER fand, daß für Merope, Mala, Q Ophiuchi, NGC 2068 und 7023 das Spektrum der Nebelmasse wonigstens ungefähr mit den Spektren der helisten eingehüllten Sterne übereinstimmt E HERTZSPRUNG<sup>3</sup> hat die Theorie einer partiellen Reflexion oder Streuung durch Photometrierung der Plejadennebel zu prüfen gesucht; er findet, daß die Flächenhelligkeit der Nebel an ibren hellsten Stellen um etwa 4 bis 5 Sterngrößen schwächer ist, als sie bei vollständiger Streuung des Lichtes des Zontralsterns an den betreffenden Punkten sein würde II N Russkll4 hat die Reflexionstheorie für die galaktischen Nebel aufgenommen und weiter die Hypothese aufgestellt, daß auch die Nebel mit Linlenspektren durch das Licht von nahehegenden Sternen zur Strahlung erregt worden. R. Hunnag hat diese Theorien auf Grund eines größeren Materials geprüst und im allgemeinen Durchschnitt gute Bestätigung gefunden. Er hebt horvor, daß in den hellen diffuson Nebeln fast immer Sterne zu finden sind, die mit der Nebelmasse in deutlicher Verbindung stehen Wenn das Sternspektrum vom Typus O-130 ist, strahlt der Nebel mit Linienspektrum, aber wenn der Spektraltypus des Sterns ein späterer ist, erscheint das Nebelspektrum kontinuierlich

HUBBLE findet auch einige interessante, aber weniger klar ausgesprochene Verschiedenheiten zwischen Nebeln mit Linienspektrum und Nebeln mit kontinuierlichem Spektrum. Die Netzwerknebel haben gewähnlich Linienspektrum,

Lowell Obs Bull Nr 55 (1912), Nr 75 (1916); Publ ASP 30, S 63 (1918); 31, S. 212

<sup>(1919)</sup>A N 195, S 449 (1913)
Wash Nat Ac Proc 8, S. 115 (1922), Obs. 44, S 72 (1921)
Wash Nat Ac Proc 8, S. 115 (1922), Obs. 44, S 72 (1921)

Mt Wilson Contr 241 = Ap J 56, S. 162 (1922), 250 = Ap J 56, S 400 (1922)

und die mehr regelmaßigen, wolkenartigen ein kontinuierliches. Die kontinuierlich strahlenden sind mit großeier Verdunklung verbunden, obgleich schweisende Ausnahmen von dieser Regel in dem Orionnebel und in NGC 7000 (Amerikanebel) gefunden werden. Die hellsten Nebel haben Linienspektrum, die ausgedehntesten kontinuierliches Spektrum. Die letzteie Klasse hat die starkere Tendenz zu einer Konzentration um in den Nebel eingehullte Steine

Auch die allgemeine Verteilung der hellen dissusen Nebel am Himmel ist von Hubble diskutiert worden. Diese Verteilung ist nicht einsach eine Konzentration gegen die galaktische Ebene. Zwei verschiedene Guitel sind zu unterscheiden, die Mischstraße und ein Gurtel, der gegen den galaktischen Kreis um ungefahr 20° geneigt ist. Die Knoten sallen ziemlich genau mit denen der hellen Heliumsterne zusammen, aber die Neigung der Nebelschicht ist eineblich großer. Die Verbindung zwischen Nebeln und Heliumsteinen wird jedoch durch diese Verteilung sehr augenscheinlich. Wir wollen im solgenden einige hervorragende Nebelselder, die für die scheinbare Mischstraßenstruktur von Bedeutung sind, kurz erwähnen.

Ein heller Nebelschleiel, der auf Milchstraßenaufnahmen der Perseusgegend (Abb 4) in markanter Weise hervortritt, ist NGC 1499 Dieser Nebel befindet sich am sudlichen Rande der Milchstraße etwas nordlich vom Stein  $\xi$  Persei (Spektraltypus Oe5), der wahrscheinlich der erleuchtende Stein ist. Der Nebel liegt nahe der weitgestieckten dunklen Masse zwischen i Tauri und  $\varepsilon$  Persei Diese Masse ist in nördlicher Richtung durch einen feinen Kanal mit einer dunklen Hohle einige Grade westlich von  $\alpha$  Aurigae, ziemlich auf der Zentrallime der Milchstraße, verbunden und hat in sudlicher Richtung Verbindung mit einer sehr dunklen Partie nordlich von  $\tau$  Tauri, die sowohl in östlicher Richtung gegen  $\beta$  Tauri als in westlicher Richtung gegen die Nebelpartien um o Persei her um schmale Kanale aussendet. Wir sind hier schon in betrachtlich sudliche galaktische Breite geführt. In der Nahe erscheint die in Nebel eingehullte Plejadengruppe<sup>1</sup>

Eine Fortsetzung der eben genannten Nebelpartien, die augenscheinlich der gegen die Milchstraße um 20° geneigten Nebelschicht angehören, bilden die

Nebel in der Oriongegend

Ziemlich in dei Zentrallinie der Milchstraße finden sich in dieser Gegend die interessanten Nebel um S Monocerotis (Abb 5) und um 12 Monocerotis herum Der letztere Nebel erscheint am Rande einei Dunkelregion, die gegen Orion hinzieht

Im sudichsten Verlaufe der Milchstraße ist von allem zu einemhen die machtige und sehr helle Nebelmasse NGC 3372 um  $\eta$  Caunae herum², die nahe zentral in der Milchstraße gelegen ist, wo diese sich zu einem schmalen hellen Lichtstrom verjungt. Die scharfe Einbuchtung der Milchstraße sudöstlich von diesem Nebel ist wohl mit großter Wahrscheinlichkeit einer nebularen Absoi ption zuzuschreiben. Nach der Franklin-Adams-Karte scheinen  $\lambda$  Contauri und naheliegende Steine am Rande der hellen Partie in helle Nebel eingehullt zu sein. Von dunklen Gebieten ist aber in dieser Himmelsgegend vor allem zu bemei ken der "Kohlensack" ostlich von  $\alpha$  und  $\beta$  Crucis. Nahe an  $\alpha$  und im nördlichsten Teil unweit von  $\beta$  ist das dunkle Gebiet sehr arm an Sternen , in sudwestlicher Richtung erstreckt sich vom Dunkelgebiet aus ein schmaler Kanal, der sich auf mehrere Grade hin verfolgen laßt

In den Sternbildern Norma, Ara und Scorpius wird die sich erweiternde Milchstraße in sehr komplizierter Weise von dunklen Flecken und Kanalen

Vgl auch Aufnahmen von Ross, Ap J 67, S 284 (1928)
 Vgl Franklin Adams Karte oder Harv Ann 80, Pl IV (1908)

zerrissen Es ist sehr wahrscheinlich, daß die sukzessive Abspaltung der zwei westlichen Milchstraßenäste in dieser Gegend auf Absorption durch dunkle Massen zurückzuführen ist. Von deutlichem Nebelcharakter erscheint eine komplizierte, vielfach in Kanäle aufgelöste, langgestreckte dunkle Region, die vom Schwanze des Skorplons nördlich von  $\lambda$  und v Scorpli in westlicher Richtung den westlichen Milchstraßenast durchquert, um in der Gegend von  $\eta$  und v Lupi ein ziemlich weitgestrecktes dunkles Gebiet zu bilden, an dessen südlichem Rande der Sternhaufen NGC 6124 gelegen ist. Von diesem Gebiets gehen schmale Kanäle weiter nach Westen. Im ganzen zeigt die Nebelpartie eine gewisse Ähnlichkeit mit den weiter nördlich gelegenen Nobeln, die mit dem hellen Nebel um v0 Ophluchi in Verbindung stehen.

Die hellen Nebel in Scorpius und Ophiuchus bilden gewissermaßen ein Gegenstück zu den Nebeln in Orion, da sie in beinahe entgegengesetzter Richtung am Himmel erscheinen und also im ganzen eine erhebliche westliche Abweichung von der zentralen Milchstraßenlinie zeigen. Von außerordentlichem Interesse ist die Nebelmasse um  $\varrho$  Ophiuchi und 22 Scorpii herum, die vielleicht auch in einiger Verbindung mit den Nebeln um  $\sigma$  und  $\nu$  Scorpii herum steht. Von diesem Nebel gehen nach Osten hin mehrere dunkle Kanāle. Einer von diesen geht auf den westlichen Ast der Milchstraße in Ophiuchus zu, teilt sich dort in einen nördlichen und einen südlichen Ast, so daß das ganze Gebilde fast die Form eines gewaltigen Ankers erhält (vgl. Ziff. 9). Der südliche Ast enthält die außerordentlich dunkle Partie südöstlich von  $\ell$  Ophiuchi. Der nördliche Ast spaltet einen Zweig in östlicher Richtung ab, der gegen den Sternhaufen M23 hinläuft, aber von diesem Haufen in südlicher Richtung umblegt und sich dann in der großen dunklen Mittelpartie zwischen den Milchstraßenästan verliert.

Die dunkle Region zwischen den Milchstraßenästen in Sagittarius enthält am östlichen Rande die zwei schönen Nebel M8¹ und M20 (NGC 6523 und 6514); der letztere ist der berühmte Trifidnebel³. Sie stehen an der Spitze einer Reihe von kleineren Sternwolken, die von der Scutumgegend über μ Sagittaril hin laufen, und die von einer "grobkörnigeren" Struktur als die umgebenden großen Wolken in Sagittarius und Ophiuchus zu sein scheinen. An die helle kleins Wolke in der Nähe von μ Sagittarii schließt sich im Söden ein dunkles Gebiet, das die Nebel NGC 6589 und 6590 anthält. Im nördlichen Teil derseiben Wolke erscheinen die bekannten dunklen Nebel Barnard 92 und 93. An die genannte Wolkenreihe schließen sich auch der Nebel M17 (NGC 6618) und der neblige Haufen M16 (NGC 6611) an, aber vor allem welter nördlich der Nebel IC 1287 (um den Stern Boss 4687), der auf allen Seiten in worte Sternleeren übergeht, zu denen die großen, die Milchstraße durchquerenden Kanäle stidlich von der Scutumwolke gehören.

Es ist wohl kaum zu bezweifeln, daß der große, in Ziff. 9 besprochens dunkle "Keil", der in die Milchstraße in Ophiuchus von Westen her einsetzt und die Aufspaltung der Milchstraße in Ophiuchus und Aquila bewirkt, in der Licht-absorption dunkler Massen seinen Ursprung hat. Eine Verbindung der absorbierenden Massen mit dem  $\varrho$  Ophiuchi-Nebel scheint nicht ausgeschlossen. Dieselbe Erklärung folgt dann mut großer Wahrscheinlichkeit für den dunklen "gebeugten Arm" der Cygnusgegend, der in seinem oberen Teil den "Nordamerika-Nebel" und die hellen Nebel um  $\varrho$  Cygni herum enthält.

Es liegt nahe zu bemerken, daß die zwel letztgenannten dunklen Gebiete von nördlicher galaktischer Breite her in der Richtung wachsender galaktischer Länge in die Milchstraße hineinreichen, während die entsprechenden dunklen

<sup>1</sup> Vgl. Aninehme von Duncan, Mt Wilson Contr 177 - Ap J 51, 8. 4 (1920).

Duncan, Mt Wilson Contr 256 - Ap J 57, S. 137 (1923).

Trennungsmassen der Milchstiaßenaste in Scorpius und Norma von überwiegend nordheher Breite gegen abnehmende Lange hinzichen. Man kann aus dieser Tatsache allem Veranlassung haben, den Schluß zu ziehen, daß die neblige Materie unserer nachsten Umgebung in großeier Haufigkeit in einer Ebene betrachtlicher Neigung gegen die Milchstraße verteilt ist, und daß diese Islame thre großte galaktische Breite in der Scorpius-Ophiuchus-Gegend einen ht. 15schemt, daß ein wesentlicher Teil der dunklen Nebelmassen, die die Milchstraße zwischen  $\alpha$  Centauri und  $\alpha$  Cygni zeistuckeln, als Ausläufer einer solchen Schicht anzusehen ist, und daß besonders der westliche Ast in dieser Milchstraßengegend durch die Nahe an dei Absorptionsebene in seiner mittleren Lichtstäuke reduziert worden ist. Wenn wir die Knoten der Ebene in Crux und Cassiopeia annehmen, scheint es moglich, viele der großten verdunkelten Gebiete anderer Gegenden als zur genannten Nebelschicht gehorig anzusehen. Es ist abei auch deutlich ersichtlich, daß die Zweiteilung der Milchstraße in Scorpius, Sagittarins und Ophiuchus zum Teil auch auf in der zentialen Milchstraßenebene orientierle dunkle Massen zuruckzufuhren ist, und wir haben somit eine doppelte Verteilung der dunklen Massen gefunden, die der vorher besprochenen Verteilung der hellen diffusen Nebel durchaus ahnelt

Der nordlichste Verlauf der Milchstraße ist reich an umegelmäßigen dunklen Gebilden, die bis in die Perseusgegend hauptsachlich auf der Nordseite der zentralen Milchstraßenlinie gelegen sind. So haben wir den "Kohlensack" nörd» lich von der klemen Cygnuswolke mit seinem in stidlicher Richtung den "Haupt» strom" der Milchstraße durchquerenden schmalen Kanal, den dunklen Pleck dathch von  $\delta$  Cepher und das langgestreckte dunkle Gebiet westlich von  $\beta$  Cassioperae

In der osthehen Milchstraßenpartie in Cygnus eischeinen AB die Awei wahrscheinlich zusammengehorigen Netzweiknebel NGC 6960 und 6992 Dath die Nebelschlinge 6960 auf der Außenseite, von 6992 aus gerechnet, von dunklen Nebeln begleitet ist, die eine merkliche Absorption austiben, ist besonders auf J C Duncans<sup>1</sup> Aufnahme mit dem Hooker-Teleskop deutlich zu erkennen

(vgl M Wolf, Ziff 22)

Östlich von der in unserer allgemeinen Beschieibung dei Milchstraße er wähnten Durchquerung des Hauptstromes bei A Cygni haben wit eine schwächtte bei  $\pi_1$  und  $\pi_2$  Cygni Dieser Kanal steht mit einem eigenatigen Nebel in Verbindung Aus einer ziemlich großen dunklen Höhle geht in sudöstlicher Richtung ein ziemlich langer, kanalartiger, sternarmer Streifen heiver. In dessen öst lichem Ende liegt ein heller, rundlicher Nebelfleck2, dei sog "Kokon-Nebel" (IIC 5146) Wir sehen hier in einem kleinen Maßstab, abei in sehn deutlicher Weise, eine Art Verbindung zwischen leuchtender und dunkler Nebelmaterie. die wir schon mehrmals, nur in etwas verschiedenei Form, gefunden haben. 128 scheint, als ob die helle Nebelpartie sich fortbewege, einen Schweif von allmählich sich weit verbreitender dunkler Materie hinterlassend. Die oben genannte Durchquerung besteht aus einem fast geradhnigen, zei hackten Zug von dunklen Stellen, der in nordlicher Richtung hinzieht und bei dem Stein 14 Cephei in einen sehr dunklen eirunden Fleck, BARNARD 169, ausmundet Diesei Fleck liegt am stidlichen Rande der Cepheuswolke

Westlich vom ehen genannten Fleck und sudlich von  $\mu$  Cephei liegt ein in ausgedehnte schwache Nebel gehullter Sternhaufen um den Stern 13 H Cepher (Oe5) herum Diese Gegend zeigt eine Menge schmaler, tiesdunklei Kanäle und Flecke und wird ringsum von großeren dunklen Partien umgeben (vgl BARNARD,

"A Photographic Atlas etc ", Pl 49)

<sup>&</sup>lt;sup>1</sup> Mt. Wilson Contr 256 = Ap J 57, S 137 (1923)

Wolf, Die Milchstraße und die kosmischen Nebel, Pl III

14. Dunkle, wohl markierte Flecke im Sternstratum Manchmal schr scharf begrenzte, tiefdunkle Flecke treten oft in außerordentlich auffälliger Weise gegen den Hintergrund einer sternreichen Gegend hervor Schon A. Secchi<sup>1</sup> hat auf tiefschwarze Höhlen in den Sternwolken in Sagittarius aufmerksum gemacht. und G F Chambers zählt solche Flecke auch in Scorpius auf. Eine kleine schwarze Höhle von nur 2' Durchmesser in der Sagittarluswolke (B 86) wurde von BARNARD' im Jahre 1883 durch visuelle Beobachtung entdeckt Diese Höhle hat den kleinen Stornhaufen NGC 6520 unmittelbar auf der östlichen Selte und erscheint daher in besonders starkem Kontrast gegen ihre Umgebung BARNARD hat sich dann besonders einem Studium der dunklen Flecke auf photographischem Wege gewidmet und schließlich einen Katalog und eine Beschreibung für 182 Objekte dieser Art gegeben\* Sem photographischer Atlas der Milchstraße enthält auch reichlich Bomerkungen tiber diese Objekte Es ist selbstverständlich, daß für die Erklärung dieser Flecke nur die Absorptionshypothese ernstlich in Frage kommon kann

Ein systematisches Aufsuchen dunkler Flecke des Himmels ist kürzlich mit Hilfe der Franklin-Adams-Platten von K. Lundmark und P J Melotte ausgeführt worden Eine Karte, welche die Verteilung der 1550 gefundenen Objekte zolgt, hat LUNDMARR' gegeben. Er schätzt das ganze Areal der dunklen Flecke auf ungefähr 850 Quadratgrade, was etwa 1 50 des ganzen Himmels ontspricht

Man muß bei der Deutung dieses Resultats die Bemerkungen vorausschieken. erstens, daß nicht alle Flecke notwendigerweise durch Absorption in dunklen Masson hervorgerufen sein müssen, sondern biswellen wurklichen sternleuren Regionen im Raume entsprechen können, was auch von LUNDMARK hervorgehoben wird, zweltons aber, daß eben die größten vordunkelten Gebiete des Himmels, deren Gronzen verwaschen oder mehr unregelmäßig definiert erscheinen. z. B das große Absorptionsgebiet in Ophiuchus, mitunter nur durch ihre dunkelsten Gebiete repräsentiert werden.

Die Verteilung der dunklen Flecke zeigt eine große Frequenz in der stidlichen Milchstraße zwischen Carina und Aquila, wie auch eine große Häufigkeit in der Orlongegend (südliche galaktische Breite) und in der Cepheus-Cassiopela-Gegend (nördliche galaktische Breite) Das Auftreten von Plecken auch in sehr beträchtlicher galaktischer Breite hat H. Shapley veranlaßt, für 50 Regionen hoher galaktischer Breite die Verteilung schwacher Sterne auf Harvard-Platten zu untersuchen Nur für eines der untersuchten Gebiete (östlich von  $\mu$  und b Serpentis) wird eine Absorption durch Dunkelwolken bestätigt; die Sterne, die schwächer sind, als es der Gronzgröße der Franklin-Adams-Platten entspricht, zeigen für andere Regionen eine wesentlich gielchförmige Verteilung. Shaplay hat vorher ein ahnliches Resultat für eine sternarme Region auf den Karten der Pariser Astrographischen Zone, auf die von E OPIK und M. Lukke hingewiesen worden war, gefunden,

15. HAGRING dunkle Nebel. Auf die Existenz dunkler Nebelwolken, die wesentlich außerhalb der Milchstraße auftreten und der t ein zusammenhängendes

<sup>1</sup> A N 41, S. 238 (1855).

Descriptive Astronomy, 3rd ed. Oxford 1877.

A N 108, S. 369 (1884)

Ap J 49, S. 1 (1919).

Pop Astr Tidakr 7, H. 18 (1926) — Upsala Modd 12; Studies of Anagalactic Nebulae, N Acta Rog Soc. Scientiarum Upsal, Volumen extra ordinem editum (1927), Upsala Medd 30, Pl. I.

Harv Bull 844 (1927). 7 Harv Circ 281 (1925). Publ Ohe Univ de Tartu (Dorpat) 26, Nr 2 (1924)

Gewebe ahnlich den Gestaltungen irdischer Wolken bilden, hat J G HAGEN<sup>1</sup> aus umfangreichen visuellen Beobachtungen mit dem 16zolligen Refiaktor der Vatikan-Steinwarte geschlossen Schon W Herschel<sup>2</sup> hatte 52 weit ausgedehnte milchige Nebelgebilde angegeben, die in allen galaktischen Breiten auftieten, und die zusammen sicher wert mehr als 150 Quadratgrade des Ilimmels bedecken In neuerer Zeit ist aber für diese Felder nur in Ausnahmefallen auf photographischem Wege die Anwesenheit von Nebelmaterie nachgewiesen worden3 Hagens Nebel umfassen auch die Herschelschen. Sie haben eine graue neutrale Farbung und fur die Dichte oder Trubung der Nebel hat HAGEN eine Skala von fünf Stufen eingefuhrt, deren Nummern mit dem Trübungsgrad wachsen Stufe V entspricht also den dichtesten, "fast alle Steine verdunkelnden" Partien In der Durchmusterung der Nebel wurde das Fernicht auf volle Grade in R A eingestellt und in Dekl. bewegt. Das Gesichtsfeld hatte 25' Duichmesser Die Beobachtungsmethode besteht in einem Überfahren ("sweeping") eines Streifens benachbaiter Gebiete.

Das Hauptresultat dei Hagenschen Untersuchungen ist, daß die dunklen Nebel ein zusammenhangendes Netzwerk bilden, das aber von kanal- und ovalformigen Lichtungen vielfach durchbrochen ist. Sie bevorzugen die außeigalaktischen Regionen des Himmels, kommen aber auch in der Milchstraße vor. Da der geschatzte Trubungsgrad augenscheinlich auf der Steinfulle berüht, so ist es von vornherein klar, daß eine negative Korrelation zwischen Dichte des Nebels und Sternanzahl zu erwarten ist

Die hellen Nebelflecke der außergalaktischen Regionen finden sich selten innerhalb großer Wolkenkontinente, sondern meist an derem Rande oder wo die Dichte sich schnell verandert. Große Wolkengebiete erschemen oft von Sternketten umsaumt

HAGEN schließt, daß unser Milchstraßensystem von einem dunklen Nebelmeer eingehullt ist, das auch die hellen außergalaktischen Nebelfiecke umfaßt Er sucht auch in weitgehender Weise die kosmogonische Stellung der dunklen Nebel aufzuklaren, nach ihm waren die dunklen Nebel der Uistoff der ursprünglich kalten und dunklen Riesensterne, die sich in dem Lockyer-Hertzsprung-Russellschen Schema weiterentwickeln

Die Resultate von Hagen sind von F Becker und J Stein daigelegt und verteidigt worden J Hellerich und V Cerulli haben zusammenfassende Übersichten gegeben

Fields Preface by J G HAGEN Paris 1928

<sup>&</sup>lt;sup>1</sup> Mem S A I t 1 (1920), M N 81, S 449 (1921), A N, Jubii -Nr (1921), 213, S 351 (1921), 214, S 449 (1921), Naturwiss 9, S 935 (1921), Scientia 31, S 185 (1922), Publ A S P 34, S 320 (1922), Atti Pontif Accad Sci 75, S 71 u 83 (1922), 76, S 31, 89 u 200 (1923), 77, S 131 (1924) (Durchmusterung und kleinere Notizen), Specola Astronomica, Vaticana, Miscellanea Astronomica 1, parte 3 (1924) (Neudruck älterer Abhandlungen), A N 224, S 421 (1925), 225, S 129 u 383 (1925), Specola Vaticana X (1922, 1925 u 1927) (Katalog), M N 86, S 144, 146, 349, 439, 548 u 642 (1926), A N 227, S 391 (1926), B Z 23 (1927), Ath Pontif Accad Sci 80, S 51 u 94 (1927), A N 229, S 303 (1927), 230, S 325 (1927), M N 87, S 106 (1926), Publ A S P 39, S 167 (1927), Ath Pontif Accad Sci 81, S 343 (1928), 82, S 263 (1929), B Z 16 (1929), Pop Astr 37, S 284 u 395 (1929), A N 235, S 313 (1929), M N 90, S 331 (1930), außerdem ,Die Nebelstraße", Anhang zu der Monographie ,Die Milchstraße" von Plassmann (1924), "Das photographische Problem der Nebelwolken", Festschrift Stella Matutina II (1931), Miscellanea Astronomica 6, No 93 (1931)

Phil Trans S 269 (1811), Coll Scientific Papers II, S 459
 Vgl besonders Mrs I Roberts, I Roberts' Atlas of 52 Regions A Guide to Herschel's

A N 223, S 303 (1925), 224, S 113 u 235 (1925), 225, S 129 (1925), Die Sterne, S 97 (1926), Specola Astronomica Vaticana XIII (1928), Dunkelwolken in der Umgebung von NGC-Objekten
 V J S 61, S 250 (1926)
 Naturwiss 14, S, 107 (1926)
 Scientia 40, S 133 (1926)

Es hut über auch nicht an Einwänden gegan Hagens Deutung seiner Beobachtungen gefehlt. So besteht die Schwierigkeit, daß auf langerponierten Platten unter Verwendung von lichtstarken Instrumenten keine den Nebeln entsprechende Struktur hervortritt. Dieser Schliß kann aus den ausgedehnten photographischen Arbeiten, z. B. von Barnard, Wolf und Hubble, gezogen werden, da diese keine diffusen Nobel in hohen galaktischen Breiten nachgewiesen haben. N. Ivanov¹ konstatierte kürzlich dasselbe Sachverhältnis für die Hagenschen Nebelwolken bei V und UW Draconis und bei R und S Tauri. Lundmark® hebt unter anderem hervor, daß Fehlerquellen wie Tierkreislicht, Erdlicht, physiologische Effekte, l'arhengieichung des Instrumentes einwirken können. Er schlägt vor, daß Hagens Beobachtungen von anderen Beobachtern, in einem anderen Khma, mit Teleskopen von größerem Öffnungsverhältnis und größerem Feld wiederholt werden sollten

Angosichts der großen Schwierigkeiten, die eine Einpassung des "Nebelmeors" in unser Weitbild vormsacht, wäre es wohl jedenfalls angemessen, eine weniger revolutionierende Erklärung des beobachteten Phänomens zu suchen. Wirtzs sicht in den Beobachtungen der Hagenschen Nebel Stufenschätzungen der scheinbaren Holligkeit des Himmelsgrundes. Der negative Korrelationskooffizient  $\tau$  zwischen Dunkelstufen und Sterndichtigkeit wird numerisch um so größer, je schwächer die Sterne der verglichenen Sternzählungen sind Bei der Grenzgröße 11,0 ist  $\tau = -0.16$ , bei 14,5 ist  $\tau = -0.64$ . Es hegt also in Hagens Resultaten ein ongmaschiges Netz grober schematischer Sternenchungen vor Praktisch denselben Schluß hat auch Shapley aus ähnlichen Überlegungen gezogen. Hagen und Becher lehnen jedoch diese Auffassung ab auf Grund von dem unmittelbarun subjektiven Eindruck, der direkt die unzweideutige Existenz der Wolken gewährleisten soll

Es scheint jedoch wohl noch die Möglichkeit su bestehen, daß der schwache graue "Nobelschein", der keine Struktur auf den photographischen Platten gibt, als "Erdlicht" im weiteren Sinne (Ziff 5) erklärt werden kann, daß er nach Hagens Angaben mit großer Stornfülle im Felde su verschwinden scheint, wäre als ein physiologischer Kontrasteffekt zu deuten Es ist schon oben der Schluß gezogen worden, daß Sternanzahl und Trübungsgrad korreliert sein müssen, da offenbar die Sternleere des Foldes als Maß der Trübung benutzt wird. Auf die Gefahr einer Selbsttäuschung bei der Einordnung benachbarter Sterne im Gesichtsfelde in "Ketten" sollte wohl auch hingewiesen werden.

Wenngleich eine "einfachere" Erklärung dieser Art gegenwärtig vielleicht vorzuziehen wäre, verdienen doch ohne Zweifel die scharfen und kühnen Beobschungen Hagens mit größtem Interesse aufgenommen zu werden, was besonders durch die zahlreichen Kommentare und Erklärungsversuche, z. B in neuester Zeit von H. Osthoff, J. Hartmann" und J Hopmann, bewiesen wird.

## f) Die astrophysikalisch-statistischen Ergebnisse über die Natur der Milchstraße.

16. Die galaktische Konzentration der Sterne und die effektive Sterngröße des Milchstraßenlichts. Es ist seit drei Jahrhunderten eine wohlbekannte Tatsache, daß das Milchstraßenphänomen auf einem scheinbaren Zusammendrängen der Sterne gegen einen gewissen Gürtel des Himmels beruht Durch die

7 AN 238, S. 285 (1930)

AN 239, S. Gt (1930).

Bullotin of the Observing Corp of the Soc. of Amsteur Astronomers of Moscow Nr 8, 8, 57 (1927)
Publ A S P 34, 8 191 (1922).

Nr 8, S. 57 (1927)

A N 223, S 123 (1924); 224, S. 267 (1925), 225, S. 299 (1925)

Harv Ciro 284 (1925).

A N 238, S. 233 (1930)

Arbeiten von Houzeau, Seeliger, Schapareitt, Pickering, Stratonoff u a wurde es auch klaigelegt, daß diese "galaktische Konzentiation" der Steine in allen Großenklassen zu finden ist, wenn auch die Steine der hellsten Großen sich eher gegen den Gouldschen Kieis (Ziff 11), als gegen die zentiale Milchstraßenlime konzentrieren Jedenfalls wurden wir, wenn wir den ganzen Himmel betrachten, eine positive Korrelation zwischen Milchstraßenlicht und Steinanzahl finden, und zwai für alle Großenklassen, auch die hellsten. In diesem Sinne kann man sagen, daß das Phanomen der Milchstraße in allen Großenklassen widergespiegelt wird, wenn auch in weit höherem Maße für die sehr schwachen Größen als für die helleren.

HOUZEAU vergleicht nach der Uranométrie Générale die Sterndichtigkeit in verschiedenen galaktischen Zonen miteinander. Wenn man die Zonen —30° bis +30°, um die Milchstraße herum, mit den übrigbleibenden Kalotten des Himmels vergleicht, findet man nach Houzeau für die so definierte galaktische Konzentration den Wert 1,38 für die Größen 1 bis 3 und 1,22 für die Größen 4 bis 6

Pickering<sup>1</sup> hat aus den Milchstiaßenzeichnungen von IILIS und Gouid eine rohe Intensitatstabelle für das Milchstiaßenlicht heigestellt. Er gibt in einer Skala von zehn Stufen die mittleien Intensitaten für Intervalle von 1<sup>h</sup> in R.A. und 5° in Dekl. Wenn er die Sternzahlen, auf gleiche Fläche reduziert, in der Milchstiaßenzone (10999 Quadratgrade) und in den außeigalaktischen Partien (25.641 Quadratgrade) vergleicht, findet er bis zur Größe 7 eine nahe konstante galaktische Konzentiation vom Betrage 1,85. Die Konzentiation ist sogar für die hellsten Größen ein wenig starker

Kapteyn und van Riijn definieren die galaktische Kondensation fur die Größe m als das Verhältnis zwischen der Anzahl der Steine von den hellsten bis zur Größe m pro Quadratgrad  $(N_m)$  in der Zone 0 bis 20° und der entsprechenden Anzahl fur die Zone 40° bis 90° Nach Searfs und van Riijn² ergeben sich für sukzessive photographische Größen die Werte in Tabelle 8 Die Kondensation ist nahezu konstant bis zur Große 10,0 und steigt dann allmählich, um für die schwachsten Größen sehr erhebliche Werte anzunehmen

Tabelle 8

101	Kond	211	Kond	311	Kond
4,0	2,5	10,0	2,6	16,0	5,8
5,0	2,5	11,0	2,9	17,0	7,1
6,0	2,5	12,0	3,1	18,0	8,5
7,0	2,5	13,0	3,5	19,0	10,7
8,0	2,5	14,0	4,1	20,0	13,2
9,0	2,5	15,0	4,8	21,0	16,2

Im Raume betrachtet sehen wir den unmittelbaren Grund des Milchstraßenphanomens und des damit verbundenen, zum Teil aquivalenten Phänomens der
galaktischen Konzentration der Steine in einem Zusammendidigen der Steine
gegen eine gewisse Ebene, die galaktische Ebene, welche durch die Zentrallime
der Milchstraße definiert wird. Wenn aber die Milchstraße etwa einer gleichförmigen Verteilung der Steine in einem zweidimensional unendlichen Stratum
entspräche und keine Absorption des Lichtes in diesem Stratum vorauszusetzen
ware, so ist es leicht einzusehen, daß die effektive Steingröße oder die Größe,
welche der maximalen Gesamthelligkeit für Steine innerhalb einer Größenklasse

<sup>&</sup>lt;sup>1</sup> Harv Ann 48, S 149 (1903)

<sup>&</sup>lt;sup>2</sup> Iransactions of the International Astronomical Union II, S 96 (1925)

entspricht, nach der Zentrallinie der Milchstraße hin sich gegen eine unendlich lichtschwache Größe verschieben würde, und daß gleichzeitig die Intensität gegen diese Zentrallinie anwachsen würde, so daß in der unmittelbaren Umgebung der genannten Linie selbst, wo die Sterne unendlich dicht gegeneinander gedrängt orscheinen würden, die Helligkeit sogar die photosphärische Helligkeit der Sterne erreichen sollte Die unmittelbare Beobachtung zeigt uns, daß die genannten Annahmen nicht zutreffend aud, was auf eine Begrenzung des Sternstratums oder auf Schwankungen der räumlichen Dichte hinweisen, aber auch durch eine Absorption des Lichts im interstellaren Raume bedingt sein kann. Mit größter Wahrscheinlichkeit sind alle drei Ursachen verhanden. Ohne Zweifel können wir jedoch a priori voraussetzen, daß die effektive Sterngröße der verschiedenen Partien der visuellen Milchstraße nicht überall dieselbe sein kann.

Wenn wir die Anzahl von Sternen zwischen den scheinbaren Größen ## und m + dm mit a(m) dm bezeichnen, so ist offenbar  $a(m) \cdot 10^{-0.4} = dm$  ein Ausdruck für die Gesamtholligkeit dieser Sterns. Wenn wir also genügend genaue Sternzählungen zur Verfügung haben, so ist es leicht, den Anteil verschiedener Größenklassen an der Gesamtlichtwirkung zu bestimmen

Für einen Quadratgrad der großen Sagittariuswelke hat S BAILEY1 eine Sternzählung bis zur 19 photographischen Größe vorgenommen Tabelle 9 gibt die Größe /(m) gemäß der Formel

$$\log/(m) = \log a(m) - 0.4 m + 3$$

für sukzessive Größenklassen nach diesen Zählungen, s(m) ist hier die Anzahl Sterno zwischen  $m-\frac{1}{2}$  und  $m+\frac{1}{4}$ .

Man orsieht aus der Tabelle, daß nach Baileys Resultaten die in dieser Gegend wirksamsten Sterne von der Größe 15 und 16 sind, abor auch daß die Funktion /(m) sich ziemlich langsam mit der Größe andert. Der Antell

Tabelle 9

	/ (=)	18	/ (=)	96	/(m)
10,0	1,5	13,0	1,4	16 <sub>1</sub> 0	5,1
11,0	1,5	14,0	2,9	17 <sub>1</sub> 0	2,8
12,0	1,0	15,0	6,9	18 <sub>1</sub> 0	1,3

der helleren Sterne an dem Gesamtlicht ist daher auch nicht unerhoblich. Für Größen heller als 10 wird jedoch die Anzahl Sterne so klein, daß es fraglich erscheint, ob die entsprechende Lichtmonge wirklich im wahrgenommenen kontinuierlichen Milchstraßenschein mitwirkt. Die effektive Größe des Milchstraßenlichts liegt daher hier wahrscheinlich nahe der Größe 15.

PANNEKOKE macht aber zu Balleys Sternzählung die Bemerkung, daß die daraus resultierende Totalhelligkeit (0,024 Sterne der Größe 0,0 pro Quadratgrad) viel kleiner ist als die ans dom Glanz der Wolke in Verbindung mit van Rhiins Messungen (Ziff. 5) ermittelte. Es ist daher möglich, daß BALLYS Zahlen von der Große 17 ab zu klein sind, wahrscheinlich infolge des Zusammendrängens der Sterne auf der Platte, oder vielleicht, daß die Größenskala nicht ganz in Ordnung ist. Nach der ersten Alternative wäre die effektive Größe noch schwächer als die oben gefundene.

Es mag in diesem Zusammenhang von Interesse sein, die am meisten effektivo Sterngröße vorschiedener galaktischer Zonen gemäß den über alle Längen gemittelten Sternzahlen, wie sie den Untersachungen über das "typische System" zugrunde liegen, zu ermitteln. In Tabelle 10 ist /(m) für die galaktische Breite 0° und 90° gemäß F H. Seares's Sternzahlen berochnet worden. Die effektive Sterngröße liegt offenbar nahe der Größe 13,0 für die galaktische Zone und nahe 8,5 für den galaktischen Pol.

BAN 4, 5 39 (1927). <sup>1</sup> Harv Circ 242 (1922).

Mt Wilson Contr 346 - Ap J 67, S. 67 (1928)

Die Beziehung der mittleren Sternzahlen zu der beobachteten Strahlung des allgemeinen Himmelsgrundes ist schon in Ziff 5 besprochen worden

HOPMANN<sup>1</sup> hat aus seinei Isophotenkaite untei Heianziehung dei von H Henie<sup>2</sup> und H Nort<sup>3</sup> ausgearbeiteten Verteilung der Sterne heller als 11<sup>m</sup>

Tabelle 40

	Tabout 10						
121	b == 0° f(m)	b == 90° f(m)	41)	b == 0° f (m)	$b = 90^{\circ}$ $f(m)$		
5 6 7 8 9 10 11	0,49 ,55 ,62 ,68 ,75 ,81 ,85	0,14 ,16 ,17 ,18 ,18 ,17	13 14 15 16 17 18 19	0,90 ,88 ,82 ,72 ,60 ,48 ,36	0,10 ,08 ,06 ,04 ,02 ,01 ,01		

den Anteil am Milchstraßenlicht der Sterne heller und schwacher als 14<sup>m</sup> fur verschiedene Regionen zu bestimmen versucht Fur die Sagittariuswolke stimmt sein Resultat qualitativ mit dem oben gegebenen überein. Für andere Regionen ergibt sich ein relativ größeier Anteil dei helleich Steine als fur die Sagittariuswolke

Ohne sehr wertgehende genaue Sternzahlungen bis zu außerordentlich

schwachen Gibßenklassen fur verschiedene Gegenden der Milchstraße konnen wir die Frage nach der effektiven Sterngröße nicht streng beantworten, und genugende Zahlungen dieser Art liegen noch kaum vor Da abei die Photographie weit mehr als die diickte Beobachtung die Umisse der Milchstraßenstruktur in isolierte Sterne auflöst, so liegt in der Milchstraßenphotographie wenigstens ein Mittel vor, eine obei e Gienze dei mittleien Helligkeit dei Steine in den Grenzgebieten der visuellen Milchstiaße zu finden. Wenn wit auf den Photographien feststellen, für welche Gienzgröße eine Struktur der Verteilung, den Umissen der visuellen Milchstraße entsprechend, zuerst hervortritt, konnen wir wenigstens den Schluß ziehen, daß die effektive Steingröße nicht meiklich heller als diese Gienzgibße sein kann Nach K Graff kann man annehmen, daß eist Steine von der Große 13 abweits die klare Begrenzung der Milchstraßenwolken hervorrufen Trotz des Umstandes, daß einige Einzelheiten der Milchstraßenstruktur schon bei helleren Größen hervortreten, können wir mit großer Sicherheit annehmen, daß die effektive Große des Milchstraßenlichts, gemaß der oben gegebenen Definition, in den helleren Partien der eben erwahnten oder sogar einer noch schwächeren Größe entspricht

Für eine Deutung dei Wolkenstruktur der Milchstraße ist es übrigens von Bedeutung, festzustellen, für welche Sterngröße die scheinbare Verteilung der Sterne inneihalb der Milchstiaßenzone eine deutliche Konselation mit dei Lichtverteilung der Milchstraße selbst zeigt. Sehr ausführlich ist dieses Problem von EASION<sup>5</sup> behandelt worden Er untersucht zuerst helle und dunklere Partien der Milchstraße in Aquila und Cygnus. Für die Steinzählungen liefeite für hellere Sterne die BD das Material, und für schwachere Sterne wurden die Sternrahlungen von HERSCHEL, CEI ORIA, EPSTEIN und WOLF innerhalb der betreffenden Regionen benutzt. Die sehr klaie Korrelation zwischen Steinzahl und Milchstraßenhelligkeit für die schwachen Steine bleibt in geringerem Maße auch für die BD-Steine schwacher als 9m bestehen, wahrend für hellere Sterne jede deutliche Kongelation verschwindet. In seiner spateren Arbeit vergleicht Easton den Dichtigkeitsgrad der BD-Steine nach der ausführlichen Bearbeitung dieser Sterne von W. STRATONOFF<sup>6</sup> mit dem Helligkeitsgrad der Milchstraße und erstreckt seine Untersuchung über den ganzen nördlichen Milchstraßenverlauf.

<sup>&</sup>lt;sup>2</sup> Lund Medd Ser II, Nr 10 (1913) <sup>1</sup> A N 222, S 86 (1924)

<sup>&</sup>lt;sup>a</sup> Recherches astron de l'Obs d'Utrecht VII (1917)

<sup>&</sup>lt;sup>1</sup> Grundriß der Astrophysik, S 715 (1928)
<sup>5</sup> A N 137, S 81 (1894), Ap J 1, S 216 (1895), A N 159, S 169 (1902), Proc Acad terdam 8, Nr 3 (1903)
<sup>6</sup> Publ Obs Taschkent 2 (1900) Amsterdam 8, Nr 3 (1903)

Es stellt sich hier horaus, daß eine kleine mit stelgender Helligkeit abnehmende Korrelation im ganzen auch für die helleren Klassen der Argelanderschen Sterne besteht Noch für die hellste Klasse, welche die Größen 0 bis 6.5 umfaßte. ist eine Spur davon vorhanden. Eine erheblich größere Korrelation für diese hellste Klasse ist aber von Newconn! horgeleitet worden, was wohl auch mit T C VAN DE LINDER Resultaten übereinstlimmt

Easton zieht aus der Übereinstimmung der Konzentrationspunkte für verschiedene Größen den Schluß, daß die schwachen Sterne der Milclistraße von uns nicht viel weiter entfernt sein können als etwa die Sterne 9, oder 40, Größe, und daß die scheinbaren Sternwelken auch wirklichen reellen Anhäufungen um Raumo entsprechen. Von unserem jetzigen Standpunkt aus müssen wir aber diese Auffassung als einen Fehlschluß betrachten. Daß eine Korrelation zwischen Sternverteilung und Milchstraßenhelligkeit auch für helle Größenklassen besteht. kann auch bedouten, daß die Ursachen der Wolkenstruktur wangstens zum Teil in unserer Nähe liegen und wesentlich in einer Absorption des Lichts in dunklen Wolken von nebliger oder staubförmiger Materie zu suchen and. Wir werden im folgenden sehen, daß diese Ausfassung in der letzten Zeit mehr und mehr Platz greift. Le ist jedoch jedenfalls ein bleibendes Verdienst von Easton, die Bedeutung der großen Streuung in absoluter Größe unter den Sternen für das Milchstraßenproblem erkannt zu haben.

NORT hat in seiner eben erwähnten Arbeit die Untersuchung von Easton auf Grund der Sternzählungen bis zur 11. Größe erweitert. Unter Verwendung einer von Easton bergestellten Isophotonkarte für den Südlimmel, die auf GOULDS, HOUZEAUS und BACKHOUSES Arbeiten beruht, hat er die Untersuchung auch auf die stidliche Milchstraße ausgedehnt. Er gibt in Tabellen und Figuren einen Vergleich zwischen Lichtintensität und Sterndichte für Gebiete der galaktischen Zone in Intervallen von 15° in L und 4° in B Er zieht den Schluß, daß das Phänomen der Milchstraße im ganzen noch nicht in der Verteilung der Sterne zwischen 9m,0 und 11m,0 undergespiegelt wird. Dieser Schluß ist in Übereinstimmung mit Pannerorrs Resultalen. daß kelne organische Verbindung zwischen der großen Masse der Sterne von der 9. bis vielleicht zu der 11. Größe und den Wolken, welche die Milchstraße bilden, besteht, widerspricht jedoch wohl in einem gewissen Grade den oben referierten Resultaten von Hofmann, nach denen in violen Fällen die Sterne heller als von der Größe 11 sogar in der Gesamtlichtwirkung dominieren sollen.

Daß eine ausgeprügte Korrelation zwischen dem Verlauf der Milchstraße und der Vertellung der Sterne bis etwa zur Größe 14 (visuell) besteht, ist z. B aus den umfangreichen Zählungen auf der Franklin-Adams-Karte, die von Charlier und seinen Mitarbeitern in Lund ausgeführt worden sind, ersichtlich. Eine Tafel, welche die Resultate bildlich wiedergibt, ist in CHARLIERS "California Lectures" gegebon.

17. Das Integralspektrum der Milchstraße. Effektive Entfernung der Milchstraßensterne. Das integrierte Spektrum von einigen galaktischen Wolken wurde zuerst von E. A. FATH auf dem Mount Wilson mit Expositionszeiten von 30, 67 und 74 Stunden erhalten. Das Ergebnis war ein Spektrum approximativ vom Sonnentypus. Da nach van Rhijns oben (Ziff 5) besprochener Arbeit ein beträchtlicher Teil der Strahlung des Himmelsgrundes auch für heile galak-

<sup>&</sup>lt;sup>1</sup> The Stars, S 273 (1902)

Do Verdeoling der boldere Sterren, S. 63 Rotterdam. Wyt & Zonen 1921.

Versi Akad Amsterdam 19, S. 243 (1910); Proc Acad Amsterdam 13, S. 239 (1910).

Lund Medd Sor II, 31 (1923)

Mem Univ Calif 7 (1926).

<sup>4</sup> Lund Medd Sar II, 31 (1923) Mt Wilson Contr 61 = Ap J 36, 8 362 (1912)

tische Regionen wahrscheinlich dem Zodiakallicht zuzuschleiben ist, so ist es

möglich, daß diese Lichtquelle in dem Resultat etwas mitspielt

E A Kreiken¹ hat fur 4000 Steine der Scutumwolke bis zur Große 14,9 die photographisch effektiven Wellenlangen bestimmt. Das Plattenmaterial hatte E Herfzsprung mit dem 60zölligen Reflektor auf dem Mount Wilson gesammelt. Im Mittel ergibt sieh ein Farbentypus, der eine Spektralklasse etwas früher als Go andeutet. Nach unseren Überlegungen in Ziff. 16 ist es wahrscheinlich, daß Kreikens Untersuchung die effektive Große des Milchstraßenlichts erreicht, und daß also die berechnete mittlere Farbe der Steine für dieses Gesamtlicht einigermaßen reprasentativ sein sollte. Das gewonnene Resultat ist naturlich von jedem Erdlicht oder Zodiakallicht frei und stutzt daher die Gultigkeit der von Fath erhaltenen Spektralklasse.

In einer spateren Arbeit<sup>3</sup> hat Kreiken unter Heranziehung anderen Materials die Farben der Milchstraßensteine bis zu noch schwacheren Großen studiert (vgl Ziff 22) Im Mittel eigibt sich für die Scutumwolke bis zur Größe 17,3 ein Farbenindex +0,38, wahrend Shapley<sup>3</sup> für 310 Steine zwischen den Größen 12 und 15 in derselben Wolke in der Umgebung des Sternhaufens M11 im Mittel +1-0,77 findet

Eine direkte Bestimmung des Faibenindex dei selben Wolke hat Pannekoekt volgenommen. Die Platten wurden von Wolff mit einem kleinen Zeiss-Tessal aufgenommen und extiafokal eingestellt, so daß die helleren Steine als isolieite Scheibehen eischeinen. Die Schwärzung auf dei Platte luhit außeidem vom galaktischen Licht und vom "Eidlicht" her, letzteies kann als übei das Feld konstant angesehen weiden. Die Valiation dei Schwalzung mit einer Valiation der photographischen Helligkeit (in Sternen dei Gloße 0 per Quadratgiad ausgedruckt) wurde aus den Steinscheibehen heller Steine einittelt. Der Zusammenhang zwischen Schwalzung und visueller Helligkeit des Milchstiaßenlichts in einer entsprechenden Einheit wurde aus den Pannekoekschen Isophoten nach ihrer Eichung gemäß van Rhijns Messungen bestimmt. Aus dem Verhaltnis der Koeffizienten der zwei Ausdrücke zieht Pannekoek den Schluß, daß die photographische Lichtstarke der Milchsträßenwolke 57/85 der visuellen beträgt. Dieses Verhaltnis entspricht einem Farbenindex von +0,43 und einer Spektralklasse F5.

Kürzlich haben W S Adams, M Humason und A. H. Joy<sup>5</sup> mit einem kleinen Spektrographen in Verbindung mit dem 40zölligen Cooke-Refraktor auf dem Mount Wilson Spektrogramme der Milchstraßenwolken in Sagittarius und Cygnus aufgenommen. Die Expositionszeiten waren 93 und 141 Stunden. Die Spektralklassen wurden in beiden Fällen früher als vom Sonnentypus, nämlich F5 für die Sagittariuswolke und F3 für die Cygnuswolke, gefunden. Infolge der kleinen Dispersion des Spektrographen laßt sich natürlich eine genauere Bestimmung der Radialgeschwindigkeit der Wolken nicht durchführen Von Bedeutung ist abei die Bemerkung, daß die Radialgeschwindigkeiten beider Wolken klein gefunden werden.

Wenn wir also für das Integralspektrum der Milchstraße die Klasse F5 annehmen, so ist es klar, daß wir es in diesem Falle mit einer Art von Mischspektrum zu tun haben, zu dem verschiedene Sterntypen mehr oder weniger ihren Beitrag liefern. Da aber die Klasse F5 und die diese Klasse in der Spektraliche unmittelbar umgebenden Typen unter den schwachen Sternen sehr zahlreich vertreten

<sup>&</sup>lt;sup>1</sup> On the Colour of Faint Stars in the Milky Way, and the Distance of the Scutum Group. Dissert Groningen 1923

Group Dissert Groningen 1923

M N 87, S 196 (1927)

Mt Wilson Contr 133 = Ap J 46, S 64 (1917)

<sup>&</sup>lt;sup>1</sup> BAN 2, S 19 (1923) <sup>5</sup> Publ ASP 39, S 368 (1927)

sind, so können wir mit einiger Wahrscheinlichkeit schließen, daß wir es in der Näho der "effoktiven" schembaren Größe im Durchschnutt mit Sternen dieser Spektralklasse zu tun haben, und zwar mit gewöhnlichen "Zwergsternen", da die "Riesen" dieser Klasse sehr selten im Raume sind und wir für die Sterne der schwachen Größenklassen keine sehr extreme Salektion nach großer absoluter Leuchtkraft vorauszusctzen haben. Wir können also für die mittlere absolute Größe der Sterne etwa +3 annehmen Die effektive Entfernung der Milchstraßensterne konnen wir als die Entfernung definieren, in der die effektive absolute Größe auf die effektive scheinbare Größe des Milchstraßenlichts reduziert wird Wenn wir für die letztere die Größe 14 fixieren, bekommen wir für die effektive Entfornung der Milchstraßensterne 1600 Parsec Für die Sagittariuswolke beträgt die effektive Entfernung etwa 2500 Parsec Der eingeführte Begriff der effektiven Entfernung ist natürlich genz unabhängig von der Frago, ob die Sterne Mitglieder einer reellen Wolkenstruktur sind oder in einem sehr ausgedehnten Stratum ziemlich gleichmäßig gestreut vorkommen Man erzieht ohne Schwierigkeit aus dem symmetrischen Verlauf von /(m) um die offektive Größe herum in Tabelle 9, daß diese Entfernung approximativ so abgemessen ist, daß eine Hälfte des galaktischen Lichts aus größerer, eine Hälfte aus kürzerer Entfernung stammt,

Eine wenn auch nur sehr grobe Kontrolle dieser Schätzung der effektiven Entfernung gibt uns das Phänomen der Tiefe oder des "dip" der Milchstraße Nach Tabelle 5, Ziff 11, bekommen wir im Mittel für die Tiefe  $\phi = \sigma - 90^\circ$  den Wert 26' Anderorseits finden wir in Ziff 21, daß die Sonne wahrscheinlich etwa 34 Parsec nördlich von der mittleren galaktischem Ebena geiegen ist. Wenn wir diese zwei Daten zusammenstellen, ergibt sich für die "affektive Entfernung" rein geometrisch etwa 4500 Parsec, was wenigstens der Größenordnung nach mit dem obigen photometrischen Resultat stimmt. Wenn wir z B PANNEKORES Wert der Tiefe,  $\phi = 65$ ', angenommen hätten, würe die Übereinstimmung viel besser.

18. Übersicht der allgemeinen statistischen Untersuchungen über die Vertellung der Sterne im Raume. Daß die Milchstraße als Phänomen durch eine Zusammenwirkung des Lichts von unzähligen Sternen, die in einer Schicht großer Sternhäufigkeit vertellt sind, entsteht, ist eine Ansicht, die im Altertum von DEMOKRIT, in der Neuzelt von KEPLER und GALILEI, und auf mehr naturphilosophischer Grundlage von Swedenborg, Wright, Kant und Lambert ausgesprochen wurde. Als Begründer der Stellarastronomie als empirischer Wissenschaft ist aber W. HERSCHEL ansusohan. Die empirische Grundlage der Feststollungen Herschels sind in don vielerwähnten Sternelchungen enthalten. Er zählte für verschiedene Punkte des Himmels die Auzahl Sterne, die im Felde seines Reflektors sichtber waren. Der Bearbeitung des Materials lag die Annahme einer bis zu einer gewissen Grenzfläche gleichförmigen Dichte im Sternsystem zugrunde Die verschiedene Fülle sichtbarer Sterne in verschiedenen Gegenden des Himmels mußte dann auf eine Erschöpfung aller Sterne bis zur Grenze des Systems zurückgeführt werden, und der Abstand der Grenze in einer gewissen Richtung wurde durch eine einfache Formel direkt aus der Sternzahl berechnet So gelangte Herschel zu der wohlbekannten Darstellung des Systems in Form eines linsenförmigen Gebildes, dessen größter und kleinster Durchmesser 860 und 220 "Sirlusabstände" betragen. In seinen späteren Jahren wurden allerdings die Ansichten Herschells etwas modifiziert; die Tiefe der Milchstraße erscheint ihm in gewissen Gogonden unermeßlich.

<sup>&</sup>lt;sup>1</sup> Phil Trans 74, S 437 (1784), 75, S 213 (1785), Collected Scientific Papers I, B. 157 fL, 223 ff

Die Weiterentwicklung der Stellarstatistik im 19 Jahrhundert ist an eine Reihe von Namen geknupft, von denen wir is G. W. Struve, G. V. Schlaparflit, II Gylden erwahnen können. Ihre vollstandigste Entwicklung und gewissermaßen einen vorlaufigen Abschluß finden die neuen Methoden in den Arbeiten II. V. Speligers<sup>1</sup>

An Stelle der Annahme, daß die Steine alle ungefahr dieselbe absolute Leuchtkraft besitzen, tritt die Annahme einer statistischen Verteilung der wichlichen Helligkeiten, die durch eine Lummositatsfunktion ausgedruckt wird. Die absolute Leuchtkraft i wird als die auf die Entfernung i reduzierte scheinbare Helligkeit verstanden, und die Proportion der Steine in einer Volumeneinbeit, die zwischen i und i+di liegen, wird durch den Ausdruck  $\varphi(i)di$  defimert, wo  $\varphi(i)$  die Lummositatsfunktion darstellt. Die Anzahl aller Steine in der Volumeneinheit für die Distanz r innerhalb der betreffenden Region des Himmels ist eine Funktion D(r) von r. Wenn wir das Problem der Verteilung in aller Allgemeinheit angreifen, mussen wir die Moglichkeit offen lassen, daß  $\varphi(i)$  von Ort zu Ort wechseln kann, m a W daß das Mischungsverhaltnis verschiedener absoluter Größen mit der Entfernung wechseln kann. Die Leuchtkraftsfunktion sollte also  $\varphi(i,r)$  geschrieben werden

Die schembare Helligkeit h ist mit i durch die Relation

$$i = \frac{h \, r^a}{\psi \left( r \right)} \tag{1}$$

verbunden, wo  $\psi(r)$  die Einwirkung einer etwaigen Absorption des Lichtes im

Raume Rechnung tragt

Die Anzahl A aller Sterne, die auf ein Flachenstück des Himmels von der Größe  $\omega$  projiziert und die heller als von der scheinbaren Lichtstärke h erscheinen, kann jetzt in der Form eines Doppelintegrals aus den Funktionen  $\varphi$ , D und  $\psi$  ausgedruckt werden. Wenn wir zuerst die Anzahl dA der Sterne im scheinbaren Helbigkeitsbereiche zwischen h und h+dh ins Auge fassen, bekommen wir fast unmittelbar die folgende Integralielation

$$\frac{dA}{dh} = -\omega \int_{0}^{\sigma} D(r) \frac{r^{1}}{\psi(r)} \varphi \left( \frac{h r^{2}}{\psi(r)}, r \right) dr, \qquad (2)$$

wo  $\sigma$  die obere Integrationsgrenze in r angibt. Fur die mittlere Parallaxe  $\pi(h)$  der in Betracht genommenen Sterne von der scheinbaren Helligkeit h oder von der scheinbaren Größe m, wo

$$m=-2,5\log h,$$

haben wir dann auch, wenn r in Paisec ausgedruckt wird,

$$\pi(h) \frac{dA}{dh} = -\omega \int_{0}^{a} D(r) \frac{r^{3}}{\psi(r)} \varphi\left(\frac{hr^{3}}{\psi(r)}, r\right) dr$$
 (3)

Fur Selecters Analyse besonders charakteristisch sind die folgenden Annahmen, erstens, daß für die absolute Leuchtkraft i eine obere Grenze H angegeben werden kann, welche allerdings vom Orte im System abhängen kann, und zweitens, daß eine Entfernung  $r_1$  gefunden werden kann, außerhalb welcher die Sterndichtigkeit so schnell abnummt, daß wir von einer wirklichen Begrenzung des Systems bei  $r=r_1$  reden können. Diese Annahmen sind natürlich von Be-

Ausführliche Bibliographie und zusammenfassende Darstellung von G. Di Urschland, V.J.S. 54, S. 25 (1919) Eine spätere Arbeit ist "Untersuchungen über das Sternsystem" Sitzber d. Bayer Akad d. Wiss, Math-phys KI (1920)

deutung für die obere Integrationsgrenze  $\sigma$  Wenn wir Sterne von so großer scheinbarer Helligkeit in Betracht ziehen, daß auch Sterne der absoluten Leuchtkraft H noch innerhalb der Grenze  $r_1$  stehen müssen, um der gewählten scheinbaren Helligkeit zu entsprechen, ergibt sich  $\sigma$  aus der Relation.

$$h = \frac{H(a) \psi(a)}{a^{4}}$$

Wenn aber die Entfernung, in der die absolut hellsten Sterne die scheinbare Helligkeit h besitzen, die Grenze  $r_1$  überschreitet, haben wir als obere Integrationsgrenze  $\sigma=r_1$  zu setzen. In dieser Weise bekommt man zwei verschiedene Ausdrücke für die theoretischen Sternzahlen und mittleren Parallaxen für hellere und schwächere Sterngrößen,

Eine Folge dieser Aufspaltung der Formeln für die theoretischen Sternzahlen bei einer gewissen Sterngröße m=n, wolche einen Stern der absoluten Helligkeit H an der Grenze  $r=r_1$  kennzeichnen würde, ist eine Unstetigkeit in den zweiten Differenzen der Sternzahlen A. Wenn wir also in üblicher Weise die Sternzahlen A durch eine Interpolationaformel  $\log A(m) = \alpha + \beta m + \gamma m^2$  darstellen wollen, so genügt diese Formel nicht in dem genzen Bereich von Größenklassen, sondern wir müssen mit Sekliger annehmen

$$\log A(m) = \alpha + \beta (m-n) - \gamma (m-n)^{n}, \quad \text{für} \quad m < n,$$

$$\log A(m) = \alpha + \beta (m-n) - \gamma_{1} (m-n)^{n}, \quad \text{für} \quad m > n$$

Um aber aus den beobechteten Stornzahlen zu einer praktischen Bestimmung der Dichte- und Luminositätsverteilung zu gelangen, müssen wir die vereinfachende Annahms einführen, daß die Luminositätsfunktion und auch die maximale Helligkeit unahhängig vom Orte sind, d. h. das Mischungsverhältnis der absoluten Helligkeiten seil überall dasselbe sein. Die Frage, ob eine Absorption im Raume vorhanden ist, kann dadurch vorläufig umgangen werden, daß wir die "scheinbare" Entfernung  $\varrho$  und Dichte  $A(\varrho)$  in folgender Weise einführen,

$$\varrho^{\mathbf{a}} = \frac{r^{\mathbf{a}}}{\psi(r)}, \quad A(\varrho) = D(r)\psi(r)\frac{dr}{d\varrho}.$$
(4)

Wir bekommen dann aus (2) für die Sternzahlen verschiedener Grenzgrößen ##

$$A(m) = \omega \int_{0}^{\pi} A(\varrho) \, \varrho^{a} \, d\varrho \int_{0}^{\pi} \varphi(\pi) \, d\pi \,, \tag{5}$$

WO

$$\sigma = \begin{cases} \sqrt{\frac{H}{h_m}}, & \text{für } m < n, \\ \sqrt{\frac{H}{h_n}}, & \text{für } m > n. \end{cases}$$

 $h_m$  und  $h_n$  sind die den Größen m und n entsprechenden Holligkelten. Für die mittleren Parallaxen haben wir dann die Formel

$$\pi(m)\frac{dA}{dh_m} = -\omega \int_0^{\pi} \Delta(\varrho) \frac{\varrho^a}{\sqrt{\psi(r)}} \varphi(h_m \varrho^a) d\varrho , \qquad (6)$$

wo also die Absorptionsfunktion w(r) explizit auftritt.

Die Sternzahlen der helleren Größenklassen folgen nahezu dem Gesetz

$$A = oh^{\frac{1-3}{2}},\tag{7}$$

wo λ mit der galaktischen Breite zunimmt. Seeliger weist nach, daß eine solche Form der Funktion Λ unabhängig von der Luminositätsfunktion einem Dichtegesetz

 $\Delta = \gamma \varrho^{-\lambda} \tag{8}$ 

entsprechen muß. Die Integralgleichung (5) für hellere Größenklassen gibt somit Aufschluß über die "scheinbare" Dichteverteilung, während die entsprechende Gleichung für schwächere Klassen die Eigenschaften der Luminositätsfunktion bestimmen kann. Die Gleichung der mittleren Parallaxen kann dann zur Bestimmung der Absorptionsfunktion  $\psi(r)$  benutzt werden, wodurch die wahre Dichtefunktion D aus  $\Delta$  hergeleitet wird; praktisch muß jedoch eine solche Verwendung dieser Gleichung für eine Verbesserung der "scheinbaren" Dichtefunktion  $\Delta$  zurücktreten. Bei zu vernachlässigender Absorption ergibt nämlich die Dichtefunktion (8)

 $\pi(m) = c \left(\frac{h_m}{H}\right)^{\frac{1}{8}} \tag{9}$ 

unabhängig von der Luminositätsfunktion, eine Formel, die mit den Kaptrynschen mittleren Parallaxen in Widerspruch steht. Zur Erzielung einer Übereinstimmung muß die Dichtefunktion (8) modifiziert werden, da nur eine Einführung der Absorptionsfunktion nicht genügt.

Die veränderte Form des Dichtigkeitsgesetzes lautet

$$\Delta(\varrho) = \gamma(\varrho^{-\lambda} - a\varrho^{-\lambda_1}), \qquad (10)$$

wo der zweite Term in der Klammer nur für unsere nähere Umgebung von Redeutung ist (allernächste Umgebung,  $\varrho=0$ , ist ausgeschlossen). Für die Luminositätsfunktion nimmt Seeliger an

 $\varphi(i) = I^* \{ x^{-r} e^{-h^2 [(\log x)^2 + b \log x + c]} - x e^{-h^2 s} \}, \tag{11}$ 

wo x = i/H ist.

Bei der Konstantenbestimmung aus den empirischen Daten vereinfacht sich jedoch dieser Ausdruck praktisch auf  $\varphi(i) = Ie^{-a(\log \epsilon)^2 - b\log \epsilon}$ . Die maximale Leuchtkraft H wird aus den mittleren Parallaxen der hellsten scheinbaren Größen gemäß (9) bestimmt. Die Grenzentfernung  $r_1$  ist durch einen Sprung in den Differentialquotienten  $\frac{d^2\log A}{dm^2}$  und  $\frac{d\log \pi}{dm}$  bei einer gewissen Größe m=n bedingt, und kann direkt durch die Beträge dieser Sprünge berechnet werden, aber auch durch die Beziehung  $\varrho_1 = H^{\frac{1}{2}}h_n^{-\frac{1}{2}}$ .

Die Beobachtungsdaten für Seeligers Untersuchungen waren in den ersten Arbeiten die BD und deren südliche Fortsetzung bis zur Dekl. --23°. Für die helleren Sterne dienten die Harvard-Photometry und die Potsdamer Durchmusterung, und für die schwächeren Größenklassen wurden die Eichungen von den beiden Herschel ausgewertet. Für spätere Arbeiten spielte das in Groningen von Kapteyn und van Rhijn zusammengestellte Material die größte Rolle. Die Werte der mittleren Parallaxen waren die von Kapteyn aus den parallaktischen Eigenbewegungen hergeleiteten.

Die Ermittlung der räumlichen Verteilung geschah teils für das schematische Sternsystem, bei welchem die Abhängigkeit der Sternzahlen von dem scheinbaren Ort völlig vernachlässigt wird, und teils für das typische Sternsystem, für welches die Abhängigkeit von der galaktischen Breite berücksichtigt wird. Das Phänomen der Milchstraße äußert sich in Smeligens Resultaten wie in den Herschelschen in einer beträchtlich größeren Ausdehnung des Systems in der Ebene der Milchstraße als in anderen Richtungen. Für die Grenze in der Milchstraßenzone gibt Seeliger in seiner letzten Arbeit den Abstand 725 Sirius-

weiten (3625 Parsec) und für die Grenze in der Richtung des galaktischen Pols den Abstand 180 Sirlusweiten (900 Parsec). W. Sametinger hat später in einer neuen Durchrechnung für die Grenzentfernung in den zwei Richtungen 2820 und

1260 Parsec gefunden

Die Schnelligkeit, mit der die Sterndichtigkeit gegen die Grenzfläche des Systems abnimmt, und auch die Entfarnung der Grenze selbst in verschiedenen Richtungen hängt natürlich von einer Schätzung der Absorption des Lichts im Raume, d h von der Funktion  $\psi(t)$ , ab. Die eben gegebenen Entfernungen der Gronze setzten vornus, daß die Absorption zu vernachlässigen ist, also daß w(r) = 1zu setzen ist, womit A und D idontisch werden Wenn man mit Sekliger vom Gesetze  $\Delta(\rho) = \gamma \rho^{-1}$  ausgeht und voraussetzt, daß die wahre Sterndichtigkeit D(r) nicht gegen die Grenzfläche hin wachsen darf, so bekommt man einen Höchstbetrag für die Absorption durch vorgelagerte Massen wie auch für eine allgemeine Absorption des Lichtes im Raume, der in beiden Fällen sehr klein ausfällt, und swar so klein, daß der Einfluß auf die räumliche Ausdehnung des Systoms als gering anzuschen ist. Im letzteren Falle hat man  $\psi(r) = e^{-rr}$  zu setzen und bekommt dann nach (4) die wahre Dichtigkeit durch die Formal

$$D(r) = \Delta \left( r \, e^{\frac{1}{4} r r} \right) \left( 1 + \frac{1}{4} r r \right) e^{\frac{1}{4} r r} \tag{12}$$

Für den maximalen Absorptionskoeffizienten (per Parsec gerechnet) in diesem

Falle findet SEELIGER 0.0000617.

Mit dieser Überlegung ist aber sicher nicht die Frage einer merklichen Absorption des Lichtes definitiv erledigt. Das vorausgesetzte "scheinbare" Dichtigkeitsgesetz, einschließlich der scharfen Grenze bei  $r=r_1$ , ist für die großen Entfernungen eine sehr schematische Annahme über die Dichtefunktion und kann keine strengere Gültigkeit beanspruchen. Es scheint schon aus diesem Grunde sehr fraglich, ob ingendeine zuverlässige Abschätzung der Absorption

nach dem genannten Prinzip gemacht worden kann

Les ist auch aus anderen Gründen ersichtlich, daß die Maschen des "typischen" Sternsystems viel zu grob sind, um die Verteilung der Sterne für größere Entfernungen in dem ditnnen gelektischen Stretum mit einiger Zuverlässigkeit zu fangen. Die Struktur der Milchstraße zeigt in mehreren Zügen unzweideutige Einflüsse einer mit dem scheinbaren Orte wechselnden Absorption durch neblige oder staubfürmige Materie. Im "typischen Sternsystem" werden Einzelhelten dieser Art, die Ahhängigkeit von der galaktischen Breite innerhalb einer Zone sowie jede Abhängigkeit von der galaktischen Länge in einer allgemeinen Mittelbildung ausgeglichen Wir werden auf die diesbezüglichen Fragen in späteren Abschnitten zurückkommen.

Die Methode, die von J. C. KAPTEYN\* und seinem Mitarbeiter und Nachfolger P. J. van Rhijns befolgt wurde, um aus boobachteten Sternzahlen und statistischen Parallaxon die Dichtigkeitsfunktion und die Leuchtkraftsfunktion su bestimmen, ist nicht an mathematisch definierte Näherungsausdrücke gebunden, sondern besteht in einer Im Prinzip voranssetzungafreieren tabellarischen Behandlung des empirisch gegebenen Materials. Die Anzahl Notes der Sterne zwischen sukzessiven Intervallen in schelnbarer Größe m und Eigenbewegung  $\mu$ wird unter Benutzung der empirisch bestimmten Funktionen  $n_{n,n}$  (mittlere Parallaxo für gegebene Werte von m und  $\mu$ ) und  $\chi_{m,m,\mu}$  (die Verteilungsfunktion der wahren Parullaxen um diesen Mittelwort horum) über aukzessive Intervalle in

<sup>&</sup>lt;sup>1</sup> SEELIGER-Festschr S. 276 (1924)

Groningen Publ Nr. 11 (1902); A J 566 (1904); Groningen Publ Nr. 29 (1918), Nr. 30 (1920); Mt Wilson Contr. 188 — Ap J. 52, S. 23 (1920).
Groningen Publ. Nr. 34 (1923), Nr. 36 (1925), Nr. 38 (1925)

 $\pi$  verteilt. Aus der resultierenden Tabelle mit doppeltem Eingang nach m und  $\pi$ können Luminositätsfunktion und Dichtigkeitsfunktion direkt abgelesen werden, und zwar wird die erstere für sukzessive Parallaxenintervalle wiederholt bestimmt. Die Methode ist im grundlegenden Prinzip frei von einer Hypothese über die Absorption des Lichtes im Raume. Die Verschiebung der Luminositätskurye zwischen sukzessiven Parallaxenintervallen ist aber durch das Vorhandensein einer Absorption bedingt; wenn man dieselbe Luminositätsfunktion für verschiedene Distanzen postuliert, kann der Absorptionsbetrag gewissermaßen beurteilt werden. Da aber keine deutliche Spur einer Absorption vorhanden ist, kann nur ein Höchstbetrag derselben geschätzt werden. Für die Luminositätsfunktion wurde in den früheren Arbeiten sehr nahe eine normale Verteilung in absoluter Größe (der Gaussschen Fehlerkurve analog) gefunden, was auch mit Seeligers Resultaten übereinstimmt. In der späteren Arbeit von van Rhijn wird jedoch dieses Ergebnis für die schwächsten absoluten Größen erheblich modifiziert, indem die Häufigkeit der schwächsten absoluten Größen keine Abnahme zeigt, sondern einen weiteren schwachen Anstieg. Für die Herleitung der Luminositätsfunktion ist hier auch eine andere Methode, welche nur gemessene trigonometrische Parallaxen benutzt, herangezogen worden.

In Analogie mit Seeligers typischem Sternsystem wird in der Kapteynschen Statistik angenommen, daß die Dichtigkeitsverteilung Rotationssymmetrie

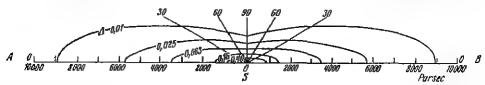


Abb. 11. Die Dichtigkeitsverteilung im typischen System nach Kaptryn und van Riija.

um eine Achse durch die Sonne senkrecht zur Milchstraße hat. Die ermittelte Dichtigkeitsverteilung ist in Abb. 11 illustriert. Die Abbildung stellt einen Schnitt durch das Sternsystem senkrecht zur Milchstraße dar. Die Kurven entsprechen Flächen konstanter Dichtigkeit und sind nur auf der einen Seite der Symmetricebene ausgezogen worden.

Eine ausführliche Darlegung der Kapteynschen Methoden in einer allgemeinen Behandlung der stellarstatistischen Probleme hat W. J. A. Schouten<sup>1</sup> gegeben.

In Seeligers Theorie sind die Annahmen einer maximalen Grenze der absoluten Leuchtkraft und einer Begrenzungsfläche, außerhalb der die Sterndichtigkeit als verschwindend klein angesehen werden kann, miteinander eng verknüpft. Die Erfahrungstatsachen, auf denen diese Annahmen beruhen, d. h. die Sprünge in den Werten gewisser Differentialquotienten, sind, wenn auch wahrscheinlich vorhanden, doch verhältnismäßig sehr geringe Effekte. Die speziellen Ansätze der eben genannten Art sind daher für eine statistische Analyse nicht als notwendig zu betrachten. Ohne irgendeine vorausgesetzte Beschränkung der absoluten Leuchtkraft i oder der oberen Integrationsgrenze in in hat Schwarzschild eine allgemeine Lösung der zwei Integralgleichungen der Sternzahlen und mittleren Parallaxen gegeben,

Von großer praktischer Bedeutung ist eine Lösung von Schwarzschild, bei der für die Sternanzahl einer Größenklasse und für die mittleren Parallaxen

On the Determination of the Principal Laws of Statistical Astronomy. Diss. Amsterdam 1918.

<sup>&</sup>lt;sup>a</sup> A N 185, S. 81 (1910).

gewisse geeignete Näherungsausdrücke gewählt worden. Wir bezeichnen mit a(m) dm die Anzahl der Sterne zwischen den Größen m und m + dm und mit  $\pi(m)$  die mittlere Parallaxe derselben Sterne. Wenn die absolute Größe

$$M = -2.5 \log i$$

eingeführt wird und die Verteilung der absoluten Größen durch eine Funktion  $\varphi_1(M)$  gegeben wird, so daß

$$\varphi(i)\,di = -\varphi_1(M)\,dM,$$

und wenn die Absorptionsfunktion  $\psi(r) = 1$  gesatzt wird, so können die Integralausdrücke für a(m) und  $\pi(m)$  in folgender Form geschrieben werden

$$a(m) = \omega \int_{0}^{\infty} D(r) \varphi_{1}(m - 5 \log r) r^{2} dr,$$

$$\pi(m) a(m) = \omega \int_{0}^{\infty} D(r) \varphi_{1}(m - 5 \log r) r dr.$$
(13)

Jetzt wird vorausgesetzt

$$\log a(m) = \kappa_0 - \kappa_1 m - \kappa_1 m^2, \log \kappa(m) = P_0 - P_1 m,$$
(14)

wo  $\kappa_0$ ,  $\kappa_1$ ,  $\kappa_2$ ,  $P_0$ ,  $P_1$  Konstanten and. Diese Annahmen führen auf die folgende Form der Funktionen D(r) und  $\varphi_1(M)$ , wenn wir  $\tau = -5\log r$  einführen,

$$\log D(r) = a_0 - a_1 r - a_n r^n,$$

$$\log \varphi_1(M) \Rightarrow b_0 - b_1 M - b_n M^n,$$
(15)

was direkt durch Einsetzung in die Gleichungen (13) und Ausführung der Integration verifiziert werden kann.

Die Funktion  $\varphi_1(M)$  ist eine GAUSSsche Fahlerkurve mit der Streuung

$$\sigma = \sqrt{\frac{\log s}{2b_0}}$$

und dem Mittelwert

$$M_0 = -\frac{1}{2} \frac{b_1}{b_1}$$

Der Ansatz (14) entspricht im Durchschmtt sehr wehl den empirischen Resultaten von Kapteyn, und die Ausdrücke (15) für D und  $\varphi_1$  geben auch die analytische Form der Hauptresultate der Kapteynschen Analyse wieder.

K Schwarzschild hat auch gozeigt, daß men unter der Annahme einer normalen Verteilung der Logarithmen der räumlichen Geschwindigkeiten der Sterne in bezug auf die Sonne die Kapthynschen Resultate für die Funktionen  $\pi_{n,\mu}$  und  $\chi_{n,\frac{m}{n},\mu}$  reproduzieren kann.

Wenn  $\varphi_1(M)$  und a(m) bekannt sind, bekommt man die Koeffizienten  $a_1$  und  $a_2$  von D nach den Formeln

$$a_{1} = -0.6 + \frac{b_{1}n_{0} - b_{0}n_{1}}{b_{0} - n_{0}},$$

$$a_{1} = \frac{b_{0}n_{0}}{b_{1} - n_{0}},$$
(16)

<sup>1</sup> A N 190, S. 361 (1912).

Aus den numerischen Werten von Kapteyn und van Rhijn<sup>1</sup> erhält man z. B. die folgenden Resultate, wo a(m) pro Quadratgrad gerechnet wird:

log 
$$a(m) = -4.542 + 0.724$$
  $m - 0.0141$   $m^2$  (Gal. Breite 0°)  
log  $a(m) = -4.903 + 0.774$   $m - 0.0221$   $m^2$  (Gal. Breite 90°)  
log  $\varphi_1(M) = -2.394 + 0.1858M - 0.03450M^2$   
log  $D(r) = -2.532 + 2.478$  log  $r - 0.593$  (log  $r$ )<sup>2</sup> (Gal. Breite 0°)  
log  $D(r) = -6.219 + 6.120$  log  $r - 1.538$  (log  $r$ )<sup>2</sup> (Gal. Breite 90°)

Die Konstanten  $a_0$  und  $b_0$  sind hier so angepaßt, daß die Dichte in der Umgebung der Sonne als Einheit für D benutzt wird, während  $\varphi_1(M)$  die Anzahl Sterne pro Kubikparsee nahe der Sonne für verschiedene absolute Größen glbt.

Die hier gegebene Funktion  $\varphi_1(M)$  entspricht

$$M_0 = +2.7, \qquad \sigma = 2.5.$$

Zu bemerken ist, daß die gegenwärtig am meisten gebrauchte Skala der absoluten Größen um fünf Einheiten größer ist als die oben benutzte. In dieser Skala, in der die absolute Größe als die auf die Entfernung 10 Parsec reduzierte scheinbare Größe definiert wird, ist daher  $M_0 = +7.7$ . Die Formel für D(r) hat natürlich keine Gültigkeit in unserer unmittelbaren Umgebung, da offenbar für r=0 die Formel D=0 gibt. Es soll schließlich betont werden, daß die eben gegebenen einfachen Ausdrücke für  $\varphi_1(M)$  und D(r) durch neuere Untersuchungen, besonders durch van Riiijns Arbeit in Groningen Publ. 38, wo auch die einzelnen Spektraltypen separat behandelt werden, in mehrfacher Weise modifiziert worden sind.

Wichtige Beiträge zu der statistischen Behandlung der Dichtigkeitsverteilung sind in C. V. L. Charliers<sup>2</sup> Arbeit "Studies in Stellar Statistics" enthalten. Unter anderem wird von Charlier bemerkt, daß, wenn man die Seeligerschen Annahmen der oberen Begrenzungen in Leuchtkraft und Entfernung fallen läßt, die Gleichung

$$\frac{dA}{dh} = -\omega \int_{0}^{\infty} D(r) \varphi(hr^{2}) r^{4} dr,$$

in Verbindung mit dem Sternzahlgesetz (7) der helleren Größen

$$\frac{dA}{dh} = ch^{-\kappa},$$

nicht mit Notwendigkeit auf die Lösung  $D(r) = \gamma r^{-1}$  und eine arbitrüre Leucht-kraftsfunktion führt, sondern daß ihr auch durch den Ansatz

$$\varphi(z) = \frac{1}{z^n} \tag{17}$$

bei beliebiger Dichteverteilung Genüge geleistet wird, und zwar ist es möglich, daß sogar unendlich viele Lösungen existieren.

CHARLIER nimmt für die Funktionen a(m) und  $q_1(M)$  normale Frequenzkurven vom "Typus A" an, wo jedoch nur die generierende Funktion selbst gebraucht wird. Die Ausätze sind also mit denen der oben besprochenen gleichzeitig publizierten Arbeit von Schwarzschild identisch. Die Dichtigkeitsfunktion D(r) wird dann auch eine normale Frequenzkurve in  $\log r$ . Die mittleren Parallaxen werden in der Form

$$\pi(m) = K e^{-\lambda m} \tag{18}$$

<sup>&</sup>lt;sup>1</sup> Mt Wilson Contr 188 = Ap J 52, S. 23 (1920).

<sup>&</sup>lt;sup>2</sup> Lund Medd Ser II, 8 (1912).

ausgedrückt,  $\lambda$  wird aus den mittleren Eigenbewegungen verschiedener scheinbarer Größen bestimmt, die einem analogen Gesetz mit demselben Werte von  $\lambda$  gehorchen. Die Konstanten der Leuchtkrufts- und Dichtigkeitsfunktionen werden gemäß diesem Resultat ermittelt.

CHARLIER verläßt die Approximation des "typischen Systems" und teilt den Himmel in 48 gleich große Flächen nach galaktischer Länge und Breite, innerhalb deren die Statistik unabhängig ausgeführt wird, was unzweifelhaft eine prinzipiell weit richtigere Problemstellung bedeutet. Eine ausführliche Übersicht der mathematisch-statistischen Grundlagen zur Analyse der Dichtigkeitsverteilung ist in Charliers vorher (Ziff 17) erwähnten "California Lectures" gegeben.

Einige für die Stellarstatistik besonders wichtige Ralationen sind von K G. Malmouist hergeleitet werden. Wenn die Leuchtkraftfunktion eines Volumens im Raumo einem normalen Verteilungsgesets gehorcht, so ist unter gewöhnlichen Bedingungen auch die scheinbare Leuchtkraftsfunktion, d. h. die Verteilung der Sterne von der scheinbaren Größe m nach absoluter Größe M, sehr nahe eine normale Frequenzkurve. Wenn die wahre Leuchtkraftsfunktion durch den Mittelwert  $M_0$  und die Dispersion  $\sigma$  bestimmt wird und wenn wir die scheinbare Leuchtkraftsfunktion durch eine Entwicklung vom Typus A,

$$F(M) = \varphi_{\mathbf{n}}(M) + A_{\mathbf{n}}\varphi_{\mathbf{n}}^{II}(M) + A_{\mathbf{d}}\varphi_{\mathbf{n}}^{IV}(M) + \cdots, \tag{19}$$

ausdrücken, wo

$$\varphi_{m}(M) = \frac{1}{\sigma_{m}\sqrt{2\pi}} s^{\frac{(M-M_{m})^{2}}{2\sigma_{m}^{2}}}$$
(20)

die generierende Funktion und  $\varphi^{III}$ ,  $\varphi^{IV}$ , die dritten und vierten Ableitungen nach M darstellen, so hat man

$$M_{m} = M_{0} - \sigma^{0} \frac{df}{dm},$$

$$\sigma_{m}^{0} = \sigma^{0} + \sigma^{d} \frac{d^{0}f}{dm^{0}},$$

$$\left[ \frac{3}{4} A_{0} = \sigma^{0} \frac{d^{0}f}{dm^{0}}, \right]$$

$$\left[ \frac{4}{4} A_{4} = \sigma^{0} \frac{d^{0}f}{dm^{0}}, \right]$$

$$(21)$$

WO

$$f(m) = \log \operatorname{nat} a(m) \tag{22}$$

Ähnliche Beziehungen gelten auch für die Leuchtkraftsfunktion der Sterne heiler als eine gewisse Größe m. Wenn  $M_0$  und  $\sigma$  für eine besondere Klasse von Sternen bekannt sind, kann die scheinbare Leuchtkraftsfunktion, durch die Ableitungen von  $\log a(m)$  in der oben gagebenen Weise gebildet, für eine Ermittlung der Dichtigkeitsverteilung der betreffenden Sterne im Raume gebraucht werden, da diese mit einfacher Rechnung durch die doppelte Verteilung der Sterne nach scheinbarer und wirklicher Größe gegeben sein muß. Von besonderer Bedeutung and diese Relationen, wenn  $\sigma$  klein ist, so daß die höheren Potanzen dieser Größe vernachlässigt werden können.

Wenn aber die Dispersion der absoluten Größen für irgendeine Klasse von Sternen klein ist, können wir auch folgendermaßen vorgehen. Wenn die Dispersion Null waru und alie Sterne dieselbe absolute Größe M<sub>6</sub> besäßen, so hätte

Lund Modd 100 - Ark Mat Astr Fys 16, Nr. 23 (1922).

man offenbar zwischen der Dichtigkeitsfunktion D(r) und der Sternzahlfunktion  $a_1(m)$  die Relation

 $\omega r^{2}D(r)dr = a_{1}(M_{0} + 5\log r)d(5\log r),$ 

also

$$D(r) = \frac{5\log\sigma}{\omega r^3} a_1(M_0 + 5\log r). \tag{23}$$

Die Variation von M, der Dispersion o entsprechend, kann jetzt als eine Abweichung von einem idealen Zustande betrachtet werden und ihr Einfluß auf a(m) dem eines gleich großen Beobachtungsfehlers in m gleichgesetzt werden, Wir suchen daher die ideale Funktion  $a_1(m)$  aus der beobachteten a(m) zu bestimmen. Nach einer Formel von Eddington haben wir in der Tat

$$a_1(m) = a(m) - \frac{\sigma^8}{2} \frac{d^3a}{dm^2} + \frac{\sigma^4}{8} \frac{d^4a}{dm^4} - \cdots$$
 (24)

Wenn a(m) tabuliert mit dem Intervalle  $\alpha$  in m vorliegt, haben wir approximativ die zweite Differenz

$$a(m+\alpha)-a(m-\alpha)-2a(m)=\alpha^2\frac{d^2\alpha}{dm^2}.$$
 (25)

woraus  $d^2a/dm^2$  bestimmt wird. Der Term in  $\sigma^4$  wird für kleines  $\sigma$  vernachlässigt.

Ernster Zweifel an der Gültigkeit der Annahme einer approximativ rotationssymmetrischen Verteilung der Sterne um die Sonne herum wurde wohl zuerst durch H. Shapleys<sup>a</sup> Studien tiber die Lagen der kugelförmigen Sternhaufen im Raume erregt. Auf die eigentümliche scheinbare Verteilung der Haufen scheint zuerst K. Bohling in einer bemerkenswerten Arbeit aufmerksam gemacht zu haben; er hat auch eine Anordnung dieser Haufen um den Zentralpunkt des Sternsystems herum für wahrscheinlich gehalten. Für diesen Punkt ergeben sich nach seinen Resultaten die Koordinaten  $L = 321^{\circ}34'$ ,  $B = -2^{\circ}56'$ . Die scheinbare Verteilung wurde weiter von A. R. Hinks4 und von E. Hertzsprung5 untersucht. Gleichzeitig mit Shapley hat Charliere die Verteilung im Raume ermittelt auf Grund der Annahme, daß der wahre Durchmesser für alle Haufen derselbe ist. Die absolute Skala der Entfernungen wurde jedoch hier viel zu klein angenommen. In Shapleys Arbeit wurde die Stellung der Haufen als trotz der gewaltigen Entfernungen zum Sternsystem gehörige Gebilde sehr wahrscheinlich gemacht. Der Zentralpunkt des Sternhaufensystems liegt nach Shap-LEY in der Richtung  $L=327^{\circ}$ ,  $B=0^{\circ}$ , in einer Entfernung von etwa 16000 Parsec. Das "System der Haufen" ist jedoch in Hinsicht auf die Dichtigkeitsverteilung so unregelmäßig definiert, daß die Schätzung der Entfernung des Zentralpunktes unsicher bleibt. (Über den Einfluß der Absorption vgl. Ziff. 33.)

Außer durch die regelmäßige Verteilung der Haufen in bezug auf die galaktische Ebene wird die Zugehörigkeit dieser Objekte zum Milchstraßensystem durch den Umstand gestützt, daß die allgemeine Intensität und Mächtigkeit der Milchstraßenwolken in der Gegend des scheinbaren Zentralpunktes ihr Maximum erreicht. Der Beweis, daß die Stellung der Sonne im Sternsystem in der Tat eine ausgeprägt exzentrische ist, und daß das Zentrum in einer Richtung nahe L = 327° zu suchen ist, wurde jedoch erst kürzlich durch die Sternzählungen schwacher Sterne in den Kapteynschen Selected Areas gegeben. Die Harvard-Groningen Durchmusterung wurde von Kreiken, zu einer Statistik der Dichte-

<sup>&</sup>lt;sup>1</sup> M N 73, S. 359 (1913).

Mt Wilson Contr 151—157, 160, 161, 175, 176, 190 u. 195; Ap J 48—52 (1918—1920),

K Svenska Vet Akad Handi 43, Nr. 10 (1909).

M N 71, S. 693 (1911).

A N 192, S. 261 (1912).

Lund Medd Ser II, 19 (1918).

M N 85, S. 499 (1925); 86, S. 665 (1926).

verteilung ausgenutzt, und endlich das vorzügliche, auf exakten photometrischen Messungen gegründete Mount Wilson-Material von Skares¹ diskutlert. Für hellore Größen wurden auch die Kataloge der photographischen Himmelskarte benutzt. Die Abweichungen  $\Delta$  der Zahlen  $\log N_{\infty}(N_{\infty}=$  Zahl der Sterne pro Quadratgrad heller als die Größe m in der internationalen photographischen Skala) von einer mittleren rotationssymmetrischen Verteilung werden von Skares versuchsweise in der Form

$$\Delta = a + b\cos(L - L') \tag{26}$$

dargestellt. Die Länge L' wurde für vorschiedene Grenzgrößen zwischen m=9 und m=18 und für verschiedene galaktische Breiten ermittelt.

Eine etwas exzentrische Stellung der Sonne in einem sphäroidischen System von konstanter Dichtigkeit gibt als theoretischen Ausdruck für ⊿

$$s + F\cos(L - L_0) \tag{27}$$

 $L_0$  ist dann die Richtung gegen des Zentrum des Systems<sup>a</sup> Aus einer systematischen Verschiedenhaut für nördliche und südliche Breiten schließt Skares auf

ememit der Sterngröße wechselnde Konrektion des Goulnschen Milchstraßenpols. Er führt daher in den theoretischen Ausdruck für A auch die Terms

$$\pm G \mp k \cos(L - L_1) \qquad (28)$$

ein, wo obere und untere Vorzeichen für nördliche bzw. südliche Breite gelten. Der wahre Pol, durch die Sterne einer gewissen Breite B ermittelt, ist um den Betrag  $\phi$  in der Länge  $L_1$  vom Gouldschen Pol entfernt, wo

$$p = \frac{k}{D}$$
,  $D = \frac{d \log N}{dB}$ . (29)

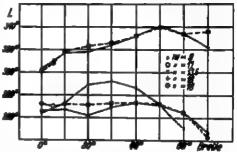


Abb 12. Die Länge des Zentrums (Ordinate) für verschiedene gelaktische Zonen (Abssisse) und verschiedene Gronsgrößen

Durch Zusammensetsung von (27) und (28) bekommt man offenbar eine Form (26), wo aber L', a, b für nördliche und südliche Breiten verschieden ausfallen. Aus den empirischen Werten für L', a, b für nördliche und südliche Breiten berechnet man dann leicht die wahre Länge  $L_{\bullet}$  der tiefsten Richtung im System und die wahre Amplitude der logarithmischen Sternzeitlen, wie auch die Werte  $L_1$  und  $\phi$ . In dieser Weise bekommt Sranze die Lagen des Pols für verschiedene Grenzgrößen, die in Ziff. 11 gegeben und diskutiert worden sind, und die folgenden Werte für die Länge des Zentrums

Die Werte  $L=L_0$  für verschiedene Zonen und Grenzgrößen werden in Abb. 12 dargestellt.

Shares findet eine markente parallele Verschlebung in  $L_0$ ,  $L_1$  und  $\phi$  mit der Starngröße m. Da aber die Werte für  $L_1$  und  $\phi$  für hellere Größen erhebliche Differenzen gegen die in direkter Weise von van Rhijn ermittelten zolgen, so dürfte wohl die mehr indirekte Methode von Seares hier nicht als ganz einwandfrei zu bezeichnen sein.

Für die schwächsten Größen m=16 und 18 findet Seares  $L_0=319^\circ$ , was sehr wohl mit Shapleys Zentralpunkt für die Kugelhaufen,  $L=327^\circ$ ,

<sup>&</sup>lt;sup>1</sup> Mt Wilson Contr 346-347 - Ap J 57 (1928)

<sup>1</sup> L baw L and bel SEARES mit L baw L bezolchnot.

harmoniert. Kreiken hatte für die Grenzgröße 17 in seiner Arbeit  $L_0=314^\circ$  gefunden. Man kann diese Werte mit Hopmanns und Pannekoeks Resultaten für die Verteilung des galaktischen Lichts vergleichen (Ziff. 5 und 11). Hopmann fand ein sehr ausgeprägtes Maximum um  $L=315^\circ$  herum, während Pannekoek

für die Länge des allgemeinen Lichtmaximums 323° herleitete.

Die Verschiebung in  $L_0$  von 267° für m=9 bis 319° für die schwächsten Größen schreibt Seares, in Übereinstimmung mit den Ansichten vieler anderer Forscher, z. B. mit Hopmanns Ausführungen in seiner eben besprochenen Arbeit, dem Einfluß eines weit ausgedehnten "lokalen Systems" zu, das hauptsächlich die Verteilung der helleren Sterne bestimmt, während die Verteilung der schwächsten Größen dem großen System entspricht. Die Ausdehnung des lokalen Systems in der galaktischen Ebene schätzt er auf ungefähr 6000 Parsec. Da die Verschiebung des Pols für die helleren Größen gegen den Pol der hellen Heliumsterne vor sich geht und gleichzeitig die Länge des Konzentrationspunktes gegen die Länge der größten Häufigkeit dieser Sterne verschoben erscheint, schließt er auf eine Zusammengehörigkeit, und daß also der Haufen der nahen Heliumsterne den Kern des großen lokalen Systems bildet (vgl. Ziff. 19). Nach van Rhijns Resultaten scheint jedoch die Verschiebung des Pols für die Größen 9 bis 13,5 sehr zweifelhaft, was die Argumentation von Seares einigermaßen abschwächt.

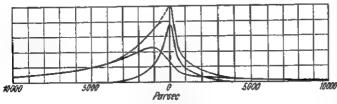


Abb. 13. Die Dichtefunktion nach Seares (obere Kurve) in zwei Telle, dem lokalen System und dem großen System entsprechend, zorlegt.

Um die Sachlage noch mehr zu beleuchten, berechnet Seares aus den Sternzahlen für die Längen  $L_0$  und  $480^{\circ} + L_0$  in der galaktischen Ebene mit Hilfe einer Gaussschen Luminositätskurve die entsprechende Dichtigkeitsverteilung nach

der Schwarzschildschen Mothode. Für die Sterndichte D(r) findet er die Resultate der Tabelle 11.

Tabelle 11.

	1	(2)		D(r)		
r	$L_{b}$	180° + L	7	$L_0$	180° + L	
1	1,00	1,00	6310	0,15	0,03	
100	0,98	0,93	7943	- 11	02	
200	,95	1 .79	10000	,08	,014	
316	,90	,63	12590	,06 ,04 ,03	,01	
500	,84 ,70	,47 ,28	15850	,04	ļ :-	
1000	70	,28	19950	,03		
2000	,49	17	25120	,02	_	
3162	,33	,08		·		
3981	,27	,06				
5012	,20	,04			1	

Die räumliche Sterndichtigkeit nimmt also viel schneller gegen das Antizentrum als gegen das Zentrum ab. Trotzdem ist ein großer Überschuß in unserer unmittelbaren Nähe ersichtlich. Seares versucht (Abb. 13) die Frequenz in zwei Kurven zu zerlegen, von denen die eine das lokale System, die andere das große System repräsentieren soll. Den totalen Durchmesser des großen Systems schätzt Seares zu 60000 bis 90000 Parsec. Daß die letztere Kurve asymmetrisch erscheint, deutet Seares als einen Einfluß der großen Absorptionsgebiete der Milchstraße in der zentralen Himmelsgegend.

Außer diesem Hinweis auf eine mögliche Absorption des Lichtes in gewissen Gegenden des Systems hat aber Srares die Möglichkeit der Erklärung der größeren Sterndichtigkeit in unserer Nähe durch eine allgemeine Absorption des Lichtes in den galaktischen Regionen nicht berücksichtigt. Wir werden spater Golegonheit haben, ein wenig auf diese Frage einzugehen.

Unter früheren wichtigen Arbeiten anderer in diesem Zusammenhang nicht erwähnter Autoren, die mit weniger Vollständigkeit des zur Verfügung stehenden Materials Abwolchungen von einer rotationssymmetrischen Verteilung studiert haben, sind zu nennen die von H Norti, H. C. PLUMMER und H H TUENER.

J. HALM stellt ornstlich in Frage, ob die gewöhnliche Annahme einer vom Orto im System unabhängigen Leuchtkraftefunktion wurklich als annähernd zutreffend anzuschen ist Es scheint nach seiner Ansicht vielmehr, daß die Hotorogonität der scheinbaren Verteilung eher durch Schwankungen der Leuchtkraftsfunktion als durch Variationen der räumhehen Dichte erklärt werden kann Es scheint sogar möglich, daß die Sterne in der Milchstraße scheinbar zahlreicher vorkommen, nicht wall sie räumlich zusammengedrängt sind, sondern weil sie eine größere absolute Leuchtkraft besitzen.

Von großer Bedeutung ist auch die Untersuchung Pannekorks fiber die Dichtigkeitsvertellung in unserer näheren Umgebung auf Grund einer erneuten sorgfültigen Analyse der Durchmusterungskataloge Er verläßt vollkommen die schematischen Annahmen des "typischen Systems" und sucht m unserer Umgebung die wahren Kondensationen zu bestimmen. Er vertritt auch die Ansicht. daß ein lokales System als eine selbständige geschlossene Einheit, eine "Wolke" nicht existiert, sondern sich in eine Mange kleinerer Gruppen, die als Individuen in das große System eingehen, auflösen läßt.

19. Die Vertellungsgesetze verschiedener Spektraltypen. Die große Streuung der allgemeinen Louchtkraftsfunktion der Sterne und die wahrscheinlich bedoutendo Abweichung dieser Funktion von einer Gaussschen Fehlerkurve für die schwachen absoluten Helligkeiten macht es sehr schwierig oder soger unmöglich, ohne eine Aufspaltung des Materials in Klassen von kleinerer Dispersion sichoro Resultate über die Dichtigkeitsverteilung im Sternsystem zu bekommen. Pine partielle Aufspaltung der genannten Art bietet schon die Klassifizierung in die Harvard-Spektraltypen und auch die in großen Zügen mit dieser Klassifizierung aquivalenten Bestimmungen der Sternfarbe. Für die "frühen", heißen Spoktraltypen bedeutet nämlich die Klassifizierung oder Ferbenbestimmung eine Grupplerung nach absoluter Größe mit verhältnismäßig kleiner Streuung innerhalb der Gruppen. Da welter die spezielleren Methoden zur spektrographischen Bestimmung absoluter Größen gegenwärtig auch für schwache Sterne, wenn auch in mehr summarischer Form, verwendbar sind, so eröffnet sich hier ein Weg zu einer genaueren Analyse der Sternverteilung in den verschiedenen Richtungen von unserem Ort im System aus. Wir sind jedoch auf diesem Geblete nech kaum über die Pionierarbeit hinausgekommen. Wir wollen hier die Hauptergubnisso der Spektraldurchmusterungen in bezug auf die allgemeine Dichtigkeitsverteilung unserer näheren Umgebung im Sternsystem kurz erwähnen und später (Ziff. 22) die spezielleren Untersuchungen der Milchstraßenregionen behandoln.

Das gegonwärtig wichtigste statistisch ausgenutzte Material ist in dem DRAFER-Katalog der Harvard-Stornwarte enthalten. Die scheinbare Verteilung

<sup>&</sup>lt;sup>1</sup> Recharches satronomiques de l'Obs d'Utrocht VII (1917)

M N 78, S. 668 (1918). M N 80, S. 162 (1919). • M N 85, B. 610 (1925).

Publ Astr Inst Univ Amsterdam Nr. 1 (1924); Nr. 2 (1929)

verschiedener Spektraltypen am Himmel ist ausführlich von G. ZAPPA<sup>1</sup>. H. Shapley<sup>2</sup>, C. V. L. Charlier<sup>8</sup>, A. Pannekoek<sup>4</sup> und O. Seydl<sup>5</sup> statistisch untersucht worden. SEYDL gibt im zweiten Teil seiner Arbeit für Sterne heller als 7<sup>m</sup>,0 die scheinbare Dichtigkeitsverteilung der verschiedenen Spektraltypen in galaktischen Koordinaten in einer Serie von Karten wieder. Die zuerst von E. C. Pickering nachgewiesene Variation der scheinbaren galaktischen Konzentration mit der Spektralklasse kommt in diesen Untersuchungen sehr schön zum Vorschein. Die viel kleinere galaktische Konzentration der Spektralklassen. von F bis M, mit den Klassen B und A verglichen, wurde oft als ein im wesentlichen scheinbarer Effekt gedeutet, der als eine Folge einer mit der Spektralklasse sich ändernden mittleren absoluten Leuchtkraft der Sterne auftritt. Eine Vergrößerung der absoluten Leuchtkraft bedeutet nämlich einen Zuwachs der mittleren Entfernung für eine und dieselbe scheinbare Größe, was infolge der allgemeinen Konzentration der Sterne gegen die galaktische Ebene eine vergrößerte scheinbare Konzentration gegen die Milchstraße mit sich bringt. Wenn auch dieser Erklärungsgrund für das Intervall B-F einigermaßen zutrifft, ist es doch wegen der ziemlich großen absoluten Helligkeiten der großen Mehrzahl der K- und M-Sterne des Katalogs, die kaum der mittleren Helligkeit der A-Sterne nachstehen, durchaus klar, daß das Phänomen auch auf reelle Verschiedenheiten in der Anhäufung gegen die Milchstraßenebene zurückzuführen ist. Einen direkten Nachweis in dieser Richtung hat P. J. van Rhijn gegeben, der eine Trennung verschiedener Spektraltypen bei Bestimmung der Leuchtkrafts- und Dichtigkeitsverteilung nach der Kapteyn-Methode unternommen hat. Die Abnahme der absoluten Dichtigkeit der A-Sterne und der Riesensterne späterer Spektraltypen mit wachsender Entfernung von der galaktischen Ebene ist auch von B. LINDBLAD<sup>8</sup> und H. Petersson<sup>9</sup> bestimmt worden. Die kleinere Konzentration der späten Riesen tritt hier sehr deutlich hervor und wird als eine Folgeder für diese Sterne größeren Dispersion der Geschwindigkeitskomponente senkrecht zur Milchstraße gedeutet (vgl. Ziff. 28).

Die Dichtigkeitsverteilung der A-Sterne in der Richtung gegen den galaktischen Pol ist von K. G. Malmouist10 ermittelt worden auf Grund einer Bestimmung der Farbenäquivalente nach der Methode von Seares für 3700 Sterne innerhalb 10° Distanz von dem galaktischen Pol, von denen jedoch nur eine kleine Prozentzahl A-Sterne sind.

Zu den bedeutendsten aus dem Harvard-Material der helleren Sterne gewonnenen stellarstatistischen Resultaten gehört dasjenige über die Verteilung der Sterne der Spektralklasse B, der Heliumsterne, in unserer Umgebung. Wichtige Untersuchungen sind hier von Kapteyn<sup>11</sup>, Charlier<sup>12</sup>, Shapley<sup>18</sup>, B.P.Gerasimo-

Publ R. Specola di Collumnia (A) 1, S. 59 (1921).
 Harv Circ 240 (1922); 248 (1923).
 Lund Medd Ser II, 36 = K Svenska Vet Akad Handl 4, Nr. 3 (1927).
 Publ Astr Inst Univ Amsterdam Nr. 2 (1929).
 Publ Obs Nat Prague 6 (1929).
 Harv Ann 26, S. 152 (1891); 56, S. 1 (1912).
 Groningen Publ 38, Tab. 27, 45 (1925).
 Nova Acta Reg. Soc. Scient. Upsallensis, Volumen extra ordinem 1927 = Upsala.
 Medd 11; Ark Mat Astr Fys 19 B, Nr. 15 (1926) = Upsala Medd 14.
 The Distribution of Distances and Velocities of Stars in the Carrington Zone on the Bosis of Spacetrophotometric Applets. Diss. Hersela 1927 = Hyperia Medd 190.

Basis of Spectrophotometric Analysis. Diss. Upsala 1927 = Upsala Medd 29.

<sup>10</sup> Lund Medd Ser II Nr. 37 und 46 (1927).

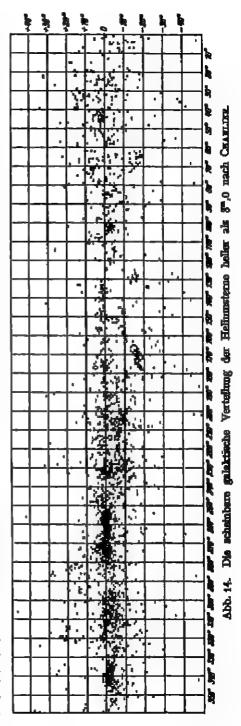
<sup>11</sup> Mt Wilson Contr 82 = Ap J 40, S. 43 (1914); Mt Wilson Contr 147 = Ap J 47, S. 104, 146 u. 255 (1918).

<sup>18</sup> Nova Acta Reg, Soc, Scient, Upsaliensis (IV) 4, Nr. 7 (1916); Ibid., Volumen extra. ordinem 1927; Lund Modd Ser II, 14 und 34.

<sup>&</sup>lt;sup>18</sup> Mt Wilson Contr 157 = Ap J 49, S. 311 (1918); Mt Wilson Comm 54 (1918); 64 (1919); Scientia, Marz 1920; A N Jub.-Nr. S. 25 (1921); Harv Circ 239 (1922); Harv Bull 846, S. 12. (1927)

VIȹ und Pannekoek® ausgoführt worden Die Hellumsterne zeigen eine sehr starke scheinbare Konzentration gegen die Milchstraße hin, aber wie oben (Ziff. 13) crwahnt wurde, hat die Symmetricchene der helleren B-Sterne emo beträchtliche Neigung gegen den aus den Milchstraßenwolken ermittelten größten Kreis Charlier gibt für den Pol der helleren B-Sterne seiner ersten Arbeit R.A. 183°,34, Dekl +28°,74, was bel Annahme des Gouldschen Milchstraßenpoles den galaktischen Koordinaten  $L = 165^{\circ}$ ,  $B = +83^{\circ}$ , 4 ontspricht und ım System der Tabelle 7, Ziff 11,  $L = 158^{\circ}$ ,  $B = +80^{\circ}$ , 0 gibt. Die Neigung der Symmetrieebene gegen die Goulde Milchatraßenlinie ist also 6°,6, mit dem aufsteigenden Knoten in  $L = 255^{\circ}$ ; die Neigung gegen die mittlere Ebeno der schwachen Sterne beträgt 10°,0. SHAPLEY selgt, daß diese Notgung mit abnohmender Helligkeit abnimmt und schon zwischen den Größen 7 und 8 fast vollständig verschwindet Dasselhe Verhältnis wiederholt alch in geringerem Maße für die A-Sterne Die Verteilung der helleren Sterne zeigt auch hier eine gewisse Neigung der Symmetricebeno gegon die Milchstraße, welche Neigung für schwächere Größen vorschwindet.

Die scheinbare Verteilung der Heliumstorno heller als 8m,0 am Himmel wird nach Charler in Abb. 14 illustriert. La ist offenbar, in walchem hohen Grade diese Storne in getrennten Flocken von beträchtlicher Konzentration auftroton, was in KAPTEYNS Arbeit eine große Rolle spielt und neuerdings von Pannekoek besonders hervorgehohen wird. Eln Maximum der Anhäufung findet sich in der Carlnagegend, um  $L = 260^{\circ}$  herum. Die Projektion der räumlichen Verteilung auf die Milchstraßenebene wird in Abb. 15 nach CHAR-LIER wiedergegeben. Die Entfernungen der individuellen Sterne sind unter der Annahme konstanter absoluter Leuchtkraft Innerhalb der Untergruppen Bo,



B1 usw. ermittelt worden. Man bekommt hier den Eindruck, daß diese Sterne eine gewisse Einheit bilden. Die Aufspaltung in kleinere Gruppen, die in der scheinbaren Verteilung so deutlich hervortritt, ist aber auch hier zu spüren. Die äußere Begrenzung des Haufens ist von der Grenzgröße des Materials (m=8.0) bedingt. Für das Zentrum des Haufens findet Charlier eine Entfernung von 63 Parsec (13 Siriometer) in der Richtung  $L=243\,^{\circ},90$ ,  $B=-13\,^{\circ},80$ .

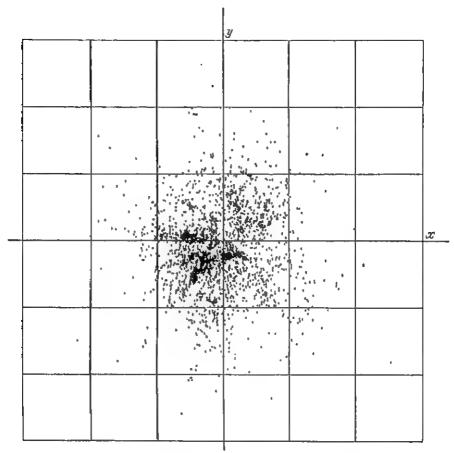


Abb. 15. Die Verteilung der Hellumsterne (Bo bis B5) heller als  $8^{m}$ ,0 in der galaktischen Ebene (X-Achse gegen  $L = 0^{\circ}$  gerichtet).

Gerasimovič teilt die Sterne in zwei Gruppen, heller und schwächer als die Größe 6,7, und findet für das Zentrum dieser Gruppen

$$m < 6.7$$
:  $L = 225^{\circ}.5$ ,  $B = -12^{\circ}.0$ ,  $R = 77$  Parsec,  $m > 6.7$ :  $L = 268^{\circ}.5$ ,  $B = -9^{\circ}.0$ ,  $R = 204$  Parsec.

Dieses Resultat stimmt mit den Ansichten Shapleys überein, nach denen wir hauptsächlich in der helleren Gruppe die Mitglieder eines lokalen Haufens vor uns haben, während wir für schwächere Helligkeiten es mit einer Mischung zwischen Haufensternen und Sternen des allgemeinen Milchstraßenstratums zu tun haben. Gerasimovic hat auch die allgemeinen Dichtigkeitsflächen der B-Sterne ermittelt. Die Abplattung der Flächen vermindert sich je nach der

Entfernung von der Sonne. Der Halbmesser des ganzen lokalen Haufens sollte wenigstens 1000 Parsec betragen. Nach Pannekoek löst sich aber der "lokale Haufen" der B-Sterne in eine Menge kleinerer, voneinander unabhängiger Haufen oder Ströme auf

Die Kurven gleicher Dichtigkeit in der Umgebung der Sonne hat Krriken<sup>1</sup>

für B- und A-Sterne zu ziehen versucht.

G. Sharn<sup>a</sup> hat einen Versuch gemacht, die Hauptzüge der räumlichen Dichtigkeitsverteilung für B-, A-, F-, K- und M-Sterne aus dem Material des Harvard-Katologa zu ermitteln. Die Abhängigkeit der scheinbaren galaktischen Konzentration vom Spektraltypus in der Some O bis F wird als ome Folge der Veränderung in mittlerer absoluter Größe gedoutet; die verhältnismäßig kleine galaktische Konzentration der K-Sterne ist nach Shajn auf eine Inhomogenität dieser Sterne in bezug auf ihre absolute Größe zurückzuführen, insbesondere auf eine Beimischung von Stornen, die intermediär zwischen "Riesen" und "Zwergen" sind, unter die Sterne in den schwächeren Größenklassen. Für die M-Sterne muß er aber sine reelle Abweichung der räumhehen Dichtigkeitsverteilung von ihrem gewähnlichen Charakter annehmen. Die Schnelhekeit der Dichtigkeitsabnahme mit der Entfornung ist für fast alle Kinssen beträchtlich größer als die von Kaptryn und van Rhijn für Sterne im allgemeinen gefundene.

Was die raumliche Dichtigkeitsverteilung in der Nähe der galaktischen Ebene bis zu größeren Entfernungen betrifft, so führen die weiteren Unterauchungen auf diesem Gebiet, angesichts der sehr erheblichen lokalen Verschiedenheiten in dem galaktischen Gürtel, mit Notwendigkeit auf detaillierte Untersuchungen der hellen und dunklen Partien der Milchstraße, die wir in Ziff. 22

näher besprechen werden.

Zur Beurteilung der allgemeineren Fragen über die galaktleche Konzentration für verschiedene Spektraltypen wird in der Zukunft ein vorzügliches Material in den Spektraluntersuchungen der Solected Areas vorliegen Ein wichtiger Beitrag liegt hier schon in F BECKERS Spektraldurchmusterung der KAPTEYN-Eichfelder des Stidhimmels vor Diese Arbeit enthält auch eine vorläufige Statistik über die Verteilung der Spaktralklassen nach galaktischer Breite und nach der scheinbaren Helligkeit sowie über die räumliche Verteilung der Storne. Weitere Beitrage werden hier in der Zukunft die Stornwarten Mount Wilson und Hamburg gebon, wo die Storne der Kapteynschen Felder bis zu etwa der Größe 12 klassifiziert werden.

Eine auf ausgewählte Partien des Himmels sich beziehende Spektraluntersuchung, die in gewissen Gegenden bis zur Größe 11,5 bis 12 reicht, wird von Miss Cannon an der Harvard-Sternwalte in der "Henry Draphe-Extension"

ausgeführt4.

Auf der Sternwarte Stockholm ist gegenwärtig eine allgemeine Untersuchung der Spaktra in gowissen Milchstraßenregionen bis zu etwa der Größe 13 begonnen worden. Es wird hier besonders eine Berticksichtigung der spektralphotometrischen Kriterien, die zur Beurteilung der absoluten Größen der Sterne dienen können, beabsichtigt.

20. Die galaktische Vertellung spezieller Objekte von großer absoluter Leuchtkraft. Die Objekte von sehr großer absoluter Helligkeit zeigen in der Regel eine außerordentlich markante scheinbare Konzentration gegen die Milch-

M N 85, S. 985 (1925).
 A N 232, S. 17 (1926).
 Publ Astrophys Obs Potsdam Nr. 88, 89, 90 (1929—1931).
 Über den Fortschritt dieser Arbeit a. besonders Shapley, "Sidereal Explorations". The Rice Institute Pamphlet 18, Nr. 2 - Harv Reprint 68 (1931).

straße. Wahrscheinlich haben wir hier eine Kombination von zwei verschiedenen Ursachen, teils einen scheinbaren Effekt der größeren mittleren Entfernung, teils aber eine allgemeine Vergrößerung der absoluten galaktischen Konzentration mit steigender absoluter Helligkeit (vgl. Ziff. 19). Um zwischen diesen beiden Effekten zu unterscheiden, müssen wir aus der scheinbaren Verteilung die wahre Verteilung im Raume herleiten. Bei unserer oft mangelhaften Kenntnis der Entfernungen ist dies in vielen Fällen nur in unvollständiger Weise möglich.

Eine Folge der großen scheinbaren galaktischen Konzentration einer hestimmten Gruppe ist es zunächst, daß auch mit einer geringen Anzahl von Objekten die Feststellung der Lage der Symmetrieebene möglich wird. E. Hentzsprung<sup>1</sup> hat (Tab. 12) eine Zusammenstellung der Lagen des Poles für ver-

schiedene Klassen von Objekten gegeben.

Tabelle 12.

Klasse	Pol der Konz	Anzahi der		
1714290	А	D	Objekto	
Heliumsterne (Oc5 bis B9).	182°,1	-l-27°,9	1402	
Spektraltypus N.,	194,2	27 ,4	228	
Oa bis Oe	190 ,7	26 9	87	
Bedeckungsveränderl	188 ,2	25 ,8	150	
Cephei-Sterne	195 ,9	26 ,8	60	
- und ac-Sterne	189 .1	26,3	98	
Gasnebel , ,	192 .7	28 ,1	130	

Für 97 Sterne vom Typus Oa—Oe5 findet W. Gyllenberg<sup>2</sup> unter der Annahme einer ellipsoidischen Verteilung für die kürzeste Achse die Richtung  $A = 191^{\circ}, 28$ ,  $D = +27^{\circ}, 13$ .

B. P. Gerasimovič<sup>3</sup> findet für 144 O-Sterne des Draper-Katalogs

$$A = 189^{\circ} 13'$$
,  $D = +27^{\circ} 22'$ ,

und für 78 planetarische Nebel

$$A = 192^{\circ} 13', D = +28^{\circ} 28',$$

unter Verwendung der Newcombschen Berechnungsmethode.

J. Schilt's findet für 340 c-Sterne eine sehr gute Übereinstimmung mit der galaktischen Ebene nach Pickering (Lage des Pols  $A=190^{\circ}, D=+28^{\circ}$ ).

Es ist übrigens augenscheinlich, daß alle Klassen außer der ersten in Tabelle 12, welche die B-Sterne umfaßt, eine Lage des Pols in sehr guter Übereinstimmung mit dem allgemeinen Milabete Bereite des Pols in sehr guter Übereinstimmung mit dem allgemeinen Milabete Bereite des Pols in sehr guter Übereinstimmung mit dem allgemeinen Milabete Bereite des Pols in sehr guter Übereinstimmung mit dem allgemeinen Milabete Bereite des Pols in sehr guter Übereinstimmung mit dem allgemeinen Milabete Bereite des Pols in sehr guter Übereinstimmung mit dem allgemeinen Milabete Bereite des Pols in sehr guter Übereinstimmung mit dem allgemeinen Milabete Bereite des Pols in sehr guter Übereinstimmung mit dem allgemeinen Milabete Bereite stimmung mit dem allgemeinen Milchstraßenpol (Ziff. 11) ergeben.

Außer den verschiedenen Graden von galaktischer Konzentration ist es auch von großer Bedeutung, daß in vielen Fällen die galaktische Länge einen sehr merklichen Einfluß auf die scheinbare Verteilung zeigt. Allerdings muß man hier vorsichtig sein, da eine Selektion auf Grund einer mehr oder weniger intensiven Beobachtung gewisser Himmelsregionen vorliegen kann.

N. C. Dunér<sup>5</sup> hatte auf die große galaktische Konzentration der Sterne von Secchis Typus IV (Harvard-Typus N und R) aufmerksam gemacht. Diese Erscheinung wurde von T. E. Espin<sup>6</sup> und J. A. Parkhurst<sup>7</sup> näher untersucht und bestätigt. Später hat Espin<sup>8</sup> die galaktische Verteilung verschiedener Objekte von pekuliaren Spektraltypen untersucht. Die größte Konzentration zeigen

<sup>&</sup>lt;sup>1</sup> A N 192, S. 261 (1912). <sup>8</sup> A N 226, S. 327 (1926).

Lund Medd 75 (1917).
BAN 2, S. 47 (1924).

Sur les étoiles à spectres de la troisième classe. K Svenska Vet Akad Haudi 21, Nr. 2,
 S. 126 (1885).
 Ap J 10, S. 169 (1899).
 Yerkes Publ 2, S. 127 (1903).
 J Can R A S 7, S. 79 (1913).

nach ihm die Wolf-Rayet-Sterne (Typus O), von denen etwa 98% zwischen galaktischer Breite 0° und ±10° liegen. Dann folgen in der Reihe abnehmender Konzentration die nouen Sterne, die Sterne mit hellen Wasserstofflinien, die Gasnebel und die N-Sterne Auffallend ist, daß « B die R-Sterne eine sehr viel kleinere Konzentration als die N-Sterne aufweisen Espin findet auch die mittlere galaktische Breite in den einzelnen Gruppen entschieden negativ, was auf eine Lage der Sonna nördlich in bozug auf die galaktusche Symmetricehene hinweist Er untersucht auch die Verteilung nach der galaktischen Länge. Für Gasnebel und noue Sterne findet er eine Konzentration gegen  $L = 335^{\circ}$  bzw 325°

Auf die Anhäufung schwacher Novae im Sagittarrusgebiet hat besonders K. Lundmark<sup>1</sup> animarksam gemacht. Es bestätigt sich hier, dom unmittelbaren Eindruck nach, die Vermutung, walche wir schon vorher mehrfach besprochen haben und welche wir später (Ziff, 28) auf Grund nouer Evidenz von ganz anderer Natur nochmals aufnehmen werden, daß die Partien der Milchstraße, welche die Sternbilder Sagittanus, Scorpius und Ophluchus berühren, im wesentlichen einem gewaltigen Zentralkern unseres Sternsystoms entsprechen. Ein Vergleich mit der Verteilung der Novae in der Zentralregion des großen Andromedansbels ist in vicler Hinsicht sohr bestechend Diese Tatsachen sind abor schon ansführlich an anderer Stelle in diesem Handbuch behandelt worden\* P Dorg\* hat die Verteilung in galaktischer Länge für verschiedene Objekte dargelegt: er zeigt besonders eine Verschiebung des Konzentrationspunktes vom Monoceros-Argo-Gebiet zum Centaurus-Sagittarius-Gebiet, wenn wir von dem B-Typus und den offenen Sternhaufen zu den O-Sternen, planetarischen Nebeln, langperiodischen Veränderlichen, Novae und Kugelsternhaufen übergehen

GYLLENBERG gibt die raumliche Verteilung der O-Sterne gemäß der Methode, wolche Charlier für die B-Sterne benutzt hat. Den Zentralpunkt für 97 Sterne findet or in der Entfernung 263 Parsec in der Richtung  $L = 328^{\circ}$ ,  $B = -4^{\circ}$ . Eine sehr eingehende Untersuchung fiber die scheinbare und räumliche Verteilung der c-Sterne hat SCHILT in einer obenerwähnten Arbeit gegeben. Wenn drei spezielle Gruppen ausgeschlossen werden, findet Schult eine Anordnung dieser Sterne im Raume, welche der von Charlier für die B-Sterne gefundenen Vorteilung ähnelt. Wie oben erwähnt, fällt aber die Symmetrieebene der c-Storne mit der allgemeinen "galaktischen" zusammen. P. Dorge untersucht die Verteilung der "Pseudo-Cepheiden" und Übergiganten der Spektraltypen F bis M. Das Material ist jedoch für stidliche Deklination sehr unvollständig C. Luttau-JANSSEN und G. HAARH® haben die räumliche Verteilung der N- und R-Storne studiert und auf die obenerwähnte große Verschiedenheit der Konzentration

gegen die galaktische Ebene für diese zwal Klassen hingewiesen

Eine sehr wichtige Aufgabe für die Kenntnis unseres Systems besteht im systematischen Aufsuchen von & Cephel-Veründerlichen, da die Relation zwischen Periode und absoluter Größe eine ziemlich genaue Ermittlung der räumlichen Vertellung erlaubt, wenn wir von Absorptionserscheinungen im interstellaren Raume abschen Hertzsprung untersucht die räumliche Verteilung der & Cephei-Sterne und der Sterne vom Typus Oe5. Shapley het in Verbindung mit seinen Untersuchungen über die Kugelhaufen (Zilf 18) die Vertellung der galaktischen d Cephel-Sterne ausführlich studiert. Eine sehr eingehende Untersuchung über die galaktische Verteilung der & Cophel-Sterne gibt M Güssows. Wohlbekennt

Publ A S P 33, S 219 u 225 (1921), Pop Astr Tidskr 4, S. 127 (1923).
 Da Handb VI, S. 257 (1928)
 J B A A 33, S 238 (1923)
 L. c.
 J B A A 36, S. 292 (1926).
 A N 214, S 383 (1921).
 Kritischo Zusammenstellung sämtlicher Beobschtungsorgebnisse der Veränderlichen. vom d Cephei-Typus und Kritik der Eddingromschen Pulsationstheorie, Inaug.-Diss. Borlin 1924

ist der auffällige Unterschied in galaktischer Konzentration zwischen den langperiodischen und kurzperiodischen Sternen dieser Art¹. Die Häufigkeit der langperiodischen  $\delta$  Cephei-Sterne zeigt nach M. Güssow Maxima in den Längen 250° bis 260° und 330° bis 360°. J. Schltt³ hat die Häufigkeit der Perioden für verschiedene Milchstraßengegenden untersucht. In der Sagittarius-Aquila-Region zeigt die Häufigkeit ein Maximum für  $\log P = 0.84$ , während für andere Regionen das Maximum für entschieden kürzere Perioden eintritt.

Eine der großartigsten Arbeiten für die Erforschung der Milchstraßenstruktur wird gegenwärtig auf der Harvard-Sternwarte und ihrer südlichen Filiale ausgeführt, wo in mehr als 200 Feldern, welche die ganze Zentralzone der Milchstraße bis ±20° Breite bedecken, durch wiederholte Aufnahmen alle Veränderlichen systematisch aufgesucht und in ihrem Lichtwechsel ver-

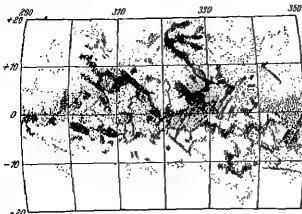


Abb. 16. Vordunklungsgebiete in der Zentralgegend der Milchstraße,

folgt werden<sup>3</sup>. Die ersten Früchte dieses Planes sind schon erschienen in mehreren Aufsätzen von H. SHAPLEY und H. W. SWOPE unter dem Titel "Studies of the Galactic Center4". Besondere Aufmerksamkeit wird nämlich darauf verwandt, die Lage, Entfernung und Dichte des galaktischen Zentrums, welches, wie oben erwähnt, mit großer Wahrscheinlichkeit in der Sagittariusregion der Milchstraße gelegen ist, zu untersuchen, Es werden kurz- und lang-

periodische & Cephel-Sterne, langperiodische Veränderliche, Novae und Bedeckungs-Veränderliche studiert.

In einem Feld von 70 Quadratgrad um das vermutete Zentrum herum wurden unter 450 Veränderlichen 78 kurzperiodische 8 Cephei-Sterne oder "Sternhaufenveränderliche" gefunden. Die scheinbaren Helligkeiten dieser Sterne sind größtenteils zwischen 15<sup>m</sup>,4 und 16<sup>m</sup>,2 verteilt, mit einem Maximum bei 15<sup>m</sup>,7. Shapley schließt, daß diese Sterne zu einer Art von System gehören, dessen mittlere Entfernung er zu 14400 Parsec schätzt. Da dieser Wert gut mit der früher von Shapley gefundenen Entfernung zum Zentrum im System der Kugelhaufen übereinstimmt, so ist es sehr wahrscheinlich, daß dieses System mit dem Kern unseres Milchstraßensystems identifiziert werden kann.

Auch die Verteilung der langperiodischen & Cephei-Veränderlichen nach scheinbarer Größe, die ein sehr starkes Maximum bei 14<sup>m</sup>,8 aufweist, spricht für die Existenz eines scharf ausgeprägten Kerns im galaktischen System.

Die erwähnten Studien von Shapley und seinen Mitarbeitern umfassen auch eine wichtige Untersuchung der Verdunklungsgebiete in der betreffenden

<sup>1</sup> Vgl. Ludendorff, Handb. der Astrophys. VI, Kap. 2, Ziff. 63.

Mt Wilson Contr 315 = Ap J 64, S. 149 (1926).
 Siche besonders "Sidereal Explorations". The Rice Institute Pamphlet 18, Nr. 2

<sup>Harv Repr 68 (1931).
Wash Nat Ac Proc 14, S. 825, 830 u. 958 (1928), 15, S. 174 (1929)
Harv Repr 51, 52, 53, 58.</sup> 

Himmelsgegend und Erwägungen über die Durchsichtigkeitsverhältnisse des interstellaren Raumes Seapley hat die auf den Photographien erkennbaren Verdunklungsgeblete der Zentralgegend in einer Zeichnung durch Schrafflerung von verschiedener Stärke zu markieren versucht (Abb. 16) Das Gebiet am Himmel entspricht dem des zusammengesetzten Bildes in Abb. 7. Er hat dann auch die Verteilung der extragalaktischen Nebel in demselben Gebiet untersucht, um daraus weitere Schlüsse über die Durchsichtigkeitsverhältnisse dieser Gegend ziehen zu können (Abb 17).

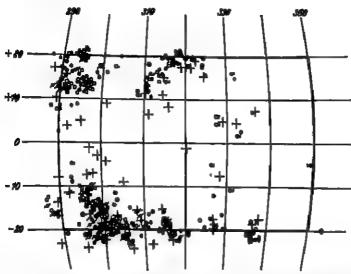


Abb 17. Die Verteilung der extragalaktischen Nebel in der Zontralgegend. In der Abbildung repräsentieren große Punkte NGC-Objekte, kleine Punkte IC-Objekte oder Nebel in publisierten Harvard-Katalogen, die kleinen Kroise neue auf dem Harvard-Observatorium entdeckte Nebel. Die durch eine Linie gekronsten Punkte sind deutlich spiralförmige Objekte. Die Krouse geben die Zentra der langexponierten Platten au.

Sharley zieht den Schluß, daß, wenngleich leicht festxustellendes absorbierendes Material einige galaktische Wolken in der Zentralregion und auch das Zentrum selbst verbirgt, die Milchstruße an den Grenzen dieser Dunkelnebel vollkommen durchsichtig ist und demnach die Beobachtung der entferntesten Sterne unseres Systems wie auch der außeren, wahrscheinlich Millionen Lichtfahre von uns entfernten "Milchstrußen" zuläßt

P. TEN BRUGGENCATE<sup>1</sup> hat in Verbindung mit einer Untersuchung über die räumliche Verteilung von neuentdeckten & Cephei-Variabela mit Perioden von mehr als einem Tage einige Bomerkungen über Shapleys größeres galaktisches System gemacht. Die Veränderlichen der betreffenden Klasse kommen im Raume unter die offenen Sternhaufen gemischt vor. Es sollen alle offenen Sternhaufen und mehrere Kugelhaufen in den Sternweiken der Milchstraße selbet liegen

Die Eigenschaften der Sternhaufen werden an anderem Orte in diesem Handbuch ausführlich behandelt. Hier sollen nur der Vollständigkeit wegen einige fundamentale Tatsachen betroffs der Verteilung der Haufen im Raume Erwähnung finden.

Die offenen Sternhaufen sind Objekte von außerordentlich starker galaktischer Konzentration. Versuche, ihre Verteilung im Raume zu bestimmen.

<sup>1</sup> BAN 4, S 195 (1928).

sind von C. V. L. Charlier<sup>1</sup>, H. Shapley<sup>2</sup>, S. Raab<sup>3</sup>, P. Collinder<sup>4</sup> und R. Trümpler<sup>5</sup> gemacht worden. Die Verteilung der zur Zeit bekannten Haufen, wie sie besonders in den zwei letztgenannten Arbeiten zutage tritt, kann folgendermaßen kurz charakterisiert werden. Die Symmetricebene des Systems erscheint ein wenig schief gegenüber der gewöhnlich angenommenen galaktischen Ebene. Trümpler findet für den Pol des Haufensystems

$$A = 192^{\circ}, 6, D = +27^{\circ}, 7 (1900).$$

Wenn wir vom Gouldschen Pol ausgehen und die entsprechenden galaktischen Koordinaten des Haufenpols suchen, bekommen wir nach TRÜMPLER

$$L = 10^{\circ}, B = +88^{\circ}, 3.$$

Es ist sehr bemerkenswert, daß diese Lage des Pols in derselben Richtung von Goulds Pol abweicht wie die Lage des Pols für die schwachen Größenklassen in Tabelle 6 (Ziff. 11) gemäß den Untersuchungen von Seares und van Rhijn. Die Abweichung ist jedoch für die Haufen von einem kleineren Betrag, was nach TRUMPLER andeutet, daß das System der Haufen weiter in den Raum hinausreicht als im Durchschnitt die Sterne 18. Größe. Das System der bekannten Haufen bildet eine sehr flache, nahe kreisförmige Scheibe von etwa 8000 Parsec Durchmesser und mit einem beträchtlichen Zuwachs an Dichtigkeit gegen das Zentrum hin. Dieses Zentrum befindet sich ziemlich nahe der Sonne. Wenn wir die zwei galaktischen Koordinatenachsen so zichen, daß gleich viele Haufen auf beiden Seiten jeder Achse liegen, so bekommen wir nach Trümpler den Schnittpunkt in der Entfernung 350 Parsec in der galaktischen Länge 247°. Dies deutet an, daß die dichte Zentralregion des Haufensystems dem Phänomen des "lokalen Systems" entspricht. Diese Zentralregion geht aber allmählich in die allgemeinen Milchstraßenregionen über, und wir haben oben gesehen, daß die Symmetrieebene der Haufen im ganzen gar nicht im Sinne des Gouldschen Kreises oder der Symmetrieebene der helleren B-Sterne von der allgemeinen Milchstraßenebene abweicht, sondern in ihrer Lage mit der Tendenz der Sterne von sehr schwachen Größenklassen übereinstimmt,

Wenn wir zu den Kugelhaufen übergehen, so spricht für ihre Zugehörigkeit zum Milchstraßensystem, außer ihrer nahezu symmetrischen Anordnung in bezug auf die galaktische Ebene und ihrer größten Häufigkeit in der Gegend der hellsten Milchstraßenwolken, unter anderem der Umstand, daß es auch Objekte großer individueller Leuchtkraft gibt, die in ihrer Verteilung gewissermaßen eine Zwischenstellung zwischen den Kugelhaufen und den Klassen von großer galaktischer Konzentration einnehmen. Eine solche Klasse bilden die planetarischen Nebel, deren Verteilung von A. R. Hinks<sup>6</sup>, C. V. L. Charlier<sup>7</sup> und H. D. Curtis<sup>8</sup> diskutiert worden ist. Diese Nebel kommen mit ziemlich großer Häufigkeit in der Sagittariusregion vor (besonders die Nebel von kleinem scheinbaren Durchmesser), zeigen aber sonst keine sehr ausgeprägte galaktische Konzentration.

Eine auffallend kleine galaktische Konzentration zeigen auch trotz hoher absoluter Leuchtkraft die R-Sterne und die helleren kurzperiodischen δ Cephei-Veränderlichen. Für ein Studium über die Verteilung dieser Sterne nach galaktischer Länge liegt aber kaum genügend homogenes Material in den verschiedenen Himmelsgegenden vor. Shapley<sup>0</sup> hat die räumliche Verteilung der letztgenannten

Lund Medd Ser II, Nr. 19 (1918).
 Lund Medd Ser. II, Nr. 28 (1922).
 Mt Wilson Comm 62 (1919).

Pop Astr Tidskr 8, S. 36 (1927); On Structural Properties of Open Galactic Clusters and their Spatial Distribution, Inaug.-Diss. Lund 1931.
 Lick Bull 14, S. 154 (1930).
 M N 71, S. 693 (1911).

Lick Bull 14, S. 154 (1930).
 Lund Medd Ser II, Nr. 19, Plate IV.
 Publ Lick Obs 13, S. 60 (1918).
 Mt Wilson Contr 153 = Ap J 48, S. 279 (1918).

Sterne aus Entfernungsbestimmungen auf Grund der Relation zwischen Poriode und absoluter Größe studiert. Die kleine galaktische Konzentration wird von Shapley als eine Folge der großen Streuung der räumlichen Geschwindigkeiten gedeutet. Wenn wir das obenerwähnte Vorkommen in der "zentralen" Milchstraßengegend im Sagittarius mitrechnen, so scheint in vieler Hinsicht eine ausgeprägte Analogie zwischen der Verteilung dieser Sterne im Raume und der Verteilung der Kugelhaufen zu bestehen

Inwiewelt die hergeleitete Vertellung einer Klasse von Objekten großer absoluter Louchtkraft das wahre Vertellungsgesotz der betreffenden Objekto ım Sternsystom wiedergibt, hängt natürlich in erster Linie von der Vollständigkeit ab, mit welcher diese Objekte in unserem statistischen Material vorkommen. Eine der größten Schwiczigkeiten der direkten stellarstatistischen Untersuchungsmethode liegt ohne Zwelfel in der Absorption des Lichts in ausgedehnten Anhaufungen von Materio im interstellaren Raume Eine solche Absorption beeinträchtigt nicht nur die Vollständigkeit des Materials, sondern verfälscht auch, wenn unberücksichtigt, die nach photometrischer Methode ermittelten Entfernungen und damit die aus diesen berechnete räumliche Dichtigkeit. Es wird durch beide Ursachen eine falsche "anthropozontrische" Verteilung vorgetäuscht. Mit großer Wahrscheinlichkeit sehen wir z. B einen Absorptionseffekt in dem scheinbaron Vermeiden einer zontralen Milchstraßenzone, welches die Kugelhaufen zeigen Trümpler rechnet in seiner obenerwähnten Arbeit mit einen aligameinen Extinktion von 0m,67 (photographisch) per 1000 Parsec innerhalb einer dünnen Schicht um die galaktische Zentralebens herum. Inwieweit diese und andere mehr unregelmäßige Absorptionserscheinungen auf die von Tudmflir gehindens Verteilung der offenen Haufen in "anthropozentrischer" Richtung cinwirken, bleibt wohl noch unaufgeklärt (vgl Ziff. 24 und 35).

21. Die Entfernung der Sonne von der Symmetrieebene der Milchstraße. In Ziff 14 haben wir für den sphärischen Radius der zentralen Milchstraßenlinie im Mittel einen gewissen Überschuß fiber 90° gefunden, was als "dip" der Milchstraße bezeichnet wird Eine genauere Abschätzung der entsprechenden Entfernung der Sonne von der Symmetrieebene gegen den nördlichen galaktischen Pol hin kann durch eine Statistik gewisser Klassen von Objekten ermittelt werden

CHARLIER findet in seiner ersten Arbeit über die helleren B-Sterne eine Stellung der Sonne nördlich von der Symmetrieebene um 20 Parsec (4 Striometer) und in seiner späteren Arbeit für die B-Sterne heller als 8<sup>m</sup>,0 eine Entfernung von 15,5 Parsec, was sehr nahe mit einer Schätzung von SHAPLEY und CANNON¹ für die Storne vom Typus B0 bis B5 im Größenintervall 7<sup>m</sup>,26 bis 8<sup>m</sup>,25 übereinstimmt.

GREASIMOVIČ findet für B-Sterne heller als 6<sup>m</sup>,7 eine Distanz von 16 Parsec und für Sterne schwächer als 6<sup>m</sup>,7 den Wert 34 Parsec. Derselbe Verfasser<sup>3</sup> hat aus den O-Sternen eine Sonnenerhöhung über die Milchstraßenebane von 31 Parsec hergeleitet

SCHILT findet in seiner in Ziff. 20 besprochenen Arbeit für die e-Sterne mit der scheinbaren Größe ziemlich varlierende Werte, die jedoch im Mittel gut mit den Resultaten für andere Klassen übereinstimmen.

Aus den & Cephel-Sternen fand HERTESPRUNG<sup>3</sup> 40 Parsec und Shapley<sup>4</sup> 60 Parsec, während kürzlich Gerasimovic und Luyten<sup>5</sup> aus verbessertem Material 34 ± 11 Parsec gefunden haben, was mit den Resultaten für Miss

Harv Circ 239 (1922)
 A N 226, S. 327 (1926).
 A N 196, S. 207 (1913).
 Mt Wilson Contr. 157 — Ap J 49, S 311 (1919)

Wash Nat Ac Proc 13, 5, 387 (1927).

Maurys c- und ac-Sterne und für die Spektralklassen O und B in bester Übereinstimmung steht. Das letztgenannte Resultat ist daher ohne Zweifel das zur Zeit zuverlässigste. Nach Trümpler liegt die Sonne 10 Parsec nördlich von der

Zentralebene der offenen Sternhaufen.

22. Spezielle Untersuchungen der Sternleeren und Sternwolken der Milchstraße. Der unmittelbare Anblick zeigt uns die Milchstraße in eine Art von Wolkenstruktur aufgelöst, die zweifellos zum großen Teil eine scheinbare, durch Absorption des Lichts in dunklen Massen hervorgerufene Zerstückelung bedeutet (vgl. Ziff. 13). Wenn wir sogar die Vermutung hegen können, daß die meisten auffälligen Risse des Milchstraßengebildes Absorptionsgebiete darstellen, so bedarf diese Behauptung doch eines direkten Nachweises, den uns in erster Linie eine statistische Analyse der Sternzahlen sukzessiver Größenklassen, soweit möglich unter Hinzufügung spektralanalytischer Daten, zu geben hat. Die Anzahl Sterne verschiedener Helligkeiten in den Dunkelgebieten wird mit den Sternzahlen benachbarter "normaler" Gebiete verglichen. Es wird dann untersucht, ob die Abweichungen durch die Einwirkung einer Absorptionsschicht in einer gewissen anzugebenden Entfernung und mit einem gewissen Absorptionsvermögen erklärt werden können.

Es ist von vornherein klar, daß eine vollständigere Analyse, die auch die Sternbewegungen berücksichtigt, für eine Beurteilung diesbezüglicher Fragen von großer Bedeutung sein würde, da ja aus den Eigenbewegungen der Sterne des Dunkelgebiets die mittleren Entfernungen hergeleitet werden können. Unsere Kenntnis der Bewegungen ist jedoch noch viel zu mangelhaft, um im allgemeinen

eine solche Analyse erfolgreich zu machen.

Schon aus einer direkten Analyse der Kurven, welche die Sternzählungen. nach scheinbarer Größe wiedergeben, können wichtige Eigenschaften des Nebols, wie Entfernung und Absorptionsgrad, wenigstens grob geschätzt werden. Für genügend schwache Größen sollten die Kurven für das freie und das verdunkelto Feld einander parallel laufen, mit einer Differenz in m gleich der Absorption & der verdunkelnden Nebelschicht für hinter dieser Schicht liegende Sterne,

Eine mathematisch-statistische Methode zur Abschätzung der Entfernung und der Absorption ist von A. PANNEKOEK<sup>2</sup> entwickelt worden. Für die Sternzahlen pro Größenklasse im freien und im verdunkelten Gebiet, a(m) und  $a_1(m)$ , setzen wir  $a_1(m) = \gamma_1 a(m) + \gamma_2 a(m-\epsilon)$ . Wenn wir für die Dichtigkeitsfunktion die Seeligersche oder die Schwarzschildsche Approximation annehmen, so werden  $\gamma_1$  und  $\gamma_2$  durch die Konstanten dieser Funktionen und durch die Entfernung r der Nebelschicht bestimmt. Durch Variation der zwei Parameter & und r wird die bestmögliche Darstellung der beobachteten Zahlen  $a_1(m)$  angestrebt. W. Gyllenberg<sup>3</sup> hat eine ähnliche Methode entwickelt, welche aber die Unbekannten in mehr direkter Weise ergibt. Die Entfernung des Nebels kann auf drei Wegen ermittelt werden, durch die mittlere scheinbare Größe, durch die Größe maximaler Frequenz oder durch die Totalsumme der Sterne des Vordergrundes. Lundmark4 hat verschiedene Methoden zur Entfernungsbestimmung für helle und dunkle Nebel skizziert.

Wie vorher auseinandergesetzt wurde, scheint in unserer Nähe eine Nebelschicht von beträchtlicher Neigung (etwa 20°) gegen die Milchstraße zu existieren, deren ausgedehnteste Absorptionsgebiete in Taurus-Orion und in Ophiuchus zu finden sind.

Das große Dunkelgebiet in Taurus zwischen R.A. 3h bis 5h 30m und nördl. Dekl. 20° bis 25° ist in einer detaillierten Abzählung auf den Franklin-Adams-

<sup>1</sup> L. c. Ziff, 20.

Amsterdam Proc 23, Nr. 5 (1920).
 (1929).
 Publ A S P 34, S, 40 (1922). Lund Medd Ser II, Nr. 52 (1929).

Platten von F W Dyson und P J Melotte<sup>1</sup> behandelt worden Die Abzählung zeigt drei Regionen starker Verdunklung im genannten Gebiet, um  $3^h$   $20^m$ ,  $+30^\circ$  herum (S W von  $\zeta$  Persei und nahe o Persei), um  $4^h$   $30^m$ ,  $+26^\circ$  herum (zwischen den Plejaden und  $\beta$  Tauri) und um  $5^h$   $20^m$ ,  $+25^\circ$  herum (S.W. von  $\beta$  Tauri) Dieses Gebiet war früher von Barnard bemerkt worden, der auf die Existenz absorbierender Materio geschlossen hatte, was durch die Anwesenheit von hollen Nobeln um so mehr wahrscheinlich wird (Ziff 13) Es wird auf der Wolfschen Aufnahme (Abb 4) wiedergegeben Dyson und Melotte schließen, daß die Entfernung der dunklen Materio nicht 300 Parsec fiberschreiten kann

Panneroek findet aus den Zählungen im Taurusgebiet ome Entfernung des dunklen Nebels von 440 Parsec und einen Absorptionsgrad in den dunkleren Partien von etwa zwei Grüßenklassen Eine Bestätigung dieses Resultats ist kürzlich von C Schalzen geliefert worden, der speziell die B- und A-Storne in der betreffenden Region untersucht und diese in "Lummositätsklassen" von wahrscheinlich sehr geringer Streuung in absoluter Größe aufgeteilt hat. Die Methode von Pannekork wurde für jede einzelne Klasse befolgt Schalen findet als Mittel aus vier Luminositätsklassen, die mitemander wohl übereinstimmende Resultate geben,

$$r = 126$$
 Parsec,  $s = 1^m, 8$ 

Aus den Zahlen der A- und K-Sterne des Draper-Katalogs hatte Shapley' als Maximalwert der Distanz 250 Parsec angegeben. Wenn die gefundene Absorption durch Rayleigh-Diffusion in Wasserstoff erklärt werden soll, wird die Masse des Taurusnebels nach Pannekoek von der Größenordnung 4 · 10° Sonnenmassen. Eine solche Masse in einer Entfernung von nur 126 Parsec führt indessen auf bedenkliche dynamische Konsoquenzen der Sternströmung gegonüber, weshalb es nach Pannekoek wahrscheinlicher ist, daß wir es mit einer Diffusion durch freie Elektronen oder mit einer Absorption durch kosmischen Staub zu tun haben, in welchem Falle sehr viel kleinere Massen zur Erklärung genügen. Dann haben wir auch keine mit der Wellenlänge sich verändernde Absorption zu erwarten, was mit der bisherigen Erfahrung über die Absorption in den ausgedehnten dunklen Nebeln übereinzustimmen scheint. Dagegen ist für Sterne, die mit heller Nebulosität verbunden sind, oftmals ein großer Farbenexzeß beobachtet worden.

A. EDDINGTON<sup>6</sup> weist nach, daß die Annahme einer Diffusion durch freie Elektronen für den Taurusnebel eine wahrscheinlich noch zu hohe Masse gibt (12·10<sup>7</sup> Sonnenmassen). Es scheint daher, daß nur die Hypothese einer "soliden Obstruktion" durch kleine Partikaln stichhaltig ist.

Die Extinktion einer solchen Wolke ist bei gegebener Masse und Dichte ein Maximum, wann der Durchmesser einer Partikel gleich der Wellenlänge des Lichtes wird. Für diese Partikelgröße geht auch der Übergang von nichtselektiver zu selektiver Extinktion vor sich Nach H. N. Russell? ist es also wahrscheinlich, daß die Extinktion des Lichts im Raume hauptsächlich von festen Partikeln von einigen zehntausendsteln Millimater ausgeübt wird

Für die Umgebung des Orionnebels hat A Korrre eine umfangreiche Sternzählung auf einer Aufnahme mit dem 16zölligen Bruce-Teleskop der Sternwarts

M N 80, S. 3 (1919)
 Ap J 25, S. 218 (1907).
 K Svenska Votensk Handi (III) 6, Nr 6 (1928) — Upsala Medd 37

Harv Circ 240 (1922).
F. H. Seares u. E. Hunele, Mt Wilson Contr 187 - Ap J 52, S. 8 (1920).

The Internal Constitution of the Stars, S. 388 (1926)
Wash Nat Ac Proc 8, S. 115 (1922) — Mt Wilson Comm 77
Publ Astrophys Obs Königmtuhl-Heldelberg 1, S. 177 (1902).

Königstuhl, Belichtungsdauer 6h 15m, durchgeführt. Die scheinbare Sterndichtigkeit ist in einer bildlichen Darstellung durch Schraffierung verschiedener Stärke wiedergegeben worden. Es zeigt sich, daß der Nebel von einer sternarmen Region umgeben ist. Diese verbreitert sich auffallend in südöstlicher Richtung, so daß der Nebel fast an der Spitze eines langgestreckten sehr dunklen Kanals gelegen ist. Ein feiner dunkler Arm geht jedoch auch in nordwestlicher Richtung vom Nebel aus; in nordöstlicher Richtung steht die leere Region mit den Nebelmassen um  $\zeta$  Orionis in Verbindung. S. Asklöp hat eine Abzählung derselben Gegend für sukzessive Größenklassen bis zur Größe 13,0 unternommen. Für die Entfernung des dunklen Nebels erhält er im Mittel 290 Parsec, was mit den Entfernungsbestimmungen für die Heliumsterne im Orion und für Doppelsterne dieser Gegend, die wahrscheinlich mit den Heliumsternen und dem hellen Nebel verbunden sind, wohl übereinstimmt.

PANNEROEK<sup>2</sup> hat für eine Partie der Milchstraße in Aquila Sternzählungen ausgeführt, aus welchen er schließt, daß das hier auftretende Dunkelgebiet durch

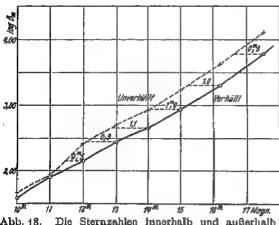


Abb. 18. Die Sternzahlen innerhalb und außerhalb des Nebels NGC 6960 nach Wolf.

eine absorbierende Nebelmasse verursacht wird, die schon für Sterne der Größen 10 und 11 sehr bemerkbar wird,

Für den großen dunklen Ophiuchusnebel gibt PanneKOEK in seiner vorher erwähnten Arbeit tiber das "lokale
Sternsystem" eine Entfernung
zwischen 100 und 200 Parsec,
also von derselben Größenordnung wie die Entfernung
des Taurusnebels. Shapley³
schätzt für die dunklen Nebel
der Ophiuchus-Scorpius-Region die Entfernung zu 200
bis 300 Parsec.

Eine Menge Sternzählungen für Absorptionsgebiete sind in den letzten Jahren von M. Wolf gemacht worden. Die erste unten aufgeführte Arbeit bezieht sich auf den Nebel NGC 6960, der sich in langem Bande fast genau durch den Stern 52 Cygni (R.A. 20h 41m, Dekl. +30° 21') hindurchzieht. Der helle Nobel ist offenbar der westliche Teil einer sehr ausgedelnten Nebelmasse, die bis zu dem ebenfalls langgestreckten Netzwerknebel NGC 6992 hinüberreicht. Wir haben schon vorher (Ziff. 1 u. 13) den großen Unterschied in den Sternzahlen auf beiden Seiten des Nebels NGC 6960 besprochen. Diese Erscheinung hat Wolf durch Sternzählungen bis zur Größe 17,5 verfolgt. Das Resultat ist in Abb. 18 wiedergegeben.

Aus der Verschiebung der Sternzahlenkurve für die Absorptionsregion kann man die Extinktion des dunklen Nebels östlich von der hellen Randpartie zu einer Größenklasse schätzen. Die Entfernung schätzt Wolf zu rund 450 Parsec. Er findet keine Spur von einem Farbenexzeß im verdunkelten Teil.

Nordisk Astr Tidsskr 5, Nr. 1 (1924); Ark Mat Astr Fys 22 A, Nr. 14 (1930) = Upsala Medd 51.
 Versl Akad Amsterdam 27, S. 1327 (1919); Amsterdam Proc 21, Nr. 10 (1919).
 Harv Circ 239 (1922).

<sup>&</sup>lt;sup>4</sup> A N 219, S. 109 (1923); 223, S. 89 (1924); 229, S. 1 (1926); Seeliger-Festschr S. 312 (1924); V J S 61, S. 263 (1926).

Ähnliche Untersuchungen von Wolf beziehen sich auf den "Amerikanebel", auf die Sternleeren bei 5 Monocerotis und auf die Sternleere neben der dichtesten Gegend der Scutumwolke Bei dem Amerikanebel und der Scutumleere beträgt die Absorption 3,5 Grüßenklassen

Schr interessant ist Wolfe Vergleichung der Sternzahlen für die vier eben genannten Regionen der Milchstraße mit den Sternzahlen am galaktischen Pol. Die letztere Gegend erscheint sternärmer als die Leeren des Milchstraßengürtels. Wichtig ist auch, daß der Gang der Sternzahlen für den galaktischen Pol von der Größe 9 bis zur Größe 16,5 wenigstens keine stärkere Absorptionswirkung durch irgendeine Dunkelwolke andeutet.

Pür den Amerikanebel liegen außer Wolfs obenerwähnter Arbeit mehrere Untersuchungen vor. So hat A Kofff¹ eine umfangreiche Sternzählung in derselben Weise wie für den großen Orionnebel ausgeführt E. Buch-Andersen¹ findet aus Sternzählungen die Entfernung des Nebels gleich der mittleren Entfernung der Sterne der Größe 8,5 in der betreffenden Region. B. Okunkv³ untersucht die Spektra von 743 Sternen zwischen R.A 20¹ 4™ und 24¹ 13™ und Dekl +40° his +47° und findet in ziemlich guter Übereinstimmung die der Entfernung des Nebels entsprechende Sterngröße zu 9,0

W. GYLLENBERG findet für die Parallaxo dieses Nebels nach seiner oben besprochenen Methode, aber in zwol etwas verschiedenen Durchführungen  $\pi=0'',0064$  bzw. 0'',0074. Für den Nebel um S Monocerotis findet er  $\pi=0'',013$ . K Lundmark hat in seiner oben besprochenen Arbeit für diese und andere Nebel nach verschiedenen Methoden genäherte Parallaxen gegeben.

O, STRUVE<sup>4</sup> hat in Verbindung mit seiner Arbeit über das interstellare Kalzum (Ziff 25) einen Dunkelnebel im Copheus behandelt und aus Sternzählungen eine Entfernung von 350 Parsec erhalten.

A UNSÖLD<sup>5</sup> hat nach Wolfs Mothodo den südlichen "Kohlensack" in Crux untersucht. Er findet eine Entfernung von ungefähr 450 Parsec und eine Extinktion von einer Größenklasse. Zu der UNSÖLDschen Arbeit hat E. VON DER PAHLEN<sup>6</sup> einige bestätigende theoretisch-statistische Bemerkungen hinzugefügt

In seiner oben besprochenen Arbeit hat Schalen für einige dunkle Gebiete der nördlichen Milchstraße durch eine sorgfältige Analyse der Sternzahlen der B- und A-Sterne unter Einteilung derseiben in spezielle Sonderklassen, die wesentlich von der Intonsität der Wasserstofflinien im Spektrum abhängen, die Entfernung und den Absorptionsgrad der Dunkelwolken bestimmt. Die Ergebnisse sind nach Schalen in Tabelle 13 aufgeführt. Die Existenz des Nebels in der Cassiopsiagegend ist nach ihm unsicher. In einer späteren Arbeit! hat er in der Cephousregion unter Heranziehung von Daten für andere Spektralklassen. Andeutungen von zwei Nebeln in den Entfernungen 250 und 410 Parsec und mit der Absorption 0,3 bzw. 0,6 Größenklassen gefunden.

Tabelle 43

Racion	Ko	ord.	Rationary	Extinities	
Profession .	Ċ	ð	in Paress	Terrental	
Cygnus	20 <sup>b</sup> 25 <sup>m</sup>	+35°	800	2**	
Cophous , , ,	21 50	+35° +58	370	0,9	
Copheus	21 45	+57	800	1,5	
Camiopola	1 50 1 30	+63) +56)	900	1	
Anriga-Teurus	4 45	+36	126	1,8	

<sup>1</sup> L<sub>1</sub> c. <sup>2</sup> Ap J 38, 8. 275 (1913)

Bulletin de l'observatoire central de Russie à Poulkovo 10, S 594 (1927).

Mt Wilson Contr 331 — Ap J 65, S. 193 (1927)
 Harv Bull 870 (1929)
 A N 238, S. 269 (1930)
 Ark Mat Astr Fye 22 A, Nr. 16 (1930) — Upsala Medd 50.

Wir haben oben vielfach die Sternleeren der Milchstraße als im großen ganzen durch absorbierende Dunkelwolken hervorgerufen angeschen. Diese Auffassung war jedoch nicht immer die geläufige. Barnard und Wolf waren beide zuerst geneigt, in den dunklen kontrastierenden Gebieten wirkliche Sternleeren zu sehen; Wolf wollte z. B. früher in den Höhlennebeln eine Art Wegfegung von Sternen durch den hellen Nebel sehen, wodurch die sternleeren Kanäle entstehen sollten. Beide wurden aber später zu entschiedenen Vertretern der Absorptionshypothese bekehrt. In den meisten Fällen ist auch sicher diese Hypothese vorzuziehen, wenn auch hervorgehoben werden muß, daß nicht alle gegen ihre Umgebungen kontrastierenden dunklen Gebiete des Himmels notwendig als durch Absorption des Lichtes entstanden zu betrachten sind, wenigstens nicht in höheren galaktischen Breiten (vgl. Ziff. 14).

Trotz dieses Ergebnisses besteht noch immer die Vorstellung, daß das System der Milchstraße räumlich in eine Menge gegeneinander isolierter Wolken aufzulösen sei. Inwieweit dieser Vorstellung etwas Reales zukommt, läßt sich zwar noch kaum völlig entscheiden, doch muß nach dem Durchbruch der Absorptionshypothese für die Deutung der Dunkelgebiete der Milchstraße die ältere Auffassung betreffs der hellen Regionen jedenfalls sehr erheblich modifiziert werden.

Die Vorstellung einer Wolkenstruktur der Milchstraße wurde aber auch zum Teil aus einer Statistik der Sternzahlen hellerer Sterne abgeleitet. W. Stratonoff¹ fand für die Argelanderschen Sterne gewisse Kondensationsregionen, von denen die wichtigsten in Cygnus, Auriga, Monoceros und Argo gelegen sind. Stratonoff hält die Sonne für ein Glied eines Haufens, dessen Mitte wir ein wenig südlich von α Cygni wahrnehmen. F. Ristenpart³ suchte die räumliche Dichtigkeit für verschiedene Regionen zu ermitteln und kam zu dem Ergebnis, daß die Sonne sich in einem Sternhaufen befindet, dessen Zentrum etwa in der galaktischen Länge 290° im Sternbilde Norma liegt. Eine zweite deutlich hervortretende Wolke ist die in Cygnus. Wie vorher erwähnt, hat auch Pannekoek kürzlich unsere nähere Umgebung in eine Serie von Wolken aufzulösen versucht, von denen die mächtigsten in Cygnus und Monoceros liegen.

Diese Ergebnisse scheinen jedoch in einem gewissen Gegensatz zu anderen vielleicht augenblicklich allgemeiner angenommenen Ansichten zu stehen, nach denen die heileren Sterne unserer Umgebung überwiegend einem großen "lokalen System" angehören, dessen Kern von dem "lokalen Haufen" der Heliumsterne gebildet wird. Dieses "lokale System" wäre aber auch als eine einheitliche Sternwolke neben anderen zu betrachten. Diese Auffassung wird vor allem durch die nach allen Seiten abnehmende Sterndichtigkeit, wie sie aus den Sternzahlen ohne Berticksichtigung einer allgemeinen Absorption ermittelt wird, gestützt. Über die Natur und Mächtigkeit dieses hypothetischen "lokalen Systems" bestehen jedoch sehr auseinandergehende Meinungen (vgl. Ziff. 18, 19, 33). Nach einer neueren Auffassung auf Grund der differentiellen Rotationseffekte (Ziff. 30) besteht wenigstens kein beständiges, in dynamischer Hinsicht gegen andere "Wolken" abgeschlossenes lokales System.

Nicht weniger gehen die Ansichten über die Entfernungen und Eigenschaften der äußeren galaktischen Wolken auseinander. Nach einer Arbeit von PanneKoek (Ziff. 16) sollte keine Verbindung zwischen den Sternen von den Größen 9 bis 11 und den wirklichen Milchstraßenwolken bestehen. Später berechnete er<sup>3</sup> aus Sternzählungen für die Cygnuswolke und die Aquilawolke Entfernungen von 40000 bis 60000 Parsec. Für die Sternzahlen wurden die der BD, die Eichungen von Herschel und Epstein und außerdem einige Zonen der photographischen

Publ Obs Taschkent Nr. 2 u. 3 (1900, 1901).

<sup>&</sup>lt;sup>2</sup> V J S 37, S. 375 (1902). <sup>8</sup> M N 79, S. 500 (1919).

Himmelskarte benutzt Der Gradient dlog N/dm zeigte ein Minimum und ein Maximum, wenn wir gegen schwache Größen fortschreiten, was PANNEKOEK als einen typischen Wolkeneffekt deutete Unter Zugrundelegung der KAPTEYNschen Luminositätskurve und mit Vernachlässigung der räumlichen Tiefe der Walke berechnete er für verschiedene Wolkenontfornungen theoretische Sternzuhlen, wobei für die Storne des Vordergrundes die Zahlen für den galaktischen Pol angenommen wurden Eine Konstante, die von der räumlichen Sterndichtigkeit der Wolke abhängt, wurde in Übereinstimmung mit der grob geschätzten Flächenhelligkeit der Wolke angenommen Der schwache Punkt dieser Entfernungsbestimmung lag in der relativen Unzuverlässigkeit und in der Inhomogenität der Quellen für die Sternzahlen. Gegen Pannekoeks Resultate hat Easton ornsto Einwände auf Grund einer neuen Ermittlung der Korrelation zwischen Sternzahlen und Milchstraßenhelligkeit erhoben. Er leitet auch die Prozentzahl der B- und A-Sterne her und berechnet die mittleren Eigenbewegungen für dunkle und helle Regionen, wobei sich zeigt, daß die Eigenbewegungen im Mittel etwas größer für die dunkleren als für die helleren EASTON schließt aus den Rosultaten auf die Zugehörigkeit eines Teils der helleren Sterne zu den Wolken Man muß jedoch hierzu die Bemerkung machen, daß Eastons Resultate wohl oher durch die kleinen Entfernungen der Dunkelwolken, welche die hellen Milchstraßenpartien trennen, als durch kleine Entfernungen der etwalgen Sternwolken erklärt werden können (vgl, Ziff, 16)

In cinem spateron Aufsatz über das Cygnusgeblet findet PANNEROBES, daß wir hler in der Nähe von y Cygni zuerst eine Anhäufung von Sternen in einer Entfernung von nur 200 bis 600 Parsec vor uns haben, ein Haufen, der aber nichts mit der wirklichen Cygnuswelke zu tun hat. Für die Entfernung der letzteren ergibt eine Revision der Annahmen in der obenerwähnten Arbeit 18000 Parsec. Easton<sup>a</sup> macht zu diesen Resultaten einige kritische Bemerkungen und verdeutlicht mit neuem Material seine Resultate für die Wolke zwischen & und z Cygni, Er lohnt auch eine weitgehende Erklärung der Milchstraßenstruktur durch Absorption in Dunkelwolken ab

Für die Cygnuswolke liegen noch viele Untersuchungen verschiedener Autoren vor. O BERGSTRAND hat photographisch effektive Wellenlängen für Storne ble zu einer photographischen Größe zwischen 13 und 14 in der Gegend R.A. 19h 49m bis 59m, Dekl. + 35° 10' bis 37° 10', bestimmt. In einer plotzlichen Erhöhung des Mittelwerts der effektiven Wellenlängen für die Größe 12 sieht er die Einwirkung der Begrenzung des lokalen Systems und schätzt die Entfernung der Grenzo zu 2500 Parsec. Die eigentliche, zwischen  $\beta$  und  $\gamma$  Cygni aich erstreckende Wolke liegt wahrscheinlich in einer noch größeren Entfornung.

A Koppp will zeigen, daß die Annahme der Gültigkeit der Kappeynschen Luminositätskurve für die Wolke auf einen zu hohen Wert der Flächenhelligkeit führt. Wenn man an Stelle dessen annimmt, daß die Wolkensterne hauptsächlich A- und F-Sterne sind, so wird man unter Zugrundelegung der Abzählungsergebnisse von PANNEKOEK auf eine Entfernung von nur 4000 bis 6000 Parsee geführt. PANNEKORK<sup>e</sup> selbst kommt später zu einem ähnlichen Resultat. Die gegebenen Daten sind jedoch nicht zuverlässig genug, um exakte Schlüsse auf die Luminositätsfunktion zu erlauben.

<sup>&</sup>lt;sup>1</sup> M N 81, S. 215 (1921)

BAN 1, S. 157 (1922)
AN 216, S. 325 (1922)

BAN 1, S. 54 (1922).

<sup>4</sup> AN Jud. - 1. (1923).

H. Shapley hat die Verteilung von 11000 Sternen in den Milchstraßenregionen studiert und bemerkt, daß die "relativ naheliegenden" Wolken in Cygnus nur die Spektralklasse A zu beeinflussen scheinen, während im vorhandenen Material nur die B-Sterne den Reichtum der Carinagegend andeuten.

O. STRUYE<sup>2</sup> hat die Korrelation zwischen den O- und B-Sternen des DRAPER-Katalogs und dessen "Extension" und der galaktischen Helligkeit studiert. Er findet eine wahrscheinliche Entfernung der Cygnuswolke von 780 Parsec. Schalen hat in seiner obenerwähnten Arbeit eine Andeutung einer Verdichtung in der Entfernung 1000 Parsec gefunden, aber sonst eine ganz kontinuierlich abnehmende Dichtigkeitskurve bis zu 4000 Parsec.

Für mehrere andere Wolkenformationen liegen astrophysikalisch-statistische Resultate vor, die dazu beitragen können, die wahre Natur der Wolkenerschei-

nungen zu enthüllen.

Shapley<sup>8</sup> hat die Farbenindizes für 310 Sterne der Scutumwolke nahe M11 bestimmt. Er findet zwischen den Größen 12 und 15 eine Abnahme des mittleren Farbenindex von +0,98 auf +0,60. Ein analoges Phänomen sollte nach einer vorläufigen Mitteilung von Seares auch für schwache Sterno anderer Milchstraßenregionen auftreten. Soweit eine genügend ausführliche Statistik möglich ist, besteht jedoch sicher im allgemeinen eine Zunahme der Farbe mit steigender Größe. Nach F. H. Seares gilt für den Farbenindex C im Mittel für den ganzen Himmel bis zur Größe 17

$$C = +0.50 + 0.029 m_v$$
,  
 $C = -0.18 + 0.071 m_p$ ,

für eine Gruppierung nach visueller bzw. photographischer Größe. Gegen die Milchstraße nimmt die mittlere Farbe schon für helle Größen merklich ab. Für die galaktische Breite +5° ermittelt Seares im wesentlichen aus Kreikens Farbenbestimmungen für schwache Milchstraßensterne (Ziff. 17)

$$C = +0.38 + 0.024 m_v$$
,  
 $C = -0.10 + 0.048 m_p$ ,

während Kreiken<sup>o</sup> für die Milchstraße in Cepheus

$$C = -0.587 + 0.0678 m_p$$

und in Scutum-Aquila

$$C = -1,120 + 0,1051 m_p$$

herleitet.

K. Grapp, hat eine photometrische Sternfolge von 73 Sternen bis zur Größe 11,5 für eine kleine Wolke am Rande der Scutumwolke zwischen R.A. 18h 29m und  $18^{\rm h}$   $36^{\rm m}$ , Dekl.  $-4^{\circ}$ ,1 und  $-5^{\circ}$ ,1 (1855) hergestellt und auch visuell die Farben geschätzt. Er findet als bemerkenswert, daß nicht weniger als 29 Sterne die Farbenstuse 3 oder tiefer zeigen, die darauf schließen läßt, daß es sich dabei um die Spektraltypen G und K handelt. Um den Stern BD -4° 4525 herum gruppiert sich ein ganzes Nest solcher gelber bzw. rotgelber Sterne.

S. BAILEYS Sternzählung in der großen Sagittariuswolke ist an anderem

Orte (Ziff, 16) besprochen worden.

E. A. Kreiken schätzt in seiner obenerwähnten Arbeit über die Farben schwacher Milchstraßensterne aus denjenigen Sternen der Scutumwolke, die wahrscheinlich dem Typus B angehören, nach Kapteyns<sup>8</sup> Methode die Entfernung dieser Wolke zu 1500 Parsec.

<sup>&</sup>lt;sup>1</sup> Harv Circ 240 (1922).

A N 231, S. 17 (1927).
S. 64 (1917). Mt Wilson Rep. 1921.

Mt Wilson Contr 133 = Ap J 46, S. 64 (1917).
 Mt Wilson Rep 1921.
 Mt Wilson Contr 287 = Ap J 61, S. 114 (1925).
 M N 87, S. 196 (1927).
 A N 218, S. 109 (1923).
 Mt Wilson Contr 82, S. 63 = Ap J 40, S. 103 (1914). 7 A N 218, S. 109 (1923).

Dieselbe Entfernung fand H Petresson<sup>1</sup> für die Aquilawolke westlich von y Aquilac aus einer Bestimmung effektiver Wellenlangen von Sternen bis zur photographischen Größe 11,5 Eine etwas kleinere Entfernung wurde von C SCHALÉN<sup>a</sup> auf Grund omer Spektralklassifizierung ermittelt

Aus den nach ihrer Ferbe wahrscheinlich zum Typus B gehörenden Sternen in der Umgebung von M37 bestimmten H von Zeipel und J Lindgeren die

Entfornung der Aurigawolke zu 2300 Parsec.

F. H SEARES leitet aus den schwachen B-Sternen einiger Milchstraßengebiete (Selected Areas) in Taurus, Perseus, Scutum und Aquila vorlänfig Entfernungen zwischen 7000 und 14000 Parsec ab

P. Doigs berechnet für die Milchstruße in Aquila aus langperiodischen

Veränderlichen die Entforming 3000 Parsec, aus Copheiden 10000 Parsec

Eine mathematisch-statistisch wohl ausgearbeitete Methode zur Bestimmung der Entfernungen und relativen Dichtigkeiten der Sternwolken ist zuerst von K G. Malmouiste angegeben worden Für die Dichtigkeitsverteilung einer gowiesen Klasse von Stornen innerhalb einer Sternwolke setzt Maluquist nach CHARLULR

$$D(r) = D_0 e^{-\frac{(r-r_0)^2}{2\sigma^2}}, \tag{30}$$

wo also die Dichtigkeit des Mittelpunktes  $D_0$ , die mittlere Entfernung  $\tau_0$  und die Dispersion q zu bestimmen sind. Für die Leuchtkraftsfunktion und die Verteilung der scheinbaren Größen werden keine bestimmten Funktionsformen eingeführt. Die erstere wird nur durch den Mittelwert  $M_0$  und die Dispersion  $\sigma$ charakterisiert und die letztere durch den Mittelwert ma, die Dispersion a und die totale Sternanzahl N.

Für das "lokale System" bekommt man nach CHARLIER, wenn r. = 0 gesetzt und mit N die Anzahl Sterne in dem räumlichen Winkel w definiert wird,

$$S \log \varrho = m_0 - M_0 - 0.792, N_0 = \omega \sqrt{\frac{\pi}{2}} D_0 \varrho^0.$$
 (31)

(Die absolute Größe M wird als die scheinbare Größe für die Einheit der Entfernung definiert ) MALEQUIST zeigt, daß für eine entfernte Sternwolke die Unbekannten aus den als bekannt vorausgesetzten Größen nach dem folgenden Schema berechnet werden können.

$$\Phi_{\mathbf{s}}\left(\frac{q}{r_0}\right) = \sqrt{\alpha^2 - \sigma^2},$$

$$5\log r_0 = m_0 - M_0 - \Phi_1\left(\frac{q}{r_0}\right),$$

$$D_0 = \frac{N}{\sigma \sqrt{2\pi}\rho\left(\rho^2 + r_0^2\right)}.$$
(32)

Die Funktionen  $\Phi_1$  und  $\Phi_0$  sind in Tabelle 14 in Abkürzung nach MALEQUIET wiedergegeben. Für die Grenze einer Wolke kann  $|r-r_0|=3 \varrho$  gewählt werden, de die Dichtigkeit für diese Entfernung vom Zentrum der Wolke nur 0,01  $D_0$ beträgt.

Ark Mat Astr Fys 19A, Nr 3 (1925) Ark Mat Astr Fys 18, Nr. 36 (1925).

K Svenska Vet Akad Handl 61, Nr 15, S. 106 (1921)
 Mt Wilson Rep (1921)
 J B B A 35, S. 128 (1925)
 K Svenska Vet Akad Handl (III) 4, Nr 2 = Lund Modd Ser II, 46 (1927)

Tabolle 14.

eir.	$\Phi_{\perp}(\varrho/r_0)$	$\Phi_{0}\left(\varrho/r_{0}\right)$	e/r <sub>a</sub>	$\Phi_1(\varrho/r_0)$	$\Phi_{0}\left(\varrho/r_{0}\right)$
1,00	1,470	0,907	0,40	0,435	0,671
0,90	1,317	,891	,30	,264	,560
,80	1,153	,867	,20	,124	,404
,70	0,981	,836	,10	,032	,213
,60	,801	,797	,00	,000	,000

Für die Anwendung seiner Berechnungsmethode wählt Malmquist die Sterne im Farbenindexintervall 0,00 bis 0,24, was nahe der Harvard-Spektralklasse A entspricht. Die Leuchtkraftsfunktion dieser Sterne setzt sich aus zwei Frequenzfunktionen zusammen, die ein wenig voneinander verschiedene Werte von  $M_n$  (Differenz etwa 1,6 Größenklassen) haben und von denen jede eine sehr kleine Dispersion zeigt.

Aus von Zeipels und Lindgrens Farbenbestimmungen in der Nähe von M37 findet Malaguist für die Aurigawolke, daß diese in einer Entfernung von ungefähr 1450 Parsec beginnt, ihre maximale Dichtigkeit bei 2900 Parsec aufwelst und sich bis zu 4350 Parsec erstreckt. Für die maximale Dichtigkeit, pro Kubiksiriometer gerechnet, bekommt er

 $D_0 = 0.023 \pm 0.004$ .

Aus Kreikens Farbenbestimmungen in der Scutumwolke findet er die entsprechenden Zahlen 1800, 3400 und 5000 Parsec und

$$D_0 = 0.055 \pm 0.011$$
.

Aus eigenen Farbenbestimmungen<sup>1</sup> in der Umgebung des galaktischen Pols findet er für die Ausdehnung des "lokalen Systems" in dieser Richtung 1090±130 Parsec und eine Dichtigkeit der A-Sterne unserer Umgebung von

$$D_0 = 0.024 \pm 0.009.$$

Die Dichtigkeit der Wolken wäre also von derselben Größenordnung wie die Dichtigkeit des "lokalen Systems".

Kreiken<sup>2</sup> hat die Hess-Diagramme für die Aurigawolke und die Scutumwolke studiert. Er findet, daß die Verteilung der Sterne nach absoluter Größe und Spektraltypus dieselbe wie in der Sonnenumgebung zu sein scheint. In den absoluten Luminositätskurven der Wolken findet er ein sekundäres Maximum, das mit einem entsprechenden, von Shapley gefundenen Maximum für die Kugelhaufen zusammenfällt. Die Entfernungen der Wolken ergeben sich zu r=2200 bzw. 2400 Parsec, in ziemlich guter Übereinstimmung mit Malmquists aus demselben Material hergeleiteten Werten,

Ein sehr brauchbares Verfahren zur Ermittlung der räumlichen Dichte für Klassen von kleiner Streuung in den absoluten Größen bedient sich der Relationen MALMQUISTS [Gl. (19) bis (22), Ziff. 18], um aus der "scheinbaren Leuchtkraftsfunktion", nach Voraussetzung einer normalen Frequenzkurve und den beobachteten Sternzahlen in sehr direkter Weise die räumliche Verteilung numerisch zu berechnen, ohne jede Voraussetzung über die Dichtigkeitsfunktion. Die Voraussetzung einer normalen Fehlerkurve für die Leuchtkraftsfunktion scheint wegen der kleinen Streuung wenig bedenklich. Diese zuerst von Malmouist<sup>8</sup> benutzle Methode ist von Lindblad und Petersson (l. c. Ziff. 19) auf A-Sterne und Riesen der späteren Spektralklassen in einigen Gebieten hoher galaktischer Breite an-

Lund Medd Sor II, 37 (1927).

8 Lund Medd 106 (1925). <sup>2</sup> BAN 5, S. 61 (1929).

gewendet worden, und auch von Schalen in seiner eben behandelten Arbeit fiber die B- und A-Sterne in gewissen Milchstraßengebloten. Für die hellsten Milchstraßenpertien in Cygnus, Cephous, Cassiopela und Auriga findet Schalen eine langsame kontinuierliche Abnahme der Sterndichtigkeit mit der Entfernung, im allgemeinen ohne deutlichen "Wolkeneffekt" Dies ist besonders bemorkenswort, da die Korrelation zwischen Milchstraßenheiligkeit und der Zahl der Sterne pro Quadratgrad in Schalens Arbeit sehr ausgeprägt ist. Daß die hier gefundene scheinbare Abnahme der Sterndichtigkeit von einer Absorption im Raume verursacht sein kann, wird in Ziff 24 näher besprochen.

Ährliche Ergebnisse, die auf eine prinzpielle Einheitlichkeit der Milchstraßenstruktur hindeuten, sind auch von A D Maxwell¹ hergeleitet worden Er hat mit einem spaltlesen Spektrographen in Verbindung mit dem Crossley-Reflektor der Licksternwarte eine Spektraßlessifikation für Sierne in sechs Selected Areas in der Milchstraße bis su einer Grenzgröße zwischen 13,5 und 14,0 ausgeführt Dabei worden Riesen und Zwerge der späten Spektraltypen durch des Zyankriterium und durch die verschiedene allgemeine Intensitätsabnahme gegen kleine Wellenlängen (verschiedene Farbe) voneinander geirennt. Die Zentralpunkte der untersuchten Areale sind in Tabelle 15 aufgeführt.

Ta,	Pe1	lo	15
-----	-----	----	----

Selected Area No.	R.A.	Dekl.	Selected Area No.	R.A	Dekl,
64	19 <sup>k</sup> 58 <sup>m</sup>	+30° 0′	19	23 <sup>3</sup> 23 <sup>34</sup>	+60° 0′
4()	20 47	-45 0	8	1 0	+60 10
18	21 24	+60 10	0	3 4	+60 20

Für die Statistik wurde auch Material aus dem Draffer-Katalog und dessen Extension herangezogen. Die verschiedenen Spektralkiassen zeigen im ganzen einander ähnliche Dichtigkeitsverteilungen. Die Dichtigkeit ist zuerst konstant bis zu Entfernungen zwischen 400 und 600 Parzee und erleicht von hier aus eine langsame Abnahme. Keine Andeutungen sekundärer Dichtigkeitsmaxima in großen Entfernungen sind vorhanden. Die Anzahl der schwachen Sterne verträgt sich gut mit Dimensionen des galaktischen Systems von der Größenordnung 40000 Parzee. Die Frequenz der Zwerge von spätem Typns in Vergleich mit den Riesen erscheint größer, als verher für unsere nähere Umgebung angenommen worden ist, weshalb auch die Luminositätskurve einen stelleren Anstieg als van Ruijns Kurve für die absolut schwachen Größen zeigt.

Für die mittlere Farbe C als eine Funktion der photographischen Größe ergibt sich

ergidt sich  $C = -0.16 + 0.054 \, \text{m}$ ,

in ziemlich guter Übereinstimmung mit den oben gegebenen Resultaten von Seares und Kristken.

Dor Koeffizient von m stimmt auch mit dem theoretischen, von G. Shajn hergeleiteten Wort -- 0,05 tiberein. Shajn geht von der Dichtefunktion nach Kapteyn und van Rhijn aus und berechnet aus der Luminositätskurve aller Sterntypen zusammen (Kapteyn und van Rhijn) und aus einer angenommenen Luminositätsfunktion für die Bo- bis A5-Sterne separat das Verhältnis der Anzahl der Bo- bis A5-Sterne zu der Anzahl der F-, G-, K-, M-Sterne für sukzessive scheinbare Größen und für verschiedene gelaktische Regionen Aus diesen Daten berechnet er für C

$$C = +0.48 + 0.05 (m - 7.0)$$
, Milchstraße,  $B = 0^{\circ}$ ,  $C = +0.74 + 0.05 (m - 7.0)$ ,  $B = \pm (40^{\circ} \text{ bis } 90^{\circ})$ 

Liok Bull 13, S 68 (1927)

M N 86, S. 382 (1926).

Eine der Maxwellschen ähnliche Untersuchung hat C. J. Krieger¹ für die Scutumwolke ausgeführt. Die Arbeit umfaßt Sterne zwischen den Größen 5 und 18. Bis zu etwa der Größe 13 hat Krieger die Spektra der Sterne mit dem spaltlosen Spektrographen photographiert, und für schwächere Sterne hat er die Farbenindizes bestimmt. Es wurden in dieser Weise alle erreichbaren Sterne innerhalb gewisser kleiner Gebiete der Wolke untersucht, Wenn man die Häufig-

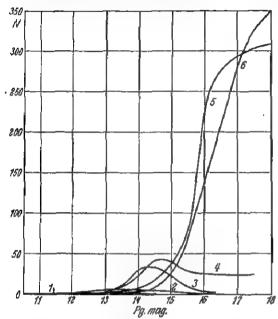


Abb. 19. Die Häufigkeit vorschiedener Farbenklassen als Funktion der photographischen Größe in der Scutumwolke nach C. J. Krieger. Die in der Figur augegebenen Nummern haben folgende Bedeutung:

Nr.	Farbenindex	Nr.	Ferbonindex
1	-0,60 bis -0,10	4	+0,40 bla +0,65
2	-0,10 ,, +0,15	5	+0,65 ,, +0,90
3	+0,15 ,, +0,40	6	+0,90 ,, +1,15

keit verschiedener Farbenklassen gegen die photographische Größe in einem Diagramm darstellt (Abb. 19), sieht man unmittelbar, in welch hohem Grade die Farbe der schwächsten Sterne (Größen 15 bis 18) mit zunehmender Größe (abnehmender Leuchtkraft) wächst.

Die Dichtefunktion hat Kriu-GER für verschiedene Spektralgruppen unter Berücksichtigung der Dispersion in absoluter Größe innerhalb der Gruppen gemäß der in Gleichungen (23) bis (25), Ziff. 18, skizzierten Methode bestimmt. Alle Spektralklassen geben eine ausgeprägte Tremung zwischen dem lokalen System und der Sternwolke (Abb. 20 bis 22). Für die Entfernung der Wolkenmitte von uns bekommt Krie-GER 2800 Parsec, was sich wohl mit Malaguists oben zitiertem Wert von 3400 Parsec verträgt, wie auch mit Kreikens letztein Wert von 2400 Parsec. Die Entfernung ist fast identisch mit den in ähnlicher Weise bestimmten Entfernungen der Sternhaufen M11 und M26, die am Himmel auf die Scutumwolke projiziert

erscheinen und also jetzt gemäß den Entfernungsbestimmungen als mit der Wolke verbunden angesehen werden können. Lindblad<sup>2</sup> hat für M11 die Distanz 2500 Parsec gefunden und TRÜMPLER<sup>2</sup> (ohne Berücksichtigung der interstellaren Absorption) 2200 Parsec für M11 und 2750 Parsec für M26.

Wenn wir Vergleiche mit den Verhältnissen in der Umgebung der Sonne nach van Riijns und Maxwells Resultaten anstellen, so erscheint die Scutumwolke ungefähr gleich reich an A-, F-, G-Sternen und an K-Sternen von der Riesenklasse und entschieden reicher an G-Sternen vom Zwergtypus, während die B-Sterne in der Wolke wahrscheinlich seltener als in unserer Umgebung sind. Krieger zieht den Schluß, daß für alle Klassen zusammen die Dichte der Wolke etwa die Hälfte der Dichte unserer Umgebung sein wird. Die Berücksichtigung

Lick Bull 14, S. 95 (1929).
 Mt Wilson Contr 228 = Ap
 Lick Bull 14, S. 154 (1930).

Mt Wilson Contr 228 = Ap J 55, S. 85 (Corr. S. 413) (1922).

Abb. 22. Die Dichtevertellung der Riesensterne in der Scutumwelks

einer oventuellen Absorption des Lichts im interstellaren Raume würde aber, gleichzeitig mit einer Reduktion der Entfernungen, eine sehr erhebliche Korrektion zu joder Schätzung der absoluten Dichte der Wolke geben

Miss L. SLOCUM1 hat ganz kürzlich durch Farbonindoxbeatimmungen für 1500 Sterne zwischen den Größen 12 und 18,5 in clen Kaptrynschen Feldern 8. o. Abb 20 Die Dichteverteilung der A-Sterne in der Scutum-18, 19, 64 die Maxwellsche Arwolks nach Kriegen beit fortgesetzt Die Dichtevertoilung im Raume wird unter Beritcksichtigung einer allgemeinen Absorption im TRUMPLERSchen Bo-At A2-A6 Sinne (Ziff. 24) hergeleitet Für die selektive Absorption ergibt sich aus 53 Sternen mit bekannten Spektren und Parbenindizes der mit Trümpler naho über-Abb 21 Die Dichtsverteilung der Zwergsterne in der Soutumwelke, F3-453

einstimmende Wert +0m,00034 per Parsec, und es wird angenommen, daß dies etwa 0,4 der allgemeinen Absorption entspricht. Für die Dichte o des absorblerenden Mediums wird ein Ausdruck  $\delta = \sigma' e^{-r/d}$ , wo c' = 2.4,  $\varrho = 9000$ , angesetzt; die Absorption nimmt also ziemlich schnell mit wachsender Entfernung ab. Die nach diesem Prinzip ermittelte Sterndichte nimmt mit steigender Ent-

<sup>1</sup> Lick Buli 15, 8 123 (1931).

fernung ab, am schnellsten in unserer Nähe, zeigt aber eine Andeutung eines sekundären Maximums für r=2000 bis 2500 Parsec, und in der Cygnusregion (Area 64) auch für r=6000 Parsec. Das letztere Ergebnis stimmt mit den obenerwähnten Entfernungsbestimmungen von Kopff und Pannekoek für die Cygnuswolke überein.

23. Spezielle Untersuchungen über die Natur der Magellanschen Wolken. Wie schon in Ziff. 40 erwähnt, ist die Stellung der Magellanschen Wolken eine ganz besondere. Die große Bedeutung dieser Gebilde in der gegenwärtigen Forschung können wir mit H. Shapley¹ etwa folgendermaßen formulieren. Sie sind uns nahe genug gelegen, um vollständig in Millionen von Sternen aufgelöst zu werden, und doch entfernt genug, um ganz von außen her gesehen und untersucht zu werden. Sie dienen als Schlüssel zur Kenntnis entfernter Milchstraßen und eröffnen hierdurch den Weg aus lokalen Regionen in ein äußeres Universum hinaus. Die Spezialforschungen auf diesem Gebiete werden in anderen Teilen dieses Handbuchs ausführlich behandelt, und wir können hier nur in einer kurzen Übersicht die wichtigeren Punkte erwähnen.

Der große Reichtum der zwei Wolken an Nebeln und Sternhaufen wurde schon von J. Herschel entdeckt, aber eine eigentliche astrophysikalische Untersuchung beginnt erst mit dem Anfang unseres Jahrhunderts durch die photographisch-photometrische Arbeit der Harvard-Sternwarte mit einem zu Arequipa aufgenommenen Plattenmaterial. Die ersten Früchte dieser Arbeit waren Miss H. Leavitts² Kataloge über die in den Wolken beobachteten veränderlichen Sterne, 808 in der großen, 969 in der kleinen Wolke. Die von Miss Leavitt für 25 å Cephei-Veränderliche in der kleinen Wolke gefundene Relation zwischen Periode und Helligkeit wurde zuerst von E. Hertzsprung³ zu einer Entfernungsbestimmung dieser Wolke benutzt. Shapleys Festlegung der Relation zwischen Periode und absoluter Größe für die å Cephei-Sterne hat dann aber eine neue Bestimmung der Entfernungen der zwei Wolken herbeigeführt. Nach seiner letzten Revision der "Period-Luminosity Curve" findet er aus 107 å Cephei-Veränderlichen in der kleineren Wolke und 50 in der großen folgende Werte<sup>4</sup>:

Die zur Zeit bekannten zehn Kugelhaufen in den Wolken haben scheinbare Durchmesser von 1 bis 2 Bogenminuten. Eine hierauf begründete Entfernungsbestimmung liefert mit den oben gegebenen sehr nahe identische Werte.

K. Lundmark<sup>5</sup> hat für die große Wolke zur Entfernungsbestimmung außer den Kugelhaufen auch die Wolf-Rayet-Sterne und die offenen Haufen benutzt und findet im Mittel den Wert  $\pi = 0'',000036$ , der offenbar sehr gut mit dem oben gegebenen übereinstimmt.

Die Magellanschen Wolken geben uns eine wichtige Gelegenheit, den Verlauf der Leuchtkraftsfunktion im Gebiet der allerhellsten Sterne zu untersuchen, und sie geben uns auch Aufschluß über die absoluten Größen verschiedener Objekte von sehr großer Leuchtkraft, wie Nebel, Haufen und Sterne von gewissen abnormen Typen. Besonders die Untersuchungen von Shapley<sup>6</sup> und seinen Mitarbeitern sind hier erfolgreich gewesen. Zu erwähnen ist, daß einzelne

Star Clusters, Harvard Monograph No. 2, S. 183 (1930).

<sup>&</sup>lt;sup>8</sup> Harv Ann 60, S. 87 (1908). O AN 196, S. 201 (1913). L. c. S. 189.

Obs 47, S. 276 (1924); Pop Astr Tidskr 5, S. 146 (1924).
 Harv Circ 255, 260, 268, 271, 275, 276, 280, 288 (1924-1925).

Sterne die überaus hellen absoluten Größen —5 und —6 erreichen Einige rote Veränderliche der Spektralklassen K bis Mc und fünf Sterne vom P Cygni-Typus gehören zu den hellsten Sternen der großen Wolke<sup>1</sup>. Die Nebol sind im allgemeinen von einem diffusen, irregulären Typus, unter ihnen ist der Riesennebel 30 Doradus, mit einer absoluten Größe wahrscheinlich heller als -13 und einem Durchmesser von etwa 30 Parsec, besonders auffallend LUNDMARK bemerkt, daß dieser Nobel eine Anzahl von dunklen Flecken in der Nobelfläche zeigt, in genau derselban Wolse, wie wir sie in vielen von den hellen Milchstraßennebeln schen. Überhaupt sind in der großen Wolke dunkle Risse von verwickelter Natur vorhanden, die sehr an Erscheinungen in der Milchstraßenstraktur erhnern,

Die Spektra der Gasnebel geben für die große Wolke eine Radialgeschwindigkeit von +276 km/sec und für die kleine +168 km/sec. Hertzsprung hat die Hypothese aufgestellt, daß gewisse Differenzen in den Radialgeschwindigkeiten für die 17 beobachteten Nebel der großen Wolke sich im wesentlichen als eine Folge einer parallelen und gleich großen Bewegung dieser Nebel im Raume erklären. Es zeigt sich dabei, daß die Redialgeschwindigkeit der kleinen. Wolke sich in diese Reihe einordnen läßt, so daß die zwei Wolken in der Tat eine gemeinsame Bewegung haben können. Als Konvergonspunkt ergibt aich & = 4h94m.  $\delta = -5^{\circ},5$  and für die Geschwindigkeit relativ zur Sonne 625 km/sec

Die Rotationatheorie der Milchatraße läßt uns aber das Problem der Bewegung der Wolken aus einem anderen Gesichtspunkt betrachten J H Ookr' bemerkt, daß mit einer Geschwindigkeit der Sonne von 286 km/sec gegen einen Punkt  $L = 55^{\circ}$ ,  $B = 0^{\circ}$  (vg), Ziff, 30) die Residuen der Radialgeschwindigkeiten die Werte +41 km/sec und -9 km/sec annohmen Es ist also recht wahrscheinlich, daß die Wolken nur kleine Geschwindigkelt relativ zum Schwerpunkt des Systems besitzen.

W J. LUYTENS hat, wesentlich auf dem Boden der Hertzsprungschen Hypothese, die möglichen Bahnformen der Wolken relativ zum Zentrum der Milchstraße unter verschiedenen Annahmen über die Masse des Milchstraßensystems diskutiert. Das Resultat ist ansærst unsicher, zelgt aber, daß auch mit einer verhältnismäßig hohen totalen Geschwindigkeit der Wolken relativ zum

crwalinton Zentrum elliptische Bahnen nicht ausgeschlossen sind.

Gegon die Annahme einer direkten Zusammengehörigkeit der zwei MAGELLANschen Wolken mit den Milchstraßenwolken hat eine andere Auffassung behauptet, daß sie oher zu den extragalaktischen Nobeln gerechnet werden sollten, also Objekte sind, die zufälligerweise in die Nähe des Milchstraßensystems gekommen sind. Die letztere Meinung ist wohl sugrat von CLEVELAND ABBE® klar ausgesprochen worden. Später hat LUNDMARK, die Ähnlichkeit der großen Wolke mit dem Nebel NGC 4449 nachgewiesen und dann auch die überaus wichtige Beobachtung gemacht, daß die Wolken sogar als Typen für eine gewisse Klasse von Nebeln dienen können. Zu den auffallenderen Objekten von dieser Klasse gehört der Nobel NGC 6822, der eingehend von E. Hubbles unteraucht worden ist. In der neuesten Zeit steht man zwar ganz auf dem Boden der letzteren Auffassung, ist aber geneigt anzunehmen, daß die Wolken doch etwa als "ferne Begleiter" dem Milchstraßensystem angehören (vgl Ziff. 34).

Zuictzt sei hier erwähnt, daß D. WATTENBERG eine eingehonde Besprechung der neueren Resultate über die Natur der Mackillanschen Wolken gegeben hat.

Miss Cannow, Harv Bull 754 u 801 (1921, 1924).

Liok Obe Publ 13, S. 168 u. 187 (1918).

M N 80, S 782 (1920); Nordisk Astr Tidaskr 1, S. 133 (1920)
B A N 4, S. 79 (1927). Wash Nat Ac Proc 14, S. 241 (1920) Wash Nat Ac Proc 14, S. 241 (1928) - Harv Rope 44.

MN 27, 6, 262 (1867) 7 K Svenska Vet Akad Handl 60, Nr 8 (1920) Mi Wilson Contr 304 - Ap J 62, 8, 409 (1925)

Naturwise 18, S. 696 (1930); A N 237, 5 401 (1930).

24. Die Absorption des Lichts im interstellaren Raume, Wil haben schon oben in Ziff 18 und 20 die große Bedeutung der Frage, ob eine allgemeine Absorption im interstellaren Raume existiert, für die Erforschung der raumlichen Dichteverteilung im Milchstraßensystem heivorgehoben Selliger und Kapilyn hatten beide einen Höchstbetrag dei Absorption berechnet unter der plausiblen Annahme, daß die wahre raumliche Dichte für große Entfernungen nicht erheblich anwachsen kann Kapteyn<sup>1</sup> hat z B aus dieser Erwagung einen Hochstbetrag von ein paar tausendstel einer Großenklasse pro Parsec angegeben, wahrend Seeliger nach dem in Ziff 18 eiwähnten Pinzip, welches eine bestimmte Funktionsform fur die "scheinbare" Dichteverteilung einschließt, nur einen noch erheblich kleineren Absorptionskoeffizient zugeben wollte. Da eine Absorption der genannten Art sehr wahrschemlich mit dei Wellenlange veranderlich sein wird, wurde das Interesse zunächst auf die Frage nach der Existenz einer selektiven Absorption gefulnt Man hat so wiederholt versucht, eine direkte Abhangigkeit der Fai be der Steine von ihrer Entfernung festzustellen. Anschemend positive Resultate in dieser Hinsicht wurden von Kapteyn, Jones, King, van Riijn u a 2 hergeleitet Diese Versuche gelangten aber zu einem gewissen Abschluß daduich. daß das Problem durch eine deutliche Abhängigkeit der Farbe von der absoluten Größe innerhalb gewisser Spektraltypen kompliziert wurde, und vor allem dadurch, daß die Evidenz aus den Farbenbestimmungen in den Kugelhaufen und für extragalaktische Nebel entschieden gegen die Existenz einer allgemeinen solcktiven Absorption sprach Eine Untersuchung von K LUNDMARK8 über die Variation der Flächenhelligkeit der extragalaktischen Nebel mit der Entfernung und von II Shapley und A Amest über den Zusammenhang zwischen Durchmesser, photometrischer Größe und Entfernung für Nebel im Coma-Virgo-Gebiet setzten eine ungeheuer enge obeie Gienze auch für eine nichtselektive allgemeine Absorption In derselben Richtung geht auch van Riijns Resultat aus einem Studium des Zusammenhanges zwischen Durchmessei und photometrisch bestimmter Entferning für die Kugelhausen wie auch Shapleys in Ziff 20 ei wähnte Folgerung betreffs der Umgebung des zentralen Verdunklungsgebietes in Sagittarius-Ophiuchus

Die Idee, daß die "anthropozentrische" Anordnung der Steine, welche die nach allen Seiten abnehmende Steindichte unserer Umgebung anzeigt, nur scheinbar sei und den Effekt einer Absorption darstelle, eine Idee, die wohl am konsequentesten von J. IIalm durchgeführt worden ist, ist jedoch niemals ganz aufgegeben worden Ganz kürzlich hat C Schalen Tiege auf Grund seiner oben (Ziff 22) besprochenen Arbeit über B- und A-Steine in ausgewählten galaktischen Regionen aufgenommen Fin die Spezialgruppen höchster Luminosität ( $\tau$  und  $\tau$ — genannt) hat er untersucht, welcher Absorptionskoessizient  $\nu$  für konstante räumliche Dichte in der Milchstraßenebene vorauszusetzen ware Wenn wir die Absorption in Größenklassen per Parsec rechnen und diesen Koessizienten mit  $\alpha$  bezeichnen, so hat man  $\alpha = 2,5\log e \cdot \nu = 1,09\nu$  Für die als normal betrachteten Regionen in Cepheus und Cassiopera findet Schalen

 $\alpha = 0,0005 \text{ mag/Parsec}$ 

Für die Autigaregion mag der größer gefundene Weit vielleicht auf eine wirkliche Abnahme der Dichte in der Richtung vom Zentrum des Milchstraßensystems (in

<sup>&</sup>lt;sup>1</sup> A J 24, S 115 (1904) <sup>2</sup> Für die historische Entwicklung des Problems siehe besonders II Kinnle, Die Absorption des Lichtes im interstellaren Raume Jahrbuch der Radioaktivität und Elektronik 20, II 1 (1922)

MN 85, S 865 (1925)
4 Harv Bull 864 (1929)
5 BAN 4, B 123 (1928)
6 MN 77, S 243 (1917), 80, S 162 (1919).
7 AN 236, S 249 (1929)

der galaktischen Länge 330°) zurückgeführt werden Auch in Cygnus findet ei einen größeren Wert Wenn die letztgenannten zwei Regionen mitgerechnet werden, kann man nach Schalan als obere Grenze  $\alpha < 0.0020$  mag/Parsec setzen.

SCHALÉNS Resultat wurde dann in sehr bemerkenswerter Weise durch R TRÜMPLERS¹ Untersuchung über die offenen Sternhaufen (Ziff. 20) bestätigt und ergänzt. Wenn wir die photometrisch ohne Berücksichtigung der Absorption bestimmte Entfernung eines Haufens mit r', die wahre Entfernung mit r bezeichnen, so haben wir

$$m - M = 5\log r' - 5$$
$$= 5\log r + \alpha r - 5$$

Wenn welter d der scheinbare Durchmesser in Bogenminuten, D' und D die mit r' bzw r gerechneten linearen Durchmesser in Parsec sind, haben wir

$$\log D' = -3.536 + \log d + \log r' \log D = -3.536 + \log d + \log r$$

Wir bekommen also

$$\log D' - \log D = \frac{\alpha}{5}r,$$

und im Mittel

$$\overline{\log D} = \frac{\alpha}{5} \, \bar{r}$$

Wenn wir jetzt eine Unterabteilung von Haufen mit kleiner Streuung in  $\log D$  betrachtan, so können wir  $\overline{\log D} = \log D$  setzen und für die direkt aus den scheinbaren Durchmessern gebildeten Differenzen

 $v' = \log D' - \overline{\log} \overline{D}'$ 

bekommen wir dann direkt

$$v'=\frac{\alpha}{5}\left(r-\bar{r}\right),$$

oder

$$v' = a + b\tau$$

WU

$$a = \frac{\alpha}{5}\bar{r}, \qquad b = \frac{\alpha}{5}$$

r wird in sukzessiven Annäherungen aus der Relation

$$\log r + br = \log r'$$

ermittelt Trümpler hat für verschiedene galaktische Längen die Werte von &, für 1000 Parsec gerechnst, zusammengestellt (Tab 16)

Es besteht offenbar eine sehr gute Übereinstimmung zwischen Schalens und Trümplers Resultaten Trümpler macht jetzt die Annahme, daß diese Absorption nur in einer verhältnismäßig dünnen Schicht um die Zentralebene der Milchstraße herum besteht Vielleicht ist diese Schicht nur etwa 200 bis 300 Parsec dick, in der Milch-

Tabollo 16.							
Galaktische Länge	ø	m, F					
330°- 45° 45110 110195 195330	0°,79 ,59 ,87 (,37)	土0 <sup>二</sup> ,09 土 ,08 土 ,17 土 ,16					
Allo	.67	士 .07					

straßenebene selbst aber wahrscheinlich seht weitgestreckt und geht vielleicht als eine Trannungsfläche durch das ganze System hindurch

<sup>1</sup> Llok Bull 14, S 154 (1930).

Auch die von Shapiley, Herrzsprung, Seares und Wallenguist konstatierten Farbenenzesse in gewissen offenen Haufen werden von Trümpler als Absolptionseffekte gedeutet. Wenn wir für den Enzeß E im Farbenindex

$$E = \iota r$$

ansetzen, bekommt Trumpler fur den Kocffizienten

$$c = +0^{m},32 \pm 0,^{m}03$$
 (per 1000 Parsec)

Da auch dieser Effekt nach Trümplers Annahme an die dunne absorbierende Zentralschicht gebunden ist, erklart sich ungezwungen, warum kein Farbeneffekt für Kugelhaufen und extragalaktische Nebel konstatiert worden ist

Der Farbeneffekt für den Hausen NGC 663 und sun Steine, die auf diesen Hausen projeziert eischeinen, ist nach Beobachtungen von Å Wallenquist und C Schalen von letzterem¹ diskutiert worden. Er sindet sur den Koeffizienten c den Weit 0<sup>m</sup>,26±0<sup>m</sup>,03 Die Farbeneffekte für entseinte Milchstraßensterne von frühem Typus haben P van de Kamp² und Y Öhman³ behandelt Der erstere findet ein Resultat in enger Übereinstimmung mit Trümpifr und leitet als besten Weit ab

$$c = +0^{\text{m}},331 \pm 0^{\text{m}},022 \text{ (per 1000 Parsec)}$$

Ei sucht auch einen Einfluß der galaktischen Breite auf die Absorption zu finden, um daraus die Dicke der absorbierenden Schicht zu bestimmen. Er findet im Mittel aus dem Absorptionsessekt für verschiedene Klassen von entseinten Objekten (Haufen, B-Sterne, Nebel) eine Dicke dieser Schicht von 175 ± 50 Parsec Dieser Wert muß aber noch als sehr unsicher betrachtet werden

Ohman deutet den oft ausgeplägten Farbenevzeß fut schwache B-Steine als einen Entleinungsesiekt und sindet aus seinem Material den Koessizienten 0,19 mag per 1000 Parsec fur ein Farbenaquivalent, welches aus dem Intensitätsverhaltnis sur die Wellenlangen  $\lambda$  3912 A und  $\lambda$  4415 A im Spektium gebildet ist Dieses Resultat läßt sich gut mit Trümplers und van die Kamps Farbenkoessizienten vereinen, welcher sur die Wellenlangen  $\lambda$  4300 A und  $\lambda$  5600 A gilt Ein mit den obigen Ergebnissen sehr nahe übereinstimmendes Resultat  $c = \pm 0^{m}$ ,34  $\pm$  0<sup>m</sup>,03 hat kürzlich Miss L Slocum<sup>4</sup> (vgl. Ziss 22) ermittelt

K F Bottlinger und H Schneller<sup>6</sup> haben endlich auf einen anderen Effekt der absorbierenden Schicht hingewiesen. Es wird die Absorption in einer derartigen Zentialschicht zur Folge haben, daß eine Klasse von Objekten, die eine einebliche Konzentration gegen die Milchstraßenebene zeigen, für größere Entfernungen scheinbar eine zu kleine Konzentration aufweisen wird. Denn berechnet man die Entfernungen ohne Berucksichtigung der Absorption, so daß diese für schwache Sterne zu groß ausfallen, so wird der Absorption, so daß diese für schwache Sterne zu groß ausfallen, so wird der Absorption, so daß diese größer wird ihr mittlerer Abstand von der galaktischen Ebene sich eirechnen In der Tabelle 17 sind die mittleren Z-Koordinaten, eistens ohne Berücksichtigung der Absorption, zweitens (Z') mit der Trömplerschen Absorption  $\alpha = 0^m$ ,67 und zuletzt (Z'') mit einer Absorption  $\alpha = 2^m$  pro 1000 Parsec gerechnet. Für diesen größeren Wert der Absorption finden Bottlinger und Schneller einige Stütze in Schalens Resultaten für die Cygnus- und Aufgaregionen

Ark Mat Astr Fys 22A, Ni 15 (1930) = Upsala Medd 49

<sup>&</sup>lt;sup>2</sup> A J 40, S 145 (1930)

Spectrophotometric Studies of B-, A- and F-Type Stars N Acta Reg Soc Sc Upsahensis
 (IV) 7, Nr 3 (1930) = Upsala Medd 48
 Lick Bull 15, S 123 (1931)

<sup>&</sup>lt;sup>5</sup> Z f Astrophys 1, S 339 (1930)

Tabolle 17

Bnijernungsbereich in Klioperies	Ansahl der Sterne	Ē	[Z]	Ŕ	[ <b>E</b> ']	P**	[E"]
0- 1	38	597	71	491	59	394	48
1- 2	33	1 524	111	1066	77	747	54
2- 3	26	2442	139	1482	85	991	55
3- 4	26	3 508	148	1862	79	1174	48
4- 6	26	4 908	144	2282	66	1386	37
6—12	10	8 486	438	2975	163	1723	94
12—25	16	16 385	448	4062	108	2182	57

Die stellerastronomische Bedeutung der Absorption Hegt vor allem darin, daß die ompirische Grundlage, auf welche die um die Sonne rotationssymmetrische Anordnung des "typischen" Sternsystems und später des "lokalen" Systems gegrundet wurde, sich aufzulösen beginnt. Es wird hier mehr und mehr offenbar, daß die Verteilung der Materio in der Milchstraßenebene bis zu sehr großen Entfernungen von uns als wesentlich gleichfürmig ansusehen ist, und daß wir berechtigt sind, jeder ausgeprägt "anthropozentrischen" Anordnung der Materie im System mit Mißtrauen zu begegnen

Die physikalische Erklärung der Absorption steht noch im wesentlichen offen 25. Die Kalziumwolken in der Milchstraße. Ein Phänomen, das violleicht mit der eben behandelten Extinktion in einer mittleren Milchstraßenschicht in Beziehung steht, haben wir in dem im Jahre 1904 von Hartmann entdeckten Absorptionseffekt der sog, "ruhenden" Kalzinmlinlen. J. HARTMANN fand, daß im Spektrum des spektroskopischen Doppelstorns & Orionis die K-Lanie die periodische Verschiebung der Linien nicht zeigte und schloß daraus, daß irgendwo auf der Verbindungslinie zwischen uns und dem Stern eine Wolke existlert, die eine Absorption in der erwähnten Linie hervorruft. Er machte auch die Beobachtung, daß im Spektrum von Nova Persol die H- und K-Linien wie auch die D-Linien als scharfe Absorptionslinien, die einer kleinen konstanten Radialgeschwindigkeit (+7 km/sec) entsprechen, vorhanden waren. Scharfe Kalziumlinien sind bald durant von E B Prost und W. S. Adams im spektroskopischen Doppelstern 9 Camelopardalis beobachtet worden und Froats machte einige Jahre später Mittellungen über scharfe Kalzlumlhilen in den Spektren von 25 Sternen. Die Linien sind dann oftmals in den Spektren der spektroskonischen Doppelsterne identifiziert worden. Das Auftreten der H- und K-Linien in den Novae hat such J. Eversuep' diskutiert. Die aus diesen Linien symittelten Radialgeschwindigkeiten für Nova Persel, Nova Gemmorum Nr 2 und Nova Aquilas wie auch für sechs spektroskopische Doppelsterne deuten an, daß die Bewegungen dieser Sterne fast gans der Sonnenbewegung entsprechen, und daß also das Kalzium sich sehr nahe in Ruhe relativ zum Zentrold der uns umgebenden Sterne hofindet. R. H Curriss hat allerdings eine langsame Veranderung der Geschwindigkeit aus den H- und K-Linien für die Nova Geminorum 1912 konstatieren wollen, während für Nova Agulias 1918 und die Nova Cygni 1920 die Linien stationär erscheinen.

Die stationaren D-Linien wurden von Miss Hegers studiert. Eine Zusammenfassung des Beobachtungsmaterials und eine eingehende Diskussion des ganzen Problems wurde zuerst von R. K. Young ausgeführt. H Luden der Ff

Situber K Akad Wiss Berl (1904), S 527, Ap J 19, S 268 (1904)
 Ap J 19, S 350 (1904)
 Ap J 29, S 234 (1909)
 Obs 42, S 85 (1919).
 Pop Astr 33, S 167 (1925)
 Lick Bull 10, S 59 (1919); 10, S 141 (1921).
 Publ Astrophys Obs Victoria 1, S 219 (1920), J Can R A S 14, S 389 (1920)
 A N 211, S 118 (1920), 212, S 11 (1921)

hat gefunden, daß die schaifen Linien speziell für die Heliumsteine mit besonders großen Massen auftreten und betont die Schwierigkeiten der verschiedenen Eiklarungshypothesen Die Theorie, daß die K-Linie in einer zu dem betreffenden Stern gehörigen Atmosphare entsteht, erscheint nicht befriedigend, und die Annahme einer kosmischen Wolke reicht auch nicht aus, da bei einigen Systemen die K-Linie Verschiebungen in derselben Periode wie die übrigen Linien zeigt, wenn auch mit kleineiei Amplitude Einen sehr erheblichen Schritt vorwarts bedeutet dann die Untersuchung der betreffenden Linien für die O-Sterne durch I S PLASKETT<sup>1</sup> Das Volkommen dei Linien in allen Typen fluhei als B3 und der wahrscheinlich interstellare Ursprung der Linien wird hier besonders betont Eine partielle Oszillation dei Linien in gewissen spektroskopischen Doppelsteinen vom B-Typus kann durch eine Kombination der stationalen interstellalen Linien mit den schwachen Kalziumlinien dei Steinatmosphaien selbst eiklait weiden, da nach R H Fowlers und E A Milnes theoretischer Arbeit die H- und K-Linien eist bei dem Typus B0 oder früher vollkommen verschwinden Unter anderen, die sich mit dem Problem beschaftigt haben, befinden sich F HENROTEAU2 und H KIENLE3, der eine eingehende Behandlung der Geschwindigkeitsdifferenzen Stein-Wolke in ihrer Abhangigkeit vom Spektialtypus gegeben hat Auflösungen fur die Sonnenbewegung haben z B Henroteau' und G Strombleg gegeben J Wolijer ji hat dei Ansicht Plaskerts eine weitere theoretische Begrundung gegeben

Em weiterer Fortschrift zur Deutung der stationaren Linien war insbesondere A S Eppingtons' theoretische Behandlung des Problems Plaskett und Woltjer hatten den Gedanken ausgesprochen, daß die Kalziumatoine vorzugsweise in der Nahe der heißeren Sterne die fur das Auttreten der Ca+-Linien notwendige Gegen diese Ansicht hebt Eddington hervor, daß die Ionisation eileiden relative Konzentiation dei Ca+-Atome in dei Nahe dei heißeren Steine als eine Folge einer zweimaligen Ionisation abnehmen muß, und er zieht den Schluß, daß die Absorption gleichmaßig langs dem Visionsiadius voi sich geht. Eine außer ordentlich dunne, allgemein ausgebreitete Materie aus Kalzium und anderen Elementen kann in genugend großer Menge vorkommen, ohne in meßbarer Weise die scheinbale Leuchtkiaft oder die Falbe der Steine zu andein

Die Temperatui dei interstellaren Materie in einem gewissen Punkte ist nach Eddington auf Grund der Geschwindigkeiten der durch Strahlungserregung aus den Atomen gelösten Elektronen von derselben Größenordnung wie die Temperatur, die der spektralen Energieverteilung der Strahlung in dem betreffenden Punkte entspricht. Für diese Temperatur T kann abei die Temperatur der umgebenden Steine, etwa 10000°, gesetzt werden Wenn wir mit  $I(v, \hat{T}) dv$ die Strahlungsdichte bei thermodynamischem Gleichgewicht für ein Frequenzintervall zwischen  $\nu$  und  $\nu + d\nu$  und für die Temperatur T bezeichnen, so setzt Eddingson für die Dichte der Strahlung im interstellaren Raume

$$I(v,T) dv/\delta$$
,

wo  $\delta$  als "factor of dilution" auftitt. Man hat dann die Regel, daß die Ionisationsverhältnisse der interstellaren Materie von der Dichte  $\rho$  dieselben sind wie in Materie von der Dichte  $\rho \delta$  in thermodynamischem Gleichgewicht bei dei Tem-

Publ Astrophys Obs Victoria 2, S 335 (1924), M N 84, S 80 (1924)

<sup>&</sup>lt;sup>2</sup> J Can R A S 15, S 62 (1921) <sup>3</sup> SEELIGER-Festschr, S 38 (1924), M N 84, S 583 (1924)

<sup>4</sup> J Can R A S 14, S 234 (1920)

Mt Wilson Conti 243 = Ap J 61, S 372 (1925)
 BAN 2, S 125 (1925)
 London R S Proc 111 A, S 424 (1926), The Internal Constitution of the Stars, S 377 Cambridge 1926

peratur T Der Ionisationsgrad wird nämlich durch Gleichsetzung der Anzahl eingefungener Elektronen mit der Anzahl durch Ionisation ausgelöster erhalten Die erstere Anzahl ist proportional der Elektronendichte, die letztere der Strahlungsdichte Eine Multiplikation von beiden mit einem Faktor  $\delta$  ändert das Gleichgewicht nicht. Der Faktor  $\delta$  kann aus dem Gesamtbetrag des Sternenlichts berechnet werden; für  $\varrho$  nimmt Eddington gemäß einer isothermen Gleichgewichtstheorie für die diffusen Nebel, die als Kondensationen in der interstellaren Materie angeschen werden können, die Größenordnung  $10^{-26}$  g/cm². Er erhält dann nach der Ionisationstheorie für die relativen Konzentrationen der verschiedenen Ca- und Na-Atome folgonde Werte

$$\frac{Ca}{Ca^{+}} = \frac{1}{300000}, \qquad \frac{Ca^{+}}{Ca^{++}} = \frac{1}{400}, \qquad \frac{Na}{Na^{+}} = \frac{1}{1000000},$$

Für Ca wäre also der weit überwiegende Teil der Atome zweimal ionisiert und diemnach zur Absorption in H und K unfähig. Ein analoges Verhältnis ergibt sich für die D-Linien des neutralen Natriums. Nur ein sehr kleiner Teil der interstellaren Materie von der angenommenen Dichte wäre also bei der Absorption in den erwähnten Linien wirksam, was auch mit den schwachen Intensitäten der Linien in den Sternspektren in Übereinstimmung staht

In O. STRUVES1 Arbeiten wurde das Problem auch empirisch von einer nouen Scite her angegriffen. Vorzagsweise für Sterne vom Spektraltypus O bis B3 hat er auf Spektrogrammen die Intensität der interstelleren K-Linie geschützt Das Arbeitsmaterial bildeten zuerst für 321 Sterne vom Typus O bis B3 Spaltspektrogramme, die auf den Sternwarten Mount Wilson, Victoria, Lick und Yerkes aufgenommen warden sind, dann für 1718 Sterne vom Typus O bis B3 und für 338 Sterne von spätoren Typen Objektivprismenplatten aus cler großen Sammlung der Harverd-Sternwarte. Die Intensitäten wurden in einer Gedächtnisskale geschätzt, wo jede sukzessive Stufe einer eben bemerkbaren Zunahme der Intonsität entspricht. Für die Spaltspektrogramme ist die Intenwitelt der K-Linie im Spektrum der Vega auf 10 fixiert worden, später wurde der Stern 9 Cephel ( $\alpha = 21^h 35^m, 2$ ,  $\delta = +61^\circ 38'$ , B2p;  $4^m, 7$ ) als Standard mut derselben Intensität benutzt. Der wahrscheinliche Fehler einer Schätzung war 0.5 Stufen für die Platten der ersteren Art und etwa 4,0 für die Harvard-Platten Nach einer genäherten Kalibrierung der Skale entspricht jede Stufe einer Größendifferenz von etwa on, in dem Intensitätsverhältnis zwischen Limenmitte und umgebondem kontinuierlichen Spektrum.

Mit seinem vollständigen Material hat Struve ausführlich die Relation zwischen Intensität, Spektraltypus und schembarer Größe untersucht. Tabelle 18 zeigt das Resultat für die Spektrultypen O bis B3. Für die späteren Unterabteilungen des B-Typus übt schen die Absorption des Kalziums in der Sternatmosphäre einen merklichen Einfluß auf die Intensität der K-Linie aus.

Man sicht aus der Tabelle unmittelbar, daß für alle Untertypen die Intensität in derselben Welse mit abnehmender scheinbarer Helligkeit wächst, und auch daß für eine und dieselbe scheinbare Größe die früheren Typen in der Regel die größere Intensität aufwelsen. Diese Erschelnungen können am emfachsten dadurch erklärt werden, daß die Intensität einfach eine Funktion der Entfernung der Sterne ist. Daß der Gang mit der scheinbaren Größe nicht auf irgendelnen systematischen Fehler zurückzufähren ist, beweist Struve durch Schätzungen der Linie 2 1924 (Sl++). Die mittlere Intensität dieser Linie zengt keine Abhängigkeit von der scheinbaren Größe

Pop Astr 33, S 639 (1925), 34, S, 158 (1926), A N 227, S, 377 (1926), Pabl A S P 38, S 211 (1926); Mt Wilson Contr 331 - Ap J 65, S, 163 (1927), Ap J 67, S, 353 (1928)

Tabelle 18

Scheinb		0	1	Bo		Bı	} !	B2	1	33
Große	ħ	I	n	1	n	I	W.	Ī	n	I
0- 1	0	_	0		1	1,0	0		0	1
1-2	0	1 -	2	2,0	4	0,7	3	0,9	1	0,4
2-3	3	0,9	6	1,2	5	1,8	7	1,4	11	1,4
3-4	1	5,1	2	2,6	5	1,4	10	1,7	24	1,8
4-5	6	3.9	9	2,6	11	[ 3,0	18	3,0	97	2,1
5- 6	12	4,1	21	4,2	8	4.0	23	3,3	141	2,5
6-7	17	4,2	45	3,4	11	4,2	42	3,2	201	2,0
7-8	24	5,0	66	3,8	17	3,8	85	3,9	197	3,2
8-9	19	4,8	94	3,9	4	3,0	87	3,9	168	3,1
9-10	9	3,8	55	3.7	0	)	44	4,3	74	4,0
10-11	3	3.7	2	4.8	0	<del></del>	7	4,4	15	4,6
1-12	1	11,0	0		0	[ -	0	-	0	-
4114	95	4,40	302	3.71	66	3,13	326	3,65	929	2,97

Die mittleren Intensitaten für verschiedene Milchstraßemegionen werden nach Struve in Abb 23 dargestellt

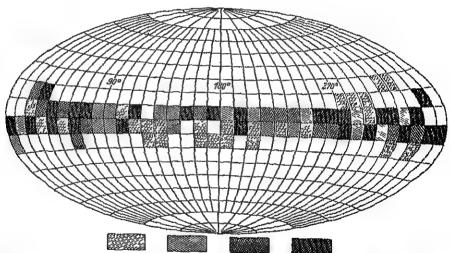


Abb 23 Galaktische Verteilung der Kalzumintensitäten Die vier Schattlerungen entsprechen der Reihe nach I < 2.8;  $2.8 \le I < 3.2$ ,  $3.2 \le I < 3.7$ ,  $3.7 \le I$  Die galaktischen Koordmaten der wichtigeren Regionen sind

Perseus Orion Monoceros Carina Crux Scorpius Sagittarius Cygnus Cepheus	$L = 100^{\circ} - 120^{\circ},$ $160 - 180$ $170 - 180$ $250 - 260$ $260 - 280$ $300 - 320$ $330 - 340$ $30 - 50$ $60 - 80$	B = -10° bis -10 0 -10 -10 -10 -10 -10	~20 ←10 ←10 ←10 ←10	(sohi schwach) (schi stark) (stark) (schi stark) (stark) (stark) (sehr stark)
		v	710	(Seni Sintki

Es besteht eine Andeutung, daß im Intervall zwischen den galaktischen Langen 80° und 250° die Intensitaten durchschnittlich schwacher sind als in der gegenüberliegenden Hemisphare

Struve bemerkt, daß bei zusammengehörenden Doppelsteinkomponenten die Linien mit derselben Intensitat auftreten, und auch daß die Variation mit

der scheinbaren Größe innerhalb physisch zusammengehörender Sterngruppen, die ja bei dem B-Typus allgomein and, aufhört. Für eine Milchstraßenregion in Cephens wurde die Beziehung der Kalzumabsorption zu einer absorbierenden Dunkelwolke, deren Entfernung Struvk auf Grund von Sternzählungen zu 350 Parsec schätzt, untersucht. Es stellt sich heraus, daß keine Spur einer direkten Verbindung zwischen den zwei Erscheinungen besteht, wenngleich die "Kalziumwolken" und die Dunkelwolken violleicht toilweise einander räumlich berühren und durchdringen

Das eben beschriebene empirische Material haben B P Gerasmovič und O Struve<sup>1</sup> von theoretischem Gesichtspunkte aus eingehend behandelt. Mit den von Gerasmovič (vgl. Zilf 19) angegebenen mittleren Parallaxen der Untertypen der Heliumsterne und unter plansiblen Annahmen über die Streuung in  $\log n$  für Sterne von derselben scheinbaren Größe berechnen die Verfasser den Absorptionskooffizienten der interstellaren K-Linie Im Falle der B3-Sterne wird für die wahrscheinliche Abweichung r in  $\log n$ , vom wahrscheinlichsten Wert  $\log n$ 0 gerechnet, nach Gerasmovič der Wert 0,094 angenommen, während im Falle B0 bis B2 für r alternativ mit den zwei Werten 0,32 und 0,16 gerechnet wird Pür den Absorptionskooffizienten  $\beta$ , per Parsec gerechnet, ergeben sich somit die Werte in Tabelle 19 Die Tabelle zeigt eine sehr gute Übereinstimmung

Tabelle 19	Mittloror				lūr	dio
	Interstella	ro K-Lin	a ber	Parsec.		

Mittiers enheinbers Grüße	<b>B</b> 0 — Ba		) jij	
	r = 0,32	r=0,16	r=0,094	
2,5	1,1 10-4	2,8 10-4	1,3 10-4	
3,5 4,5	1,1	2,8	3,0	
4,5	1.7	4,2 5,0	3,6	
5,5	2,0	5,0	4,2	
6,5	1,6	4,0	4,4	
7.5	1,6	4,0	4.1	
8,5	1,4	4,0 3,5	3,6	
9,5	1.3	3,2	2,9	
10,5	1,3 - 10-4	3,2 · 10-4	3.7 • 10-4	
Mittol	1,4 10-4	3,6 10-4	3,4 • 10-	

der  $\beta$ -Worte für die verschiedenen scheinbaren Größen einerseits und für die B0- bis B2-Sterne (r=0.16) und die B3-Sterne andererseits. Man schließt aus diesen Resultaten, daß  $\beta$  bis zur Grenze der Boobachtungen konstant ist. Im Mittel ergibt sich  $\beta=3.4\cdot 10^{-4}$  oder per ein gerechnet,

Die Theorie für die Absorption in der K-Linie gibt, wenn der Einsteinsche Koeffizient  $A_{\rm RI}$  nach Millers Resultat für die Kalziumehromosphäre angenommen wird, die Anzahl  $N^+$  der einmal ionisierten Kalziumatome per cm³ in ihrer Beziehung zur totalen Absorption in der Linie. Für die letztere Größe wird gesetzt  $\beta\Delta\lambda$ , wo  $\Delta\lambda$  die Breite der Linie, etwa 0,3 A, ist. Wenn die Masse des Kalziumatoms in Rochnung gezogen wird, ergibt sich dann für die Dichte des einmal ionisierten Kalziums der Wert

Mit einer Strahlungstemperatur  $T=15300^\circ$  und einem "factor of dilution"  $W=2.2\cdot 10^{-17}$  ergibt die Ionisationstheorie, daß der weit überwiegende Teil

<sup>1</sup> Ap J 69, S 7 (1929)

dei Kalzumatome im zweisach ionisierten Zustande (Ca<sup>++</sup>) sein miß. Die totale Dichte des interstellaren Mediums ist naturlich außerdem dadurch hestimmt, in welcher Proportion das Kalzum überhaupt im Medium vorhanden ist Gerasimovič und Struve rechnen hier mit zwei alternativen Annahmen Erstens wird die partielle Konzentiation  $\phi$  der Kalzumatome gleich 1, zweitensgleich dem entsprechenden Wert für die Erdkruste, 1,5–10<sup>-2</sup>, augenommen In den zwei Fallen ergibt sich für die Totaldichte

Werte, die sicher als extreme angesehen werden konnen. Da die interstellaren Wolken wahrscheinlich durch einen standigen Ausführ von Atomen aus den Sternatmospharen durch die Wirkung eines selektiven Strahlungsdruckes bedingt sind, so ist die Konzentiation des Kalziums wahrscheinlich großer als in der Erdrinde

Da nur dei Bruchteil  $10^{-11}$  von den Kalziumatomen im neutralen Zustande ist, so konnen wir gewiß nicht ein meikbares Auftreten der Linien des neutralen Kalziums in den Sternspektren erwarten. Außer den Linien H und K des (al-Atoms sollte aber auch die infraiote Doppellinie sichtbar sein. Von besonderem Interesse sind die Prinzipallinien vom Typus  $1\sigma-1\delta$ , die vom Korrespondenzprinzip "verboten" sind. Diese Übergange sollten die zwei Linien im Rot  $\lambda$  7293,43 A und  $\lambda$  7325,91 A geben

Y ÖHMAN¹ hat die Moglichkeit für das Auftreten der Ca¹-Limen im Ermission im Spektrum des Nachthimmels diskutiert. Er kommt zu dem Schluß, daß die H- und K-Limen kaum zu erwarten sind, daß aber gewisse Möglichkeiten für die eben erwahnten "verbotenen" Limen bestehen. Er betont, daß uns eventuelle Emissionslimen des interstellaren Kalziums Auskunft über die Dichte des Stratums und über die Dimensionen des Milchstraßensystems geben konnten

Gerasimovič und Struve diskutieren auch das interstellare Naturum, für welches jedoch gegenwartig weit weniger Beobachtungsmaterial vorliegt. Sie gehen schließlich zu einer Diskussion der mittleren Radialgeschwindigkeiten des Kalziums für sukzessive Intervalle in galaktischer Lange über. Die Doppelwelle der Oortschen differentiellen Rotation der zentralen Milchstraßenschricht ist hier besonders deutlich ausgepragt. Eine Auflösung nach der Formel

$$K + rA \sin 2(L - 325^\circ) = \bar{\varrho},$$

wo  $\bar{\varrho}$  die mittlere Radialgeschwindigkeit für die Lange L ist, gibt

$$rA = +5.3 \text{ km/sec} \pm 1.0 \text{ (w F)},$$
  
 $K = -0.6 \text{ km/sec} \pm 0.7 \text{ (w F)}$ 

Eine weitere Diskussion der diesbezuglichen Fragen wild in Ziff 31 folgen Zuletzt sei hier noch erwähnt, daß O Struve im Verdunkelungsveranderlichen U Ophiuchi vom Typus B8 (nach Struve etwa B5) nahe dem Zeitpunkt dei maximalen Trennung der stellaren K-Linien zwischen diesen Linien die interstellare K-Linie beobachtet hat Dei Stern zeigt auch interstellare Natitumlinien Diese geben in gutei Übereinstimmung mit der erwähnten K-Linie eine Radialgeschwindigkeit von —21 km/sec Nach Abzug dei parallaktischen Bewegung gibt dies für die Restgeschwindigkeit der interstellaren Linien —3,5 km/sec Die Erklarung des Verschwindens der interstellaren K-Linie für Typen später als B3 durch ein Überdecken der interstellaren Linie durch die stellare oder wenigstens durch eine in gewohnlichen Fällen zu nahe Nachbarschaft der bewenigstens durch eine in gewohnlichen Fällen zu nahe Nachbarschaft der be-

<sup>&</sup>lt;sup>1</sup> Nature, Aug 3 (1929) <sup>2</sup> Ap J 72, S 199 (1930)

treffenden Linien im Spektrum gewinnt durch STRUVES Beobachtung sehr an Wahrscheinlichkeit.

Nach Gerasimovič und Struve ist das interstellare Gas in seiner Gesamtmasse von nur geringer dynamischer Bedeutung. Die Totalmasse kann kaum <sup>1</sup>/<sub>100</sub> der totalen Masse der Sterne betragen, und der Widerstandseffekt auf die Bewegungen der Sterne in ihren Bahnen muß verschwindend sein.

Andererseits ergibt sich die interstellare Materie als mögliche Quelle der harten kosmischen Strahlung. Wenn diese nach Millikans Hypothese aus einer Transmutation von H in He herrührt, wäre mit der gegebenen Energiedichte der kosmischen Strahlung, 4·10<sup>-16</sup> erg/cm³, eine Transmutation eines gewissen Atomes einmal während 10<sup>88</sup> Jahren zu erwarten. Das interstellare Gas ist aber als für die kosmische Strahlung fast vollkommen durchsichtig zu betrachten. Die monochromatische Absorption und eine Absorption für kurze Wellenlängen außerhalb der Seriengrenze ausgenommen, besteht die Durchsichtigkeit für alle Wellenlängen. Ein eventueller Zusammenhang mit dem absorbierenden Medium in der zeutralen Milchstraßenzone kann daher wenigstens kein direkter sein.

## g) Die Dynamik der Milchstraße.

26. Milchstraße und Gastheorie. Rotation der Milchstraße. Lord Kelvin und H. Poincaré<sup>1</sup> haben auf die Analogie zwischen den Sternen in der Milchstraße und den Molekeln eines Gases hingewiesen. Wenn wir das Gesamtsystem der Milchstraße ins Auge fassen, können wir die Sterne als eine große Menge materieller Punkte betrachten, die einander nach dem Newtonschen Gesetze anziehen und die gegeneinander in jedem Augenblicke translatorische Bewegungen in allerlei Richtungen haben. Bei starken Annäherungen zwischen zwei Sternen werden die Bahnen nach den Gesetzen der hyperbolischen Bewegung geknickt. Die Repulsionskraft zwischen Gasmolekeln, die sehr schnell mit dem Abstande zwischen den Molekeln abnimmt, wird also hier durch eine NEWTONsche Attraktion ersetzt, die für ein einzelnes Sternpaar mit wachsender Entfernung unmerkbar wird. Wir haben also eine ziemlich bestechende Analogie. Das "Sterngas" der Milchstraße muß aber als extrem verdünnt angesehen werden. Wenn wir den Aktionsradius eines Sterns so groß annehmen, daß ein Vortibergang eines anderen Sternes in dieser Entfernung eine Ablenkung der Bahnen von nur einem Bruchteil eines Grades verursacht, werden wir doch auf eine freie Weglänge geführt, die die wahrscheinlichen Dimensionen des Systems weit übertrifft.

Eine naheliegende Erklärung der augenscheinlich großen Abplattung des Sternsystems wäre, was wohl zuerst von J. Herschel ausgesprochen wurde, die, daß das System als Ganzes eine allgemeine Rotationsbewegung besitzt und daß die Abplattung aus dem Gleichgewicht der Zentrifugalkraft mit der Newtonschen Attraktionskraft folgt. Poincaré hat gezeigt, daß für ein kontinuierliches Medium der Dichte φ eine obere Grenze der Winkelgeschwindigkeit ω durch die Relation

 $\frac{\omega^2}{2\pi G\varrho} < 1$ 

gegeben ist, wo G die Gravitationskonstante bedeutet. Da im Sternsystem  $\varrho$  sehr klein ist, wird  $\omega$  auch sehr klein, und die minimale Rotationszeit T lang, von der Größenordnung 10<sup>7</sup> Jahre. (Diese Schätzung nach einem neueren Wert von  $\varrho$  ergibt eine beträchtlich kleinere Grenze von T als Poincarés Wert von  $5 \cdot 10^8$  Jahren.)

<sup>8</sup> B A 2, S. 109 (1885).

Leçons sur les hypothèses cosmogoniques, S. 257. Paris 1911.

Da das astronomische Koordinatensystem ein Inertialsystem ist und die Lagebestimmungen, wie C V L CHARLIER hervorhebt, auf die invariable Ebene des Planetensystems ubergeführt werden können, so wäre es möglich, in den Eigenbewegungen der Sterne einen solchen Rotationseffekt zu finden Unter den ersten Versuchen, in den Eigenbewegungen einen Rotationseffekt aufzuspuren, ist voi allem derjenige von II GYLDÉN in einer unten (Ziff 31) naher besprochenen Arbeit aus dem Jahre 1871 zu nennen Andere Untersuchungen ruhren von E Schonfeld<sup>1</sup>, F Bolte<sup>2</sup> und F RANCKEN<sup>3</sup> her L Struvi L führte Rotationsterme in die Gleichungen zur Bestimmung der Prazessionskonstante ein Charlier scheint der erste zu sein, der einen ziemlich zuverlassigen Wert hergeleitet hat Die letzte von ihm ausgeführte Bestimmungs gibt eine mittlere Eigenbewegung in galaktischei Lange von -0",0024, pio Jahi gerechnet Charlier macht die Bemerkung, daß eine retrograde Prazession der invariablen Ebene infolge einer dynamischen Einwirkung des umgebenden Sternsystems auf unser Planetensystem diesen Weit bedeutend erhöhen kann Wir werden unten auf andere Bestimmungen eingehen und dabei auch bemeiken, daß die mittlere Bewegung in galaktischer Lange (mit B bezeichnet) durch einen anderen Rotationseffekt, der auf einer in der Milchstraßenebene mit dem Abstande vom Zentrum varuerenden Winkelgeschwindigkeit bezuht, wahrscheinlich vermindert wird und also nicht unmittelbai dei Winkelgeschwindigkeit m entspricht

Eine Rotationsbewegung wurde weiter mit negativem Zeichen in die durch Anschluß an umgebende Sterne bestimmten Eigenbewegungen der "anagalaktischen" Nebel eingehen, wenn diese, was gegenwaitig als gesichert angeschen werden kann, außerhalb des Sternsystems gelegen sind Diesen Weg hat kurzlich K Lundmark eingeschlagen Die Resultate geben wenigstens eine Andeutung von einem Effekt der oben genannten Ait, abei das Material ist noch nicht für eine sichere Bestimmung hinreichend Es gilt aber auch hier, daß nicht unmittelbar die Winkelgeschwindigkeit  $\omega$ , sondern die Größe B gemessen wird

27. Allgemeine statistische Mechanik des Sternsystems. Grund der Analogie zwischen Sterndynamik und Gastheorie aus der letzteren Konsequenzen fur die ersteie zu ziehen, können wir von vornheiem die Eigenschaften der Steine als Massenpunkte einführen und eine statistische Mechanik auf Grund des Newtonschen Gesetzes aufbauen Un begegnen hier sogleich einer großen Verschiedenheit zwischen Stern- und Gasdynamik In dem Steinsystem ist namlich die das System zusammenhaltende "reguldre" Kraft nur eine Summe derjenigen Krafte, die auch als Passage- oder Stoßkrafte auftieten, wenn die Sterne einander paarweise gegenubergestellt werden. Es läßt sich also nicht ohne weiteres um einen Stern ein Stoßbereich, der klein ist gegen die mittleie Distanz zwischen den Sternen und außerhalb dessen die Passagekräfte ignorieit werden konnen, absondern Mit wachsender Entfernung vom betrachteten Stein aus haben wir es aber mit einem mehr und mehr komplizierten Zustand vielfacher Passagen zu tun, und die Passagekrafte gehen allmahlich durch Summierung ın die regularen Krafte uber Wir konnen daher mehr oder weniger willkinlich eine obere Grenze fur die Distanz der Passagen fixieien und nur den Einfluß der individuellen Vorubergänge innerhalb einer gewissen Sphare in Rechnung

ordinem (1927), Upsala Medd 30

<sup>&</sup>lt;sup>1</sup> V J S 17, S 255 (1882) <sup>2</sup> Diss Bonn (1883) <sup>3</sup> A N 104, S 149 (1883), auch Diss Helsingfors

Mémoires de l'Academie Impériale de St Pétersbourg (VII) 35, Nr 3 (1887)

The Motion and the Distribution of the Stars Mem Univ Calif 7, S 32 (1926) 6 Studies of Anagalactic Nebulae, S 38 Nova Acta Reg Soc Sc Upsala, Volumen extra

ziehen. Die Kräfte der außerhalb dieser Sphäre gelegenen Massen werden dann

in eine reguläre Kräfteresultante zusammengesetzt.

J H JEANS<sup>1</sup> hat besonders den Einfinß der nahen Passagen auf die reguläre Bahn eines Sterns untersucht. Wenn wir mit  $\sigma$  den kleinsten Abstand zwischen zwei Sternen von den Massen M und M' bei einem Vorübergang, dem eine kleine Defiektion  $\psi$  der relativen Bahn entspricht, bezeichnen, so haben wir

$$\sigma = \frac{2G(M+M')}{wv^4},$$

wo v die relative Geschwindigkeit ist. Nehmen wir  $\psi=1^\circ$  und mit Jeans  $M+M'=6,8\cdot 10^{10}$  g (= 3.4 Sonnenmassen),  $v=4\cdot 10^6$  cm/sec (40 km/sec), so finden wir  $\sigma=3,2\cdot 10^{10}$  cm, einen Wert, der ungefähr siebenmal größer als der Durchmesser der Noptunbahn ist. Die mittlere Zeit t swischen Passagen in Distanzen  $\leq \sigma$  kann aus der gasthooretischen Formel  $t=\frac{1}{\pi r \sigma^2 v}$  berechnet werden, wo v die Anzahl Sterns pro Volumensinheit ist. Die mittlere Zeit zwischen den Passagen wird von der Größenordnung  $t^{0.1}$  Jahre. Für Kollisionen innerhalb einer Distanz gleich dem Radius der Noptunbahn ergibt sich die mittlere Zwischenzeit zu  $t^{0.10}$  Jahre. Während sehr langer Zeiten können wir daher die sehr nahen Passagen ignorieren.

Für den kumulativen Effekt der Passagon zwischen den Distanzen  $\sigma_1$  und  $\sigma_2$ 

während der Zeit i leitet JRANS die Formal ab

$$\sigma_n^0 = i \cdot \frac{6\pi r G^0 M^{\prime 0}}{\overline{\sigma}} \log \frac{\sigma_0}{\sigma_1} , \qquad (1)$$

wo  $v_s$  die gugen die ursprüngliche Bewegungsrichtung senkrechte Geschwindigkeitskomponente eines Sterns ist. Wenn wir für  $\sigma_1$  den obigen Wert von  $\sigma$  für  $\varphi = 1^\circ$  annehmen und nur die Passagen ziemlich nahellegender Sterne, innerhalb 20 Parsec, berücksichtigen, bekommen wir

$$v_n = \frac{1}{4}\sqrt{\ell}, \tag{2}$$

also ome transversale Goschwindigkeitserhöhung von ½ cm/sec in einem Jahre und 1 km/sec nach 40000 Millionen Jahre. In dieser Weise hat JEANS bewiesen, daß der Einfluß der Passagen nahellegender Sterne in der ersten Approximation zu vernachlässigen ist, und daß die Sterndynamik in erster Linie das Problem

der Bowegung unter den regulären Kräften des Systems enthält.

CHARLIER<sup>2</sup> hat nach dem Vorbild der kinetischen Gastheorie eine statistische Mechanik auf Grund des Newtonschen Gesetzes entwickelt. Die Anzahl Storne innerhalb des Volumenslementes dzdyds um den Punkt z, y, s herum, welche Geschwindigkeitskomponenten innerhalb dududw um den Punkt u, v, w im Geschwindigkeitsraume herum haben, sei mit /(z, y, s, u, v, w, t) bezeichnet. Die fundamentale Differentialgleichung der Vertellungsfunktion kann man in der Boltzmannschen Form

$$\frac{\partial f}{\partial t} + u \frac{\partial f}{\partial w} + v \frac{\partial f}{\partial u} + w \frac{\partial f}{\partial u} + X \frac{\partial f}{\partial u} + Y \frac{\partial f}{\partial v} + Z \frac{\partial f}{\partial w} = V(f) + \Box (f)$$
 (3)

ausdrücken, wo X, Y, Z die Komponenten der regulären Kraft im Punkte x, y, s eind. P(f) ist die "Passagefunktion" und [](f) die "Koilisionsfunktion" P(f) wird wie in der kinetischen Gastheorie gomäß der Dynamik der Passagen als ein mehrfaches Integral ausgedrückt Die Funktion [](f), die wirklichen Zusammenstößen der Sterne Rechnung trägt, wird im Hauptteil der Charlierschen Arbeit

<sup>2</sup> Lund Modd Sor II, 16 (1917).

<sup>1</sup> Problems of Cosmogony and Stellar Dynamics, S. 224. Cambridge 1919

weggelassen, da sie wahrend absebbaiei Zeitiaume keine Rolle spielt. Charlii R entwickelt die Funktion / in eine Frequenzfunktion vom Typus A und leitet aus der Bolizmannschen Gleichung für die Koeffizienten Differentialgleichungen ab Fur die obere Grenze der Distanz, innerhalb welcher eine Passage gerechnet wird, nimmt Charlier die halbe mittlere Entfernung zwischen den Steinen

unserer Umgebung an

Aus den Differentialgleichungen der Koeffizienten zweiter Ordnung leitet Charlier ab, daß eine ursprunglich ellipsoidische Verteilung der Geschwindigkeiten u, v, w mit der Zeit nach Gleichheit der Dispersion in verschiedenen Richtungen strebt. Die Zeit, in der ein Überschuß des Quadrates der Dispersion in einer Richtung auf 1/e seines Betrages reduziert wird, die "Relaxationszeit", wird von Charlier zu 3,6 10<sup>16</sup> Jahren geschatzt. Die Langsamkeit der Wirkung der Steinpassagen ist also hier bestatigt worden

C F LUNDAIL hat CHARLIERS Ausemandersetzungen unter spezieller Be-

rucksichtigung der Kollisionsfunktion fortgesetzt

Da offenbar  $\Gamma(f)$  und  $\Gamma(f)$  nur eine sehr langsame Veranderung der Prequenzfunktion / herbeifuhren konnen, mussen wir zuerst in der Bolizmannschen Gleichung Passagefunktion und Kollisionsfunktion außer acht lassen und den Bewegungszustand des Systems unter der alleinigen Wirkung der regularen Systemkrafte X, Y, Z studieren Wir haben also

$$\frac{\partial f}{\partial t} + u \frac{\partial f}{\partial v} + v \frac{\partial f}{\partial y} + u \frac{\partial f}{\partial z} + X \frac{\partial f}{\partial u} + Y \frac{\partial f}{\partial v} + Z \frac{\partial f}{\partial w} = 0 \tag{4}$$

$$X = \frac{du}{dt}, \quad Y = \frac{dv}{dt}, \quad Z = \frac{dw}{dt}$$
 (5)

$$\varrho = \iiint_{-\infty}^{+\infty} m / du \, dv \, dw \,. \tag{6}$$

Diffuse gasformige Materie im Raume denken wir uns übei die Partikeln verteilt und in m eingerechnet. Wenn wir die Verteilung von  $\varrho$  nach  $\lambda$ ,  $\gamma$ , z für einen gewissen Augenblick festhalten, so können wir gemaß dieser Dichtigkeitsverteilung und gemaß den augenblicklichen Lagen und Geschwindigkeiten der Partikeln ihre Bahnen im sechsdimensionalen Raume berechnen. Das Gravitationspotential V wird nach Poissons Gleichung bestimmt

$$\frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} + \frac{\partial^2 V}{\partial z^2} = -4\pi G\varrho \tag{7}$$

In der wirklichen Bewegung wird aber im allgemeinen Falle die Dichtefunktion  $\varrho$  stetig modifiziert, wir wollen sagen durch eine Funktion  $\Delta\varrho$ , welche von den Koordinaten x, y, z und der Zeit  $\Delta t$  abhangt. Wenn wir eine kontinuierliche Variation der Dichtigkeit  $\varrho$  und der mittleien Geschwindigkeiten u, v, wmit x, y, z voraussetzen, so kann gemaß der Kontinuitatsgleichung

$$\frac{\partial \varrho}{\partial t} + \frac{\partial (\varrho \, \overline{u})}{\partial x} + \frac{\partial (\varrho \, \overline{v})}{\partial y} + \frac{\partial (\varrho \, \overline{w})}{\partial z} = 0 \tag{8}$$

<sup>&</sup>lt;sup>1</sup> Lund Medd Ser II, 45 (1926)

 $\partial \varrho/\partial t$  nie ins Unendliche wachsen. Wenn wir demgemäß während des Zeitelements  $\Delta t$  erster Ordnung das Integral  $\int \int |\Delta \varrho| dx dy dz$ , über das ganze System erstreckt, als eine kleine Größe von der ersten oder von höherer Ordnung betrachten, so erscheinen "Störungskräfte" erster oder höherer Ordnung mit Komponenten von der Form  $\int \int \frac{\Delta \varrho}{r^2} x dx dy dz$ , wo r die Distanz von dem betrachteten Ort (Origo) bis zum Punkte x, y, z ist. In der Bewegung einer Partikel während des Zeitelements  $\Delta t$  erleiden daher die Geschwindigkeitskomponenten u, v, w "Störungen"  $\Delta u$ ,  $\Delta v$ ,  $\Delta v$  zweiter oder höherer Ordnung, während jedoch die entsprechenden  $\Delta x, \Delta y, \Delta z$  von höherer Ordnung als der zweiten sind. Für die Berechnung der Dichtigkeitsverteilung nach einem kleinen Zeitintervall  $\Delta t$  von dem betrachteten Zeitpunkt an können wir daher bis auf Größen höherer Ordnung als der zweiten die wahre Bewegung der Partikeln durch die Bewegung in den augenblicklichen sechsdimensionalen Bahnen ersetzen. Wir können diese Bahnen auch als Stromlinien in der sechsdimensionalen Mannigfaltigkeit bezeichnen.

Wenn wir aber auf die Verhältnisse für längere Zeiten Rücksicht nehmen, werden infolge der Veränderungen des Kraftfeldes die Partikeln längs einer gewissen augenblicklichen Bahn über eine Serie verschiedener, mehr oder weniger benachbarter Bahnen eines späteren Zeitmoments gestreut. Dieser Umstand, wie auch die verschiedenen angulären Geschwindigkeiten in den Bahnen um den Schwerpunkt herum bewirken eine fortschreitende Mischung der Materie des Systems und eine stetige Ausgleichung der Frequenz zwischen einander benachbarten sechsdimensionalen Bahnen.

Wir nehmen jetzt an, daß eine weitgehende Mischung und Ausgleichung in der Materie des Systems stattgefunden hat. Wir teilen die Materie in eine Unzahl von augenblicklichen, sechsdimensionalen Bahnen, jede Bahn mit einer gewissen mittleren Dichtigkeit /, auf und setzen infolge der Mischung eine im wesentlichen regellose Verteilung der Partikeln längs einer Bahn voraus. Da die räumliche Dichtigkeit  $\varrho$  aus einer Integration in u,v,w bestimmt wird, also aus einer Summierung über unendlich viele Bahnen, die den betrachteten Punkt durchkreuzen, so ist sie also, von kleinen Schwankungen abgesehen, als wahrscheinlich von der Zeit unabhängig zu betrachten. Die sechsdimensionalen Partikelbahnen werden dann stationär, und da wir die Verteilung in diesen Bahnen als regellos betrachten, so ist die a priori zu erwartende Frequenz / in einer solchen Bahn als von der Zeit unabhängig anzusehen, was mit der Gleichung

$$\frac{\partial f}{\partial t} = 0, \tag{9}$$

oder der daraus gemäß der Gleichung (4) folgenden

$$\frac{\partial f}{\partial w}dx + \frac{\partial f}{\partial v}dy + \frac{\partial f}{\partial z}dz + \frac{\partial f}{\partial u}du + \frac{\partial f}{\partial v}dv + \frac{\partial f}{\partial w}dw = 0$$
 (10)

äquivalent ist. Dieses Resultat stimmt mit einem Satz von Poincant überein, nach welchem in einem stationären Zustande die Dichtigkeit der Partikeln im generalisierten Raume der kanonischen Variabeln  $q_1, q_2, \ldots, q_n, p_1, p_2, \ldots, p_n$  längs der Bahn einer Partikel in diesem Raume konstant ist. Wenn die Bewegungsgleichungen k erste Integrale

$$I_1 = \text{konst.}, \quad I_2 = \text{konst.}, \quad \dots, \quad I_k = \text{konst.}$$
 (11)

haben, so kann die Verteilungsfunktion

$$f(I_1, I_2, \ldots, I_k) \tag{12}$$

<sup>&</sup>lt;sup>1</sup> Leçons sur les hypothèses cosmogoniques, S. 100 (1911).

geschrieben werden, vorausgesetzt, daß die Bahn einer Partikel das Gebiet von 2n-k Dimensionen, welches durch die Gleichungen (11) definiert wird, ausfullt.

Im aktuellen Falle betrachten wir jetzt sowohl die Lagen als die Geschwindigkeiten in bezug auf den Schweipunkt des Systems Fui eine allgemeine Dichtigkeitsverteilung haben wir nur ein eistes Integral, das Energieintegral

$$I_1 = u^2 + v^2 + w^2 - 2V = \text{konst}$$
 (13)

Eine Verteilung  $f(I_1)$  wird aber ein endliches Rotationsmoment der Masse ausschließen

Fur einen stationalen Zustand bei endlichem Rotationsmoment muß daher eine rotationssymmetrische Veilteilung um eine gegen die fundamentale Rotationsachse senkrechte Achse volausgesetzt werden. Die Frequenzfunktion kann dann geschileben weiden

 $/(I_1, I_2), \tag{14}$ 

wo

$$I_2 = vv - uy, \tag{15}$$

wenn die  $\iota y$ -Ebene die Ebene maximaler Flachengeschwindigkeit des Systems ist. In dieser Form ist Poincarés Theorem speziell von Jeans¹ und von Charlier² aufgenommen und diskutiert worden. Die Existenz eines Gleichgewichtszustandes, welcher durch eine gewählte Funktion  $f(I_1, I_2)$  bestimmt wird, unterliegt naturlich der Bedingung, daß Poissons Gleichung Genuge geleistet wird, d. h. daß V gemäß einer aus (14), (6) und (7) resultierenden Gleichung  $\Delta V = \Psi(V, R)$  bestimmt werden kann, wo  $R^2 = v^2 + y^2$ 

In dem eben zitiei ten Werke hat Poincaré auch das wichtige Theorem von Jacobi, welches im Virialtheorem von Clausius enthalten ist, in die theoretische Behandlung der astronomischen Partikelsysteme eingeführt. Eine Anwendung dieses Theorems auf den Bewegungszustand in Sternhaufen ist spater von Eddingfon<sup>8</sup> gemacht worden. Wenn J das Tragheitsmoment in bezug auf den Koordmatenanfangspunkt, T die kinetische und W die potentielle Energie (W = 0 für unendliche Verdunnung des Systems) ist, so haben wir

$$\frac{1}{2}\frac{d^2f}{dt^2} = 2T + W \tag{16}$$

Im stationaren Zustande ist also

$$2T + W = 0 \tag{17}$$

Jeans<sup>4</sup> hat dieses Theorem auf die Frage nach dem Ursprung des galaktischen Systems angewandt. Konnen wir uns z. B. denken, daß unser System aus einem Zusammenfließen von einzelnen kleineren Sternhaufen entstanden ist? Weim  $T_1$  und  $W_1$  die kinetische und die potentielle Energie eines einzelnen Haufens von dem Zusammenstoß mit anderen Haufen,  $U_1$  die Translationsenergie des Haufens in bezug auf den gemeinsamen Schweipunkt aller Haufen,  $T_0$  und  $W_0$  die kinetische und die potentielle Energie des resultierenden Systems sind, so gilt  $T_0 + W_0 = \sum (T_1 + W_1 + U_1)$ 

Wenn jeder Haufen vor dem Zusammenstoß in einem stationaren Zustand sich befunden hat, so haben wir außerdem

$$2T_1 + W_1 = 0$$

und auch, sobald das große System stationar wird,

$$2T_0 + W_0 = 0$$

<sup>&</sup>lt;sup>1</sup> M N 76, S 70 (1915) 
<sup>2</sup> Lund Medd Ser I, 82 (1917) 
<sup>3</sup> M N 76, S 525 (1916) 
<sup>4</sup> M N 82, S 138 (1922), Astronomy and Cosmogony, S 377 (1929)

Man bekommt nach diesen Voraussetzungen sofort

$$W_0 = \sum W_1 + 2 \sum U_1 \tag{18}$$

Die Translationsenergie der Haufen wird also in potentielle Energie verwandelt, und in der Regel muß also eine gewaltige Expansion auf ein Zusammenfließen von der genannten Art folgen Die große Ausdehnung des galaktischen Systems steht also durchaus nicht in Widerspruch zu einem eventuellen Ursprung in einer Kombination einer Anzahl viel kleinerer Systome, die sich allmählich durch gegenseitige Einwirkungen auflösen

Eine aussührliche geschichtliche Übersicht der hier behandeiten Probleme und eine Weiterführung der Theorie des stationaren Zustandes hat J. Ohlsson<sup>1</sup> gegoben In Analogie mit einem Resultat der Ohlssonschen Arbeit beweist U WEGNER durch eine exakte Lösung der Boltzmannschen Gleichung für den Fall einer zweidimensionalen achsensymmetrischen Verteilungsfunktion von CHARLIERS Typus A, daß diese Funktion sich notwendig auf die MAXWELLsche Form C . o2 V-w- reduziert

28. Theorie der Sternströmung im typischen Sternsystem. Die kapitale Entdeckung von Kapteyn, daß die pekullaren Bewegungen der Sterne nicht regellos verteilt sind, sondern eine gewase Richtung im Raume bevorzugen, die sehr nahe in der Milchstraßenebene gelegen ist, weckte die Hoffnung, dieses Phanomen als eine Eigenschaft eines stationaren Zustandes deuten zu konnen. um damit über den Aufban des Milchstraßensystems wichtige Schlüsse zu siehen Die erste Deutung des Phanomens im Sinne der Kapteynschen Zweistromtheorie sagt ja schon etwas in der Richtung einer dynamischen Erklärung aus, aber nichts zu der Frage, ob diese Bewegungsart eine stationäre Erscheinung an unserem Orte im System sein kann. H H. TURNER® stellte die Hypothese auf, daß die Sternströmung der ein- und ausgehenden Bewegung in Bahnen, die mit großer Exzentrizität um den Schwerpunkt des Systems verlaufen, ontsprochen könne Da der Vertex der Sternströmung ungefähr in der galaktischen Länge 340° llegt, also in der Gogend der hellsten Milchstraßenwolken, hatte diese Hypothese an sich eine nicht unerhebliche Wahrscheinlichkeit, würde aber eine sehr erhebliche zantrale Kondonsation der Materie voraussetzen. Nach einer strengen Theorie gemäß den oben (Ziff. 27) gegebenen Aussinandersetzungen ist weiter in einem abgeplatteten System nur dine gegon den Radiusvector transversale Sternströmung möglich (vgl unten JEANS) und kann eine radiale stationare Sternströmung nur in Systemen von sphärischer Massenverteilung vonkommen

Daß bel sphärischer Symmetrie eine radiale, überall ellipsoidische Sternströmung möglich ist, wurde suerst von Endington nachgewiesen. Die außerdem einzige Möglichkeit einer überall strong ellipsoldischen Geschwindigkeitsverteilung (and zwar in einer nahe radialen Richtung) besteht nach Eddington für ein abgeplattetes System, wenn das System ein Untersystem ist und die Gravitationskraft von einer vorherrschenden aphärischen Masse konstanter Dichte bestimmt wird

Die Hypothese einer radialen Sternströmung wurde später praktisch außerhalb der Diskussion gelassen. JRANS suchte die Frequenzfunktion im stationären rotationssymmetrischen Zustande auf die Behandlung des Problems anzuwenden In diesem Falle ist die Frequenzfunktion in der Form  $f(I_1, I_2)$  zu schreiben, wo  $I_1$  das Energieintegral und  $I_2$  das Plächenintegral für die Symmetriechene ist. Jeans führt zylindrische Koordinaten R,  $\theta$ , s ein, wobel die ontsprechenden

Lund Medd Ser II, Nr 48 (1927)
 MN 72, S 387 (1912).
 MN 75, S 366 (1915).
 MN 76, S 37 (1915); Obs 41, S 132 (1918) \* Zf Phys 45, 8 539 (1927).

hnearen Geschwindigkeiten mit  $\Pi$ ,  $\Theta$ , Z bezeichnet werden. Das Flachenintegral ist dann  $R\Theta$ , und die Frequenzfunktion schreibt sich

$$f(II^2 + \Theta^2 + Z^2 - 2V, R\Theta) \tag{19}$$

Die Geschwindigkeitsverteilung ist somit symmetrisch in H und Z, eine preferentielle Strömung ist nur in  $\Theta$  möglich, also in der Richtung senkt er litzum Radiusvector. Aus diesem Umstand schloß Jeans zuerst, daß die Sternströmung nicht als eine stetige Bewegung im Steinsystem gedeutet werden kann.

Charler wies abei auf die Tatsache hin, daß die Hehumsteine in unseier Nahe um ein Zentrum in der galaktischen Lange 240° herum verteilt sind und daß die Richtung gegen dieses Zentrum nahezu senkrecht gegen die Vertextichtung der Sternströmung ist. Da weiter die stellarstatistisch gefunderen Geschwindigkeitsellipsoide nahezu eine verlangerte, rotationssymmetrische Form haben, wird auch sehr nahe die Bedingung erfullt, daß im stationären Zustande die Verteilung in den Komponenten II und Z rotationssymmetrisch um die O-Komponente sein soll, wenn wir eine stationare Bewegung um den Zentralpunkt der Hehumsterne annehmen. Diese Theorie kann mit der Anschauung eing versungen werden, nach der die Heliumsteine den Kein eines "lokalen Systems", einer Sternwolke innerhalb des größeren Milchstraßensystems, bilden. Eine obenerwahnte Arbeit von Eddington zeigt jedoch, daß die Geschwindigkeits verteilung bei transversaler Sternströmung micht überall im System streng ellipsoidisch sein kann.

Auf einem ganz anderen Wege hat Kapteyn' einen großartigen Versuch gemacht, eine Dynamik des Sternsystems zu begrunden. Ei ging dabei von der empirisch gegebenen Sternverteilung im typischen Sternsystem aus, berechnete unter einigen vereinfachenden Annahmen die Gravitationskraft (zunächst in einer willkurlichen Einheit) in verschiedenen Punkten des Systems und suchte dann die empirischen Ergebnisse der Geschwindigkeitsverteilung in diesen Rahmen hmemzupassen Fur die Abhangigkeit der Dichte von der Höhe über der galak tischen Ebene und die barometrische Gleichung angewandt; es eight sich daber, daß die mittlere Masse der Sterne, die den Absolutwert der Gravitationskraft bestimmt, von 2,2 Sonnenmassen in unserer Nahe auf 1,4 fur die außerste herucksichtigte Dichtigkeitsschale abnummt. Für das Gleichgewicht in der galaktischen Ebene ist eine Rotationsbewegung notwendig, die für größere Distanzen nahezu konstant und gleich 19,5 km/sec wird. Die Steinströmung wird durch zwei einander entgegengesetzte Rotationsbewegungen eikläit, die also eine relative Geschwindigkeit von rund 40 km/sec, in Übereinstimmung mit dem emphisch gefundenen Wert, gibt Das Zentrum soll in einer gegen die Steinströmung senkrechten Richtung, in einem Abstande von ca 650 Paisce, gesucht werden

Die Kapteynschen Resultate veranlaßten Jeans² zu einen mathematisch sehr eleganten Behandlung des Problems Von det oben gegebenen Form det Frequenzfunktion im rotationssymmetrischen Falle ausgehend, bildet Jeans die quadratischen Momente der Geschwindigkeitskomponenten, d h die Mittelwerte  $\widehat{HO}$  nsw Wenn  $\nu$  die Anzahl Sterne pro Volumeneinheit bedeutet, eihält man

$$\nu \overline{IIO} = 0$$
,  $\nu \overline{IIZ} = 0$ ,  $\nu \overline{OZ} = 0$ ,  $\nu \overline{II}^2 = \nu \overline{Z}^2$ .

JEANS schreibt

$$\nu \overline{II^2} = \nu \overline{Z^2} = p \,, \qquad \nu \overline{\Theta^2} = q \tag{20}$$

<sup>&</sup>lt;sup>1</sup> Mt Wilson Contr 230 = Ap J 55, S 302 (1922)
<sup>2</sup> M N 82, S 122 (1922)

und zieht dann zur weiteren Behandlung des Problems die Gielchungen der Massenbewegung in einem System materieller Punkte heran, die unter Verwendung rechtwinkliger Koordinaten von der folgenden Form sind

$$\frac{d}{dt}(\nu\bar{u}) + \frac{\partial}{\partial w}(\nu\bar{w}) + \frac{\partial}{\partial y}(\nu\bar{w}) + \frac{\partial}{\partial z}(\nu\bar{w}) = \nu\frac{\partial V}{\partial w}.$$
 (21)

Im stationaren Zustande verschwindet der erste Term. Wichtig ist zu bemerken, daß in diesem Falle die Erftlllung der "Druckgleichungen" (21) die Folge einer Frequenzfunktion vom Typus (19) ist, wovon man sich durch Berechnung der linken Selte in (21) unter Voraussetzung einer Frequenz nach (19) überzeugt Wir bekommen nach Einführung zylindrischer Koordinaten

$$\frac{\partial p}{\partial s} = v \frac{\partial V}{\partial s}, 
\frac{\partial p}{\partial R} + \frac{p - q}{R} = v \frac{\partial V}{\partial R}.$$
(22)

Diese Gleichungen gelten für jeden einzelnen physikalisch definlerten Sterntypus für sich, nur ist V immer des Gravitationspotential, des von allen Sternen und aller dunklen Materie zusammengenommen herrührt

Wenn v und dann V, in einer von der mittleren Masse der Sterne abhängigen Einheit, als bekannte Größen angenommen worden, kann þ für einen Punkt des Systems aus

 $\dot{p} = -\int \nu \frac{\partial V}{\partial z} dz$ (23)

berechnet werden, wo die Integration vom betrachteten Punkt sich der s-Achse parallel bis in eine Region, wo r zu vernachlässigen ist, erstreckt.  $P = \overline{H^2} = \overline{Z^2}$ kann in dieser Welse für jeden Punkt des Systems in einer später zu bestimmenden Einheit berechnet werden. Dann ergibt sich aus der Gleichung die Größe  $\frac{p-q}{R}$ , woraus ?-P für jeden Punkt erhalten werden kann.

Wenn  $h_1$ ,  $h_2$  die Halbachsen des Geschwindigkeitsellipsoids sind, haben wir

$$\frac{M}{M} = \frac{\sum G^2}{\sum Z^2} = \frac{g}{b}. \tag{24}$$

In der Nähe der Sonne nimmt JEANS  $h_1/h_2 = 0,577$  an, und daraus folgt

$$\frac{q-p}{r} = 2,00 \cdot \frac{p}{r} \,. \tag{25}$$

Aus dieser Bedingung kann die Distanz R der Sonne von der Rotationsachse mit Hilfe einer berechneten Tabelle zusammengehöriger Werte von  $\frac{q-p}{r}$  und  $\frac{p}{r}$  bestimmt werden. JRANS findet R=1090 Parsec Der Wert von  $\frac{q-p}{r}$ in der angenommenen willkürlichen Einheit wird dementsprechend aus der Tabelle entnommen. Die Absolutworte von g/r und p/r sind aber durch die gegebenen Werte von h, und h, bestimmt, oder man hat, wenn man nach der Zweistromtheorie die Strömungsgeschwindigkeiten U' und U'' annimmt, wie leicht zu ersehen ist,

q = p = U'U''. (26)

Durch Vergleich der zwei Werte von 2-P erhält man den Wert der früher unbestimmten Einheit des Potentials V, und darans die mittlere Sternmasse. Diese ergibt sich zu 6,34 · 10<sup>38</sup> g oder 3,2 Sonnenmassen. Dieser Wert ist aber als derjenige Mittelwert der Masse anzusehen, der erhalten wird, wenn die ganze Masse des Systems auf die leuchtenden Sterne verteilt wird. Die dunkle und

neblige Materie ist also in diesem Mittelwert eingerechnet.

Da Kapteyns typisches System Rotationssymmetrie um die Sonne besitzt, die Sternströmungstheorie nach den soeben angewendeten Prinzipern aber eine exzentrische Stellung der Sonne fordert, muß dem Kapteynschen System eine gewisse Retusche gegeben werden, damit die obigen Auseinandersetzungen logisch miteinander vereinbar sind. Diese Retusche spielt dann eine gewisse Rolle für die Schätzung des Abstandes der Sonne von der Rotationsachse und auch für die Schätzung der mittleren Sternmasse. Jeans erhält in dieser Weise zuletzt

$$R = 700 \text{ Parsec}, M = 2.4 \text{ Sonnenmassen},$$

in offenbarer Übereinstimmung mit Kapteyns Werten.

Sehr interessant ist Jeans' Anwendung der Methode auf Charliers System der Heliumsterne. Er zeigt hier, daß die beobachtete Verteilung der Heliumsterne im Raume als notwendige Bedingung sehr kleine Geschwindigkeiten dieser Sterne voraussetzt. Die theoretischen Geschwindigkeiten Z und II im Zentrum sind von der Größenordnung 4 km/sec und die Sternströmung für eine Distanz von 90 Parsec (die Entfernung der Sonne) vom Zentrum ist nur 2,2 km/sec.

Es ist aber klar, daß die Ansichten von Charlier und von Kapteyn und Jeans, wenn auch miteinander verwandt, doch nicht zusammenfallen. Die oben geforderte Distanz von 700 Parsec vom Zentrum ist nicht mit dem Abstande des Zentrums im System der Heliumsterne vereinbar. Jeans nimmt daher an, daß Charliers System der B-Sterne den Charakter eines "moving cluster" hat.

Man kann aber wohl die Frage stellen, ob wirklich dem Kaptrynschen typischen System eine dynamische Realität zukommt. Die Zeugnisse der letzten Zeit deuten auf sehr erhebliche Abweichungen von der Rotationssymmetrie um die Sonne, die es sehr fraglich erscheinen lassen, ob dem typischen System eine wirkliche Annäherung an die wahre Sternverteilung im Raume zuzuschreiben ist. Besonders aber sind wir auf dem Gebiete der Sterngeschwindigkeiten auf neue Phänomene gekommen, die innerhalb des typischen Systems nicht genügend Raum finden. Man kann sich jetzt fragen, ob es möglich sei, die genannten Züge der Sternverteilung im Raume und der Geschwindigkeitsverteilung in irgendeine Theorie zusammenzufassen, die aber auch den vorher besprochenen empirischen Resultaten Genüge leistet.

29. Einheitliche Theorie des Milchstraßensystems. Wir haben schon vorher (Ziff. 26) hervorgehoben, daß die große Abplattung des Milchstraßengebildes als Ganzes wahrscheinlich auf eine Rotationsbewegung des großen Systems zurückgeführt werden kann. In der Theorie des typischen Systems wird aber die Abplattung des Systems nicht als Folge einer einheitlichen Rotationsbewegung, sondern durch eine in beiden Richtungen um das Zentrum herum vor sich gehende Bewegung oder Strömung erklärt. Da aber das typische Sternsystem offenbar nicht die ganze Struktur des Sternsystems darstellen kann, so könnte man sich einen Kompromiß derart denken, daß das typische Sternsystem wesentlich die Rolle eines lokalen Systems spielt, während das große System als ein System von Wolken oder lokalen Systemen einheitlich rotiert.

Man kann aber, wie oben gesagt, ernstlich in Frage stellen, ob wirklich dem typischen System irgendeine geschlossene Einheit, wenn auch nur als lokales System, zukommt. Zwei Phänomene, denen auf dieser Grundlage eine genügende Erklärung zu geben aussichtslos erscheint, sind die asymmetrische Verschiebung der Geschwindigkeitsellipsoide verschiedener Sterngruppen mit steigender Streu-

1.501 13. Chia

ung der Geschwindigkeiten (Bd. VI, Chap. 1, Ziff. 18) und die unten (Ziff. 30) besprochenen "differentiellen" Rotationseffekte in den mittleren Sternbewegungen. Die Tatsache, daß Gruppen von großer Streuung und großer asymmetrischer Verschiebung des Geschwindigkeitsmittelpunktes, welche offenbar nicht in einem lokalen System gebunden sein können, eine ellipsoidische Verteilung von ungefähr demselben Charakter wie für Gruppen kleinerer Streuung aufweisen, deutet auch an, daß der Grund der ellipsoidischen Verteilung oder der Kapteynschen Sternströmung nicht im lokalen System, sondern in den Eigenschaften des großen Systems selbst zu suchen ist. Von diesen Ausgangspunkten aus haben B. LINDBLAD1 und J. H. Oort2 das Problem behandelt.

Es wird in LINDBLADS Arbeit zunächst einem Zusammenhang zwischen dem Phänomen der Asymmetrie der Geschwindigkeiten, wie sie besonders in G. Ström-BERGS<sup>8</sup> Arbeit hervortritt, und allgemein anerkannten Tatsachen betreffs der räumlichen Verteilung der Materie im Sternsystem nachgeforscht. Wir können hier besonders die folgenden hauptsächlichen Gesichtspunkte in Betracht ziehen.

1. Wenn auch die auffallenden Unterschiede in scheinbarer galaktischer Konzentration zwischen verschiedenen Arten von Objekten gewissermaßen auf verschiedene mittlere Entfernung der Individuen der betreffenden Gruppen zurückgeführt werden können, so ist es doch in vielen Fällen offenbar, daß es für verschiedene Gruppen von Objekten auch eine wirkliche Variation in der "absoluten" räumlichen Konzentration gegen die Milchstraßenebene gibt. So besteht wahrscheinlich eine wirkliche Verschledenheit in galaktischer Konzentration zwischen den A-Sternen und den Riesensternen von späterem Spektraltypus. Wir können auch extreme Gruppen wie O-Sterne und langperiodische & Cephei-Sterne auf der einen Seite mit planetarischen Nebeln, kurzperiodischen δ Cephei-Sternen, Kugelhaufen auf der anderen Seite einander gegentiberstellen.

2. Es werden diese Verschiedenheiten in der wahren galaktischen Konzentration von einer Variation der inneren Streuung in den Geschwindigkeiten relativ zum Zentroid begleitet und zwar in direktester Weise von dieser Varlation aus erklärt. Zufolge einer größeren allgemeinen Streuung der zentrojdalen Geschwindigkeiten wird die Bindung der betreffenden Objekte an die Milchstraßencbene weniger stark, die Amplituden in der Bewegung senkrecht zu dieser Ebene im Durchschnitt größer und die galaktische Konzentration weniger ausgeprägt.

3. Die fundamentale Einstellung zum Problem hängt jetzt wesentlich davon ab, daß wir zur Erklärung des Phänomens der "asymmetrischen Geschwindigkeitsverteilung" die Hypothese einführen, daß die Streuung der Geschwindigkeiten relativ zum Zentroid klein ist gegen die systematische Bewegung des Zentroides selbst relativ zum Schwerpunkt des Systems als Ganzem. Wir werden gleich unten diese systematische Bewegung mit einer allgemeinen Rotationsbewegung identifizieren.

4. Gemäß unsren Resultaten über die allgemeine Verteilung des Milchstraßenlichts (Ziff, 9, 11), über die räumliche Verteilung der Kugelhaufen, der schwachen Sterne (Ziff. 48) und der Objekte hoher absoluter Leuchtkraft (Ziff. 20) suchen wir den Schwerpunkt des Systems in der Sagittariusgegond,

etwa in den galaktischen Längen 325°-330°.

5. Wir führen hier weiter die Annahme ein, daß das System sich wenigstens in groben Zügen in einen dynamisch stationären Zustand angeordnet hat. Eine

Ark Mat Astr Fys 19A, Nr. 21, 27 u. 35; 19B, Nr. 7; 20A, Nr. 17; 21A, Nr. 3 u. 15 (1925-1929); A N 236, S. 481 (1929); M N 87, S. 553 (1927); 90, S. 503 (1930); Upsala Medd 3, 4, 6, 13, 24, 26, Stockholm Medd 1, 2, 4, 5.
 BAN 3, S. 275 (1927); 4, S. 79 und S. 91 (1927); 4, S. 269 (1928).
 Mt Wilson Contr 275 → Ap J 59, S. 228 (1924); Mt Wilson Contr 293 → Ap J 61, (1928)

S. 363 (1925).

ziemlich weitgehende Mischung der Materie von verschiedenen Bahnkom im System wird in der Tat schon nach wenigen Umläufen in der Rote bewegung erfolgen, und wir müssen von vornherein nicht mehr in den ]

des stationären Zustandes hineinlegen (vgl. Ziff. 27).

6. Um hier noch einen Schritt weiter tun zu können, ziehen wir zue eine Erfahrungstatsache den Umstand heran, daß für die Objektgruppe kleinster Streuung in den Geschwindigkeiten (z. B. die Gruppen der langpschen  $\delta$  Cephei-Sterne) wir in der galaktischen Ebene wenigstens keine ill auffallenden systematischen Veränderungen in der räumlichen Dichteverte und auch nicht in der Geschwindigkeitsstreuung, beobachtet haben, wenn hier oftmals die beobachteten Objekte wegen ihrer großen absoluten Leuch innerhalb eines ziemlich weiten Kreises um uns herum gestreut vorkor Wenn wir dann auf das System als Ganzes eine Theorie analog derjenige vorigen Ziffer, Gleichungen (19) bis (22), anwenden und die entsprech Bezeichnungen einführen (die Richtung gegen den Schwerpunkt aber  $\xi$  den obigen Auseinandersetzungen in einer anderen Himmelsgegend anneh so folgt für eine solche Gruppe aus der Kleinheit von  $\widehat{H}^{\mathfrak{s}}$  und  $\partial \widehat{H}^{\mathfrak{s}}/\partial R$  (vgl. Zi und aus der Endlichkeit von  $\partial r/\partial R$ 

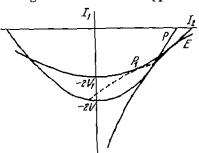


Abb. 24. Diagramm zur Erklärung der Eigenschaften einer Frequenzfunktion  $f(I_1, I_2)$ .

$$\frac{\partial p}{\partial R} = 0$$
,

und demnach aus der zweiten Gleichung wenn wir p an der Seite von q ver lässigen,

$$\frac{q}{r} = -R \frac{\partial V}{\partial R}$$

oder

$$\overline{\Theta^2} = -R \frac{\partial V}{\partial R}.$$

Wir können hier  $\overline{\Theta^2}$  mit  $\Theta^2_0$  vertauschen  $\Theta_0$  die mittlere Geschwindigkeit in der g tischen Ebene senkrecht zur Richtung  $\xi$  den Schwerpunkt des Systems bezeic

Dies zeigt uns, daß  $\Theta_0$  mit der Geschwindigkeit der zirkularen Beweg um den Schwerpunkt herum identisch ist. Mit verschwindender Streuung Bewegungen innerhalb einer Gruppe von Objekten geht also die Bewegungt in eine Kreisbewegung um den Schwerpunkt herum über, während gl zeitig die galaktische Konzentration der betreffenden Objekte außerordlich stark ausgeprägt wird. Für diesen Satz werden wir unten (Ziff. 31 Anschluß an eine Diskussion des interstellaren Kalziums eine wichtige Stinden.

Wir wenden uns aber zunächst zur unmittelbaren theoretischen Bedeu und Begründung des Satzes. Wenn wir einen stationären Zustand ge Poincarés Theorem annehmen wollen, so scheint zwar die einzige Möglich der zuerst von Jeans und Charlier angegebene Spezialfall zu sein, wo die quenzfunktion von den zwei Integralen, Energieintegral und Flächeninte abhängt, was eine rotationssymmetrische Anordnung des Systems im Ra einschließt (Ziff. 27). Wir haben dann für die Frequenzfunktion einen Ausd

$$f(I_1, I_2),$$

$$I_1 = II^2 + \Theta^2 + Z^2 - 2V, \quad I_2 = R\Theta.$$

R ist wie vorher die Projektion des Radiusvektors vom Schwerpunkt auf Milchstraßenebene, H die entsprechende Geschwindigkeit,  $\Theta$  die Geschwindigkeit,

in der galaktischen Ebene senkrecht zu R, Z die Geschwindigkeit senkrecht zur galaktischen Ebene. V ist das Gravitationspotential. — Wir können jetzt die Funktion  $f(I_1, I_2)$  in der Weise studieren, daß wir in ein Diagramm (Abb 24)  $I_2$  als Abszisse und  $I_1$  als Ordinate eintragen und das Flächenelement  $dI_1 dI_2$  das sechsdumensionale Element  $RdRd\theta dHd\theta dZ$  formal repräsentieren lassen.

Die Grenzgeschwindigkeit im stationären Zustande an irgendemem Punkte

des Systems wird durch die Bedingung

$$I_1 < 0 \tag{30}$$

ausgedrückt Man muß nämlich erwarten, daß ein Stern mit größerer Geschwindigkeit in seiner weiteren Bahn definitiv aus dem System entweicht. Wir können also eine endliche Frequenz / nur unterhalb der Achso  $I_1 = 0$  habon. Eine weitere Grenzlinie im Diagramm ergibt sich aus der selbstverständlichen Bedingung

 $I_1^* \le R^*(I_1 + 2V)$ , (31)

welche für einen Punkt R, s im System gilt. Die Parabellinie  $I_1^s = R^s(I_1 + 2V)$  nonnen wir die charakteristische Parabel des betreffenden Punktes. Auf dieser Parabel ist offenbar

$$II = Z = 0$$

Da für ein und denselhen Radius R des Potentiel V mit der Entfernung s von der galaktischen Symmetrieebene abnehmen muß, wir also für einen gegebenen Wert von V umgekehrt R — max für s=0 haben, so entspricht die Linie s=0 auf der Potentialfläche V= konst einem maximalen Parameter  $\frac{1}{4}R^s$  der charaktenstischen Parabel mit beibehaltenem Vertexpunkt  $(I_0=0,\ I_1=-2V)$  im Diagramm Das Gebiet des Diagramms, welches für das System als Ganzes in Frage kommen kann, wird also von der Enveloppe (E) der charakteristischen Parabel für Punkte in der galaktischen Ebene (s=0) begrenzt. Wie man sich leicht überzeugt, wird diese Enveloppe durch die Relation

$$I_{\bullet}^{a} = -R^{a} \frac{\partial V}{\partial R} \tag{32}$$

charakterisiert, woraus folgt

$$G^2 = -R \frac{\partial V}{\partial R}$$
.

Da außerdem H=Z=0, so bedeutet diese Bewegung eine zirkulare Bewegung um das Zentrum herum. Umgekehrt bedeutet also eine Konzentration gegen zirkulare Bewegungen in der galaktischen Ebene eine Konzentration der Frequens f gegen die betrachtete Grenzlinie E im Diagramm. Da wir aber eine allgemeine Rotationsbewegung nur in einer Richtung voraussetzen, wird nur der eine von den zwei Enveloppenzweigen von Bedeutung

Die Sache liegt demnach so, daß wir für einen gegebenen Punkt (R, s) im System mögliche Kombinationen von  $I_1$  und  $I_2$  im Diagramm nur zwischen der Achse  $I_1 = 0$  und der dem Punkt entsprechenden charakteristischen Parabel haben, während für das System als Ganzes das in Frage kommende Gebiet zwischen der Achse  $I_1 = 0$  und der Enveloppe (E), welche zirkularen Bowegungen in der galaktischen Ebene entspricht, liegt

Die individuellen Partikeln, deren  $I_1$ ,  $I_2$ -Punkte im Diagramm innerhalb einer gewissen charakteristischen Parabel liegen, können wir aber als Partikeln die in dem betreffenden Punkte (R, s) des Systems gegeneinander stoßen, betrachten. Mit dem Begriff "Stoß" meinen wir dann natürlich eine nahe Passage von zwei oder mehreren Partikeln in ihren Bahnen. Es ist unzweifelhaft, daß

in diesem Vorgang wenigstens eine Tendenz zu einer Gleichverteilung der Emergie der Partikeln vorhanden sein muß. Wenn wir nur das Gebiet einer und derselben charakteristischen Parabel in Betracht zichen, so würden wir, wenn die Masse einer Partikel mit m und die Geschwindigkeitsdispersion für Partikeln der Masse imit  $\sigma$  bezeichnet wird, eine Frequenzfunktion

$$I = C e^{-\frac{m}{2\sigma^2}(I_1 - 2\omega I_2)} \tag{33}$$

erwarten.  $\omega$  ist die mittlere Winkelgeschwindigkeit der Rotationsbewegung. Die Linien konstanter Frequenz in dem  $I_1$ ,  $I_2$ -Diagramm wären somit gerade Linien mit einem Winkelkoeffizienten gleich  $2\omega$ . Wenn wir aber in Betracht ziehen, daß alle Punkte des betrachteten Gebietes im Diagramm, außer den Punkten auf der Enveloppe (E) selbst, gleichzeitig verschiedenen charakteristischen Parabeln angehören, so müssen wir doch für die Frequenzlinien Kurven von allgemeinerer Natur voraussetzen. Der Prozeß der Gleichverteihung ist so langsam, daß wir eine vollkommene Ausgleichung als einen niemals erreichten Grenzfall betrachten können.

Es ist durchaus möglich, daß in der Nähe der Enveloppe die für eine kurze Strecke als die Geraden

$$I_1 - 2\omega I_2 = \text{konst.} \tag{34}$$

angenommenen Frequenzlinien mit der Tangente der charakteristischen Parabel in ihrem Kontaktpunkte mit der Enveloppe (E) parallel werden. Dies bedeutet, daß die mittlere Winkelgeschwindigkeit  $\omega$  mit der Winkelgeschwindigkeit der zirkularen Bahn identisch wird. In diesem Falle werden wir eine starke Konzentration gegen die Enveloppe (E) im Diagramm und, räumlich interpretiert, gegen die zirkularen Bewegungen in der Ebene zu erwarten haben. Es ist bemerkenswert, daß (34) das Jacobische Integral für die Bewegung um eine lokale Kondensation, welche einer zirkularen Bewegung mit der Winkelgeschwindigkeit  $\omega$  folgt, darstellt. Es ist in der Tat möglich, daß in dem allgemeinen Ausgleichungsprozeß auch höhere Einheiten als einzelne Sterne, d. h. mehr oder weniger lockere Anhäufungen von Sternen, mitspielen, was besonders für die Ausgleichung der Frequenz nahe der Enveloppe von Bedeutung sein wird, da die Sterne sich hier mit kleinen relativen Geschwindigkeiten bewegen.

Nach den obigen Auseinandersetzungen ist also die charakteristische Verteilung der Geschwindigkeiten in unserem Punkte des Systems wie auch die räumliche Konzentration gegen eine gewisse Ebene (Milchstraßenphänomen) durch eine Konzentration gegen die Enveloppe der charakteristischen Parabel und gleichzeitig durch eine gegen  $I_1 = 0$  kontinuierlich gegen

Null abnehmende Frequenz bedingt.

HALM¹, CHARLIER² und SEARES® haben die Gleichverteilung der Energie für Sterne verschiedener Massen in unserer näheren Umgebung diskutiert. Zweifellos ist in den Geschwindigkeiten relativ zum Zentroid eine deutliche Tendenz zu einer Gleichverteilung vorhanden. Es ist aber offenbar, wenn wir das System als Ganzes betrachten, daß wichtige Ausnahmen verzeichnet werden müssen. Eine Erklärung dieser Verhältnisse muß offenbar eng mit einer Kosmogonie des Systems zusammenhängen.

Wir haben oben stillschweigend vorausgesetzt, daß ein stationärer Zustand mit einer Frequenzfunktion vom Typus  $f(I_1, I_2)$  wirklich existiert, d.h. daß man mit einer solchen Funktion der Poissonschen Gleichung Genüge leisten kann (vgl. Ziff. 27). Die Existenz des stationären Zustandes für spezielle ana-

8 Mt Wilson Contr 226 - Ap J 55, S. 165 (1922).

<sup>&</sup>lt;sup>1</sup> M N 71, S. 610 (1911). <sup>2</sup> Lund Medd Nr. 76 und 81 (1917).

lytisch definierte Funktionen  $I(I_1, I_2)$  wird in den oben zitierten Arbeiten von OHLSSON und WHENER behandelt Wir können aber hier besonders auf die Existenz des Grenzfalles hinweisen, we eine endliche Frequenz / nur an der Enveloppe E im  $I_1$ ,  $I_2$  Diagramm vorhanden ist, was offenbar bedeutet, daß die Materio des Systems in zirkularen Bahnen in der Ebene um den Schwerpunkt schwingt, in Analogie mit den Bewegungen im Sonnensystem. Nach der hier behandelten Theorie wird das System, als Ganzes betrachtet, sich nicht sehr viel von diesem Zustand unterscheiden, und es schemt offenbar, daß auch in der

Nähe vom "Sonnensystemtypus" Lösungen existieren milssen Die "Druckgloichungen" (21), deren zwei letzte Terme auf der linken Seite wir gewissermaßen als "Viskositätsterme" bezeichnen können, and, wie schon oben in Zliff, 28 bemorkt worden ist, bei der hier angenommenen Frequenzfunktion  $I(I_1, I_2)$  von solbst critilit. Wenn wir den Effekt der nahen Passagen in Botracht zichen, würde zwar die lange freie Weglänge einer Partikel außerdem einen großen Viskositätskooffizienten, nach abstrakter Analogie mit der Gastheorie gerechnet, herbeiführen. Die unmittelbere Analogie mit den Gasen versagt aber offenbar, de der Weg eines Storns swischen den Stößen gar nicht als geradlinig vorauszusetzen ist, sondern die ganze gekrümmte Bahnbewegung einer Partikel im System innorhalb der freien Weglänge fällt (vgl. Ziff, 27) Wenn wir im System oine geschlossene Rotationsiläche mit dem Schwerpunkt als Mittelpunkt betrachten, so worden die Sterne, die etwa in einem gewissen Augenblicke über diese Fläche nach außen ziehen, im allgemeinen zwischen zwei Passagen in ihrer Bahnbewegung mehrmals über diese Plache hin und her ziehen Der Bereich um die Flüche herum, innerhalb der die betrachteten Sterne einen Austausch von Moment vermitteln können, wird im allgemeinen wegen der Bahnbewegung ziemlich eng begrenzt. Der wirkliche Transport von Moment über die Fläche infolge der Passagen wird daher sehr langsam.

Es soil außerdem hier betont werden, daß es durchaus nicht notwendig ist. einen stationären Zustand in dem vollen abstrakten Sinne dieses Wortes anzunehmon. Was vorausgesetzt wird, ist, daß eine ziemlich vollständige Mischung der Materie des Systems, wie in Ziff. 27 auseinandergesetzt, stattgefunden hat, Es kann vorkommen, daß gewisse Eigenschaften eines stationaren Systems nur so laugsam eintreten, daß sie in der tatsächlichen Entwicklung des Systems noch nicht erreicht worden sind. Da das System offenbar gegen eine Symmetriesbene sehr abgeplattet ist, und die Bewegung in der Nahe dieser Ebene von nahe zwaidimensionaler Natur ist, so besteht z. B. eine sehr schwache statistische Verbindung zwischen der Bewegung parallel zur Ebene und der Bewegung senkrecht dazu. Da die Kraftkomponente in der s-Richtung sich nur langsam mit R andern wird, so können wir in der Tat die Abhängigkeit der vertikalen Kraftkomponenta von z als eine konstante Funktion längs der ganzen Bahn eines Sterns anschen, wodurch die Bewegung in s unabhängig von der Bewegung parallel zur galaktischen Ebene wird. Um diesen Verhältnissen Rechnung zu tragen, schreiben

wir das Energieintegral

$$I_1 = \Pi^0 + \Theta^0 + Z_0^0 - 2V_0(R), \quad Z_0^0 = Z^0 - 2(V(R, s) - V_0(R)), \quad (35)$$

wo  $V_0$  die in der Ebene herrschende Potentialfunktion ist,  $Z_0$  der Z-Wert für s=0, and we verausgesetzt wird, daß die Differenz  $V(R,s)-V_0(R)$  sich nur langsam mit R ändert. Diese Differenz kann gewissermaßen als ein Mittel für die Potentialdifferenzen zwischen den Höhen z und 0 in verschiedenen, alch in der Höhe s mit demselben Wert von Z kreuzenden Bahnen betrachtet werden.  $Z_{ullet}$  wird dann als eine Konstante in der Bewegung eines einzelnen Sterns vorausgesetzt. In der unmittelbaren Umgebung der galaktischen Ebene haben wir wo

 $\Delta_D^{(s)}$ 

dann nach (28) für jedes Intervall  $dZ_0$  die zweidimensionale Verteilung

$$dZ_0 \cdot \varphi_0(R, \Pi, \Theta, Z_0) R dR dz d\Pi d\Theta,$$
  

$$\varphi_0(R, \Pi, \Theta, Z_0) = f(I_1, I_0),$$
(36)

und wo  $I_1$  gemäß (35) ausgedrückt wird. Eine allgemeinere stationäre Verteilung

für beliebige Entfernung a von der galaktischen Ebene können wir dann folgendermaßen definieren

 $\varphi(R, z, \Pi, \Theta, Z) R dR dz d\Pi d\Theta dZ = \varphi_0(R, \Pi, \Theta, Z_0) R dR dz d\Pi d\Theta \cdot F(Z_0^2) dZ_0$ 

wo  $F(Z_0^2)$  eine a priori unbekannte, beliebige Funktion ist. Wir haben auf der rechten Seite  $dZ_0$  durch dZ ersetzt, weil in der Bewegung dz dZ invariant ist. Es ergibt sich also

 $\varphi = \varphi_0 \cdot F(Z_0^2)$ ,

wo der Ausdruck für  $Z_0$  gemäß (35) eingesetzt wird. Für z=0,  $Z=Z_0=0$ , ist  $\varphi = \varphi_0$ , also gilt F(0) = 1.

Was sonst die Funktion F angeht, so ist es jedenfalls sehr wahrscheinlich, daß für jeden Wert von R die Streuungen in den Komponenten II und Z in enger Beziehung zueinander stehen. Es ist aber nicht notwendig, daß sie gleich sind, wie man unter strenger Rechnung nach (28) fordern müßte. In unserer Umgebung gilt, daß  $ar{Z^2}$  etwas kleiner als  $ar{H^2}$  ausfällt. Wenn wir im folgenden der Einfachheit wegen mit (28) rechnen, setzen wir voraus, daß für Fragen, die mit der Verteilung senkrecht zur Milchstraßenebene von Bedeutung sind, eine Transformation zu machen ist, wobei die allgemeinere Verteilungsfunktion  $\varphi$  gemäß (37) zu bilden ist.  $F(Z_0^2)$  ist gemäß dem empirisch ermittelten Geschwindigkeitskörper zu wählen, unter Beachtung der Relation (38).

30. Die asymmetrische Geschwindigkeitsverteilung in ihrer Beziehung zur Rotation. Wir wollen eine gewisse Klasse von Objekten ins Auge fassen und im

1, I2-Diagramm (Abb. 24) eine Linie konstanter Frequenz

$$/(I_1, I_2) = \text{konst.}$$

ür diese Klasse ziehen. Der innerhalb einer charakteristischen Parabel eineschlossene Teil der Frequenzlinie entspricht einer geschlossenen Fläche im reschwindigkeitsraume. Nehmen wir an, daß die Frequenzlinie (gestrichelte inie in der Abbildung) durch eine Parabellinie

$$I_1 + \frac{1}{2p}(I_2 - M)^2 = N \tag{39}$$

pproximiert werden kann, woM, N, pzur Verfügung stehende Konstanten nd. Die Differenz  $\Delta I_1$  in den Ordinaten zwischen einem Punkte auf der Freuenzlinie und der charakteristischen Parabel

$$I_2^2 = R^2(I_1 + 2V) (40)$$

t gleich  $II^2+Z^2$ , da auf der letzteren Kurve II=Z=0 ist, während die tangenelle Geschwindigkeitskomponente durch die Relation  $\Theta = \frac{1}{R} I_2$  gegeben ist. an findet dann nach einigen einfachen Reduktionen für die Geschwindigkeltsiche, welche der Frequenzlinie (39) entspricht, folgenden Ausdruck:

$$\frac{II^{3} + Z^{3}}{a^{3}} + \frac{(\Theta - \Theta_{0})^{3}}{b^{3}} = 1, \tag{41}$$

$$\Theta_0 = \frac{MR}{R^4 + 2p}, \quad a^4 = 2V + N - \frac{M^4}{R^4 + 2p}, \quad \frac{b^4}{a^4} = \frac{2p}{R^4 + 2p}$$
(42)

Die Geschwindigkeitsfläche ist also für  $\phi > 0$  ein in der  $\Theta$ -Richtung abgeplattetes Sphäroid Bezeichnen wir mit a und  $\beta$  die Halbachsen des sog Geschwindigkeitsellipsoids für einen gegebenen Ort, so haben wir also gemäß der obigen Approximation (39)

 $\int_{-\infty}^{+\infty} \int_{0}^{+\infty} e^{-\frac{1}{2}\left(\frac{H^{0}+Z^{0}}{G^{0}}+\frac{(\Theta-\Theta_{0})^{0}}{\beta^{0}}\right)}$ (43)

WO

$$\alpha^{0} = \frac{\sigma^{0}}{m}, \quad \frac{\beta^{0}}{\alpha^{0}} = \frac{2\beta}{R^{0} + 2\beta}. \tag{44}$$

Soweit eine ellipsoidische Approximation gilt, ist also & konstant für verschiedene Punkte des Systems, während \$\beta\$ mit \$R\$ (aber nicht mit \$\epsilon\$) variiert Da offenbar  $\alpha^{0} = II^{0}$ , so kann man also auf Grundlage der Theorie eines stationären Zustandes wenigstens keine schnelle Variation von  $\overline{\mathcal{I}}^{\underline{s}}$  mit der Lage (R,s) des betrachteten Punktes im System voraussetzen. Dies ist in Übereinstimmung mit unserer oben für die Sterne mit kleinem  $\overline{IP}$  getroffenen Annahme der Kleinheit van  $\partial \Pi^2/\partial R$ .

Die beobachtete Asymmetrie der Geschwindigkeitsverteilung müssen wir von unserem Standpunkte aus als eine Variation der mittleren Rotationsgeschwindigkeit  $\Theta_0$  mit der Strenung der individuellen Geschwindigkeiten deuten. Die Richtung der asymmotrischen Verschiebung der Geschwindigkeitsmittelpunkte soll dann offenbar senkrecht zur Richtung gegen das Zentrum des Systems stohen Nach STRÖMBERGS Arbeit über die Asymmetrie ist dies auch sehr nahe erfüllt. Wir erhalten nach seinen Resultaten für die galaktische Länge des Zentrums 331°,5 ± 5°, was sehr wohl mit Shapleys aus der Verteilung der Kugelhaufen horgoleitetem Wert 327° übereinstummt

Wir wollon jetzt eine gewisse Klasse von Sternen auswählen, die wir auch mit dem Wort "Untersystem" kennzeichnen können. Wir führen für ein solches Untersystem den Begriff "effektive Grenzfläche" ein, deren Radius in der galaktischen Ebene wir mit R, bezeichnen. Wir definieren die "effektive" Begrenzungsfläche siemlich willkürlich derart, daß an dieser Fläche der Frequenziaktor /... der Gleichung (43) im Verhältnis 1/s, mit dem Werte an unserem Orte im Raume vergilchen, abgenommen haben soll. Die Bedeutung des eingeführten Begriffs folgt aus der folgenden Überlegung Betrachten wir im Geschwindigkeitsraume unseres Ortes cine ellipsoidische Schale (42), wo  $a^3=2\alpha^3, b^2=2\beta^2$  An dieser Schale wird offenbar gemäß (43) die Frequens 1/4 fo herrschen Die Geschwindigkeitsschale entspricht einer gewissen Frequenzlinie im  $I_1$ ,  $I_2$ -Diagramm, und es 1st klar, daß wir einen neuen Ort  $(R_1,0)$  so wählen können, daß die charakteristische Parabel für diesen Punkt die genannte Frequenziinie tangiert Wir haben dann für diesen Ort eine Frequenz  $\frac{1}{s} f_0$  für  $H = Z = \Theta - \Theta_0 = 0$ . Der Wert von  $a^2$  für  $R = R_1$  muß daher verschwinden. Wir haben also gemäß (42) zu setzen, den zwei betrachteten Ortern im System entsprechend,

$$2\alpha^{0} = 2V + N - \frac{M^{3}}{R^{3} + 2p},$$

$$0 = 2V_{1} + N - \frac{M^{3}}{R^{3} + 2p}.$$
(45)

Wenn wir aus diesen Relationen und den Gleichungen (42, 44) die Parameter M, N und p eliminieren, bekommen wir

$$\theta_0^2 + 2\alpha^2 \left( \frac{R_1^4}{R_1^2 - R^2} - \frac{\beta^2}{\alpha^2} \right) = 2(V - V_1) \left( \frac{R_1^4}{R_1^2 - R^2} - \frac{\beta^2}{\alpha^2} \right). \tag{46}$$

Für  $\beta/\alpha$  ist nahe 0,7 zu setzen. Wenn wir aber annehmen, daß  $R_1-R$  klein gegenüber R selbst ist, die Sonne also sehr exzentrisch im System liegt, so vereinfacht sich diese Gleichung mit sehr guter Approximation auf die folgende:

$$\Theta_0^2 + \alpha^2 \frac{R_1}{R_1 - R} = -R \frac{\partial V}{\partial R}. \tag{47}$$

Wir können jetzt auch, wenn wir verschiedene Untersysteme betrachten, annehmen, daß  $R_1 - R$  nicht gleichzeitig mit  $\alpha$  verschwindet, und dies ist damit gleichbedeutend, daß mit verschwindender Streuung a die mittlere tangentiale Bewegung  $\Theta_{\mathfrak{o}}$  einer Gruppe sich der zirkularen Bewegung  $\Theta_{\mathfrak{o}}$  um das Zentrum herum nähert. Wir haben somit  $\Theta_0 = \max_{\alpha} = \Theta_0$  für  $\alpha = 0$ , und demnach

$$(\Theta_0)_{\max}^2 = \Theta_0^2 = -R \frac{\partial V}{\partial R}. \tag{48}$$

Die asymmetrische Geschwindigkeitsverschiebung wird als

$$S = \Theta_{\mathbf{a}} - \Theta_{\mathbf{0}} \tag{49}$$

definiert. Wir haben jetzt dieses Verschiebungsgesetz mit der von Strömberg<sup>1</sup> durch ein Studium der Radialgeschwindigkeiten hergeleiteten Relation zwischen Geschwindigkeitsstreuung und "asymmetrical drift" zu vergleichen. STRÖMBERG leitet eine parabolische Relation ab, die aber auch eine langgestreckte elliptische sein kann, der Gleichung (46) entsprechend, wenn wir in diese  $R_1 = \text{konst. einsetzen.}$ 

Wenn wir annehmen, daß das Untersystem der Kugclsternhaufen im Mittel keine merkliche Rotationsbewegung besitzt, können wir eine rohe Abschätzung von ⊕ machen. Nach Lundmarks und Strömbergs Resultaten für die Sonnengeschwindigkeit in bezug auf die Haufen ergibt sich  $\Theta_{e}$  zu rund 300 km/sec. Wir nehmen hier nach Strömberg (vgl. Tabelle 20, Kugelhaufen)  $\Theta_a = 275 \text{ km/sec}$ 

Tabelle 20.

Kiasse	Н	ø	s	$\frac{R_1-R}{R_1}$	Klasse	Н	α	S	$\frac{R_1-R}{R_1}$
M0-M9 K4-K9	-1,9 bls + 3,0	39.0 +	- 2,1 -14,6 - 7,4	0,33 0,19 0,10	F0—F9 "	$\leq$ -2,0 -1,9 bis 0,0 +0,1 ,, + 3,0	24,0	+ 5.4 + 7.2 + 1.7	0,13 0,15 (0,90)
" G9~K3	-1,9 bis +3 ,0 ≥ +3,1 ≤ -3,0	29,6  -	-15,5  - 3,7	0,11 (1,35) 0,08	", B6A9	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	48,4 122	+ 6,8 + 95,0	0.63
,, ,,	-2,9 bis - 2,0 -1,9 ,, - 1,0 -0,9 ,, 0,0	19.6 23,2 26,0	1,9 + 2,5	0,37 0,39	B0—B5	$ \begin{vmatrix} -2.9 & + 2.7 \\ \leq -4.0 \\ -3.9 & bis + 0.1 \end{vmatrix} $	16,4 8,1 7,4	+ 0,9 + 8,5 + 9,4	0,54 (0,01) (0,01)
,,	+0,1 ,, + 1,0 +1,1 ,, + 3,0	28,9	1		Sterne: Per. > 2,0 d. Per. < 0,7 d.	-	17,3	- 1,0	
G0-G8	$+3.1$ , $+12.0$ $\leq -2.0$ $-1.9$ bis $+1.0$	33.7 17.6 25.8	+ 14,5 + 3,4		O5-O9 c-Sterne P	- 		+ 97 + 23,5 + 9,4	
n n	+1,1 ,, + 5,0 +5,1 ,, +10,0	44,0 46,2	+ 9.7	0,37	M1e—M6e M2e—M5e Kugelhaufen	, 	64,7 52 88 117	+ 15,6 + 50,5 +151 +275	

L. c.
 Publ A S P 35, S. 318 (1923).
 Mt Wilson Contr 292 = Ap J 61, S. 353 (1925).

an. Die Entfernung der Sonne von der effektiven Grenze des Systems, wenn wir als Einheit den Radius selbst nahmen, berechnen wir aus

$$\frac{R_{\rm I}-R}{R_{\rm I}} = \frac{\alpha^{\rm B}}{S(2\theta_{\rm e}-S)} \,. \tag{50}$$

Tabelle 20 gibt  $\alpha$ , S und  $\frac{R_1-R}{R_1}$  für die verschiedenen Gruppen in Strömbergs Arbeit S wird vom "limiting center", d. h. dem Vertex der Parabal, längs deren Achse, gerechnet.  $\alpha$  ist mit der größeren Achse des Geschwindigkeitsellipsoids in der galaktischen Ebene identisch genommen. H ist die Quantität  $m+5\log\mu$ 

Es ist aus der Tabolle ersichtlich, daß die meisten Gruppen eine bemerkenswerte Übereinstimmung zeigen. Wenn wir einige extreme Werte ausschließen (zwei extrem große und die sehr klemen Werte der frühen B-Sterne), so bekom-

men wir im Mittal für 27 Gruppen

$$\frac{R_1-R}{R_1}=0.23\pm0.03$$
 (m. F.).

Die Sonne ist also um 23 % des Radius innerhalb der "effektiven" Grenze des Systems, also sohr exzentrisch, gelegen

Für die räumliche Dichtigkeit  $\nu$  eines Untersystems ergibt sich durch Integration von (43)  $\nu=(2\pi)^{3/2}\alpha^2\beta/a$ . Man bekommt dann gemäß (44) und nach der Definition der "effektiven Grenze" für die Dichtigkeit  $\nu_1$  an dieser Grenze

$$\frac{r_1}{r} := \frac{\beta_1}{\beta} \frac{1}{\sigma},$$

und weiter gomāB (39)

$$\left(\frac{\beta_1}{\beta}\right)^2 = \frac{R^2 + 2p}{R_1^2 + 2p}, \quad \left(\frac{\beta}{\alpha}\right)^2 = \frac{2p}{R^2 + 2p}.$$

Nach Elimination von p ergibt sich

$$\frac{r_1}{r} = \left(\frac{\sigma^4 R^6}{\int_0^1 R^4 + (\sigma^6 - f^2) R^4}\right)^{\frac{1}{6}} \cdot \frac{1}{\sigma} \,, \tag{51}$$

Numerisch erhält man gemäß den oben für  $\beta/\alpha$  und  $R/R_1$  gegebonen Werten  $\nu_1/\nu = 0.32$ . Die räumliche Dichtigkeit an der "Grenze" ist also 0.32 der Dichtig-

keit in unserer Umgebung.

Die allgemeine Dichtigkeitsverteilung in der galaktischen Ebene gemäß der ellipsoidischen Approximation ergibt sich aus (43) und dem Diagramm Abb. 24 unter Benutzung einer Methode, welche zu Gleichungen, die mit (45) und (46) analog sind, führt. Wir bezeichnen jetzt mit  $R_0$ ,  $\nu_0$  und  $V_0$  für unseren Punkt im System geltende Werte, und mit R die laufende Koordinate. Wenn die Geschwindigkeitsverteilung an unserem Punkte wie vorher durch  $\Theta_0$ ,  $\alpha$ ,  $\beta$  charakterisiert ist, so haben wir für das betreffende Untersystem

$$\log \frac{r}{r_0} = \frac{1}{2} \log \frac{\alpha^3 R_0^3}{\beta^3 R_0^3 + (\alpha^3 - \beta^3) R^3} + \frac{1}{\alpha^4} \left( V - V_0 + \frac{1}{2} \Theta_0^3 \frac{\alpha^3 (R^3 - R_0^3)}{\beta^3 R_0^3 + (\alpha^3 - \beta^3) R^3} \right) \log \sigma. (52)$$

Der erste Term auf der rechten Seite ist kieln Wir können mittels dieser Gleichung den Radiusvektor R für beliebige Werte von  $r/r_0$  berechnen, sobald wir in genügender Weise die Kraftfunktion für sukzessive Werte von R, worans  $V - V_0$  berechnet wird, kennen. Durch Differentiation der Gleichung können wir  $\partial \log r/\partial R$  in Relation zu  $\theta_0$ ,  $\alpha$  und  $\partial V/\partial R$  bringen, worans, wie wir unten sehen werden, eine alternative, aber im Prinzip mit dam obigen identische Behandlung des Phänomens der Asymmetrie sich ergibt.

Eine Erklärung der approximativen Konstanz von  $R_1$  kann uns eine Betrachtung der Abb. 24 geben. Mit wachsendem R nähert sich die charakteristische Parabel des betrachteten Systempunktes mehr und mehr der  $I_a$ -Achse, um im Limes mit dieser Achse zusammenzufallen. Wenn wir annehmen, daß die Geschwindigkeit der zirkularen Bewegung an unserem Orte nicht sehr weit von der Grenzgeschwindigkeit, welche  $I_1=0$  entspricht, liegt, so ist der Berührungspunkt zwischen der charakteristischen Parabel und der Enveloppe nicht weit von der  $I_a$ -Achse entfernt, und die charakteristische Parabel unseres Ortes verläuft in der Nähe dieser Achse. Da für alle Untersysteme die Frequenz  $I(I_1,I_2)$  gegen die Achse  $I_1=0$  sukzessiv gegen Null abnimmt, so ist es a priori

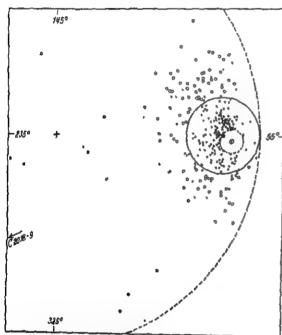


Abb. 25. Die Verteilung in der galaktischen Ebene für große Geschwindigkeiten relativ zur Sonne (nach Oort). Die schwarzen Punkte entsprechen einem homogenen Material für Geschwindigkeitsdifferenzen gegen die Sonne größer als 19,5 km/sec. Der größere (voll gezogene) Kreis entspricht Geschwindigkeiten von 65 km/sec relativ zum Zentroid. Das Kreuz soll die Schwerpunktsgeschwindigkeit des Systems repräsentieren, und der große (unterbrochene) Kreis mit dem Kreuz als Zentrum hat einen Radius von 365 km/sec.

wahrscheinlich, wenigstens für die Gruppen von großer Asymmetrie, daß in der Figur eine einzige charakteristische Parabel, welche approximatiy der effektiven Grenze  $R = R_1$  verschiedener Untersysteme entspricht, gezogen werden kann. Die Abnahme der räumlichen Dichtigkeit gegen eine "effektive Grenzfläche", wie auch das ganze Phänomen der Asymmetrie der Geschwindigkeitsverteilung erscheint also als eine Folge der Bedingung, daß die Partikeln des Systems der Relation  $I_1 < 0$ genügen müssen, mit einer kontinuierlichen Abnahme der Frequenz gegen dieso Grenze im  $I_1$ ,  $I_2$ -Diagramm.

Daß die zirkulare Geschwindigkeit an unserem Orte in der Tat nicht sehr weit von der "velocity of escape" entfernt ist, wird angedeutet¹ durch die volkommene Abwesenheit von großen Geschwindigkeiten relativ zum Zentroid in

einer Richtung, welche eine gerade Fortsetzung des Geschwindigkeitsvektors  $\Theta_0$  bildet. Dieses Phänomen wird sehr gut durch ein Dlagramm von J. H. OORT<sup>2</sup> veranschaulicht (Abb. 25), wo die absoluten Geschwindigkeiten für Sterne, welche große zentroidale Bewegungen zeigen, innerhalb eines Geschwindigkeitskreises vom Radius 365 km/sec gelegen erscheinen.

Oort hat eine in der Form beträchtlich verschiedene, aber der obigen prinzipiell ähnliche Behandlung des Phänomens der Asymmetrie ausgeführt.

<sup>&</sup>lt;sup>1</sup> Lindblad, V J S 61, S. 265 (1926). <sup>2</sup> B A N 4, S. 269 (1928).

Die Behandlung des stationären Zustandes in der Umgebung der Sonne ist rein analytisch, wobei eine ellipsoidische Verteilung der Geschwindigkeiten für jede Untergruppe vorausgesetzt wird. Obgleich die Oortsche Methode durch diese Annahme im ganzen etwas weniger generell als die oben gegebene wird, ist sie für unsere Umgebung gerechtfertigt, wo wir wissen, daß die ellipsoidische Verteilung als Approximation im ganzen zulässig ist, von welchem Sachverhältnis wir auch oben Gebrauch gemacht haben. Die Gleichung, welche (46) und (47) oben entspricht, ergibt sich aus (52) und schreibt sich nach Oort

$$\Theta_0^2 = -R \frac{\partial V}{\partial R} + \alpha^3 \left( \frac{R}{\nu} \frac{\partial \nu}{\partial R} + 1 - \frac{\beta^3}{\alpha^3} \right), \tag{53}$$

woraus, wenn wir mit Oort  $\Theta_0/R = 0.043$  km/sec Parsec annehmen, für die asymmetrische Drift  $S = \Theta_a - \tilde{\Theta}_a$  gilt

$$S = -11.6 \,\alpha^2 \left( \frac{1}{\text{Mod.}} \, \frac{\partial \log r}{\partial R} + \frac{1}{R} \left( 1 - \frac{\beta^2}{\alpha^2} \right) \right). \tag{54}$$

Der Gradient  $\partial \log r/\partial R$  ergibt sich als von derselben Größenordnung für verschiedene Gruppen und entspricht etwa einem Faktor 2 in der Dichtigkeit für

eine Distanz von 1000 Parsec. Für die gewöhnlichen Spektraltypen in Ström-BERGS Tabelle ergibt sich im Mittel

 $\partial \log v / \partial R = -0.00019 + 0.00005$ 

(m. F.).

Im vereinfachten Falle einer ebenen Bewegung der Sterne um ein Massenzentrum können wir mit K. F. Bott-LINGER<sup>1</sup> die Abhängigkeit der Asymmetrie von der parabolischen Grenzgeschwindigkeit und von der Konzentration der Sterne gegen das Zentrum hin anschaulich machen. Die Bahnen durch unseren Ort im System können, wie Abb. 26 zeigt, nach Exzentrizität & a-1 und Halbachsenlänge klassifiziert werden, was offenbar einer Aufteilung nach  $I_1$  und  $I_2$  entspricht, da  $I_1$  die Halbachsenlänge a, und die Flächengeschwindigkeit I2 bei gegebenem a die Exzentrizität e bestimmt, Linic von O nach einem beliebigen Punkt in der Abbildung entspricht einer Geschwindigkeit in bezug auf den Schwerpunkt des Systems, und man kann sogleich die entsprechenden Werte von a und e ablesen. Der Punkt P markiert die Kreisbewegung, S die Sonnenbewegung. Die Asymmetrie der Geschwindigkeitsverteilung, von P oder S aus gerechnet, wird um so größer, je stärker die inneren Bahnen, n < 1, im

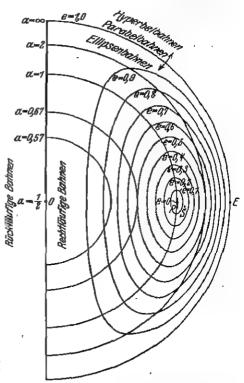


Abb. 26. Geschwindigkeitsetrenung der Bahnen durch einen gewissen Ort des Systems im Falle ebener Bewegung um ein Masson-

Vergleich mit den äußeren, a > 1, besetzt sind. Von diesem Gesichtspunkte aus

Naturwiss 19, S. 297 (1931); Berlin-Babelsberg Veröffentl 8, H. 5 (1931).

wären also die Sterne mit großer asymmetrischer Bewegung solche, die vorzugsweise in den inneren Partien des Systems vorkommen.

Es ist wohlbekannt, daß die Geschwindigkeitsellipsoide in den meisten Fällen nicht sphäroidisch mit der kürzesten Achse in der galaktischen Ebene, sondern beträchtlich gegen die galaktische Ebene abgeplattet gefunden werden. Wie oben (Ziff. 29) erwähnt, hängt dies damit zusammen, daß die Bewegung in der Ebene von zweidimensionaler Natur ist, und daß eine Ausgleichung zwischen dieser Bewegung und der allgemeineren dreidimensionalen nur sehr langsam vor sich geht. Eine starke Korrelation zwischen den Streuungen in  $\Pi$  und Z müssen wir jedenfalls voraussetzen, was auch der empirischen Erfahrung entspricht. Es ist dann aber klar, daß Gruppen von verschiedener Rotationsgeschwindigkeit und verschiedener Streuung, also verschiedene Untersysteme, auch ver-

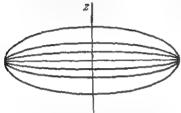


Abb. 27. Schematischer Meridionalschnitt durch das Sternsystem. Die Grenzflächen repräsentieren verschiedene Untersysteme.

schiedene Konzentration gegen die galaktische Ebene zeigen müssen. Wenn wir einen Meridionalschnitt durch die "effektiven Begrenzungsflächen" ziehen, so bekommen wir also die schematische Darstellung der Untersysteme, welche in Abb. 27 gegeben ist.

Wir können jedenfalls auf die Bewegung in z senkrecht zur Milchstraßenebene das Massen-

bewegungsgesetz

$$\frac{\partial (\nu \overline{Z^{\mathbf{a}}})}{\partial z} = \nu \frac{\partial V}{\partial z} \tag{55}$$

anwenden. Eine unmittelbare Verwendung kaun diese Formei für die A-Sterne erhalten, da diese praktisch in einem so dünnen Stratum enthalten sind, daß wir annehmen können

$$\frac{\partial V}{\partial z} = -4\pi G \varrho z, \tag{56}$$

wo  $\varrho$  die Dichtigkeit des zentralen galaktischen Stratums ist. Wenn  $v_0, z_0, Z_0$ die für die A-Sterne nahe unserem Punkte im System geltenden Werte der Dichtigkeit, Distanz von der Symmetrieebene und Geschwindigkeitsstreuung

Dichtigkeit, Distanz von der Symmetrieebene und Geschwindigkeitsstrettung in 
$$Z$$
 sind, so haben wir 
$$Z_0^2 = -\int_{z_0}^{\infty} \frac{\partial V}{\partial z} dz = 4\pi G \varrho \int_{z_0}^{\infty} \frac{v}{v_0} z dz.$$
 (57)

Wir können für  $z_0$  den Wert 30 Parsec annehmen und für  $\nu/\nu_0$  z. B. die von Petersson und Lindblad (Ziff. 19) hergeleitete Veränderung der Dichtigkeit mit der Entfernung von der Milchstraßenebene. Für Ze hat Strömberg 9,1 km/sec gefunden. Nach Ausführung einer numerischen Integration finden wir dann für  $\rho$ , in Sonnenmassen per Kubikparsec ausgedrückt, den Wert

$$\varrho = 0.11$$

was mit anderen Schätzungen der Dichtigkeit in unserer Umgebung ziernlich übereinstimmt.

Eine ähnliche Untersuchung hat Bottlinger für die Sterne von großer absoluter Leuchtkraft ausgeführt. Aus dem durchschnittlichen Abstand der hellen Sterne von der Milchstraßenebene (etwa 40 Parsec) läßt sich mit Hilfe der Masse und der Dimensionen des großen Systems (vgl., Ziff. 33) eine Geschwindigkeitsstreuung von 3,6 km/sec berechnen. Eine sorgfältige Diskussion der Radialgeschwindigkeiten ergibt das Resultat, daß die Streuung der O- und

<sup>1</sup> L, c.

B-Sterne im Rahmen dessen liegt, was man nach der Rotationstheorie erwarten muß.

Eine sehr ausführliche Arbeit über diesbezügliche Fragen ist ganz kürzlich von OORT1 veröffentlicht worden. Wenn wir die senkrecht zur Milchstraßenebene wirkende Kraftkomponente  $\partial V/\partial z$  mit K(z) bezeichnen und diese als im wesentlichen in der Bewegung eines Sterns von R unabhängig betrachten, so haben wir für die Bewegung in Z, gemäß dem zweiten Teil unserer Gleichung (35) oben,

 $Z_0^2 = Z^2 - 2 \int_A^z K(z) dz$ , (58)

und es ist leicht einzusehen, z. B. durch unsere Gleichung (37) oben, daß im Falle einer stationären Verteilungsfunktion  $\varphi(z,Z)$  diese einfach eine Funktion von  $Z_0$ sein wird. Im Falle einer Gaussschen Verteilung der Geschwindigkeiten für z = 0 haben wir

$$\varphi(0, Z) = \nu_0 \frac{l}{\sqrt{\pi}} e^{-l^2 Z_0^2}, \tag{59}$$

und also für beliebige z-Werte

$$\varphi(z,Z) = \nu_0 e^{2\pi \int_0^z H(z) dz} \cdot \frac{l}{\sqrt{\pi}} e^{-l^n Z^n}, \qquad (60)$$

woraus wir ableiten

$$v(z) = v_0 e^{2v \int_0^z K(z) dz}$$
 (6i)

Diese Formel ist identisch mit der von Kapteyn für einen analogen Zweck benutzten (Ziff. 28). Wenn wir die empirische Geschwindigkeitsverteilung als eine Summe von Gaussschen Verteilungen approximieren, welche je die Bruchteile  $\theta_1, \theta_2, \ldots$ , der Sterne in unserer Nähe umfassen, so bekommen wir

$$\nu(s) = \nu_0 \left\{ \theta_1 e^{\frac{2i\eta}{\delta} \int_0^s K(s)ds} + \theta_2 e^{\frac{2i\eta}{\delta} \int_0^s K(s)ds} + \cdots \right\}. \tag{62}$$

Durch die statistisch ermittelten  $\nu(z)$  und gegebene Werte der  $\theta$  und l können wir die Funktion K(z) in sukzessiver Approximation ermitteln.

Oorr bestimmt aus den Radialgeschwindigkeiten für verschiedene Sterntypen die Streuung in den vertikalen Geschwindigkeitskomponenten Z, woraus die Werte von I sich ergeben. Hauptsächlich unter Benutzung der van Rhijnschen Resultate für die Dichtefunktion in hohen galaktischen Breiten (für A-Sterne

und Riesensterne von spätem Typus werden auch die oben erwähnten Resultate von LINDBLAD und PETERSSON zum Vergleich herangezogen) berechnet Oort die Funktion K(z) für z zwischen 0 und 600 Parsec. Das Hauptresultat wird in Tabelle 21 wiedergegeben, wo K in cm/sec<sup>2</sup> ausgedrückt ist. Der numerische Wert von K (z) wächst linear bis ungefähr in der Höhe von 200 Parsec, der Gang mit z wird dann beträchtlich langsamer. Wenn umgekehrt für die Dichtefunktion der Ausdruck (62) angenommen wird, kann man aus ihm und aus der als bekannt vorausgesetzten Leuchtkraftsfunktion die Sternzahlen für verschiedene scheinbare Größen berechnen, und als Kontrolle werden von Oort weitläufige Rech-

Tabelle 21.					
g	K(z)·10 <sup>a</sup>				
50 100 150 200 250 300 400 600	-0,77 1,55 2,59 3,52 3,78 3,86 3,68 4,44				

nungen dieser Art ausgeführt. Da eine Berechnung der Sternzahlen der schwächsten Größen Kenntnis von K(z) bis zu etwa 5000 Parsec voraussetzt, so kann

<sup>&</sup>lt;sup>1</sup> II A N 6, S. 249 (1932).

man aus diesen Sternzahlen eine grobe Kontrolle etwaiger Extrapolationen von K(z) für große Höhen bekommen, eine Möglichkeit, die auch von Oort ausgenutzt wird, doch vorläufig ohne definitive Resultate. Den Verlauf der Sternzahlen mit galaktischer Länge nach Seares benutzt Ookt, um den Gradienten  $\partial \log r/\partial R$  zu berechnen, welchen Wert er im Mittel zu -0.0003, in guter Ubereinstimmung mit dem oben besprochenen Resultat aus der asymmetrischen Drift, berechnet. Ein Schnitt der Dichtigkeitsflächen senkrecht zur Milchstraße in der Richtung  $L = 320^{\circ}$  gibt für hohe galaktische Breiten Kurven, die sehr wehl als Ellipsen mit Zentrum in der Milchstraßenebene in der Entfernung 10000 Parsec angesehen werden können. Die Ellipse, bei der die Dichte des photographischen Lichts 1/95 der entsprechenden Dichte in der Nübe der Sonne ist, hat die Achsen a=12200, b=1340, und die Ellipse für die Dichte  $\frac{1}{100}$ die Achsen a = 14300, b = 2240, in Parsec ausgedrückt. Oort herechnet aus K(s) unter verschiedenen schematischen Annahmen über die Massenverteilung im System die Totaldichte e der Materie in der Umgebung der Sonne. Er findet Werte zwischen 0,079 und 0,108 Sonnenmassen per Kubikparsec, womit offenbar LINDBLADS oben gegebener Wert gut übereinstimmt. KAPTEYN hatte den Wert 0,099 gefunden, JEANS aus der Sternströmungstheorie (Ziff. 28) 0,143. Durch Vergleich mit der wahrscheinlichen Anzahl von Sternen per Volumeneinheit zieht Oort den Schluß, daß Nebel und Meteore zusammen zu der Totalmasse weniger als die Sterne beitragen, möglicherweise sogar viel weniger.

81. Differentielle Rotationseffekte in den beobachteten Geschwindigkeiten. Nach der eben besprochenen Theorie liegt die Richtung der asymmetrischen Verschiebung der Geschwindigkeitsmittelpunkte senkrecht zur Richtung von uns nach dem Zentrum des Systems. Die asymmetrische Verschiebung ist eine differentielle Rotation verschiedener Gruppen von Objekten relativ gegeneinander. Vom Nordpol der Milchstraße gesehen, geht die Rotation in retrograder Richtung.

von links nach rechts.

Es ist aber J. H. Oort¹ gelungen, auf anderem Wege eine Bestimmung der Lage des dynamischen Zentrums zu gewinnen. Die mittleren Geschwindigkeiten  $\Theta_0$  sind überall senkrecht zum Radiusvektor gerichtet, werden ja aber nicht unmittelbar beobachtet. Was in der Beobachtung gemessen wird, ist die vektorielle Differenz zwischen  $\Theta_0$  und der Geschwindigkeit der Sonne. Wir betrachten jetzt Sterne in der galaktischen Ebene in der Entfernung r von uns. Die eben erwähnte vektorielle Differenz zerlegen wir in ihre Komponente längs r, die Radialgeschwindigkeit, und ihre Komponente senkrecht zu r, die transversale Geschwindigkeit. Durch Abziehen der Komponenten der Sonnenbewegung in bezug auf die umgebenden Sterne der betreffenden Klasse bekommen wir Residuen, welche die vektorielle Differenz zwischen den ringsherum im Abstande r geltenden  $\Theta_0$ -Werten und dem  $\Theta_0$ -Wert des Sonnenorts derstellen. Wenn r gegen R klein ist, bekommen wir dann für die Radialgeschwindigkeiten eine Abhängigkeit von der galaktischen Länge der beobachteten Objekte von der Form

$$rA\sin 2(L-L_0), \tag{63}$$

wo  $L_{\mathbf{0}}$  die galaktische Länge des Zentrums ist, und für die transversalen Geschwindigkeiten

$$rA\cos 2(L-L_0)+rB, \tag{64}$$

Wo

$$A = \frac{1}{2} \left( \frac{\Theta_0}{R} - \frac{\partial \Theta_0}{\partial R} \right), \quad B = \frac{1}{2} \left( -\frac{\Theta_0}{R} - \frac{\partial \Theta_0}{\partial R} \right). \tag{65}$$

<sup>&</sup>lt;sup>1</sup> BAN 3, S. 275; 4, S. 79 u. S. 91 (1927).

Wir haben also  $B = A - \omega$ , wo  $\omega = \frac{1}{R} \Theta_0$  die Winkelgeschwindigkeit der Rotationsbewegung ist. In dem speziellen Falle, wo  $\Theta_0$  die Geschwindigkeit der zirkularen Bewegung ist, also wenn die Dispersion  $\alpha$  sehr klein ist, haben wir

$$A = \frac{1}{4} \left( \omega + \frac{1}{\omega} \frac{\partial^2 V}{\partial R^2} \right). \tag{66}$$

In Übereinstimmung mit den Ergebnissen aus dem Phänomen der Asymmetrie setzen wir voraus, daß  $\omega$  eine retrograde Bewegung ist, also eine Rotation von links nach rechts, wenn sie von einem Punkte nördlich von der galaktischen Ebene betrachtet wird. Die transversale Geschwindigkeit wird im Sinne wachsender galaktischer Länge gezählt. Für die mittleren Eigenbewegungen in galaktischer Länge bekommen wir, wenn A und B in Kilometern per Sekunde für die Entfernung von einem Parsec und die Eigenbewegungen in Bogensekunden ausgedrückt werden,

$$4,74 \,\mu_L = A\cos 2\left(L - L_0\right) + B. \tag{67}$$

Die oben gemachten Ansätze haben viel gemeinsam mit den Gedanken, welche zuerst Gylden in einer Arbeit entwickelte, in der die Sternbewegungen mit den geozentrischen Bewegungen der kleinen Planeten verglichen wurden. GYLDEN entwickelt die mittleren Eigenbewegungen in Rektaszonsion (a) für verschiedene α innerhalb einer Deklinationszone in eine Fouriersche Reihe, deren einzelne Glieder von den sin und cos für sukzessive Viclfache von & abhängig sind. Als Terme von reeller Bedeutung behandelt er besonders den konstanten Term und die Terme in α und 2α, Die Terme in α geben den Reflex der Sonnenbewegung in bezug auf die betrachteten Sterne (sind aber zum Teil auch von galaktischen Rotationseffekten oben beschriebener Art bedingt); für den Apex findet Gylden hieraus  $\alpha = 270^{\circ}$ . Die übrigen Terme deuten aber nach ihm auf eine allgemeine Umlaufsbewegung der Sterne um ein gemeinsames Zentrum hin. Zwar bekommt GYLDEN aus seinem Material, speziell nach einer Korrektion der Präzession von Nyren, einen konstanten Term, der einer direkten Rotationsbewegung entspricht. Aus der qualitativen Übereinstimmung der Koeffizienten der Entwicklung mit denen der geozentrischen Bewegungen der kleinen Planeten am 21. März 1868 zieht er weiter den Schluß, daß das Zentrum des Sternsystems in einer Richtung liegt, deren R.A. mit der R.A. der Sonne in der späteren Hälfte des März zusammenfällt, also in der Himmelsregion zwischen Auriga und Cygnus. Wenn man aber eine retrograde Bewegung voraussetzt, bekommt man aus GYLDENS Koeffizienten für cos 2 a und sin 2a die Werte -1".21 und -0".40 pro 100 Jahre und für das Zentrum zwei um 180° verschiedene alternative Werte, von denen der eine einer galaktischen Länge des Zentrums von 359° entspricht, was in ziemlich guter Übereinstimmung mit unseren jetzigen Ansichten steht.

In besonders interessanter Weise hat S. Oppenheim die Gyldenschen Ideen weiter zu entwickeln gesucht und für die spezielle Klasse der B-Sterne die harmonische Analyse auch auf die Radialgeschwindigkeiten ausgedehnt. Sein Ziel war zuerst, unter Voraussetzung einer Analogie mit den kleinen Planeten, die Bahnebene der Bewegungen zu ermitteln und durch harmonische Analyse der Bewegungen parallel dieser Ebene die Lage des Bewegungszentrums zu finden. Er führt später, im Anschluß an die Bessel-Koboldsche Methode zur Apexbestimmung in Harzers Ausführung, ein "Momentenellipsold" ein (das

Overs K Vetenskapsakad Förhandl 28, S. 956 (1871).

A N 188, S. 137 (1911); Wien Denkechr Math Nat Kl 87, S. 297 (1912); Astron Kal 1913, S. 126; Wien Denkschr Math Nat Kl 92; A N 201, S. 241 u. 417 (1915); Wien Denkschr Math Nat Kl 93; A N 202, S. 89 (1916); 204, S. 447 (1917); Seeliger-Festschr S. 131 (1924);

von dem Momentenellipsoide in Charlier-Wicksells statistischer Theorie der zentroidalen Bewegungen zu unterscheiden ist) von der Form

$$Ax^{2} + By^{2} + Cz^{2} + 2Dyz + 2Ezx + 2Fxy = 1,$$
 (68)

wo

$$A = \Sigma(ll),$$
  $C = \Sigma(nn),$   $E = \Sigma(nl),$   
 $B = \Sigma(mm),$   $D = \Sigma(mn),$   $F = \Sigma(lm),$   
 $l = \sin i \sin \Omega,$   $m = -\sin i \cos \Omega,$   $n = \cos i.$  (69)

 $\Omega$  und i sind die R.A. des aufsteigenden Knotens und die Neigung des Bewegungskreises eines Sterns. Die größte Achse dieses Ellipsoids soll gegen den Apex der Sonnenbewegung, die mittlere Achse gegen das Zentrum der Bewegung und die kleinste Achse gegen den Pol der Bewegungsebene zeigen. Aus den Eigenbewegungen der Sterne ergeben sich aber zwei Bestimmungen dieses Ellipsoids, da die Werte von  $\Omega$  (nach einer einheitlichen Regel bestimmt) zwei voneinander sehr verschiedene Gruppen andeuten, die auch räumlich voneinander getrennt sind. Nach Vertauschung der zwei kleineren Achsen in dem sekundären Ellipsoid, das sonst keine verständliche Beziehung zur Milchstraßenebene zeigt, werden die Achsenrichtungen jedoch fast identisch und ein Mittel kann gebildet werden. Die Theorie ergibt, auf die Bewegungen der kleinen Planeten und der Kometen angewandt, sehr interessante und zum Teil leicht interpretierbare Resultate.

Für die Sterne des Boss-Kataloges findet Oppenheim als Mittel für die Hauptrichtungen der zwei Ellipsoide in der oben gegebenen Ordnung

$$\alpha_1 = 271^\circ,5 
\delta_1 = +32^\circ,3$$
 $\alpha_8 = 31^\circ,4 
\delta_2 = +38^\circ,1$ 
 $\alpha_8 = 155^\circ,1 
\delta_3 = +35^\circ,2$ 

Die erste Richtung ist in guter Übereinstimmung mit dem allgemein angenommenen Apexwert, die letzte zeigt gegen eine hohe galaktische Breite ( $+60^{\circ}$ ). Die der zweiten Richtung gerade entgegengesetzte am Himmel, die ebensogut die Richtung gegen das Zentrum andeuten kann, entspricht den galaktischen Koordinaten  $L=288^{\circ}$ ,  $B=+21^{\circ}$ , also einem Punkte, der nicht allzu weit von Shapleys Anhäufungspunkt der Kugelhaufen entfernt ist.

Oorr hat in erster Linie die Radialgeschwindigkeiten für Objekte von großer Entfernung in niedrigen galaktischen Breiten untersucht, um die Existenz des Rotationstermes (63) nachzuweisen. Es stellte sich bei dieser Untersuchung heraus, daß entfernte Objekte von verschiedener physikalischer Natur im ganzen miteinander wohl übereinstimmende Werte von  $L_0$  und A ergaben. Für die

Tabelle 22.

Стирре	L <sub>0</sub>	m.F.
B3-B5	322°	士 5°
$A-G\left\{ \begin{array}{l} \mu < 0'',020 \\ 4,0 < m \le 5.8 \end{array} \right\}$	345	士 9
B0−B2	322	± 5
c-Sterne m < 5.0	330	士 8
$A - G \left\{ \begin{array}{l} \mu < 0'', 020 \\ m > 5.8 \end{array} \right\} \dots$	337	± 8
Oo5	308	土 7
с-Sterne ж ≧ 5.0	321	± 4
Planet, Nebel	333	土10

Länge des Attraktionszentrums erhielt Oort die Werte in Tabelle 22, wo die Gruppen grob nach mittlerer Entfernung (von 300 bis etwa 1200 Parsec) angeordnet worden sind. Das unter Berücksichtigung der Gewichte berechnete Mittel für  $L_0$  wird  $324^{\circ}\pm 2^{\circ}$  (m. F.), was offenbar sehr gut mit Shapleys Konzentrationspunkt für die Kugelhaufen übereinstimmt und sich

auch mit der Länge des Zentrums, wie sie aus der Asymmetrie der Geschwindigkeitsverteilung (Ziff. 30) hervorgeht, gut verträgt.

Für den Koeffizienten A ergab sich im Mittel +0,019 km/sec per Parsec ±0,003 (m.F.). Da A die Abweichung von einer gleichförmigen angulären Rotations-

geschwindigkeit mißt, so ist also gemäß diesen Resultaten die vektorielle Differenz der Rotation im oben angegebenen Sinne oder die "differentielle Rotation", innerhalb unserer Umgebung des Sternstratums nachweisbar Es deutet dies a.n., daß das Gravitationsfeld an unserem Ort im System nicht etwa dem Felde eines homogenen Rotationsellipsolds in seiner Äquatorebene entspricht, sondern, mit diesem Fall verglichen, auf eine merkliche Verdichtung der Materie gegen die zentralen Regionen des Systems schließen läßt

Um aber eine entscheidende Evidenz für die Realität der differentiellen Rotation zu bekommen, müssen auch die Effekte (67) in den Eigenbewegungen untersucht werden. Oort hat die Eigenbewegungen des Preliminary General Catalogue von Boss behandelt Korrektionen für die Bewegung des Frühlings-Dunktes und für die Prazessionakonstante wurden aus den Bewegungakompomenten in galaktischer Breite bestimmt. Als Korrektionen der Newconnschen Werte für die zwei erwähnten Größen findet Oort  $+0^{\circ},0137 \pm 0^{\circ},0020$  (m F) lozw, +0'',0113  $\pm 0''$ ,0020 (m.F). Als Wert der Lumsolarpräzession ergibt sich also 50",3821 (1900) Die korrigierten Eigenbewegungen in galaktischer Länge wurden zur Bestimmung von  $L_a$ , A und B benutzt. Die Werte von  $L_a$  stimmen gut mit den oben gegebenen, aus den Radialgeschwindigkeiten ermittelten fiberein, während A nicht unerheblich kleiner als der oben gegebene Wert ausfällt, was aber nach Oort sohr wohl durch Fehler in den Eigenbewegungen, speziell für Sterne in der südlichen Milchstraße, verursacht sein kann. Für die mittlere Bowegung B/4.74 längs der Milchstraße gibt Oort, gemäß den Resultaten für drei Gruppen von sehr entfornten Sternen, als wahrscheinlich besten Wert -0",0050 oder B = -0.024 km/sec per Parsec  $\pm 0.005$  (m.F) (vgl Ziff. 26 and 32)

Zur weiteren Beleuchtung des überaus wichtigen Effektes der differentiellen Rotation in den Radialbewogungen konnte J S Plaskett<sup>1</sup> ein vorzügliches neues Material von Goschwindigkeiten für Wolf-Rayer- und Helium-Sterne ausnutzen, die auf dem Observatorium in Victoria gemessen worden sind Für die Rotationsgrößen  $L_0$  und tA und den K-Term hat er die in Tabelle 23 aufgeführten Werte mit den angegebenen wahrscheinlichen Fehlern gefunden Im Mittel bekommt Plaskett hier  $L_0 = 324^\circ, 5 \pm 1^\circ, 8, A = +0.0155 \pm 0.0007 \,\mathrm{km/sec}$  per Parsec.

Tabolle 23

Rieme und Größ	•		1.0	L,	E lon/sea	FA hoo/was
B0-B2 <6,21 B0-B2 >6,20 B3-B5 <6,21 B3-B5 >6,20		66 66 181 175 65	5,00 6,94 5,16 6,79 6,43	332°,7 ± 9,8 328 .5 ± 3,0 308 .5 ± 2,6 325 .0 ± 2,1 322 .3 ± 7,2	+3.2 ± 1.0 -0.4 ± 0.9 +0.9 ± 0.3 -1.2 ± 0.3 +5.8 ± 2.9	+ 5.9 ± 0.9 +16.7 ± 1.1 + 4.8 ± 0.5 + 5.9 ± 0.3 +17.1 ± 4.0

Eine schr große Bedeutung hat gegenwärtig die Theorie der differentiellen Rotation für die Erschelnung der "stationären" Kalziumlinien (Ziff. 25) gewonnen. Oort berechnete den Rotationskoeffizient für 40 Ca<sup>+</sup>-Geschwindigkeiten zu +5,6 km/sec ± 2,2 (m F.). Gerasimovič und O. Struve<sup>3</sup> haben dann die galaktische Rotation des interstellaren Kalziums aus den Ca<sup>+</sup>-Geschwindigkeiten für 103 Sterne vom Typus O-B2 studiert. Der Koeffizient 7A für die "Wolken" ergibt sich zu +5,3 km, während für die Sterne selbst +12,0 km aus Plasketts obenerwähnten Werten berechnet wurde Das Verhältnis 1 2,3 zwischen den mittleren Entfernungen wurde als Zeugnis für eine approximativ gleichförmige Verteilung des Kalziums gemäß Eddingtons Hypothese betrachtet.

<sup>&</sup>lt;sup>1</sup> M N 88, S. 395 (1928)

Einen ungemein großen Fortschritt zur Aufklärung der diesbeztiglichen Verhältnisse bedeutet aber vor allem die Arbeit von J. S. Plaskert und J. A. Pearce1, die im wesentlichen auf dem umfangreichen Material von Goschwindigkeiten für B0-B5-Sterne heller als 7m,5 visuell und nördlich von der Dekl. -11° beruht, welches in den letzten Jahren auf dem Observatorium in Victoria ge-sammelt worden ist. Für 261 Sterne, deren galaktische Verteilung in Abb. 28 dargestellt wird, sind Ca+-Geschwindigkeiten vorhanden. Mit einer angenommenen Sonnengeschwindigkeit von +20.0 km gegen den Apex  $L=21^{\circ}.8$ ,  $B=+20^{\circ}$  ergaben sich für den K-Term und die Rotationsgrößen die Resultate  $K=-0.61\pm0.57$  km,  $rA=+7.90\pm0.79$  km,  $L_0=331^\circ.7\pm5^\circ.7$ . Der Rotationskoeffizient kommt also hier mit einem Werte heraus, der zehn mal größer als sein wahrscheinlicher Fehler ist. Die Länge La erscheint fast exakt um 90° gegen Strömbergs Asymmetrielinie gedreht.

Die 235 Sterne, für welche sowohl "stellare" als "interstellare" Gosch windigkeiten vorliegen, wurden zuerst in Gruppen nach scheinbarer Größe geteilt und

Tabelle 24. Gruppierung nach Größe,

iii ii	п	r.A		n rA K		ζ
		Sterne	Wolken	Stema	Wolken	
4,41 5,60 6,03 7,08 7,34	37 45 79 119 69	+ 1,81 ± 2,83 +10,26 ± 2,12 +13,86 ± 1,75 +16,58 ± 2,20 +20,49 ± 2,32	+ 3,85 ± 1,22 + 5,02 ± 1,24 + 7,66 ± 0,90 + 8,31 ± 1,36 +10,08 ± 1,57	+7.12 ± 1.42 +3.99 ± 0.96 +1.67 ± 0.77 +1.39 ± 1.46 +2.34 ± 0.86	+0,02 ± 0,61 +0,97 ± 0,56 +0,09 ± 0,40 -0,69 ± 0,90 +0,23 ± 0,56	

innerhalb jeder Gruppe ist dann der Rotationskoeffizient FA und der K-Term sowohl für Sterne als für Wolken bestimmt worden. Pür  $L_0$  wurde hier immer der Wert 325° angenommen. Die Resultate sind in Tabelle 24 aufgeführt.

Für die vier letzten Gruppen, in mittleren Entfernungen von etwa 600. 800, 1000 und 1200 Parsec, ist das Verhältnis der Rotationskoeffizienten 7A für Sterne und Wolken der Reihe nach 2,04, 1,81, 1,99, 2,03 oder im Mittel 1,97. Die Eddingtonsche Hypothese, daß die interstellare Materie gleichförmig verteilt ist, wird also hier in außerordentlich deutlicher Weise bestätigt.

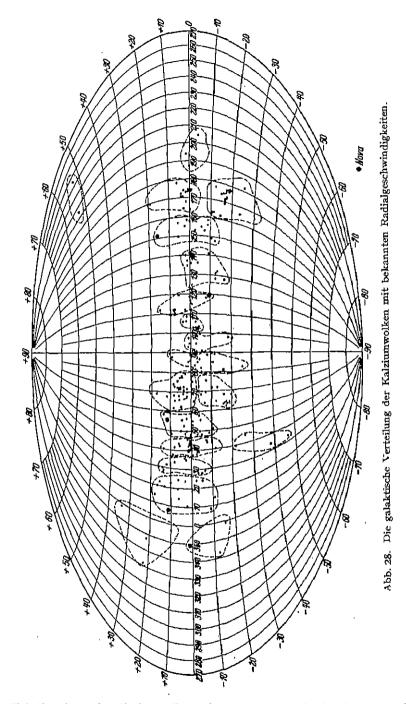
Ähnliche Resultate gibt eine Einteilung des Materials nach der Intensität der interstellaren K-Linie, wie Tabelle 25 zeigt. Die erste Kolumne gibt die benutzten Intervalle in Intensität in einer konventionellen Skala,

Tabelle 25. Gruppierung nach Intensität der interstellaren Linian.

Inten	ulust	Ī.	A	. ,	
Intervall	Mittel	Storne	Wolken	Stame	Wolken
6,0-6,9 4,4-6,9 7,0-7,9 8,0-9,5	4,72 6,50 6,08 7,46 8,42	+ 3.64 ± 3.25 + 12.12 ± 1.88 + 10.22 ± 1.72 + 14.53 ± 2.93 + 27.52 ± 2.46	+ 4.97 ± 0.77 + 4.93 ± 0.92 + 5.03 ± 0.85 + 6.91 ± 1.06 + 13.72 ± 1.16	+6,12 ± 2,14 +4,66 ± 1,27 +5,24 ± 1,17 -0,14 ± 1,95 +3,18 ± 1,74	+1,15 ± 0,50 +0,10 ± 0,62 +0,10 ± 0,58 -0,21 ± 0,70 -1,17 ± 0,82

Es stellt sich heraus, daß die Intensität der interstellaren Linie ein besseres Entfernungskriterium als die scheinbare Größe ist. Aus den Werten von 7/1 für die letzte Gruppe der Tahelle kann man die mittlere Entfernung zu etwa 1600 Parsec berechnen. In wie hohem Maße der Rotationsterm  $rA\sin 2(L-325)$ die Geschwindigkeiten innerhalb der einzelnen Längengruppen wiedergibt, zeigt

<sup>&</sup>lt;sup>1</sup> M N 90, S. 243 (1930).



uns die Tabelle 26, wo für die letzte Intensitätsgruppe die beobachteten und die berechneten Geschwindigkeiten relativ zum Zentroid für verschiedene galaktische Längen gegeben worden sind.

Tabelle 26.

Mittlere		Ste	rne	Wolken	
Lange	п	Beob.	Bor,	Beob.	13er.
358"	2	+35,7	+24,3	+ 8,2	-1-9,4
17	2	+12.2	+29,5	+ 6,1	41175
34	6	+21.5	+21,3	十 7.5	十7.9
47	2	+11.8	+10,4	+ 6,6	+ 2,4
70	12	- 3.4	~- 10,4	5.4	- 8,0
97	4	<b>-26,8</b>	23,4	15,5	-14,3
107	9	-28,4	-23,5	<b>₩17,7</b>	14,5
141	4	- 4,1	- 0,9	+ 1,2	- 3,2
169	2	+13,6	+16,0	+ 1,9	5,3

Oort hat eine Auflösung für diese Gruppe allein mit Lo, rA und K als Unbekannten gemacht, wobei die Bestimmung von  $L_0$  beträchtliches Gewicht hat. Er bekommt als Resultat die folgenden Werte:

Sterne	Wolken				
$L_0 = 330^{\circ}, 1 \pm 2^{\circ}, 6 \text{ (w.f.)}$	$L_0 = 329^{\circ}, 3 \pm 4^{\circ}, 3 \text{ (w.F.)}$				
7A = 26,0 ± 2,2 km/sec	7A = 12,4±1,7 km/sec				
$K = +0.9 \pm 1.6$	$K = -2,2 \pm 1,2,$				

Es ist ohne weiteres augenscheinlich, in welch hohem Grade die Resultate von Plaskett und Pearce unsere Vorstellungen fiber die allgemeinen Eigenschaften des rotierenden Sternsystems stützen, erstens durch die Bestätigung des Rotationseffektes selbst und zweitens durch den Schluß auf eine gleichförmige Verteilung der interstellaren Materie in der galaktischen Ebene innerhalb eines sehr weiten Kreises um uns herum. Keines von diesen Ergebnissen läßt sich wohl mit der Existenz eines lokalen Systems vereinigen, wenn mit diesem Ausdruck irgendeine dynamisch abgeschlossene Einheit gemeint wird,

Eddingtons hat auch hervorgehoben, daß die Existenz einer derartigen Schicht von dünnem Gase, die sich gegen das Zentroid der in ihr eingelagerten Sterne in Ruhe befindet, die beste Stütze dafür ist, daß die Bewegung des Zentroids relativ zum Schwerpunkt des Systems eine Kreisbahn beschreibt. Denn da das interstellare Gas zu gleichförmig verteilt erscheint, um wesentlich von irgendeinem hydrodynamischen Druckgradienten gegen die Attraktion des Systems getragen zu sein, so muß das Gleichgewicht durch die Zentrifugalkraft allein bewirkt werden und demnach die mittlere Bewegung innerhalb eines Elementarvolumens des Gases mit der Kreisbewegung übereinstimmen. In dieser Weise können wir mit Eddington behaupten, daß schon die Existenz der kosmischen Wolken ein Beweis für die Existenz der Rotation ist. Der Beweis für die Kreisbewegung ist übrigens analog mit unserem oben (Ziff. 29) für die Storne von kleiner Geschwindigkeitsdispersion gegebenen.

Es ist aber an sich sehr bemerkenswert, wie Eddington und Oort hervorheben, daß die Bewegung der Wolken so exakt mit dem Zentroide der Sternbewegungen zusammenfällt (nach Oorr innerhalb 1 km/sec), wenn wir bedenken, daß die Rotationsgeschwindigkeit auf ungefähr 300 km/sec zu schätzen ist.

In den oben referierten Arbeiten von Oort und von Plaskett und Plarce sind besonders Gruppen von Objekten mit großer mittlerer Entfernung und mit kleiner Streuung in den zentroidalen Geschwindigkeiten behandelt worden. Es sind aber auch Versuche gemacht worden, die Rotationsgrößen für ein mehr normales Material zu bestimmen. Es ist klar, daß die Schwierigkeiten, ein zu-

<sup>1</sup> BAN 5, S. 192 (1930).
2 The Rotation of the Galaxy. Halley Lecture. Oxford; Clarendon Press (1930).

verlässiges Resultat zu bekommen, mit abnehmender mittlerer Entfernung (wolche direkt auf die Amplitude 7A dinwirkt) und mit einer stoigenden Streuung der Geschwindigkeiten (wolche den Ausgloich der partikularen Bewogungen herabsetzt) erheblich wachsen. Im Falle der Elgenbewegungen bleibt zwar die Rotationsgröße dieselbe, wird aber mit abnehmender Entfernung immer kleiner im Verhältnis zur mittleren Eigenbewegung der Storne Eine Tatsache betreffs der Rotationseffekte für die gewöhnlichen Riesensterne der Spektralklassen A bis K scheint jedoch ziemlich wohl begründet. Es stellt sich heraus, daß die Länge  $L_0$  des Rotationszentrums ein wenig höhere Worte als für die entfernteren Objekte von kleinerer Streuung in den Geschwindigkeiten annimmt Dieses Phinomen ist schon durch Oorrs Resultate in Tabolle 22 angedeutet worden, wo für die A bis G-Sterne Lo = 345° bzw 337° gefunden wurde Lindblad findet für die Storne vom Typus F bis K und  $\mu < 0^{\prime\prime}$ ,040 den Wert  $L_0 = 346^{\circ}$  Redman<sup>3</sup> findet für 425 K-Sterne im Größenintervall 7,0 bla 7,5 und größtenteils innerhalb ±10° galaktischer Breite, deren Radialgeschwindigkeiten von ihm selbst in Victoria bestimmt worden and, die differentielle Rotation  $7A = 1.9 \pm 1.3$  km/sec,  $L_0 = 17^{\circ} \pm 18^{\circ}$  (w F) Die Sterne in diesem Material zeigen aber eine ziemlich große Streuung in den Geschwindigkeiten, und nach gewissen Eigenschaften der Frequenzkurve der Geschwindigkeiten in verschiedenen Gegenden des Himmels scheint es sehr wohl möglich, daß spezielle Strömungen unter den Sternen auf das Resultat ungünstig eingewirkt haben H Nordström hat deshalb, anstatt das arithmetische Mittel der Geschwindigkeiten verschiedener Gegenden zu benutzen, in einem Ausgleichungsvorfahren die Goschwindigkeit maximaler Frequonz für jedes Arcal bestimmt und in die Gleichungen für die differentielle Rotation elegesetzt. Er findet dann aus REDMANS Material im Mittel 7A = 3.0.  $L_{\bullet} = 333^{\circ}$ , was als ganz normal anzuschon ist und auch sehr wohl mit seinen Resultaten für K- und M-Sterne heller als 6m,0 übereinstimmt

Es lat von großem Interesse, die eben erwähnten Resultate mit den aus einer Behandlung der Eigenbewegungen gewonnenen zu vergleichen. Für eine gesammelte Gruppe von B-, c-, O-, N- und  $\delta$  Cephel-Sternen (also sehr entfernten Objekten) hat Oort gefunden  $A = +0'',0024 \pm 0'',0016$  (m F.),  $B = -0'',0050 \pm 0'',0011$  (m F.),  $L_0 = 326^{\circ} \pm 17^{\circ}$  (m F.), während Dyson's für B0- bis A0-Sterne die fast identischen Werte A = +0'',0025, B = -0'',0046,  $L_0 = 326^{\circ}$  erhält. J. Schilt's, der speziell die Eigenbewegungen verschiedener AG-Zonen auf die diesbezüglichen Effekte hin analysiert hat, findet aber folgende Worte

J. E. MERRILL<sup>6</sup> findet aus dem Yale-Katalog für nördl Dekl 50° bla 55°,  $A = +0^{\circ},0073$ ,  $L_0 = 0^{\circ}$ 

Da unter den von Schut und Merrill untersuchten Zonensternen die Mehrheit normale Riesensterne vom Typus A bis K sein werden, so können die eben gegebenen Resultate an die Seite der aus den Radialgeschwindigkeiten für diese Typen hergeleiteten gestellt werden. Es ergibt sich also ein höherer Wert der galaktischen Länge des Zentrums  $L_{\rm o}$ ; außerdem geben offenbar die

M N 90, S 503 (1930) — Stockholm Medd 5

M N 90, S 690 (1930), 92, S 107 (1931), Publ Astrophys Obs Viotoria (IV) Nr. 20 (1930) Lund Medd 131 (1933) M N 90, S. 239 (1930).

Wash Nat Ac Proo 13, 8 642 (1927), A J 38, S. 149 (1928); 39, S 17 (1928).
A J 39, S. 90 (1929)

Daten aus den Eigenbewegungen der Zonensterne einen ziemlich hohen Wert für den Amplitudenfaktor A. Zum Vergleich mag erwähnt werden, daß der Wert A = +0,0155 km/sec per Parsec aus den Radialgeschwindigkeiten, durch Division mit 4.74, dem Werte  $A = +0^{\prime\prime},0033$  im Eigenbewegungseffekt entspricht. Es liegt nahe zu bemerken, daß die Länge Lo für die normalen Riesensterne besser mit dem beobachteten Vertex des Geschwindigkeitsellipsolds als

mit der Länge L. für die entfernten Sterngruppen übereinstimmt.

Es sind schon verschiedene Erklärungen für das eben geschilderte Phänomen vorgeschlagen worden. H. MINEUR1 macht darauf aufmerksam, dall wir die Länge L, um 90° ändern können, wenn wir gleichzeitig das Vorzeichen von A ändern. Er sucht dann das Material in zwei Gruppen zu trennen, eine Klasso von sehr entfernten Objekten, die sich um ein Zentrum in der Länge 325° hewegen und eine Klasse von nahen Sternen, die sich um ein lokales Zentrum etwa in der Länge 240° drehen; die letztere Länge atlmmt mit dom Zontrum des lokalen Haufens nach Charlier und Shapley überein. Es können jedoch wohl ernste Einwände gegen Mineurs Auffassung erhoben werden. Vor allern ist die Entfernung zum Zentrum des "lokalen Haufens" zu klein, um die Theorie der differentiellen Rotation in der Ooktschen Form hier anzuwenden. Es scheint auch, daß der spezielle Rotationseffekt in MINEURS Analyse, den er zur Scheidung zwischen den zwei Rotationsarten heranzieht, von grundsätzlich anderem Charak-

ter als der oben diskutierte Effekt ist (Ziff. 34).

S. S. Hough und J. Halms haben schon in ihren wichtigen Arbeiten über die Sternbewegungen die harmonischen Terme von zweiter Ordnung in den Radialgeschwindigkeiten und in den Eigenbewegungen gefunden und studiert. Sie sehen aber die Ursache der Erscheinung in einem verschiedenen Mischungsverhältnis der drei großen Sterntriften (KAPTEYNS Triften I, II und HALMS o-Trift) in verschiedenen Gegenden des Himmels. In neuerer Zeit ist auch J. Schilt's geneigt, die Theorie der differentiellen Rotation zur Erklärung der harmonischen Terme zweiter Ordnung in den Sternbewegungen ganz aufzugeben. Er bildet eine Größe U, welche die Form der Frequenzkurve für die Eigenbewegungen repräsentiert und zeigt, daß ähnliche harmonische Terme in dieser Größe auftreten. Er zieht hieraus den Schluß, daß die harmonischen Terme zweiter Ordnung einem verschiedenen Mischungsverhältnis von Sternströmen in verschiedenen Gegenden des Himmels zuzuschreiben sind. Daß die erwähnte Verschiebung in  $ar{L}_0$  wahrscheinlich im Phanomen der Sternströmung ihren Grund hat, wird auch von REDMAN und LINDBLAD behauptet. Es ist aber nicht notwendig, deshalb die Rotationstheorie aufzugeben, was besonders nach den Ergebnissen von Oort, Plaskett und Pearce kaum möglich ist. Ein enger Zusammenhang zwischen dem Geschwindigkeitsellipsoid oder der Sternströmung überhaupt und der differentiellen Rotation ist übrigens durchaus in Einklang mit der Theorie, wie wir im folgenden in Ziff. 32 näher auseinandersetzen werden. Nach der Rotationstheorie hängen nämlich sowohl der Effekt der differentiellen Rotation wie die Richtung und das Größenverhältnis der Achsen des Geschwindigkeitsellipsoids in der Milchstraßenebene unmittelbar von dem Scherungsessekt einer gegenseitigen Translation der Geschwindigkeitsmittelpunkte für einander benachbarte Orter im System ab. Diese Translation soll der Richtung der Kreisbewegung folgen und ihre Größe nur auf der Differenz der Entfernung vom Zentrum zwischen den betreffenden Örtern beruhen. Es ist aber durchaus nicht

<sup>&</sup>lt;sup>1</sup> CR 188, S. 236, 1086 p. 1378 (1929); 190, S. 1050 (1930); BA 5, S. 505 (1929); MN 90, S. 516 (1930).

3 M N 70, S. 85 und 568 (1909, 1910); 71, S. 610 (1911).

befremdend, daß eine Abweichung der Vertexrichtung oder andere Anomalien der allgemeinen Sternströmung, die etwa in einzelnen ausgeprägten Sternströmen ihren Grund haben, von entsprechenden Effekten in den ermittelten Rotationsquantitäten begleitet sein können.

82. Die Beziehung zwischen dem Geschwindigkeitsellipsoid und der Rotation. Nach der abstrakten Theorie sollte das Geschwindigkeitsellipsoid ein Sphäroid sein, dessen Äquatorebene auf der galaktischen Ebene senkrecht steht und mit der Ebene, welche die Rotationsachse des Systems enthält, zusammenfällt. Das Verhältnis der Achsen  $\alpha$  und  $\beta$  soll aber auch in einer gewissen Beziehung zu der Größe A und zu der Winkelgeschwindigkeit  $\omega$  der Rotation stehen. Wir haben gemäß den Gleichungen (65), (42), (44)

$$A = \frac{1}{2} \left( \frac{\theta_0}{R} - \frac{\partial \theta_0}{\partial R} \right), \qquad \theta_0 = \frac{MR}{R^3 + 2p}, \qquad \left( \frac{\beta}{\alpha} \right)^2 = \frac{2p}{R^3 + 2p}$$

und bekommen dann die Relation

$$A = \omega \left[ 1 - \left( \frac{\beta}{\alpha} \right)^3 \right]. \tag{70}$$

 $\omega$  wird positiv in retrograder Richtung gerechnet.  $\alpha$  ist die Achse, welche in der Milchstraßenebene gegen das Zentrum des Systems zeigt. In Ziff. 30 haben wir weiter aus der Theorie ermittelt, daß, wenn die ellipsoidische Approximation streng wäre, die Achse  $\alpha$  für alle Punkte des Systems konstant sein sollte, während  $\beta$  mit R (aber nicht mit s) variiert.

Die Bedeutung der Gleichung (70) ist eine zweifache: Erstens, da es sehr wohl möglich ist, daß A und  $\beta/\alpha$  für verschiedene Gruppen von Sternen verschiedene Werte annehmen, können wir hoffen, durch Koordination der gemessenen Werte von A und  $\beta/\alpha$  im Vergleich mit der Gleichung eine wertvolle Kontrolle der Theorie selbst zu bekommen. Zweitens können wir in dieser Weise die Größe  $\omega$  bestimmen, was sonst durch direkte Analyse der Eigenbewegungen geschehen muß. Die mittlere Eigenbewegung B in galaktischer Länge ist mit A und  $\omega$  durch die Relation  $B = A - \omega$  verbunden. Der Wert von B aus den Eigenbewegungen muß mit dem aus dieser Relation ermittelten verglichen werden.

Gemäß den oblgen Auseinandersetzungen und unserer Deutung der empirischen Daten in der vorigen Ziff, 31 betrachten wir A und  $\omega$  als positive Größen. Die Achse  $\alpha$  soll also die größere sein und die Vertexlinie der Sternströmung

soll gegen das Zentrum hin zeigen.

Eine quantitative Vergleichung zwischen differentieller Rotation und Geschwindigkeitsellipsoid hat B. LINDBLAD¹ unter Benutzung des zur Zeit zugänglichen Materials von Radialgeschwindigkeiten für gewöhnliche Spektraltypen versucht. Die Resultate sind in Tabelle 27 aufgeführt. Für die Typen A bis K sind die Sterne in Gruppen nach Eigenbewegung aufgeteilt worden. Die Bestimmung von A und  $L_0$  ist nur für die entfernteste Gruppe möglich gewesen.

Tabelle 27.

Gruppe	А	$L_0$	Vertex	¢. km/sea	/) km/see	y km/seo	21
B0-B7	+0,006 + ,013 + ,033 + ,021 	324° 334 319 346 —	289° 275 21 335 356 342 349	10,9 12,4 18,6 17,5 19,1 27,7 36,3	9,8 10,5 12,4 13,6 8,4 19,4 21,4	4,5 11,4 3,9 16,5 10,0 16,9 25,5	445 250 304 714 391 857 825

<sup>&</sup>lt;sup>1</sup> M N 90, S. 503 (1930) = Stockholm Medd 5.

Die Sterne vom Typus B zeigen nur geringe Spuren einer Vorzugsrichtung der relativen Bewegungen in der Milchstraßenebene, was wohl in der kleinen Streuung der Geschwindigkeiten und dem Zusammengehen dieser Sterne in mehr oder weniger losen Haufen seinen Grund hat. Im A-Typus setzt der Ursa Major-Strom ein, und dies führt eine sehr merkliche Distorsion der Geschwindigkeitsfläche mit sich. Die späteren Typen zeigen ziemlich hohe Werte von  $L_0$  und der Länge des Vertex, ein Phänomen, das wir schon in der vorigen Ziff. 31 besprochen haben. Im ganzen scheint es sehr wohl möglich, daß die Abweichungen des Ellipsoids von den idealen Verhältnissen der Theorie wenigstens großenteils auf den Einfinß irregulärer Strömungen in unserer näheren Umgebung zurückgeführt werden können.

Zur Erklärung des Umstandes, daß die dritte Achse gewöhnlich viel kleiner als die größte Achse in der Vertexrichtung herauskommt, haben wir schon in Ziff. 29 und 30 angeführt, daß die Bewegung parallel zur Milchstraßenebene in der unmittelbaren Nachbarschaft von dieser Ebene von nahe zweidimensionaler Natur ist, und daß demnach die statistische Ausgleichung zwischen den galaktischen Bewegungskomponenten und der dritten Bewegungskomponente senkrecht zur Milchstraßenebene eine außerordentlich langsame sein muß. Spezielle Strömungen in der Milchstraßenebene werden daher auch nur sehr langsam auf die Streuung in Z einwirken.

Nur für die erste Gruppe F bis K in Tabelle 27 ist ein direkter Vergleich zwischen dem Ellipsoid und den Größen der differentiellen Rotation möglich. Der Wert von A ist jedoch hier mit einem ziemlich großen mittleren Fehler behaftet. Wenn wir an Stelle dessen Plasketts Wert A = 0.0155 annehmen und für  $\beta/\alpha$  als normalen Wert 0.78, so bekommen wir aus der Formel

$$\omega = +0.040$$
,  $B = -0.024$ .

Durch Division mit dem Faktor 4,74 ergibt sich

$$\omega = +0'',0084$$
,  $B = -0'',0051$ ,

ein Resultat, das sich im ganzen wohl mit den direkt aus den Eigenbewegungen ermittelten Werten verträgt (vgl. Ziff. 31).

H. Raymond und R. E. Wilson<sup>1</sup> haben in einer Untersuchung über die Raumgeschwindigkeiten von 4233 Sternen die diesbezüglichen Fragen einer eingehenden Besprechung unterzogen. Die beiden Verfasser haben nach neuen Methoden eine Analyse der Asymmetrie der Geschwindigkeitsverteilung ausgeführt, welche für die Asymmetrierichtung  $L=62^{\circ}$ ,  $B=+6^{\circ}$  gibt, in wesentlicher Übereinstimmung mit Strömbergs Resultaten, und sie haben die offenbare Verbindung zwischen dieser Asymmetrie und den nahe senkrecht dazu vor sich gehenden allgemeinen Vertexbewegungen untersucht. Zuletzt haben sie sehr ausführlich die Relation zwischen den Rotationsgrößen und den Eigenschaften der Geschwindigkeitsellipsoide diskutiert. Als mittleren Wert für das Achsenverhältnis  $\beta/\alpha$  erhalten sie 0,72, woraus für A=+0.015

$$\omega = +0.031$$
,  $B = -0.016$ 

folgt, oder in Bogensekunden

$$\omega = +0'',0065, B = -0'',0034.$$

Unser oben hergeleiteter Wert  $B=-0^{\prime\prime},0054$  stimmt mit dem von Oort aus den Eigenbewegungen sehr entfernter Sterne bestimmten überein. Nach Raymond und Wilson steht jedoch der kleinere Wert  $B=-0^{\prime\prime},0034$  in besserer . Übereinstimmung mit der mittleren Eigenbewegung in galaktischer Länge für

<sup>1</sup> A J 40, S. 121 (1930).

die Sterne im allgemeinen. Die Verfasser haben auch aus ihrem Material die Konstanten der differentiellen Rotation sowohl für Radialgeschwindigkeiten wie für Eigenbewegungen bestimmt. Die ersteren, in zwei Gruppen nach der mittleren Parallaxe der Sterne geordnet, gaben folgendes Resultat:

$$\tilde{\pi}$$
  $L_0$   $\tilde{\tau}A$   $A$  0,0121 329° +1,29 ± 0,34 +0,0155 0,0046 355 +3,05 ± 0,40 +0,0140

Die Resultate sind in guter Übereinstimmung mit den in der vorigen Ziff. 31 referierten. Der hohe Wert von  $L_0$  für die zweite Gruppe ist auffallend.

In den Eigenbewegungen wird ein Term vom Typus  $C\cos 3(L-L_I)$  eingeführt, dessen Koeffizient  $C=+0'',0022\pm0,0003$  gefunden wird, und wo sich für  $L_1$  der Wert -+10° ergibt. F. W. Dyson hatte einen ähnlichen Term für die B-Sterne eingeführt. Wahrscheinlich liegt der Grund dieses Termes in speziellen Strombewegungen, möglicherweise sogar im Ursa Major-Strom und im Taurus-Strom. Der erstere geht nahe gegen die Länge 0°, wo  $\cos 3L$  und  $\cos L$  Maxima haben, während der letztere gegen  $L=150^\circ$  zeigt, wo  $\sin 3L$  ein Maximum hat. Für A und B ergeben sich die sehr kleinen Werte

$$A = +0'',0013, B = -0'',0005.$$

Der Übersicht wegen stellen wir in Tabelle 28 einige repräsentative Bestimmungen der wichtigen Konstanten B zusammen. Die als theoretisch bezeichneten Werte sind die ans dem Achsenverhältnis des Geschwindigkeitsellipsoids berechneten.

Tabelle 28.

	В	Autorität
-0",0024 -0 ,0015 -0 ,0023 -0 ,0005 -0 ,0050 -0 ,0051 -0 ,0034	13-, c-, O-, N-, & CophSter Theorotisch	CHARLIER <sup>1</sup> FOTHERINGHAM <sup>2</sup> OORT RAYMOND UND WILSON THE LINDBLAD RAYMOND UND WILSON

Ein einfaches Mittel aus diesen Werten gibt  $B=-0^{\prime\prime}$ ,0029, und dieser Wert

kann vorläufig als der beste für diese Größe gelten.

88. Die Dimensionen, die Masse und die Rotationszeit der Milchstraße. Wenn wir gemäß Tabelle 28 für die Konstante B im Mittel -0'',0029 annehmen und für A den Wert +0'',0033, so gibt uns die Relation  $\omega=A-B$  für die Winkelgeschwindigkeit der Rotation  $\omega=0'',0062$ . Nachdem wir den Wert von  $\omega$  bestimmt haben, gibt uns eine Ermittlung der linearen Rotationsgeschwindigkeit  $\Theta_0$  unmittelbar unsere Entfernung R vom Zentrum des Systems. Aus den Apexbestimmungen für die Kugelhaufen haben wir oben  $\Theta_0$  für Gruppen kleiner Geschwindigkeitsstreuung zu 275 km/sec angenommen. Der entsprechende Wert der Zentrumsentfernung ist R=9400 Parsec.

Die Rotationsdauer an unserem Orte wird etwa

$$P =$$
 200 Millionen Jahre.

Für die Zentralkraft an unserem Orte haben wir offenbar, da für kleine Geschwindigkeitsstreuung  $\Theta_0$  die Geschwindigkeit der Kreisbewegung ist,

$$\frac{\partial V}{\partial R} = -\frac{1}{R} \Theta_0^2 = -R \omega^2. \tag{71}$$

- (6/s.)

<sup>&</sup>lt;sup>1</sup> Mem Univ Calif 7 (1926). <sup>2</sup> M N 86, S. 424 (1926).

Wn konnen eine "effektive Masse" des Systems in der Weise einsitteln, daß wir diese Kraft als durch ein schematisches System eizeugt denken, welches aus einer spharischen Zentialmasse  $M_1$  und einer sehr abgeplatteten, homogenen, spharoidischen Verteilung von der Gesamtmasse  $M_2$  mit dem galaktischen Radius  $R_1$  besteht Das Verhältnis zwischen  $M_1$  und  $M_2$  soll so angepaßt werden, daß es für zirkulare Bewegungen einen differentiellen Rotationseffekt A gibt Wir haben dann also gemaß (71)

$$\frac{\partial V}{\partial R} = -G\left(\frac{M_1}{R^2} + \frac{3\pi}{4R_1^2}RM_2\right) = -R\omega^2 \tag{72}$$

Wii konnen weiter schieiben

$$A = \frac{1}{4\omega} \left( -\frac{1}{R} \frac{\partial V}{\partial R} + \frac{\partial^8 V}{\partial R^8} \right) = \frac{3}{4} G \frac{M_1}{\omega R^8} , \tag{73}$$

und bekommen dann nach einigen Reduktionen

$$M_1 = \frac{4R^3}{3G}\omega A$$
,  $M_2 = \frac{4R_1^3}{3\pi G}\omega(\omega - \frac{4}{3}A)$  (74)

Wenn wn R in Parsec und  $\Theta_0$  in km/sec ausdrücken, bekommen wn nach Ausrechnung des Zahlenfaktors

$$M_1 = 0.617 \cdot 10^{88} \frac{A}{\omega} R \Theta_0^3 g,$$
 (75)

$$\frac{M_8}{M_1} = \frac{1}{\pi} \left(\frac{R_1}{R}\right)^3 \left(\frac{\omega}{A} - \frac{4}{3}\right). \tag{76}$$

Mit den obigen Werten von A,  $\omega$  und R bekommen wit, wenn wit übrigens  $R_1$  mit dem "effektiven Radius" in Ziff 30 identifizieren,

$$M_1 = 233 \cdot 10^{12} \,\mathrm{g}, \quad M_2 = 89 \cdot 10^{42} \,\mathrm{g}$$

und also fur die Totalmasse

$$M_1 + M_2 = 322 \cdot 10^{42} \,\mathrm{g} = 16 \cdot 10^{10} \,\mathrm{Sonnenmassen}$$

Die Masse des Systems ergibt sich also von der Großenordnung 10<sup>11</sup> Sonnenmassen. Die anderen hier gewonnenen Resultate konnen verschieden interpretiert werden Trotz des Umstandes, daß die galaktische Länge des Zentiums gemäß dem Phanomen der differentiellen Rotation in die Gegend der hellsten Milchstraßenwolken fallt, zeigt Pannekoek<sup>1</sup>, daß die Lichtstaike der Wolken keine Ansammlung von Steinen, die einer Masse von der Größenordnung von  $M_1$  entspricht, zuläßt, auch wenn wir mit ziemlich erheblichen Absorptionseffekten rechnen. Er weist darauf hin, daß die gasförmige interstellare Materie moglicher weise ausreichend ist, um eine gegen das Zentrum konzentrierte Masse von der angeführten Größe zu geben. Andererseits ist in Shapley's obenei wähnten Resultaten die Anwesenheit einer wirklichen zentralen Kondensation angedeutet Der große Wert von  $M_1/M_2$  in unserem schematischen System ist ja doch nur von der Natur des Kraftfeldes in unserer Umgebung bedingt und kann nach Oorr<sup>2</sup> sowohl auf eine wirkliche zentrale Kondensation wie auf einen ziemlich schnellen Zuwachs der Dichtigkeit gegen das Zentrum hin in unserer unmittelbaren Umgebung zuruckgefuhrt werden

Zwischen der oben angenommenen Zentrumdistanz von 9400 Parsec und den aus der Verteilung von Kugelhaufen (Shapley, Ziff 18) und von Veranderlichen in einem Milchstraßenfelde (Shapley und Swope, Ziff 20) ermittelten Weiten, 16400 bzw. 14400 Parsec, besteht offenbai eine Inkongruitat Die neuen Resultate, die auf die mögliche Existenz eines absorbierenden Stratums

BAN4, S 39 (1927) BAN4, S 92 (1927)

nahe der Milchstraßenebene hindeuten (Ziff, 24), stellen aber eine Revision der aus den photometrischen Daten berechneten Entfernungen in Aussicht, van der Kamp¹ hat kürzlich dieses Problem zur Behandlung aufgenommen. Nach dieser Untersuchung stellt sich gegenwärtig die Sache so, wie Tabelle 29 angibt. van der Kamp hat sowohl mit Trümplers Absorptionskoeffizienten wie mit dem von Bottlinger und Schneller, unter Annahme einer Dieke der absorbierenden Schicht von 175 Parsec, die Entfernungen der betraffenden Objekte neu ausgerechnet.

Tabelle 29

		Absorpt lon		
Material	Keine Absorption	σ=,57per 1000 Parson	2ºn per togo Parses	
Geometrisches Zentrum des Systems) der Kugelhaufen	16700 Parmee	13 700 Parnoo	9700 Parsec	
Veränderliche in Harvard Milky Way Field 185 [Pol nach Pickerico (a) bzw yan Reijn (b)]	14400	(a) 11 600 (b) 12 500	(a) 7400 (b) 9400	
Galaktische Rotation	·	7000-110	000 Parnec	

Es scheint nach diesen Resultaten nicht ausgeschlossen, daß die Werte der verschiedenen Methoden sich in dieser Weise miteinander in leidlichen Einklang bringen lassen.

34. Übersicht verschiedener Anschauungen über die Natur des Milchstraßensystems. Wenngleich die eben besprochene Theorie eine beträchtliche unere Einheitlichkeit besitzt und in der Tat auf einem Minimum von Hypothesen beruht, so treten neben ihr andere, mehr oder wuniger grundverschiedene Auffassungen hervor. Wir haben schon vorher mehrfach die Theorie erwähnt, die ein im wesentlichen dynamisch geschlossenes "lokales System" voraussetzt Die dynamischen Eigenschaften dieses Systems werden wohl im allgemeinen im Sinne des Kapteyn-Jransschen Systems in Ziff. 28 angenommen. Von diesem Gesichtspunkte aus erscheint sogar die Existenz eines allgemeinen, alle als galaktisch erkannten Objekte zusammenhaltenden Kraftfeldes fraglich. So hat früher G. Strömerge in dem Phänomen der Asymmetrie der Geschwindigkeitsverteilung den direkten Einfuß der Eigenschaft eines fundamentalen Raumos, die Größe der m ihm gemessenen Geschwindigkeiten zu beschränken, in Verbindung mit einer Tendenz der Materie in unserer Umgebung zu einem lokalen Zusammengehen gesucht.

Eine Theorie, welche in vielen Zügen Berührungspunkte mit der oben referierten Rotationstheorie hat, in anderen aber eine grundverschiedene Einstellung nimmt, haben kürzlich E. von den Pahlen und E. F. Freundlich vorgelegt. Diese Verfasser gehen von dem K-Effekt der Radialgeschwindigkeiten der Hellumsterne und dessen Variation mit der galaktischen Länge aus. Hier aber wird der ganze K-Effekt als ein Dilatationseffekt der uns umgebenden Gruppe von B-Sternen infolge einer Bahnbewegung dieser Gruppe im großen System erklärt. Die Bewegung kann als ein "Fallen" der Sterngruppe im Gravitationsfelde des großen Systems beschrieben werden. Unter der Annahme, daß wir uns mit der Sterngruppe dem Zentrum nähern, beobachten wir, daß die uns in der Bahn voraneilenden Sterne sich relativ zu uns entfernen, da ale bereits dem Zentrum näher sind, während in der entgegengesetzten Richtung

A J 44, S. 81 (1931).
 L. c. Siehe such "Conference on Michelson-Morley-Experiment". Mt Wilson Contr
 373, S 61 = Ap J 68, S. 401 (1928)
 Publ Astrophys Obs Poted 26, H. J. Nr. 86 (1928).

die Sterne mit kleinerer Geschwindigkeit zuruckbleiben. Die Richtung, in der die Bewegung von sich geht, wird aus den galaktischen Langen der Maxima des K-Effektes zu eiwa  $L=10^{\circ}$  gefunden, eine Richtung, welche einen Winkel von etwa 45° mit der Richtung gegen das Shapleysche Zentrum einschließt Aus den folgenden Daten. Maximalbetrag des Effektes, Ausdehnung des betrachteten Hautens von B-Steinen in der galaktischen Ebene, Entfernung vom Zentrum des großen Systems, werden die Elemente der Bahnbewegung bestimmt, unter der Voraussetzung, daß das Gravitationsfeld als von einer Punktmasse im eben genannten Zentrum herruhrend angesehen werden kann

Unter Berucksichtigung der Radialgeschwindigkeiten der Kugelhaufen wird die Geschwindigkeit in der Bahn zu 70 km/see geschatzt. Wenn die Entfeinung vom Zentrum zu 12000 Paisce geschatzt wird, ergibt sich eine Masse im Zentrum von der Größenordnung 10<sup>11</sup> Sonnenmassen und eine Umlaufszeit von 10<sup>8</sup> Jahren, Die Eigenschaften der schnellbewegten Steine und die Kaptrynschen Steinstrome werden dann diskutiert. Als Zusammenfassung gilt nach dieser Ansicht, daß die Steine im Raumgebiet um unseien Punkt im System herum in ihrei uberwiegenden Mehrzahl sehr langgestreckte elliptische Bahnen im Gravitationsfelde der großen Masse im zentralen Teil des von den Kugelsternhaufen definierten galaktischen Systems, an dessen Rande sich unser lokales Sternsystem befindet, beschreiben. Die Steine dieses lokalen Systems zerfallen im wesentlichen in zwei Wolken, die zwai sehi ahnliche, jedoch schon mei klich verschiedene Bahnen beschreiben, wobei die Gruppen der helleren B-Sterne der einen Wolke, die Sonne abei dei zweiten Wolke mit etwas kleinerer Exzentrizitat (etwa 0,90) und augenblicklich größeier Bahngeschwindigkeit (etwa 90 bis 100 km/sec) angehören Der Unterschied der Bahnen und der augenblickhehen Geschwindigkeiten bedingt das Phanomen der beiden Steinstrome Das Sternsystem befindet sich also noch sehr weit von einem stationaren Zustande, und die erhaltenen Bahnen sind nui "momentane" Wie ein deraitiges momentanes Zusammenballen von Sternen in dei Wolke des "lokalen Systems", dessen eigene Gravitationski aft keinen mei klichen storenden Einfluß auf die Bewegungen im System, msbesondere keine merkliche zusammenhaltende Kraft auf seine eigenen Mitglieder ausüben soll, zustande kommt, bleibt wohl aber gänzlich unerklärt. Die Streuung in den relativen Geschwindigkeiten innerhalb des lokalen Systems ist ja in der Tat viel gibßei als die Amplitude des K-Effekts, auf den die Eigengravitation des lokalen Systems keine merkliche Einwirkung haben soll. Das lokale System gemäß dieser Theorie könnte also nicht etwa durch allmähliche Auflockerung eines ursprunglich geschlossenen Systems entwickelt worden sein und kann überhaupt nicht mit dem lokalen System der geläufigen Vorstellung identifiziert werden

J Rosenhagen<sup>1</sup> hat eine allgemeine Untersuchung über den K-Effekt für die normalen Spektraltypen unter Ausnutzung des gesamten Materials der zur Zeit bestimmten Radialgeschwindigkeiten ausgeführt. Er untersucht den Gang des K-Termes mit einer Langenkoordinate sowohl in der Milchstraßenebene wie in zwei senkrecht zu ihr und zueinander stehenden "orthogalaktischen" Ebenen und findet auch für die letzteren eine ausgeprägte Variation, die durch eine zweigipfelige Smuskurve approximiert werden kann. Die Maxima eischeinen ziemlich nahe an den Polen dei Milchstraße gelegen. Er sucht seine Ergebnisse sowohl nach der Theorie von von der Pahlen und Freundlich wie nach einer Erweiterung der Oortschen Ansatze zu deuten, ohne ein entscheidendes Argument für diese oder jene zu bekommen. Im letzteren Falle muß er zur

<sup>&</sup>lt;sup>1</sup> A N 242, 5 401 (1931)

Deutung der "orthogalaktischen" Kurven eine Variation der Geschwindigkeitsmittelpunkte in unserer Umgebung nicht pur mit der Zentrumsentfernung R, sondern auch mit der s-Koordinate annehmen. Die Rotationsgeschwindigkeit So soll also  $\Theta_n(R, s)$  geschrieben werden. Die nördlichen Schichten der Milchstraße sollten eine höhere Rotationsgeschwindigkeit als die südlichen haben Dor K-Effekt in der Milchstraße gibt in Überemstimmung mit den oben in Ziff, 32 diskutlerten Resultaten für die gewöhnlichen Spektraltypen eine Zentrumslänge  $L_0 = 350^{\circ}$  Eine Variation der Geschwindigkeitsmittelpunkte mit der s-Koordinate ist früher von H Mineur! eingeführt worden, der eine allgemeine Analyse des K-Effektes nach Kugelfunktionen entwickelt hat. MINEUR findet emen Effekt, aus dem er eine Rotation um ein lokalos Zentrum in der galaktischen Lange 240° herlettet Die anguläre Geschwindigkeit dieser Rotation soll nur wenig von der Entfernung zum Rotationszontrum abhängen, dagegen aber mit der Höhe über der galaktischen Ebene beträchtlich veränderlich sein. Der genannte Effekt läßt sich folgendermaßen beschreiben. Wenn wir die Achsen x, y, z im Raumo in die folgenden Richtungen legen

$$x \begin{cases} L = 232^{\circ} \\ B = 0^{\circ} \end{cases} y \begin{bmatrix} L = 322^{\circ} \\ B = -10^{\circ} \end{bmatrix} x \begin{bmatrix} L = 320^{\circ} \\ B = +80^{\circ}, \end{cases}$$

so existiert ein Term o in den Radialgeschwindigkeiten von der Form

$$\varphi = -0.058 \, yz$$

Es scheint, daß dieser Effekt auch quantitativ mit Rosenhagens K-Variation in einer mit der ve-Ebene nahe zusammenfallenden orthogalaktischen Ebene (G''-Ebeno genannt) ziemlich übereinstimmt.

Es ist wohl nach den geschilderten Verhältnissen klar, daß, wenn wir auf dem Boden der Rotationstheorie bleiben, wir sichere Auskunft über die Rotationsbewegungen im großen System am besten aus den sehr entfernten Objekten in der Milchstraßenebene, in der Weise, wie es besonders Oort sowie Plaskett und Prance gemacht haben, bekommen, daß aber, wenn wir zur großen Masse der uns verhältnismäßig nahellegenden Sterne mit größerer Geschwindigkeitsdispersion übergeben, der differentielle Rotationseffekt tellweise durch Störungen tiberlagert wird, tiber deren wahre Natur wir noch in Unklarheit sind. Es ist jedenfalls von Interesse, zu konstatieren, daß diese Störungen den Vertexpunkt des Geschwindigkeitzellipsoids und die Länge L. um denzeiben Betrag verschieben.

Von größter Bedeutung für die kosmologischen Ideen während der letzten zwei Jahrhundorte ist die Frage nach einer möglichen Analogie zwischen unserem Milchstraßensystem und den "außergalaktischen" oder "anagalaktischen" Nebalflecken gewesen Die "Weltinseltheorie" wurde wohl zuerst in HERSCHELS Arbeit "On the Construction of the Heavens" (1785) ausgebildet<sup>3</sup>, doch macht HERSCHEL hier noch keinen prinzipiellen Unterschied zwischen wirklichen und acheinbaren Nebeln, sondern nimmt an, daß die Nobel überhaupt von der letzteren Art sind und demnach nichts anderes als entfernte Sternansammlungen darstallen In selnen späteren Arbeiten hat er die zwei Nebelarten erkannt, nelgte aber allmählich mehr und mehr zu der Ansicht, daß die Milchstraße in ihrer eigenen Ebene eine ungeheure Ausdehnung besitze, und daß sie wahrscheinlich in ihrem System alle für uns wahrnehmbaren Objekte einschließe. Bis in die letzten Jahre haben in der Tat die Ansichten über die wahre Natur der Milchstraße zwischen

B A 5, S, 505 (1929).
 Vgl. goschichtliche Übersicht von K. Lurdmark, Studies of Anagalactic Nebulac.
 Nova Acta Reg Soc Sc Uppel, Volumen extra ordinem 1927

den beiden Extremen der Weltinseltheorie einerseits und der Theorie eines

praktisch allumfassenden Milchstraßensystems andererseits geschwankt.

Nach Lord Rosses Entdeckung der Spiralform einiger Nebel (1845) ist die Weltinseltheorie in interessanter Weise von Stephen Alexander<sup>1</sup> und von Cleveland Abbe<sup>2</sup> entwickelt worden. Der erstere kann, wie Lundmark bemerkt, durch seine Theorie über die Nebel als sternproduzierende Mechanismen als ein Vorgänger von JEANS betrachtet werden,

Die spektroskopische und spektrographische Scheidung der galaktischen Gasnebel von den Nebeln mit typischem Absorptionsspektrum hat dann in besonderer Weise die Diskussion gefördert. Da im letzteren Falle Spektra von angenähertem Sonnentypus sich ergeben, hat man hier gleich eine schwer-

wiegende Bestätigung der Weltinseltheorie gesehen.

Unter den Verfassern, die sich in neuerer Zeit mit den diesbezüglichen Fragen beschäftigt haben, ist besonders Easton<sup>a</sup> zu nennen, der auf Grund seiner eigenen Forschungen aus dem verwickelten Verlauf der Milchstraße am Himmel die Gestalt eines gewaltigen Spiralnebels mit dem Kern in der Cygnus-

region herauszulesen versuchte.

Nach Shapleys grundlegenden Untersuchungen über das größere galaktische System, die eine unerwartete Erweiterung unserer Vorstellungen über den Umfang des Milchstraßensystems als Ganzem mit sich führten, neigte die Auffassung wohl zugunsten der Theorie einer praktisch allumfassenden Milchstraße, um so mehr, da die van Maanenschen direkt gemessenen Rotationsgeschwindigkeiten der Spiralnebel gegen genügend große, der Weltinseltheorie entsprechende Entfernungen für diese Objekte sprachen. Besonders durch die Studien von CURTIS, LUNDMARK, HUBBLE u. a. über die Natur der außergalaktischen Nebel hat aber die Weltinseltheorie ihre alte Stellung als bevorzugte Theorie wiedererobert. Die gegenwärtigen Grundlagen der Entfernungsbestimmungen für die Spiralnebel und die verwandten Objekte haben schon einen bemerkenswerten Grad von Zuverlässigkeit gewonnen, und die Distanzen kommen genitgend groß heraus, um in genereller Weise der Weltinseltheorie zu entsprechen,

Mit dieser wahrscheinlich endgültigen Entscheidung einer alten Streitfrage sind aber keineswegs die Fragen über die Natur und Stellung des Milchstraßensystems erledigt worden. Es scheint zwar an sich wahrscheinlich, daß unter den verschiedenen Typen von Nebeln ein "Modell" zu unserem eigenen System gefunden werden könnte, jedoch ist von vornherein klar, daß das Material für eine rein morphologische Klassifizierung unseres Milchstraßensystems noch nicht vorliegt, und daß hier besonders große Schwierigkeiten, vor allem die mehr oder weniger regelmäßigen Absorptionserscheinungen, zu überwinden sind. SEARES hat der Lösung der Frage auf dem Wege der Flächenhelligkeiten näherzukommen versucht. Er berechnet aus Kapteyns und van Rhijns Dichtefunktion die Flächenhelligkeit des von einem sehr entfernten Punkt in der Richtung des galaktischen Pols aus gesehenen galaktischen Systems. Er findet, daß diese Helligkeit etwa der visuellen Größe 23 per Bogensekundenquadrat entspricht, etwa 100 mal kleiner als die Flächenhelligkeit der helleren Partien in typischen Spiralnebeln. Daß wir so verhältnismäßig leicht die galaktischen Wolken wahrnehmen, beruht nach Skares einfach auf dem großen Areal dieser Gebilde am Himmel. Dieses Resultat, das auf eine vom galaktischen System verschiedene Konstitution der Spiralnebel deutet, verliert wohl aber erheblich an Beweiskraft, wenn wir nicht länger das Zentrum des galaktischen Systems in unserer unmittelbaren Nachbarschaft suchen. In einer späteren, oben in

Mt Wilson Contr 191 = Ap J 52, S. 162 (1920).

<sup>&</sup>lt;sup>1</sup> A J 2 (1852), <sup>8</sup> MN 27, S. 262 (1867). \* Ap J 12, S. 136 (1900).

in den änßeren Teilen unseres Systems nach der eben erwähnten Theorie wohl möglich, wenngleich die wahrscheinlich erhebliche zentrale Kondensation der Materie im System eine sahr mächtige Entwicklung der Spiralstruktur verhindern mag. Es soll aber hier zuletzt erwähnt werden, daß H. Vogr¹ die Bedeutung der neuen Ergebnisse über die Expansion der Welt zur Erklärung der Spiralform herangezogen hat, und es ist möglich, daß dieses Phänomen auch für unser eigenes System wichtige Konsequenzen mit sich geführt haben kann

Von den oben referierten Gesichtspunkten wesentlich verschiedene, aber namiteinder verwandte Hypothesen über die Natur des Milchstraßensystems haben gleichzeitig Lundmarks, Shapleys und Trümplers aufgestellt. Nach den Ansichten der zwei ersteren Verfasser ist das Milchstraßensystem kein einheitliches Objekt, das mit irgendeinem einzigen außergalektischen Nebel verglichen werden kann Shapley sicht eher in den Nebelhaufen. z. B. in der Coma-Virgo-Gruppe oder noch mehr in der dichteren Centaurusgruppe, unserem Milchstraßensystem Ahnliche Formationen Die einzelnen Glieder unseres Systems, die mit den Nebeln einer Gruppe vergleichbar wären, sind die Sternwolken der Milchstraße, unter die ein lokales System gerechnet wird, ferner die Magellanschen Wolken und die Kugelhaufen. LUNDMARK teilt die eigentliche Milchstraße in wesentlich zwei Tellsysteme, das lokale System und das zum großen Tell durch Absorption in Dunkelnebeln verborgene Sagittariussystem Er betont besonders eine mögliche Verwandtschaft zwischen den Kugelhaufen und den elliptischen außergalaktischen Nebeln TRUMPLER deutet sein System von offenen Sternhaufen, das ziemlich Rotationssymmetrie um die Sonne besitzt, als gewissermaßen einen Grundriß zur eigentlichen Milchstraßenstruktur. Dieses um die Sonne zentrierte System wird dann in der Tat die Hauptmasse des Systems enthalten, und die Existent des verborgenen Sagitterlussystems schelnt in Frage gestellt. TRUMPLER deutet das System als einen Spiralnebel mit gegen rechts gewundenen Armen, vom Nordpol der Milchstraße aus gesehen. Die Kugelhaufen sind nicht organisch in dieses System singegliedert. Es mag erwähnt werden, daß TRUMP-LERS System sich nicht mit dem Shaplerschen lokalen System oder lokalen Haufen deckt, sondern ein viel weiter gestrecktes Gebilde darstellt. Der lokale Haufen nach Shaptey könnte aber als die Zentralregion des Milchstraßennebels autgefaßt werden.

Wenigstens gegen welt getriebene Hypothesen in der Richtung einer Aufteilung des Milchstraßensystems in isolierte Teilsysteme kann wohl mit Recht hervorgehoben werden, daß es als ein merkwürdiger Zufall zu bezeichnen würe, daß die Teilsysteme, die nach dieser Annahme die eigentliche Milchstraße aufbauen, alle so nahe in einer und derselben Ebene orientlert liegen. Man darf auch sagen, daß die Anwesenheit der Kugelhaufen, welches ihr Ursprung auch sein mag, keineswegs an und für sich unserem Milchstraßensystem die Würde einer Organisation von höherer Ordnung als die gewöhnlichen Nebel verleihen kann. Ähnliche Phänomene treten wahrscheinlich auch bei Systemen von verhältnismäßig bescheidener Größe auf. Objekte, die als Kugelhaufen zu bezeichnan sind, sind ja z B. in der unmittelbaren Umgebung der großen Magellanschen Wolke verhanden, in der Weise, daß sie offenbar mit der Wolke in Verbindung stehen. Die Angliederung der Magellanschen Wolken als "ferne Begleiter" unseres Systems erinnert ja auch an die zwei eiliptischen Nebel NGC 205 und 221 bei M31. Wenn wir diese zwei Satellitennebel zum System des Andromeda-

<sup>1</sup> AN 242, S. 181 (1931), 245, S. 281 (1932).

Publ A S P 42, S 23 (1930), Pop Astr Tidskr 11, S. 85 (1930).

Harv Circ 350 (1930)

<sup>4</sup> Lick Bull 14, S 154 (1930).

nebels rechnen wollen, so bekommen wir zwar ein mehrfaches System, der Haupt-

körper selbst erscheint jedoch vollkommen einheitlich

Gegen Trumplers Auffassung seines Haufensystemes macht Bortlinger<sup>1</sup> den Einwurf, daß jenei die Einwirkung der Absorption des Lichtes im System meht genugend berucksichtigt hat TRUMPFFR ist nicht daraut gekommen, daß die von ihm gefundene Absorption in einer engen Milchstraßenschicht vielleicht die Ursache sei, die uns eine Dichteabnahme langs dei Milchstraßenebene vortausche Es ist in der Tat sehr wohl moglich, daß die Extinktion in gewissen Richtungen, & B. gegen das Zentium des Systems in Sagittarius, so intensiv sem kann, daß sie die Vollstandigkeit des Haufenmaterials in sehr hohem Grade herabsetzt Die Neigung des Haufensystems gegen die Milchstraßenebene mag durch eine etwas nördliche Absorptionszone in der Sagittariusrichtung erklart werden Trümplers Haufensystem stellt dann einen schragen Schnitt durch das System dar

Die Existenz eines "lokalen Systems" in dem gelaufigen Sinne dieses Wortes ist nach dei Rotationstheorie nicht möglich, da die Materie in unserer Umgebung durch die beobachteten Effekte der differentiellen Rotation stetig zeigliedert werden muß Es wären also, wenn das ortliche System etwas Geschlossenes und Beständiges 1st, diese Effekte in anderei Weise zu deuten. Bei der inneren Einheithehkeit dei eiwähnten Theorie, die quantitativ eine Reihe Phänomene mitemander verknüpft, die sonst als isolierte Tatsachen auftreten und besonders nach der Bestätigung der differentiellen Rotation für die Sterne mit interstellaren Ca-Limen durch die Arbeit von Plaskell und Plarce, muß man wohl doch von anderen Theorien fordern, daß sie in ebenso direkter Weise und ohne komphzierte Hilfshypothesen etwas Ahnliches leisten. Es fehlt ja auch nicht an Tatsachen, die auf eine weitgehende Heterogenität des "lokalen Systems" deuten Es 1st in der Tat wohl möglich, daß der beobachtete Überschuß an Dichtigkeit in unserer Nähe, sowert er sich nicht durch Absorption des Lichts in der Milchstraßenebene erklärt, eine Folge der machtigen Stromungen ist, die sich hier zufälligerweise raumlich überemanderlagern. Wir können unter solchen Strömungen den Taurus-Strom, den Ursa major-Strom und die großen Triften der Heliumsterne nennen. Das Phänomen des "lokalen Systems" wäre dann mit den beobachteten kleineren Abweichungen von regulären Verhältnissen in der Geschwindigkeitsverteilung in Verbindung zu setzen (vgl. Ziff 31 u. 32), hätte aber an sich nichts, was mit den großen Linien der einheitlichen Theorie in Widerspruch steht. Es mag hier der Klarheit wegen bemerkt werden, daß nach dieser Theorie die Bahnen der erwähnten großen Stromungen nur wenig von der zukularen Bewegung um das Zentium heium abweichen. Was wit unmittelbai beobachten, sind natürlich nur ihre relativen Geschwindigkeiten.

Wenn wit auf dem Boden der Rotationstheorie etwa nach dem Ursprung der beobachteten Sedimentation verschiedener Gruppen von Objekten in "Untersysteme" von verschiedenen dynamischen Eigenschaften fragen, so ist es möglich, wie in Ziff, 29 auseinandergesetzt, daß Effekte einer langsamen Gleichverteilung der Energie durch "Passage" hier mitspielen können, wenn wir nur eine gentigend lange, nach der Formation des Systems verflossene Zeit voraussetzen dürfen Andere Gesichtspunkte lassen sich auch finden So ist es vielleicht möglich, daß im Untersystem von größter Rotationsgeschwindigkeit, wo die Materie sich in nahe relativer Ruhe bewegt, sich vorzugsweise Steine mit großer Masse und verhältnismäßig großer Dichte gebildet haben<sup>2</sup>, was die gioße ielative Häufigkeit dei Steine von frühem Spektraltypus in diesem Untersysteme eikläien

Borlin-Babelsb Veröff 8, II 5 (1934)

<sup>&</sup>lt;sup>2</sup> Lindblad, Ark Mat Astr Fys 21 A, Nr 3 = Stockholm Medd 1, S 24 (1928)

könnte. Die Häufigkeit gewisser Arten von Veränderlichen, wie kurzperiodische d-Cepheisterne und Me-Sterne, in den Untersystemen von großen relativen Geschwindigkeiten und von geringer Abplattung gegen die Milchstrußenebene kann vielleicht damit in Verhindung gebracht werden, daß die Mitglieder dieser Untersysteme individuell genommen in radialer Richtung sehr langgestreckto Bahaen beschreiben, welche die betreffenden Sterne ziemlich oft in die dichten Gegenden des Zentrums führen Es besteht wenigstens die Möglichkeit, daß ein Auftreten gewisser singulärer Typen von Starnen in diesen Gegenden leichter vor sich gehen wird als in anderen. Welcher Wert derartigen Gedanken zukommt, läßt sich allerdings gegenwärtig kaum eutscheiden. Ohne Zwolfel kann man jedoch sagen, daß überhaupt die allgemeinen Fragen tiber die Entwicklung der Sterntypen wichtige Berührungspunkte mit den Fragen nach der Struktur und der Entwicklungsgeschichte des Sternsystems haben

Es ist jedoch ohne weiteres klar, daß man bei dem jetzigen Stande der Milchstraßenforschung jeden Schluß nur mit der größten Vorsicht zu siehen hat Für die direkten Untersuchungen der Dichteverteilung im System scheint gegenwärtig das Problem der Absorption des Lichtes in der Milchstraßenschicht das wichtigste zu sein. Erst wenn wir einen zuverlässigen Weg zur Beseitlgung der aus diesem Phänomen herkommenden Schwierigkeiten gefunden haben, können wir eine volle Einigung der rein empirischen Morphologie des Systems

mit irgendeiner dynamischen Theorie erwarten.

#### Appendices to Chapter 4.

# Luminosities, Colours, Diameters, Densities, Masses of the Stars.

By
KNUT LUNDMARK-Lund
(Continued)

### I, Catalogue of Stars Brighter than 5<sup>m</sup>,00.

Contents Col i contains the number in the PGC by L Boss (upper line) and the RHP number (lower line). This number also corresponds to the number in Schresinger's work, "Catalogue of Bright Stars", New Haven 1930. The catalogue of Schresinger was not accessible to me when I compiled the present catalogue but it has been used for check work during the proof-reading of this chapter.

Col 2 contains the name of the stars in the usual nomenclature together with the BD number, when in italics this refers to the nearest whole degree according to the wellknown rules concurring the course of the precession

Col 3 and 4 contain the  $\alpha$  and  $\delta$  for 1900,0

Col 5 contains the spectral type

Col 6 contains the colour in Osthoff's scale and the estimates according to Franks (Specola Astronomica Vaticana VIII, IX and XV.) Only in a few cases the estimates of the present writer have been added. These estimates are given in the Osthoff Scale.

Col. 7 contains the apparent magnitudes according to RIIP and to Zinner's work, "Helligkeitsverzeichnis von 2373 Steinen bis zur Große 5,50". The latter magnitudes are based upon an extensive discussion of practically all available determinations of stellar magnitude and they follow very closely the scale defined

by PD (See ciph 40.)

Col. 8 and 9 contain on the upper line the total proper motion (unit is 0",001), or the quantity  $\mu = [(\mu_{\alpha}\cos\delta)^2 + \mu_{\delta}^2]^{\frac{1}{2}}$  and the direction  $\psi$  of the proper motion (unit is 1°), counted in the same way as the position angles and defined as tg  $\psi = \mu_{\alpha}\cos\delta/\mu_{\delta}$ , and on the lower line the  $\tau$ - and  $\nu$ -components, which according to Kapifyn's definition are  $\tau = \mu\sin(\chi - \psi)$  and  $v = \mu\cos(\chi - \psi)$ , where  $\chi$  is the angle of the great encle through the Apex with the declination circle, counted in the same way as the position angles. The quantities  $\mu$ ,  $\psi$ ,  $\tau$ , and  $\nu$ , given in columns 8 and 9 have in most cases been taken over from an unpublished determination carried out under the supervision of Kapifyn by Dutch prisoners. The results of this extensive work of computation has been distributed earlier in typewritten manuscript to several observatories. I am under much obligation to Kapifyn's family as well as to P. I van Rhijn, Director of the Kapifyn Laboratory for kind permission to include the mentioned data in the present catalogue.

Col 10 gives the radial velocity of the star, expressed in kilometer per second. The work of J. H. Moore, "A General Catalogue of the Radial Velocities of Stars, Nebulae and Clusters", was not accessible to me, when the present catalogue was compiled but has been used for a general check when reading the proofs. When a velocity is indicated by "Var." there are no conclusive evidences as to the nature of variation of the radial velocity. When the velocity is indicated by "Var." and a number, this number in most cases refers to the velocity of the system, derived from the variation in radial velocities interpreted

as caused by orbital motion in binary systems.

Col. 11 contains on the upper line the arithmetic mean of existing parallax determinations (trigonometric or spectrographic, or in a few cases theoretic values), on the lower line the geometric mean of the same determinations, provided that they are positive. In both cases the unit is 0",001.

Col 12 gives the number of parallax determinations used when forming the mean values in col 11. When in column 12, instead of a number, an (a) is given, the parallax value in the preceding column has been inserted from additional sources, being available since the catalogue was compiled in 1927 to 1928.

Col. 13 contains on the upper line the absolute magnitude M in the RHP system and on the lower the absolute proper motion magnitude  $H=m+5+5\log\mu$ . In cases of variable stars the M- and H-values correspond to the magnitude at maximum.

Col. 14 and 15 contain the galactic longitude and latitude computed with aid of the tables computed at the Observatory in Lund and distributed in mimeograph form. When more accurate values for these coordinates are needed the extensive tables, "Lund Observatory Tables for the Conversion of Equatorial Coordinates into Galactic Coordinates" (Ann. Obs. Lund No. 3), should be consulted.

A few remarks as to binaries, variable stars etc. have been added to the table. In these remarks ADS rafers to R G. ATTRIENS work, "Now General Catalogue of Double Stars within 120° of the North Pole I—II" [Wash Carnegie Inst Publ No. 417 (1932)].

						U-,				-				
<u> </u>	а	3	. 4	5	6	7	8	9	10	11	12	13	14	
1 3	33 Placinm 6357	0-,2	- 6°16′	K0	5°.7	4",68 4 ,85	92 + 67		6,3	23 23	(2)	1,5 4,5	67*	-
10 _15	a Andromedae	3 ,2	+28 32	Aop	1°.7	2 .15 2 .39	213 - 77	139° + 198	-13,0	48 47	(5)	0,5 3,8	81	1
12 21	# Camiopelas 3	3 ,8	+58 36	<b>F</b> 5	3",1 Ya	2 ,42 2 ,56	559 - 11	109°	+11,8	71 71	(4)	6,2	85	-
16 25	# Phoenicle 16	4 ,3	-46 18	K0		3 ,94 4 ,04	219 — 131		- 9,2	25 25	(2)	0,9 5,6	290	-
27 39	7 Pegari 14	8 ,1	+14 38	B2	2*,2 W	2 ,87 3 ,16	- 11	180° + 6	+ 4,9	6	(4)	-3,2 -1,6	79	F
91 45	Z Peguel 27	9,4	+19 39	Me	7",3 Y"	4 ,94 4 ,94	94 十 37	97° + 86	-45,3	5	(4)	-1,2 4,8	80	-
33 48	7 Cetl 21		-19 30	Ma	7,0 0Y	4 ,68 4 ,64	- 68 67	201 + 10	-22,7	13 13	(3)	0,2 3,8	52	٦
43 63	9 Andromedas 84	" "	+38 8	A2	A1 34'0	4 ,44 4 ,65	52 40	247	+ 4,7	23 22	(4)	1,1 3,0	84	7
50 68	σ Andromedae 44			A2	2',9 Y¹	4 ,51 4 ,70	- 70	,	Vаг. — 1°	15 15	(4)	0,2 4,0	84	F
53 74	48 Cett	14 ,3	- 9 23	Ko	5'.9 Y	3 .75 3 .76	37 - 37	+ 1	+18,2	20 19	(3)	0,1	71	F
55 77	Tucanas 13	14 ,5		F8		4 ,34 4 ,46	2058		+ 9,3	146 146	(1)	5,1 10,9	274	F
92	B Camlopelse	19 ,2		Mb?	Ver	-5 ,0 to		-	-	1	(1)	-157	88	7
95	47 Tuonnae 35		-72 39	G 5		[4 .5]		=	-	0,2	(1)	-8,8	272	F
74 98	/ Hydrl 16	20 ,	1	Go	44,7	2 ,90 3 ,02	2240 + 381	82° +2195	+23,0	160 160	(2)	3,9 9,6	271	H
78 99	a Phoenicis	21 ,3	_	K <sub>0</sub>	5°.7	2 ,44 2 .57	445 - 307	154	+74,2	60	(3)		284	Ħ
77 100	и Phoenicle 101	21 ,3	-44 14	A3		3 ,90 4 ,25	+ 63	74° + 87	+ 9	12	(4)		283	Ħ

HR 92. Move H Cardopoles of 1572. Permits from the spectral properties of the 19m,8 star possessed to be the Nove. — HR 95, Q1, the 1900 (c). Permits from the brightest stars in the Market stars in the Mark

Oh. 11 15 б 7 8 9 10 11 12 13 1 298° 820 4m,96 210°+11,2 22m,9 -33° 34' Mb 56 n Sculptous 83 4,96 55 б 3.7 152 105 1059-10 88 (a) -0,9 - 8 **B**8 10,9 4 .88 48 7 97 / Cassiopeiae 26 ,2 +53 59 YΙ 8 48 3,3 5,02 82 123 Vai 25 (1) 1,9 275 26 ,6 -49 22 ,88 128 83° -69 11 Phoenicis A2 99 .97 25 5.4 - 5 52 116 125 115 103 122° +10 34 (4) 1,2 272 -- 54 4,52 B1 Tucanac 27,0-63 $B_0$ 100 4,6 ,61 40 95 126 50 4 34 (a) B2 Tucanae 4 ,48 108 125 94 9,9 1,1 272 -54 A2 27.0 - 6331 101 4,6 4 .59 48 97 127 50 (3)11 85° 3 -3,4 89 و َ±ٍ 130 30,5 ,21 \* Cassiopeiae 27,3 + 6223 103 Υï 0,6 4,41 5 10 3 130 102 1139+ 2.0 (4) -3,3 20,6 Ω 89 9 ¿ Cassiopeiae **B**3 3 .72 23 122 31 4 十53 YG1 3,98 23 4 0,5 153 105 23 20,5 113° 8,8 3 (3)2,6 88 -29 **B**3 ,44 # Andromedae 31 .5 -- 33 10 123 1,3 W 4 ,58 23 101 154  $\bar{2}22$ -83.430 (4)88 1,8 33,3 + 2840,7 ,52 336 -33 s Andromedae 46 G5 130 28 7.2  $Y^2$ ,60 329 64 4 163 103 60.0 162 122 7,2 29 <u>(4)</u> 0,9 88 - 32 3 ,49 δ Andromedae 34 .0 -1 30 IC2 132 Ϋ́8 30 4,5 162 3 165 91 3,49 (4) Ko 50,0 2,47 60 121° 4.1 21 0,9 89 6 135 с Сачноронас 34 .8 -1-55 OY3 2,53 6 59 21 1.4 168 139 .85 6 (2)1,3 89 36 ,5 +49 58 **B**3 20,7 Y1 4 21 109 - 9,4 -12 & Cassioperac 141 б 1,5 3 21 5 ,07 179 164 -16.5 (2)0,4 272 4,65 38 227 14 -71 38 Κö 142 a Phoenicis 36 ,6 -46 4 .73 19 14 2,6 33 180 180 0.003 (3)- 18, 89 -21 - 300 30,2 ,90] 33 Andromedae 37 2 +40 G 4 [4 182 148 80° (2)-81 -13.3 41 0,3 90 KO 5<sup>u</sup>,8 2,21 230 38,6 - 18147 B Ceti 32 41 4,0 Y 2,30 143 182 188 115 315 4-10 270 -- 60 10 38,8-58 $\Lambda_0$ 4 ,53 148 n Phoenicis 1 -0.56 Я 4,62 42 191 (2)**B**2 3°,0 4,70 22 103° 7.5 5 -- 1,8 90 --- 14 o Cassiopeiae 39 .2 -1-47 44 152 5 Y1 6-1-21 1,4 4 ,88 193 183 ,93 18394 0.6 15 (1) 0,8 90 -73 Ĭζο 5°,2 110 m1 Celi 151 39 ,2 -- 11 γa 15 5,1 4 ,94 99:-1 48 194 128 Vai 2310 (4)-38 50.5 129 25 1.2 Z Andromedac 42 ,0 +23 43 Ko 4,30 164 4,8 Y8 123 43 -25,9 24 4,31 106 215 (9) 4.4 ,64 1159+ 9.9 148 91 5 F8 40,5 3 1242 168 и Саявторетае 43 ,0 +57 17 ,74 9,1 ٧å 3 25 +1242 145 219 150 1189 (4)0,4 -55 ,55 4-31.9 16 92 60,9 43,5 + 72 IC5 4. 93 173 & Piscium 15 OB 4,4 4 .59 7 93 107 224 138" Vลเ 7 (3) - 1,3 91 -21 ,42 28 32 **B**3 20,2 v Andromedae 44 ,3 +40 175 27 - 24,0 98° - 9,4 1,7 8-18 7 w 4 ,71 171 226 ,96 134 270 -43 IC 5 1 Hydu 45 ,1 -75 182 ,08 5.6 21 + 133 5 236 64 338° +-21,3 (4) 3.7 2 56 91 F8 40,5 4 ,93 188 189 Cassiopoiae 47 ,1 +60 34 ,04  $\mathbf{Y}^{2}$ 5 126 -139 56 6.3 244 124 -- 64 200° + 15.5 12 (4)0,1 94 20 Cell 47.9 - 141 Κō б°,5 4 92 17 191 Υŝ 11 1,1 4 ,88 17 3 248 114 214° 15 (3)0.8 91 4 Ko 60.0 53 -23,1v<sup>1</sup>Cassiopeiae 49 1 +58 26 4 ,95 193  $Y^3$ 3,6 ,94 52 6 15 4 134 253 (3) 2 94 Vau 17 2,2 92 26,1 30 y Cassiopeine Bop 2 ,25 199 50 ,7 +60 11 ,48 28 6,8 13 0,4 W 2 12 264 144 1,7 92 3 245 -47,0 29 (5)50.4 ,83 100 v2 Cassiopelae 50.7 + 5838 Kο 200 4.8 ,82 24  $\mathbf{Y}^{3}$ 79 62 4 138 265

33 Andr The Great Andromeda Nobula | The parallax of 0",000003 | determined on basis of | 1 Capheid stars, 2 Novao, 3 Non variable stars observed in this object

Oh to 1h

					$O_{I^{\dagger}}$	to 1h.								
1	2	3	4	5	6	7_	8	9	10	11	12	13	14	15
203 269	μ Andromedae 175	51 <sup>m</sup> ,2	+37° 5	7' A2	2°,6 W	3 <sup>ts</sup> ,94 4,08	153 + 103		+ 8	33	(4)	1,5 4,9	93°	-24°
206 271	η Andromedae 153	51 ,9	+22 52	2 G 5	5°,0 Y <sup>2</sup>	4 ,62 4 ,63	60 - 59	225°	-10:	12 12	(5)	0,2 3,5	94	-39
212 280	α Sculptoris 297	53 ,8	-29 54	4 B5		4 ,39 4 ,55	7 + 4	82°	+ 10,5			-1,3	216	<b>-8</b> 5
218 285	Cephei 19	55 .0	+85 43	3 Ko	6°,2 OY*	4 .52 4 .46	86 + 21	93° + 83	+ 8,5	15 15	(3)	0,4	90	+24
226 294	ε Piscium 153	57 ,8	+ 7 2	Ko	5°,4 Y <sup>3</sup>	4 .45 4 .51	85 - 20	289° 82	+ 6,9		(5)	0,8	98	-55
235 310	ψ <sup>1</sup> Piscium 156	0 ,4	+20 56	5 A2	2°,0 Y1	5 .55 5 .69	58 + 14	10 <b>8°</b> 十 56				1,0 +,4	96	-41
236 311	ψ <sup>1</sup> Piscium 157	0 ,4	+20 50	6 A0	1°,9 W	5 ,82 5 ,95	47 + 11	120° + 47	- 4	12	(a)	1,2	96	-41
245 322	β Phoenicis 324	1,6	-47 15	Ko	4°,3	3 ,35 3 ,57	45 - 22	252° - 39	- 1,3	24 24	(4)		258	70
255 334	η Ceti 240	3 ,6	<del>-10 43</del>	Ko	6°,0 Y	3 ,60 3 ,62	246 - 17		+11,3	33 33	(2)		109	-72
257 335	φ Andromedae 275	3 ,7	+46 42		3°,0	4 ,28 4 ,45	- 10 - 2	135° + 10	- 2:	10	(5)	-0.7 0.7	94	-15
259 337	β Andromedae 198	4 ,1	+35 5		OX3 60,3	2 .37 2 ,27	216 + 6	122° + 216	+ 0,5	41 41	(5)	0,4 4,0	96	27
260 338	ζ Phoenicis 241	4 ,2		B8		4 ,13 4 ,27	27 + 27	15°	Var.				263	61
264 343	O Cassiopelae 236		+54 37		3°,7 Y1	4 ,52 4 ,63	230 + 101		+11	24 26	(4)	0,8 6,3	93	- 7
270 351	χ Piscium 172		+20 30		5°,6 Ya	4 ,89 4 ,79	21 + 17		+15.7	12 12	(4)	0,3	98	42
271 352	r Piscium 190		+29 34		5°,7	4 ,70 4 ,64	- 81 + 10		+30,5	16 16	(4)	0,7 4,2	96	-32
281 360	q Pisclum 158		+24 3		5°,5 OY2	4 ,64 4 ,73	47 - 21	+ 42	+ 5,1	12	(6)	0,4 3,0	98	-38
288 370	v Phoenicis 346	10 ,6	<b>-46</b> 4	Go		4 ,88 5 ,17	687 + 309		+11,5				252	-71
294 377	45 Tucanae	12 ,4	<b>-69</b> 24			4 ,96 5 ,09	413		+ 9,2	160 160	(1)		260	-49
300 383	v Pisclum 220	14 ,0			2º,1 Y1	4 ,67 4 ,92	26 + 4	118° + 26	Var. + 5:	21 19	(3)		100	-34
304 390	₹ Andromedae 287	16 ,4			5°,4 Y2	4 ,99 4 ,99	41 + 27	84° + 31		17	(3)	1,1	97	-17
310 399	ψ Cassiopeiae	18 ,9			6°,4 OY8	4 ,96 4 ,94	<b>8</b> 6 十 69	67° + 52°	- 12,0	13	(4)	0,5	94	- <del>-</del> 6
313 402	# Ceti 244	19 ,0			7°,6	3 ,83 3 ,82	228 - 226	201° + 36	+17.5	27 26	(4)	0,9	119	69
314 403	o Cassiopeiae 248	19 ,3		-	3°,0 Y1	2 ,80 2 ,99	306 + 125	99° + 278	+ 9	55 47	(5)	1,2 5,2	95	- 2
417	ω Andromedae 307	- 1			4°,1 Y1	4 ,96 5 ,05	356	106° + 335	+10	34 33	(4)	2,5 7.7	98	16
325 424	α Ursae Minor				3°,8 Y1.6	2 ,12 2 ,21	44 + 16	89° + 41	Vаг. —17.4	12	(5)	-2,5 2,9	90	+27
329 429	γ Phoenicis 449		<b>-43 50</b>		6º,7	3 ,40 3 ,49	221 - 221	188°	Var. +25,7	24 24	(2)	0.3	243	<b>-7</b> 1
335 437	η Piscium 231		+14 50		5°,4 Y*	3 ,72 3 ,91	31 + 9	109°	+15,3	15 14	(4)	-0,6 1,2	106	-46
336 440	o Phoenicis 425		<b>-49 35</b>			3,96 4,10	194 + 161	40°	— б,5	31 30	(2)	1,4	251	-66
Bos	s 218. Also 2 Urs. M	lo. – F	loss 31/ To	vorioble v	with an a-			- ·						7

Bots 218. Also 2 Urs. Min. — Boss 314. Is variable with an amplitude of 0m,1. — Boss 325. ADS 1477. Caphold variable 1 2m,3—2m,4; is only 0,08 according to photoelectric measurements.

						1 <sup>h</sup>								
1	2	3	1	5	6	7	8	9	10	11	12	13	14	15
338 442	/ Cassiopeiae 260	27 <sup>m</sup> ,4	58°4	4′ K0	Хя 1г'0	4 <sup>m</sup> ,88 4 ,83	38		+ 6,8	14 13	(5)	0,4 2,8	96°	- 2°
350 458	n Andromedac 332	30 ,9	+40 5	4 G0	1°,4 1,3	4 ,18 4 ,28	418		28,6	79 78	(4)	3,6 7,3	100	20
357 464	51 Andromedae 467	31 ,9	18	7 Ko	Aa Q.'0	3 .77 3 .78	127 52	151°	1 15,9	21 24	(4)	0,7 4,3	99	-13
363 472	a Eridani 334	34,0	-57 4	5 B5	2,0	0 ,60 0 ,89	94	108°	+19	45 45	(2)		257	— 58
369 477	7 Andromedae	34 ,7	+40	4 B8	2°,3 W	4 ,90 5 ,15	29 - 11	151°	1Š	8	(t)	0,6 4,2	101	-2i
378 489	Piscium 293	36 ,2	F 4 5	9 K0	_6°,6 _Y³	4 ,68 4 ,66	21		+ 0, 1	2+: 20	(4)		Īij	- 54
384 496	p Persei	37 ,1	+ 50 I	1 Вор	2°,7	4,19	33 + 2	123°	Vai ? 1,4	14	(2)	-0,6 1,8	99	- 11
391 509	τ Cetı 295	39 ,4	— ĭ6 2	8 Ko	5°,5	3 ,65 3 ,68	1922 - 38	296°		312 310	(5)	6,1 10,0	142	-71
393 510	o Piscium 273	40 ,1	8 3	9 K0	5°,3 Y2	1,50 4,49	85		+13,8	14	(4)	0,1 4,2	114	50
411 531	y Cet1 352	44 ,7	-11 1	ı Fo	4°,0 Y1	4 ,77 4 ,89	178 - 148		- 0,9	35 35	(1)	2,5 5,8	134	67
416 539	ζ ( Gtı 350	46 ,5	-10 5	0 150	6°,2 Y¹	3 ,92	49		+ 7	39 32	(2)	1,5 2,4	135	<del>-</del> 67
419 542	& Cassiopeião 320	47 ,2	+63 1	1 B3	2°,7 W	3 ,44 3 ,63	43 F 9			11 12	(5)	1,2 1,6	98	<b>- 2</b>
421 544	α Trianguli 812	47 ,4	' '	6 1.5	42,1 Y2	3 ,58 3 ,66	233 - 168	161	- 12,6	40	(4)	1,6 5,4	107	-31
422 545	γ Arietis N 243	48 ,0		8 Aop	2',2 W	4 ,83 4 ,99	138	∦ <del>- -</del> 131		16 16	(2)	5,4		40
423 546	y Arietis S 243	48,0		9	2 <sup>t</sup> ,2 W	4 ,75	- 32	2 - 131		14	(1)	5,4		40
426 _ 549_	ξ 1 <sup>3</sup> 15c1um 290	48″,4	'	2 Ku	5°,8	4 .84 4 .85	33 + 3°	3 3	1-1-3ō	18 18	(4)	1,1 2,4	121	- 55
428 553	β Ariotis 306		'	9 A5	2°,6 W	2 ,72 2 ,96	147 25	5  - 144	√Ωι ? — 0,6		(5)	1,6 3,6		39
429 555	y Phoenicis			8 Mb		4 ,41	- 98	3 - 86	6,8			5,0	1	-66
433 558	φ Phoenicis 58 3		43	0 139	_	5 ,00 5 ,20	- 42	231	- -12				230	69
438 566	y Budani 244	52 ,0		7 G5		3 ,73 3 ,87	+ 269	676		78 78	(2)	8,0		-61
441 569	λ A11etis 288	52 ,4	-	7 A5	3°,5	4 ,83 5 ,03	90 - 75		- - 1	26 26	(4)	4,7		-36 -
442 570	η <sup>®</sup> Hyd11 101	52 ,4	68	9 Ko		4 ,72 4 ,83	+ 7		- 16,2	30 28	(2)	4,9	261	-49
445 574	Phoenicis 597	53 ,2	-47 !	3 G5		4 ,74 4 ,86	104 + 13		411.9	36 36		2,5 4,8	240	-65
446 575	A Cassiopeiae	53 ,8	F70 2	25 A3	3°,6 Y1	4 .61 4 .77	6			31	(7)	2,0 3,5		+ 9
449 <b>58</b> 0	50 Cassiopeiae 117	54 ,9	+71	6 A2	3°,1	4 ,06 4 ,18	4.		Vai ?	25	(4)		96	<del> -</del> 11
453 585	ν Cell 358	55 ,3	21	34 Ma	7°,2	4 ,18 4 ,17	13		°十17,9				165	-71
459 590	g Perser	55 ,0	+ 54	1 B8	2°,9 YG1	4 ,99 5 ,21	4	******	Var	10	(3)		101	- 6
458 591	α Hydri 162	55 .	6 -62	3 10	40,1	3 ,02 3 ,16	25		4- 7	67	1		1 255	-54
*		-												

Boss 146 Visual binary ADS 1598 5m,0, 7m,5, period 63 years

11 to 2h

					14	to 2h.						_		
	1	3	4	5	6	7		9	10	11	12	13	#	15
463	ø Piscium	56=.9	+ 2°17′	A2p	20,4	5=,23			Var.				1 <b>2</b> 4°	<b>−55</b> *
595	317 α Plectum	56 0	+ 2 17	A2p	B' 3°,1	4 ,33	42	98*	+ 9.9	20	(3)	0,4	124	55
463 596	317				w	4 ,12	+ 19		+ 9.3	20			132	<del>- 67</del>
467 602	2 Phoenida 659	57 .7	-45 12	K o		4 ,96 5 ,05	56 - 48		- 30,6	1		3.6		
468	y Andromedue)	57, 8	+41 51	Ko	54,4	2 ,28	70		-11,1	30 26	(7)	−0,6 1,5	105	-18
603 469	395 z <sup>2</sup> Andromedae	57 A	+41 51	Αo	As As	2 ,40 5 ,08	72	+ 69 140°	-12"	40		-0,6	105	18
604	395			]	BGs	5 ,20	- 10	+ 71				1.6	191	-72
474 612	# Fornacia 706	0.0	-29 47	AOp		4 ,74 4 ,90	12 + 5	80°	+18			0,1	<u> </u>	
477	a Arietis	1 ,5	+22 59	K.2	5°,4 Yª	2 ,23	239 + 17		-14,1	53 51	(6)	0,8 4,1	113	-35
480	506 58 Andromedae	2.5	+37 23	A2	20,8	4 .77	157		Var	24	(3)	1.7	107	-22
620	486			AS	3",3	4 ,9 <u>5</u> 3 ,08	+ 71 160		10,4	39	(6)	_5.7   _0.0	109	-24
482 622	/ Trlanguli 381	3 ,0	+34 31	-	Y1_	3,29	+ 70		71037	36		4,1	l	
499	b Andromedae	6 ,9	+43 45	Kop	69,9	5,08	- 10		-44,0	9	(2)	-0,2	100	-15
<u>643</u> 505	447 £1 Cotil	7 .7	+ 8 23	G5	50.5	4 ,54	20	254	Yar	7	(2)	-1,2	124	-48
649 517	345 7 Trianguli	41.4	+33 23	Ao	2º,7	4,64	- 21		- 4,0 + 6	21	(2)	1.6   0.7	111	-25
664	397	l		1	Yi	4 ,26	- 1	+ 65		21		3,2	.l	-60
524 674	φ Rridani 886	12 ,9	-51 59	B8		3,78	- 3°		1+10	15	(1)	-0,3	241	ł
530	o Ceti	14 .3	3 - 3 26	Mdp	70,0	2,00	23	181	+62,2		(1)		136	56
<u>681</u> 545	353 65 Andromedae	18 .9	+49 50	K5	5°,9	2 ,00 4 ,86	- 19 <u>1</u>		- 4,6	9	(4)	3.9 -0.9	106	- 9
699	656	<u> </u>	1		Oa	4 ,82	+ _	7 + 30		7	(1)	2,3	257	-46
548 705	ð Hydri 113	20 ,0	-69 7	A.2	1	4,26	+ 3	1 - 46	+11.	144		3,0	·L	ł
550	¿ Casalopatao	20 ,8	+66 57	ASP	3°,9 Y¹	4 ,59	+ 1	5 344 B 13	Ver + 3,3	27 27	(4)	1,8	100	+ 7
707 551	213 o Coti	21 .1	1 -12 44	AO	2.6	4 .77	2			14	(2)	0,6	152	-62
708	451	00.	8 + 8 1	Ao	₩ 2º,5	5 ,08	<u> </u>		Var.	14	(3)	3,1	129	-46
560 718	388	24 ,	+ 6 1	AU	W_	4 ,34 4 ,49	+ 2	2 + 32	+ 7	17	(3)	2.3		
563 721	# Kridenl 637	23 ,	3 -48 9	B5		4 ,44 4 .53	1	B 137				0,7	232	-61
575	σ Cetl	27 .	3 -15 41	P5	3°,5	4 ,82	14	1 215	9-29,		(2)	2,5	160	-62
740 580	e Fornação	20 .	5 -28 40	<b>B</b> 9	Y1	4 ,91	1 14 2		_	34	-	5,0	189	66
749	819	<u> </u>	ļ,	1	<u> </u>	5 ,12	2	3 - 16	+10	1	<u> </u>	2,2		1
604 779	8 Cett 406	34 ,	4-06	B2	2°,4 W	4 ,04 4 ,21		0 84 7 + 7	9+12	14	(2)	-3,0  -1,0	139	51
610	12 Persel	35 .	9 +39 46	Go	4°,5	4 ,99	19	184	d Ast.	29	(1)	2,3	1113	-17
788 611	610 s Brideni	36 -	0 -43 20	A2	1 ×-	5 ,15 4 ,53	9	8 + 132 0 115		29	-	<u></u>	220	-62
789	814				<del> </del>	4 ,67	<u> </u>	8 + 8		1_	1	4,3		1
614 794	i Reklant 689	30,	7 -40 17	Ko		4 ,06 4 ,12		14 104 11 + 122	1	2 31 31	(2)	1,: 4,:	215	-63
617	Ø Persei	37 .	4 +48 48	F8	4°,0						(7)		109	- 9
799 620	746 35 Ariotis	37	6 +27 17	193	2.1	4,32		7 + 29 14 16:	+23	5	(1)	6,9 -1,9	119	-28
801	424	1	1		Aı	4 ,85	i—	6 + 13	, l	5	1,	0,	3 l	I
المستعلمة	and 463. Bloomy AD	D 1015	17, 307			e a spani	ا معربسه	7 00	OCIAL DE		- ALC 1		M -	- TOP 105

Bear 45. Blazy ADS 1615: 2",7, 307" Hack companent is a spectroscopic blazzy No orbit determined for either pair ~ Bose 468.

Biany ADS 1630: period 55 years. — Ross 530. Vizziable: 1%,7 to 5%,5 in 332 days. Prototype for the Mint class; has a 10% companion 0",78, 128,9 (1926) evidently physically connected with a Caff.

2h to 3h.

1	2	3	4	5	6	7	8	9	10	11	12	13	11	15
622 804	γ Cetι 422	38 <sup>m</sup> ,1		A2	2º,9 Y <sup>8</sup>	3 <sup>m</sup> ,58	210 210	224°		36 36	(5)			48°
621 806	e Hydri 161	38 ,1	-68 42	В9		4 ,26 4 ,36	92		+ 6	-30			256	-45
627 811	л Celi 519	39 ,4	-14 17	B5	2°,7 W	4 ,39 4 ,55	- 16 - 16	207°	+ 15,0	11	(1)		160	<b>−59</b>
629 813	μ Celi 359	39 .5	+ 9 42	Fo	4º,0 Y¹	4 ,36 4 ,45	282 + 169	95°		32 32	(2)	1,9 6,6	132	-42
631 818	z <sup>1</sup> Eridanı 518	40 ,5		175	4°,5 Y2	4 ,61 4 ,70	327 + 177	82° + 275		57 57	(i)	3.4 7,2		-61
634 824	39 Arletis 462	42 ,0	-1-28 50	Ko	6°,4 Y3	4 ,62 4 ,65	196 - 27	191	- 15,0	19 18	(5)	0,9 6,1	_	-26
639 834	η Porseι 714	43 ,4		K <sub>0</sub>	6°,8 O <sup>8</sup>	3 ,93 3 ,92	30  - 9	+ 29		10 13	(6)	-1,8 1,3		- 3
642 837	ζ IIydrae 169		68 3	A2		4 ,90 4 ,99	† 20	+ 74		9	(1)	4.3	254	-46
643 838	41 Ariotis	14 ,1		B8	2°,6 W	3 ,68 3 ,75	132 - 28	+ 129	0	22 21	(3)	0,3 4,3		-27
644 840 645	16 Persei 646 β Fornacis	44 ,2		Fo Ko	3°,8 Y1	4 ,27 4 ,45 4 ,50	+ 72 190	十_199_		32 30 27	(4) -(2)	5,9	115	-18 -63
841 646	1025 17 Poises	44 ,9	-32 50 +34 39	IKO IK5	7°, 1	4 ,52	+ 177	1 68	十 13.9	27 13	(5)	5.9	117	-20
843 650	527 7 <sup>2</sup> Endani	46 ,5		Ko		4 ,64	- 34 53	H 69		12 16	(4)	4,1	173	Ē1
850 653	509 7 Person		+52 21	Go i	4".0	4 .80 4 .06	- 31		1	16 20	(5)	6,2	i	- 5
854	641 R Hoiol		5 - 50 18	A5 }	Ā,	4 ,13 4,0—10,2		8 +	4-60	.17		1,4		58
868	- 860 v Hydri	1	<b>-75 29</b>	ĪK2	-	4 ,70	63			15	(2)		259	- 4ō
872 665	204 η Eildani	51 .	- 9 18	-KO	54,8	4_,82 4_,05	+ 3; 229	160	20,4	15	<sup>-</sup> (2)	3,6	155	
874 668	<u>553</u> # Perser	52 ,	+39 16	A2	Ya 20,5	- 4 ,05 4 ,62	= 137 63	3 143	+18	27 19	(2)		1116	-16
879 670	68 i 24 Persor	52 .	+34 47	-Kō	6°,1	4 ,85	6:		-36,0	19	(2)		119	- 20
882 674	550 8 Arietis	53 ,	+20 56	A2	0Y2 3°,2 W, Y	5 ,02	- 40	7 242	- 8 - 6}	12   13   13	(2)	4,0 0,2 0,2	127	- 32
887-888 679 896	λ Coti	54 ,	F 8 3Ī	B5	2°,5	4 ,80 4 ,69 4 ,91	- 10 - 11 + 2	-1 -		9	(2)	-0,5	136	-42
680 897	#55 #Endani 771	54 ,	-40 42	A2	3°,8	3,42	6 + 3	7 301		22			215	-60
681 898	∂ <sup>2</sup> Eridanı 771	54 ,	540 42	A2	3º,8	4 ,42 4 ,63	7 + 2	7 285	°-1-19			3,8	215	-60
691 911	a Coli 419	57 ,	1 + 3 42	Ma	6°,7 O8	2 ,82 2 ,85	7	8 190 6 + 41	°-25.3	22		-0,5 2,3	141	
694 915	γ Poisci 054	57 ,	6 +53 7	F5 A3	4º,5 Y <sup>2</sup>	3 ,08 3 ,19	1	0 156 2 + 10		21		1,9		
697 918	k Persei 767		0 +56 19	Ko	5°,5 Y2	5 ,08 4 ,98	+ 4	0 - 58		19		4.3	108	1
696 919	τ <sup>3</sup> E1idani 1387		0 -24 1	A.3	4º Y1	4 ,16 4 ,33		0 - 120		28 28		5,0		
698 921	Q Persei 630	58 ,	8 +38 27	Mb	6º,6	3,4-4,3		3 128 2 169	+28,2	18		4.0		-16

Boss 674 The components of this binary, ADS 2251, are in the RHP system 5,55 and 5,25 - Boss 698 Irregular variable

1084 Appendices to Chap 4 K.Lundmark . Luminosities, Colours, Diameters, etc. of the Stars

3h.

						<del></del>								
1	2	3	4	5	6	7	8	9	iD	11	12	13_	14	15
705 932	Се <b>мі</b> ореіне 168		+74° 1	<u> </u>	2°,4 Y¹	4 <sup>10</sup> ,89 5 ,10	88 32	+ 82	+24 '	15 15	(2)	0,8 4,6		+15°
708 936	# Persei 673	1 .7	+40 34	198	1°.9	2 ,1 2 ,47	- 5	125° + 7	Var + 5.7	34 33	(3)	-0,3 3,1	116	-14
710	Persol	1 ,8	+49 14	Go	4°,1 Y <sup>8</sup>	4 ,17	1269		+50,3	104 101	(4)	_	112	<del>- 7</del>
937 713	857 и Регвоі	2 .7	+44 29	Ko	5",8	4 ,25	240	130°		23	(6)	0,7	116	-11
941 717	631	4 9	+39 14	Ko	Y* 5°,4	3 ,99 4 ,82	+ 53 22	+ 233 278°	+ 6,1	13	(4)	5,9 0,2	118	15
947	724				Y	4 .75	<b>— 16</b>	- 16		12		1,5	131	-31
718 951	d Arlotis 477		+19 21	Ko	X. 3	4 ,53 4 ,56	152 + 111	+ 103	+24,6	22 19	(5)	5,4	_	
723 963	a Pornacia	7 .8	-29 23	P8	5",6 Y <sup>a</sup>	3 ,95 4 ,04	726 + 711	26° + 152	-20,7	82 82	(3)	3,5 8,3	191	<b>—57</b>
730	ζ Arletis 527	9 ,2	+20 40	AO	2º,6 W	4 ,95 5 ,13	79		+15	15 15	(5)	0,8	130	-29
739	Rridani	11 ,0	- 9 11	A3	3°,8	4 ,90	45	355°	Ver				159	-49
984 741	624 Camelopardalis	11 ,2	+65 17	Взр	2°,3	5 ,08	+ 35 12	115	Var.	8	(1)	$=\frac{3,2}{0,7}$	105	+ 8
985 746	340 Persei	12 ,5		Ko	7º.2	5 ,00	+ 6		+ 2,2	10	(4)	0,2 -0,1	123	18
991	619				7°.2 Y*	4 ,91	- 3	+ 13		10		0,5	146	-42
752 996	и Cetí 618	14 ,1	, -		A1	4 ,96 5 ,08	282 + 254	+ 124		105	(3)	7,2	<u> </u>	
755 999	Arietia 576	14 ,3	+28 41	K5	6°,6	4 ,72 4 ,61	- 18	186 + 20	- 2,1	13	(3)	0,3	126	-22
757 1002	1 Peraci 750	14 ,7	+42 58	A2	2°,9	4 ,98 5 ,19	- 58 - 53	260°	Ver - 6,6	15	(2)		118	-10
759 1003	r Erideni S84	15 ,1	-22 7	ЖЬ	60,9	3 .95 3 .94	6		+42,4		(3)		179	-34
764	e Erideni	15 ,9	-43 27	G5		4 ,30 4 ,38	3168		+86,8		(1)		216	<b>—55</b>
100B	4028 # Porsei	17 ,2	+49 30	7.5	3°,4	1 ,90	39	136	- 2,1	23	(4)	-1,4	114	- 5
778	917 o Tauri	19 ,4	+ 8 41	G5	4°,9	3 ,80	10		Var	22   17	(5)		142	<b>- 36</b>
1030 780	511 Porsel	20 ,9	+48 43	<u> 195</u>	24,1	3 ,85	- 10°	2 + 10 2 120	-20 Var	15	(5)	3,9	1115	- 5
1034	920				W	5 ,18	_	+ 30	+11	8	L	2,5		+ 4
781 1035	Camalopardalla 660	21 ,(			3°,8	4 ,42	_	4 104° 3+ 3	- 6,6	7	(2)	_2.6		
784 1038	f Tauri 439	21 ,	+ 9 2	B8	2°,3 YG¹	3 .75	† 1:	2 125 6+ 70	Var	17	(1)	3,0		36
786 1040	Camelopardalia 607	21 ,	+58 3	Aop	4°,5	4 ,76 4 ,86	1		Var - 8,4	2		-3,7 0,0	110	+ 3
790	34 Persol	22 ,	+49 10	B5	2',0 Y1	4 ,67	4	4 139		9	(6)		116	5
791	945 Camelopardalla	22 ,	+ 55	/ A2	2.1	4 ,89	3		+ 4	14	(4)	0.7	1112	ō
1046 795	o Persol	23 -	5 +47 3	Ko	₩ 6°,4	5 ,21 4 ,55	<u> </u>	9 — 16 3 — 15	9+14,5	14		0.1	1116	- 6
1052	843 Persed		4 +43 3		O <sup>8</sup>	4 ,51 0,0—13,	+ 1	7- 15		13		1,4		
1057	l		<u>.</u>	Nova	ļ		_ 1	3+ 10				<u> </u>	7	
804 1066	f Tauri 486	25 ,	4 +12 3		5°,3	4 ,28 4 ,33		1+ 14		19 18		0,0	5	-33
806 1070	17 Erideni 674	25 .	6 - 5 2	5 B9	2*,4 W	4 ,80			+ 9	10	(B,)	Τ.,	157	<b>-45</b>
				. '			4				411			-

Box 703. Algel or Algol. A inipie spectroscopic system with puriods of 29 days and 1,87 years, respectively

3h.

_						5" <b>.</b>									
	3	ş		5	6	7	8		9	10	11	13	13	11	15
	27 <sup>m</sup> ,6	-63°	18′	F5		4 <sup>m</sup> ,80 4 ,93	519 + 88	+	44° 509	+12,0	ļ		8,3	214°	-46°
ļ	28 ,2	9	48	Кo	5°,8 Y³	3 ,81 3 ,81	972 - 573	,	271° 787		290 290	(5)		164	-47
	29 ,4	<del>1</del> -47	51	В5р	2º,8 YG1	4 ,26 4 ,52	+ 10	+	127° 41	+ 3	10	(3)	-1,0 2,5	117	- 5
	29 ,4	-21	58	<b>J38</b>	3°,6 W	4 ,32 4 ,49	44	1	117 <sup>6</sup>	+-15,0	13	(1)	-0,1 2,5	181	-51
	31 ,8	+ 0	5	G-5	4°,4 Y2	4 ,40 4 ,43	536 - 509		206°	-1-28,3	71 73	(4)		153	-40
	33 .5	-4ō	36	Ko Ko		4 ,58 4 ,61	44 - 42	1	191°	+ 9,9	18 18	(2)		212	-53
	35 ,8	+47	28	B5	2°,5 W	3,10	46 + 11		136° 45	+13	14 13	(6)	-1,3 1,4	118	- 5
9	37,3	+63	2	1· 5, A 0	4°,5 Y2	4,96 5,00	- i	1 .	163°	Var 2,8	12 12	(2)	0,4	109	+ 7
	38 ,0	+31	58	131	2°,7 YG1	3 ,94 3 ,99	20		157° 26		8	(3)	- 1,5 1,0	128	-17
	38 ,3	32	15	B5		4 ,93 5 ,11	+	7 —	324°	Var + 2,6			-0,4	197	-52
	38 ,4	1 42	16	L 5	3°,8 Y¹	3 ,93 4 ,02	1 .	7	276° 5	-13,1	19 19	(4)	0,3 1,3	122	- 9
	38 .5	-10	6	Ko	5°.7	3 ,72 3 ,71	749 + 53		353° 532	1	110 110	(4)	3,9 0,7	166	-45
	39 10	-  23	48	135p	3",0 W	3 ,81 1 ,01	- 1		52	+ 11	15 14	(6)	-0,5 2,4	134	-22
	39 ,1	-37	38	K2		4 ,64 4 ,65	- 7		85	+ 9,9	16 15	(2)	0,5 4,8	207	-51
	39 .3	24	10	B5	2°,9 W	4 ,37 4 ,59	- 1	9 7 +	167°	+ 6	12 11	(5)	-0,4 2,8	134	-22
	39 ,8	¥71	1	Ao -	2°,6	4 ,67 4 ,84	A	6 - 7 +	141 46		19 19	(1)	1,1 3,0	104	+14
	39 ,		4	135	2°,9 W	4 ,02 4 ,16	5	↓ 0 - -	147 54	+10	12 12	(5)	-0,6 2,7	134	-22
IS	40 ,4	1 65	13	Ma	7°,1	4 ,71 4 ,58		4 3 —	284 3	- 3,2	9	(3)	-0.5 $-2.3$	108	+ 9
	40 ,4	1 4 23	39	135	2°,9 W	4 ,25 4 ,42		9 0 <u>十</u>	58	° +- 1	12 11	(4)	3,1		-22
_	41 ,	1 12	25	Ma Ma	7°,5 OY2	4 ,64 4 ,60	+ 6	9 8 —	30 7		12	(1)	3,8		-45
	41 1	F 23	48	135p	2°,9 G1	2 ,96 3 ,13	- 1	2  0 +_	51	+ 5	20 17	(6)	1,5		-22
	42 ,			1.8	Yı Yı	4 ,33 4 ,42		8 ±	38	7.1	60	(3)	8,0		
	1	9 65		Ko		3 ,80 3 ,96		4-4-	76 270	+50	24 24	(2)	6,	_	
_	1	2   -23		1	3°,1 YG¹	3 ,80 3 ,96		3 0 +	52	°+ 3	7		2,4		
		$\overline{9} - 3\overline{7}$				5 ,42 5 ,56		9	77	°- - 15,9	25	(a)	1,4 4,5		50
	1	9 - 37				4 ,86 5 ,00	_ 2	32 24 +	. 79				4,		
		7 -30		l		4 ,24 4 ,27	<u> - '</u>	1  8	53		16	` `	3.	3 205 5	
~	47 ,	8 +31	35	B1	2°,8 Y1	2 ,91 3 ,12		3+		19,:	2 3		-4, -0,		-15

Boss 856 Taygeta — Boss 860 Maia — Boss 869 Aleyone — Boss 877 Atlas A difficult binary 0" 43, 39°,4 ; 881, 885 Doubtless II physical pair,

					8	to 4h.								
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
896 1204	Cemelopardalis 628	48=,6	+62*47	В9	2°.5 Y¹	4 <sup>n</sup> ,87 5 ,12	+ 5	68° + 1	+ 6:	13 13	(3)	- 1,6	L	+ 8*
899 1208	7 Hydrl 276	48 ,8	<b>-74 33</b>	Ma.	6",0	3 ,17 3 ,36	124 + 38	21° + 118	+15.7	17 17	(1)	-0,7 <b>2,</b> 7	256	<b>— 38</b>
901 1211	32 Eridani ) 631	49 ,2	- 3 14	A	G <sup>2</sup>	6 ,33 4 ,73	160 + 22	145° + 158				0,6 5,7	159	<del>- 39</del>
901 1212	32 Erldani 631	49 ,2	- 3 14	G5	6°,0	4 ,95 4 ,73	34	83° 十 20	+26,9	12	(5)	0,4 2,5	159	39
902	e Briden!	49 .5	-24 55	18 5	4 Y1	4 ,76 4 ,91	34		Var +23			2,5	187	-48
910 1220	Persei	51 ,1	+39 43	B1	2°,2 W	2 ,96	39		Var	5	(6)		125	- 9
913	895 F Persel	52 ,5	+35 30	Oe 5	3",2 Y1	4 ,05	+ 20 + 2	142	Var. +67.4	1 2	(2)		129	-12
915	775 7 Brideni	53 ,4	-13 48	K5	7°,0	3,19	130 - 57	151	+61,5	23 23	(4)		173	-43
920	781 2 Touri	55 ,1	+12 12	В3	2°,3	3,4-4,2 3,7-4,2	15		Var. 13,0	2	(2)	31-	147	-28
923	539	55 .7	-24 (E	ÅOp	2 W	4 ,69	9	63	Var +23,2	12	(m.)	0,1	187	-46
930	8 Reticuli	57 ,2	-61 41	Ma	17	4 ,41	十 7	165*	- 0,8			0,9	241	-43
932	# Tauri	57 .8	+ 5 43	Αo	3°,0	3 .94	7	172*	- 6	23 22	(4)		152	-32
936	581 A <sup>1</sup> Tauri	58 ,8	+21 49	Ko	50,4	4 ,15	113		+ 9.9	19 18	(4)		140	-21
938	385 2 Persel	59 ,1	+50 5	Ao	3,0	4 ,48	+ 47	185"	+ 5.	16	(2)	0,4	120	0
940	7 Reticuli	59 .5	-62 27	МЬ	W.	4 ,52	2	7	- 5.9	16		2,2	240	-43
941	Reticuli	59 .7	-61 22	K5		4 ,58	+ 17	28"	+60,5	-		1,2	239	-43
1266 947	c Persel	1,4	+47 27	Взр	2,8	4 ,92	44		Var	12	(4)		122	<b>– 3</b>
963	939 o Brkiani	7 ,0	- 7 6	F2	¥G1	4,26	+ 10	6	+ 4	22	(3)		167	-37
1298 966	8 Horologii	7 4	-42 15	Fo	<b>T</b> 1	4 ,24	+ 62	710	+37:	21	<u> </u>	3.7	223	-45
1302 967	μ Persol	7 1	+48 9	Go	5*,5	4 ,98	+ 4		Var.	16	(3)	6,4 -0,2	122	- 1
1303 970	1063	8 ,1	+40 14	Gō	6°,1	4 ,33	3		+ 7.8 Var.	13	(2)	1,7 -2,7	_	- 7
1306 972	912 47 Tenri	8 ,	+ 9 1	G5	20'0	4 ,89	+ 4	4+ 31 6 196°	+ 3 - 6,4	10	(2)	2,4	151	28
<u>1311</u> 981	669	10 ,	+ 8 38	<b>B</b> 3	2°,6	5 ,02	- 2°	7 + 24 4 126°	+17	10	(4)	2,8 -0,7	151	-28
1320	657 b Persel		7 +50 3	A2	3°,0	4 .52	+ 1	3 + 32 6 135°	Var,	10		2,0		+ 1
1324	0 Eridani		7 - 7 49	1	W	4 ,80		8 + 71		16		4,0		-37
1325 985	780 a Horologii	1	7 -42 32	Ko	5°.7	4 ,52 3 ,83		2 + 899		207		12,5		1
1326 989	1425		+20 20		2,9	3 ,91	- 2i	7- 31		35	Ľ	5.5		-20
1329 994	724		1 -62 1	1	4°,4	5 .08	- 5	4 + 38		28	<u> </u>	3.9		-41
1336	332	1.3	-62 43	1 93	1 45,4	3 ,36 3 ,51	+ 1	0+ 69	+35.5	22		2,6	241	-41

Boss 901 ADS 1939, 6",98, 347",2 (1923,8). The dynamic parallex is 0",002. Probably a physical system although the proper motions differ considerably — Boss 920. Edipsing binary Pariod 3,923 days.

4h.

	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1				—— <u></u>				<u> </u>	<u> </u>				227°	-44°
995	γ Doradus	13 <sup>10</sup> ,4	-51°44′	F 5		4 <sup>m</sup> ,36 4 ,48	202  + 89	27° + 182	+27   	- }	1	5,9	441	— 4 <i>7</i>
1338	- 1066   7	14 ,1	+15 23	Ko l	5°, i	3 ,86	120		+ 38,5	25	(7)		147	$-23^{-}$
1346	612	\	13 -5		$\mathbf{Y}_{3}$	3 ,90	E .	+ 77		25		4,3		<b>-</b> .
1001	v4 Eridani	14 ,1	-34 3	В9		3,59	58			- {	1		202	-44
1347	1614					3 ,77	<u>  4</u>		+17.6		- <sub>(4)</sub> -	2,4 -0,9	124	2
1003	d Persei	14 ,3	+46 16	<b>B</b> 3	2°,8	4 ,89 5 ,07	45  + 8		1	7 7	(4)	3,2	124	
1350	872 & Reticuli	14 ,7	-59 32	K2		4,12	177		+28,8	31	(2)		237	-42
1005 l 1355	324	1 77	39 32		ì	4,54	- 65	k		29	` _ }	5.7		
1017	di oi d Lauii	17 ,2	+17 18	K0	5°,5	3 ,93	115		° - - 38,5	25	(7)		146	-21
1373	712				Y25	1 _00	+ 83			25	10	4,2	146	-21
1022	δ <sup>2</sup> or 64 Tauri	18 ,4	+17 13	A5	2°,5 YG¹	4 ,84 5 ,09	124	109° 5 +89	°  Vai  -}-36,6	25 24	(5)	5,3	140	
1380 1026	714 2 Tauli )	10	22 4	A3	$\frac{10}{3^{\circ},1}$	$-\frac{5}{4},\frac{.09}{.36}$	112			26	(5)		143	-17
1387	642	יי, ענון	724 7	1-5	YG1	4 ,57	1	1	1	26		4,6	}	_
1027	ж <sup>2</sup> 01 67 Tau11	. <sup>-</sup> 91	$+21^{-58}$	To	20,9	5 ,42	132		° - -16	22	<u>(1)</u>		143	17
1388	643 J	ll			Y <sup>1</sup>		+ 79		0 1 0 0 3	22	/ t-\_	6,0	146	$-\bar{20}^{-}$
1029	δ <sup>8</sup> or 68 I auri	19 .	7 +17 42	A2	2°,4 YG1	4 ,24 4 ,48	109		° +- 36,3	29   28	(5)	4,4	140	_20
1389	719   υ <sup>1</sup> or 69 Ιαυιι	<u> </u>	3 +22 35	- A5	30,6	4 ,40	12:			25	(4)	i,4	142	<u> </u>
1033 1392	696	20 ,.	3 1 22 33	1-3	Y1,5	4 ,56	- - 7	7 + 96	+33	25		4,8		
1032	d Endani	20 ,	3 - 34 15	IX 5		4 ,06	7			15	(1)		202	-43
1393	1664					4,11		3 + 58		15	(6)	-3.6	148	21
1034	71 Lauri	20 ,	6 + 15 23	A.5	3º,0 Y1	4 ,60 4 ,89	11-			20	(6)	5,0		2.
1394	625 π Tau11	20-	9  -11 29	Ko	5°,3	4 ,91	- 3 · 3	1 .	_		(1)	1	148	21
1036 1396	697	20 ,	יניי זון פ	1	Y <sup>3</sup>	4 ,95		6 31	1 '	10	`	2,7		1
1044	s Janu	22 ,	$\frac{18}{8} + 18^{-58}$	Ko	5°,4	3,63	12			32	(5)		146	18
1409	640				Y2	3.73		9 <del>+</del> 80		31 28	161	4,0	148	-20
1045	91 fami	22 ,	8 + 15 44	17.0	5°,6 OY3	4 ,04 3 ,99	10	1 + 71	°-1-37.7	29	(6)	4,2		20
1411	631 92 Lauri	- 22	9 + 15 39	- <sub>170</sub> -	20,9	3,62	10	7 -104	° Vai	33	(6)		148	-20
1046 1412	632	, 22	7 7 7 3	1	w	3,73		0 -1- 71	1 -1-42,6		) ` '	3,8		_
1054	lauri	24,	8 15 59	A5	30,0	4 ,84	11			27			148	20
1427	637	1.			Y1		1-1-8	7 + 77 3 180				5,2	163	29
1063	45 Eridani	26 ,	8 - 0 16	KO	5°,3 OY2	97, 4 97, 4	\		)° ++ 16,2 }	'\	1	-2,		
1437	713 Q Tauri	28		$\Lambda \bar{s}$	3°,3	4 ,75		- !		24	(5)		5 150	-20
1067 1444	720	20	,2 1 10		Yı	4 ,92		0 + 63	7	23		4,		
1073	v1 Eridani	29	6 - 29 57	Ko	40,4	4 ,59					1 7 1	6,	1 197	41
1453	1883				- 60.0	$\begin{bmatrix} -4 & 59 \\ -4 & 46 \end{bmatrix}$		33 — 64 35 — 194		$\frac{136}{9}$	1		7 129	_ 3
1074	e Peisci	29	,7 <del>  1</del> -41 4	K0 A3	6°,2 OY <sup>4</sup>	4,46		14 - 2				1,		
$-\frac{1454}{1077}$	1000 « Lauri	~   <sub>30</sub>	,2 +16 19		6°,3	1,06						0,	5 149	19
1457	629	١٠٠	,2 ( 10 .)		OY3	1,08		18]+- 20.	3	_ 70		2,		
1076		30	,2 + 9 57	A 3	3°,2	4 ,38		56 13		21			9 154	-23
1458		_			Yı.	4 .51			4 <u> +28,</u> 0° Vai	1 20			4 168	3 = 30
1079		31	$ \vec{3}  = 3^{\circ} 33$	B2	2º,7 W	4 ,12 4 ,28			2 -+ 15,4			-4		
1463 1080		- 31	7 -30 46	Ko	50.7	3 .88		59 26		_   ~ .		0,	2 198	3 -40
1464		"	,,, ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		. Ì	3 93	3	10 - 5	8	18				_}
1081		31	-55 15	AOp	3°,8	3 ,47	7		2°-+25,	6		,	230	0 -41
1465	663	_		1		3 ,62		$\frac{41}{04} + \frac{3}{9}$	3 6° Vai	+ ,	1 (5)	2	8 15	3 -21
1087		32	,6 +12 19	A3	2°,9 W	4 ,30			5 -1-54	3	1		4	-
1473	618  oss 1026, 1027   Pro	dvalder =	i nhugical nair	Also m						•	•	•		

Boss 1026, 1027 Probably a physical pair Also member of the Taurus cluster - Boss 1076 Eclipsing binary

## 4088 Appendices to Chap 4 K Lumphann' Luminosities, Colours, Diameters, etc of the Stars

4b.

				-т-		-	<del>4</del> ",	_				T	40			<del></del>
		3	4		5	6	7		-+	9	10		12	D	14	13
1090 1479	666	33**.5	+15°		<b>A</b> 3	2°,9 Y¹	4 <sup>m</sup> ,85 5 ,00	+_	84 66	104° + 52	Var +22	24 23	(4)	1,7 4,5	149°	19°
1091 1481	l Eridani 933	33 .6	-14	30	Ka	5°,6 OY3	3 ,98 4 ,01		179 170	205° + 55	Var +41,8	36 36	(2)	1,8 5,2	179	<b>—35</b>
1101	R Doradus	35 ,6	-62	16	Mo	<del></del> -	Var		125	226	+26,1	-			239	<del>-39</del>
1492		36 ,1		-	Ma	6°,8	4,8-6,8 4,54	±_	28 94	- 121 165°	22.5		(2)	5.3-7.3	185	25
1105 1496	988	1, 00	-19	52	I	O <sup>®</sup>	4 ,53	<b> -</b> -	62		- 33.5	13	(4)	0,1 4,4	ן נפין	<b>-36</b>
1107 1497	739	36 .2	+22	46	B5	2",3 W	4 ,33 4 ,50		23	165°	+ 9.6	9	(4)	~0,9 1,1	144	-14
1110 1502	σ. Caoli 1587	37 .3	-42	3	F2		4 ,52 4 ,63	_	169 12	238° 169	Vor. - 1,3	27 27	(1)	5.7	213	-41
1123 1520	# Erideni 876	40 .5	- 3	26	B5	20,5 W	4 ,18 4 ,34	+	22	117		10	(4)		168	- 28
1139 1542	a Camelopard 358	44 ,1	+66	10	Во	3°,0 ₩	4 ,38 4 ,56	+	9	55		-6 2	(3)		112	+15
1140 1543	# Orionia 762	44 ,4	+ 6	47	F8	4°,0 Y <sup>1</sup>	3 ,31 3 ,45		471 438	87	+25,0		(4)	3.7 6.7	159	<b>–</b> 2ι
1141 1544	na Orionia 777	45 ,1	+ 8	44	Ao	3°,0	4 ,35 4 ,60	Ė	33 19	191	Var	22 22	(1)		157	<del>-20</del>
1148 1551	2 Auriges 952	45 ,9	+36	33	K2	6º,6 O	5 ,04 4 ,96		26 19	211	— <del>16.</del> 7	11	(1)	-0,8 2,1	134	- 3
1147 1552	n <sup>4</sup> Orlonia 745	45 .9	+ 5	26	В3	2°,5 W	3 ,78 3 ,98		7	214° + 4	Var. +23.3	4	(5)	_	161	-23
1149 1556	e <sup>1</sup> Orlonia 777	46 ,9	+14	5	Ma	7°,6	5 ,19 4 ,98	_	59 21			10	(=)		153	-17
1153 1560	∞ Eridani 1068	48 ,0	<b>— 5</b>	37	Fo	4",6 Y1	4 ,45 4 ,59		<b>27</b>	315 - 26	- 8·	30 30	(1)		172	-27
1159 1507	π <sup>a</sup> Orionia 810	49 ,0	+ 2	17	В3	26,1 W	3 ,87 4 ,04	_	4	225°	Ver +23,4	5	(6)	-2,6 -3,1	164	-23
1161 1568	7 Camelopard 829	49 .3	+53	35	A2	2°,7 Y1	4 ,44 4 ,66		12	305° — 9	Var - 7.9	21 21	(2)	1,1 -0,2	122	+ 8
1163 1570	ភា Orlonia ៩៩៩	49 ,4	+10	0	Ao	3°,2	4,74		145		+ 4	17 17	(3)	0,9 5,6	157	-19
1107 1577	s Aurigno 866	50 .5	+33	0	K2	6°,1	2 ,90 2 ,89	+	28 1	162° + 28	+17.5	25 25	(5)	-0,7 0,1	138	<b>→</b> 5
1169 . 1580	of Orlonia 740	50 .7	+13	21	Ko	5°,9 Y®	4 ,28 4 ,25	_	102 98			19 19	(3)	0,7 4,3	155	16
1178 1592	4 Aurigae 1005	52 .5	+37	44	Ao	2°,5	4 ,99 5 ,16	+	115	+ 113	+ 6	33 33	(1)	2,5 5,3	135	- 1
1181 1601	of Orlonia 872	l	Ι'	33	K <sub>0</sub>	0.0	4 ,73 4 ,66	_	6 5	+ 3	+ 14,0	15 15	(3)	0,6 1,4	165	-23
1185 1603	# Camelopard, 856			- 1	Gop	5°,1	4 ,22		13	+ 13		5	(5)	-2,3 -0,2	117	+12
1187 1605	# Aurigae 1166		L'		F5p	4°,3 Y	3,31-4,01 —	+	14	+ 14	<u> </u>		(3)		132	+ 2
1189 1611	S Kridani 1047		3 —12		Fo	4° Y1	4 ,85 4 ,99	_	107 22	+ 105		22 22	(1)	1,6 5,0	180	29
1190 1612	¿ Aurigae 1142		+40			O*	3 ,94 3 ,90	+	32	160 + 32	Var + 11,0	24 11	(3)	1,5	.L_	+ 1
1192 1617	ψ Eridani 948	56 ,6	6 - 7	20	B8	2',9 W	4 ,81 4 ,98	+	10	- 9		5 5	(3)	-1,7 -0,2	174	-26
1194 1620	751	l	+21		AS	3 ,1 W	4 ,70 4 ,90	+	82 52	+ 64		16 14	(5)	0,4 4,3		<u> </u>
1193 1621	Leports 990	57 .	1 -20	12	В9	2°,4	4 ,99 5 ,16	+	41	+ 39	+24			3,1	187	-32

Boss 1101. Long period variable, pariod 345 days. — Boss 1187. Long period solipsing binary, pariod 27,1 years. — Boss 1189. Probably not a variable.

4h to 5h.

					- 4"	to 5 <sup>n</sup> .								
i	2	3	4	5	6	7	8	9	10	11	12	13	16	15
198 628	Lepous 1975	58 <sup>m</sup> ,1	-26°2	5' K0	6° O2	5 <sup>n1</sup> ,01 5 ,00	122 41		31° +27	,8		5,4	194°	
202 637	9 Aurigae 1024	58 ,8	+51 2	9 10	3°,9 Y1	4 ,99 5 ,15	178 - 55		85° 1	4 4		3,2 6,2	125	+ 8
203	11 Orionis	58 ,5	+ 15 1	6 - 1B9	2°,3	4 ,65 4 ,95	41	1	52° Vai 40 + 15			-1	154	14
638 204	732 η Aurigae	59 .5	+41	6 B3	1º,8 B1	3 ,28	81		58° - 2		1 (5)		133	+ 2
$\frac{641}{208}$	<u>γ Caeh</u>	8, 0	—35 <sup>-</sup> 3	7 Kō	60,0	3 ,48 4 ,62	128	3	ī4°į+11	. 1	(2)	t .	206	-35
6 <u>52</u> 211	2089 ε Lepoiis —	1,2	-22 3	0 K5	6°,2	4 ,64 3 ,29	82 72	2 1	99 59° + 0	,9 2	8 (4)	0,5	191	-32
654 218	- η <sup>2</sup> Pictoris	2,3	-49 1	3 K5	OY2	3 ,34 4 ,92	39	5	60 78°+36	0 2	6 (a)		223	36
663 220	1662 B Isridani	2,9	 5 I	3 A3	30,2	5 ,02	- 24 118		26 28° – 11				173	
666 225	1162 5 Doradus	_ '	57 3	_	Ψ1	3 ,12 4 ,76	- 11; 11;		33 37° — 2	4	5	3,3	233	${-36}$
671 227	735 15 Orionis	4,0		8 10	40,1	4 ,89	-  84 1		76 58°+31	4 1	3 (1)	5,0 0,1	155	$-\overline{1}_3$
6 <u>76</u> 231	752 - 7 Fridani	1,4		_	20,6	5 ,08 4 ,31	+	1 -}-	11 60° V	1	3   7   (3)	0,1	177	-25
679	1040			<u> </u>	Y(+1 3°,0	1,54	1	1 1	9 ± 3	3	$\frac{7}{6}$ (3)	-0.7	136	1
236 689	μ Aurigae - 1063	6,6	_		Y1 20,7	4,99	3	3 ⊦_	68 +20	) ] 3	5 (2)	4,2		-20
239 696	1095 1095			59 B8	]_W	4,54	- 1	7-1	27	_  _1	0	3,1		<u>-19</u>
240 698	<i>θ</i> Orionis 888	8 ,1	[ .	15 Ko	OY3	4 ,64 4 ,61		7 F_	13 +3	3,8 1	9 (2)	0,5		
241 702	μ Lepous 1072	8 ,4	- 16	l	W	3 ,30 3 ,48	1	6	125° +-2 47	2	6 (1) 6 (1)	1,8		-27
242 705	и I epons S 1092	8 ,7	13	3 38	2°,8 W	4 ,46 4 ,60	- 2	2 -	236° - -2°	- 1	6 (2)	1,2		-26
246 708	& Aurigae	9 ,	4-45	54 G0	3°,3	0 ,21	43	9 -	168° - -34 137		37 (4) 35	3,4		
250 713	β Orionia 1063	9 ,	7 - 8	ī9   B8p	1°,2	0 ,34		1 :	135° Va	ս 3,6	6 (2)	5.8 9.1	3 176 7	24
258 726	16 Aurigae 1000	11 ,	G +33	17 Ko	6°,3	4 ,81	•		159° Va 185 —2	- 1	20   (3) 19	1,2 6,2		1
259	λ Aurigae 1248	12,	1 + 40	1 G0	4°,6 Y2	4 ,85 4 ,90	84	В	141°+6 742	6,6	74 (6) 70	)   4.:   9.:	1 135	+ 3
729 262	7 Orionis	12 ,	8 ~ 6	57 B5	3°,1	3 ,68 3 ,84	7		246°   1 0	8	10 (3, 10	) = 1,: -0,:		-23
735 270	o Columbae	13 ,	9 -35	0 <b>K</b> 0		19,4	35			1,2	32 (2 32		4 200	-33
743 269	2214 Doradus	13 ,	9 -67	18 Ko	-	4 ,78		18	353° V	an	13 (2 13	$\begin{pmatrix} 0_1 \\ 0_2 \\ 3_1 \end{pmatrix}$	4 244	-34
744 277		15,	0 -13	17 Bi	20,6	4 ,90	-	19 F 3 1 —	00-1-2	0,0	5 (2	) 2,	2 182	-24
756 281	1127		2 -21	20 A 0	- W 2°,8	4 ,45	:	20	3 45°+3	<u>o</u> †	5 12 (1		1 1190	-28
762 284	1135	16	7 - 0	29 .B3					233 +	27,9	12 5 5 5	)   1, ;)   1,	9 170	<u>-18</u>
765 289	930	-	,6 + 3			4 ,81		5 <del>   -</del> 7	2 180° +	18	5 5 (2 5		5 16:	7 -17
770 299	871	19			Y <sup>1</sup>	5 ,20		_2 <u>+</u> _ 42 2	7 207° –	18,4	20 (1		2 7 17	3 -21
784				·	A <sub>3</sub>	4 ,24	- ]	31 - -	29	1	20   pared w	23 ith the	) dotern	) duation o

Boss 1220 Member of Ursa Major Cluster? — Boss 1216 Capella Interferometer measurements as compared with the determination of orbit on basis of variable radial velocity lead to m parallax of 0",0632 which probably is the most accurate parallax value so far determined any star

Бþ

						2 <sub>p</sub>							
1	2	3	4	S	6	7	8	9	10	11	12	13	24   15
1301	7 Orionia	19 <sup>m</sup> ,4	- 2° 29′	Bı	24,3 W	3",44	6	80° + 1	Var +19,5	10	(5)	-1,8 -2,7	172 - 19
1788	1235 25 Orionia	19 ,6	+ 1 45	Взр	2",6 W	3 ,64 4 ,73 5 ,04	+ 6 21 -14	209°	+18,9	- 8 8	(2)		169 - 17
1789 1303	y Orlonia	19,8	+ 6 16	B2	11,7 W	1 ,70	20 -11	200°	+18,7	14	(6)		165 -15
1790 1304	919 Tauri	20 ,0	+28 31	B8	14,6	1 .78	180	+ 17	+11	33	(4)	-0.7 -3.1	145 2
1791 1315	795 o Tauri	21 ,6	+21 51	B3	W 1",8	1,98	17	+180	- -15,8	32 7	(4)	-1,3 -1,3	151 - FA
1314	947  P Orlania	21 ,6	+ 3 0	B2	W 2',2	5 ,05 4 ,66	+ 8	+ 15 197°	Var	4	(7)	=1,0	108 , 19
1811	982 # Leporie	24 ,0	-20 50	G <sub>0</sub>	Q. A.	4 ,87	+ 7	+ 12	+12.0 -13.8	<u>5</u>	(3)	$\frac{0,4}{-1,8}$	191 26
1829	1096 31 Orionia	24 .7	- 1 11	K5	Y* 7°,2	4 ,97	-50 28		+ 7.9	11		2,8	172 17
1834 1331	913 A Orionia	25 4	+ 5 52	В3	20,7	4 ,93	+ 3 38		+15	14	(4)	2,2	105 -14
1839	939 T Aurigae	25 ,6	+30 2	Pec	Ver	4 ,50 4,4-14,7			<b>—218</b> ?	0,5	(1)	2,3 -7,1	145 - 1
1841	923a z Aurigae	26 ,2	+32 7	Nova Bi	3*.5	4 ,88	<del>- 2</del>	+ 2 160°	Var	3	(2)	-3,0 -2,7	143 - 0
1843	1024 119 Tanri	26,3	+18 32	Ma	7°,8	5,01	+ 4	17 132°	- 0,2 +22,3	3	(3)	1,0 -2,9	154  - 7
1845	875 ð Orlonia		- 0 22	Bo	19,9	4 ,63	+ 8	10 146°	Var	3	(7)	0,3	171 - 16
1852	983 v Orlonis		- 7 23	<b>B</b> 3	20,1	2,66	+ 1	4 166ª	+19.9 +16.6	5	(4)	-4.5 -1.9	178 - 19
1855 1344	1106 # Columbae		-35 33	Ko	W	4 ,81	<u> </u>	+ 12	Var	5 17	(2)	0,0	208 - 30
1862	2348 & Laporia		-17 54	Fo	30,0	3 ,96	-55 3	- 6	- 3,8 +24,5	17	(4)	2.7	189 24
1865	1166		+ 9 25	Во	Ψ1 2°,5	2 ,87	+ 2	- 2 187°	Var	17	(5)	-4.8 -2.5	163 - 11
1876	877		+ 9 53		₹G 2°,6	4 ,70	- 2 12	+ 8	+33,2 +33	4 7	(5)	-1 n -3,3	162 - 11
1879	879		+ 9 52	Oo 5	W 20	3 ,69	+ 2	+ 12	+35	7	(3)	-1,1 -1,4	162 = 11
1880	879 Octobals	30 .1		Bı	Ŷ# 2°,5	5 ,58	4	140	H29	_		-1,7	177  - 19
1886 1362	1233 Orlonia	30 ,1		Bi	B1		+ 2	- 3 27°	Ľ			-1,4	
1887	1234 c <sup>1</sup> Orlonia	30 ,4		B <sub>3</sub>	2°.3 YG¹	4 ,67 4 ,87	+ 5	_ 5	+28	- W	121	-9.3	177 -19
1892	1185			L 3	2*,8 W	4 ,65 4 ,80	+ 0	153° + 2	+28	5	(3)	-1,9 -3.9	176 - 18
1893 1363	1315	30 A			OR1	6 ,84	+ 7	- 56° - 2	+32	3	(1)	-1,9	176 - 18
1894	1315	lL		Oas	3,8	7 .93		1	Ver 24			-0,8	176 13
1363 1895	#1 Orionia 1315	30 ,4				5 ,36			Var +23			-3,4	
1363 1896	2 <sup>1</sup> Orlonia 1315	<u> </u>	- 5 27			6 ,85			Var +27			L	176 -18
1366 1899	4 Orlonia 194	30 ,	- 5 59	Oa 5	2°,8 W	2 ,87 3 ,09	<b>- 7</b>	124°	+21,3	5		-3,6 -3.6	177 - 18
Box	a 1304. Also mane	d v Aug	tone - Bos	1327 V	Indiahio .	eter — CT O	rionia .	- Boss 13	to Hee		مامحد	- 425 4	L-1 4- 8-

Hom 1304. Also memori y Arrigma. — Hom 1329 Variable star = CJ Orionia. — Bosz 1339. Hen a conspandon 53" diet. 6m,ky — Bosz 1337 Leeding star in an open charter — Rosz 136; 1362. No doubt a physical pair — Bosz 1363. The Texperium A sociétée systems or rather part of an open steller charter. Best value for the parallex second to be 0",0018. Zerrene makes the intel magnitude 4,96 which corresponds to the total magnitude of 5,18 according to Harvard determinations. The total magnitude of the nebula is 2m,9.

 $5^{h}$ .

1	2	3	4	5	6	7	В	9	10	11	12	13	14	15
1370	€ Orionia	311111	- 1° 16′	Bo	1º,6	1 <sup>m</sup> ,75	2	180°	+25,4	9	(5)	-3,7	<u> </u>	<del></del>
1903	969	1			W	2 ,03	- 0	+ 2	1.723,4	8	(3)	-6.7	1/3	13
1373	φ* Orlonis 898	31 ,4	+ 9 15	Kο	6°,0 Ya	4, 39 4,30	321 + 45		+99.3	28 28	(4)		164	-10
1375	& Tauri	31 ,7	+21 5	Взр	10,9	3 ,00	28	+ 318 174°	Var.	10	(4)	$\frac{6.9}{-2.8}$	153	4
1910	908				W	3 24	<u> </u>	+ 28	+16,4	_ 7		0,2		
1922	# Doradus 487	32 ,8	-62 33	F5p	6ª,3	3 ,81 3 ,94	16 + 10	+ 12	- <del>-</del> 7,4			0,2	239	-32
1388 1928	125 Tauri 902	33 ,5	- <b>+25</b> 50	133	1°,5	5 ,00	44	135°	Var.	5	(3)	1.5	149	1
1389	σ Orionia	33 ,7	<b>- 2 3</b> 9	В0	20,7	5 <sub>1</sub> 33 3 <sub>1</sub> 78	+ 28	+ 34	14,8 Var.	$\frac{5}{3}$	(6)	$\frac{3.2}{-3.2}$	175	<del>-16</del>
1931	1326 ω Orionis	22 0	+ 4 4	Dan	W	3 ,97	+ 0	- 1 72°	+28,4 Var.	4		<u>- რ.2</u>	160	
1934	1002			Взр	2°,8 W	4 ,54 4 ,74	+ 6	- 1	- -22,0	5	(3)	-2,0 -1,6	108	-12
1392 1937	d Orionis 1142	34 ,0	- 7 16	A 3	3°,7 Y¹	4 ,88 5 ,04	50 - 26	199° + 42	Var.	17	(2)		178	-18
1396	(26 Tauri	35 ,5	+16 29	В3	20,1	4 ,87	31	155°	- -28:	8	(5)	$\frac{3.4}{-(1.9)}$	158	- 6
1946 1398	841 ζ Orionis	35 ,7	- 2 · i		W	5,09 2,05	+ 10	十 29 131°	- - 19	_ <del>7</del> _5	(7)	$\frac{2,3}{-4,1}$	174	— I 5
1948	1338			Во	1°,6 W	2 ,14	+ 7	4- 9	'	õ	W	-2,9		
1398	C Orionis	35 ,7	- 2 0		YG1	4 ,21			+13			-13 -06	174	15
1399 1952	Orionis 1004	35 ,8	- 1 11	133	1",8 3V	5,00	14 - 13	236°	+26,1	ი ი	(3)	- 1,1	173	15
1401	a Columbae	36,0	-34 8	Bsp	3°.5	2 ,75	35	173	- <del></del> 39	25	(2)	-0.7	206	28
1956 1419	2375 y Leporis	40 ,3	-22 27	G 5	6º,2	6 41	- 32 451	- 15 218°	<u></u> 9,2	24		(),5	195	-23
1982	1210			_	O <sub>0</sub>		365	+275						
1983	y Leporis 1211	40 ,3	-22 29	168	4º,6 ¥º	3 ,80 3 ,90	468 412	216" +220	- 9,2	118	(3)	7.2	195	23
1429 1995	τ Aurigae 1418	42 ,3	+39 9	Ko	5°,0 Y <sup>2</sup>	4 ,64 4 ,64	35 - 26	223°	19,5	14   14	(5)	0,4 -2,4	139	- - 7
1432 1998	ζ Leporis 1232	12 .4	-14 52	Λ2	3°,4 YG¹	3 ,67	17	277°	+13	46	(1)	2,()	187	-20
1434	132 Tauri	12 ,9	+24 32	Кo	0°,0	3 ,84	<u>- 16</u>	- 6	+15,0	46	(3)	0,1 2,1	152	0
2002 1435	970 Orionis		- 9 42	-Bo		5 ,00	±	-l- 36		26		2,8		
2004	1235			טגג	2°,5 W	2 ,20 2 ,44	+ 2	149°	-1-21,7	12	(5)	2,8 3,8	102	-17
1438 2010	134 Tauri 912	43 ,9	+12 37	ВЭ	2º,3 Y1	4 ,92 5 ,11	29 15	207° 十 25	-1-22,0	10	(2)	-0,1 2,2	162	- 6
1439	n Aurigae	44 ,2	+37 16	Ma	60,9	4 ,99	52	137°	+37.9	10	(3)	0,0	141	+ 6
1442	1336	44 ,6	+39 7	Ko	5°,0	4 ,90_ 4 ,18	+ 33	+_40 - 320°	+ 9.9	10	(6)	3,6	139	+ 7
2012	1429			—;; <del> </del>	Ϋ́я	4 ,18	- 5	6		17		-1.3		
1443 2015	8 Dorndus 496	44 ,6	-65 <b>4</b> 6	A5		4 ,52 4 ,62	39 十 38	285" + 7	- 3:			2,5	243	—3i
1446 2020	β Pictoris 1620	44 ,9	-51 6	Λ3	~ -	3 ,94 4 ,07	<del>90</del> 十 6	4° + 90	+28:	58	(ຄ)	2.7 3.7	225	-30
1453	& Aurigae	46 ,5	+55 41	A 2	20,9	4 ,92	14	326°	-12	10	(4)	-0.3	124	+16
2029 1457	1027 136 Tauri	47 ,0	+27 35	Λ0	2°,3	5 ,14	22	12 146°	Var,	9 14	(2)	0,3	149	+ 2
2034	899 3 Leporis			T/ n	$\mathbf{Y}^{1}$	4 .76	+ 11	+ 19	-16,1	14		1.3		
1456 2035	1211	47 ,0	<b>-20</b> 53	Ko	6° Y <sup>3</sup>	3 ,90 3 ,92	696 + 63	160° +696	+99,6	66 55	(7)	2,6 8,1	193	21
1458 2037	56 Orionis 1151	47 ,3	+ 1 50	Ko	6°,2 Y <sup>3</sup>	5 ,01 4 ,99	- 11 - 1	180° + 11	+10,3	6	(1)	-1,0, 0,2	172	-10
		•			_				1	. ~	1	1 1/12	ı	I

Boss 1384. Cephold variable 4m,2 to 5m,6; period 9,8 days. — Boss 1398; H.R. 1948, 1949. A visual binary, 2",5. — Boss 1419, 420. A wide pair 95", 350°.

# 1092 Appendices to Chap 4 K Lundmark Luminosities, Colours, Diameters, etc of the Stars

Бħ.

						5ª.								
1	2	3	4	5	6	7	8	9	10	44	12	13	14	15
1459 2040	β Columbas 2546	47 <sup>m</sup> .4	-35°48	Ko	4",3	3 <sup>m</sup> ,22 3 ,30	397 +131	7° +377	+89,1	29 29	(3)	0,5 6,2	209°	—26°
1460 2043	7 Pictoria 946	48 .0	56 12	Ko		4 ,38 4 ,50	96 - 75	135° 60	+17.0	17 17	(2)	0,5 4,3	231	<del>- 30</del>
1461	z¹ Orlonia	48 ,5	+20 10	F8	5",0	4,62	208 189	243° + 85	14,1	87 89	(5)		156	- 1
1463	1162 Plotons	48 .7	-52 l	Ko	-	4 ,98	90	179°	+ 1,2	- 59			227	29
2049 1467	794 I Columbae	49 .5	-33 50	B5		5 ,08	- 11 28	- 89 2°	+30	14	(1)	4,8 0,6	207	-25
2056 1468	2599		+ 7 3	Ma.	6°,5	0 ,92	+ 15	+ 24 74°	+20,8	14	(5)	2,1	168	- 8
2061	1055				O	1 ,00	+ 28	<b>–</b> 6		12		1,8		
1472	<b>ð Aurigae</b> 970	51 .3	+54 17		5*,5 Y*	3 ,88 3 ,91	153 + 83	145 <sup>8</sup> +129	+ 7.7	25 23	(4)	0,7 4,8	127	+16
1475 2084	139 Tauri 1052	51 ,8	+25 5	B2	2°,8 ¥1	4 ,90 5 ,07	- 4	194° + 3	+ 8,5	3	(5)	-2.7	152	+ 3
1476 2085	9 Laports 1286	51 ,9	-14 1	Fo	4",0 Y1	3 ,77 3 ,90	138 - 29	343° -135	- 1,6	49 48	(3)	2,2 4,5	187	-17
1478	β Aurigao 1328	52 ,2	+44 50	Aop	1*,9 W	2 ,07 2 ,26	47 - 47	264° + 4	-18,7	41 38	(6)		135	+12
1479	# Aurigae	52 ,5	+45 50	Ma.	7,1	4 .59	11	1350	+ 0,9	6	(3)	-1.5	134	-12
1482	4217 4 Aurigne	52 .9	+37 12	AOp	1,9	4 ,47	105	+ 8 149°	+29	6 34	(6)		142	+ 8
2095 1486	1380 Doradus	53 .4	-63	3 Ko	_w_	2 ,90 4 ,53	+ 52 562	+ 91 14°	+24,7	32 21	(1)	2,8	239	-30
1490	498 7 Columbae		-35 4	B B3		4 ,64	-118	+551 297°	+24.2	7	(1)	8,3	208	<u></u>
2106	2612 Orionia				<b>20.</b> 6	4 ,51	+ 4	+ 1 169°	1	27	(2)	-2,6		=11
1494 2113	1256	55 ,1			5°,5	4 ,67	+ 13	+ 83	+25.9	28		4,3	L.	
1497 2120	# Calumbas 2266	56 ,1	-42 4	Ko	l	4 ,03 4 ,08	33 - 23	140° — 23	十17.9	13 13	(2)	1,6		-26
1501 2124	μ Orionis 1064	56 ,9	+ 9 3	A2	3°,6	4 ,19 4 ,37	34 + 18	148° + 29	+42	33 32	(3)	1,7	166	- 5
1503 2128	3 Monocerotis 1349	57 .1	-10 3	8 118	2º,1 W	4 ,97	+ 1	_ 2°	<b>Var</b> +39	6	(2)	-1,1 -1,0	185	-15
1508	1 Geminorum	58 ,0	+23 1	5 G5	5°,4	4 ,30 4 ,35	108	184° +108	Var +20	32 31	(5)		155	+ 2
2134 1507	2 <sup>8</sup> Orlouis	58 ,0	+20	B B2p	44,3	4 .71	15	148*	Var	6	(3)	-1,4	157	0
1522	1233 Deports	1 ,6	-14 5	6 A0	20,6	4 ,86	+ 8	+ 13 343°	+32°	19	(1)	0,6	189	-15
2155 1525	1331 # Orlon#	1.6	+14 4	7 B2	2°,5	4 ,84	<del>~ 8</del>	- 23 166°	Var.	19	(3)	1,6	163	- 1
2159 1550	1152 f <sup>1</sup> Orionia			9 B3	W 2º.4	4 ,60	+ 10	+ 36	+22,1	7 8	(2)	2,2		-
2198	1035		ļ		W	5 ,15	+ 7	+ 23	+28	8	] ` `	1,8	1	
1548 2199	1187	1	3 + 14 1		26,5 W	4 ,56	+ 10	165° + 34	+24,1	9	(3)	2,1		1 1
1556 2209	Camelopardalb 371	7 ,	+69 2	1 Ao	2°,5 Y¹	4 ,73 4 ,94	+ 15	+108		13 13	(1)	0,3 4,9	113	+23
1558 2212	d Pictoria 980	8,4	-54 5	6 B <sub>1</sub>		4 ,84 4 ,94	24 + 23		Var.			1,7	230	-27
1561 2216	g Geminorum 1241	8 ,	+22 3	2 Ma	6,9	Var 3,3-4.	65	255°	+19,4	13			156	+ 4
1565	M Aurigne	9 ,1	+29 3	3 Ko	5*.5	4 ,45	274	194°	+20,5	18	(5)	0,7	150	+ 7
2219	1154   1468   Dataleanes	Variat	Her on on		Y	4,47		+269	 	18 	•	6,6	•	 

Boss 1466. Betsigroum. Variables: 0m,00—0m,80. The variations in the light seem to be corollated with the variations in the discovery as derived on bosis of interferometer measurements. On basis of that assumption a paintiles parallel of 0",007 has been derived. — Boss 1478, Mescher of Urse Major Cluster. Religating binary — Boss 1561. Long pariod variable. Period 231,4 days.

6h.

						0							1	
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1570 2227	y Monocerotis 1469	10 <sup>to</sup> ,0	— 6°11′	Кo	6°,5 Y <sup>8</sup>	4 <sup>ta</sup> ,09 4 ,14	21 _ 2	+ 21		16 16	(2)	0,7	182°	
1575	2 J yncia 959	8, 01	+59 3	A0	2°,1	4 ,42 4 ,63	- 22 6	- 21	4	24	(4)	1,3	`	- <del> -20</del>
1580 2244	Canıs maj 1411	Īi ,i	$-13 \ 41$	B9	2 <sup>1</sup> , 1 W	4 ,99 5 15	7  - 7	- 0	∓33			-0,7	189	-13
1579 2245	η <sup>2</sup> Doradus 561	11 ,1	65 34	Mb		4 ,88 1 ,99	112 + 18	1111	- 34,5	6	(a)	5, 1 5, 1	243	-28
1587	zenumbac zenu	13.,0	-35 6	Ko	_	4 ,51 4 ,53	76 - 36	1 66	1-24,5	13 13	(2)	5,1	210	-21
1601 2282	ζ Canıq maj 3038	16 ,5	- 30 1	B3	3°,0 W_	3 ,10 3 ,30		- 8	34	6 6	(1)	-2,4	205	18
1601 2286	μ Gommorum 1304	16 ,9	+22 34	Ma	7.3 0.0	3 ,19 3 ,13	128	<b> -106</b>	54.4	16 16	(5)	3.7	157	+ 0
1609 2294	β Canis maj 1467		-17 51	31	2°,1 W	1,99 2,21	= 7	+ 2	Vai  +34,  -	10 10	(5)	-3,0 -3,6_	193	-13
1610 <b>229</b> 6	8 Columbae 2927		-33 23	(+5		3 ,98 4 ,05	+ 6	- 6	- 2,4	22 22	(1)	0,7 8,1	208	- 19
1611 2298	8 Monocerotis 1 1236	18",5	+ 4 39	Λ.5	4°,0 Y1	4 ,48 4 54	- I	256°	10,6	19 19	(2)	0,9 -0,1	173	- 3
1611 2299	8 Monocerotis 1236		+ 4 39		Ÿ1	6 ,54	Į		+15.8				173	- 3
2308	BL Orionia (283	ļ.	+14 17	N 6		4,7-6,6	1	8 —			.5."		164	- 3
1622 2326	& Catmao 914	]	-52 38	]		-0 ,86 -0 ,67	1	7 + 6	+ 20.7	14	(2)	- 5, 1 - 2,8	229	-25
1629 2332	RI Aurigae 1238	}	+30 33			Vai 5,24-5,97		1 + 21	`	3	(1)		150	+10
1635 2343	p Gommorum 1441		+20 17	_	2°,9 W	4 ,06 4 ,32	. !	6 F 21		10	(3)	- 0,9	160	+ 6
1634 2344	10 Monoccrotis 1526	l	4 42		2°,3 W	4 ,98 5 ,18		5 - 13	F21	5	(2)	- 1,5 0,7	183	- 6
1639 2356	111 Monocerotis		6 58		3°,0	4 ,73		6 F 8	-	12 12	(2)	2.5	184	7
1640 2357	1 12 Monocerolis 1 574	Ί		Day	M A1	5 ,22	- 3	7 273° 6 + 6	1		_	3,0	184	- 7
1640 2358	112 Monocorotis	24 ,0	- 6 58	_\ _	W	5 ,60			F-23			1,0 3,4	184	
1641 2361	2 Canta maj 3066	1	-32 31			4 ,48 4 ,64		8 + 31		13	' '	0,1 2,0	209	i
1657 2385	13 Monocciolis 1337	27 ,	5 -F 7 24	_	3°,1	4 ,50 4 ,70		0 163° 4 + 9	1	] 13	\	0,1	172	+ 1
1660 2387	3991		0 -23 2		3 Y1	4 ,35	1	8 83°	- 26,7			- 1,8 - 1,2	199	-13
1682 2414	La Canis maj 1458		-22 5	1	2 Y1	4 ,54 4 ,70		4 25°		25 25	}	0,2	200	
1690 2421	γ Geininotum 1223	1	+16 2		1°,9 W	2 ,25	_]_15	5 136° 2  - 39	1	54		1,0		+ 0
1695 <b>2</b> 429	r <sup>2</sup> Canis maj 1502	}	3 - 19 10	I	5°,4 Y <sup>8</sup>	4 ,14 4 ,16	_ + º	07 136° 04   23		5 59	(a)	3,0	_	
1696 2435	N Carmae 953	Ť	8 52 5:			4 ,44 4 ,55	+- !	7 237°	]		-	0,5	229	_\
1698 2443	r <sup>3</sup> Canıs maj 1492		1	) Ko	5°,1	63, 4		6 243° 9 + 13	1,!	1		0,6	<b>-</b> l	
	Pictoris	34	2 -62 3			1,0-12,7	+ 4	15 245 14 — 10			3 (1)	-0.7	_	
1703 2450	1525	34	1	3   Ko	6°,5		1+	11 175 6+ 10	)	1		0,2	•	
-	Ross 1611 Probably h	Juan	. Bose 1640	Han been	a Include	ed hecouse	its max	lmum mae	nltude me	av falli	yory	close to	the lir	nit 5.0 -

Boss 1611 Probably binary — Boss 1629 Has been included because its maximum magnitude may fall very close to the limit 5,0 — Boss 1639—40 A triple system, the total magnitude of which is 3m,91 in the Harvard system and 1m,14 in Linnar's system

2456 1711 2462 1716 2470  2472 1717 2473 1721 2478 1725 2491 1737 2503 1740 1556 1758 1761 2538 1763 2540 1769 2550 1773 2553 1773 2554	* Puppls 2576 S Monocerotis 1890 Puppls 2417 12 Lyncis 1015 Gominorum 1406 to Gerninorum 1390 F Geminorum 1396 # Canis maj 1591 17 Monocerotis 1496 18 Monocerotis 1397	36 .0 37 .4 37 .8 37 .8 38 .1 39 .7	+ 9 59 -48 8 +59 33 +30 2 +25 14 +33 20	B8 Oe5 K0 A2 Pec Nova G5	2°.5 (,1 2°.5 W	6 <sup>h</sup> .  7  3 <sup>m</sup> ,18 3 ,39 4 ,68 4 ,87 5 ,00 5 ,10 4 ,89 5 ,05	8 + 10 7 14 + 7 15	- 17 138° + 6	10 +28 +28,8 +27.7	25 25 6 4	(1)	-0,3	14 219°	-1 +
2451 1706 2456 1711 2462 1716 2470 2470 2472 1717 2473 1721 2473 1723 2484 1732 2484 1732 2491 1737 2503 1740 2506 1758 2527 1761 2538 1763 2540 1763 2540 1773 2553 1773 2553	2576 S Monocerotis 1890 Puppls 2417 12 Lyncis 1015 Geminorum 1406 O Geminorum 1390 F Geminorum 1390 F Canis maj 1591 17 Monocerotis 1496	35 .5 36 .0 37 .4 37 .8 37 .8 38 .1	+ 9 59 -48 8 +59 33 +30 2 +25 14 +33 20	B8 Oe5 K0 A2 Pec Nova	2°.5 W	3",18 3 ,39 4 ,68 4 ,87 5 ,00 5 ,10 4 ,89	20 + 10 9 + 7 14 + 7	177° - 17 138° + 6 304°	+28 +28,8	25 25	(1)	0,2 -0,3 -2,3	219°	-1
1706 S 2456 1711 2462 1716 2470 2472 1717 2473 1721 2478 1725 2484 1732 2491 1737 2503 1740 2508 1758 1758 1758 1761 2538 1763 2540 1763 2540 1773 2553 1773 2554	Monocerotia 1890 Puppla 2417 12 Lyncia 1015 Gominorum 1406 10 Geminorum 1390 F Geminorum 1390 or Cania maj 1591 17 Monocerotia 1496	36 .0 37 .4 37 .8 37 .8 38 .1 39 .7	-48 8 +59 33 +30 2 +25 14 +33 20	Ko A2 Pec Nova	2°.5 W	4 ,68 4 ,87 5 ,00 5 ,10 4 ,89	+ 7 + 7 + 7	+ 6 304°			(5)	-2,3	<u></u>	+
1711 2462 1716 2470 2472 1717 2473 1721 2478 1725 2484 1732 2491 1732 2506 1758 2506 1758 2527 1761 2538 1763 2540 1763 2540 1763 2540 1763 2550 1763 2550 1763 2550 1763 2550 1763 2550 1773 2553	Puppls 2417 12 Lyncis 1015 Gominorum 406 Gorninorum 1390 F Geminorum 1396 & Canis maj 1591 17 Monocerotis 1496	37 ,4 37 ,8 37 ,8 38 ,1 39 ,7	+59 33 +30 2 +25 14 +33 20	Poc Nova	2°.5 W	5 ,00 5 ,10 4 ,89	+ 7 + 7	304°	+27.7	4		-0,8	224	
1716 2470 2472 1717 2473 1721 3478 1725 2484 1732 2491 1737 2503 1740 2506 1758 2527 1761 2538 1763 2540 1769 2550 1773 2553 1773 2553	12 Lyncis 1015 Gominorum 1406 Gominorum 1390 F Geminorum 1396 # Canis maj 1591 17 Manacerotis 1496	37 ,8 37 ,8 38 ,1 39 ,7	+30 2 +25 14 +33 20	Poc Nova	W	4 ,89	15	T 14				۱	224	-2
2472 1717 2473 1721 2473 1721 2484 1725 2484 1732 2491 1737 2503 1740 2503 1758 2527 1761 2538 1763 2540 1763 2540 1763 2540 1763 2550 1773 2553 1773 2554	s Geminorum 1406 to Geminorum 1390 £ Geminorum 1396 st Canis maj 1591 17 Monocerotis 1496	37 ,8 38 ,1 39 ,7	+25 14	Nova		3 103	- 15	274°	+ 7	24 24	(2)		123	+:
2473 1721 2478 1725 2484 1732 2491 1737 2503 1740 2506 1758 2527 2528 1761 2538 1763 2540 1769 2550 1773 2553 1773 2554	1406 10 Geralnerum 1390 E Geralnerum 1396 or Canis maj 1591 17 Monocerotis 1496 18 Monocerotis	38 ,1 39 ,7	+33 20	GS		5,0-16,3	7	240°		-		-0,8	153	+ 1
2478 1725 2484 1732 2491 1737 2503 1740 1558 2527 1761 2538 1763 2540 1763 2540 1763 2550 1772 2553 1773 2554	1390 F Geminorum 1396 A Canis maj 1591 17 Monocerotis 1496 18 Monocerotis	39 ,7			5°,9 Y8	3,18	+ 30 + 3		+ 9,6	10 10	(4)		157	+-1
2484 1732 2491 1737 2503 1740 12506 1758 2527 1761 2538 1763 2540 1769 2550 1779 2553 1773 2554	#396 # Canis maj 1591 17 Monocerotis 1496 18 Monocerotis			Ko	6°, 1 Y <sup>0</sup>	4 .65	76 + 18	178	+13,0	19	(1)		168	+
2491 1737 2503 1740 2506 1758 2527 1761 2538 1763 2540 1769 2550 1772 2553 1773 2554	1591 17 Monocerotis 1496 18 Monocerotis			F 5	3°,9	3 ,40 3 ,57	231 - 72	210°	+ 24		(5)		168	+
2503 1740 2506 1758 2527 1761 2538 1763 2540 1769 2550 1772 2553 1773 2554	1496 18 Monocerotta	1	-16 35	An	0°,7	-1,58 -1,30	1316 + 184	204° +1303	- 7.5		(7)		195	-
2506 1758 2527 1761 2538 1763 2540 1769 2550 1772 2553 1773 2554	130%			Ro		5,00	- 15		+47	12	(B)		173	+
2527 1761 2538 1763 2540 1769 2550 1772 2553 1773 2554	Camelopard			Κo	Va.s	4 .70 4 .65	26 + 2	+ 26		15 15	(4)	1,8		+
2538 1763 6 2540 1769 2550 1772 2553 1773 2554	266 M Carls maj	45 ,5	+77 6 -32 23	K5	6º,4 OYº	4 ,75	+ 85 + 85	0	-29,4	15 15	(2)	0,6 4,4	"	+:
2540 1769 2550 1772 2553 1773 2554	3404 7 Geminorum	46 ,2		Bap Aa	20 4	3 .78	10			7 7	(1)	-2,0 -1,2		·
2550 1772 2553 1773 2554	1481 « Pictoris		-61 50	A5	2°,5 W	3 ,64 3 ,83	54 + 16		Var	24 24	(3)	0,5 2,3		+
2553 1773 2554	720 r Puppie		-50 30	Ko	7",U	3 ,30 3 ,44 2 ,83	272 - 14 90	343° + 272 164°		24	721	5,5	239	- 2
	2415 A Carinas		-53 31	Gs		3 ,04	+ 22	<b>– 8</b> 7	+36.0	31 31 15	(3)	0,3 2,6		12
	1168		+32 16	Pec	Var	4 .50 3.7—14.5	- 13 21	+ 21 225°		15	(1)	0,3	150	
1776	15 Lynch		+58 33	Nova Go	5°,4	4 ,54	- 12 134	十 18	+ 8.6	15	(5)	0,3		+2
	982 a Gominorum			Fo	40,0	4 .58	+ 29 112	+ 130 139		14	(6)	5,2		+
2564 1781 1	1462 15 Canis maj	49 ,2	<b>-20</b> 6	Bt	3ª	4 ,81	+ 93 8	+ 63	+30	38 5	(2)	4,9 -1,9		_
2571 1783 2574	1616 6 Canta maj 1681	49 .5	-11 55	K2	6°,6	4 .73	- 3 138	8 264	+96,5	5 21	(3)	0,8 0,9		=-
1785 d 2580	o <sup>1</sup> Cania maj 4567	49 ,9	-24 4	K2p	6'.7	4 ,12	<u>– 112</u>	+ 81 306°	+36,8	21	(B)	5.0 -3.9	202	_
	ψ <sup>10</sup> Aurigae 1367	50 ,4	+45 14	A2	2',4 W	4 ,11	- 13 25	265°	-22 :	22	(1)		139	+2
		51 ,3	<b>-2</b> 0 1	F5	Ā.m. 4₀	5 ,07 4 ,62	- 24 67	57	+ 8.	22	_		199	_
	Canbo maj	51 ,7	-16 55	B5	2°,8	4 ,71 4 ,39 4 ,58	+ 14 - 11 - 7	- 66 355° - 8	+40,6	7	(1)	3,8 -1,4	196	=
1800 2608	Puppis 2601	53 ,6	-48 35	Ma		4 ,88 4 ,99	- / 9 + 4	297°	+22,1	7		-0,4 -0,3	226	-1
2618	a Cania maj 3666	54 .7	-28 50	B1	2°,3 G1	1 ,63	+ 1		+28,3	8	(3)	-0,3 -3,9 -8,4	208	-1
2646	3544	- 1	-27 47	K5	7º ORª	3 ,68 3 .73	11		+21,8		(2)	-6,4 -1,3 -1,1	207	<u>-</u> 1
1812 19 2648		57 ,9	- 4 6	B3	2",3 W	4 ,89 5 ,11	- 4	353	+23	5	(2)	-1,1 -1,6 -0,6	185	+

6h to 7h.

					6	$^{n}$ to $7^{n}$ .								
1	2	3	1	5	6	7	8	9	10	11	12	13	11	15
1815 2650	ζ Gemmorum 1687	58 <sup>ta</sup> ,2	20°43′	Gop	4°,6 ¥2	3 <sup>m</sup> ,6 -4 <sup>m</sup> ,5 3 ,7-1 ,3	15 O	196° 15	+ 6,7	4 3	(2)		163°	+13°
1817 2653	o² Canis maj 4797	58 8	-23 11	B5p	3° Y(r1	3,12	9 + 1	229°	<del>-</del> -48,4	6	(2)	-9,0 $-2,1$	204	- 7
1819 2657	γ Canis maj 1625	59 ,2	$-15\bar{5}29$	135	2°,8 W	4 ,07	14	184°	+276	8	(2)	$-\frac{1}{1.4}$	196	3
1839 2693	δ Canis maj 3916	4,3	26 14	1.8p	5° -	1 98	5	292°	+31,5	10 10	(2)	-3,0 -4,5	206	- 7
1841 2696	63 Aurigat 1882	4.8	39 29	J. 2	()g ()g	5 .07	48 47	94°	-27,0	15 15	¯(ī)¯		J46	22
1840 2697	r Gemmorum 1439	4 ,8	F30 25	Īζο	_6' 3 Ƴ¹	4 ,48 4 ,50	53	208° + 52	+22,1	18 18	(3)	1-0,8 3,1	155	+18
1844 2701	20 Monocerotis 1840	_5 ,2	- 4 5	K()	5°,0 ¥3	5 ,02 4 ,96	217 102	-191	+785		_	5.7	186	3
1845 2702	A Puppis 3105	5 ,5	39 29	13 3		4 ,85 5 ,01	13 - 3	283°  +13	19,5	22 22	(1)	1,6	218	13
1853 2714	8 Monocerotis 1636	6 8	- 0 20	Ao	-3° () W	+ ,09 4 ,25	- 1i	15°	14	19 19	(2)	-0.7	184	4- 6
1866 - 2735	y <sup>1</sup> Volantis ) 600	9,6	-70 20	(+()		5 ,81 5 ,98	90 30	15°	Vai - 3			3,3 5,8	248	-24
1867 2736	y <sup>2</sup> Volantis 600	96	,	ำไร้เก		3 .87 4 .01	97 - 61	15°  - 76	-1 2,7	3 I 3 I	(2)	+1.3 3.8	248	-24
1869 27 10	I Puppis 2977	7 7	46 35	b o		4 ,47 4 ,62	172	302° -  169	- 14		]	5.7	225	16
1872 2715	27 Canis maj 4057	10 ,2	26 10	13 5 p	2' \\V\	4 ,66 4 ,82	- 8	311'  1	V.u - -25	8 8	(1)	-0,9 -0,5	206	- <u>6</u> °
1875 2748	1 <sup>3</sup> Puppis 3227	10 ,5		Md		Vai 3, 3 - 5,2	332 159	18°	-1 5 3,0			5,9		- 14
1877 2710	ω Canis maj 4073	10 .7	26 35	13 3 p	3" VV	3 ,83 4 ,01	+ 6	207°	-1 29	5 5	(1)	1,4	208	ō -
1870 2751	1612	10 19	149 38	A2	I <sup>d</sup> ,8	4 ,80 5 ,09	- 3	212°	- 8	11	(1)	-0,0 -0,4	135	-  26
1884 2762	Puppis 2807		45 0	138		4 ,88 4 ,98	- 16 16	38°	-  -  -  -			(1,9	227	- 15
1886 2763	7 (remmorum 1443	12 ,3		ΛŽ	3°,0 Y(x1	3 ,65 18, 3	68 - 29	225°	Vai 13,8		(4)	2,8	168	-15
1888 2764	Canis maj 5189	12 4		K 5		4 ,82	61 59	314	1 27.9	4	(a)	-2,2 3.8		- 4  - 6
1889 2766	Cama maj 3852	12 (6		Mb	7" () 1	1 .77 4 .76	45 44	3336	-1 10,6	10	(1)	3,0	208	
1896 2773	# Puppis	13 ,6		10.5	60,3	2 ,74 2 ,85	<u>4</u>	256°	+15,5	17	(2)	-15 -2,8	)	11
1898 2777	8 Gemmorum 1615	14 ,2	}	10	3° 7	3,51	25  -  1	227	Va1 2	49	(5)	0,5	164	-18
1899 2781	29 Canis maj 5173	14 .5		Oa	Y. 3	4 ,90	12	233° 9	12,1 Vai	5	(2)	- 1,6 0,3		5
190 I 2782	* Canis maj 5176	14 ,5			30 Y1	4 ,40	- 6	330°	-1-40,4		(1)	-1,1	206	5
1907 2787	** 1 Puppis _ 3512		-36 33	133		4 ,68 4 ,83 - 4 ,83	15 1 15	208°	+19	11	(1)	- 0,1 _ 0,6		
1917 2803	δ Voluntis 730	!	-67 46	I 5		4 ,02	+ 21 + 21	253° + 4	+22,6		(2)	0,6 - 0,9		-23
1924 2812	Canis maj 1806		-18 50	138 -A0	700.6	5 ,07	8 1	210° + 8	+25.9	7 7 18	(2)	O, G		+27
1928 2818	21 Lyncis 1623	19 ,2	F49 25	A.O	2°,6	4,45	+ 8	187°  - 48	-1-45.9	18		2,9		T41

Boss 1815 Cepheld variable 3m,7 to 4m,3, period 10,2 days. This star has often been considered as prototype for a certain class of Cephelds but there seems to be few if any reasons nowadays to divide the Cephelds according to the shape of their light curve. — Boss 1839. A complex system

76

						7h.								
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1931 2821	i Geminorum 1385	197,5	+28° 0′	Ko	7°.3	3 <b>-</b> ,89 3 ,93	- 14 <u>!</u> - 77		+ 8,0	23 23	(3)	0,7 4,7	158°	+21°
1934 2827	n Canis maj 4328	20 ,1	-29 6	B5p	4° Y1	2 ,43 2 ,65	10		+39	7 7	(1)	-3.3 -2,6	210	<b>–</b> 5
1944 2845	β Canle min 1774	21 ,7	+ 8 29	BB	7°,2 W	3 ,09 3 ,25	— 60 — 20	229	Vаг +23	24 24	(4)		178	+13
1952 2852	g Geminorum 1562	22 ,7	+31 59	Fo	3°,7	4 ,18 4 ,36	230 + 70	39	- 4	40 39	(6)	2,1 6,0	155	+23
1953 2854	y Canie min 1660	22, ,8	+ 9 8	Ko	Oa Oa	4 ,60 4 ,44	6		Var +47	12	(2)	-0,2 3,7	177	+14
1962 2864	6 Canis min 1567	24 ,2	+12 13	Ko	6",2 Y*	4 ,85 4 ,79	+ 1	171	-15,4	13	(4)	0,4	174	+15
1968 2874	Pupple 1897	25 ,6	-22 49	A3		4 ,80 4 ,96	1		+36,9	28 28	(1)	2,0	205	<b>– 2</b>
1972	o Puppia 3260	26 ,1	<b>-43</b> 6	K5		3 ,27 3 ,38	19	1 341 0+ 139	+87.3	23 22	(3)	0,0	223	-11
1973	Puppla 4620	26 ,9	-30 45	Go		4 .77 4 .87	_ 3		+14,4				213	- 5
2890	g Gaminorum 1581	ļ.	+32 6		й_	2 ,85 3 ,08	20 - 12	3 237 0+ 164	- 1,2	79 78	(3)		155	+24
2890	or Geminorum 1581	28 ,2	+32 6	A0	1°,9 W	1 ,99 1 ,81	- 12		+ 6,0		(3)		155	+24
1987 2905	v Geminorum 1424		+27 7	K5	6°,5	4 ,22 4 ,19	- 11		-20,9	16 14	(5)	-0,1 4,6	160	+22
1988 2906	Puppls 9007	29 ,8	-22 5	I'8		4 ,52 4 ,61	8		4-60,9			4,1	205	土 0
1994 2922	p Puppla 4566	31 ,4	<b>-28</b> 9	B8	AG1	4 ,55 4 ,71	7		+13 :			3,9	211	- 2
2001 2930	o Gominorum 1649	32 ,6	+34 49	To	3°,4 Y1	4 ,92 5 ,08	12		4 8	20 20	(5)	1,4	152	+26
2003 2934	Q Carinas †231	33 ,2		K5		4 ,92 5 ,03			+61,1			1,9	232	-14
2004 2937	1 Puppls 3755	33 ,6	34 44	B8		4 ,62	3		4-24	13	(2)	0,2	217	- 6
2008 2943	a Canis min 1739	34 ,1	+ 5 29	F5	20,7 Y1	0 ,48 0 ,64	124		4- 3	317 320	(5)		182	+14
2009 2944	m Puppls 4828	34 ,1	}	Bs	4°-5°	4 ,64 4 ,80	+	6 240 3+ 10	441	6	(1)		208	- 1
2010 2946	24 Lynds 1108	34 ,9	+58 57	A2	2°,7 W	4 .96		6 + 6	+ 5:	16	(2)		125	ا 30
2011 2948	* Puppls 4707	34 ,7	-26 34	Bs	~	4 ,50			+23.6		(2)		210	- 1
2012 2949	Pupple 4707	34 ,2		B3	Ţ.	4 ,62 4 ,83	;		+33	12	(2)		210	- 1
2017 2961	d¹ Puppis 3531		-38 4			4 ,91 5 ,08	1 :	23 25 11 + 2	+26	22	(1)		220	- 7
2021 2970	α Monocerotis 2172	36 7.	5 → 9 19	Ko	6°,2 Y8	4 ,07 4 ,10			14-11.3	+	(2)		195	+ 8
2023 2973	d Geminorum 1590	1	+29 7	Ko	6°,1	4 ,26 4 ,32	2	47 16 56+ 19	Var	33	(4)		159	+24
2029 2985	w Geminorum 1759	38 ,	+24 38	G 5	4".7 Y	3 ,68 3 ,74		66 20 6+ 6	5° +20,4	-	(7)		163	+23
2031 2990	# Geminorum 1463	39 ,	2 +28 16	Ko	4°,4 X3	1 ,21	6		4 + 3,0		(5)		160	+25
2032	1 Puppls 4767	39 ,	5-28 10	K5	OR*	4 ,10 4 ,16		14 33	0°+31,7			0,	212	- 1
	1000 Consular a			- Toods	· •	- 7k- k	-							

1979. Complex system consisting of at least the members. The bright stars at and at are spectroscopic binaries of periods 2,9 "spectively Caster C is a star of 9m at 7.2" distance which shares the p. m. of the bright stars and which list is a spectroscopic Purthermone a seventh member of the system close to H.R. 2890 has been suspected from perturbations in the visual orbit. — Binary 40", 348°

7h to 8h.

			<del></del>		7" ((							,		
1	2	3	1	. 5	6	7	8	9	10	11	12	13	11	15
2035 2996	4774		28° 43′	A2p	4 <sup>c</sup> Y <sup>1</sup>	1 <sup>m</sup> ,10 4 ,26	10 + 9	+ 5	4-23,6			- 0,9	2120	
2040 3003	g Gemmorum 1733	40 ,3	+18 45	K2	6°,5 O²	5 ,02 4 ,99	97 - 30	225° + 92	Vu +80,4	11 11	(1)	0,2 5 0	169	22
3016	Puppis ]	41 .5	37 39	В3		6 ,45			+21,ō		_	-	220	6
2052 3017	c Puppis []	41 ,7	- 37 44	К. 5		3 ,72 3 ,80	26   12	252°	18,3	-		0,8	220	- 6
2056 3024	ζ Volantis 627	43 ,0	-72 22	Ko	-	3 .89 4 .04	_ 9 _ 8	1	-1-48.7	32 32	(2)	1,4 1 3	251	-22
206 î 3034	o Puppis	43 .9	25 42	B2	7 (* 1 20	1 .59 4 .78	+ 3	240°	only $\mathcal L$ lines	6	(i)	- 1,5 5,1	210	1
2065 3045	ξ Γ <sup>0</sup> υρρις 6030	45 ,1	-24 37	Gop	6°,7 Y3	3 ,47 3 ,57	7		1- 3.9	3	(2)	4, î 2,2		1- 1
2067 3046	Q Puppis 3451	45,3	-46 50	Ко		4 ,64 4 ,80	128  - 122		0,5	20 20	(1)	1,1 5,2	228	-10
2070 3055	P Puppis 3458_	46 ,2	1	Во		4 ,25 4 ,30	11 - 13	231° 1+ 6	-24,0	8 8	(ī)	- 1,2 0,0		-10
2078 3067	η Gemmorum 1499	47 ,4	+27 Î	Λ2	2°,5 Y1	4 ,99 5 ,21	47 10	H 46	Vat - - 3	17 17	(2)	3,3	162	26
2087 3080	a Puppis 3579	48 ,8		G 5		3 ,76 3 ,86	+_ 13	16	1-24.5	21 21	(1)	0,3		- 6
2089 3084	b Puppis 3769		-38 36	B3		4 ,53 4 ,62	+ 15	5-1- 5		9	(1)	0,5	The second second	
2094 3089	Puppis 3137	50 ,2		133		4 ,83 4 ,92		2- - 15	<u> </u>	14	(1)	0,6		11
2095 3090	3396 3396	50 ,3		Bi		4 ,32 4 ,43	+ 13 + 13	7 - 7			4.5	0,6	1	-10
2099 3102	o or 1 Pupper 2087	52.,(		1.8	78 V8	4 ,35 4 ,45	- 4·	9 - 12	Ľ	28	(1)	2,4		-1 4
2108 3113	Puppis 5286	53 1		Λ2	3º Y1	4 ,85 5 ,01		0 - 9	1		(a)	1,7 0,5		+ 1
2111 3117	χ Carmae	54 ,2		133	-	3,60		5 4- 38		30		1,5		-12
2119 3129	V Puppis 3349	55 ,1		Bip		4 ,50	+ 20	0  - 22		21	(1)	1,1	) -	- 10 7
2120 3131	13upp14 2118	55 ,4		A2	2°,8 Y1	4 ,04 4 ,83		4 + 31		17	(ī) -//	2,9		
2126 3141	28 Monocorotis 1882	"		021	00,1 OYa	4 ,88 4 ,84		4 25	,	14	1	4,8	mi i	
2130 3145	13 Canis min 1854	57	'	Ko B3	6°,3	4 ,52 4 ,55	- 9	2 - 53		19	''	4,0	)   186 5 1   244	
2136 3159	1) Carmae 866	59 ,		Od	20 0	4 ,96 5 ,04	2	14 20	9- 20 9- 20	12	1 ` '	_ h,		
2141 3165	ζ Риррия 3939	l	1 - 39 43		3°,0 2°,7	2 ,27 2 ,53		5 + 32		27		-0,3		
2145 3173	27 Lyncis 1391 g Puppis	Ì	9 +51 48	F5	- NV S <sup>a</sup>	4 ,87 5 ,05 2 ,88	4 10	6   31		1 7		3,0		
2153 3185 2154	6828 Velorum	1	3 -24 1 5 -44 58	K <sub>0</sub>	Ā,	2,97 5,02	7	4 + 67		10		2		
3187 2155	4051 \$ Monoceretis	1	5 -44 50 6 - 2 41	GO	50,7	4 ,99		4 + 4 5 253			(3)	0,		
3188 2158	2450 16 Puppis	1	5 - 18 57	-B3	Y3 20	4 .51	_ 1	3 + 32			(2)	_   _1,	4 207	
3192		1 "	3 - 10 3/	"3	w	4 ,50		0 + 10			, l \"	0,		'

Boss 2119 Eclipsing binary Relative velocity is 610 km/sec Varies from 4m,1 to 1m,8 in 1,5 days

1098 Appendices to Chap 4 K Lumbhark Luminosities, Colours, Diameters, etc of the Sturs

8ª.

						0-,	_							
1	2	3	4	5	6	7		9	10	11	12	13	14	15
2166 3206	y¹ Valorum ) 8846	6 4	-47° 3′	B3	: 	4 <b></b> 79 5 .03	17 + 17	205° + 1	Var			0.7 1.0	230°	– 7°
2167 3207	7 Velorum 3847	6 ,5	<b>-47</b> 3	Овр	34.5	2 ,22 2 ,09	2	180° 2	+35	15 15	(2)	-1,9	230	- 7 L
2168 2169	Cancri Cancri	6 .5	+17 57	Go	4°,9 3°,0	5 ,56 6 ,26	155	155°	-10,6 - 5,6	44	(1)	2,9	173	+26
3208 to 3210	1867				AC <sub>1</sub>	6,02	+132	+ 82		44		5.7		
2170 3211	19 Pupple 2385		-12 37	Ko	5".4 Y"	4 ,68 4 ,66		294° + 13	十36,3	36	(a)	1,9	202	+12
2177 3220	B Caringe 1074	7 ,3	-60 <b>59</b>	F5		4 ,80 4 ,91	326 +319	208° 68	+25,0	53	(a)	3.4 7.4	242	15
2179 3223	Voluntia 736	7 ,6	<b>68</b> 19	B5		4 .46	28 - 3	321 a + 28	+ 9,6			1.7	245)	-18
2180 3225	h <sup>1</sup> Рпррія 4084	7 ,8	-39 19	K5		4 ,43 4 ,46	20 + 20	180° - 2	Var +15,9			0,9	224	- 2
2181 3226	Pupple 3979	8 ,0	-42 41	A3	_	4 ,87 5 ,02	+ 5	191° - 0	+19,2	2	(a)	-3,6 -1,6	227	<u> </u>
2187 3237	r Puppla 4349	9 ,7	-35 35	ВЗр	_	4 ,77	+ 13		+34	5	(1)	-1,7 0,4	221	<del>-</del> 1
2188 3240	Puppla d368	10 ,2	-36 t	B3		5 ,12 5 ,27	+ 5	125°	+18			0,0	221	- 1
2189 3241	Puppls	10 ,2	-36 2	B8		5 .95	23 — 18	135°				2,7	221	- 1
2192 3243	h* Puppia 4198	10 ,5	-40 2	Ko		4 ,43 4 ,46	88 + 61	143°	Var	15 15	(2)		225	~ <u>s</u>
2195 3249	β Cancri 1917	11 ,1	+ 9 30	K2	64.3 OY	3 .76	75	224 0	+22,4 +16,9	13	(4)		182	<del>1</del> 25
2207 3270	q Puppls	14 ,8	-36 21	A.5		4 ,43 4 ,60	144 85	307 °	+ 5	42	(n)	5,2	222	4 4
2208 3275	31 Lyncks 1815	16,0	+43 31	K5	7',0 OY	4 ,43 4 ,33	107 + 44	185ª	+24,3	16 16	(4)		144	+ 36
2214 3280	Volantia 907	17 ,2	-65 18	Ko		4 ,98	31 - 29	21 8	0,0			0,7	246	- 16
2216 3282	w Puppla 5185	17 .5	-32 44	Ko		4 .94	+ 3	248°	+33,2			0,1	22()	∓ 3
2226 3294	B Volorum 3734	19 ,5	-48 10	B2		4 ,90 4 ,99	17 + 8	263°	+26	11	(1)		233	- 6
2233 3307	a Carinae 1032	20 ,5	-59 11	Ko	G*,4	1 ,74	+ 4	296°	+11,9	10	(1)		242	-12
2237 3314	30 Monocerotia 2339	20 ,7	- 3 35	ΔO	3°,0	3 .95 4 ,11	71	249°	+ 7	19	(4)		196	+20
	c Chamaeleont.	21 ,1	-76 36	P5	- ''	4 ,08	146	38°	-13.7	<u> </u>		4,9	257	-22
2247 3323	o Uzsae maj	22 ,0	+61 3	Go	4",6 Y"	3 .47	166		+19,2	6	(2)		123	+36
	Chamseleont,	23 ,6	-77 10	Ko	-	3 ,54 4 ,26 4 ,39	151	279°	+22,4	17 17	(2)		257	-22
2258 3347	# Volantia 933	24 ,6	-65 48	Ro		3 .65	十 y3 十 154	193°	+27,0	25 25	(1)		248	-16
2290. 3403	n Urme maj	31 ,5	+64 40	Ko	6',1 Y	4 .76	52		+14,7	17	(4)		118	+ 37
2291 3407	C Volorum 3646	31 .7	-49 36	Ko	_	4 ,87	3		+ 4,4	†"		-2,6	235	— <u>s</u>
2295 3410	ð Hydrae 2001	32 ,4	+ 6 3	Ao	2°.5 YG¹	4 ,18 4 ,37	74	<del>                                     </del>	Var +10,3	20 20			188	+27
	- 0146 0147 Theb-			11/1/ 0000	. 10.		- The 1		المراجعة	·				n 1- 1

Bom 2166, 2167 Probably a physical pair 4t", 220" — Bom 2168, 2169. The total magnitude of \$\chi\_{\chi}\$ Canori is 4\(\mathre{\chi}\_{\chi}\)1 and 4\(\mathre{\chi}\_{\chi}\)0 in t two systems used here

" 1±,\#

 $8^{\rm h}$ 

	2	3	1	5	6	7	8	9	10	11	12	13	14	15
2299	e <sup>2</sup> Carmae	33 <sup>m</sup> ,0	-57° 40′	Kο		4 <sup>10</sup> ,80	31		+ 23,6				241°	10°
3414	# 1591 # Hydrae	- - 1 - 1	F 3 42	<u>K</u> 0	6 <sup>c</sup> ,5	4 ,91	22 27	22 222°	+25.9	14	( <u>6</u> )	2,3	190	- - - - 26
2302 3418	2026				A3	4 ,55		1 27	25.9	15		1,7		
2307 3126	a Velorum 4451	34 ,2	-12 38	A 5		4 ,13 4 29	15 -  გ	247° -1 13	-20,0	17	(4)	0,2	230	1
2318	# Pyxidis	36 ,2	-34 57	G 5	-	4 ,04	20	165°	-118	11	(i)	-0,2	224	+ 5
3138	5128	3 72 1		Ř()	en a	4 ,11	- 20	- 4 182°	1,8	31	(2)	$-\frac{0.5}{-2.5}$	200	+16
2321 3111	9 Hydrae 2551	37 ,1		K.O	Y2 Y2	4 ,98 4 ,97	99 + 83	+ 53	1,0	32	(2)	5,0	260Y	FF 10
2324	b Velorum	37 ,3	16 18	I 5p		4 ,06	15	208 <sup>To</sup>	Var			0,0	233	- 2
2325	4438   o Velorum	37 .4	-52 34	J3 3 "		3 ,88	1 11 20	1 4 307°	+25.3 +17	12	-(i)		238	- 7
3447	1583	,				3 ,82	- 6	F 19		12		0,2		
2327 3 149	y Cancii 1895	37 .5	<b>├21</b> 50	A0	2°,3	4 ,73 4 ,91	- 50	243 <sup>节</sup> 十102	Vai <sup>™</sup>  - 36	12	(3)	-0,1 5,0	172	⊣ੌ35
2329	n Velorum	37 ,9	- 46 57	Α.3		4,85	29	262°	Val				234	- 2
3452 2330	4148 n Hydrae	38 J.C	1 3 46	33.3	2°,()	4 ,91	+ 11	- 27   265°	- 17   Vai	- 7	(3)	2,2 -1.4	ī9ī	+ 27
3454	2039			-	W	_4 .53	- 14	± 17_	F 23,8	7	` '	1,0		
2331 3457	d Carmae 1080	38 ,5	-59 24	132		1 ,42	— 25 — 17	256"   18	+ 12,9		(1)	-0,4	213	10
2335	31 Monocerotis	38 ,7	- 6 52	(±()	60,4	1,70	7	1170	1346	- 5	(1)	1,8	202	22
2336	2708 8 Cancii	30) ,0	 	Ko	5°,5	4 <sub>1</sub> 79   4 .17	210	181"	17. L	5     18	(6)	1,0 0,5		F 35
3461	2027	יי, פינ	1 10 31		Λ3	4 76	F 134	1 199	J	18	' '	6,1		1
2342	a Pyxidis	39 ,(	32 50	132		3 ,70 3 ,88	13	299°	F-16,5	6	(1)	−2.4   -0,8	223	Ī- 7
3468 2348	5651 1 (anci: )	40 ,0	+29 8°	A 5	() <sup>0</sup> , 1	6,61		1-' '''	i	"	ĺ		164	1 38
3474	1824		l lan P	(r5	138		64	202	    - 15,2	1.5	(5)	- (), <u>3</u>	164	<del> -</del> 38
2348 3175	# Cancri   1821	10 ,0	29 8		5°,4 Y3	4,20	54   13	1 52	[-13,4	11	(3)	2,9	1	
2349	d Velorum	40 ,1	42 17	( ± 5		4 ,12	18	341"	- 1,0	11	(1)	- 0,2 9,4		1 1
_ 3477 2354	4569 # Hydrae	41 ,	5 1 6 17	J-8-	5-,3	4 ,20 3 ,48	16 196	254	[- 36,8	1 '	(7)		189	+30
3482	2036	1	ì		2,3	3 ,58	- 98	1 171	Vai	32	1	4,0	207	1 20
2355 3484	12 Hydrac 2673	41 ,	7 -13 <sup></sup> 11	(+5	A, v	4,44	31	127°	- 8,5	4	(2)	2,0		1
2356	δ Velorum	41.5	-54 21	Λo	4%,1	2,01	96		- 2	30	(u)		240	6
2358 2358	1788 a Velorum	42 .	6 -45 40	Λο		2 ,25	1 77	231	F23,6			1.0	233	- 1
3487	4517					4 111	+_ 16	+ 14			1	0,7		
2361 3492	<i>Q</i> Hydrac 2040	43 ,	1   6   13	A 0	2º,4 W	4 ,42	1 15	1	1 33.4	11 9	(3)	2,1		-F-30
2363	f Carmae	44 ,	1 -56 25	B3	- 1	4 ,63	5	259°	+27				241	- 8
_3498 2375	1865 2 Pyxidia	16-	27 21	K2	6ª	4 .72	159	1 -	-24,7	17	(1)	$\frac{-1.9}{0.3}$	220	+ 12
3518	5986	[70]	, 4/ 41		A3	4 ,19	116	H- 108	1	17		2,8	3	1
2382	f Velorum	47 ,	2 -46 10	30		4 ,89 5 ,27	23		Vai			1,;	231	1
3527 2393	4661 ζ Hydrae	50,	1 + 6 20	Ko	5°,5	3 ,30	104	276°	+-22,7			-0,8	190	-  31
3547	2060		1	A 0	$ \nabla^1 $	3 ,34	- 81	E 66	1	17		3,4		 
2399 3556	ð Pyxidis 6072	51,	3 -27 18	A2	2°-3°	4 .87 5 .04	127 +123	30	1		1	5,4	1	
2404	i Ursae maj	52 ,	4 +48 26	A.5	36,4	3 ,12	502	240°	+13	62 59	(8)	2,0	0 139	-  42
3569	1707	i No to	 	of white	Y 15	3,36	1 - 200	<del>+</del> 457	1	ן ויי	1	į Oy		'

Boss 2318 A binary, the total magnitude of which is 1m,20 (RHP)

# 1100 Appendices to Chap 4. K.Lundmark Luminosities, Colours, Diameters, etc of the Stars

8h to 9h.

					8º	to 9º.								
1	2	3	4	5	6	7		9	10	lτ	12	13	14	12
2406 3571	o Carinao 1243	52 <sup>11</sup> ,8	-60° 16′	ВВ		3™,98 4 ,10	62 - 40	+ 48		22 22	(1)	2,9		10 <sup>q</sup>
2407 3572	α Centri 1948	53 ,0	+12 15	A 3	3°,3 W	4 ,27 4 ,50	54 + 54		<del>- 13,6</del>	30 30	(3)	1,7 2,9	185	+35
2408 3574	H Volorum 1788	53 .3	52 21	<b>B</b> 5		4 .77 4 ,86	11 + 11	195* 0	Var +22,2	3	(1)	-2,8 00	239	- 4
2411 3576	g Ursae maj 551	53 .5	+68 1	Ма	7'.1 OY'	4 ,99 4 ,93	- 21 - 21	315°	+ 4,8	ÿ 9	(4)	-0,2 1,6	113	+38
2413 3579	10 Urase maj 1956	54 ,2	+42 11	F 5	4*,1 Yu.	4 ,09	504 - 186	239° + 469	+27.1	69	(4)	3,3 7,6	147	+42
2421 3591	₩ Velorum 4810	56 ,3	-40 52	F8		4 42 4 54	68 - 32	299° + 60	Var 65	28	(B)	1,6 3,6	231	+ 4
2424 3594	# Urmac maj	56 ,8	+47 33	A0	2*,9 YG1	3 ,68 3 ,87	73 + 16	204°	+ 5	23	(2)	0,5 3,0	139	+43
2437 3612	Urano maj 2200	0 ,2	+38 51	G-5	5',9 Y'	4 ,71 4 ,76	43 - 12	234	+17.4	5	(4)	-1,8 2,9	151	+43
2438 3614	c Velorum 4883	0 ,7	-46 42	Ko		3 ,69 3 ,83	74 + 33	251 + 66	+24,2	22 22	(±)	0,4 3,0	236	Ŧ 0
2440 3615	a Volantia	0 ,9	-66 0	A.5		4 ,18 4 ,29	103 + 96		+ 7.7	27 27	(2)	1,3	250	-13
2441 3616	o Urane maj	1 ,6	+67 32	F	4°,2 Y	4 ,87 5 ,00	+ 40	184° + 57	- 1,8	53 52	(4)	3,5 4,1	113	+39
2443 3619	f Ursao maj 1365	1 ,9	+52 0	A3p	3',9	4 ,54 4 ,71	132 - 84	253° + 102	- 1,0	19 6	(2)	- 1,6 5,2	133	+43
2446 3624	v Ursao maj 798	2 ,7	+63 55	1°5 A 5	4°,2 Y1	4 ,74 4 ,83	122 + 122		- 6,5	19 19	(2)	1,1 5,2	118	+40
2450 3628	n Pyzidis 6895	3 .7	-25 27	K5	6°-7°	4 ,82 4 ,80	+ 21		-44,7	13	(2)	0,2 2,8	220	+16
2452 3634	1 Velorum 4990	4 ,3	-43 2	K5	7".3	2,22	- 26 - 4		+18,5	19 18	(2)	-1,5 -0,7	234	+ 3
2457 3642	It Carinac 861	4 ,8	—70 <b>8</b>	Взр		4 ,86 4 ,95	- 1		+35			-0,6	253	-15
2458 3643	G Carinao 779	4 ,9	-72 13	F5	<u> </u>	4 ,50 4 ,63	+ 20	252 + 17	+21,3			1,6	255	-17
2467 3654	Velorum 5206	7 1	-44 27	B5		4 .96 5 .11	+ 14		+35,4	7	(1)	-0,8 0,7	235	+ 3
2473 3659	s Caringo 1419	8 ,4	<b>-58 33</b>	B3		3 ,56 3 ,70	+ 44 + 18	263 + 37	+23,1	20 21	(2)	0,2 1,6	246	- 7
2476 3662	o Ureae maj 1285	9 ,0	+54 26	A.5	34'2	4 .89 5 ,05	+ 80		Ver — 16,9	19 19	(3)	1,3 4,6	130	+44
2477 3663	i Carinae 1201	9 ,0	-61 54	B3		4 ,18 4 ,29	+ 47		+16,6	25 24	(2)	1,1 2,5	248	-10
2479 3665	# Hydrac 2167	9 2	+ 2 44	AO	2°,9 Y¹	3 ,84 4 ,12	334 + 324	4+ 98		22 22	L'.	6,5		+34
2489 3682	1 Velorum 5408	11 ,		Ko		4 ,98		4 + 78	1	14 14	, , ,	0,7 4,4	231	+ 8
2491 3684	k Veloram		<del>-37 0</del>	F5		4 ,70 4 ,78	+ 2;	3 95 4— 23	+12			1,5		+ 9
2493 3685	/ Carinae 1023		-69 18		46,1	1 ,80 2 ,07	193	3 301 6 + 193	- 5			3,2	253	}
2495 3690	38 Lyncks 1965	12 ,6	6 +37 14	1	2°,9 Y¹	3 ,82 4 ,00	+ 6	7 191 8 + 119	+ 4	29 27		1,0 4,5	154	+40
2500 3696	g Carinae 1961	1	-57 7	1		4 ,18 4 ,31	31	6 233 9 + 21	1	13	(1)		245	
2503 3699	(Carinae 1465	14 ,	-58 51	Fo	4",1	2 ,25 2 ,43	2	6 266 0 + 24	+13.2	1		-0,6	246	F

9հ

						9"								
1	2	3	1	5	6	7	8	9	10	11	12	13	T.F	15
2506 3706	26 Hydiae 2609	15 <sup>m</sup> ,0	11° 33′	(75	5°,8 Y8	4 <sup>tn</sup> ,91 4,98	21 14		- 0'8	10 10	(1)	-0,1 _1,5	212°	+26°
2507 3705	40 Lyncis 1979	15,0	+34 49	K 5	0.23 0.23	3 ,30 3 ,34	216 - 171		十37.9	24 16	(4)	-0,7 5,0	157	+46
2511 3709	27 Hydrac 2613	15 ,6	9 8	Cr 5	5°,4 Y <sup>3</sup>	4 ,97 5 ,01	33 十 10	220° - 32	+25.5	15 15	(i)	0,9 2,6	209	+28
2516 3718	θ Pyxidis 7114	17 ,1	25 32	Ma	7° O³	4 ,93 4 ,91	+ 22 + 2	+ 22		14	(2)	0.7 1,6	223	+ 17
2521 3728	k Carmac 1242	18 ,5	-61 58	Ko		4 ,86 4 ,97	+ 10		<u></u> -			0,9	218	- 9
2524 3731	Leon19 1939	18 ,8	+26 37	Ko	A2 Q0'1	4 ,61 1 ,61	61  - 13	+_ 59		15	(5)	-0,2 3,6		+46
2525 3733	λ Pyxidis 7196	18 ,9	-28 24	021	Ϋ́2	1,90 4,81	150 64	142		39	(1)	5,9		+16
2526 3734	y Velorum 2219	19 ,0		B3	30,1	2 ,63 2 ,84	1 21	+ 19		12	(3)	-2,0 -0,8		<b>-</b> 3
2533 3748	a IIydiac 2680	22 ,7			Q <sub>8</sub>	2,16 2,24	3!	5 4	1	28 23	(4)	-1,0 -0,1	_	31
2534 3749	(+ IIydıac 2802	22 ,7				4 ,91	25 + 22	1 - 118	_[	17	(1)	6,9	-	
2536 3751	Diaconts 302	22 ,9	<u>_</u>	-	6°,6 ¥3	4 ,58 4 ,49	+ 1	3 -1 24		13	(3)	0,2		+33
2540 3757	h Ursao maj 845	23 ,7		_	3º,8	3 .75	11  - 6	7 96		36	(4)	4,1		1-42
2541 3759	1 Hydiae 2901	24 ,1			4°,2	1 ,78 4 ,89	- <u>i</u> 9	1 - 91	1	48 48	(1)	5,3		
2544 3765	s Anthac 5724	25 ,1				4 ,61 4 ,65	3. 1	5 -1 30		12	(1)	2,2	-1	+11
2549 3 <u>77</u> 1	d U15ae maj 565	25 ,0			5°,0 Y1 8	4 ,57	- 8	9 – 9	27.5	46	(5)	4,3		1-40
2550 3773	4 Leonis 2107	26 ,			6°,9	4 ,48 4 ,48		1 52	_	15 15	(4)	3,2		-1 46
2552 3775	## ###################################		2 + 52 8	_	3º,8 Y2	3 ,26 3 ,43	109 - 33	9 + 1037	4 15.5	73 73	1	2,0 8,5	5	1 46
2558 3786	ψ Velorum 6680	26 ,				3 ,64 3 ,76	~	8 + 184		65 65		. 5,		- <del> -</del> 9  - <del> -36</del>
2559 3787	74 Hydrag 2211	26	1		2°,8 Y1	4 ,50 4 ,69	_ - -	4 4 25	°+ 7	26 26 18	_	1,0		1-47
2565 3799	26 Ursae maj	_	1 + 36 5		2°,5 y1 5°,3	4 ,65 4 ,82 4 ,62	<u> </u>	2 + 72 0 154		18		4,0		
2566 3800 2567	10 Leonis min 2004 N Velorum	28 ,			0 Y 2 64,3	4 ,71	_+_2	8 + 11		19		2,		
3803	2270 Lyncis	}	8 +40	4 Ko	5°,3	3 ,23	+	5 + 40	)	39	` `	1,		
2570 3809 2574	2224 R Carinao		7 -62 2		Y2	4 ,96 Var	2	23 F 21		. 10		2,		1
3816 2581	1253 h Carinae	1	5 58 4		-	4,4-10 4 ,20		29 + 33 18 308	3 ° - - 22, 1				3 248	<u> </u>
3825 2589	1576 2 Soxtantis	ļ	_	6 Ko		4 .31	17		)°+44,9		(3)		3 198	+-40
3834 2590	2207 M Velorum		.3 —48 5	5 A.5	. Xa	4 ,81	1:		°- -21	_ 2(	1	6,	241	+ 2
3836	4836	l 7:	n 4 and 4m	1	1	4 .59		15十 124		1	ı	ا (	0	ı

Boss 2567 Varies between 3m,4 and 4m,2

#### 1102 Appendices to Chap 4 K. Lundmark Luminosities, Colours, Diameters, etc of the Stars.

					8р	to 10 <sup>h</sup>								
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
2595 3845	# Hydrae 2231	34 <sup>m</sup> .7	- 0°41'	Ko	6°,2 OY <sup>B</sup>	4 <sup>3</sup> ,10 4 ,10	+ 85 + 85	148°	+24,3	23 23	(2)	0,9	205°	+37°
2600 3849	# Hydrac 2917	35 .5	-13 53	В3	2°,3 W	4 ,96 5 ,22	31 + 2	238° + 31	+17	9	(3)	-0,3 2,5	217	+29
2602 3852	o Loonia 2044	35 ,8	+10 21	F5 A3	4°,0 Y¹	3 .76	150 - 66	255° + 135	+27,0	18	(4)	-0,1 4,6	194	+43
2604 3856	m Carinae 1477	36 ,6	-60 <b>53</b>	В9		4 ,67 4 ,79	- 10	299°	+24	17	(1)	0,8 2,6	249	<u> </u>
2605 3858	I Hydrae 2884	36 ,7	-23 8	B2p		4 .74 4 .95	- 17 12		+26			0.9	224	+22
2615 3871	Antilac 6881	39 .7	-27 19	F5p	Ãа 2.	4 ,98 5 ,05	64 - 40	291° + 50	+24,0	51	(B)		228	+20
2618 3873	a Leonia 2129	40 ,2	+24 14	GOp	4",5 Y",1	3 ,12 3 ,22	48 - 10		+ 4.5	18	(5)	-2.1 1.5	175	+49
2627 3882	R Loonia 2098	42, ,2	+11 54	Md	7°.9 OR°	Ver 5.0-10,2	33 + 22		+10	2	(a)	-3.5 2.6	192	+45
2628 3884	1 Carlnue 1888	42 ,5	-62 3	Go		Var 3,6-5,0	- 15	314° + 27	+ 4,0	4	(a)	-4,4 1,1	250	- 7
2632 3888	e Ureso maj 1268	43 ,9	+59 31	Fo	3°,8 YG1	3 ,89 4 ,02	330 - 79	241° + 320	+32	35 33	(4)	1,5 6,5	120	+46
2635 3890	v Carinac 1084	44 ,6	-64 36	Fo		3 .t5 3 ,23	21 - 0	287° + 21	+13,8				253	— <u>ş</u>
2635 3891	บ Carinae 1084	44 ,6	-64 36			6 ,03						2,6	253	<del>-</del> 9
2637 3894	φ Ursee maj, 1331	45 ,4	+54 32	Λ2	2°,8 Y1	4 ,54 4 ,72	- 6	_ 0°	-12,7	15 15	(6)	0,4 -0,7	127	<del>-  48</del>
2645 3903	u Hydrae 2963	46 ,7	-14 23	Ko	54,8 Ya	4 ,29 4 ,25	30 + 30	154° + 1	-14,5	11	(1)	-0,5 1,7	220	+31
2648 3905	μ Leonia 2019	47 ,1	+26 29	Ko	X10	4 ,10 4 ,08	227 102		+14,3	22 21	(6)	0,7 5,9	173	+52
2651 3912	12 Velorum 5508	47 .9	-46 5	Gs		4 .56	39 + 26	226° + 29	Var +10,8			2,5	242	+ 6
2657 3919	Hydrao 7585	49 ,6	-25 28	Ko		5 ,00 4 ,99	212 — 121	285° 十 174	+51,9	13 13	(1)	0,6 6,6	228	+23
2674 3940	9 Volorum 8075		<b>-54</b> 6	B5		3 .70 3 .85	- 23 + 8	255° + 22	+14,1	10 10	(2)	-1,3 0,5	247	U
2680 3950	# Leonis 2301	54 ,9		Me	71.3	4 ,89 4 ,82	+ 43 + 1	+ 43	+23,2	8 8	(4)	-0,6 3,1		+47
2690 3970 2692	Hydrao 3073		-12 35	B8	3°,8 YG¹	4 ,72 4 .89	38 28	+ 25	+24	13 13	(1)	0,3 2,6		+34
3974 2694	21 Loonis min 2110 2 Loonis		+35 44	AS	2°,9 W	4 ,47 4 ,68	54 + 40	96° 36	-12	26 26	(5)	1,6 3,1		+55
3975 2696	2171 A Leonis		+17 15	Aop	2°,2 YG¹	3 ,58 3 ,80	+ 9	+ 8	+ 2,1	8	(1)	-1,9 -1,0		+52
3980 2697	2112 15 Sextantia		+10 30	K2	6°,9 O"	4 ,58 4 ,53		+ 117	+40,2	15 15	(2)	0,5 4,9		+50
3981 2698	2615		+12 27	B8	1°.5	4 ,50 4 ,69 1 ,34		+ 29	+ 9,8	14	(2)	0,2 1,9	•	+43
3982 2706	2149		-11 52	Ko	5",5	1, 61	247 - 148 221	+ 198	+ 7· +19.9	64 63 18	(3)	3,3		+50
3994 2723	2820 q Volorum		-41 38	A2	Y	3 ,87		+ 221 281		17	(3)	0,0 5,5		+36 +12
4023	5713 2627. Long period					4 .23	- 54	+ 150	(	36	\''	5,1		T-14

Boss 2627, Long period veriable 5m,0 to 10m,2 is 310 days. — Boss 2626, Capheld veriables period 35,5 days. — Boss 2635. A binary 5", 128" — Boss 2637 ADS 7545. A well observed visual binary with a period of 113 years.

The state of the s

10h.

1	2	3	4	5	6	7	8	9	10	11	12	13	13	15
2730	ζ Leonis	[[m,1	1 23° 55′	Fo	3°,1	3 <sup>m</sup> ,65	27	125°	-11	23	(6)	0,1	178°	-1 56°
4031	2209				_ Y2	3,71	1 26	8		20	. –.	8,0		
2729 4033	2 Ursae maj 2005	11,1	F43 25	A2	2°,3	3 ,52 3 ,70	165 - 71	255  - 153	F 18	18	(4)	1,1 4,6	143	-1 56
2733	ω C 11111ac	11 ,4	-69 32	T3 S	- '' ¦	3,56	28	266°	<u> </u>	-   -	(2)	-1,2	258	- 12
4037	1178		_			3,70	F 8	+27		-11		0,8		
2739 4050	q Carmac 1817	13 .7	~60 50	K 5		3,44	16		-  8,1	12	(1)	1,2 1,7	253	4
2741	40 I conis	14 .3	4 19 59	- I· 5	444	1.97	329,		  - - <b>5</b> ,8	47	(4)	-33	185	- <del> -</del> 55
4054	2.166				γι	5 ,08	- 39 <sup>t</sup>	326		47		7,6		, , , ,
2742 4057	y <sup>t</sup> Leonis 2467	14 ,5	十20 21		5°,2	2,30 2,70	338 <sub>1</sub> + 308 <sub>1</sub>	117° 142	-36,0	30   25	(8)	-0,3 5,1	185	4-55
2743	y <sup>a</sup> I conis	14.5	- 20 21	Ko	A('8	3 ,80	353	121°	36.0	23		1,2	185	F 5 5
4058	2467				YG.	3 ,89	328	127		1		6,6		
2747	V Velorum	15 ,8	-54 32	Ko		1.58	22	214"	-[ 13.0		(1)		250	1
4063 2751	3474 M U19ae maj	16 4	+42 0	K 5	_6°.8	4,70   3,21	1	- 1284°	Vat	33	(4)	$\frac{1}{0,7}$	145	-1-57
4069	2115		' ' ' '		O3	3 ,25	- 67	4- 50	20 3	32		4,7		, ,
2754 4072	Uisae maj 664	16 ,9	166 1	Α0	2°,3	4,92 5,15	25		1,4	15	(3)	0,8 1,9	Ī 10	-46
2755	J Velorum	17 ,2	- 55 33	B5p		4,65	1 12		+10	[2]		112	251	<del></del>
4074	3286	•				4 .74	0	<del> -</del> 18			. –. –	1,0	}	L
2758 4080	ı Velorum 5809	18 ,1	-41 9	ĪČ 5		1,99 5,02	- 58	328°	1 20,9	6	(n)	1,0 3,9	243	- 13
2768	30 Teonis min	20 ,2	1 34 18	10	34,5	4 .83	107	217°	1 13.7	31	(3)		160	- - 59
4090	2128				Αı	4 .95	26	- - 104		32	` '	5,0	ļ	
2771 4094	μ Hydrae 3052	21,3	-16 20	IC 5	ნ⁰,3 O <sup>2</sup>	4,06 4,09	153	236°   151	F39.7	23	(2)	5,0	228	-1-34
2776	B Leonis min	22 ,1	-1 37 13	Ιζο	5°.3	4,41	161	227	-1 6.8	21	(5)		154	à 60
4100	2080	ļ			A3	4 ,36	114	l '		20		5,4		~ . ~
2778 4102	1 Carmac 733	22 ,4	-73 32	J+ 5		4,08	28 - 25		- 1,3			1,3	261	15
2779	a Anthao	22 ,6	-30 34	K 5	_	4 ,42	68	270°	- 15,2	10	(1)	-0,6	239	+22
4104	8465			 		4 ,44	= _22			10		_3,6		
2783 4110	Carmae 3256	23 .7	57 8	b 5 p		4 <sub>1</sub> 94 5 <sub>1</sub> 06	7  - 7	196°	- 1,2			~0,8	252	[2]- O
2785	36 ปัวจกอาทกา	24 ,2	- 56 30	1-5	4°,5	4 .84	182	l .	+9,60	70	(4)		120	j∓ 52
4112	1459				Ya.	5,01	75	1		69		G, 1		
2784 4114	5 Carmao 2227	24 ,2	58 14	[+0		4,08	18	243°	10,0			0,4	253	- 1
2792	30 Sextantis	25 ,2	0 8	135	16,9	4 ,95	54		4-11	- 8	(3)	-0,5	215	1-1-48
4119	2663	l <u>.</u>			W	5 ,22	- 1	F 54		- 8	(4)	3,6		- 
2802 4132	Ursae maj	27 ,5	F40 57	A5	3°,5	4 ,84 5 ,04	141		15	25 25	(4)	5,6		1~1 00
2804	Q Leonis	27 ,	-1 9 49	Вор	2",0	3 .85	9	I	37.6	11	(4)	-1,9	204	-1 54
4133	2166			-4.0	W	4 ,03	+_1	1 9	1 - 4 - 4	_7		-1.4	260	-  ,a
2809 4138	K Carmao 1034	27 ,	71 29	Λ2		4 ,94 5 ,03	39	- 148°	7.6			2,9		12
2811	p Carmao	28 ,	61 11	B5p		3 .58	26	286					254	<del>- 3</del>
4140	1704	000	, no 43	<sub>1277</sub>	_	3 ,72		F 25	 	- 140	10	0.7		12
2812 4142	Carmao 981	28 ,;	7 72 43	K5		4 ,90 5 ,01	9		11,2	10	(2)	-0,1 -0,3		13
2823	ı Carınac	31 ,8	8 -57 3	K 5		4 ,54	24	237	十 9,8	10	(1)	(), 5	253	- <del> </del> 1
4159	3544	20	[	- <sub>N11</sub>		4 ,66 Var	$\pm -\frac{13}{40}$		 	10		1,4		-I- 70
2827 4163	U Hydrae	32 ,0	6 12 52	Nb		4,8-5,6	40 - 32	110	18,8				229	+39
	ss 27 i2 A well obs	erved b	inary with n	- period as	ound 400						-	,		

10h to 14h.

	10 <sup>th</sup> to 11 <sup>th</sup> .													
1	2	3	4	5	đ	7	8	9	10	11	13	13	14	15
2829 4166	37 Leonis min 2061	33=,1	+32° 30′	Go	5°,3 Y°	4 <sup>m</sup> ,77 4 ,87	- 7 + 6	117° - 3	- 6,9	13 12	(3)	-1,0	162°	+62°
2830 4167	p Velorum 6042	33 ,1	-47 42	F2 A3		4,06	167 + 5	259° +167	+19,2	26 26	(1)	1,1 5,2	249	+ 9
2837 4174	γ Chamaeleont 822	34 .3	<b>-78</b> 6	Ma.		4 ,10 4 ,23	<del>- 45</del>	-	<b>—22,</b> 8	7	(a)	-1,7 2,4	263	- 18
2840 4177	t Carinsa 2460	34 .9	-58 40	K5		4 .73 4 .84	14 + 13	159°	+11,0	14	(a)	0,4	255	1
2842	z Velorum 3916	35 .3	-55 5	Go		4 .37	28	226ª	+20.7		_	' —	253	+ 3
4180	# Carinae	39 ,4	-63 52	Во	3°,8	3 ,03	+ 18 24	293°	Var	7	(3)	-2.7	257	- 3
4199 2863	1599 W Carinas	39 .7	<b>−6</b> 0 3	IK 5	_	3 ,20	- 9 38		+24.0 +12.2	_7 16	(a)		256	- 1
4200 2871	9882 7 Carinae	41 ,2	<b>-59 10</b>	Pec		4 ,60 Var	+ 7	+ 37 478	<b>-25.0</b>		(1)	2,4 -9,5	255	+ 0
4210 2875	2620 μ Velorum	42 ,5	-48 54	Nova G5	5",5	-1,0 to 8,5	- 4 78	<u> </u>	+ 7.3	30	(2)	-6,8 0,2	254	+ 9
4216 2888	5913 F Hydrae		-15 40	Ko	5°,8	3 ,01	+ 66	- 41	- 1,2	30 33	(3)	2,3		+ 38
4232	3138				A.	3 ,31	- 128	-171		33	/3)	5,0		
2889 4234	650		<b>-80</b> 1	Вэ		4,62	+ 14 + 14	+ 46	+21.7		-, ,-	3,0	265	-19
2899 4247	46 Leonis min 2172		+34 45	Ko	4°,9	3 ,92	304 + 289	+ 94	+16,2	37 35	(7)	6,3	157	+65
2900 4248	2058	48 ,2	+43 43	Ao	2°,4 ¥1	4 ,84 4 ,96	57 + 54	+ 18	-18,4	12	(3)	0,2 3,6	137	+62
2908 4257	u Carinac 2834	49 ,4	<b>-59 19</b>	Ko		3 ,88	65	1 2	+ 8.4	30 30	(1)	1,3	256	+ 1
2909 4259	54 Leonie 2314	50 ,2	+25 17		2°,9	4 ,51 4 ,49	77	257	+6	20 20	(3)		180	+64
2909 4260	54 Leonia 2314	50 ,2	+25 17	AO	0°	6 ,30		, <u>, , -</u> .					180	+64
2919 4273	Antileo 6808	52 ,1	-36 36	Ko	<del></del>	4 ,70	164		- 0,2	14	(1)		247	+21
2925	d' Cruteria	54 ,9	-17 46	Ko	2°,3	4,71	+ 159 481	284*	+47,6	14	(2)	0,1	239	+38
4287 2929	1 Velorum	55 .5	-41 41	A2	0 2 -	4 ,23	- 317 25	107°	- 5.1	15		7,6	250	+16
4293 2930	6276    # Ursas maj.	55 ,8	+56 55	ΔO	1*,9	4 ,71	+ 14 85		-11,4	45	(7)	0.7	115	+55
4295 2931	1808 p <sup>3</sup> Loonie	56 ,8	~ 1 57	Ma	74,3	2 ,67	+ 17		-13	44	(3)	2,2 -0,5	226	+ 51
4299 2932	2471 b Leonis	57 .6	+20 43	Ao	O <sup>8</sup>	4 ,42	+ 41	<b>∮</b> + 4	-10.6	8	(4)	3,0	191	+65
4300 2933	a Urma maj.		+62 17	Ro	W 5",0	4,62	- 28 139	- 1	9	14	(4)	1,7	110	+ 52
4301	1161 g Leonis			1	Ye	2 ,07	+ 13	+139	- 9	55 54	(4)	2,7		
2942 4310	9455		+ 7 53	Fo	3°,9	4 ,66 4 ,83		+318	+ 6,1	13	(4)	7.4		+- 59
2952 4325	2067		61 53	Κo		4 ,76 4 ,87		4+ 18		13 13		0,3 1,6	259	<b>- 2</b>
295B 4335	1897		+45 2	Ko	5°,1 Yn	3 ,15 3 ,21	+ 69	237° + 69	- 4,2		(4)		132	+64
2960 1337		4 ,4	-58 26	F8p		4 ,02 4 ,15	19		Ver. + 7.3			0,4	258	+ 2
964 141	β Crateria	6 ,	-22 17	A2	4 W	4 ,52 4 ,69	10:			$\vdash$	1		243	+35
	1 2909. Honey: A	" LDG 207	9. <i>6</i> 7.1. 1085	!4 (1025)				<b>7</b> 1	IT UN	ŀ	ı	4.5	1	1

₹2909. Hossy: ADS 7979. 6",3, 108",4 (1925,6). Dynamic parallex 0",025,

30. 44 

30 44

11<sup>h</sup>.

						LI"•								
1	2	3	ŧ	5	6	7	. 8	9	10	11	12	13	14	15
2966 4352	y Carinae 3190	8 <sup>m</sup> ,3	59° 46′	F5p		4 <sup>m</sup> .73 4 ,85	11 + 6	117°	- 8,4			-0,1	259°	
2972 4357	δ Leonis 2298	8,8	+21 4	A3	2°,8 Y1	2,58	207 + 203	135° - 43	23,2	66 64	(7)	1,6 4,2	194	- - 68
2974 4359	θ Leonis 2234	9 ,0	+15 59	A0	2°,5 W	3 ,41 3 ,59	106 + 38		+ 7,2	26 26	(6)	0,5	204	+65
2976 4362	72 Leonis 2322	9,9	+23 39	Ma	6°,8	4 ,87 4 ,78	18 0	236°	+15.8	8	(3)		185	-j-68
2982 4368	φ Leonis 3316	11 ,6	- 3 6	A.5	3°,5	4 ,58 4 ,77	120 - 19	248°	- 7	29 29	Ĩ(1)		232	+ 52
2984 4374	& Uisao maj ) 2132	12,9	+32 6	Go	4º Y2	4 ,87 4 ,96	732 + 285	215°	-15,5	- 1	(7)		163	- <del> -</del> 70
2984 4375	£ Uisae maj 2132	12,9	+32 6	Go	4°,0 ¥3	4 ,41 4 ,50	732 + 285	215°	Vai. -15,9				163	+73
2985 4377	v Ursae maj 2098	13 ,1	+33 38	Κo	5°,9 OY8	3 ,71 3 ,67	27	304° - 27		16 14	(3)		157	+70
2987 4380	55 Ursac maj 2225	13 ,7	+38 44	A2	2º,8 W	4 ,78 4 ,96	102 + 43	214°	Var 3	14 14	(5)		143	- <del> -</del> 68
2989 4382	δ Crateris 3346	14 ,3	-14 14	Ko	5°,4 Ya	3 ,82	230 - 230	328°	5,1	20 18	(4)	-1 -	240	+43
2990 4386	σ Leonis 2437	16 ,0	+ 6 35	A0	2°,8 YG1	4 ,13 4 ,34	95	261°	Var 5,3	16 16	(4)	0,2	222	+61
2992 4390	π Centau11 4498	16 ,4	-53 56	B5		4 ,26 4 ,38	+ 10	243°	+16.	14	(2)	0,0	258	+ 6
2999 4399	Leonis 2348	18 ,7	+11 5	1,75	3°,7	4 ,03	176 + 153	119°	10,0	51 51	(3)		218	+65
3005 4405	γ Cratoria 3214	19 ,9	-17 8	As	4°,0 W	4 ,14 4 ,33	107 - 47		-1- 4	31 31	(2)		244	-1-41
3031 1434	λ Draconis 005	25 ,5	+69 53	Ma.	6°,9	4,06	45	238	+ 7.0	15 15	(5)	-0,1 2,3		-1-47
3035 4441	o <sup>1</sup> Contauri 3692	27 ,1	-58 53	F8p		4 ,96 5 ,09	18	174	-20			1,3	261	+ 2
3036 4442	o <sup>a</sup> Contaum 3693	27 ,1	-58 58	A2p		5 ,26 5 ,33	29 + 13	232°	-16,8			2,6	261	+ 2
3042 4450	ξ Hydrae 9083	28 ,1	-31 18	G5		3,72	- 36 - 36	256°	- 4.3	16	(1)	0,3 5,3		+29
3048 4460	A Contaun 4637	30 ,0	-53 42	_B8_		4 ,82 4 ,91	65	267°	+ 4	22 22	(2)	3,9	260	+ 7
3054 4467	l Centauri 2127	31 ,2	-62 28	В9	1	3 ,34 3 ,51	48	242°	+ 8	18 18	(3)	-0,4		- 1
3055 4468	v Cratoris	31 ,6	9 15	139	2º,4 W	4 ,81 4 ,98	- 32	271° + 52	_ 1·	14 14	(4)	3,7	244	+50
3058 4471	v Leonis 2458	31 ,8	- 0 16	K0	5°,4 Y <sup>8</sup>	4 .47	- 3: - 30		1,2	18 17	(4)	0,0	237	+58
3073 4494	a Hydrae 7610	35 ,2	-34 11	138		4 ,88 4 ,98	→ 13	272° 3 + 27	+ 6	8	(1)	-0,0 2,3	255	+26
3076 4499	Centauri 2514	36 ,2	→61 32	Go		4 ,88 5 ,01	;	68	° Var - -14,2			-1,0	263	- 1
3087 4514	ζ Ciateris 3460	39 ,7	-17 48	G 5	4°,8 OY <sup>9</sup>	4 ,90 4 ,93	+ 50	139	°  4,6			3,1	251	+42
3089 4517	v Virginis 2479	40 ,;	7 + 7 5	Ma.	6°,7	4 ,20 4 ,18	18		+ 50,6			- 0,2 5,0	233	4-64
3090 4518	χ Ürsac maj 1966	40 ,8	+48 20	ΙĆΟ	5°,5 OY8	3 ,85 3 ,85	13	7 276 9 + 119		1 -			3 116	+66
3092 4520	λ Muscao 1640	40 ,	−66 10	A 5		3 ,80 3 ,94	10:		416			3,	264	- 5

Boss 2984 Wellknown visual binary. Period 60 years,

# 1100 Appondices to Chap. 4 K Lundmark | Lumboshiles, Colonis, Diameters, etc. of the State

11h to 12h.

11 <sup>h</sup> to 12 <sup>h</sup> .													
1	2	3	4	5	h	y	#	, "	10	11	17	11 11	
3094	Contauti	41°°,7	60° 37′	(+0		47,24	10	23.34	45	41	(4)	2,1263	rt 0•
4522	3325 93 Leoniu	40	- <b>  2</b> 0 40	1-8	414	4 .44 4 .54	22   155	402 °	} iVus ¹	- 401  - 481	(4)	4.9]   2.4,207	 
3098 4527	2358	ባፉ ነበ	7 40 70	T. D	Yi	4 ,68	57	1 (4)	0,0	•	47	88	۱٬٬۵
3099	и Минено	43 ,4	~~66i 15	K5		4 .71	10	108"	1 37.4	.		2014	- 5
4530 3101	1649 # Languis	44 .0	115 8	A2	2.5	4,82   2,24	10   5 1	250	   U ;	. 84 !	(11)	3,1    10,222	   1-71
4534	2383	יין, דר	1.3 "		γĭ	2 .53	118	1491	1	Hall	<b>,</b> ,	5 H	'''
3103	j Continuel	44 .H	<b>63 14</b>	115		4 .53	1 11	#45" 1 17	1 17	1 1		10/84	- 2`
4537 3104	HRQ1 Milwale	45 ,2	60 40	(v 5		4 ,63		JII5"	1   [-[K <sub>1</sub> 2]	स्वा	(1)	4.1.465	~ 9~
4538	1595					5 ,01	1	11	'	1 4		11,1	1
3105 4540	// Viryinia 24H/)	45 .5	1 2 20	1-8	47,2 YI	1 (8) (9), F	791	111" 494	1 44	UH I	(4)	1.7.241	+60_
3100	li Contauri	46 ,1	-44 37	Ko	*	4 .71	138	J711"	1 2,4	, , ,			+16
4546	7614	· .				4 ,68	- 15	1 91	1	į	4.4	4.7	
3115 4552	# Hydrae Bol8	47 ,8	<b>11 21</b>	119	'	4 40	56 EN	264 1 51	1.	. [4] 14]	(1)	14,1 446	+28
3117	y Unan maj.	48 ,6	4 54 15	Αu	159	2 ,54	į įH	KR"	11	48	(r)	0 1 107	F62
4554	1475				W	2 .72	11 31	, 149	35	444	(4.1)	1 4.4	
3139 4589	ក Yinghila 2502	55 .7	4 7 10	A3	2",5 Y	4 37	33	187"	24.0	172	(4)	1.4 241	+66
3146	Pt Crecks	58 ,0	-02 45	A5		4 ,48	140	269"	- 2,5	14	(4)	100 265	- t-
4599 3151	2543 61 ( male	in 2	-62 30	31.4		4 ,58	11 6	{	1      164	1 !		5.3    28.5	  ⊷ 1
1603	2501	37 14	100	<b>"</b> "	ŀ	5 (16)	l_	11 5	11 1161	,		- 10	'
	e Chamaoleent.	30 .0	<b>-75 57</b>	K 5		5 (41	91	1 208	1 44			268	-14
4605 3155	777 n Virginis	0 ,1	+ 9 18	Ci S	51.1	4 .24	1 44	1 24	29,4	31	। . (न)	1 4,81 0,6,241	. F69
4608	2583		' ' ' ' '		Υï	4 28	- 141	1 174	-20	19	,	0,11	-
3160 4610	y Cruch Midă	1 .7	<b>64 3</b>	Fo	Į	4 (4)	46	180°	1 94	1	i	266 2,ი:	- 2
3162	Contanti )	2 ,9	-50 6	Ds		4 .81	1 41 1 <b>3</b> 0	Ziei <sup>6</sup>	1 10	1	. (A)	0,7 264	+12
4618	0#18		-			4 (90	- 0	1 39	44	8		2,2	
3165 4621	d Contaurl 6697	3 ,2	— <u>5</u> 0 10	B3p	47,0	1.07	1 43	340"	Var.	15	(1)	~ 1,2 264	+12
3166	a Corvi	3 .3	-24 10	Fa	5° Y4	4 .18	93	133*	+ 4,6	42	(2)	2.3 260	+ 37
4623	10174	١.,		w <sub>0</sub>		4 ,28	十期	- 45		43		4,01	1
3172 4630	# Corvi 3487	, s	-22 4	K0	37.9	3 ,21	- 05 - 37	276° 中 33	4.4	28 28	(6)	1 2,3	+39
3176	g Centauri	6 4	-51 4B	В3		4 ,20	40	211	+ 21	13	(2)	0,1 261	<b>10</b>
4638	6455 8 Crucis	9,8	-55 12	B3	350	4,32	+ 5	+ 49 - 246*	-4-26	15	  - (2)	! 3,7 } !- 1,0,200	+ 4
4656	4189	' '		",	J 100	3 ,25	+ 3	48	+	13	144	1.5	_
3190 4660	A Urano maj.	10 ,5	+57 35	A2	21.7	3 .44	110	189ª	12	41	(6)	1.5 99	+59
3191	y Corvi	10 .2	-16 59	Da	350	2 78	160		. Var.	40		0,9 361	+44
_4662	3424	1		_	W	2 .98	- 90	+ 133	- 4,2	42		3,8	
3197 4671	Muscus 1931	12 ,1	-67 24	Мь		4 ,16	237  - 21	259° +237	<sub>1</sub> + 7.2	44	(=)		- 5
3199	# Chamnelson t	12 ,5	-78 45	115		4 ,38	49	284°	+23	16	(1)	0.4 30	-17
4674	741	Į.		`		4 .49	- 20	+ 45	r	16	1	2,8	L
3200 1079	¢ Crucie 2235	13 ,0	-63 26	B3		4 ,26	1 30	: 347" }+ 50	+19	16		0,3 267	- 1
3203	# Centauri	13 ,6	-54 35	Ma		4 ,98	7 94	241*	- 6.9	l-		260	+ 1
4682	5113 = 1161 1161 1164	\ -	43-4-41	I	ı		14 11	i+ 93	1	1	1	4,9	

Ross 3162, 3163. Probably a wide double.

12h

						12 <sup>h</sup> .								
1	2	3	1	5	6	7	8	9	10	11	12	13	11	15
3210 4689	η Virginis 2926	14 <sup>m</sup> ,8	- 0° 7′	A <sub>0</sub>	3°,0 W	4 <sup>tn</sup> ,00 4 ,21	67	248° + 66	Var + 7	25 24	(2)	0,9 3,1	257°	+61°
3216 4697	11 Comae Bei 2592	15 ,6	+18 21	Ko	5°,5	4 ,91 4 ,87	139 -122	303° + 65	+42,4	15 14	(4)	1	242	+ 78
3218 4700	ε Ci μοις 4188	15 ,9	-59 51	K2	7,0	3 .57 3 .73	199 133	292°	- 4,8			5,1	267	+ 2
3224 4707	12 Comae Bu 2337	17 .5	+26 24	F5	4°,1 Y2	4 ,78 4 ,92	+ 8	205°	Vai + 1,9	36 36	(1)		200	+84
3230 4716	5 Canum Ven 1626	19 ,2	+52 7	Ko	4°,3 Y <sup>2</sup>	4 ,97 4 ,96	11	52° - 10	-13,4	11 11	(3)	0,2	97	<b>465</b>
3237 4730	α <sup>1</sup> Crucis 2745	21 ,0	62 33	B1		1,58	47 + 17	228°	Vai ? —12,2	18 17	(5)	-2,1	268	1
3238 4731	α <sup>2</sup> Crucis 2745	21 ,1	-62 32	_B1	2,3	2,09	49 - 1	251° + 49	Var? + 0.3			- 1,6 +0,5	268	= 1
3242 4737	γ Comae Ber 2288	22 ,0	+28 49	ΚΌ	5',2 Y8	4 ,56 4 ,52	122 + 40	225° +116	+ 4,0	13 10	(6)	0,4 5,0	163	+85
3245 4743	σ Centaurı 7115	22,6	<del>-49</del> 40	В3		4 ,16 4 ,27	47 + 10	233° + 46	+12	14	(2)	0,1 2,5	267	+12
3256 4757	δ 01 δº Corvi 3482	24 .7	-15 58	Ao	3°,5 YG1	3 ,11 3 ,31	251 + 18	235° +251	- 4.	22 18	(2)	-0,6 5,1	264	+46
3263 4763	γ Crucis 5272	25 ,6	-56 33	Mb	6°,9	1,61	273 +259	176° + 90	+21,4	-		3,8	268	+ 5
3263 4764	7 Crucis 5272	25 ,6	<b>-56</b> 33	^A2	-	6 ,68 6 ,84							268	<del>- -</del> 5
3269 4773	γ Muscae 1336	26 ,5	<b>-71</b> 35	B5		4 ,04 4 ,14	46	253° + 46	+14	15 15	(2)	-0,1 2,3	269	10
3272 4775	η Co1v1 3489	26 ,9	-15 38	Fo	5°,2	4 ,42 4 ,54	444 164	261° +413	<b>- 5</b>	45 45	(3)	-	266	-∓-46
3279 4785	β Čanum Von ¨ 2321	29 ,0	+41 54	Go	5°,0 Y1	4 .32 4 .43	758 508	292°	+ 6,1	109 110	(4)	4,5 8,7	99	<b>∓75</b>
3280 4786	β Co.v. 3401	29 ,1	-22 51	G 5	_4°,8 	2 ,84 2 ,93	61 + 52	180° + 32	- 7,1	26 26	(3)	-0,1 1,8	266	+39
3281 4787	₩ Dracoms 703	29 ,2	70 20	B5p	2°,2 W	3 ,88 4 ,08	60 10	276° + 59	Var. 11,4	7	(4)	-2,2 2,8	92	+48
3283 4789	23 Comae Ber, 2475	29 ,9	+23 11	AO	2 <sup>6</sup> ,7 W	4 ,78 5 ,03	- 72 - 39	276° + 60	-23.	12 12	(5)	0,2	244	∓83
3284 4791	24 <sup>1</sup> ComacBot.) 2684	30 ,1	+18 56	A3	⊢1° BV²	6 ,72	19 - 19	325° + 2	+ 3,7	9	(2)	-0,3 1,4	257	+80
3285 4792	24 <sup>9</sup> Comae Ber. 2584	30 ,1	+18 56	021	5°,9	5 ,18 4 ,98	16 - 12	14° 11		11 11	(1)	0,4	257	十80
3289 4798	M Muscao 1702	31 ,2	<b>-68</b> 35	B3	2°,8	2 ,94 3 ,13	+ 42	240° + 41	+18	13	(4)	-1,5 1,0	269	7
3292 4802	7 Centauri 7745	32 ,3	47 59	A2		4 ,02 4 ,15	+ 7	228° + 26	+ 5:	9	(1)	-1,2 1,2	269	<del>+</del> 14
3298 4813	7 V11 gin1s 3452	34 ,1	' '	Ko	6°,0 Y2	4 ,78 4 ,74	85 8	244 ° + 84	19.7	14 14	(2)	0,5 4,4	267 <sup>°</sup>	+55
3300 4817	l Centauri 7748	34 ,4		B8		4 ,79 4 ,94	- 63 + 14	227° + 61	<b>+15</b>			3,8	268	+23
3302 4819	γ Contauri 7597	l	-48 25	A0	30,8	2 ,38 2 ,59	200 - 82	266° + 182	8	17 17	(2)	-1,5 0,9	269	+14
3307 4825	y Virginis 2601		- 0 54	Fo	3°,6 Y1	3 ,65 3 ,92	564 -299	271° +479	19,8	_		7,4	268	<b>∔61</b>
3307 4826	γ Virginis 2601	1	- 0 <del>54</del>	Fo	3°,3	3 ,68 3 ,95	564 299	271° 十479	20,0	67 65	(8)	1,8 7,8	268	L
3309 4828	Q Virginis 2486	36 ,8	+10 47	ΑO	2°,5 W	4 ,95 5 ,14	135 +132	138° - 28	0:	13 13	(5)	0,5 5,6	267	+73

Boss 3263 Bluary? — Boss 3284, 3285 A binary included on basis of its total magnitude 4,95 (RIIP) — Boss 3307 Visual binary rith a period of about \$180 years

12h to 18h.

			12"	to 184.		
ı	2	1 4	5 1 6	3 { 15	9 (a) 11	14   14   15   15
3311	w Configuri	37™.1 -48° 16′	Ka ¦	4",65 (29) 4 ,76   1 t	248° 11.7 11 1128 ' 14	(1) 02.269 1.44* 5.2
4831 3319	760H 7 Trucki	B) ,7; -~60 26	Ku ¦	4 ,68   128	129" (1 8,9 24	(I) 1 ii 200 (E. 2)
4842 3320	4273 // Morao	40 .1 -67 34	1 161	4 49 1111 3 46 11	24   42   31	1,2 -(5) 1,230 0
4844	2004	]	l Nef.	1,44   10 1,010 to 5	[ 68 ] 19 - 55*+1 [4   8)	Б. 1 - ин з <b>5.1</b>
3322 4846	Y Camma Ven 1817	40 4 145 59	Wh   Viu ,		1111	
J324 4648	Criu is 5215	40 ,6 - 55 50	113	4 366 55	- 224° (1 1647, 146 - 1 52 (1 146	(2) 0 11 27 0 1 to
3328	#Crin is	41.9 -59 9	351   257	1 ,50 56	210° (20,0, 11 1 50 - 11	(4) ; 3 (A) ; (4) ; (5) ; (4) ; (5) ; (5) ; (6) ; (7)
4857 3351	1454 o Centau <del>ri</del>	47 .5 - 48 24	K2	4 (35 1 103	JS1" 0,7 18	(1) 100 471 (14)
48HR 3352	՝ 7753   ը (տվայցի	17 9 -39 18	] Λ5 (	4	140"     3 H 	1 124 124 1 4 4
4889	7H9		183	4 350   67	- 17   ' - 110   116   148	(K (J) 11, J71 (J)
3357 4897	4 Criu.le 4 584	48 .7 58 36		ा के अने । क्री	1 46 1 15	14
1358 4878	μ <sup>t</sup> Crucle 54H7	4H ,H -56 3B	11.3	4 ,16 10	248"   1129, 13   16   18	(a) 271 F \$ 2,1
3359 4899	μ <sup>4</sup> Crus Is 5487	44 .8 -50 37	33p	5 .46 A7	1 30 131°   1971	11 4 471 (4) \$
3362	y Virginia	49,24,~9 0	Mb 3740	4 (91 ),14	1 42 17,61 3 1 42 9	14) 0,4 274 +53
4902 3363	J449 * Urnea nusj	49 .6; 1-56 30	Aop 15.0	1,68 115	944 80 51	2,4 (2) 0,1 24 +61
4905 3367	l 1627 ' ð Virginis	54 .6 F 3 56	W   Max   07.6	1 2 03 F 25 3 66 479	112   149 262"   17.9   18	2 (3) 0,2 277 1 65
4910	addy at Cumum Von 1		Y*   Aup   3°	1 .65 187	1444   147 - 464 - 53	7.1 0,2 78 +78
3370 4914	1 4680	51 ,4 +38 52	QK <sub>T</sub>		Later	4.7
3371 4915	2880	SL:4 <sup>1</sup> 十3H 52	Aup 27.9	3 .05 -114	141" - 1 K 31	(5) 14.7 7A + 7B 4.7
3374 4920	36 Commo Her	58 .0 +17 57	Mu 6".7	4 ,96 ' ,56	(92° ~ 1,7 11   [9]   11	(4) 11 2 286 +79 2 7
3377	A Muscus 1848	55 ,4 -71 1	K2	3 ,63 264 7 ,79 4 137	, uy^ 1 56,1 26 227   20	(1) 0 ( 271 - 9 5 #
- 4923 - 3382	76 Ursen maj.	30 .5 +56 55	Fu 5.4	4 .89 Iut	[U]* }- 9 35	(7) 26 #3 +61
4931 3383	1408 Virginis	57 .2 +11 30	toYt   Ko,\$*.0	1 2 .95 174	~ 95 35 271* -115 29	4 9 (4) 0,2 284 +73
4932 3390	2529 i Contauri	0 4 -47 56	13 1 Ya	1 .02 -145	+2)2 '44 , 221' + 9 16	5.1 (a) 1.0 22.1 +14
1510	BONE		-	3 .04 + 17	14 57 10	J.H.
3393 4942	7644	1 ,0 ~49 23	B3	4 ,40 42	335"   Var. 33  -   48     14,3 33	(a) 0.0 371 +11 2.5
3401 4954	41 Comas Bar 2185	2 14 +28 10	Ks GA	4 ,90 89 4 ,91 + KK	164" 16.3 12 + 9 12	
3109	8 Virginia	4 .8 - 5 U	λο 37.7 W	4 44 57		(5) 0.3 ## + +56°
4963 3412	a Comas Ber.	7 5 .3 +18 4		5 ,22 450	2864 ,-17.5	4,6 294 +78
4968 3412	2697  a Comeo Ber.	5 .5 +18 4	P5 Yi	5 30 -30x 5 ,22	+333 1 77	4,6 296 475
4969 3419	2697	6 ,0 -59 23	BE	5 .30 1 4 .76 61	236*   Var. 18	·
4975	4815			4 35 + 4	+ 61   15	3.7
3421 4979	Centauri 8437	6 ,5 -37 16	01	4 ,59 390 4 ,94 -342	, 274" [-15.8 24 +308 } 24	,(1) 4.8 275 千型 7.8
D <sub>0</sub>	m 1358, 3350, Å b	danyi 36", 17"	Decs 3370, 3371	A blooms as a sec-	- None 1462. Walliam	era bisagra wata di penjadi d

Dem 3368, 3359. A blancy: 36", 17" — Boss 3370, 3371. A binary: 26", 266" — Boss 3462. Walkenson binary with a pusit Also years, 16s lotal magnitude is 4=,67 (RMP).

13h.

						<u>, 1</u>	10".	l e	i c	1 40	0,0	42	12	14	15
<u> </u>	2	3	1		5	6	7	8	9	10	11	12	13	-	
24 83	β Comae Ber 2193	7 <sup>111</sup> ,2	+28°	23'	G0	3',9 YG1	4™,32 4 ,44	1184 1101	+ 126		112	(4)	4,5 9,7	3°	+ 84°
29	η Muscae	8 ,5	-67	22	В8		4 ,95	32	234	Var	9	(2)	-0,3	273	- 5
93	2224 Muscae	40 "	66	4.5	Ko		5 ,04 4 ,78	+ 4 35		+ 5 -10,3	- 9		2,5	273	
37 102	2142	1		<sup>13</sup>	77.0		4,90	+ 26	+ 23			,	2,5		- 
46	σ V11 gmis 2722	12 ,6	+ 6	0	Ma	6°,9 OYa	5 ,01 4 ,93	16 15		-26,7	5	(1)	-1,7 1,0	291	+66
115 47	20 Canum Von	13 ,1	-+41	6	Fo	3",5	4 ,66	125	272	+ 8,7	10	(4)	-0,6	66	-H-75
148	2380 61 Virginis	13 ,2	17	45	G5 I	Ψ1 4',6	4 ,87 4 ,80	35 1529	-	 	9	(4)	$\frac{5,1}{5,2}$	280	+43
219	3813			1		Ya	4 ,84	+ 260	1498		122		10,7	ļ	
149 120	γ IIydiae 3554	13,5	-22	39	G 5	5',0 OY2	3 ,33 3 ,41	+ 80 + 80	— 24		28 26	(5)	2,9	280	38
152	i Centauri	15 ,0	-36	11	Ā2	40,5	2 ,91	+ 353		0			5.7	278	+25
)28 156	8497 Centaun )	16 .1	-60	27	В3	-	3 ,13 6 ,51	20	233	o - 7				274	+ 2
234	4627				12 #		6 ,81	39		4-26	11	(2)	3,6	274	+ 2
157 03.5	J Centauri 4627	16 ,2	-60	28	B5		4,72	- 2	4 39		11	120)	2,3		
164 041	ın Contauri 2732	17 ,2	64	1	Go		4 ,50 4 ,62	+ 50		412,1			3,0	274	- 2
463	LI Muscae	17 ,2	-74	22	Ko-	-	4 ,96	20;	3 222	°+28,8	14	(a)	0,7	273	- 12
042 474	1057   \$\alpha^1 \text{ Ursao maj } \]	19 ,9	+55	27	A0p		5,06 2,40	+ 73			44	(12)	5 <sub>ي</sub> 6 6,0		+62
054	1598		l			1°,9 W	2,64	F 3	6 - 125	9,9	44		3,0		+62
475 055	ζ <sup>n</sup> Ursae maj 1598	19 ,9	+55	26	ΛO	G <sup>8</sup>	3 ,96 4 ,20	+ 4	2 - 129				2,2 4,6		
476	a Viighis	19,9	-10	38	B2	1º,6 W	1 ,21	5	5 229 6+ 54		23	(4)	-2,2 -0,8	285	+ 50
056	3672 ω Contauri	20 ,8	46	47	-	3°.5	1 ,52	-	7,1		0,14	(1)		277	ī ī ¯
100	g Urate maj	21 ,2		~ 30	^ A 5	30,2	4 ,02	12	  3 <sup> </sup>   102	-12	37	(7)	1,8	78	+61
480 062	1603	, , , , , , , , , , , , , , , , , , ,	Į		_	OY1	4 ,19	+ 3	2- 119	)	36		4,5	5	-1-46
1482 1068	69 Vitginis 3668	22 ,1	-15	27	Ko	5º,6 Ya	4 ,89 4 ,85	- 12	7 270 5 + 94	5° — 13,7			2,7		
1491	R Hydrae	24 ,2	-22	46	Md	79,6	Vai	7	3 273		0			283	+ 38
1080 1496	d Centauri	25 ,2	38	54	Ko	OR8	3,9-10,		7 + 50 19 211	3,1				279	+22
,089	8592					20.2	4 ,01	+ 7	1 + 2	1	1	(4)	1,3	3   3  291	+ 54
3499 5095	1 Viiginis 3714	26 ,8	5	45	Ma	7°,3	4 ,83 4 ,79		3 <sup>1</sup> + 11:		11		5.1	1	
3506	o Virginis	29 ,	1 + 4	10	A2p	2°,4 W	4 ,93 5 ,14		32 <sup>1</sup> 12 18 <sup>1</sup> — 1		18	(7)	3,	298	+ 63
5105 3508	2764 Vuginis	29 ,	6 — ō	5	A2	3º,4	3 ,44	28	38 27	7°-13	36	(3)	1,	2 295	+ 60
5107	3076	30 ,	1	42	Fo	3°.7	3 ,62 4 ,96		34'-  22: 50 10:	2 ° Var	36	(3)	5,		+75
3511 5110		30 ,	J T3/	14	1.0	Yi	5 ,11	+ 3	38¦ 7	6 +62	32		4.	6	
3512 5112		30 ,	4 +49	32	A3	3',3 W	4 ,63 4 ,88		18 27 26 + 11		17	(4)	5,	. 1	
3518	24 Canum ven	33 ,	0 +36	48	Fo	30,4	4 ,92	10	04 27	8° Vai	27		1,	8 41	+ 75
5127 3521		33	5 - 52	57	В1	Y¹   2 <sup>1</sup> ,8	5,05		41¦- - 9 41 <b>22</b> 9	6 - 6	-24 11	1	5,  -2,	2 278	+ 8
5132	6655	_			1		2 .77	' +	3+ 4	1	_ 11		0,	6	
3530 5154		36 ,	9 + 5!	12	Ma	70,0	4 ,7:	1 1 -	13+ 2	2° — 16,	9 10	4 '-'	$\begin{vmatrix} -0 \\ 2 \end{vmatrix}$	0	
3544	Centauri	40	,o <del>- 3</del> 2	33	F5	Ì	4 ,30	5 4		2° -23	61		)   7	,8 284	+27
5168	3   9603 Bore 2456, 3457 Bir	l 60	// 0428	n.	2484	ी करणार विके	4,4%								ng perle

Boss 3456, 3457 Binary: 60", 343° -- Boss 3474, 3475 Binary: 14", 150°, member of Ursa Major Cluster -- Boss 3491 Long period ariable, period 114 days

## 1110 Appendices to Chap.4 K.Lummark Luminosities, Colours, Diameters, etc of the Stars

18h to	14h.
--------	------

						Yo-	W 17 4								
1	2	3	4		5	6	7	8	9	10	11	12	13	14	15
547 172	M Centrori 8017	40 <b>™</b> ,4	50°	56′	Ko		4 <b>-</b> ,68 4 ,79	32 + 27	176° + 18	Var. — 5,8	14 14	(1)	2,2		
558 185	7 Bootle	42 .5		57	¥5	3°,8 Y¹	4 ,51 4 ,65	487 <b>22</b> 9	273° +429	-15.7	71 67	(6)	3,7 7,9		+73
564 190	y Centauri 8171	43 .5		11	B2		3 ,53 3 ,71	- 42 - 3	234° + 42	+ 8,8	8	(4)	-1,9 1,6		+19
5 <b>66</b> 191	η Useso maj. 2027		+49	49	B3	1°,3 ₩	1, 91 2 ,21	- 57	260° +104	16	16 10	(4)	-3,1 2,3	66	+65
567 192	g Contaurl 9358		33	58	Мъ		4 .40 4 .43	† 12 † 12	220° + 71	+40,8	54	(2)	3,7	285	+26 +18
565 193	ا Contaurl 8172		-41	59	B2p	61.4	3 ,32 3 ,51	28 0	230 <sup>8</sup> + 28 288 <sup>8</sup>	+12,6	7 7 46	(1)	0,5	282 3 <del>24</del>	+70
572 200	ข Bootin 2564		+16	17	K5	6",4 0¥"	4 ,28 4 ,18 4 ,72	- 73 66	+ 76 230°	- 6,3	31 15	(3)	4,4	285	+27
577 210	k Centauri 9676 k Centauri		-32 -32	30	B5		4 ,86	- 0 17	+ 60 80°	+13,8	15	(4)	3.5	285	+27
578 211 584	9676		+34	57	Ma	6°,9	6 ,31	+ 4	- 16 212*	-43,6	10	(4)	0,6	29	+73
219	9496 h Centenri		<b>-31</b>	26	B5	0	4 ,91	+ 30	+ 32	+ 5,2	10	/-//	3,2	287	+29
221 589	10729 1 Dracoms		+65	13	Ма	7°.2	4 ,91	+ 4	+ 28	-10,7	- 8	(6)	2,0 0,7	78	+51
226 1593	963 Centauri	49 ,3		48	Вар	7°,2 0Y	4 ,74 3 ,06	+ 2	- 3 230°	Var	8 16	(4)	-2,2 -0,5	_	+13
5231 1596	8949 # Bootla	L	+18	54	GO	3*,8	3 ,01	373	+ 82 190°	Ver.	15 105	(4)	2,6	334	+72
235 599	1785 Cantauri	50 ,4		11	Ko	Āħ	3 ,00 4 ,68	+306	+213 215°	- 0,2 +22,2	100	(1)		278	- 2
341 3602	3070 p Centauri	52 ,2	-41	36	<b>B</b> 3		4 .79	+ 18	+ 60 233°	+ 7.4		(1)		284	+18
348 3603	8329 v- Centauri	52 ,5	-44	19	Вз		4 ,17	46	+ 34 226°	+ 7	12	(2)		283	+16
5249 3610	9010 9 Centauri	55 ,4	-45	7	IF5		4 ,18	+ 2	+ 46 198°	Ver	12		2,5	283	+14
5260 3612 5264	9040 7 Virginia 2761	56 ,6	+ 3	2	A2	3°,0	4 ,57 4 ,34 4 ,51	+ 21 + 32 + 32	+ 35 141°	<u>- 1:</u> - 5	20 18	(5)	2,5 0,6 1,9	308	+58
3615 5267	β Centsuri 5365	56 ,8	-59	53	Bi	2,6	0 ,86	+ 8	219° + 40	Ver -12	18	(5)	-3,1 -1,1	279	+ 1
3621 5285	g Centauri 8405	59 .9	-40	42	В3		4 ,54 4 ,69	38 + 13	208° + 36	+12,1	9	(2)	-0,7 2,4	286	+19
3622 5287	# Hydrae 10095	0 ,7	-26	12	Ko	6° Y0	3 ,48 3 ,54	166 +149	165° + 73	+27.1	_	(3)	1,3 3,6	291	+33
3623 5288	Ø Centauri 9260	3, 0	-35	53	Кo	6",5	2 ,26 2 ,32	750 + 38	225° +750	+ 1,8		(4)	2,3 6,6	288	+23
3626 5291	a Draconis	1 ,7	+64	51	Aop	2°,1	3 ,64 3 ,84	- 54 3	286° + 54	Var 16,0	22	(3)		76	+51
3628 5297	Centeuri 7028		<b>-52</b>		Ko		4 ,78 4 ,90	189 — 23	235° +187	-17,0	18 18	(1)		283	+ 7
3633 5303	η Apodia 706		-80		A2p		4 ,97 5 ,06	+ 39	208° + 79	Var - 9			4,7	273	-20
3635 5304	d Bootla 2737		+25		F5	A.'8	4 ,82 5 ,00	76 + 60	198° + 47	Var + 9,8	$\overline{}$	(3)	4,2		+70
3639 5313	Virginia 2867	7.2	+ 2	53	Aop	2*,4 W	4 ,90 5 ,18	60 - 3	+ 60	+ 3	12 12	(2)	0,3 3,8	314	+ 57
Bor	≈ 3577, 3578. A 1±	MATERIAL ST.	, top"												

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
3642 5315	× Vuguis 3878	7 <sup>tn</sup> ,6	- 9°48′	K0	6°,5 Y <sup>8</sup>	4 <sup>10</sup> ,31 4 30	130 96		- 4,0	35 31	(4)	1,8 4,9	302°	+46°
3649 5321	4 Ursae min 478	9,2	+78 1	K0	6°,3 OY2	5 ,00 4 ,95	38 - 11	313°	+10	17	(4)	1,0	84	+-39
3652 5328	21 Bootis 1782	9,9	+52 16		3°,5	6 ,61	67 + 43	140°	-23,2			3.7	62	+61
3654 5329	* Bootis 1782	9,9	+52 16	A.5	XG <sub>1</sub>	4,60 4,81	69 + 11	103°	14,9	26 26	(6)	1,5 3,6	62	<b>∓61</b>
3660 5338	Vuginis 3843	10 ,8	- 5 31	F5	4°,3 YG <sup>2</sup>	4 ,16 4 ,26	427 - 320		+11,5	37 36	(3)		307	+49
3661 5339	δ Octantis _ 557	10 ,9	-83 13	K2		4 ,14 4 ,28	93 44	+ 82	+ 5,0	19 19	(1)	4,0	273	-22
3662 5340	α Boots 2777	11 ,1		K0	4°.7 OY8	0 ,24 0 ,14	2282 +1369	+1826		138 115	(5)	7,0	344	+68
3667 5350	1300tis 178d		+51 50	A5	3°,9 Y1	4 ,78 4 ,98	169 - 74	+ 152	-17	26 26	(1)	1,9 5,9	61	+60
3666 _ 5351	λ .I3ootia 1949	12 ,6		A0	2°,6 W	4 ,26 4 ,43		+ 183	— S	31 29	(4)	1,5 6,1	52	+63
3668 5354	Lupi 9084	13 ,0		B3 ~		4 ,10 3 ,99	- 12 - 1	+ 12	+22	3 8	(1)	-0,5	286	+13
3670 5358	v Centaum 5984	13 ,3		B5 A2	20 0	4,41	- 32 - 32	+ 32	+ 4,6	8	(2)	-1,1 4,0 0,9	283 302	+ 4 +43
3672 5359 3673	l Virginis 4018 A Bootis		-12 55 +35 58	iΩo	3°,2 W	4 ,60 4 ,75 4 ,83	32 16	+ 2	Var.	18	(3)	2,1	28	+68
5361 3680	2468 10 Contauri		-37 26	Ao	5°,5	4 ,87	+ 1	16	-25,6 - 4		(3)	0,9	290	<del>+</del> 22
5367 3681	9336 20 Bools	15 ,0		Ko	6°,0	4 ,34	- 38 15	61	- 7.3	18	(2)	3,5	339	+65
5370 3682	2637 Centauri		-58 0	Go	A <sub>3</sub>	4 ,99	- 110 50	4- 110	+ 18,4	18	-	5.9	282	+ 2
5371 3688	6619 a Centauri		3 -39 3	B5		5,08	<u>- 39</u>	+ 32	+ 8,7			3,4	290	+19
5378 3689	9329 lt Hydrae	17		K2	6°7°	4 ,70		8-1- 48	+19,9	13	(3)	3,0	295	+30
5381 3692	9803 Bootie	18 .			Aa	4 ,91	49	+ 226 2 250°	Var	13	(2)	6,7	324	+60
5385 3692	2882 I300tis	18 ,	1	A0	2°,3 V <sup>2</sup> W	6,82	1	4± <u>- 71</u>		13	-	6,1	324	+60
5386 3699	2882 1 Lupi	19 ,				5 ,29 4 ,65	- 3	0 197	-17.7		-	5,8	288	+14
5395 3700	9322 74 Lupi	19 ,	 B  <b>44</b> 56	178		4 .49	2	All and the second	<u> </u>		(1)	1,9 -1,3	288	+14
5396 3704	9323 ## Bootis	21 ,	8 + 52 19	F8	4°,4	4 ,64	47	1 210°	-11,2			3,3	59	+ 59
5404 3707	1804 1 Hydrae	22 ,	4 29 3	- B8	2º	5,00	4		+ 6	68 11	(2)	0,2	295	+28
5407 3710	φ Viiginis	23 ,	0 - 1 47	Kõ	X2 5°,0	5 ,18	13	6+ 42 4 266° 2+ 113	- 9,4	36 36		3,1 2,8 5,6	314	+51
5409 3716	2957 o Lupi	25 ,	9 50 1	B2	χ	4 ,98 4 ,60 4 ,69	5		<b>- 2</b>	12	(1)	0,0	287	+ 9
3717	8831 Q Bootis 2628	27 ,	5 +30 49	Ko	5°,4 Ya	3 ,78 3 ,77	14		-13,8		(4)	0,8	14	+66
5429 3718	5 Ursae min	27 .	7 +76 8	K2	6°,4 Y3	4 ,37	2		+10,5		(2)	0,7	82	
5430 3722 5435	y Bootis	28,	+38 45	Fo	2º,9 YG¹	3,00	18	323°	-35	63 60	(4)	1,9	34	+65
U-102	nes 1652, 1654. Te d	au hi iosa	o physical st	· mtam /Al					021 - Bo	osa 36	92 Bi	nary, A	DS 92	47 6",4,

Hoss 3652, 3654 Is doubtless a physical system (ADS 9173) The dynamic parallax is 0",021 — Boss 3692 Binary, ADS 9247 6",4, 190° (1925). The fainter star is itself a binary, 0",2, 283° (1926). The close pair has a period of 40,5 years

						14 <sup>h</sup> .						
1	2	3	4	5	b	7	, A	ıj	10)	81   12	11   14	15
3724 5410	y Contauri	29 <sup>14</sup> ,2	- 41°43′	H3p A2p	3°,4	27,05 2,85	49	324*	u,	14 (1)	' En 201' ' 1,1	) 10°
3720	8917 a Hootis	30 .1	4 30 4L	10 kg	<b>(*,</b> 0)		22%	5ጸ"	1 162	41 (4)	. 25 12	) ten
5417	2536		40.0		γı	1,66	71 51	217   223°	(   1-44	40 14 <sup>1</sup> (2)	; υ, € - υ, € 286	1.9
3732 5453	9198 8019	31 24	49 O	115		4 ,14   4 ,J5	11 11	1 51	1 7 7 1	13:	2,7	,
3735	of Contauri	J2 .ll	i ~60 <b>25</b>	GO		0.33	36360	.181		771 (6)	4,5 484	, 1
5459 3735	54H3	32 ,8	 !⊸60-25	IK 5	5",0	1 ,70	41.2H 08ar	1 1950 281"	- 23.2	7H41	N, I 0, 2, 2, 14	- 1
5460	5483	3- 1"		***,		1 ,61	31,48	1 1940	ı		9.6	•
3739 5463	a Circini 2977	14 4	-04 12	100		4 a41   4 a50	247 1- 152	185"	1 7.1	661 (1) 661	2, 1, 2M2 5, 1	6
3745	a Laud	15 .3	46 5H	112	3".5	2 80	15	1 * *	1 <b>1 7</b>	9: (4)	4, (490	FII
5169	9501					2 ,76		1 35		9	1 (1 (1	
3746 5470	и Ајкији Кој	35 14	-7H 17	K5		1 ,81	34   - 6		1 (1,4)	17   (1) 17	1.4	- 1H
3747	h Contauri	35 .7	- 37 21	11.3		4 (09	1. 44		1 4	11 (2)	10,7,294	4 20
5471 3749	griff al Boothi i	36 .0	 5 + 16 - 51	Au	27,4	) 4 ,26 ) 4 ,94	[+ 14   16	1 42		11 ;   16   (4)	A 4   DAN 544	4.61
5475	2768	On It	7 10 31	"	W	5 (1)	1 3		"	15	1,01	[""
3750	a <sup>a</sup> Dootia 8768	36 ,0	+16 31	V0	IS1	18, 7				1	1,2,444	4 61
5476 3752	¿ Dontie	36 .4	+14 9		jų.	5 .95   4 .84	61	116*	- a.	:   201 (7)	1,2 139	4 50
5477	2770		' ' '	A2	2",5	1	1 56	- 35	, "	19	1,11	
3752 5478	2 1 100tis 277()	36 14	+14		Ar	4 ,43	1				114 710	+ 59
3757	ol Centauri	37 .5	- 34 44	Ko		4 44	2017		- 18,7		1 296	4 21
5485	y868 # Virginia			   1/5	۱	4 ,10	F   7! 				5,7 2,2,315	1 47
3756 5467	3936	37 .1	5 5 13	1 23	4 .0 Y1	3 ,05	ir iii		ן די ויין	44 (4)   44	0.61	) 77
3759	co Contauri	38 ,4	\$ <b>—34</b> −46	Å0		1 4 .00	1. 10		~ 5	l f	4.5. 297	+21
5489 3761	9888 34 Booth	100 .0	  3.  -26. 57	Ma	6,0	1 5 ,15 1 6, 4 1	i++ 10	i' (I )   Lyqa	+ 5.2	7 (3)	4,000 -081-5	+63
5490	8413				Oa	4 .91	4 0	(1 11		7	1.8	
3770 5502	u 13ootis 2780	40 /	+17 23	Ko	57.6 OY*	4,69	4 30	1 221°	- 6'9	- 17 (2) / 17	0,81345 4,31	14-60
3771	# Hooth	40 ,6	+27 30	ΛO		3 .12		]	- 18,8	( "F	1,81 7	+63
3505	2417 a Bootis	40	N 1 0P 20	120	4°.3	1	1 4		1 44			1.44
3771 5506	2417	יי פיין	# <del>+27 3</del> 0	Ro	OXa	2 .70	49		- 15,4	23 (6) 22	-00 7	+63
3772	109 Virginis	41 8	2 + 2 19	A0	27.7	3 .76	136	1	- 9	24 (3)	0.6 323	14-51
_5511 3781	2862 38 Hydrae	44 .	5 -27 32	K2	7.	3 .98	1- 40 1- 25	1 " " " "	- 9.9	' 23 - 24 (2)	4,2 2,2 '301	+ 27
5526	10073		7	1	Q4	4 ,62	- 13	1+ 212		33	66	,
3783 5528	o Jaipi 9391	45 .	1 -43 9	11.5		4 .49		) 335° (4 50	+ 7,0		0,1 2493  - jo	+ 14
3784	a Libras	45 .	2 -15 35	1.5	3*	1 3 .33			  ⊷24,1	13 100 (1)	. 4	+ 37
5530	3965	,.		1	Kı	5 .43	<b>-</b> 2	2   12%		100	1 39	
3787 5531	a Librae 3966	13 ,	3 - 15 38	EA	3.0 3.0	1 2 ,90 10, 10	12	8 231° 8 + 127	10	47 (1) 47	1,3 308 3 4 '	+ 37
3798	# Bootis	46 ,	B +19 31	G 5	5.3	4 ,80	16	129*	+ 4,2	115 (8)	4,5 352	+60
\$544 3809	2870 // Urses mis.	14	Q +74 34	   K5	I Š	4 .72	{+ 15 3		+16,9	104 :	5.71	) (14.48)
3563	595	]"	7/7 31	J	ΟΫ́			2+ 17		29 (4)	0.3 79 -0.4	+40
3814	10 Libras	52 ,	0 - 3 56	Fo	3,3	4 .59			+24	1 32 , (3)		+45
5570 <b>3</b> 0	3696 ee 3749, 1750, This	j maje /A	i Daanaa b ∼		operates)			6+ 184		32	, 6,0} -aran — 1	 9460
Wellhoom	a binary ADB 9343	Dysu	ale peralles o	OLL P	red 130	yanga Mar		of the orbit	factive ty - bearing	at that of a		100

14h to 15h.

					14"	to 10".					<del>, , , , , , , , , , , , , , , ,</del>			
1	2	3	1	5	6	7	8	9	10	11	12	13	11	15
3815 5571	β Lupı 9853	52 <sup>m</sup> ,0	-42°44′	В2р		2 <sup>m</sup> ,81 3 ,02	69 5	223° + 69	0	14	(4)	1,5   2,0		+13°
3818 5576	и Centaum 9342	52 ,7	-41 42	В3	4º,5	3 ,35 3 ,55	36  - 7	208° + 35	+ 9,1	9	(4)	1,9 1,2	295	- <del> -</del> 14
3825 5586	δ Librae 3938		- 8 7	Ao		4,84 5,16,3	69 - 39	261° + 57	Vai 45,0	14 14	(1)	0,6 4,0		-1-41
3827 5589	Uisae min 878	56 ,0	+66 20	Mb	7°,1 O <sup>2</sup>	4 ,86 4 ,79	+ 82 + 8	293°	Var + 6.8	8	(4)	-0,6 4,4		- <del> -</del> 46
3834 5600	ω Bootis 2861	_	+25 24	K5	6°,4 OY8	4 ,93 5 ,09	+ 52 + 52	187° + 26	+13.5	13	(1)	3,8	3	4-59 4-48
3835 5601	110 Virginis 2905		+ 2 28	K0	5°,8	4 ,62 4 ,64	- 30 - 30	268° + 40 227°	-16.7 -19.9	16 16 21	(4)	3,1 0,1	327	+ 59
3836   5602   3837	# Bootis 2840 a Libiao		+40 47 -24 53	G5 Mb	4°,9 Y <sup>2</sup> 7°	3 ,63 3 ,68 3 ,41	63 + 43	+ 46 234°	- 4,0	20	(2)	2,6	305	+28
5603 3838	11834 7 Lupi )	58 ,2 58 ,3		-B5	,Ö <sub>8</sub>	3 .50	- 23 40	+ 91 215°	+16	24	(22)	3,3	293	+ 9
5605 3838	9773 π Lupi	1	-46 40	Ko		4 .85	1 19	+ 40 118°	- 3,1	10	(2)	2,7	293	+ 9
5606 3842	9773 y Bootis	ľ	+27 20	Ko	5°,9	4 .95	+ 19 178	3 264°	26,2	10 16	(3)	1,2 0,7		+ 59
5616 3847	2447 1 Bootis	., o ً	+48 3	Go	Y9,5	4 ,63	387	+174   274°	25,6	16 76	(ō)	5.9 4.2	46	<del>+</del> 56
5618 3852	2259 7 Lupi	2 ,	-44 54	В3	Y <sub>3</sub>	4 ,39	+_39 31 - 7	+383 230° -1 30	+18	75	(2)	7.9 1.4 1.8	294	+10
5626 3862 5646	9889 ** Lupi 9704	5 ,0	-48 21	139		4 ,45 4 ,14 4 ,25	121 - 44	237°	+ 3.	29 29	(1)		293	+ 7
3863 5647	9704 ж <sup>3</sup> Lupi 9705	5 ,	0 48 22	AO	-	6 ,04	116	245°	0			6,3		+ 7
3864 5649	ζ Lupi 8830	5 ,	-51 43	Ko		3 ,50 3 ,66	127 - 46	- <u> -</u> 118		17 17	(1)	-0.4 4.0	)	4
3865 5651	e Lupi 9932	6				4 ,92 5 ,06	- 12	+ 49	+11		-/-	3,!		+11
3866 5652	ι Librao 4047	6,			2º-3 YG1	4 .82	+ 3	+ 61		13	(3)	3,0	311	
3871 5660	1 Lupt 11 813		5 -31 9	1		4 ,95 5 ,07 4 ,84	18 + 14	12				1,3		
3876 5666 3880	ε Circini 3544 β Circini	-	2 - 63   15	ĺ	1	4 ,95	+ 4	- - 8				-0,4		
5670 3879	5875		6 -68 1		4",3	4 ,28	+ !	十 178 7 249	Ι.	-	-	5,	283	-10
5671 3887	2383 d Bootis		5 +33 4		40,6	23, 23 3, 54	15	5 144	· 12,6		(4)	2,	4 20	+ 57
5681 3888	2561 μ Lupi	11		1 В8	Y	4 .36	5	9 212	+15	15	(2)	4, 0, 3,	2 295	5 -1- 7
5683 3890	9860 β Librae	11	,6 - 9	1 B8	2°,4		10		Vai -37	15 26 26	(1)	1-0,	2 320 8	+ 38
5685 3891	3935 f Lupi 11630	11	,7 -29 4	7 Ko	6°	4 ,43	2		— 3,:	1	(3)	O,	4 30	5 - 22
5686 3896 <b>56</b> 95	δ1 upi 9538	14	,8 -40 1	7 B2	30,5	I '	3 3	3   192 3  + 30	°  + 2	9	(2)	1	,8 306 ,0 [	
3901 5704	γ Circini 5908	15	,4 58 !	8 B5-F	8	4 ,54 4 ,64	}	3 193 5 + 40	°  -17	11	ı   ' '	2	,3 28 ,7	
3903 5705	φ <sup>1</sup> Lupi 10236	15	,5 -35	4 K5		3 .59 3 .6	5 !- 2	6 135	1	12	5	4	,6 30 ,3	1
	on 1929 Doubletil	22 a m	Source tealer	Ress 1	RAT Vis	mal hinary i	ADS 040	1) period:	205 Vears	The	compa	njon 6¤	4,1, 3‴	,38, 245°,

Boss 3838 Doubtful if a physical pair — Boss 3847 Visual binary (ADS 9491), period 205 years The companion 6m,1, 3",38, 245°,3 (1926) is Boss 3846 and has very near the same p m as the principal The dynamic parallex is 0",082

					:	ibh.								
1	2	3	4	5	6	7	li I	9	ţn	11	Iλ	111	14	Л
3905	# Lupi	15 <sup>in</sup> ,9	-44° 20'	133	3".5	5™.7·I	28	215 <sup>th</sup>	Var	н	(4)		2117'	1.10
5708	10066		20.00	١	ļ	1 .76	1 1	KL	1 45	- 1	4 -1	1 0,9		
3910 5712	9 <sup>8</sup> l upi 10103	10 '8	-36 70	113	ŀ	4 .69	,3N	#15"    -  -  -	'	13	(4)	4,5	1141	1 15
3921	k Lupi	18 ,8	-38 22	A <sub>0</sub>		4 .68	01	285"			i		(n)	1 14
5724	10289		J			4 ,81	17	1 40			ļ	lite	•	' ''
3926	μ <sup>®</sup> Bootle	20 ,7	1 37 44	Fo	3',0	4 ,47	(64)	A974	4 N,01	(f) (f)	(4)	ر الديام د د ا	47	i 55
5733 3027	2036 nt Itoothi	211 ,7	1 37 42	Ro	J	00,  - 00, 0	70     174	150    104*	0.4	1111		र्मातः नीत्र	47	1.55
5734	2617		1 (2) 1000	100	ųKr ∣	n ,83	Uff :	1 141	] ' '			7,8	-,	ניגון
3928	y Urano min	20 ,9	F72 11	A2	27,2	3.44	17.	115"	Vist	41	(4)	Liti	75	4 41
5735 3936	679 เ 1)กษณะโด	22 .7	1 59 19	Ku	W   5°.5	1 .41	"	1 17 .	] 3.93   10.9	44	1.43	~(1,7 (1,1)	59	
5744	1654	"	1 39 19	***	γï	1 37	7	ו לי' וי	1 1000	10	(4)	1.5	9.76	1 48
3940	#Coronua Hor.	23 .7	+29 27	Eop	31.1	1 ,72	I IVII	204"	43	[44]	(r <sub>1</sub> )	0,8	12	4 54
5747 3947	2670 • Friang, Aust	2. /		l i Ko	Att	1 ,KH	113	1154		30	4	5,1		
5771	3102	27 ,6	<b>−65</b> 59	""		4,31	75	164"    - 50	14,4	27 27	(1)	1, 1 : 4, 5	2116	- 9
3949	r <sup>a</sup> Houth	28 ,2	F41 14	Λ3	P.5	4 ,98	27	230°	24	211	(4)	1,4	12	1151
5774 3950	2611 9 Lupi	28 .5	40 50	<b>1</b> 3	Y(-1	5,20	1111	_404.4   30		191	4-1	3,1		
5770	9760	28 ,5	- 40 50	, ,,	47.5	3 .95	30  - 5	1 19	F 10 1		(3)	- 1,5 0,9	jot	4.11
3952	37 Librus	28 .7	~ 9 43	Kn	5'.7	4 .83	380	1104	445.5		(3)	1 40		+ 34
5777 3953	4171 # Coronna Bor	28 .9	+31 42	113	Y*	4.86   4.17	L3K9	()   224*	4/5	42		7,8		
5778	2750	30 13	מר ונידן	123	W	1 766	17	1 30	(6	12	(1)	(1,4 3,0)	17	+ 53
3954	d Lupl	29 ,0	-44 37	113	ĺ	4 ,84	39 (	180%	1 8	y	(1)	H <sub>e</sub>	199	+ #
5781 3959	10239 y Librus	29 .9	- 14 27	Ko	5".7	4 ,87 4 ,02	il 15	1 16   91"	*****	4	1-0	2,8	4 4	
5787	4237		11 0/	1 1117	ijΫŧ	4 (0)	+ 33	49	- <b>37</b> ,01	' 보니   기사	(3)	17 S	140	+ 32
3960	å Berpentin Ni San 1	34) '0	140 53	Fo	r.	5 .16	વસ [	2550	~14	1		3,1	145	F47
5788 3960	d Sernouth N	30 ,0	F10 53	Po	YG4 3'.4	5 .40 4 .24	66	262*	18	700	(12)	40	144	) 
5789	2891	-	1 100 00	- "	W	4 .43	- 46	1 40	,	39 36	1141	1,1	345	+47
3961 5793	a Coronne Bor 2512	30 ,5	+27 3	Au	2",1	3 (3)	194	1 22.2	+ 0.4	47		0.7	9	+ 53
3962	p Lilmae	30 .9	-27 48	Ка	W 7"	2 .53   3 .78		5H 241 <sup>4</sup>	- 14 1	47' 44'		1.1	110	3.00
5794	10464		<b>-,</b> (		QĂr	3 .80	- 4	1 9	34,7		(2)	~ 1.2	314	+20
3964 5797	# ไ.upl 10601	31 ,3	-42 14	K5		4 .37	171	391	- 4.4	23	(1)		301	+10
3973	r Librac	32 .6	-20 27	03	3*	4 .35 1 .80	- 16H	+ 32 ! 216°	Var .	21°   10°		5,5 1,2,	100	   <b>+ 20</b>
5812	11817	-,-,-			W	3 .99	- 3	F 41	0.1	101	1-,	1,9	<b>,</b> , , ,	7 40
3978 5820	10831	33 .5	-34 5	Ko		4 ,63	. 15	127*	~21,8:		(1)	0,9	306	+16
3980	g Lapi	34 ,3	-44 20	F5	! 	4 .69	15 124	2152	· 7 1	3#		0,5	300	+ 8
5825	10310					4 .75		+ 324		] }		7,2	300	Т .
3988 5833	Coronacilior )	35 ,6	+36 58		Br 4,	6 .00	26		-23	9	(4)	1 0,81	25	+ 52
3988	Coronas Bur,	35 .6	+36 58	138	2'.4	6 ,18 1 5 ,07	1 21	15	-28.6	9		3,1 ~0,2	25	+ 53
5834	9888				W	5 .25						ا هرون ۱۰۰۰		) T ) =
3990 5838	и Librae 4188	36 ,2	-19 21	K,	7,0 0Y4	4 ,96	459	318*	Var.	10	(2)		317	+ 27
3991	y Lupi	36 ,3	-34 2j	135	- I	4 ,82	- 55 40	121 <sup>6</sup> 3	- 4,9	12	(1)	8,3 D,2	107	+13
5839	10494					4 ,05	- 8	+ 48	+ B.5		(1)	3,3	an i	{
3994 5842	r Berpentis 3138	37 .1	+20 0	A2	2',4 W	4 ,49	91	332		13	(3)	0,1		+49
	5927 A wide physi	igal pajy	(AI)% 9826).	The false			+ 19   	+ 69   2=-1, 1*	17,4   46.41°	13    2101		( 4,3 ( =		i ma Tha

Boss 3237 A wide physical pair (ADS 9226). The fainter star is itself a history dw.,1.—7m,3, 1",41, 41",1 (1933,6). Pariet 234 years. To dynamic parallex of 10. is (7',022, — Boss 396) — ADS 9701 Dynamic parallex of ",022 — 0",011 — Boss 3961 Estimate blassy Pariet 1.335 day.

15h.

						,	.5 <sup>n</sup> ∙								
1	2	3	4		5	6	7	8	9	10	11	12	13	11	15
,998 ,849	y Coronae Bor 2722	38 <sup>m</sup> ,5	+26°3	37'	Ao	2°,6 YG1	3 <sup>m</sup> ,93 4 ,05	<b>10</b> 5		Va1 10,4	22 22	(6)	0,6 4,0	9°	+∙ 51 °
1001 1854	α Scrpentis 3088	39 ,3	+ 6 4	14	Ko	5°,3 Y8	2 ,75 2 ,84	- 40 12	_	+ 3,0	49	(5)	1,2	342	+42
1009	# Serpentis	41 ,6	+ 15 4	14	Λ2	2°,6 Y1	3 ,74 3 ,89	91 + 80	1 127°	<b>–</b> 7	25 25	(6)	0,7	354	+47
1010 1868	2911 7 Serpentis 3023	41 ,6	+74	10	Go	4'.4 Yis	4 ,42 4 ,57	244 - 100	129°	<b>⊸</b> 66,1	97 98	(4)	3,6 6,4	344	+43
1015 1879	% Serpentis	44 ,2	+18 2	27 -	K5	6',7 O8	4 ,28 4 ,19	+ 68	204°	-39,3	14	(4)	0,0 4,5	357	+47
1079 1016 1881	μ Serpentis	44 ,4	- 3	7	Ao	2º,8 W	3 ,63 3 ,80	92	252	11	29 29	(3)	0,9	333	+36
1018 3883	μ Lup1 10754	44 ,6	33 1	19	В9		4 ,11 4 ,27	- 29 -+ (	$9 198^{\circ}$ 6 + 28	Var	7 7	(1)	-1,7 1,4	309	<del>- -</del> 15
1019	b Scorpu 11131	45 ,0	-25 2	27	В3	2º W	4 .77 4 .93	43		-10	10	(3)	-0,2 2,9	314	+21
1024 5889	δ Coronae Bor 2737	45 ,4	+26 2	23	Ğ5	Y2 Y2	4 .73	110 + 5	222	-19,3	25 23	(4)	1,5	8	<del>- </del> -49
1026	s Serpentis	45,8	+ 4 4	47	A2	3°,2 W	3 ,75	130	66	9,8	37	(4)	1,6 4,4	341	+41
1030 5897	#Triang. Aust	46 ,3	-63	7	Fo	5",1	3,01	53	8 210° 0+538	+ 1.	90 90	(1)	2,8 6,7	289	- 8
1031 5899	Q Serpentis	46 ,9	-ĥ21 1	17	K.5	6",6 OYa	4 ,88 4 ,87	- 4	9 270		13 13	(3)	O, 5	i	1-47
1032 5901	и Cotonae Bot 2652	47 ,5	+35	59	Ko	5°,9 OY <sup>3,6</sup>	4 .77 4 .88	36 + 36	4 182' 4 + 7	-25,0	28 27	(5)	7,6	24	+49
4035 5903	ζ Uısao mm 527	47 ,6	+78	6	A2	2º,4 W	4 ,34 4 ,53	2 - 1		Var	25 25	(2)	1,3	79	<b>+</b> 36
1034 5904	A Scorpu 12 352	47 ,6	-25	2	B3	3°	4 ,66 4 ,83	- 3	4 200°	-12	9	(2)	-0,6 2,3	315	<b>-</b> 1-20
4039 5908	# Libiae	48 ,1	16 2	27	Ko	5°,2 Ya	4 ,34 4 ,32	15		+ 3,4			5,3	322	+27
4042 5914	χ Heiculis 2648	49 ,2	+42	44	Go <sup>*</sup>	4°,4 'Y <sup>2</sup>	4 ,61 4 ,76	76 - 70		-55,8	77	(5)	4,0 9,0	34	+49
4049 5925	[ Lupi 10826	50 ,5	-33 4	40 -	ĀO		5 ,37 5 ,52	5	6 157	-10		4-3	2,2	309	+14
4050 5926	ξ <sup>2</sup> Lup <sub>1</sub> 10826	50 ,5	-33 4	40	A0		5 ,73 5 ,88	5		-12	24	(a)	2,6 4,5	309	+14
4052 5928	q Scorps 11714	50 ,7	-28	55	В3	4º Y1	4 ,02 4 ,19	3		+ 2,8	9	(3)	-1,2 1,6	313	+17
4055 5933	γ Serpentis	51 ,8	- -15 !	59	F5	4°,4 Y2	3 ,86 3 ,99	133		+ 6,9	1 -	(5)	3,8	355	44
4059 5941	48 Libiae 4302	52 ,6	-13	59	Взр	-	4 ,68 4 ,88	3		_14	9	(1)	-0,6 2,3	324	- - 27
4062 5944	π Scorph 11228	52 ,8	25	50	В2	2°-3° YG1	3,00	3	9 <b>2</b> 03 5 + 39		11	(4)	-1,8 1,0	315	+19
4063 5947	s Coronae Bor 2558	53 ,4	+27	10	Kō -	5°,6 OY3	4 ,22 4 ,23	10		°-31,8		(3)	1,0	10	+48
4064 5948	η Lupi 10797	53 .4	-38	6	В3-		3 ,61 3 ,80	4	4 207 1 + 44	4 7	11 11	(2)	-1,2 1,8	307	+-10
4066 5953	δ Scorpii 4068	54 ,4	-22 :	20	Во	20-3° G1	2 ,54 2 ,77	4	1 198 9 + 40	-19,2		(3)	-2,3 0,6	318	+-22
3733	T Coronae Bot.	55 73	+26	13	Mb Nova		2,0 to 10,3	J	3 32 7 - 10	° – 5	1,5	(3)	-7.1 -2.4	10	+47
4072 5960	2765 Draconis 1793	55 ,4	+55	2	A5	3°,3	4 ,96 5 ,18	19		Var.	28 27	(2)	2,1 6,4	52	+46

Boss 4049, 4050 Binary: 11", 49° Certainly a physical system

15h to 16h.

<del></del>			<del></del>			10 10-		r				<del></del>			
1	2	3	4	5	6	7	- 8	9	10	11	12	11	14		11
4071	11 Normae	55 <sup>111</sup> ,4	-57°29'	Λ2		411,87	147	229°	·~ 18:		ļ		294°		⊣t"
5961	7500		40 #**	/3 /		4 ,96	57	-l-135			}	5.7			
4073 <b>5</b> 962	η Normae 10512	55 ,8	-48 57	G 5		4 ,74 4 ,86	30  - - 29	106° ~ 5	(l <sub>a.</sub> }	16	(1)	0.8	300	- 1.	ı
4076	Lupi	56 .8	~38 19	B5		4 .97	44	2170	0:	111	(2)		307	i India	111
5967	10832	30 10	30 17			5 ,13	7	4. 43	1/3	11	(2)	3,2		1	• • •
4080	Coronae Bor.	57 .4	+30 7	Ao	2",3	4 ,91	45	238°	Var.	14	(4)	0,6	15	- -	47
5971	2738	at. ** 1			W	5 ,20	-l· 17	+ 42		14		3,2			
4081 5972	π Scrpentis 2886	57 .9	+23 4	Λ2	2",4 W	4 ,82 5 ,06	17 12	25°	Var.	48	(3)	1.1		-+	40
4082	E Scorpii	58 ,9	-11 6		40 50	5 ,07	1.2	12	- 30,1	18		3,2		-1	28
5977	4237	"		330	$\Lambda_{a}$	5 ,16	1		i			,5,2	13211	Т	AB(1.7
4083	E Scorpli	58 ,9	-41 6	1,8	50,0	4 .77	71	241°	-33,6	12	(5)	2,0	328	14	2X
5978 4084	4237 ) 5 Normae	الينا		١. ـ	A3	4 ,86	- 32	4. 63		42		4,0			
5980	10625	59 .5	-44 54	АЗр		4 ,84 4 ,98	17	30	15,5	14	(a)	0,6	303	1	4
4089	v Horoulis	50 .6	-1-46 19	B9	2º,3	4 .64	- 7 89	16 140°	- - 5,5	11	(2)	0,9  ⊷0,2	30		47
5982	2142			-,	w	4 ,91	40	- 79	1. 313	l ii	(#/	4.4	117	7	7 7
4086	β <sup>1</sup> Scorpii )	59 ,6	-19 32	`	1"-2"	2,90	31	201 <sup>q</sup>	Var.	8	(4)	-2,6	321	1+	23
5984 4087	4307 {			134	G1 .	3 ,13	4- 5	4- 31	4.3	8		0.3			
5985	4307	59,0	-19 32		Va 1º	5 ,06 5 ,29	- 34 - 7	223°	4,3			·- (),4		1	22
4090	v Draconis	0.0	+58 50	F8	49,3	4 /11	458	1- 33 318°	   8,5	77	(4)	2.7	57	 	44
5986	_ 1608	l.	, , ,		Y1.5	4 ,22	72	- -452	"""	75	1.14	7.4	3,	Т	71.71
4091	# Lupi	0,0	-36 32	133		4 ,33	44	211	-1-15	10	(2)	- 0.7	308	-4	100
5987 4093	10642 ar Scorpii	1 ,0	-20 24	Tio.	an 0	1 48	- 4	-1- 41		10		2,4			
5993	4405	1,0	-20 24	B2	2",8 YG1	4 ,13 4 ,29	34 + 11	192° 32	8	9	(2)	1,1		+	21
4095	n) Scorpii	1,6	-20 36	Go	5",1	4 ,58	70	143°	- 5,2	12	(1)	1,8		يار	21
5997	1408				Y 1	4 .67	+ 64	+ 27	31~	12	\'''	3,8	Jac		
4108 6018	7 Coronae Bor. 2699	5 ,3	+36 45	ICO	5,4	4 ,94	325	349"	17,0		(6)	2,7	26	+	46
4109	δ¹ Apodlis	5 ,4	-78 27	"МЪ	Ϋ́ª	4 <sub>1</sub> 93 4 <sub>1</sub> 78	-312 42	-1- 94 207°		36		7.5		ŀ	
6020	1092	3 ,1	-/0 2/	MLD		4,90	1	-l· 42	12,0			2,9	280	-	20
4110	გგ Vboqja	5 .5	-78 25	IX 5		5 ,22	32	175°	10,2				280		20
6021 4112	1093			2		5 .32	+ 16	+ 27		, :		2.7		1	
6023	φ Herculis 2376	5 ,6	+45 12	B9p	2",5 W	4 ,26	32	221°	15.4	16	(3)	0,3	37	+	46
4116	"Scorpil	6.2	-19 12	Α	30	4 ,46	- 48 12	- <del> -</del> 165 189°		15		1.8			
6026	4332		., .,	**	13A#	6 ,67	- 'î	+ 12	•			1.7		+	22
4117	Scorpii	6,2	-19 12	B3	34	4 ,29	34	300°	Var.	12	(3)	n,5		- -	22
6027 4115	4333 J			^ 45 a	Ψ1	4 .34	+ 5	+ 34	- 6,5	11		1,9		•	
6028	10841	6 ,1	-27 40	B3	3° W	4 ,70 4 ,85	47 8	216°	ન- 9:	10	(3)	0,3	315	바	វេត្
4118	oTrining, Aust.	6 ,4	-63 26	Go	**	4 ,03	18	171°	   5,1	10	1	3,1		1	
6030	3854					4,16	+ 10	- - 15				0.3	291	_	£ Çi
4119 6031	ψ Scorpii	6,6	- 9 48	A2	2°,8	. 4 ,91	27	189°	7,9	18	(1)		330	- -	27
4134	4324 d Ophiuchi	0 1	- 3 26	3.5-	W	5 .11		-  25		18		2,1	,	'	
6056	3903	וני ע	- 5 ZO	Ma	6°,9	3 ,03 3 ,05	161	198°	19,9		(5)	0,5	337	+	31
4135	γ <sup>1</sup> Normae	9 ,6	-49 49	F8p		2 ,00	+ 47	- -155   236°	18,5	31	143	4.1			
6058	10474					5 ,12	- 4	+ 6	10,3		(1)	0.7	300	_	1
4143 6070	d Scorpil	12 ,1	-28 22	Αo	3" T	4 ,87	114	197°	-12,4			Ĭ !	317	4	14
4145	γ Normae	12 ,4	-49 55	- Ko	W	5 .08	+ 16	+113				5.2		Ĺ.	
6072	10 536	120 34	ככ עד־	WU		4 ,14 4 ,27	182 140	253° +116	-28,8			ارما	30 i	-	1
Box	4082, ADS 9909.	Wall at	worund binar	u with a	ı Lamente i		.70	- x 10			1	5,4		1	

Boss 4082, ADS 9909. Well observed binary with a period of 45 years. Dynamic parallax 6",045. — Boss 4066, 4067. Doubtiess a physical system. ADS 9913. — Boss 4093, 4095. Forms possibly a physical pair in spite of the differences in p. m., rad. vel. and parallax. — parallax 0",007.

Poss 4106, 4117. Probably a physical system. — Boss 4116, 4117. Probably a physical system (ADS 9951) 2",03, 49°,6 (1925,0). Dynamic

							16"								
1	2	3	4		5	6	7	8		10	11	12	13	11	15
147	4086	13 <sup>m</sup> ,0	4°	27'	ΙζΟ	5',1 Y <sup>2</sup>	3™,34 3_,39	86 -  48	68° - 71	9,8	31 30	(3)	3,0		+30° —
1 55 5081	o Scorpii 12849	14 ,6	-23	56	A3	$OX_1$ $Q_a$	4 ,76 4 ,92	42   5	199° + 42	- 8,5	16	(2)	0,6 2,9	320	+16
11 58 5084	σ Scorpπ 11485	15 ,1	25	21	B4	3° W	3 ,08 3 ,28	34 F 3	200° - - 34	V u - 3,2	9	(4)	-2,2 0,7	320	+16
F1 62 5092	7 Herculis 2169	16 ,7	4-46	33	B5	2º,4 W	3 ,91 4 ,13	32 20	338° + 25	-13,8	13	(1)	-0,5 1,4	40	- <del></del> -44
F1 63 5093	σ Sei pentis 3215	17 ,0	+ 1	16	Fo	3°.7 Y1	4 ,80 4 ,96	172 159	285°	-46	29 29	(5)		342	+32
1465 5095	7 Herculis 3086	17 .5	+19	23	Fo	3°,7 Y1	3,79	62	309°	-43	29	(5)	1,0 2,8	2	-+4ō
1166	& Iriang Aust	17 ,6	-69	52	GŌ		4 ,93	228	63°	Vai + 8,5			6,7	287	-15
5098 1168	2558 y Apodis	18 ,1	-78	40	ŢĶo_	-	3,90	141 - 79	237° +117	+ 5,1	20 20	(i)		280	-21
\$102 \$169	1103 © Coronae Bor	18 ,2	- <del>-</del> -31	7	Ιζο¯	5°,4 Y2	4 ,72	132 102	314°	-29,7	17	(5)	0,9		+43
5103 1170	2845 ψ Ophmehi	18 ,3	19	49	Ιζο	5°,4 Y <sup>2</sup>	4 ,84 4 ,59 4 ,58	66	196°	+ 0,2	13 13	(1)		323	7-19
5104 1173	<sup>4365</sup> <sup>1</sup> Coronao Bor	18 ,6	-+ 34	2	Mā	7',1 OY8	5 .36	49 + 49	174°	13,6	11	(i)	0,6	22	+43
5107 1175	2773 r <sup>2</sup> Coronae Boi	18 ,7	+33	56	IC 5	7",0 () Y <sup>0</sup>	5 ,28	55 - 55	- 4° - 3	-39,8	12	(1)	0,7	22	+43
5108 1180	2771 s Normae	19 ,8	-47	20	13 5	<u></u>	5 ,39 4 ,71 4 ,80	10	217°	Vai.	2	(1)	-3,8 -0,3	304	± 0 -
51 15 F1 82	10765 ω Herculis	20 ,8	+14	16	AOp	2º,9 W	4 ,53	79	146°	7 -	20 20	(3)	1	357	+37
5117 4183	χ Ophtuchi	21 ,2	-18	14	ВЗр	-3"- W	4 ,85 5 ,01	+ 78 31 + 10	188°	Va 8,1	8	(3)	-0,6 2,4	326	+20
5118 1189	υ Ophruchi	22 ,4	- 8	9	A2	2',8 W	4 ,68	84 - 76	276°	-30,8		(1)		334	-1-26
5129 4192	4243 η Diaconis	22 ,0	61	44	-G5	5°,1	2 ,89	62	343°	-14,2	1	(5)	0,9	59	+40
61 32 41 93	1591 at Scorps	23 ,	26	13	Ma A3	7°,2 OR	1 ,22	34	192°	Var - 3,0	1 15	(5)		320	14
6134 4198	11359 22 Scorpu	24 ,	-24	54	B3	20 T	4 ,87	28	188°		7 7	(3)		321	+14
6141 4200	12695 N Scorpii	24 ,	B -34	29	IB 3	. **	4 ,33	26	200°	Vat 0,4	6	(2)		3 14	-1- 8
6143 4201	g Herculis	25 ,	4 +42	6	Mb	7°.4	4 ,49 5 ,02	+ 1 28 + 8	130°		-	-(1)	1, 2,	7 33	+43
6146 4202	φ Ophiuchi	25 ,	<del>4</del> —16	23	Ľ.	5°,1	4,7-5,5 4 ,40 4 ,42	66 - 34	236°	-34,4				2 328	- <del>1</del> -20
6147 4204	β Herculis	25 ,	9 +21	42	Ko	5°,1	2 ,81	107	257°	25,8	27	I	0,: 3,	2 7	+39
6148 4203	2934 2 Ophiuchi	25 ,	9 + 2	12	Ao	2º,6 W	3 .85	- 31 97	210°	Var 15,9	25 20 15	(5)		3 344	-l-31
6149 4206	3118 ω Ophluchi	26 ,	2 -21	15	Fo	2º Y1	4 ,02	+ 9 33	39°	+ 2,5	24	(3)		5 324	+17
6153 4212	h Herculis	27	9 +11	42	K5	6°,9	4 ,69	+ 9 204	245°	+ 3,1		(4)	0,	9 355	-1-35
6159 4213	A Draconis	28	2 +68	59	B8p		4 ,91	79 42	325°		11	(4)		2 68	+37
6161 4215		28	8 -77	18	Ko	- X1	5 ,20 4 ,16	_ + 3   451	220	- 9,1 - 28,9	- 1		3,	282	<u>-20</u>
6163	1221	1	I		1	1	4 ,29	1-15	3  - -424	1	1	1	1 7	5	Ē

Boss 4173, 4175. Seem not to form a physical pair Have been included on basis of equally large parallaxes — Boss 4193 Antares

radial velocity undergoes slight changes which seem to be real. No variations in the light of this star have been discovered so far —

DBS 4203 Well known binary — ADS 10087 The period seems to be around 150 years. The dynamic parallax is 0",022—0",038

16h to 17h.

					10"	to 17".					
ı	а	3	-1	9	fi	7	1 8	ų v	10	11 14	11 15 13
4218 u165	7 Scorpil 11016	20°.7	2H°	1' No	T F	2º,91 3 .11	39	197"	1 14	40 (1)	110 112
4219 61 <b>6</b> 6	H Scorpil	29 .8	35	3 Ma	ĺ	4 .33	1 41	124"	1,2	- 10 - (1) - 10	0.7 114   1.7
1220 6168	a Horculia 2724	30 ,9	F-422 3	19 A O	25,6 W	1 .25	17 27	143"   25	ų		사 [14]
1225	idoulik(O )	31 ,7	-40 2	12   Ho	2',6	2,70	21	45"	20 1	H (4)	2.4 444 , [ 22
0175 4246	4350 g Horoulis	37 .5	131 4	  7   GO	4,4	19, K     3,91	1 1	110°	- 71	81 (6)   91   (6)	י ל <sub>י</sub> סי 1,7 20 קו
6212 4250	2864 a Triong Aust.	38 .1	68 ·	 	0.'8	3 ,13 1 ,88	388 32	1464 448″	3.4	88	(+1) (+1) 20)  16
6217	2822 v Hercalls					2.10	1 24	1 31		la .	H <sub>d</sub> fr
4255 6220	3029	39 .5	+39	7 Ko	Y.1	3 ,61 3 ,66	101	460 '	- H,0	17	1/0 %   1/0
4259 6223	g Draconis 1145	40 ,2	-1 64 4	7 10	Arr. 00	5 ,00 4 ,03	1 17	167°	1 (4.3)	설(1	1,0 62 (4-38
4263 6229	<i>ң</i> Атао 6906	41 .1	58 !	2 K 5		3 ,68 3 ,84	57 1- 46	144*	1 9.7	20 (1) 20	1,0 407 ~ 10
4270 6237	Druconbi 1702	43 ,4	F 56 ;	8 ј Го	4°,0	4 ,88 5 ,04	62  - 54	26" 10	0	11 (2) 31	4.5 12 pt 39
4272 6241	# Scorpii 11285	43 ,7	34	7 Ko	54.9	2 .30	667 520	248 <sup>4</sup> 1420	2,3		
4273 6243	20 Ophluchi 4394	44 .3	10 3	6 F5	4",0 Y1	4 .73	133 -1-110	1414	0.1		4.4 335 4 19
4277 6247	#1 Scorpii 11033	45 .1	<b>→37</b> 5	и изр	2",0	3 ,09	31	1944	Var ,	91 (4)	2,1 114 1+ 3
4281	#* Scorpil	45 ,6	<b>-37</b> 9	1 132		3 ,46 3 ,64	- 2    34	4 J1 214°	14	: 1) 1   7   (4)	17,5 } ,~2,1 314 pt 3
6252 4284	11037 52 Herenila	46 ,3	  -  46   1	0 A2p	2",8	3 ,92 4 ,86	40     76	163. <sup>5</sup>	1 0.8	7 (3)	7 1,1 1 1 0,6 38 +39
6254 4287	2220 č <sup>i</sup> Scorpli	47 .0	-42 1	2 H1p	w	\$ ,05 4 .88	1- 44   20	- ((4   1647	20	14	4.3.
6262 4292	11633 C* Scorpti					5 .02	111	+ 17		1	1,4
6271	11616			2 K5		3 .75 3 .82	266 - 51	207°	- 18,6	17 (1)	5,9
4302 6281	(Ophluchi 3092	49 ,3	+10 2	D B8	2",1 W	4 ,29 4 ,51	- 73 - 19	# 71	Var. 21	19 (3) 18	3,6 +29
4304 6285	7766	50 ,3	-55 5	0 165	7",5	3 ,US -	- 47	209 <sup>4</sup> + 46	- 6,1	21 (2) 21	1.4 300 - 9
4313 6295	10 37 9	51 ,6	- 53	0 K2		4 ,15		284 4	<b>+24</b> ,4	19 (1)	
4315 6299	a Ophluchi 3208	52 ,9	+93	a Ko	<b>\$</b> 7	\$ ,42 3 ,41	295 -236	2674 + 177	- \$6,2	39 (2)	1,3 356 +28
4322 6315	h Draconis 1157	55 ,4	4 65 1	7 F 5	3 <sub>2</sub> 7	4 ,82	252	79*	Ver.	37 64 (4)	5.8 3.9 62 +36
4323 6318	30 Ophluchi	55 ,8	<b></b> "4	4 Ko	6 .7 Y	4 ,96 5 ,00	<b>244</b>     103	55   211"	22,6 0,7	64     14   (3)	0,7,343 +21
4327	#215 # Urino min.	56 .2	8a f	2 65	5.6	4,08	16     15	4 103	Var.	14   7   (2)	5,1 1,4 52 +31
6322 4328	498 • Horoulie	56 ,5	<b>+ 31</b>	4 A0	Y1 27.7	4 .41 3 .92	14     31	6 295°	Ver.	7 24 (3)	0,1
6324 4334	k Scorpil	58 ,2	-33 !	9 Btp	W	4 ,14 4 ,87	- 24 i	+ 45   82°	-25,1 +10	24	2,5
6334 4346	11 706 60 Horoulis		+12 ·		24.6	5 ,03	+ 7	- 3 :		45.	-0.7
6355 4360	3142 5 Ophiuchi	,			YG1	4 ,91 _ 5 ,09 _ 6	+ 54	108°	- 3,2	19 (3) 19	3,6)
6378	4467		-15 3		3".3 W		+ 13	- 92	- 1,a	30 (3) 28	-0,1 334 + 12 2,5
_ Down	1346. Wellknown I	Mary -	- Boss 437	77. 43ML CH	rialoly o	okwiesi wel	r _ House	John Jan	l Dome		

Boss 4346. Wellinown binary — Boss 4377, 4281. Cartainly a physical pair — Boss 4387, 4398. Doos out smar to in a physical pair. — Boss 4315. Variable 428,1—328,0 photographic.

							17".									
1	2	3	1		5	6	7	8		9	10	44	12	13	14	15
4361 6380	η Scorpπ 11485	5m,0	-43°	6'	F2		3 <sup>m</sup> ,44 3 ,56		295 86	1750	-28,4			۳.0	312°	- 3°
4368	ζ Diaconis	8 ,5	+65	50	B5	20,2	3,22	<u>+</u> -	21	+ 283 327°		- 18	<b>(</b> 4 <u>)</u>	5,8 0,8	63	干35
<b>63</b> 96   <b>43</b> 70	1170 36 Ophruchi \	9.2	-26	27	1	W_ oʻ	3 .45 <u>-</u> 5 .33	+ - 12	6 235	+ 23 202°	- 0.2	16 158	(1)	0,1	326	<del>-</del> 6
_ 6401	12 026 36 Ophuchi			1	Ko	$\mathbf{Y}^{3}$	5,32	1	198	+1223				10.8		
4371 6402	12026	9 ,2	-26	27	1	<b>Да</b> Q,	5 ,29 5 ,28		224 208	203° +1200	<b>~ 0,</b> 6	158		6,3 10,7	326	Ŧ 6
4373 6406	al Herculis	10 ,1	+14	30	Mb	7°,0	3 ,32 3 ,52	_	30 25	336° - 17	- 32,6	9	(7)	-2.5	- 3	+27
4374	αº Herculis	10 ,1	114	30	G	50	5 .39		32	349°	- 38,0			-0,1	3	<del>-</del> -27
_ 6407   4376	3207 J 8 Herculis	10 ,9	+24	Š7	Λ2	BG <sup>2</sup> 2°,5	5_43_ 3_16	_	22 165	23 188°	Vai	38	(5)	2,8 1,1	14	- <del> -</del> 30
6410 4379	3221 41 Ophiuchi	11 ,5		20	K5	G1 5°.7	3 ,41		127 65	+_106 204°	-39 Vai	38		4,3	_	+ 19
6415	3255			]		Y's	4 ,82	-	6	+ 65	- 2,6	17	(4)	1,0 3,9	348	
4380 6417	ζ Apodis 3310	11 ,5	67	40	K2		4 .74		38 37	290° 6	-1-12,6			2,6	291	18
4381 <b>6</b> 418	τ Herculis 2844	11 ,6	+36	55	K 5	6°,0 Y3	3 ,36 3 ,32	+	25 14	265°	25.7	22 22	(4)	0,1	28	<del>-1</del> -33
4388	68 u Herculis	13,6	+-33	12	133	Ĩ°,9	Vai	ľ	24	237°	Var	5	(a)	0,3	23	+32
_ 6431 4391	2864 o Herculis	14 ,2	+37	24	Λ2	2°,2	5,01 — 5,5 4 ,80	+	17 66	1 17 323°	10	19	(2)	1,2	28	_ - <del> </del> -33
6436 4394	2864 & Ophiuchi	15 ,0	' '	4	F 5	G1 4º	4 ,89	-	22 315	+ 62 131°	- 9,2	19 65		_3,9		
6445	4731		1			Y1	4 .55		274	4- 151		03	(a)	7,0	331	+ 7
4395 <b>6</b> 446	Serpentis	15 ,2	-12	45	AO	3°,7 YG1	4 ,35	-	36 35	87° - 10	+ 7	21	(2)	1,0	338	+12
4399 6453	# Ophiuchi 13292	15 ,9	-24	54	1B 3	2º W	3 .37	-	31	182°	- 1	7 7	(3)	-2,4 0,9		<b>+</b> 5
4406	<i>β</i> А180	17,0	-55	26	K2	7°,0	2,80		36	204°	- 0,8	17	(2)	-1,1		-12
<b>6</b> 461 <b>4</b> 405	8100 y Aine	17 ,0	-56	_ <sub>17</sub> _	1B 1	2°,5	3,01	-	9 13		   4	17	(2)	0,6	_	12
<b>64</b> 62 <b>44</b> 19	8225	20 2	+37	14		36	3 ,67		34	十 _ 13 _	20	4	` '	-0,9 0,0		
<b>64</b> 84	2878				Αo	$\mathbb{R}^1$		+	8	+ 33				3,1		31
4419 6485	Q Herculis 2878	20 ,2	+37	14		2º,2 G1	4 ,52	+	38 15	264° + 35	-21	12	(4)	-1,0 2,4	1	+31
4420 6486	b Ophuchi 43337	20 ,3	-24	_5	Fo	3ª	4 ,28 4 ,41	+	132		-37,2	33 33	(2)	la i	330	+ 5
4421	d Ophiuchi	21 ,0	-29	47	F 5	4"	4 .37		157	173°	+ 37,8	33			324	+ 2
_ 6492 4423	43 557 Ophruchi	21 ,3	- 5	0	Fo	4°,0	4,47	+	44 104	+ 151 242°	Var	21	(3)	5,4 1,0	346	+15
6493 4425	d276 o Ophwehi		i + 4	 14	   Ko	<b>Y</b> 1,6 6°.4	4 .73	-	77	十 70	+ 0.4 -27.3	19 16		4,7		- <u>+</u> 19
6498	3422		'	_	]	Ya	4 ,40	+	2	4		16	(2)	-2,6		
4426 6500	8 Aras 6842	22 ,1	60	36	В8		3 ,79 3 ,94	_	102 43	213° + 93	+12	27	(1)	3,8	298	-16
4429 6508	v Scorpii 11 638	24 ,0	-37	13	В3	20,3	2 ,80		42	183°	Vai. +18	10 10	(3)		319	3
4431	A Alao	24 ,1	-49	48	Взр	3°.7	3,01	15	90	201°	Var,	21	(3)	-0,5	308	-10
6510	11511 Nov Ophluchi	24 .0	 5  <b>21</b>	24	Nov		3,16 -4to15	7	2.2	十87	_ 2,2	20		2,7		+ 5
6595	c <sup>2</sup> Ophluchi			_		3°		-	40	178°	-12	20	101			<u> </u>
<b>4434</b> <b>65</b> 19	13412	25 iš	-23	53	A.0	W	4 ,89 5 ,04	+	38	+ 37	-12	38	(a)	2,8	330	+ 4
n.	- 1000 1001 C	al-Tan a	£lana.					*		a .at			-21 - 4 -	**		

174

							17h.								
1	2	3	4		3	Ú	y	U	9	111	11	14	13	14	13
4438 6526	2 Herculia 3034	26 <sup>m</sup> .7	-  26°	11'	Ko	(7,3 () <sup>0</sup>	4°,48 4 ,51	21 - 4	45° 21	- 26,8	21 '	(5)	1,1	176	+ 27°
4439 6527	λ Scoupii 116/3	26 ,H	37	2	112	3",0	1 .71 1 .99	36   1	186°   36	Var	14 12	( i)	(1,9 (0,5)		<b>-  </b>
4443 6536	# Diaconia 2065	28 ,2	4 52	23	(rt)	Z",()	2 .99 3 .08	16	397"   11	~ 20,9	N 7	(1)	3,8 1 0	40	1 32
4445 6537	и Arus 11 <b>6</b> 61	28 ,3	- 46	<b>2</b> 6	Au I		4 .01 4 .72	56 35	326°   44	1 4	٠		4.4	112	9
4450 6546	Q Scorpii 12044	29,6		34 (	Ko		4 .17	210 <u> </u>   6	185° [ 216	49,2	201 <sub>1</sub> 201 <sub>1</sub>	(1)	0,8  6,0		•
4437 6553	# Henryll 12312	30 ,1	-42	56	ko	4".7	3 ,74	12	160°   11	1 1.4	1		2,6	114	7
4458 . 6554	# Draconia   1914	30 ,2	"	15	Λ5	3,'à	4 ,9H 5 ,1H	158	73"	14,2	30 · 2N ·	(5)	6,0	50)	H
4400 6555	1945	30 ,3	1	(A	ΛS	27,0 Yi	4 .9% 5 .16	165 -165	7.1"  - 5	Vor 17			1,2 (i, t	Sa)	F33
4459 6556	r Ophlacki 3252	30 ,3		38	Λ5	27,5 W	2,14	262 十 189	144"	Var  -15	53	(4)	4.3		14 22
4462 6561	F Surpentis 4621	31 ,9		2()	A5	4",0 Yı	3 .64	34	312"   76	42 <sub>N</sub>	50	(1)	3,1	ļ., i	+ 7
4465 6567	بد Ophluoisi 4472 کا کا  32 ,4		3	118 175	3",6 \V	4 ,05	29	1H9*	18	9	(2)	1,7		+11	
4466 6569 4474	7 11 61 6 11 61 6 11 61 61 M	32 ,0		21	B2		4 .84 4 .96 2 .51	4 123 224	149° 4 169	+ 3.7		(4)	6.4	310	-11
6580 1475	12137 o Sorpontia		-12	59   40	A2	27,5	2 .76	_ 8	20(° - - 27 23(°	-10	7 20		3,3 143   149		- 6
6581 4476	4808 v Pavenis		-64	41	Ko	¥(†1	4 .55	- 62 50	4 65 188*	30	20 18	(1)	4.2		-19
6582 4479	3662 (Horoulin	36 .6		7	133	27.1	3 .77	- N	1 56	-	18	٠.	2, 1 - 3, K	39	+30
6588 4481	2349 58 Ophluoid	37 ,4	,	38	1/5	₩ 3"	4 .02	-  F	+ 1 230°	* 1140   E   1140	i	\JI	i-1.7	333	+ 3
6595 4483	4712 m Draconia	37 .5		48	I's	ซุเ   454	4 ,94	- 83 327	4 62 2*	Var	36	(4)	5,0 2,7	66	+32
6596	949 Ophlucki	38 .5	ļ ·	37	Ko	¥ι	4 ,99	- 52 158	_	-14,0 -12,2	36 33	(4)	7.4	-	+16
4492	3489 4 Beorpil	40 .0	'	5	Fip"	9°.5 21 4°.4	3,01	- dy	- 137 50°	-26.7	32 7	(1)	3.0		- 7
4493	11838 X Bagittarii	41 ,3	-27	48	F8	34	3 .27 Var.	+ 3	- 2 1934		7	(1)	-3.9	328	_ 1
6616 4497	11930 # Herculis	42 ,5		47	Gş	Y	4,4-5,0 3 ,48		+ 23 203*	-16,1	102	(5)	3.5	20	+25
_602 <u>3</u> 4498	2888 Scorpii	42 .7	-31	40	B8	   Āæ	3 .59	- 90 24	+R11	13	100 6	(1)	8,0 -1.3		_ 4
6628 4500	14 609 y Ophiuold	42 ,9	1 2	45	Åο	2,2	4 ,98	+ 5	+ 24 199*	Var.	6 17	(3)	1.7 0.7		+14
4501	3403 O Scorpil	43 ,0	-37	4	k2	W   6°,3	4 ,00	18 68	+ 81 73*	1-24,6	13 28	(2)	3.3 0,5		- 6
4503 4503	11 907 1 Scorpit	43 .1	-40	4	A2p		3 .34 4 ,88	+ 64	- 23 160°	]	25		2,4	319	_ s
6631 4504 6036	41886	43 .7	+72	12		49.1	4 ,90	267	1768	-10,2	39	(6)	2,9	70	+31
4505 4637	# Draconia 805	43 .7	+72	12	F5	Ϋ́	6 ,07 6 ,13	279		10,3	39		7.0		  +31
	, בנים	1	I	- 1		1	6,13	ļ <b>5</b>	-274	I	į l		8,3	l	1

Ham 4401. Casheld variables maded 9.5 days.

17h to 18h.

						17	h to 18h.	•								
1	2	3	1		5	6	7		8	9	10	11	12	13	11	15
4519 6675	Scorpu 12201	49"',5	44°	19'	Ko		4 <sup>m</sup> ,98 5 ,02	_	28 22	232° - 18	+44,9			2,2	315°	-11°
4525 6682	Scorpu 12231	50 ,7	-41	42	Ma		4 ,89 4 ,93	_	33, 16 +	211° - 29	+ 4,4			2,5	318	-10
4531 6688	La Diaconis	51 ,8	+56	53	Кo	Z, '0	3 ,90 3 ,93	_	123 <sub> </sub> 101 -	52°	-25,2	29 <b>29</b>	(5)	0,9		+29
1535 6695	# Herculis	52,8	+37	16	Ko	5",6 Y <sup>a</sup>	3 ,99 3 ,97	_	6, 5 <sub>1</sub> -t	45°	-28,1	11 8	(7)	1,5 -2,1		- -25
1536 6698	1 Ophiuchi 1632	53 ,5	- 9	46	K0	5',1 Y <sup>2</sup>	3 ,50 3 ,52		118	186°	+12,7	22 20	(3)	0,2	345	+ 6 <sup>-</sup>
4537 6700	4 Sagittarii 13731	53 .7	-23	48	Ao	2' Y1	4 ,76 4 ,90		58 2 -	179° - 58	-22	8	(a)	-0,7 3,6		- 1
4538 6703	3156	53 ,9	+29	16	Кo	5°.4 'ya	3 ,82	4	90 89. –	107° -	- 1,8	26 26	(5)	0,7	22	+23
1541 6705	y Diaconis 2282	54 ,3	+51	30	K.5	6',5 O'Y3	2 ,42 2 ,47	+	27 <sub>1</sub>	197° - 26	27,2	33 30	(3)	0,2 -0,4	47	- <b> -29</b>
4542 6707	r Heroulis 3093	54 ,7	+30	11	1.0	3',8 Y1	4 ,48 4 ,67	_	6 3,-l	51°	-22,1	12	(3)	-4,0 -2,5	23	+22
1544 6710	ζ Scipentis 1217	55 ,2	3	41	10	3',9 Y1	4 ,60 4 ,72	+	153 144' {	111° - 52	-43	31 31	(2)	2,1 5,5	351	+- 8
4545 6712	66 Ophiuchu 3570	55 ,3	+ 4	23	B3	2',5 Y <sup>8</sup>	4 ,81 4 ,97		19, 7 -1	205°	Va1	8	(3)	-0.7	358	+12
4547 6713	93 Heroulis 3335	55 ,6	+16	46	Кo	5",9 W	4 ,71		12 6 -1	215° 10	-23,0	11	(4)	-0,1 0,1	10	+17
4548 6714	67 Ophiuchi 3458	55 ,6	+ 2	56	В5р	2°,9 W	3 ,92 4 ,14	+	14 2-1	172°	- 4,4	5 4	(4)	-3,1 -0,4	357	+11
4552 6723	68 Ophtuchi 3560	56 ,7	+ 1	19	Λ2	3°,3 W	4 ,44 4 60	+	26 9 -	162° 25	Vai	20 20	(3)	0,9	356	+10~
4556 6729	95 Herculia   3280	57 ,3	+21	36	G5	3',9	5 ,21 5 ,28	4	30 11 -	27°	30,9	8 8	(1)	-0,3 2,6	15	+19
4557 6730	95 Herculis 3280	57 ,2	+21	36	A3	G1	5 ,13 5 ,20	+	30 11 -	. 48	-27	14	(a)	0,8 2,5	15	+19
4559 6733	τ Ophiuchi 4549	57 ,6	- 8	11	773.0	4°,3 'Y¹	6,04	+	45 21 +	152° - 40	Var	18 18	(1)	2,3 4,3	348	+ 6
4559 6734	7 Ophiuchi 4549	57 ,6	- 8	11	Fo	4°,2 Y1	5 ,34 5 ,49							1,6	348	+ 6
4564 6742	W Sagitiann 14447	58 ,6	-29	35	F8p	Y2	Vai 4,3-5,1	+	15 9+	143° · 12	25.0				329	- 6
4565 6743	θ Αιπο 11720	58 ,8	-50	б	B1p		3 ,90 4 ,04	_	30 12 +	203° 28	+ 3	8	(2)	— 1,ნ 1,3	311	15
4566 6745	π Pavonis 4292	58 ,9	<b>63</b>	40	A.5		4 ,44 4 ,54	+	192 17+		-14.9	29	(a)	1.7 5.9	297	-21
4568 6746	y Sagittarli 15215	59 .4	30	26	Кo	5°.3	3,07		203 59 +	197° 195	+21,5	34 32	(3)	0,6 4,6	329	<b>–</b> 6
4571	70 Ophluchi	0,4	+ 2	31	Kο	5°.3 6°—7°	4,07		131	1678	- 7,2		(8)		358	+10
6752 4577	3482 Sagitlarii	1 ,8	-28	28	Кo	6°	4 ,10 4 ,66	+	238 + 37	153°	4,5	96			331	6 <sup>-</sup>
6766 4580	14174 71 Ophwchi		+ 8		G5	OY <sup>3</sup> 5°,6	4 ,64	+	16 + 25	33 0°	— 3,5	12	(2)	2,5 0,1	4	+12
_6770 4581	3582 72 Ophuchi		+ 9		A3	2°,8	4 ,78		0 103	25 323°	25	12 43	(3)	1.7	5	+13
_ 6771 4584	3564 o Holoulis	3,6	+28	45	A0	Y1 2°,2	3 ,95	-	_58 ~ 4	· 85 56°	27	43 24	(2)	3,8		+-20
6779 4588	2925 s Telescopii	[ [	-45		Кo	_w		+	41	205°	<b>-26.5</b>	24 11	(1)	-3,2 -0,2	315	14
6783	12251						4 ,71	-	18+	37		11	•	2,7		

Boss 4559. ADS 11005 Wellknown visual binary the period of which is around 224 years. The dynamic parallax is 0",028 — Boss 4564. Cepheld variable, period 7,6 days — Boss 4571 The components are 410,28 and 510,98 — Boss 4581 Light possibly variable.

18<sup>h</sup>.

1	2	3	4	_ 5	6	7	8	9	10	H	12	13	14	15
4590 6787	102 Herculis 3674	4™,4	+20°48′	В3	2º,0 W	4 <sup>m</sup> ,32 4 ,56	- 17 - 3	183° + 17	13,5	5	(1)	-2,2 0,5	15°	+17°
4591 6789	d Ursae min. 269	4 ,5	+86 37	ΛO	2°,3 W	4 ,44 4 ,66	52 19	22° + 48	- 8:	17 17	(2)	0,6 3,0	87	+28
4604 6812	μ Sagittarii 4908	7 ,8	-21 5	B8p	3°,7 Y1	4 ,01 4 ,20	6 + 4	141° + 5	Var. + 9.2	12	(a)	-0,6 -2,0	338	- 3
4617 6832	η Sagittarli 12423	10,9	-36 47	Mb	5°,2	3 ,16 3 ,24	216 145	219° +160	+ 0,1	20 20	(2)		324	-11
4619 <b>6</b> 84 <b>2</b>	Sugittarii 12684	11 ,8	-27 5	K 5	Os 8 <sub>0</sub>	4 ,69 4 ,66	10 + 8	53° - 5	16,9	11	(1)	-0,1 -0,3	333	- 7
4625 6855	ξ Pavonis 6140	14 ,0	-6i 33	K2		4 ,25 4 ,38	11 - 7	319° - 9	Var.	23 23	(1)		300	-21
4628 6859	å Sagittarii 14834	14 ,6	-29 52	Ko	6°-7° OY8	2 ,84 2 ,94	51 + 34	135° + 38	-20,0	28 28	(3)		331	~ 9
4635 <b>6</b> 866	74 Ophiuchi 3680	15,8	+ 3 20	G 5	5°,4 Y <sup>8</sup>	4 ,92 4 ,90	15 - 15	259°	+ 5,1	9	(2)	-0,3 0,8	Ö	+ 7
4636 6868	106 Herculis 3390	16 ,1	+21 55	IC 5	6°,1 Y <sup>8</sup>	4 ,98 4 ,97	62 - 15	171° 60	-32,0	11	(3)	0,2	17	+15
4638 6869	η Serpentis 4599	16 ,1	- 2 55	Ko	5°,6 ¥8	3 ,42 3 ,52	898 647	219° +620	+ 8,9	56 56	(5)		355	+ 4
4639 6872	и Lyrae 3094	16 ,4	+36 1	Ιζο	5°.7 Ya,s	4 ,34 4 ,41	38 + 36	325° + 12	-22,7	17	(4)	0,4	31	+20
4645 6879	≥ Sagittarii 12784	17,5	-34 26	AO	4°,5	1 ,95	139 - 51	198° +129	-11			2,7	327	-11
4650 6884		18 ,2	- 8 59	G 5	5°,4 YB	4 ,83 4 ,89	62 + 47	44° 40	Var. - 4,7	16 16	(4)		349	+ 1
4656 6895	109 Herculis 3411	19 ,4	+21 43	Ко	5°,4 Ya	3 ,92 3 ,98	324 + 55	144° +318	-58,2	35 31	(5)	1,4 6,5	18	+14
4655 6896	21 Sagittarii 5134	19 ,4	-20 35	Ko Ao	6°,2 OY <sup>3</sup>	4 ,96 4 ,92	23 + 7	158° + 22	-11,5	10	(E)		339	- 6
4657 <b>6</b> 897	α Telescopii 12379	19,6	-46 <b>1</b>	В3		3 .76 3 .88	53 15	191°	- 0,8	12 11	(3)	-1,0 2,4	316	-17
4662 6905	₹ Telescopii 12153	21 ,1	-49 7	Ko		4 ,14 4 ,28	294 +121	151° +268	-30,5	22 22	(1)		313	-18
4665 <b>69</b> 13	λ Sagittarii 13149	21 ,8	-25 29	Ko	6°	2 ,94	197 67	194° -+ 185	-43,2	58 31	(5)		335	- 7
4666 <b>6</b> 916	" Pavonis 5879	22 ,6	-62 20	В8		4 ,81 4 ,90	34 10	192° + 33	+59			2,5	300	-22
4670 6920	φ Draconis 889	22 ,2	+71 17	AOp	2°,2 W	4 ,24 4 ,46	32 + 8	353° + 31	Var. -16,8	12	(3)	-0,8 1,8	68	+28
4671 6923	b Draconis 1809	22 ,5	+58 45	A2	2°,7 W	4 ,85 5 ,14	64 + 43	329° + 47	Var. -12	26 25	(3)	1,8 3,9	55	+26
4672 6927	χ Draconis 839	22 ,9	+72 41	F8	4°,7 Y <sup>8</sup>	3 ,69 3 ,77	638 568	125°	+32,1		(4)	4,1	71	+28
4674 6930	y Scuti 5071	23 .5	-14 38	A3	2°,7 Y¹	4 .73	9 + 2	<del></del>	-51	19	(1)		345	- 4
4686 6945	42 Draconis 1271		+65 30	Ko	5°,6 Ya	4 ,99 4 ,96	104	105°	+33,2		^(3) <sup>-</sup>	1,3	63	+27
4689 6951	D Coronas Aust 13378	26 ,4	-42 23	G 5		4 ,69 4 ,76	47 + 36	125° + 30	-0,5	8	(1)	-0,8 3,0	320	-16
4705 6973	α Scuti 4638	29 ,8	- 8 19	Кo	6°,1 Ya	4 ,06 4 ,03	318 - 83	184° +308	+35,6		(4)		352	- 1
4707 6978	d Draconis 2113	30 ,9	+56 58	F8p	4º,8 Y1.6	4 ,95 5 ,03	11 + 1	202° — 11	-11,3	3	(1)	-2,7 0,2	53	+24
4709 6982	ζ Pavonis 2553	31 ,4	-71 31	Ко		4 ,10 4 ,24	155	184° +152	-16,9		(1)		290	26

18h.

						10 1								
1	2	3	4	ه	6	7	8	9	10	11	12	13	14	15
4722 7001	a Lyiac 3238	33 <sup>m</sup> ,6			1°,3 B1	0 <sup>m</sup> ,14 0 ,31	346 + 48	36° +343	-14,2	115 111	(4)	0,4	35°	
4725 7012	Pavonis 3948	35 ,7	-64 5	8 A2		4 ,90 4 ,98	1 14	182° 十141	+ 5			5,7	298	-25
4731 7020	8 Scuti 4796	36 ,8	9	9 Fo	4°,0 Y¹	4 ,74 4 ,83	14	107°	Vai 47.9	14 12	(2)		352	— 3 <sup>-</sup>
4734 7029	Sagittarii 12876	37 ,6	-35 4	5 B3	-	4 ,82	53	180° + 52	+ 2,8	14 14	(ĭ)		327	<u>-15</u>
4739 7039	φ Sagittarii 13170	39 ,4		6 338	3' YG1	3,30	48 + 47	91° + 12	Van 	16 16	(1)	-0,7	336	-12
4747 7051	<sup>1</sup> Ly1ae 3509	41 ,0		4	2º,8 Y <sup>8</sup>	5,06 5,30	52 + 32	10° + 41	31,2	18		1,3 3,6	37	+18
1748 7052	ε <sup>1</sup> Lyrae 3509	41,0	+39 3	4 A3	OR1	6,02	57 + 42	1° + 39	33,5	18	(1)	2,3 4,8	37	+18
4749 7053	3510	41 ,1	, , -	0 A5	2°,9 Y1	5,14 5,46		·	-15				37	<del>- -</del> 18 <sup>-</sup>
4749 7054	ε <sup>2</sup> Lyrae 3510	41 ,1		0	Ar	5 ,37, 5 ,69	64 + 36	14° 53	-16		-	4,4	37	+18
4752 7056	ζ¹ Lyıne 3222	41 ,3	' " "	0 Å3	3°,6	4 ,29	31	56° + 31	Var	30 30	(6)	1,7	35	+17
4752 7057	ζ <sup>2</sup> Ι-γιαο 3223	41,3			3°,0	5 .87	31	56° + 31			-	3,3 3,3	35	+17
4753 7061	110 Ilerculis 3926	41 ,4	ŕ		A.'0	4 ,26	345 -238	183° +248	- -22,2	65 65	(4)	3,3 6,9	18	-F 9
4756 7063	# Scuts 4582	41 ,9		1 Gō	Z, Z, S	4 ,47 4 ,56	25 16	205° + 19	Vat -20,9	10	(3)	0,8 1,5	356	2
4758 7064	Ly1ae 3349	42 ,0			5',7 'X8	4 ,92 5 ,11	29 - 29	27°	- 16,9	19 19	(2)	1,3 2,2	25	+11
4759 7066	13 Souts 4760	42 ,2		9 Kōï	O <sup>2</sup>	Vai 4,7-8,0		243° + 15	Var. 1-38,3	<del>-</del> 3	(a)	- 4,0	356	- 3
4761 7069	111 Herculis 3823	42 ,6	,	4 A3	2°,7	4 ,37 4 ,50	123 +113	- 48	Vat 46,7	38 36	(5)	2,2 4,8	16	+ 7
4762 7074	λ Pavonis 5983	43 ,0				4 ,42	- 17	235° + 8	+-20			0,8	301	-25
	Aquilae	43 ,8	0 2	Nova	Vai	-0,2 to	- <sup>18</sup>	194° +_16	13	3,1	(3)	-8,3 -3,9	0	= 1
4776 7106	β¹ Lyrao 3223	46 ,4	- -33 1	B21	Y16	Vai 3,4-4,1	- 8 - 8	152° + 3		8	(1)		30	+14
4778 7107	# Pavonis 3603	46 ,6	-67 2	1 F5p		Vai 3,8-5,2	- 17 - 4	335° - 16	十36,3	3	(a)		296	-26
4781 7116	r <sup>1</sup> Sagittarii 4907	48 ,1	22 5	2 G5	S",6 OY <sup>R</sup>	4 ,96 4 ,99	+ 3	158° + 18	11,6	a	(a)	0,5 1,3		-12
4784 7121	σ Sagitlarii 13595	49 ,1	-26 2	5   133	1°2°	2,14	- 66 7	173° -  65	10,7	16 16	(2)	- 1,8 1,2	337	-13
4790 7125	o Draconia 1925	49 ,7	-1-59 1	6 Ko	6°,1 Ya	4 ,78	86 68	74° -1 53	Vai - - 19,5	12 12	(5)	0,2 4,4	56	+23
4797 7133	113 Herculis 3524	50 ,5	- -22 3	2 G0 A3	4,9 Va		5 + 2	325° 5	23,8	18 14	(5)	0,3 1,9		+ 9
4799 7137	Diaconis 2686		+50 3		4°,9 Y <sup>8</sup>	4 ,97 5 ,08	33 - 16	178° 29	+ 8,2	10	(1)	0,0 2,6	48	+20
4800 7139	ა 1.yıaə 3319		-1-36 4		7°,0 O <sup>8</sup>	4 ,52 4 ,44	+ 9	307° - 4	26,6	7	(3)	-1,3 -0,5		+14
4802 7141	θ <sup>1</sup> Serpentis 3916	51 ,2	+ 4	4 A5	3°,0	4 ,50 4 ,89	53 + 52	59°	41	22 22	(2)	1,2 3,1	_5	- 1
4803 7142	3917	51 ,2	+ 4	4 A5	3°,0	5 ,37	48 + 48	68° + 1	42			2,1 3,8	<b>5</b>	- 1

Boss 4722 Has a variable radial velocity and might also vary in light Photoelectric methods have revealed a slight variation in the light (Gurinner) — Boss 4752 Zinner gives the combined magnitude 120,60 for this pair — Boss 4759 Irregular variable 420,5 to 910 — Boss 4778 Copield variable, period 9,1 days

## 4124 Appendices to Chap.4 K. Lumdhark Luminosities, Colours, Diameters, etc. of the Stars

					18	to 19h.								
1	2	3	4	5	6	7	6	9	10	11	12	13	14	15
4808 7149	η Scuti 4976	51 <sup>tt</sup> ,		1	5°,9 Y*	5 <sup>10</sup> ,04 5 ,00	71 + 50	117° + 50	-93,1			4.2	356°	
4809 7150	€¹ Sogittarii 5201	51 ,	-21 14	Кo	5°.7	3 ,61 3 ,60	37 + 27	120° + 26	20,1	23	(4)		342	-12
4810 7152	e Coronae Aust 13001	52 ,0	-37 14	15	_	4 .87 5 .04	161 148	235°	+53	24		1,5	327	<u>—19</u>
4814 7157	R Lyrae 3117	52 ,3	+43 49	МЬ	6º,6 OYª	4 ,32	77	+ 63	-27	8	(5)	5,9	41	+17
4823 7176	₹ Aquilao 3736	55 ,1	+14 56	Ko	5',6 Y	4 ,21	100	+ 70 220°	-51,6	21	(5)	3.8 0.8		  +40
4824 7178	у <b>Lyrao</b> 3286	55 ,2	+32 33	Aop	2°,9	3 ,30	- 97 8	+ 22 203 <sup>B</sup>	Var.	21 18	(5)	4,2 -0,5		+12
4825 7180	v Draconis	55 ,6	+71 10	Ko	6,1	4 .91	- 7 66	- 4 53°	Var	17	(1)	-2,2 0,5		+25
4830 7188	Coronae Aust	56 ,1	-42 14	_Ao-	- As	4 ,94	- 37 82	+ 55	- 7,2 - 7	13	_	4,0		-21
7189	Sagitherit	56 ,2	-13 18	Peo.		5 ,00 4.7-157	+ 44	+ 69		_		4,4		-10
4834 7193	Aquilao	56 ,3	- 5 53	Nova	5,0	4 ,15	48	220	-44,3	28	(5)	-,,	357	- 6
4832	4840 Sagittarii	56 ,3	<del>-30</del> 4	A2	3°,9	2 ,71	- 41 21	+ 25 270°	+22	28 43	(2)	2,6		_
7194 4847	16575 o Sagittarii	58 ,7	<del>-21</del> <u>53</u>	10	4",7	3 ,90	- 18 98	- 5 133*	+25,8	40	L.	-0,7	L	-17
7217 4851	y Coronae Aust.	59 .7	-37 12	ĎВ	4,0	3 ,86	+ 51	+ 84 161°	-51,0	28 65	(3)	3.8	342	-14
7226 4857	13048 r Sagittarii	0,7	-27 49	Ko	69	4 ,37	+ 27 267	+301 193*	Var		(a)	6.7	328	<b>-20</b>
7234 4858	13 564	0 ,8	+13 43	Ao	Ŏ¥9 2°,7	3,47	-125	+235	-45,7	40 39	(3)	5,6	337	-17
7235 4859	3899	0 ,9	- 5 a	Bo	YG1	3,26	- 69	186° + 74	Var -26	35 35	(5)	0.7 3,1	1 1	+ 2
7236 4862	4876 Coronge Aust	1 .3	-40 39	Ko .	W	3 ,55 3 ,72	93 - 55	195° + 75	-13	28 27	(2)	0,7 3,4	358	7
7242	13061 «Coronae Aust.		-38 4	_ I		4 ,66 4 ,69	49 + 24	136° + 43	+21,7	_		3,1	324	-21
7254	13350 Corongo Aust.			A2		4 ,12 4 ,35	136 + 56	141° +124	-18	19 19	(1)	0,5 4,8	327	-21
7259 4874	13146 # Sagittarii	3 ,1	<b>-39 30</b>	G 5		4 ,16 4 ,29	36 - 15	184° + 33	+ 2,9	9	(1)	-1,1 2,0	325	-22
7264 4891	5275	3 ,6	-21 11	F2	(4°,6) Ya	3 ,02 3 ,14	- 40 - 18	189° + 36	-10,2	17	(3)	-0,8 1,0	344	<del></del> 15
7292 4897	♥ Sagittarii 13866		-25 26	F5	A1	4 ,93 5 ,00	53 + 28	131° + 46	Ver 33.7		_		340	-17
7298	я Lyrae 3490		+38 58	B3	2°,1 W	4 ,46	- 3 - 3	180°	- 8.7	5	(3)	-2,1 -3,2	38	<del>+12</del>
4906 7306	3713		+21 13	29.5	2°,1 W	4 ,60 4 ,89	4	180°	-17.4	8	(2)	-0,3	22	+ 3
4909 7310	1129	12 ,5	+67 29	K <sub>0</sub>	5°,1	3 ,24 3 ,29	133	48°	+25,9	35	(4)	<u>-2,4</u>	65	+23
4912 7314	2 Lyras 3398	12 ,9	+37 57	K <sub>0</sub>	6°,0	4 ,46 4 ,48	10	+124 253°	-30,5	35 9	(6)	3,9 1,0	37	+11
4923 7328	и Судпі 2216	14 ,8	+53 11	Ko	5°,2 Ya	3,98	133	- 10 30°	-29,2	8 29	(5)	-0,5 1,2	52	+17
4929 7337		15 ,4	-44 39	B8		4 ,24	19	+130 183°	- 8	28 4	(1)	4,6 -2,8	321	-25
4932 7340		15 ,9	-18 2	A5	8*,8 YC1	3 .95	31		+ 3	43	(4)	0,6 2,1	348	-16
4934 7342		16 ,0		Bap	YG1	4 ,14	- 15  - 3	- 27 217°	+11,9	43		1,4		-15
	4814. Variable 410,0	i do dan i	i do she titir	182p	AG1	4 ,77	- 4 l	+ 3		1	Į.	1,9		

Boss 4814. Variable 4m,0 to 4m,5 in the RHP-system — Boss 4814 Binary, the components of which are each 5m,0 in the RHP-system.

19<sup>h</sup>.

<del></del>	2	3	4	5	6	7	8	9	10	11	12	13	14	15
4933 7343	// <sup>2</sup> Sagittarn <i>13171</i>	16 <sup>u</sup> ,0	-44° 59′	Fo		I™,51 4 ,52	125 - 84	1	<b>  22</b>	28	(a)	1,7 5,0	321°	-25°
4936 7348	α Sagittain 13215	17,0	-40 48	В8		1,11	129 — 13	168°	-1 1	26 25	(2)	1,1	325	24
4940 7352	7 Diaconis 857	17 .5	+73 10	Ko	6',0 OY2	4 ,63 4 ,53	176 + 171	309°	Vai 30, 1	16 16	(2)	0,7 5,8	72	1-24
4942 7358	3 Vulpeculae 3811		+26 F	В5	2',1 W	4 ,92 5 ,23	— 15 — 15	_	13,2	8	(3)	-0,6 0,8	27	- - 4
4948 7371	π Draconis 1345	20 ,2	+65 31	A2	2',7 W	4 ,63 4 ,82	45  - <del> -</del> 4	+ 45		19 19	(3)	1,0 2,9		- <b> - 21</b>
4949 1372	2 Cygni 3584	20 ,2		В3	1',9 W	4 ,86 5 ,08		+ 7	-23	4	(1)	2,1 0,4	30	- <del>-</del> - 5
4953   7377	δ Aquilae 3879	20 .5		FO	3°,9	3 ,44 3 ,65	265 + 254	74		59 58	(6)	2,3 5,6	7	- 7
4962 7387	Aquilae 4206	21 ,4		F0	4°,4 Y <sup>2</sup>	4 .86 4 .93	- 6	- 9		32 32	(1)	2,4 0,1 0,2	5	- 9 
14976 7405 4986	α Vulpeculae   3759   β <sup>1</sup> Cygni )		+24 28    +27 45	Ma Ko	б',9 ОҰ <sup>8</sup> 5",4	4 ,36 4 ,52 3 ,24	170 155	70		13 13 20	(5) (5)	5.5	30	+ 3
7417 4987	β <sup>a</sup> Cygni		+27 45	A0 B9	OY3 1	3 ,19 5 ,36	- <u>\$</u>	) _ 0		14	131	2,0 1,1	30	+ 3
7 118 4988	3411 ¿Cygni	Ì	+51 31	Λ2	B <sup>3</sup>	5,65	- 11 120	9 9	1	24	(4)	+1,1	52	- <del></del> 15
7420 4992	2605 8 Cygni		+34 14	В3	YG1 2°,4	4 .07		3 <u>+ 100</u>		19 6	(2)	4,4 1,3	35	4- 6
7426 4995	3590 μ Aquilae	29 ,2	+ 7 10	Кo	W 6°,3	4 ,97	262		° —22,9	22	(5)	2,1 1,3	12	- 7
_7429 _4998	4132 9 Vulpeculae	30 ,2	+19 33	В8	Y8 2°,0	4 .59 4 .88	1 4	BI+ 254 4 117	4	11	(2)	0,1	23	- 1
7437 4999	4063 h <sup>a</sup> Sagittarii	30 ,0	-25 6	-B9	4.	5,14	70		°19	12	-	2,1	342	-22
_7440 _5004	14 184 4 Aquilao	31 .6	5 — 1 31	В5	3°,1	4 ,82	1		°20	8 8	(2)	4.1	4	12
7447 5009	3782 a Diaconis 1053	32 ,	+69 29	ΚO	5°,2 Y <sup>2</sup>	4 ,59 4 ,78 4 ,79	184		4-26.6	163 163	(5)	-0,4 5,8 11,1	68	+22
7462 5014 7469	⊕ Cygni	33 .	8 +49 59	F5	3°,9	4 ,64 4 ,68	24 + 21	9 353	°-27,9	61 61	(4)	3,5 6,6	50	+ 13
5021 7478	φ Cygn1 3684	35,	5 +29 56	Ko	5°,3	4 ,79	3 + 3	5 355	+ 5.2	15	(4)	0,7	33	+ 3
5023 7479	a Sagittac	35 ,	6 +17 47	Go	5°,1 Y <sup>2</sup>	4 ,37	3	6 153 7 + 32		8	(4)		22	- 3
5027 7488	# Sagittae	36 .	6 +17 15	K0	5".7 Ya	4 ,45		8 178 0 + 24	<b>!</b> ]	15 15		2,3	1_	
5047 7 <b>5</b> 25		41 ,	5 +10 22		6",2 OY3	2 ,80	+	4 107 6 + _ 12	2   _	28 27		_ 1,5		
5048 7528	3234		9 +44 53		2°,4 Y¹	2 ,97	+ 1	0+ 6		37	1	4,0	1	
5052 7536	4240		9 + 18 17	A0	6°,7	3 ,78 3 ,83	+	-	5° Var 4	12		1,2 1,4		
7539	11 Vulpecula Nova 1670		5 +27 4			3,0-12	1 _		60 42				31	.
5058 7546	4254		5 +18 53		2°,3 YG¹	1,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	+ :	31 +	6° 17	24	1	2.4	F ] _	
5062 7557		45	,9 + 8 3	5 A.5	2º,4 Y1	0 ,89	1- 6		4° 26,1 2	16:		)   2,0   5,0		6 -10

Boss 5048 Visual binary ADS 12880 Has a period of some 500 years The dynamic parallax is 0",026-0",036.

19h to 20h.

<del></del>		_		<del></del>		10 20 -			<del></del>					
	2	3	4	5	6	7	8	9	10	11	12	13	14	15
5067	χ Cygni	46 <sup>11</sup> .7	+32°40	Md	7°.5	Var. 4 <sup>m</sup> ,2 to	91		0,5				37°	+ 2°
7564	3593			- Da	ORB	13 <sup>m</sup> ,2	- 67					4,0	   <u>-</u>	ļ. <u> </u>
5068 7565	12 Vulpeculae 3833	46 ,8	+22 21	В3	1°,5 W	4 ,91 5 ,12	- 29 - 8		-28:	7	(2)	-0,9 2,2	27	- 4
5071 7570	η Aquilae 4337	47 .4	+ 0 45	Gop	5°,1 Y <sup>2</sup>	3,5-4,7 3,8-4,5	12 + 1		<del>-14.8</del>	5	(3)		9	-14
5078 7581	Sagittarii 14 549	48 ,4	-42 8	Ko		4 ,21 4 ,26	53 + 30	10°	+36,2	20	(a)	0,7	325	-30
5079 7582	8 Draconts 1070	48 ,5	+70 1	Ko	5°,1 Y <sup>8</sup>	3 ,99	87	69°	+ 3,1	18 14	(5)	-0,3 3,7	70	+21
5084 7590	s Pavonis 2086	49 ,0	<b>-73 10</b>	Ao		4 ,10 4 ,22	149 + 10	152°	0:		~~~	5,0	289	-32
5086 7592	13 Vulpeculae 3820	49 ,2	+23 50	A0	2°,6 Y¹	4 ,50 4 ,73	+ 36	46°	-33	15 15	(2)	0,4	29	- 3
5089 7595	š Aquilae 4261	49 ,4	+ 8 12	ΙζΟ	5°,5	4 ,86 4 ,83	126	131°	-41,9	20	(5)	0,9 5,4	15	-11
5091 7597	ω Sagittarli 14637	49 .7	-26 34	G5	OAs	4 ,81 4 ,84	225 + 225	68°	-21,3	40	(1)		342	-26
5093 7602	β Aquilac 4357	50 ,4	+69	Ko	5°,1 OY8	3 ,90 3 ,86	484 — 305	176°	-40,0	81 80	(5)	3,4 7,3	14	-12
5095 7604	b Sagittarii 14 399	50 ,8	-27 26	K2	OYs 6°	4 ,62 4 ,61	19	164°	Var. -16,2	12	(2)		342	-27
5102 7613	22 Cygni 3817	<b>52</b> ,3	+38 13	В3	1°,8 W	4 ,87 5 ,11	<b>12</b>	211°		6	(4)	-1,2 0,3	41	+ 4
5103 7615	η Cygni 3798	52 ,6	+34 49	Ко	5°,1 Y <sup>3</sup>	4 ,03 4 ,03	52 38		-26,3	33 30	(5)	1,4 2,6	39	+ 3
5104 7618	A Sagittarii 14682	52 ,8	<b>-2</b> 6 28	G5	5° OYs	4 ,95 4 ,99	38 + 35	40°	Var. -48,6	8	(1)	-0,5 2,8	343	-27
5105 7619	ψ Cygni 2572	53 ,0	+52 10	A3	2°,5 W	4 ,80 5 ,06	- 51 - 3		-17:	13 12	(5)	0,2 3,3	53	+12
5108 7623	₱ Sagittarii  13831	53 ,2	<b>-3</b> 5 33	В3		4 ,39 4 ,55	47		+ 0,9	12 12	(1)	-0,2 2,7	332	-30
5118 7635	y Sagittae 4229	54 ,3	+19 13	K5	6°,5 O'Yª	3 .71 3 .75	62 + 44	75°	-34,1	20 19	(5)	0,1	25	— б
	Cygni	55 ,9	+53 21	Nova	Var.	1,5 to 16,5?			-17				55	+12
5129 7650	c Sagittarli 16355	56 ,5	-27 59	Mb	6°,7 OYa	4 ,60 4 ,59	+ 36	74° + 7	+11,5	13 13	(2)	0,2 2,4	341	-28
5131 7652	Sagittarii 13828	56 ,9		K5		4 .79 4 ,80	119 + 29	140° 十 115	-38,3	14 14	(1)	5,2	330	-31
5132 _7653	15 Vulpeculae 3587	57 ,0		A.5	3°,2 Y¹	4 ,74 4 ,92	52 十 19	+ 48	,5	26 26	(3)	1,8 3,3	33	- 2
5138 7665	ð Pavonis 3474		-66 26		7°,0	3 ,64 3 .79	1625 十 536	+1544		60 43	(3)	1,8 9,7	297	-33
5147 7673	ξ Telescopii 9794		-53 10			4 ,86 4 ,97	24 - 22	- 10	+36,9			1,8	313	-34
5153 7685	φ Draconis 1222		+67 35	1	6°,5 O <sup>B</sup>	4 ,66 4 ,66	+ 20	+ 47		18		1,1 3,2		+18
5170 7708	bi Cygni 3907		+36 33		2°,4 Y¹	4 ,82 5 ,13	+ 9	- 4	-13,6		,	1,3 -0,2		+ 🖻
5171 7710	∂ Aquilao 3911		- 1 7		2°,8 W	3 ,37 3 ,59		+ 19	-28,6		(3)	0,9	370	-18
5182 7724	Q Aquilae 4227		+14 54		2°,8 W	4 ,96 5 ,15		+ 15	-24,5		` '	1,3 4,3		-11
5186 7730	o¹ Cygni 2881	10 ,2	+46 31	A2	2°,5 YG <sup>3</sup>	4 ,96 5 ,07	17  - 14	123° + 10		15		0,7 1,1	50	+ 6

Boss 5071. Cophold variable; period 7,2 days.

20h.

1	2	3	1	5	6	7	8	9	10	11	12	13	11	15
5187 7735	o² Cygn1 2882	10 <sup>m</sup> ,5	+46°26′	Ko B8	6°,5 O²	3 <sup>m</sup> .95 3 .93	2 0	63° + 2	Var - 3.0	8	(4)	2,6 4,6	50°	+ 6°
5188 7736	b <sup>8</sup> Cygni 3955	10 ,8	+36 30	A0	2°,7	4 ,98 5 ,17	94	44° + 68	-22	16 15	(4)	0,9	43	ō
5190 7739	Vulpeculae 4165	11,0	+25 17	_B3	1º.9 W	4 ,82 5 ,04	4	236° 2	Vai	6	(2)	-1.3 $-2.2$	33	— б
5191 7740	33 Cygni 2376	11,1	+56 16	A3	3°,3	4 ,32 4 ,52	102 + 34	37° + 97	28,6	32 32	(1)	1,9		- - 11
5195 7744	23 Vulpeculae	11 ,7	<b>+ 27 30</b>	K5	6',5 Y <sup>8</sup>	4 ,73 4 ,69	43	278° - 27	+ 2,6	12	(1)	0, i 2, 9	35	5
5197 7747	а <sup>1</sup> Сарысови 5683	12 ,1	-12 49	Gop	5°,6 Y4	4 ,55	15 + 15	67°	-25.9	3 1	(3)	- 5,4 0,5	359	<b>2</b> 6_
5199 7750	ж Серћег 764	12 ,3	+77 25	В9	2°,4 Y1	4 ,40 4 ,61		25° + 28	22,6	14 14	(3)	0.1	77	+22
5200 7751	o <sup>2</sup> Cygni 3059	12 ,3	+47 24	Ko A3	6°,9 O²	4 ,16 4 ,15	5 0	68°	Vai	3	(2)	-1,3 $-2,3$	51	+ 6
5202 7754	α <sup>2</sup> Capμeoini 5685	12 ,5	-12 51	G 5	5°,5 Y <sup>8</sup>	3 ,77 3 ,85	58 + 50	85° + 30	+ 0,1	25 17	(6)	-0,1 2,6	359	26
5208 7763	P Cygni 3871	14 ,1	+37 43	B <sub>1</sub> p Nova	4°,1 Y <sup>3</sup>	4 ,88 5 ,07	16 - 10	227° - 12	- 7.9	-9 1	(2)	-5,1 0,9	44	1
5214 7773	y Capricorni 5642	15 ,1	13 4	Λ0 -	2°,5 W	4 ,84 5 ,00	18 - 4	158° + 17	- 2,8	18 18	(1)	1,1	359	-27
5215 7775	β <sup>1</sup> Capπeomi 5626	15 ,2	-15 6	B9	→1 <sup>0</sup> B2	6 ,16	45 + 36	87° + 22		17	(a)	2,3 4,4	357	-28
5216 7776	// <sup>3</sup> Capucoun 5629	15 ,4	-15 6	G <sub>0</sub>	5°,5	3 ,25 3 ,37	+ 29	88° + 19	Vai 19,0	20 16	(3)	0.7 1.0	357	<b>→28</b>
5223 7790	a Pavonis 9674	17 ,7	-57 3	В3	10,8	2 ,12 2 ,35	86 38	177° 十 77	- - 1,8	13 13	(2)	-2,3 1,8		<b>—36</b>
5229 7796	γ Cygni 4159	18,6	+39 56	F8p	4°,5 Y <sup>2</sup>	2 ,32 2 ,44	3	162°	- 5,4	6 5	(4)	-4,2 2,0	46	十 1
5235 7806	39 Cygni 4062	19 ,9	+31 52	K2	6°, 1	4 ,60 4 ,60	+ 41 + 3	93° + 41	- 13,9	15 15	(4)	0,5 2,7	40	- 4
5244 7822	ρ Capricorni 5689	_	-18 9	Fo	3º	4 ,96 5 ,09	26 24	213° + 9	+19	20 18	(4)	2.1	355	31
5255 _7834	41 Cygni 4057		+30 2	1.5	4°,2	4 ,09 4 ,24	- 10 - 2	114°	18,6	2 5	(4)	2,4 0,9		6
5265 7844	ω <sup>2</sup> Cygn1 3142		+48 37	133	14,8 W	4 ,89 5 ,10	+ 1	66° + 10	14.	5	(2)	-1.6 -0.1		<b>→38</b>
5268 7848	φ Pavonis 6402		-60 55	Fo		4 ,84 4 ,95	176 46	163° +171	-19		4-3-	6,1	303	37
5270 7850	## Copher 1821		+62 39	Ì	3°,3	4 ,28 4 ,42	- 49 - 42	112° + 26	Vai - 4,9	1	(2)	1,4 2,7	_	<del>+</del> 14
5272 7852	s Delphini 4321				2°,5	3 ,98 4 ,25	- 16	161° + 23	-18	5	(3)	2,5 1,2	24	18 
5279 7866	47 Cygni 4079		+34 54	A3	0°,8	4 ,85	14 14	188°	- 4,4	4	(2)	-2,1 0,6	<u> </u>	- 4
5281 7869	α Indi 13477		-47 38		40,3	3 ,40	+ 66	→ 30	- 1,8	30	(2)	2,5		—38 ———
5282 7871	\$ Delphini 4353		414 20		3°,0	4 ,69 4 ,83	38 + 24	+ 30	~24	21 20	(4)	2,6		-17 -47
5291 7882	β Delphini 4369		+14 15	\	4°,0 Y2	3 ,72	+ 25	十110	Var 22,9 Var	1	(6)	4,0		
5294 7884	l Aquilae 4016	1	2 - 1 27	1	5°,1 Y <sup>2</sup>	4 ,51 4 ,50	28 10	+ 26	- 5,8	1	(3)	1,8		25 13
5301 7891	29 Vulpeculae 4658	34 ,	1 +20 51	A0	2º,4 W	4 ,78 5 ,01	58 + 24	+ 53	<b>- 1</b> 6	12	(4)	3,6	32	13

Boss 5215, 5216 A wide pair. The bright star is a spectroscopic binary

206 to 214.

					20 <sup>b</sup>	to 21 <sup>h</sup> .								
1	2	3	4	3	6	7	8	9	10	11	12	13	14	15
5310 7906	a Delphini 4222	35 <sup>m</sup> ,0	+15°34	138	3'.3 Y1	3™,86 4 ,10	65 + 25	97° + 60		17 17	(3)	0,0 2,9	29°	16°
5315 7913	# Pavonia 3501		-66 34	.	4",9	3 ,60 3 ,75	49 - 31	286 - 38	+ 9,8	29	( <u>e</u> )	0.9	295	<b>-37</b>
5318 7920	η Indi 11752	36 ,7	-52 17			4 ,70 4 ,78	148 + 92	109°	- 2	34	(B)	2,4 5,6	314	-40
5320 7924	a Cygni 3541	38 ,0	+44 5		2',1 Y1	1 ,33 1 ,55	1 1	180°	Var 4	8	(2)	—4,1 —8,7	52	+ 2
5323 7928	∂ Delphini 4403		+14 4		4°,0 Y¹	4 ,53 4 ,63	56 - 55	204°	+ 8,3	20 18	(2)	0,8 3.3	28	<del>- 18</del>
5328 7936	w Capricorni 15018		-25 31		4" Y1	4 ,26 4 ,35	169 142	200° + 91		50 50	(1)	2.8 5.4	347	<b>—37</b>
5331 7942	52 Cygni 4167		+30 2		5°,6 Y*	4 ,34 4 ,40	27 + 20	329° 18		24 23	(6)	1,1 1,5	41	— B
5334 7947	7 Delphini 4255		+15 4		3°.5 BG®	5 ,47 5 ,84			- 7,4				30	-18
5335 7948	7 Delphini   4255		+15 4		5,4 0Y	4 ,49 4 ,86	207 -193	189° + 75		36 36	<u>(5)</u>	2 <sub>1</sub> 3 6,1	30	-18
5336 7949	4018	42 ,2			5°,5 ¥8	2,69	483 +362	48 +319		47 46	(6)	0,9 6,1	44	- 7 
5337 7950	Aquarii AAOO	42 ,3			3°,0	3 ,83 4 ,01	- 44 - 3	141' + 44	-15	28 28	(4)	1,1 3,0	6	- 32
5338 7951	k Aquarit 5378 & Yacki		- 5 2		7°,1	4 ,60 4 ,60	- <u>39</u>	189		15 15	(2)	0,5 2,6	_	- 29
5340 7952 5344	13718 Caphai		-46 3		-	4 ,90 5 ,02 4 ,63	+ 39	73 + 13	- 5,2		-/4	3,0	321	41 8
7955 5346	2240		+57 1		5°,0 Y4	4 .71	241 -178 826	196 161 7 8		57 56	(4)	3,4 6,5	62	T °
7957 5350	2050 1 Cygni			7 35	2°,4	3 ,59 3 ,58 4 ,47	+653	+512	-87.0	87 85 19	(4)	3,2 8,2 0,8	L.	s
7963 5352	4967	43 ,8		120	w	4 ,77	- 11 39	+ 3	-25 -14.5	18	(1)	-0,1	337	-40
7965 5361	14660 55 Cygni		+45 4		3°,0	5 ,01	- 21 5	+ 33 143	- 3,9	11	(2)	3,0		+ 1
7977 5363	3291 & Capricorni		-27 i		Y1 -	5 ,03	- 4 17	+ 2		3	(1)	-1,6		<del>-38</del>
7980 5367	15082 # Indi	47 ,0			Ó <b>Yª</b>	4 ,22	- 16 29	+ 6	- 4.7	13	(1)	0,4		-40
7986 5371	7788 μ Aquarli	47 3			4°.2	3 ,88	- 5 51	+ 28 133		18	(2)	1,0	L	-32
7990 5373	5598 31 Vulpeculae			3 G5	4°,2 X° 5°,4	4 .76	+ 4	+ 51	- 0,5	27	(4)	3,4		-12
<u>7995</u> 5375	4017 57 Cygni		, , , , , , , , , , , , , , , , , , ,	0 B3	1°,9	4 ,79	- 90 18	<b>– 52</b>		11	(2)	4,8 0,8	L	0
5393	8755 ν Cygni	53 ,4	+40 4	7 A0	2",8	4 ,91	+ 3 25		°-30	12	(2)	1,0 -1,4	51	- 3
8028 5402	7 Microscopii		-32 3		₹G¹	4 ,17	- 24 9		417,6	10	(1)	1,0 0,3	339	-42
<u>8039</u> 5410	16353 11 Cygnl	56 ,4	+47	8 B0p		4 ,75	+ 9	+ 2	Ver	10	(2)	<u>-0,5</u> -2,1	56	0
8047 5417	# Capricorni	58 ,	-20 1	5 A3	3°,1	5 ,01	+ 2	224	+24	21	(2)	1,5	356	-40
5427	6115	0 ,	3 - 17 3	8 Ao	2",0	5 .10 4 ,19	<u> </u>	129	<del>*</del> -10	21	(1)	3,8	359	-39
8075	6174 = 150 Daneb As	   Ma =	 Het —ladt	 	W	4 .34	+ 15	+104	 	21	1	4,3	1	1.1.1.

Box 5320. Doneb As the radial velocity is veriable in a way segmenting potentions this star should be tested for an eventual vertability in its light. — Box 5334, 5335. ADS 44279. Doubtions a physical pair. The dynamic parallex is 0",042.

 $21^{\rm h}$ 

1	2	3	4	5	6	7	8	9	10	11	12	13	11	15
5431	ς Cygni 3800		43° 32′	К5	0,'0	3'",92 3 ,88	7	117°	Var — 19,9	6	(3)	-2,2 - 1,9	5 ‡ °	- 2°
8079 5130 8080	A C upricorni 15235	. 1 ,3 -:	25 24	Ma	6"-7"	4 ,60 4 ,56	59	210°	+32,4	14 14	(2)	U,3 3,5	ა 50	41
5436 8089	- 13233 12 Cygm 3292	3,2+	47 15	K5	6',3 Y³	4 ,88 4 ,75	14	126° + 10	-26,5	9	(3)	-0,4 0,6	57	1
5441 8093	r Aquam 5538	4 ,1	11 47	Ko	5'.8 X	4 .52 4 .50	94	98°	11,8	29 30	(2)	1,9 4,4	б	37
5443 8097	y Isquulci 4732	5 ,5 +	9 44	rop	3',4 T	4 ,76	169 106	162°	-17,1	21 18	(6)	1,0 5,9	28	-25
5452 8115	ζ Cygnι 4348	8,7+	29 49	I/0	5',1 Ya	3 ,40 3 ,13	59 - 58	183° + 11	+17,0	17 17	(4)	-0,4 0,6	45	- 13
5455 8123	ბ Equulei 4746	9,6+	9 36	1.5	4",5 Y <sup>2</sup>	4 ,61 4 ,69	306 230	172° +202	-15,4	62 62	(7)	3,6 7,0	<b>2</b> 9	<b> 2</b> 6
5460 8130	z Cygni 4210	10 ,8 -		Fo	4',0 Y2	3 ,82 3 ,93	455 +441	20°	Var 22,0	48 48	(6)	2,2 7,1	51	— B
5461 8131	م Equulei 4635	10 ,8 -		F8 A3	4",6 Y1	4 ,11 4 ,18	- 101 - 37	117°	Vai 15,9	31 31	(5)	1,6 4,2	25	- 30
5464 8135	# Microscopii 16498	11 ,9 -		A0		4 ,79 4 ,92	66	121°	- 1			3,9	340	45
5467 8140	# Indi 10037	12 ,7		A5	21.4	4,60	+ 39 + 8	123°   131   220°	Var		( <del>1</del> )	5.3 4.3	310 - 52	44 7
5469 8143	6 Cygni 4431	13 ,5 + 13 ,8 +		Aop	3',1 'Y1 '2',5	4 ,28 4 ,47 4 ,42	- 6 29	- 5   136°	3,8 +- 6	-1 0 12	(2)	- 1,2 - 0,2	48	
5471 _8146 _5473	v Cygni 4371 V Microscopii	1	34 29 41 14	133p A2p	w	4 ,61	- 17 85	+ 23 90°	F 2	12	-	1,7	329	-46
_8151 _5480	14475 & Copher		62 10	A 5	20,8	5,06	+ 64	+ 56 1 72°	- 8	73	(5)	4,0	68	+ 9
8162 5484	2.111 Lapricoini		17 16	Ko	YG1 5",4	2 ,81	- 11 32	1-160 79°	- - - 11,2	73	(1)	3,6	_ <u>_</u>	42
8167 5489	6245 1 Pogasi	17 ,5 +		Ko	Za 20,10	4 29 4 24	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+ 18 60°	-76,3	16	(5)	6,3	38	22
8173 5493	4691 y Pavonis	18 ,2 -		F8	Ys .	4 ,23	+ 96	+ 70	30 1	28 129	(1)	4,6	295	-41
8181 5507	3918 & Capilcoini	21 ,0 -	22 51	G5p	5°_	4 ,43 3 ,86	+603 23	546 0°	+ 2	129	(2)	8,9 -3,1	354	-45
8204 5513	b Capricoini	23 ,0 -	22 15	G 5	¥26	3 92	+ 16	- 17 93°	-22,0		(2)		356	45
8213 5522	5692 2 Pegasi	25 ,5 +	23 12	IC 5	Y 9,8	4 ,61	+ 88	+ 98 103°	18,9		(5)	5,2 0,3	42	-20
8225 5527	4325 β Aquarii	26 ,3 -	6 1	Go	O'Ya 4°,6 'Ya	3 .07	17	+ 17   115°	-1- 6,8		į (4)	0,9 -3,4 -0,7	16	<u>~</u> 39
8232 5532	β Copher	27 ,4 -	-70 7	B1	2°,4	3 ,20 3 ,32 3 ,53	+ 4 12 0	+ 16 65° + 12	Va1 7,2	5 6 6	(5)	-2,8 -1,3	75	-F14
8238 \$543 8252	1173 g Cygni 3865	30 ,2 4	-45 9	Ko	5°,1 Y8	4 ,22 4 ,20	99	196°			(4)	0,7	58	<u></u> 5
5544 8254	r Octantis	30 ,4 -	-77 50	IÇ0		3 .74	234 140	169⁰	Var +32,1	31	(1)		281	-36
5546 8255	72 Cygni 4359	30 ,7 -	-38 5	Ko	€°,0	4 ,98 4 ,97	148 +105	52°			(5)	0,7	54	-11
5549 8260	P Capitcorni 0251	31 .5 -	-19 54	BSp	2-3° Y1		+ 4	104°	-25	7		-1,0 -0,8	0	
5551 8264	§ Aquarii 5701	32 ,4 -	- 8 18	A.5	3°,2 W	4 ,78 4 ,93	114 + 54	102° +100	-20	24 24		1,7 5,1		-41

Boss 5460 Wellknown binary = ADS 11787 The period in 49,2 years The bright star is a very short-period spectroscopic binary

21th to 22th.

					21	• to 223⁵	<u>.                                    </u>							
1	2	3	4	5	6	7	6	9	10	11	12	13	14	15
5562 8278	7 Capricorni 6340	34=,6	-17° 7′	Fop	3',9	3°,80 3 ,93	188 + 111		Var 31,2	15 15	(3)	-0,9 5,2		-46
5563 8279	9 Cephol 2169	35 2	+61 38	В2р	3",7 Y1	4 ,87 5 ,07	5	68°	-14.7	3	(3)	-4,7 -1,6	70	+ 7
5570 8288	x Capticorni 6152	37 ,1	-19 19	G 5	5',6 OY'	4 ,82 4 ,86	142		- 3,1	6	(2)	-1,3 5,6	2	-47
8296	Q Cygni	37 .8	+42 23	Pec. Nova		3,0-15,4	4			· ·		4,0	57	- 8
5580 8301	al Cygnl 3410	38 ,6	+50 44	В3	2',2 W	4 .78 4 .96	6		Var.	5	(3)	-1.7 -1.3	64	<b>– 2</b>
5582 8305	i Piecia Aust. 15734	39 ,0	-33 29	Ao		4 ,35	93 — 34	157°	+ 2	-	_	4,2	341	51
5584 8308	s Pognal 4891	39 .3	+ 9 25	Ko	6°,1	2 .54	25 + 12	92 8	+ 4.7	21 15	(5)	-1.6	34	<del>- 33</del>
5587 8309	μ¹ Cygni 4169	39 ,6	+28 18		4",1	4 ,73	350	132° + 333	+18,5	58 59	(5)	_0,5 3,6	49	19
5588 8310	μ Cygnl 4169	39 ,6	+28 18	F5	$\lambda_{\scriptscriptstyle I}$	6,08	325	130° + 309	+16,3	37		7,4 4,9 8,6	49	<del>- 19</del>
5590 8313	9 Pogusi 4582	39 ,8	+16 54	G 5	5',8 Y	4 ,52 4 ,49	— 13	143*	_ _22,3	11	(3)	-0,3 1,8	40	<b>—27</b>
5592 8315	и Родані 4403	40 ,1	+25 11	F5	4',0 Y	4 ,27	133 + 14	86*	-10,3	42 38	(8)	2,2 1,9	46	-22
5593 8316	μ Cephei 2316	40 ,4	+58 19	Ma	7'.9 OR	3.92-4.53 3.7-4.7		207*	Var +20,5	2 2	(i)	1,9	68	+ 4
5594 8317	11 Cephol 1193	40 ,5	+70 51	Ko	5 . 8 Y	4 ,85 4 ,76	153	51 + 147	-37.3	13 13	(5)	0,4 5,8	76	<del>+14</del>
5600 8322	6 Capricorni 5943	41 .5	-16 35	<b>A</b> 5	3°.7	2 ,98 3 ,18	392	139° + 388	Var. - 6,4	78 76	(4)	2,4 6,0		-47
5608 8334	7 Cephel 2288	42 ,6	+60 40	A2p	4°,4 Y1	4 ,46 4 ,58	+ 0	270	-23.7	12 11	(2)	-0,3 4,0	70	+ 6
5609 8335	n Cygni 3504	43 ,1	+48 51	В3	21,3 W	4 ,26 4 ,44	5	127°	<del>-19.</del>	5	(3)	-2,2 2,2	63	<b>⊢</b> _4
5617 8343	14 Pogasi 4525	45 .4	+29 43	Δo	21,6 W	5 ,00 5 ,30	39 - 18	134°	-22	10	(3)	-0,2 3,0	51	— 1B
5624 8353	y Gruis 14536	47 .9	<b>-37</b> 50	В8	34,7	3 ,16 3 ,37	111 + 65	98° + 90	- 2	18	(a)	-0,5 3,4	333	53
5635 8368	ð Indi 9733	51 ,1	-55 28	Po		4 ,56 4 ,63	59 + 19	114°	+15			3,4	306	49
5650 8383	VV Coplied 8007	53 ,8	+63 9	Map		4,9 to 5,6	9 + 7	311° 6	Ver,	5	(a)	317	73	+ 7
5654 8387	# In(i 10015	55 .7	<b>-57</b> 12	K5		4 .74 4 .85	4696 + 657	123° +4649	-40,4	267 265	(2)	6,8 13,0	303	<del>- 49</del>
5663 8402	o Aquarii 5681	58 ,1	- 2 38	135 p	2º,5 W	4 ,66 4 ,86	- 18 - 1	128 <sup>6</sup> + 18	+16.	13 13	(1)	0,2		<del>- 4</del> 3
5672 8411	አ Grale 14639	0 ,1	-40 2	K2		4 ,60 4 ,62	124 110	195	+40,0	17 17	(1)		329	— <u>-</u> 55
5674 8413	≠ Pegasi 4800	0,6	+ 4 34	K5	7',0 OY	4 ,90 4 ,97	144 + 138	50°	-17,2	13	(4)	0,5 5,7	34	<del> 39</del>
5676 8414	a Aquarii 4246	0 ,6	- 0 48	Go	4°,8 Y*	3 ,19 3 ,32	15 + 3	1130	+ 7,6		(3)	-2,3 -0,9	28	<b>-43</b>
5677 8417	# Cephel 1808	0,9	+64 8	G	5°,0 Y1	6 ,47	225	66				4,8 8,2		+ 7
5679 8417	# Cephel   1808	0 ,9	+64 8	<b>A</b> 3	A <sub>1</sub> '8	4 ,57	226 + 43	68° + 221	<b>– 6</b> ,0	53 47	(5)	2,9 6,3	73	+ 7
5680 8418	i Aquarii 6209	1,0	-14 21	B8	3°,0	4 ,35 4 ,54	70 24	149*	Var.	15 15	(1)	0,2 3,6		50
5684 8425	a Grids 14063	1 ,9	-47 27	B5	20,4	2 ,16 2 ,22	200	145° + 194	+12	31 30	(2)	-0.5 3,7	318	<b>— 53</b>
Boss	5677, 5679. Doubl	ilom a	ubwalesi nele	The	-						-4			١., .

Boss 5677, 5679. Doubtions a physical pair The dynamical parallex is 0",041 The combined magnitude is 4m,40 (RHP), 4m,40 (Zinema).

					-	421" •								
1	2	3	1 1	5	0 1	7	8	9	10	11	12	13	11	15
5688 8430	ι Pegası 4533	2™,4	+21° 51'	F5	3°,9	3 <sup>111</sup> ,96 4 ,03	299 -126	86°  - -272	4,3	78 78	(5)	3, F 6,3	51°	25°
5689 8431	μ Piscis Aust 15922	2,5	-33 29	A2		4 ,62 4 ,78	82 + 17	119° + 80	12			4,2	342	56
5703	v Pegasi	5 ,2	+ 5 42	^A2	20.7	3 ,70	276	83°	Var	26	(3)	0,7	36	39
-8450 5709	# Pegasi	5.5	+32 41	F5	₹V 4°,1	3 <u>.</u> 96_ 4 ,38	1-174 26	+215 209°	$\frac{-7}{+2}$	25	(5)	5,9 0,5	56	-19
8454	4352			Ko	6°,0	4 48	25 12	- 6 55°	-18,2	17	<del>-</del> (1)	$-\frac{1.5}{0.2}$	71	+ 2
5714 8465	ζ Cephei 2475		+57 42	KU	O <sup>2</sup>	3,61	+ 6	10		21	•	<u>— 1,0</u>	_	
5716 8468	24 Cepher		+71 51	G5	5°,5 Y <sup>2</sup>	4 ,99 _ 4 ,99	28 - 4	82° - - 28	- 15,0	5	(3)	-1,5 2,2	79	+13
5732 8485	I accitac 1711	9,6	+39 13	K2	6°,2 Y3	4 ,64 4 ,58	49 + 14	84°   47	- 10,8	11	(2)	-0,1 3,1	60	14
5733 8486	- μ <sup>1</sup> G1u15 14810	9,6	-41 51	Go		4 ,86 4 ,97	57  - 55	57°	- 7,2	6	(a)	-1,2 3,7	325	<b>— 56</b>
5742 8494	6 Cepher 2711	11 ,3	+56 33	F0	3º,6 Y¹ a	4 ,23	452 + 23	84° +452	- 1	56 50	(5)	2,7 7,5	71	<del>- -</del> 1
5746 8498	1 I accitae 4526	11 ,0	+37 15	¯K0	$X_3$ $Q_{G}, Q$	4 ,22 4 ,26	20 + 1	101	- 8,5	12 10	(5)	0,8 0,7	60	<del>-16</del>
5744 8499		11,6	- 8 17	Ko	5°,5	4 ,32 4 ,33	112 + 49	100° +101	14,7	14 13	(3)	-0,1 4,6		— 50 
5747 8502	α Lucanae 7561	11 .	—60 45	K2	54,4	2 ,91 3 ,12	87 - 75	249° 45	+45	36 36	(1)	0,7 2,6		<del>- 49</del>
5761 8518	γ Aquain 5741	16 ,.	5 – 1 53	Λo	2°,6	3 ,97 4 ,12	123 + 76	-86° 1-97	Vai 21	43 38	(2)	1,9 4,4		47
5762 8520	31 Pegası 4784	16 ,6	11 42	В3р	2°,2 W	4 ,93	+ 6	67°	+ 8	7	(a)	-0,9 -1,2	1	-37
5763 8522	32 Pegasi 4299	16 ,	7 +27 50	В8	2°,8 W	4 ,88 5 ,06	5 0	112°	+ 7	8	(1)	-0,6 -1,6		24
5764 8523	2 Laccitae 3894	16 ,	+46 2	B5	26,1 W	4 ,66	20	90°	Vai → 9,0	18 14	(3)	0,4	1	- 9
5776 8538	β Lacertae 3358	19 ,	6 +51 44	Ко	5°,6 Y3	4 ,58 4 ,56	190 190	184°	10,6	24 24	(5)	1,5 6,0		4
5777 8539	# Aquani 4872	20 ,	2 + 0 52	Вір	2°,9	4 ,64	13 + 10	85°	+ 4,4	6 6	(1)	1,5 0,4		46
5778 8540	δ Tucanae 4044	20 ,	2 -65 28	В9		4 ,80	67 + 46	81°	+12			3,9	291	47
5779 8541	4 Lacertae 3715	20 ,	4 -1-48 58	-В8р	3°, 1 W	4 ,64 4 ,80	14 12	216°	26,7			0,4	68	- 7
5790 8551	35 Pegasi 4710	22 ,	8 + 4 12	ко	5°,0 Y8	4 ,93 4 ,90	325 - 23	167° +231	+54,0	25 25	(4)	1,9		44
5791	δ <sup>1</sup> Grus 14931	23 ,	3 -44 0	~Gs		4 ,02 4 ,19	26 + 17	88 9	+ 5,0	12 12	(1)		320	58
8556 5793	4 Aquarir	23 .	7 - 0 32		40,5	4 ,59	173 +107	85°	+28,9	P	(6)	2,0 5,8	34	<del></del> 48
8558 5794	4365 - ζ <sup>2</sup> Ληματίί 4365	23 ,	7 - 0 32	F2	A <sub>3</sub>	4 ,42 4 ,53	212	790	- -24,5	3		1,9 6,0	34	<del>-</del> 48
_8 <u>5</u> 59 5795 8560		23	8 44 15	Mb		4 ,31 4 ,42	18	280°	+ 3,0			0,	320	<b> 58</b>
5807 8571	δ Cepher 2548	25	4 1-57 54	Go	4°,7 Y26	Var	14	86°	16,4	5		2, 0,	7	+- 1
5804	5 Lacertae 3719	25	4 +47 11	Ko Ao	7º,2	4 ,61 4 ,54	21	239°	11,9	4		-2,		- 9
8572 5803 8573	a Aquarii 5850	25	,4 — 11 11	1	2°,7	4 ,89	30	180°	+14	15	(2)	0,	6 21	54
	on the motor		II. Control de	i tod r					11″. 402°			•		

Boss 5807 The prototype of the Cophelds, period 5,4 days. Has also a companion 7m,5, 11", 192°, which shares its p m

					_	-								
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
5808 8576	β Piscis Anst 17126	<b>25™</b> ,9	-32°52′	A0		4=,36 4 ,51	61 + 22	109° + 57	+ 6.3			3,3	3 <b>42°</b>	–60°
5810 8579	6 Lecertse 4420	26 ,1	+42 36	133	2°,5	4 ,54	13	261 °	Ver	- 6 6	(3)	-1,6 0,1	65	<b>—12</b>
5811	7 Tucango	26 ,2	-62 29	Мь	<u> </u>	4 ,92	39	151°	- 3,4				294	-49
85 <u>82</u> 5813	6348 & Lacurtae	27 ,2	+49 46	Λo	2.9	5 ,03 3 ,85	142 142	+ 35 85°	-14	36	(3)	2,9 1,6	69	<u>~</u> 7
8585 5824	3875 # Aquarli	30 ,2	— o 38	188	Y1 2'.6	3 ,99 4 ,13	+ 24 105	+139 121	- 8	35 17	(1)	4,6 0,3	35	<b>48</b>
8597	4384 Lacortac			Poc	W	4 ,33	+ 3	+105 0°	<u> </u>	17	<del>``</del> -	4,2	71	<del>- 5</del>
		31 ,7	+52 112	Nova		4,5 to 14,5	+ 1	a		_		- 5.5		_
5837 8613	9 Locertue 3770	33 ,2	+51 1	A5	3°,4 Y <sup>1</sup>	4 ,83 4 ,97	116 106	210° - 49	+19	25 25	(1)	1,8 5,2	70	- 6
5844 8622	10 Lacertse 4826	34 ,8	+38 32	Oos	2°,0 W	4 ,91 5 ,10	11	165°	Var		_	0,3	65	-17
5849	r Pisois Aust.	35 .1	-27 34	Ba	1"-2"	4 ,22	24	94	+ 3				352	-62
8628 5850	16010	35 ,8	-81 54	Fo-	Y1	4 ,41	上. <u>[3</u>	+ 20 275	+25	H		1,1	275	—35 <sup>—</sup>
8630 5852	889	36 .	+43 46	Ko.	6°,4	4 ,47	- 21 97	- 59 85°	-10,7	17	(4)	3,3 0,8		-13
8632 5853	4266 [ Pegast			Ва	Oa	4 .59	+ 27	十 93		17		4,6	L.	-42
8634	4797		+10 19	)	21,7 W	3 ,61 3 ,79	78 + 27	99°  + 73	+ 4	12	(3)	-2,2 3,1	<u> </u>	
5854 8636	# Gruis 14308	36 ,7	-47 24	Мъ	64,8	2,24	130 + 57	99°	+ 1,0	15	(1)	-1,9 2,8	314	59
5858 8641	o Pogasi 4436	37 .1	+28 47	AO	2°,4 YG1	4 .85 5 ,04	36 - 35	191°	+ 7,9	17	(3)	1,0	60	-26
5860	e Gruis	37 .7	-41 56	Ko.	==	4 ,89	84	183°	+ 30,4	14	(1)	0,6	323	61
<u>8644</u> 5864	18049 g Aquarii	38 .:	-19 21	TK 5	5,3	4 ,92	<u> 71</u>	+ 45 215°	+21,6	14	(1)	4,5 0,1	11	-60
8649 5865	6324 7 Pegasi	38 ,	+29 42	Gō.	5",0	4 ,84 3 ,10	<u> </u>	+ 1	+ 4,4	11	(3)	2,0 -0,2		— <u>25</u>
8650 5867	4741 7 Grus		-54 1	Ko	Y.	3 ,22 4 ,86	- 29 25	+ 21	<u> </u>	22		0,9		-56
8655	10123					4 .97	+ 24	+_6	1	24 24	(1)	1,9		
5874 8665	F Pognal 4875	41 ,0	11 40	F5	4",8 Y	4 ,31 4 ,32	545 -322	155°	- 4,5	59 58	(5)	3,1 8,0		<b>-41</b>
5875 8667	1 Pegnsi 4709	41 ,	+23 2	Ko	5°,1	4 ,14 4 ,15	+ 10		3,8	21 18	(4)	0,4 3,0		-31
5880 8675	a Gruin 13 389	42 ,	5 -51 51	A2		3 .69 3 .83	120	122	0	1	abla	7	304	-58
5884	T Aquaril	44	3 -14 7	K 5	7,0	4 ,21	39	204	+ 1,2			0,0	5 21	-59
8679 5885	6354 μ Pegnal	45	2 +24 4	K <sub>0</sub>	0° 5°,3	3 ,67	- 38 154	107	+13,	19 3 31		$-\frac{2.3}{1.5}$		-31
_ <u>8684</u> 5891	#618	l.	1 +65 40	Ko	Y"	3 ,75	+ 18			_ 31		4,0	5	L
8694 5893	1814	J		ι	Y	3 ,66	-11E	74		34		4,4	4	i _
8695	16270	[		1		4 ,52 4 ,68	<u> </u>	- <del>-</del> 6	. L		Ľ	2,5		— 6 <b>5</b>
5895 86 <b>9</b> 8	3 Aquarii 5968	47	4 - 8 7	Ma	0A.0	3 ,84 3 ,87			<u> </u>	5 18		0,		-57
5899 8702	Cophel 703	47 .	9 +82 37	K5	6°,4	4 ,97	7 64	32	-31,		(3)		4 86	+22
5904	d Aquarii	49	3 -16 21	A2	2",8	3 ,51	52	246	+20	39	(2)	1,	5 19	-61
<u>8709</u> 5910		50	,2 + 8 17	AD	2°,8		7:	1 79	-12	12	<b>(4)</b>	<del>2,</del>		- 50
8717	4961	I	1	1	W		+ 40	3  + 54		9	ol '''	4,	2	1

22h to 23h.

1	2	3	1	5	6	7	8	9	10	-11	12	13	11	15
5911 8720	δ Piscis Aust 16303	50 <sup>11</sup> ,4	-33° 4′	Ko		4 <sup>n</sup> ,33 4,35	36 + 36	39°  - 3	-11,9	23 23	(1)	1,1 3	11°	-65°
5916 8728	a Piscis Aust 19370	52 ,1	-30 9	A3	2',6	1 ,29	365 - 51	117° +361	-1 6,5		(2)	1,5 3	48	66
5926 8747	4 Gaus 10382	55 .0	-53 17	Gr 5		4 ,18 4 ,30	66 - 38	266° 51	Vai - 3	17 17	Ĩ(1)	0,3 30	00	- 58
5927 8718	36 Cepher 610	55 ,2	-1-83 49	K5		4 ,96 4 ,86	106	73°  +106	+ 2,9	13 13	(2)		87	23
5933 8762	o Andromedac 4664	57 .3	+11 47	B5 A2p	2',3 W	3 ,63 3 ,91	32 13	131°	15	11	(4)		70	-16
5939 8773	# Piscium 4818	58 ,6	+ 3 17	В5р	2",4 W	4 ,58 4 ,75	13	129°	+ 2	10	(1)	1 1	48	— 5 i
5910 8775	# Pegasi 4480	58 ,9	+27 32	Ma	6",8 OY <sup>2</sup>	2 ,61 2 ,66	234  -199	55°  -124	+ 8,7	23 22	(5)		05	29
5942 8780	3 Andromedae 4028	59 ,7	+19 30	Ко	2,'8	1 ,91 1 ,61	230	46°	-31,8	14	(5)		74	- 9
5911 8781	л Редач 4926	59 ,8	1 14 40	A0	1,'8	2 ,57	71	128° - + 73	Vai — 4	32 32	(4)		57	-41
5919 8787	0 Gruis 15149	1 ,2	-11-1	5 دا		1,35 4,56	57 - 53	233°	+ 9.6	10	(a)	-0,6 31 3 2	15	64
5950 8789	61 Aquuu 17 197	I,3	- 21 17	(45	5' 6' () Y <sup>2</sup>	1,77 4,81	1 38	90° + 56	+15,2	13	(Ī)	-0,7 3,9	4	67
\$952 8795	55 Pegasi 4997	2,0	+ 8 52	Ma	0,18	+ ,69 + ,61	- 16 - 8	153° -  14	5,7	9	(5)		53	<b></b> 46
5954 8796	56 Pegasi 4716	2 ,2	1 24 56	Ko	6.4	4 ,98 1 ,95	38 35	180° 16	26,9	16 14	(4)	,	63	<b>-32</b>
5955 8797	1 Cassiopoiao 2515	2 ,4	+58 53	В1	2',6 Y1	1 .93 5 .07	12	59°  -  10	Vai 8.5	3	(3)		77	— 1 <sup>-</sup>
5960 8812	6 Aquaru 6 368	4 ,ī	-21 43	Ιζο	5°-0°	3 ,80	59 1-56	51°	<b>+21,1</b>	23 23	(3)		10	—67 <sup>~</sup>
5963 8817	c <sup>a</sup> Aquain 17771	4 ,5	-23 O	(+0 A2	2' Y1	4 ,94	13 + 3	108°  - 13	4,8	9	(2)	-0.3 0.5	7	<b>—67</b>
5966 8819	# Cephei	4 ,7	+71 51	G-5	5',2 Y1	4 ,56	28 26	154°	Vai 19,3	17 12	(7)		84	14
5965 8820	t Gruis 1+947	4 ,7	- 15 47	Κo		+ ,to 4 ,19	145 + 38	106° +141	Var - 4,4	17	(1)	0.3 31	10	63 ¯
5975 8830	7 Andromedão 3964	8 ,0	<u>+48 51</u>	1.0	3°,8	4 ,62 4 ,73	134 +115	44°- + 70	+13	42 41	(4)		75	-10
5978 8834	9 Aquani 6170	9,1	- 6 35	Ma.	7°,0 OY3	4 40	193 149	1724	- 0,4	14	(4)		40	- 59
5981 8841	ψ <sup>1</sup> Aquatii 6156	10 ,7	- 9 38	Ko	2°,9	4 ,46	367 -+191	92° +316	<del>-2</del> 7,0	21	(3)	7.3	37	-62
5985 8848	y l'ucanae 8062	11 ,6	-58 47	Ì:2		4 ,10	89 - - 57	336° - 69	+18		_		90	<del>-55</del>
5988 8852	γ 1 <sup>3</sup> 18cmm 4648	12 ,0	+ 2 14	Ko	5°,6	3 ,85	753 - -407	88° +633	14,0	25 25	(4)		52	52
5992 8858	ψ <sup>4</sup> Aquarit 6160	12 ,7	- 9 44	135	2°,6 YG1	4 ,56 4 ,73	13	103° + 12	- 3·	10	(î)		37	−62 <sup>~</sup>
5993 8860	8 Andromedae 3991	13,1	+48 28	Ma	7°, I O8	4 ,99	38 15	- 81° + 35	- 8,3	10 10	(4)		75	11
5995 8863	y Sculptoris	13 ,4	-33 5	Ko		4 ,51 4 ,53	71 - 43	159° + 57	+16,7	15	(1)	0,4 3. 7,0	37	<del></del> 70
6000 8872	o Cophel	14 ,5	+67 34	G5	i –	4 ,90 4 ,92	66 + 20	75° + 63	-17,8	22 21	(7)	-	82	+-7-
6005 8880	7 Pegasi 4810	15 ,7	+23 12	A.5	2°,8 Y1	4 ,65 4 ,75	35	127° + 34	+17	28	(2)		66	35
6012 8892	b1 Aquatii 6587	17 ,7	-20 39	Ko	5°-6°		153 142	233°   55	- 5,6	27 27	(3)		15	69
6024 8905	n Pegasi 4833	20 ,4	+22 51	Go	4º,7 Y <sup>2</sup>	4 ,57	191 +107	820	-13	21 21	(4)	1,2	67	<del>-35</del>

						20".			_					
1	2	3	4	5	6	7	8	9	10	11	12	33	14	13
6026 8906	b <sup>a</sup> Aquarii 6420	20 <sup>10</sup> ,8	-21°12′	K5	6°,3 Ƴ³	4 <sup>m</sup> ,52 4 ,53	83 - 81	226° 20	+15,4	24 24	(1)	1,4	16	-70°
6031 8911	n Piscinm 4998	21 ,8	+ 0 42	A2p	2°,6 W	4 ,94 5 ,17	24 - 32	136° +120	- 4.9	22 21	(5)	1,0		-56
6037 8916	D Pischum 5173	22, ,9	+ 5 50	G5	5°.3	4 ,45 4 ,48	138	252° - 92	+ 6,1	9	(3)	1,3 5,2		-51
6040 8923	q Pegasi 5009	24 ,1	+12 13	K0	5°,4 Y	4 ,67	62 + 51	64° + 35	-15,0	10	(4)	-0,8 3,6	63	-46
6046 8926	Camiopeiae 9748	35 ,4	+58 0	B3	2°,5,2° W, V	4 ,89	28 + 18	62° + 22	Ver 14,8	6	(3)	-1,2 2,1		- 3
6054 8937	# Sculptoria 15527	27 ,6	38 22	139	1	4 ,46	92 + 54	83° + 75	+ 2		Ì	4,3	322	-71
6057 8939	b Aquarii 6437	28 ,0	-21 28	Αo	1° ₩	4 .76	18 + 11	338° - 15	+15	_		1,1	20	-72
6062 8949	4 Phoenicis 15420	29 .7	-43 10	A2p	<u> </u>	4 ,80 4 ,94	27	110°	+19	_	İ	2.0	309)	-69
6068 8959	Phoenick 14720	32 ,5	<b>-46</b> 3	A2		4 ,86	68	111° + 67	+10			4,0	303	-67
6071 8961	1 Andromedae 4283	32 .7	+45 55	K <sub>0</sub>	5",5 Y"	4 ,00 3 ,98	449 -350	159° -283	+ 6.7	45	(4)	2,3	78	-14
6073 8965	Andromedae	33 ,2	+42 43	B8	2°,9	4 ,28	26	97°	0,0	4 <u>5</u> 13	(4) <sup>-</sup>	7,3 -0,2	77	-17
6077 8969	· Piecinm 5085	34 ,8	+ 5 5	F8	3 ,9 Y	4 ,47	+ 6	+ 25	+ 5,6	13 70	(4)	1,4 3,5	62	-54
6078 8974	7 Cephel 928	35 ,2	+77 4	Ko	5°,4	4 ,34 3 ,42	-195 169	+ 540 340	-43,2	-69 -69	(4)	8,1 2,6	86	+15
6080 8976	≈ Andromedse 4522	35 ,5	+43 47	Αo	2°,6 W	3 ,45 4 ,33	+157 83	- 63	<b>– 9.</b>	14	(2)	4,6 0,1	78	-17
6083 8982	A Aquerii 6358	36 ,6	-18 23	Gū	41,9 Y	4 ,49	+ 4	+ 83 68°	+ 4.8	13. 2	(1)	3,9 -3,6	31	-72
6084 8964	2 Pischum 5037	36 ,9	+ 1 14	À5	3°,3 Y¹	5 ,05 4 ,61	+ 14 199	+ 11 223°	+ 8 ^	36	(6)	1,3 2,2	39	-57
6087 8988	∞ Aquarii 6476	37 .5	-15 6	Δo	24,8	4 ,62	-195 106	125	3	33 16	(1)	0,1 0,6	39	-70
6094 8997	78 Pegari 4627	39 ,0	+28 49	K <sub>0</sub>	5°,9	4 ,78	- <u>7</u>	+106 117	- 6,8	16 16	(5)	-4.7	75	<b>—31</b>
6110 9016	d Sculptoria	43 .7	-28 41	Δū	Y 1	4 ,64	146	+ 80 133°	+14.	16 36	(A)	4,5 2,4	351	-77
6135		49 ,4	+56 57	F8p	<b>Y¹</b> 6*,7	4 ,81	- 35 7	+142 315°	-42,5	-8	(5)	5,4 2,1	83	- 4
9045 6150 9064	9 Pegasi	52 ,7	+24 35	Ma	Y* 7°,3	4 .75	+ 3 56	- 6 228°	<del>- 54</del>	12	(3)	-0,9 -0,1	77	36
6155	4865 σ Cassiopeiae 8089	53 ,9	+55 12	B <sub>2</sub>	ΟY* 2*,8	4 ,74	- 53 12	- 19 115°	- 6.1	12	(3)	3,5	83	- 6
9071 6156	Ο Pischm	54 ,2	+ 6 19	F5	₩ 4°,1	5 ,14 4 ,03	- 1 186	+ 12 126°	- 2	<u>4</u> 31	(4)	- 0,3 0,5	70	<b>— 54</b>
9072 6160	5227 a Tucanas	54 .7	-66 8	В9	A,	4 ,23	17 48	+186 121*	+11	33		5.4	277	<del>-50</del>
6165	3819 Octantia	56 ,4	<b>-77 37</b>	K <sub>0</sub>		4 ,80	- 14 171	+ 46 204	+23,7			3,1	273	<del>-40</del>
9084 6171	1596 30 Plectum	56 ,8	<b>- 6 35</b>	МЪ	75,0	4 ,84	-164 53	- 48 130°	-11,8	11	(3)	_5 <u>.9</u> _0,1	61	-66
90 <del>89</del> 6173		57 ,2	<b>-30 16</b>	B5	OB	4 ,65	- 8 26	+ <u>12</u> 94	Var	11		3,3	345	-80
9091 6179	19790 2 Cett	58 ,6	-17 54	A0	3°	5 .15	+ 10	+ 24 113*	+ 0,3 - 5	14	7/1	2,1		
9098   Boss	6417 6046, Relipting bire	- 1			Υı	4 77	+ 3	+ 21	_	16	(1)	0,6 1,2	43	<b>-76</b>
		_,		- ~~00 C	THE - 200	moust Ve	mahia did	T 433 4 10	Company of the Compan					

i. Period 6,066 days. — Boss 6135. Variable star 4m,4 to 5m,1

In the presenting table have been included the two globulers MGC 104 and 1139 on comming its several Uranomatrics. To the objects brighter than 5m,00 should also be added several globular clusters and open educions and also the two Magellando Clouds. The last mentioned objects have, according to the photographic estimates of the present writer, a total magellands of on,5 and 2m,0, respectively.

## II. Catalogue of Stellar Diameters

Explanations to the catalogue Col i gives the Boss number Foi further details as to the objects the preceding catalogue should be consulted

Col 2 gives the name of the star

Col 3 gives the hypothetical apparent radius according to Herrisprung's determination in Annalen van de Storiewacht te Leiden XIV, part 1 (1922)

Col 4 the quantity 107,5 x radius (unit 0",001)

(ol 5, 6 and 7 contain the mean ingonometric parallax, the mean spectrographic parallar, and the spectral proper motion parallax, respectively (unit 0",001) By compiling this catalogue the available parallax material up to the beginning of 1929 was used. Later on have been added a number of new determinations of trigonometric parallaxes. In a very few cases the dynamic parallax has also been included in the value of  $\pi_1$ . The parallax values have been reduced to absolute values and corrected for systematic errors according to van Maanins tables

Col 8, 9 and 10 contain the linear radii computed by the aid of the three different parallax values  $\pi_1$ ,  $\pi_2$ , and  $\pi_3$  respectively

Col 11 the visual Harvard magnitude (RHP)

Col. 12 the Harvard spectral class according to the HD Catalogue

Col 13 the quantity  $H = m + 5 + 5 \log \mu$  computed on basis of Boss's proper motions When the radius is within parenthesis this indicates that the value is considered to be rather maccurate. In a few cases the radu have not been computed on basis of  $\pi_8$ , because of the fact that the parallax value falls outside the domain within which a fair value of  $\pi_n$  can be derived

	value of m <sub>B</sub> can	De cietta	ou									
No		Ilypothe		filg	Spectro	Spestral	Ser	ni diamet	CTS			
Boss PGC	Name	radius (unit is 0",0001)	107,5 M radius	parallax T1	graphio parallax	motion parallax ma	<u>d</u> 1 2	₫ <sub>8</sub>	<u>d</u> <sub>8</sub> 2	m, ja (Hai vard)	Spectral Class (Harvard)	п
10 12 27 31 43	α Andromedae β Cassropoiae γ Pogasi χ Pogasi & Andromedae	7 12 4 32 4	75,2 129,0 43,0 344,0 43,0	16 71 - 3 - 9 - 2	52 71 7 11 26	59 131 8 13 23	4,7 1,8 — —	1,4 1,8 6,1 31,3 1,7	1,3 0,9 5,4 26,5 1,9	2,15 2,42 2,87 4,94 4,44	A0p F5 B2 Ma A2	3,8 6,2 1,6 4,8 3,0
50 97 103 122 123	σ Andromedae λ Cassropeiae m Cassropeiae ζ Cassropeiae σ Andromedae	2 1 5 3 2	21,5 10,8 53,8 32,2 21,5	14 9 -21 - 8	21 4 5 8	23 17 3 8 5	1,5 1,2 —	1,0 13,4 6,4 2,7	1,3 0,3 17,9 4,0 4,3	4,51 4,88 4,24 3,72 4,44	A2 "B8 B0 B3 B3	4,0 3,3 0,6 0,5 1,3
130 132 135 141 152	s Andromedae δ Andromedae α Cassropeiae ξ Cassropeiae ο Cassropeiae	8 32 35 2 3	86,0 344,0 376,3 21,5 32,2	40 26 16	27 30 23 5	28 26 33 4 3	2,1 13,2 23,5	3,2 11,5 16,4 4,3	3,0 13,2 11,4 5,4 10,7	4,52 3,49 2,47 4,85 4,70	G5 K2 K0 B3 B2	7,2 4,5 1,4 1,5 1,4
164 168 173 175 189	<ul> <li>ζ Andromedae</li> <li>η Cassiopeiae</li> <li>δ Piscium</li> <li>γ Andromedae</li> <li>Cassiopeiae</li> </ul>	17 11 34 2 6	182,8 118,3 365,5 21,5 64,5	34 182 14	22 141 16 7 56	19 130 16 5 52	5,4 0,7 26,1	8,3 0,8 22,8 3,1 1,2	9,6 0,9 22,8 4,3 1,2	4,30 3,64 4,55 4,42 4,93	K0 F8 K5 B3 F8	4,8 9,1 4,4 1,7 6,3
191 193 199 200 203	20 Ceti $v^1$ Cassiopeiae $\gamma$ Cassiopeiae $v^2$ Cassiopeiae $\mu$ Andromedae .	22 15 7 14 4	236,5 161,3 75,3 150,5 43,0	36 39 33	12 13 16	11 13 129 15 34	2,1 3,9 1,3	19,7 12,4 9,4	21,5 12,4 0,6 10,0 1,3	4,92 4,95 2,25 4,83 3,94	Ko Ko Bop Ko A2	1.1 3.6 -0.4 4.8 4.9
206 218 226 257 259	η Andromedae 2 Ursae minoris ■ Piscium φ Andromedae β Andromedae	10 24 13 3 81	107,5 258,0 139,8 32,3 870,7	8 25 10 45	15 15 15 11 40	15 16 17 13 39	13,4 5,6 19,3	7,2 17,2 9,3 2,9 21,8	7,2 16,1 8,2 2,5 22,3	4,62 4,52 4,45 4,28 2,37	G5 K0 K0 B8 Ma	3.5 4,2 4,1 -0,7 4,0

	11,0 -11					Basel -1	8-	مسولل-اس				
No.		Hypothe-	107.5	Trig parellax	grayida grayida	proper				Myle (Har-	Sportral ciase	_
PGC	Name	mdius (mait is (1000,"0	x midten	parellex e <sub>1</sub>	parallax Ma	parallax parallax	<u>d1</u>	4 2	<u>4</u> ,	vard)	(Harvani)	H
264	# Casslopelan	4	43,0	9	30	34	4,6	1,4	1,3	4,52	A.5	6.3
270 271	7 Pisclum 7 Pisclum	13	96,7 139,7	10 38	13 17	12 15	9.7	7,4 8,2	8,1 9,3	4,89 4,70	Ko Ko	1,5 4,2
281	o Piscium	12	129,0	_8 8	16	14	'	8,1	9,2	4,64	Ko	3,0
300	v Piscium	2	21,5	13		16	1,7		1,3	4,67	A2	1,8
304	£ Andromedae .	10	107,5		17	12		6,3	9,0	4.99	Ko	3,0
310	φ Cassiopeine	16 8	172,0		14 68	13 48		12,3	13,2	4,96 2,80	KO KO	4,6 4,2
314 321	o Cassiopeine ω Andromodae	5	86,0 53,7	24	38	51	2,2	1,4	1,1	4,96	FS	7,7
325	α Ureao minoria	20	215,0	20	11	33	10,7	19.5	6,5	2,12	F8	-0,3
335	η Piscium	19	204,2	9	17	16	22,7	12,0	12,8	3.72	G5	1,2
338	z Camiopeias . v Andromedas .	9 8	96,7	17 61	12 84	12 96	5.7 1,4	8,1 1,0	8,1	4,88 4,18	ICO GO	2,8 7,3
350 357	v Pousel	31	86,0 333,2	17	27	23	19,6	12,3	14,5	3,77	Ko	4,3
369	z Andromedao	2	21,5		_,	11			2,0	4,90	B8	2,2
378	Pisalum	24	258,0	52	15	12	5,0	17,2	21,5	4,68	Ko	1,3
384	φ Persei	3	32,2	20 14	46	12   17	1,6 8,4	7.0	2,5 7,0	4,19 4,50	Hop Ko	1,8 4,2
393 419	Cassiopeiss	11 4	118,2 43,0	12	15 13	8	3,4	7.9 3.3	5,4	3,44	B3	1.6
421	α Trianguli	ا • و	96.7	51	37	67	1,9	2,6	1,4	3,58	F5	5.4
422	y Arietis	2	21,5	7		20	3,1		(1,1)	4,04	AOp	4.7
426 428	E Piscinm  B Aristis	10	107,5 86,0	64	19	12 57	1,3	5.7 1,0	9,0	4,84 2,72	ICO A 5	2,4 3,6
441	β Arietta	3	32,2	25	25	25	1,3	1,3	1,3	4,83	ĀS	4,7
446	A Casalopelas	4	43,0	23	37	22	1,9	1,2	1.9	4,61	A3	3.5
449	50 Cazalopelae	4	43,0	-00	25	22		1,7	1,9	4,06	A2	2,3
459 463	g Porsei	4	21,5 43,0	28	10 22	15 17	0,8	1,9	1,4 2,5	4,99 3,94	138 A2p	3,0 2,1
468	yl Andromedes	72	774,0	13	38	38	59.5	20,4	20,4	2,28	Ko Ko	1,5
477	a Ariotis	50	537,5	33	57	45	16,3	9,4	11,9	2,23	K2	4,1
480	58 Andromedaa .	2	21,5		4.0	27			0,8	4,77	A2	5.7
482 505	f Trianguil El Coti	7	75,3 118,2	14   34	49 7	50 12	5,4 3,5	1,5	1,5	3,08 4,54	A5 G5	4,6
517	7 Trianguli	3 1	32,2	20	•	23	1,6	1019	1,4	4.07	Ãŏ	3,2
545	65 Andromedae .	37	397.7	4	12	10	99,4	33,4	39,8	4,86	K5	2.3
550	(Camiopelee .	4	43.0	24	24	33	1,8	2,0	1,3	4,59	A5p	0,5
560 604	¿Cotl	2 2	21,5	21	3	17	1,0	7,2	1,3	4,34	A0 B2	2.3 -+.0
610	12 Porsei	5	21,5 53,8	20	, ,	12	2,7	/	4,5	4,99	Go	6.4
617	& Persel	7	75.3	80	94	75	0,9	0,8	1,0	4,22	P8	6.9
620	35 Arietis	] 4 ]	10,8		5	22	1	2,2	0,5	4,58	B3	0,1
622	7 Cett	6	64,5	38	36	42	1,7	1,8	1,5	3,58	A2	5.2
629 634	μ Cetil	22	64,5 236,5	32 26	17	19	2,0 9,1	13,9	1,5	4,36	Fo Ko	6,¢ 6,1
639	η Persel	61	655.7	-7	15	17		43.7	38,6	3.93	Ko	1,
643	41 Arietta	4	43,0	33	21	29	1,3	2,0	1,5	3,68	138	4.
644	16 Persel	6	64,5	21	35	38	3.1	1,8	1.7	4.27	Fo	5.
646 653	17 Persol	38 12	408,5 129,0	19	14	15	45,4 6,8	29,2 5,0	27,2	4,67 4,06	K 5	4.
668	# Persel	2	21,5	, "		21	ال ا	المرد ا	1,0	4,62	A2	3.
670	24 Porsel	14	150,5		10	13	l	15,1	11,6	4,97	K0	4.
674	a Ariotia ,	3	32,2	10	13	15	3,2	2,5	2.1	4,64	A2	+0
679 691	A Cett	71	21,5 763,2	11	10 26	22	69,4	2,1	3,1 34,7	4,69	B5	-0 2
694	y Persel	16	172,0		26	15	14,3				F5, A3	
312	t, Polecia. The president	•			elty relati		-					- :

ī				Hypothu		2 1-	Spectro	Spectral	Sem	d diamet	ers.		Constral	
1	н	No Boss PGC	Num	tical radius (unit is O",0001)	107,5 > radius	Trig puality vi	graphic parallax 72	proper parality i	$\frac{d_1}{2}$	<u>d<sub>1</sub></u> <u>2</u>	$\frac{d_4}{2}$	##vls (Har vard)	Spectral Class (Harvard)	11
1	6,3	698	g Perser .	62	666,5	38	11	24	17,5	60,6	(27,8)	3,4 to 4,2	Mb	4,6
	1.5 4.2 3.0	705 708	Сахморенае # Регчет	2 9	21,5 96,7	29 27	14 45	21	0,7 3,6	1,5 2,1	1,0	4,89 2,2 to 3,7	A2 B8	4,6 -3,1
	1,8 3,0 4,6	710 713	Persei .  ** Potsei	8 21	86,0 225,7	92 29	108 26	113 24	0,9 7,8	0,8 8,7	0,8 9,4	4,17	Go Ko	9.7 5.9
	4.2 7.7 -0.3 1,2 2,8	717 718 730 741 746	<ul> <li>φ Poiser</li> <li>δ Arietis</li> <li>ζ Arietis</li> <li>Camelopardalis</li> <li>Poiser</li> </ul>	11 16 2 2 31	118,2 172,0 21,5 21,5 333,2	23 47 16 7	15 16 12 10	12 18 18 22 10	5,1 3,7 1,3 3,1 30,3	7,9 10,8 1,8	9,8 9,6 1,2 1,0 33,3	4,82 4,53 4,95 4,76 4,92	Ko Ko Ao B3p Ko	1,5 5,4 4,4 0,2 0,5
į,	7.3 4.3 2.2 1.3	752 755 757 772 778	R Ceti Arietis 1 Person & Porsen o Lauri	7 26 2 20 16	75,3 279,5 21,5 215,0 172,0	116	100 13 16 27 20	61 10 19 33 23	0,6 14,3 34,4	0,8 21,5 1,3 8,0 8,6	1,2 27,9 1,1 6,5 7,5	4,96 4,72 4,98 1,90 3,80	G 5 K 5 A 2 F 5 G 5	7,2 1,9 3,8 -0,1 3,9
p	4,2 1,6 5,4 4,7 2,4	780 781 784 786 790	Perser Camelopardalis & Lauri Camelopardalis 34 Perser	33 5 3 6 2	354.7 53.8 32,2 64.5 21,5	13	7 12 7	21 10 26 10 12	1,7	50,7 4,5	16,9 5,4 1,2 6,5 1,8	4,94 4,42 3,75 4,76 4,67	B5 B9p B8 A0p B5	2,5 -2,6 3,0 0,0 2,9
	3,6 4,7 3,5 2,3 3,0	791 795 804 817 825	Camelopardalis o Persor f Tauri w Persor 10 Tauri	2 27 15 4	21,5 290,2 161,2 43,0 75,3	12	14 13 19 76	18 16 15 13 96	24,2	1,5 22,3 8,5 1,0	1,2 18,1 10,7 3,3 0,8	4,98 4,55 4,28 4,26 4,40	A2 K0 K0 B5p G5	2,6 1,4 0,6 2,5 8,0
I	2,1 1,5 4,1 5,7 4,1 1,6	838 842 844 847 852	of Person , Camelopardalis m Person p Person 17 Laura	5 9 4 9	53,8 96,7 43,0 96,7 32,2	5 13 17 20	20 12 5 20 18	17 9 6 22 14	10,8 3,3 5,7 1,6	2,7 8,1 8,6 4,8 1,8	3,2 10,8 7,2 4,4 2,3	3,10 4,96 3,94 3,93 3,81	B5 F5, A B1 F5 B5p	1,4 0,7 1,0 -1,3 2,4
1 3	3,2 2,3	856 858 860 861 865		2 2 3 45 3	21,5 21,5 32,2 483,7 32,2		13 19 14 10 14	12 16 14 9 14	2,4	1,7 1,1 2,3 48,4 2,3	1,8 1,3 2,3 53,7 2,3	4,37 4,67 4,02 4,71 4,25	B5 A0 B5 Ma B5	2,8 3,0 2,7 2,3 3,1
3	6,4 6,9 0,3 5,2	869 877 894 896 901	27 Lauri 4 Person Camelopardalis	5 4 7 3 9	53.8 43.0 75.3 32.2 96.7	- 26 10	28 22 7 13 J5	19 24 8 9 11	7.7 7.5 32,2	1,9 2,0 10,8 2,5 6,4	9,4 3,6	4,87	B5p B8 B1 B9 A, G5	1,5 2,4 0,5 1,6 2,3
0	6,1 1,3 4,3	910 913 920	β Perser	5 4 5	53.8 43.0 53.8	)   3	7 5 7	11 5 6		7.7 8,6 7.7	8,6	4,05	Oc 5	0,9 0,3 0,8
	5,9 5 4,1 A 5 1,4	932 930		4 12	43.0 129.0		29 20		3,3 43,0			3,94		-1,8 4,8
2	3,6 0 4,0 2 +0,8 0,1 2,3	938 947 967 970 972	7 c Persei . 7 μ Persei 9 f Persei	3 4 16 17 12	32,3 43,0 172,0 182,1	15 28		16 11 11 9	2,9 6,1 16,1		2,0 3,9 15,6 20,3	4,03 4,28 4,89	B3p G0 G0, A	1,7
l	A3 →1.9 2⊙		Handinch dor	Astrophysi	k V, 2							72		
		1												

1138 Appendices to Chap.4. K.Lundmark; Luminosities, Colours, Diameters, etc. of the Stars.

		Hypotha-				Spectral-	Sen	nl-dlamet	eTO			
No. Boss PGC	Name	tical radius (unit is 0",0001)	107,5 x xadhis	Trig paralisa n	Spectro- graphic parallax	proper motion parallax	$\frac{d_1}{2}$	$\frac{d_0}{2}$	d <sub>4</sub> 2	<sup>filvis</sup> (Har- yard)	Spectral Class (Harvard)	H
981 986 989 1000 1003	μ Tauri b <sup>1</sup> Persei	2 3 4 16 2	21,5 32,2 43,0 172,0 21,5	29	9 28 23 5	10 22 20 22 10	5,9	2,4 1,5 7,5 4,3	2,2 1,5 2,2 7,8 2,2	4,32 4,57 4,80 3,86 4,89	B3 A2 A3 K0 B3	2,0 4,0 3,9 4,3 3,2
1017 1022 1026 1029 1033	δ <sup>1</sup> Tauri	19 2 4 3 5	204,2 21,5 43,0 32,2 53,8	17 28 24 25 26	26 34 30 28 30	21 26 29 28 30	12,0 0.8 1,8 1,3 2,1	7.8 0.6 1.4 1.2 1.8	9.7 0,8 1,5 1,1 1,8	3,93 4,84 4,36 4,24 4,40	K0 A5 A3 A2 A5	4,2 5,3 4,6 4,4 4,8
1034 1036 1044 1045 1046	71 Tauri	3 9 22 20 4	32,2 96,7 236,5 215,0 43,0	24 31 37 28	29 34 28 42	27 12 24 21 25	1,3 7,6 5,8 1,5	1,1 6,9 7,7 1,0	1,2 8,0 9,8 10,2 1,7	4,60 4,94 3,63 4,04 3,62	A5 K0 K0 K0 F0	5.0 2.7 4.0 4.2 3.8
1054 1063 1067 1074 1077	Tauri	3 13 4 25 176	32,2 139,7 43,0 268,7 1892,0	28 23 28 57	25 28 4 83	26 10 26 13 60	1,2 1,9 9,6 33,2	1,3 1,5 67,2 22,8	1,2 14,0 1,7 20,7 31,5	4,84 4,97 4,75 4,46 1,06	A5 K0 A5 K0, A3 K5	5,2 -2,6 4,8 1,4 2,6
1076 1079 1087 1090 1107	d Tauri	4 2 3 2 2	43.0 21.5 32,2 21.5 21.5	27 22 8	19 4 36 28 9	24 (2) 29 21 9	1,2 1,0 2,7	2,3 5,4 0,9 0,8 2,4	1,8 (10,8) 1,1 1,0 2,4	4,38 4,12 4,30 4,85 4,33	A3 B2 A3 A3 B5	3,5 -4,4 4,4 4,5 1,1
1123 1139 1140 1141 1147	μ Eridani	3 10 3	21,5 32,2 107,5 32,2 32,2	-25 136 2	9 4 122 4	10 3 115 16 7	0,8	2,4 8,1 0,9 8,0	2,2 10,7 0,9 2,0 4,6	4,18 4,38 3,31 4,35 3,78	B5 B0 F8 A0 B3	0,9 -0,8 6,7 2,0 -2,0
1159 1161 1163 1167 1169	π <sup>5</sup> Orionis , ? Camelopardalis π <sup>1</sup> Orionis ε Aurigae ο <sup>2</sup> Orionis	2 3 3 60 23	21,5 32,2 32,2 645,0 247,2	3 18 20	7 20 18 27 19	6 14 24 20 18	7,1 35,8 12,3	3,1 1,6 1,8 23,9 13,0	3,6 2,3 1,3 32,2 13,7	3,87 4,44 4,74 2,90 4,28	B3 A2 A0 K2 K0	-3,1 -0,2 5,6 0,1 4,3
1178 1181 1185 1187 1190	4 Aurigae	28 13 13 41	21.5 301.0 139.7 139.7 440.8	27 16 2 - 3	15 4 7 38	20 10 24 11 12	0,8 8,6 (69,6)	20,1 34,9 20,0 11,6	1,1 30,1 5,8 12,5 36,7	4,99 4,73 -4,22 (3,18) 3,94	A0 K0 G0p F5p K0, B1	5.3 -1.4 -0.1 -1.5
1194 1202 1203 1204 1227	t Taurl	3 5 2 3 4	32,2 53,8 21,5 32,2 43,0	~19 16 14 25	30 34 10	25 30 17 19 14	1,4 2,3	1,1 1,6 3,2	1,3 1,8 1,3 1,7 3,1	4,70 4,99 4,65 3,28 4,86	A5 F0 B9 B3 F0	4,3 6,2 2,7 2,8 0,1
1236 1240 1246 1258 1259	μ Aurigae	3 20 56 20 7	32,2 215,0 602,0 215,0 75,3	68 5 75 13 68	22 91 13 83	22 12 91 17	0,5 (43,0) 8,0 16,5 1,1	6,6 16,5	1,5 17,9 6,6 12,6 0,9	4,78 4,64 0,21 4,81 4,85	A3 K0 G0 K0 G0	4,2 0,5 3,4 6,2 9,5

						<del></del>						
No.		Hypothe-		Trig	Spectro-	Spectral- proper	Se	nıl-dleano	ters	$m_{ m vls}$	Spectral	
Boss PGC	Name	radius (unit la 0",0001)	107,5 x radius	parallax n <sub>1</sub>	graphic patalinx m <sub>s</sub>	motion paraliax na	<u>d</u> <sub>1</sub>	2	<u>d₀</u> 2	(Har- vard)	Class (Harvard)	H
1284 1289 1301 1302 1303	o Orionis m Orionis $\eta$ Orionis $\psi^1$ Orionis $\gamma$ Orionis	2 1 3 2 7	21,5 10,8 32,2 21,5 75,3	12 19	4 5 7	6 5 5 7 16	2 <b>,</b> 7	5,4 2,2 4,6 4,7	3.6 2.2 6.4 3.1 4.7	4,65 4,99 3,44 4,73 1,70	B3 B3 B1 B3p B2	-0,4 -0,8 -2,7 1,3 -1,8
1304 1315 1314 1327 1331	$\beta$ Tauri $\sigma$ Tauri $\psi$ Orionis	8 2 1 35 2	86,0 21,5 10,8 376,2 21,5	24 12 15	37 5 11	67 7 5 9	3.6  1.4	2,3 2,2 2,0	1,3 3,1 2,2 41,8 2,1	1.78 4.83 4.66 4.97 4.32	B8 B3 B2 K5 B3	3,1 1,0 0,4 2,2 2,2
1333 1335 1339 1353 1357	χ Aurigae	3 66 5 2 3	32,2 709,5 53,8 21,5 32,2	9 2 6	3 7 6 4	4 8 5 3 4	6,0 10,7 5,4	236,5 7,7 3,6 8,1	8,1 88,7 10,8 7,2 8,1	4,88 4,73 2,48 4,53 3,49	B1 Ma B0 B0 Oc5	1,0 0,3 -4,5 -1,0 -1,3
1364 1370 1373 1375 1389	c¹ Orionis	2 7 18 4 3	21,5 75,3 193,5 43,0 32,2	17 5 27 - 1 - 9	6 12 28 15	4 7 24 13 3	15.1 7.2 —	3,6 6,3 6,9 2,9 8,1	5,4 10,8 8,1 3,3 10,7	4,65 1,75 4,39 3,00 3,78	В3 В0 Ко В3р В0	-3,9 -6,7 6,9 0,2 -6,2
1391 1396 1398	ω Orionis 126 Tauri ζ Orionis	2 2 6	21,5 21,5 64,5	7 19	4 5 8	5 8 7 3	3.1	5,4 4,3 8,1	4,3 2,7 9,2 21,5	4.54 4.87 2.05 4.21	B3P B3 B0	-1,6 2,3 -2,9
1399 1429	Orlonis	2 10	21,5 107,5	2	7 15	5 14	53,8	3,1 7,2	4,3	5.00 4.64	<b>В3</b> Ко	0,7 2,4
1438 1439 1442 1453 1457	134 Tauri	2 33 19 2 3	21,5 354,7 204,2 21,5 32,2	19 14 16	10 18 20 15	14 10 13 12 13	10,7	35,5 11,3 1,1 2,1	1,5 35,5 15,7 1,8 2,5	4,92 4,99 4,18 4,92 4,54	B9 Ma K0 A2 A0	2,2 3,6 -1,3 0,7 1,3
1461 1468 1472 1475 1478	χ Orionis	8 211 18 2 8	86,0 2268,2 193,5 21,5 86,0	104 11 18 34	94 10 28 4 63	57 39 23 3 38	0,8 206,2 10,7	0,9 226,8 6,9 5,4 1,4	1,5 58,2 8,4 7,1 2,3	4,62 (0,34) 3,88 4,90 2,07	F8 Ma K0 B2 A0p	6,2 1,8 -4,8 2,1 0,4
1479 1482 1494 1501 1508	π Aurigae  ∂ Aurigae  Orionis  μ Orionis  1 Geminorum	39 6 14 5 14	419,2 64,5 150,5 53,8 150,5	16 43 28	6 34 30 27 37	8 40 15 19 20	4,0 1,3 5,4	69,9 1,9 5,0 2,0 4,1	52,4 1,6 10,0 2,8 7,5	4,59 2,71 4,68 4,19 4,30	Ma Aop Ko A2 G5	-0,2 2,8 4,3 1,8 4,5
1507 1525 1550 1548 1556	χ <sup>R</sup> Orionis	5 2 2 2 2	53,8 21,5 21,5 21,5 21,5 21,5	-31	4 4 7 13	5 9 7 9 21	1,8	13,4 5,4 3,1 1,7	10,8 2,4 3,1 2,4 1,0	4,71 4,40 4,92 4,35 4,73	B2p B2 B3 B3 A0	0,6 2,2 1,8 2,1 4,9
1561 1565 1575 1604 1611	η Geminorum  » Aurigae  2 Lyncis  μ Geminorum  8 Monocorotis.	82 13 2 66 4	881,5 139,7 21,5 709,5 43,0	14 14 34 16	12 19 24 15	22 14 23	63,0 10,0 0,6 44,4 2,8	73,4 7,4 0,9 47,3	67.8 6.3 1.5 30.8	(3,2) 4,45 4,42 3,19 4,33	Ma Ko Ao Ma A5	2,3 6,6 1,1 3,7 -0,3

1468.  $\alpha$  Orionis. This is the only star for which natural variations in the diameter have been measured by the interferometer methods. For details about these measurements consult the text. The diameter as computed from the  $\pi_1$ 's ranges from 116,4  $\bigcirc$  (maximum) to 174,4  $\bigcirc$  (minimum). The interferometer measures show also that the diameter is largest at minimum light.

72\*

· · · · · · · · · · · · · · · · · · ·	1140	Hypothe-	- 1			Spectral-	Sen	ni-diamot	ers		<u> </u>	<u>-</u>
No. Boss PGC	Name	tical radius (unit is 0",0001)	107,5 ∡ radius	Trig parallax n <sub>1</sub>	Spectro- graphic parallax	proper motion parallax	<u>d<sub>1</sub></u>	$\frac{d_k}{2}$	49 2	"tyle (Har- vard)	Spectral Class (Harvard)	   
1635 1657 1690 1706 1716	y Geminorum	3 3 9 2 2	32,2 32,2 96,7 21,5 21,5	19 -18 43 8 20	10 13 63 4 14	9 11 41 (3) 14	1,7  2,2 2,7 1,1	3,2 2,5 1,5 5,4 1,5	3,6 2,9 2,4 (7,1) 1,5	4,06 4,50 1,93 4,68 4,89	B 5 A 0 p A 0 O e 5 A 2	0,8 -0,9 1,0 -0,8
1717 1721 1725 1740 1758	a Geminorum	45 19 10 15 23	483.7 204,2 107,5 161,2 247,2	7 14 48 19 13	11 19 49 14 13	18 15 72 12 15	69,1  2,2 8,5 19,0	44,0 10,7 2,2 11,5 19,0	26,9 13,6 1,5 13,4 16,5	3,18 4,65 3,40 4,70 4,75	G 5 K 0 I' 5 K 0 K 5	0.0 4.0 5.2 1.8 4.4
1763 1776 1778 1786 1812	<ul> <li>Ø Geminoram</li> <li>15 Lyneis</li> <li>e Geminorum</li> <li>ψ<sup>10</sup> Aurigae</li> <li>19 Monocerotis</li> </ul>	4 11 4 2 2	43,0 118,2 43,0 21,5 21,5	19 6 44	19 34 6	21 17 27 15 4	2,3 19,7 1,0	6,2 1,3	2,0 7,0 1,6 1,4 5,4	3,64 4,54 4,70 4,80 4,89	A2 G0 F0 A2 B3	2,: 5,: 4,: 1,: 0,:
1815	ζ Geminorum	14	150,5	5	3	4	30,1	50,2	37,6	3,6 to	Gop	-1.
1840 1853 1879 1886	7 Geminorum 8 Monocerotis	24 3 3 5	258,0 32,2 32,2 53,8	5 20 38	18	15 13 6 12	51,6 1,6	14,3	17,2 2,5 5,4 4,5	4,48 4,09 4,80 3,65	Ko A0 A2 A2	3, -0, -0, 2,
1898 1928 1931 1944 1952	d Geminorum	8 2 18 4 6	86,0 21,5 193,5 43,0 64,5	60 25 20 52	25 30 37	27 18 23 32 42	7,7 2,1 1,2	2,0 7,7 1,4 1,7	3,2 1,2 8,4 1,3 1,5	3,51 4,45 3,89 3,09 4,18	FO AO KO B8 FO	0, 2, 4, 2, 6,
1953 1962 1979	γ Canls minorls . 6 Canls minorls . α Geminorum	33 20 11	354,7 215,0 118,2	5 19 77	9 12 66	15 11 39}	71,0 11,3 1,5	39,4 17,9 1,8	23,6 19,5 3,0			3, 1, 3,
1987 2001	v Geminorum	39 4	419,2 43,0	11 25	18 19	58 5 20 27	38,1 1,7	23.3	2,0 J 21,0 1,6	1,99 4,22 4,92	K 5 Fo	4,
2008 2010 2023 2029 2031	α Canis minoris .  24 Lyncis  σ Geminorum  κ Geminorum  β Geminorum	31 3 20 17 64	333,2 32,2 215,0 182,7 688,0	312 20 22 101	331 19 40 25 129	305 19 22 9 83	1,1 10,7 8,3 6,8	1,0 1,7 5,4 7,3 5,3	1,1 1,7 9,8 20,3 8,3	0,48 4,96 4,26 3,68 1,21	Ko	5: 4 6 2
2078 2126 2130 2145 2155	27 Lyncis	2 16 24 2 14	21,5 172,0 258,0 21,5 150,5	19 -17 - 7	16 19 16 4	17 15 17 18 10	13,6	1,3 13,6 1,3 37,6	1,3 11,5 15,2 1,2 15,1	4,99 4,88 4,52 4,87 4,41	Ko Ko A2	3 4 4 3
2168 2195 2208 2237 2247	β Cancri	38 42 4	75,3 408,5 451,5 43,0 204,2		44 18 16 24 15	25 20 18 24 24	1,6  22,6 5,4 	22,7 28,2	3,0 20,4 25,1 1,8 8,5	3,76 4,43 3,95	IC2 IC5 A0	5 3 4 3
2290 2295 2302 2327 2330	δ Hydrae σ Hydrae γ Cancri	3 24 2	182,7 32,2 258,0 21,5 21,5	14 6	19 20 14	13 22 14 22 10	14,1 18,4 3,6		18,4	4,18 4,54 4,73	A0 K0 A0	3 3 1 5

1815. Cepheid variable. The parallax value derived on basis of the period-luminosity relation is 6",004.

. .

No		Hypothe tical		P	Spectro	Spectral	Sen	ni dinmet	ers			
Boss PGC	Nune	1.0001)	107,5 \ 1adius	Frig parallax #1	graphic parallax t <sub>2</sub>	proper motion parallax <sup>7</sup> 8	d <sub>1</sub> 2	$\frac{d_2}{2}$	$\frac{d_3}{2}$	m <sub>i is</sub> (Har yaed)	Spectral Class (Harvard)	11
2336 2348	δ Cancri ι Cancri	18 19	193,5 204,2	16 21	19 10	<b>23</b> 16	12,1 9,7	10,2 20,4	8,4 12,8	4,17 4,20	Ko G5	6,1 2,9
2351 2361 2393	e Hydrac g Hydrac g Hydrac	16 2 25	172,0 21,5 268,8	15 4 14	54 13 19	84 16 26	11,5 (5,4) 19,2	3,2 1,6 11,1	2,0 1,3 10,3	3,48 4,42 3,30	1:8 Ao Ko	4,9 2,4 3,4
2404 2407	ι Uisae majoris α Cancii	8	86,0 32,2	70 30	66 30	69 22	1,2 1,1	1,3	1,2 1,5	3, 12 1,27	A 5 A 3	6,6
2411 2413 2424	β Ursae majons 10 Ursae majons κ Ursae majons	27 6 4	290,2 64,5 43,0	70 17	69 26	8 72 25	0,9	32,2 0,9 1,7	36,3 0,9 1,7	4,99 4,09 3,68	Ma 1· 5 A0	1,6 7,6 3,0
2437 2441 2443 2446 2476	Uisae majoris  o <sup>a</sup> Uisae majoris  f Ursae majoris  r Uisae majoris  e Uisae majoris	15 4 5 5	161,2 43,0 53,8 53,8 32,2	-43 -2	54 41 23 18	12 40 28 39 24	1,0	40,3 0,8 1,3 2,3 1,8	13,4 1,1 1,9 1,4 1,3	4,71 4,87 4,54 4,74 4,89	G5 F8 A3p 1.5, A5	2,9 4,1 5,2 5,2 4,6
2479 2495 2507 2524 2536	<ul> <li>θ Hydrae</li> <li>38 Lyncis</li> <li>40 Lyncis</li> <li>κ I coms</li> <li>Dracoms</li> </ul>	3 4 61 21 20	32,3 43,0 655,7 225,7 215,0	17 32 2 - 7	25 21 31 20 15	41 33 33 15	1,9 1,3 327,8 —	1,3 2,0 21,2 11,3 14,3	0,9 1,3 19,9 15,0 19,5	3,84 3,82 3,30 4,61 4,58	A0 A2 K5 K0 K2	6,5 4,5 5,0 3,6 1,7
2540 2541 2549 2550 2552	h Uisae majoris t <sup>i</sup> Hydrae d Uisae majoris & Leonis & Uisae majoris	7 5 9 39 10	75,3 53,8 96,7 419,2 107,5	29 77 43 21 56	43 42 14 79	20 37 14 14 147	2,6 0,7 2,2 20,0 1,9	1,8 2,3 29,9 1,4	3,8 1,5 6,9 29,9 0,7	3.75 4,78 4,57 4,48 3,26	F0 F5 G0 K5 F8p	4,1 5,3 4,3 3,2 8,5
2559 2565 2566 2570 2589	z² llydrac 26 Ursae majoris 10 Leonis minoris Lyncis 2 Sextantis	3 2 11 11 21	32,2 21,5 118,2 118,2 225,7		16 20 20	17 20 12 28 18		1,3 5,9 11,3	1,9 1,1 9,8 4,2 12,5	4,50 4,65 4,62 4,99 4,78	A3 A0 G5 K0 K0	1,6 4,0 2,0 2,4 6,0
2595 2602 2618 2632 2637	i Ilydrae o Leonis m I coms υ Ursae majoris φ Ursae majoris	28 8 18 7 3	301,0 86,0 193,5 75,3 32,2	19 26 — 1	22 12 16 38 15	19 56 18 53 12	15,8 3,3 — 4,7	13,7 7,2 12,1 2,0 2,1	15,8 1,5 10,8 1,4 2,7	4,10 3,76 3,12 3,89 4,54	K0 F5, A3 G0p F0 A2	3,8 4,6 1,5 6,5 0,7
2648 2680 2692 2694 2696	μ Leonis τ Leonis 21 Leonis minoris η Leonis Α I conis	24 42 3 3 3	258,0 451,5 32,2 32,3 397,8	19	24 7 28 14	23 10 26 10 17	13,6	10,7 64.5 1,2 28,4	11,2 45,2 1,2 3,2 23,4	4,10 4,89 4,47 3,58 4,58	Ko Ma A5 A0p K2	5,9 3,1 3,1 -1,0 4,9
2697 2698 2730 2729 2741	15 Sextantis . α Leonis ζ Leonis λ Urace majoris 40 Leonis	10 6 4 6	21,5 107,5 64,5 43,0 64,5	58 9 10 50	66 29 46	9 81 28 50	1,9 7,2 — 1,3	1,6 2,2	2,4 1,3 2,3	4,50 1,34 3,67 3,52 4,97	A0 B8 F0 A2 I:5	1,9 3,3 0,8 4,6 7,6
2742	y <sup>1</sup> and y <sup>2</sup> Leonis	43	462,2	4	43	43 29	(115,5)	10,7	10,7	2,61 3,80	ко	5,3 6,5
2751 2754 2768 2776	μ Ursae majoris Ursae majoris 30 Leonis minoris 31 Leonis minoris	71 2 3 12	763,2 21,5 32,2 129,0	34	32 14 32 26	29) 24 12 26 20	22,4	23,9 1,5 1,0 5,0	15,95 31,8 1,8 1,2 6,4	3,21 4,92 4,83 4,41	K5 A0 F0 K0	3,8 1,9 5,0 5,4

1142 Appendices to Chap 4 K.Lumnmark Luminosities, Colours, Diameters, etc of the Stars,

	·	Hypothe-			Spectm-	Spectral	Send-diameters					
No. Boss PGC	Manas	tical radius (unit is 0",0001)	107.5 × 1=11=1	Trig parallex s <sub>1</sub>	graphic parallax	peoper motion perallex	41 2	4 2	<u>d<sub>0</sub></u>	(Her- vard)	Spectral Class (Harvard)	н ;
		0 100011									<u> </u>	
2785	36 Urago majoria	7	75.3	80	67	43	0,9	1,1	1,8	4.84	F5	6.1
2792	30 Sextantis	1	10.8		8	12		1,3	0,9	4,95	B5	3,6
2802	Urane majoria ,	3	32,2	26	30	27	1,2	1,1	1,2	4,84	A5	5,6
2504	o Loonis	2	21.5	29	5	4	0,7	4,4	5,4	3,85	B0p	-1,4
2829	37 Leonis minoris	10	107.5	21	8	6	5,1	13,4	17.9	4,77	Go	<b>— 1,0</b>
2899	46 Leonis minoris	16	172,0	31	33	27	5,5	5,2	6,4	3,92	Ko	6,3
2900	e Urace majoria	2	21.5	3.		16	313	21-	1,3	4.84	A.O	3,6
2909	54 Locals ,	2	21.5		18	21		1,2	1,0	4.32	ΛO	3.8
2930	β Urase majoria	7	75.3	47	54	41	1,6	1,4	1,8	2,44	A0	2,2
2931	p Leonis	46	494,5	25	12	9	19,8	41,2	54,9	4.97	Ma	3,0
2932	b Leonis	3	32,2	10		9	3,2		3,6	4,42	Ao	1.7
2933	g Urses majoris	47	505.2	21	54	49	24.0	9,4	10,3	1,95	Ko	2.7
2942	g Leonia	75	53.8	10	14	44	5,4	3,8	1,2	4.66	Fo	7.4
2958	p Umas majoris	29	311.7	.~	44	27	314	7.1	11,5	3,15	Ko	23
2972	d Loopis	ě	86,0	78	58	60	1,1	1.5	1,4	2,58	A3	4,2
	6 ¥ to	١.	44.0	١		ا ۔. ا						
2974	# Leonis	4	43,0	19	32	31 8	2,3	1,3	1,4	3,41	AO Ma	3,5
2976 2982	72 Leonis	27	290,2 32,2	1	8	_		36,3	36,3 1,2	4,87 4,58	A5	1,2 5,0
2984	g Ureso majoris .	3 8	86,0	146	126	27 60)	0,6	0,7	1,41	4,87	Go	8,2
4001	77		444	_		745		14.0	1,2	4,41	Ko	·
2985	# Ursas majoris .	33	354,7	7	21	19	50,7	16,9	18,7	3,71	L.O	0,9
2987	55 Urtae majoria	2	21,5	13	16	22	1,7	1,3	1,0	4,78	<b>A2</b>	4,6
2990	o Leonis	3	32,2		15	25		2,1	1,3	4,13	A0	4,0
2999	Leonis	7	75.3	58	51	54	1,3	1,5	1,4	4,03	F5	5.3
3031	A Draconia	44	473,0	22	14	13	21,5	33,8	36,4	406	Mo.	2,3
3058	v Leonis , , , ,	11	118,3	12	21	15	9,9	5,6	7.9	4,47	Ko	2,2
3089	7 Virginia .	40	430,0	,	15	20	61,4	28,7	21,5	4,20	Ma,	5,6
3090	z Ureaa majoris .	22	236,5	12	29	22	19.7	8,2	10,8	3,85	K0	4.5
3098	93 Laonis	6	64,5	29	45	54	2,2	1,4	1,2	4,54	B8	5.5
3101	/ Leonis	9	96,7	101	73	86	1,0	1,3	1,1	2,23	A2	5.8
3105	// Virginia	9	96,7	101	90	110	1,0	1,1	0,9	3,80	F8	8,3
3117	y Ursae majoris .	6	64,5	4	48	39	(16,1)	1,3	1,7	2,54	Ao	2.4
3139	≈ Virgina	3	32.2		22	18	``-', '	1,5	1.8	4,57	A3	2,2
3155	o Virginis	13	139.7	38	15	25	3,7	9.3	5,6	4.24	G5	6.0
3190	d Urma majoria .	4	43,0	45	32	36	1,0	1,3	1,2	3,44	A2	3.7
3210	o Virgini≡ .	3	32,2		-	23		"	1,4	4,00	A <sub>0</sub>	3,1
\$216	11 ComaeBereniose	10	107.5		20	16	1	5,4	6,7	4,91	Ko	5,6
3224	12 Comae Berenices		64,5		36	21		1,8	3,1	4,78	F5	0.8
3230	5 Can Venati-	"			30				1			1
	commu ,	8	86,0		11	10	I.	7,8	8,6	4.97	Ko	0.2
9242	y Comac Berenices	14	150,5	1	18	18	(150,5)	8,4	8,4	4,56	K0	5.0
3279	B Can. Venati-		1	1	1				1	1		ا ا
4	corum	10	107,5	107	110	96	1,0	1,0	1,1	4,32	Go	8,7
3281	и Draconia	1 2	21,5	- 3	13	17	l –	1.7	1,3	3,88	В5р	28 4.1 4.2 6.2
3283	23 Comae Berenices		21,5	- 1	14	18	-	1.5	1,2	4,78	A0	4.4
3284	24 ComneBerenices	11	118,2		10	1	1	11,8		4,95	ΚO	1 44
3283 3284 3307	y Virginia .	10	107.5	73	64	59)	1,5	1,7	1,8	3,65	) Fo	<b>9</b> /Z
3309	o Virginia . '.	1 2	21,5		13	58		1,6	1,9			遊園
فمادد	1 % 4 TO THE		1 41,3	•	1 73		•	1,0	, 1,0	נענד ו	, 110,	1.514

1144 Appendices to Chap.4. K.Lundmark: Luminosities, Colours, Diameters, etc. of the Stars.

		Hypothe			Spectro-	Spectral-	Sen	nl-diamot	ers			
No, Boss PGC	Name	tical radius (unit is 0"',0001)	107,5 × radius	Trig parollax n <sub>1</sub>	graphic parallax	proper motion paraliax #0	<u>d</u> <sub>1</sub>	$\frac{d_1}{2}$	$\frac{d_0}{2}$	# <sub>vls</sub> (Har- vard)	Spectral Class (Harvard)	11
3770 3771 3772 3798	o Bootis	12 23 4 10	129,0 247,2 43,0 107,5	45 16	25 149	15 31 22 20	2,9 15,5	9,9	8,6 8,0 2,0 5,4	4,69 2,59 3,76 4,64	K0 K0, A0 A0 G5	4,3 1,1 4,2 5,2
3809	β Ursae minoris .	82	881,5	11	41	21	80,1	21,5	42,0	2,24	IX5	-0.4
3814 3827 3834 3835 3836	16 Librae Ursac majoris	3 33 21 13	32,2 354.7 225.7 139,7 182,7	22 23	32 7 39 19	35 12 13 14 20	6,3 7,9	1,0 50,7 3,6 9,6	0,9 29,6 17,4 10,0 9,1	4,59 4,86 4,93 4,62 3,63	FO Mb K5 K0 G5	6,0 4,4 3,8 3,1 2,6
3842 3847 3887 3926 3928	ψ Bootis	15 7 17 4 5	161,2 75,2 182,7 43,0 53,8	76 24 34	16 77 25 36 42	19 68 26 33 24	1,0 7,6 1,3	10,1 1,0 7,3 1,2 1,3	8.5 1.1 7.0 1.3 2.2	4,67 4,86 3,54 4,33 3,14	Ko Go Ko Fo, Ko	5.9 7.9 4.5
3936 3940 3949 3953 3960	Draconis β Coronae borealis	30 5 2 3 5	322,5 53,8 21,5 32,2 53,8	34 16	30 33 30	17 45 8 12 28	9,5	10,8 1,6	19,0 1,2 2,7 2,7 1,9	3,47 3,72 4,98 4,17 3,85	Ko Fop A2 B5 Fo	-1.5 5.1 2,1 2,0 3,4
3961 3988 3994 3998 4001	α Coronae borealis  Coronae borealis  Serpentis  Coronae borealis  Serpentis  Serpentis	6 2 2 4 37	64,5 21,5 21,5 43,0 397,8	53 18 7 22 46	51 9 20 23 44	50 7 24 27 35	1,2 1,2 3,1 2,0 8,6	1,3 2,4 1,1 1,9 9,0	1,3 3,1 0,9 1,6 11,4	2,31 4,69 4,49 3,93 2,75	A0 B8 A2 A0 K0	3,3 0,4 4,3 4,0 3,5
4009 4010 4015 4016 4024	β Serpentis	4 8 45 4	43,0 86,0 483,7 43,0 96,7	32 87 19 14	30 101 14 22 28	27 60 19 28 16	1,3 1,0 2,3 6,9	1,4 0,9 34,6 2,0 3,5	1,6 1,4 25,5 1,5 6,0	3,74 4,42 4,28 3,63 4,73	A2 G0 K5 A0 G5	3.5 6.4 4.5 3.4 4.9
4026 4031 4032 4035 4042	e Sorpentis	4 25 16 2 8	43,0 268,7 172,0 21,5 86,0	36 31 69	42 13 28 22 85	34 12 23 17 72	1,2 5,5 1,2	1,0 20,7 6,1 1,0	1,3 22,4 7,5 1,3 1,2	3,75 4,88 4,77 4,34 4,61	A2 K5 K0 A2 G0	4,4 3,3 7,6 1,3 9,0
4055 4063 4072 4080 4081	γ Serpentis	4	86,0 225,7 43,0 21,5 21,5	78	118 23 32 15	102 19 28 15	1,1	0,7 9,8 1,3 1,4	0,7 11,9 1,5 1,4 1,7	3,86 4,22 4,96 4,91 4,82	F5 K0 A5 A0 A2	9,5 4,4 6,4 3,2 1,0
4089 4090 4108 4112 4134	<ul> <li>Draconis</li> <li>Coronae borealis</li> <li>Herculis</li> </ul>	2 8 12 2 67	21,5 86,0 129,0 21,5 720,2	30 14 40	63 34 30	12 87 21 18 26	4,3 1,5 18,0	1,4 3,8 24,0	1,8 1,0 6,1 1,2 27,7	4,64 4,11 4,94 4,26 3,03	B9 F8 K0 B9p Ma	4,4 7,4 7,5 1,8 4,1
4147 4162 4163 4165 4169	r Herculis o Serpentis r Herculis	3 4 7	236,5 32,2 43,0 75,3 129,0	32 18 15	23 13 28 31 17	26 11 31 32 16	5,1 1,3 4,2 . 8,6	10,3 2,5 1,5 2,4 7,6	9,1 2,9 1,4 2,4 8,1	3,34 3,91 4,80 3,79 4,72	Ko B5 F0 F0 Ko	3,0 1,4 6,0 2,8 5,3

				Ü								
		Hypothe-			Spectro-	Spectral-	Sem	l-dlamote	18			
No. Boss PGC	Name	tleni mdius (unit is 0",0001)	107,5 × radius	Trig parallax x <sub>1</sub>	graphic parallax	proper motion parallax $\pi_{a}$	$\frac{d_1}{2}$	<u>d</u> <sub>k</sub> 2	<u>d<sub>11</sub></u>	Sivie (Her- vard)	Spectral Class (Harvard)	Н
4182 4192 4204 4203 4212	ω Herculis η Draconis β Horculis λ Ophiuchl h Herculis	2 25 26 3 30	21,5 268,7 279,5 32,2 322,5	42 30 0	19 42 26 29 13	20 25 34 27 19	6,4 9,3 —	1,1 6,4 10,7 1,1 24,8	1,1 10,7 8,2 1,2 17,0	4,53 2,89 2,81 3,85 4,92	Aop G5 K0 A0 K5	4,0 1,8 3,0 3,8 6,5
4213 4220 4246 4255 4259	A Draconis σ Herculis ξ Herculis η Horculis g Draconis	2 3 15 18 14	21,5 32,2 161,2 193,5 150,5	31 111 53 19	14 96 31 21	15 18 132 24 10	0,7 1,5 3,7 7,9	1,6 1,7 6,2 7,2	1,4 1,8 1,2 8,1 15,1	4,98 4,25 3,00 3,61 5,00	B8p A0 G0 K0 K0	3,1 2,1 6,9 3,6 1,1
4270 4284 4302 4315 4322	Draconis 52 Herculis Ophluchi Ophluchi	5 2 2 29 4	53,8 21,5 21,5 311,7 43,0	3 61	33 16 39 70	22 20 23 31 36	7,2 0,7	1,5 1,3 8,0 0,6	2,4 1,1 0,9 10,1 1,2	4,88 4,86 4,29 3,42 4,82	F0 A2p B8 K0 F5	3,8 4,3 3,6 5,8 6,8
4323 4327 4328 4346 4368	30 Ophiuchi s Ursae minoris s Herculis 60 Herculis	19 12 3 2 4	204,2 129,0 32,2 21,5 43,0	13 23 19	11 7 25 17 15	14 10 21 18 11	9,9 1,4 2,3	18,6 18,4 1,3 1,3 2,9	14,6 12,9 1,5 1,2 3,9	5,00 4,40 3,92 4,91 3,22	K0 G5 A0 A3 B5	5,1 0,3 2,5 3,6 0,1
4373 4376 4379 4381 4388	α Herculis δ Herculis	64 6 15 39	688,0 64,5 161,2 419,2 10,8	- 2 29 19 -21	6 42 16 24 5	44 14 13 9	2,2 22,1 —	114,8 1,5 10,1 17,5 2,2	86,0 1,5 11,5 32,2 1,2	3,48 3,16 4,82 3,36 4,6 to 5,4	Mb A2 K0 K5 B3	0.7 4.3 3.9 0.3 1.5
4391 4419 4423 4425 4438	c Herculis	2 2 4 29 26	21,5 21,5 43,0 311,7 279,5	- 2 19	17 14 19 18 21	19 12 27 15 13	14.7	1,3 1,5 2,3 17,3 13,3	1,1 1,6 1,6 20,8 21,5	4,80 4,14 4,61 4,44 4,48	A2 A0 F0 K0	3,9 2,0 4,7 -2,6 1,1
4443 4458 4460 4459 4479	β Draconis	3 3	236,5 32,2 32,2 107,5 32,2	4 23 49 - 3	7 34 40 52 6	14 27 27 78 6	59,1 1,4 2,2	33,8 0,9 0,8 2,1 5,4	16,9 1,2 1,2 1,4 5,4	2,99 4,98 4,95 2,14 3,79	G0 A5 A5 A5 B3	-1,0 6,0 6,1 4,2 -1,7
4483 4487 4497 4500 4504		35 8 3	64,5 376,2 86,0 32,2 53,8	8	36 41 105 21 40	48 34 139 27 45	1,9 15,7 0,8 4,0 1,2	1,8 9,2 8,2 1,5 1,3	1,3 11,1 0,6 1,2 1,2	4,87 2,94 3,48 3,74 4,58	G5 A0	7.4 3.9 8.0 3.3 6.7
4531 4535 4538 4541 4542	# Herculis	22 17 90	268,7 236,5 182,7 967,5 53,8	0 20 17	29 16 28 41 18	22 13 22 20 12	9,6 — 9,1 56,9 17,9	23,6		3,99 3,82 2,42	Ko Ko K5	4,3 -2,1 3,6 -0,4 -2,5
4544 4545 4547 4548 4552	66 Ophluchi	17 3	53,8 21,5 182,7 32,2 32,2	4 2		34 7 11 8 17	45,6 16,1 2,0	2,7 15,2 5,4	3,1 16,6 4,0	4,81 4,71 3,91	B3 K0 B5p	5,5 1,2 0,1 -0,4 1,5

Name   Name		1140 Appendic		.p. 4		THE BUILT			,				
Pige   Name   Pige	No				l rio			Sen	i dinmet	ers	ni, is	Spectral	
4559   70 Ophunelts	Boss	Name	radius (unit is	107,5 × radius	parallax	parallax	motion parallax	$\frac{d_1}{2}$	d <sub>3</sub> /2	$\frac{d_8}{2}$	(Har	Class	H
1			5										
4584   72 Ophuchn   5   53.8   40   42   33   4.3   4.3   4.3   4.3   4.4   3.0   3.8   4.6   4.5					192			0,7					
4   43,0   3   7   (14,3)   6,1   3,83   Λ0   -3.2					40			1,3				1	
4501   d Ursae minorus										6,1	3,83	Ao	-3,2
4635 74 Ophurch         10         107.5         8         9         13.4         11.9         4.92         C5         0.8           4636 106 Hreuths         16         172.0         11         13         1.56         13.2         4.92         C5         0.8           4638 π         2 Perpents         23         247.2         65         54         50         3.8         4.6         4.9         3.42         IXO         8.2           4639 π         χ Lyrae         1         48.28         12         41         16         15.2         4.5         11.4         4.34         IXO         0.6         4.69         3.42         A.0         0.6         4.69         0.0         1.1         1.3         4.24         A.0         0.6         4.66         1.0         1.0         1.0         1.1         1.3         4.24         A.0         0.6         4.6         1.0         1.0         4.0         2.2         4.0         1.0         1.0         1.1         4.3         1.1         1.3         4.24         A.0         0.5         1.8         4.0         0.7         4.85         A.2         3.9         4.0         0.1         3.3         3.0         1.8 </td <td></td> <td></td> <td></td> <td></td> <td>٠,,</td> <td>4.5</td> <td></td> <td>ا ۽ ا</td> <td>4.0</td> <td></td> <td></td> <td></td> <td></td>					٠,,	4.5		ا ۽ ا	4.0				
4636   106   Herculus   16   472,0   11   13   15,6   13,2   4,98   K5   3,9   3,9   3,42   K0   8,2   4,639   x Lyrae   20   215,0   12   40   27   17,9   5,4   8,0   3,92   K0   6,5   6,70   0,0   0,0   0,0   1,2   3,69   K6   3,4   4,64   4,94   K0   2,2   24,5   5   1,0   1,		74 Ophruch			10			113					
# Lyrae   17	4636	106 Herculis	16	172,0		11	13		15,6	13,2	4,98	IX 5	3,9
4656   109   Díoculhe   20   215.0   12   40   27   17.9   5.4   8.0   3.02   KO   6.5	4638	η Serpentis .	23	247,2	65	54	50	3,8	4,6	4,9	3,42	KO	8,2
4671   Draconis   2   241,5   7   19   16   3,1   1,1   1,3   4,24   A Op   4,8   A Op   4,9							1						
4671   D Draconis   2   21,5   36   31   0,6   0,9   0,9   1,2   3,69   F8   7,7     4686   42 Draconis   12   129,0   24   18   14   5,3   7,2   9,2   4,99   K0   5,4     4707   d Draconis   7   75,3   6   11   12,5   6,8   4,95   F8p   0,2     4722   α Lyrae   19   204,2   124   123   129   1,6   1,7   1,6   0,14   Λ0   2,8     4747   ε Lyrae   2   21,5   1   16   -													
4686 42 Draconis . 12 129,0 24 18 14 5,3 7,2 9,2 4,99 KO 5,4 4707 d Draconis . 7 75,3 6 11 12,5 6,8 4,95 F8p 0,2 4722 α Lyrne . 19 204,2 12,4 123 129 1,6 1,7 1,6 0,14 ΛΟ 2,8 4747 s Lyrne . 2 21,5 - 1 16 - 1,4 4,68 A3 3,7 4,749 s Lyrne . 3 32,2 - 1,7 - 1,9 4,50 Λ5 3,5 3,5 4,84 11 11 11 11 11 11 11 11 11 11 11 11 11	4671			21,5	36		31	0,6		0.7	4,85		3,9
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		•	10	107,5		123	105	'	0,9	1,2	3,69		
4722       α Lyrae       .       19       204.2       124       123       129       1,6       1,7       1,6       0,14       AO       2.8         4747       e² Lyrae       .       2       21,5        1       16        1,6       0,14       4,66       A3       3,7         4749       e² Lyrae       .       6       64,5       54       69       61       1,2       0,9       1,1       4,26       DF5       6,9       1,475       1,1       4,26       DF5       6,0       1,5       1,475 </td <td></td> <td></td> <td>1</td> <td></td> <td></td> <td>18</td> <td></td> <td></td> <td>7,2</td> <td></td> <td></td> <td></td> <td></td>			1			18			7,2				
4747		α Lyrae				123			1.7				
4752   ξ <sup>1</sup> Lyrae	4747	s <sup>1</sup> Lyiae	2	21,5			16			1,4	4,68	Α3	3.7
4753       140 Herculis       .       6       64,5       54       69       61       1,2       0,9       1,1       4,26       F5       6,9         4756       β Scuth.       .       12 129,0       18       9       10       7,2       14,3       12,9       4,47       GO       1,5         4761       111 Herculis       .       3       32,2       54       33       28       0,6       1,0       1,1       4,37       A3       4,8         4776       β Lyrae       .       6       64,5       -14         4,96       B2p       -2,1       KO       4,48       4,49       0,6       4,78       KO       4,44       4,78       KO       4,47       4,78       KO       4,44       4,78       KO       4,47       4,78       KO       4,47       4,78       KO       4,44       4,47       0,6       4,5       A,5       3,3       28       4,40       0,6       4,5       GS       3,3       3,1       1,1       4,49       4,6       4,1					_							1	
4756   β South   12   129,0   18   9   10   7,2   14,3   12,9   4,47   Go   1,5   4,758   Lyrae   11   118,2   12   12   6,2   9,8   4,92   KO   2,2   4,761   111   Iloroulis   .   3   32,2   54   33   28   0,6   1,0   1,1   4,37   A   3   4,8   4,796   A   4,790   A		ζ' Lyrae . 140 Herculis .											
4758       Lyrae .       11       148,2       19       12       6,2       9,8       4,92       K0       2,2         4761       111 Horoulis .       3       32,2       54       33       28       0,6       1,0       1,1       4,37       A3       4,8         4776       β¹ Lyrae .       6       64,5       -14       -14	4756	β Scutı.		129,0						12,9			
## April													2,2
4790         c Draconis						33	20	0,0	1,0	1,1		_	i
4797   113   Horoulis     9   96,7   20   22   6   4,8   4,4   0,6   4,56   G5, Λ3   -1,9   2,6   4800   δ½ Lyrae     35   376,2   7   8   53,8   47,0   4,52   Mlb   -0,5   4802   δ Serpentis   4   43,0   24   22   21   1,8   1,9   2,0   4,10   Λ   5, Λ   5   3,8   4823   ε Aquilae     18   193,5   21   20   19   9,2   9,7   10,2   4,21   K0   4,2   4824   γ Lyrae     5   53,8   11   21   17   4,9   2,6   3,2   3,30   Λ0   -2,2   4825   ν Draconis   16   172,0   -20   14   -   12,3   4,91   K0   4,0   4858   Λ   Λ   Λ   Λ   Λ   Λ   Λ   Λ   Λ		o Draconis	_	182,7		13	15	16,6	14.1	12.2			
4800       δ* Lyrae       .       35       376,2       7       8       53,8       47,0       4,52       Mb       -0,5         4802       δ Scrpentis       .       4       43,0       24       22       21       1,8       1,9       2,0       4,10       A5, A5       3,1         4814       R Lyrae       .       25       268,7       6       7       14       44,8       38,4       19,2       4,32       Mb       3,8         4823       s Aquilae       .       18       193,5       21       20       19       9,2       9,7       10,2       4,21       KO       4,2         4824       y Lyrae       .       5       53,8       11       21       17       4,9       2,6       3,2       3,30       Aop -2,2       4,0         4825       v Draconis       .       16       64,5       40       34       36       1,6       1,9       1,8       3,02       Ao       3,1         4858       A Aquilae       .       6       64,5       40       34       36       1,6       1,9       1,8       3,02       Ao       3,1         4897       y Lyrae <td></td> <td>113 Horoulis</td> <td></td> <td>96,7</td> <td></td> <td></td> <td>б</td> <td></td> <td></td> <td>0,6</td> <td>4,56</td> <td></td> <td>-1,9</td>		113 Horoulis		96,7			б			0,6	4,56		-1,9
## 4802  ## Serpentis		Draconis				7			£18				2,6
## A Lyrae		, i			24								}
## ## ## ## ## ## ## ## ## ## ## ## ##		73 7		268,7									
4825       v Draconis .       16       172,0       -20       14       -       12,3       4,91       K0       4,0         4858       ζ Aquilae .       6       64,5       40       34       36       1,6       1,9       1,8       3,02       A0       3,1         4859       λ Aquilae .       4       43,0       38       31       1,1       1,4       3,55       B9       3,4         4897       η Lyrae .       2       21,5       5       4       4,3       5,4       4,6       B3       -3,2         4906       1 Vulpeculae .       2       21,5       7       4       3,1       5,4       4,6       B3       -3,2         4909       δ Draconis .       23       247,2       38       34       28       6,5       7,3       8,8       3,24       K0       -8,2         4912       Φ Lyrae .       23       247,2       -7       11       12       -       22,5       20,6       4,46       K0       -0,5         4923       x Cygni .       17       182,7       35       27       22       5,2       6,8       8,3       3,98       K0       4,6				193,5	ı	20		9,2			4,21		4,2
4858		v Draconis				21			2,6				
4859 / 4897       λ Aquilae       4       43,0       38       31       1,4       1,4       3,55       B9       3,4         4906 / 4906       γ Lyrae       .       2       21,5       5       4       4,3       5,4       4,46       B3       -3,2         4909 / 4909       δ Draconis       .       23       247,2       38       34       28       6,5       7,3       8,8       3,24       K0       3,9         4912 / 4923       ½ Lyrae       .       23       247,2       -7       11       12       -       22,5       20,6       4,46       K0       -0,5         4923 / 2923       ½ Cygni       .       17       182,7       35       27       22       5,2       6,8       8,3       3,98       K0       4,6         4940 / 7 Draconis       .       18       193,5       12       16       48       16,1       12,1       4,0       4,63       K0       8,0         4942 / 3 Vulpeculae       .       2       21,5       9       6       2,4       3,6       4,92       B5       0,8         4949 / 7 Sorranis       .       1       10,8       4       5       2,7	4858	¢ Aquilae	6		40	34	36	1,6	1,9				
4906 1 Vulpeculae . 2 21,5 7 4 3,1 5,4 4,60 B5 -2,4 4909 Δ Draconis . 23 247,2 38 34 28 6,5 7,3 8,8 3,24 K0 3,9  4912 Δ Lyrae 23 247,2 -7 11 12 - 22,5 20,6 4,46 K0 -0,5 4923 κ Cygni 17 182,7 35 27 22 5,2 6,8 8,3 3,98 K0 4,6 4940 τ Draconis 18 193,5 12 16 48 16,1 12,1 4,0 4,63 K0 8,0 4942 3 Vulpeculae . 2 21,5 9 6 2,4 3,6 4,92 B5 0,8 4948 π Draconis 2 21,5 16 22 18 1,3 1,0 1,2 4,63 A2 2,9  4949 2 Cygni 1 10,8 4 5 2,7 2,2 4,86 B3 0,4 4953 δ Aquilae . 8 86,0 57 56 54 1,5 1,5 1,6 3,44 F0 5,6 4962 π Aquilae 6 64,5 -12 32 13 - 2,0 5,0 4,86 F0 0,1 4976 6 Vulpeculae 29 311,7 13 12 17 24,0 26,0 18,3 4,63 Ma 5,8 4986 β Cygni 43 462,2 3 29 19 (154,4) 15,9 24,3 3,24 K0 -2,0		λ Aquilae		43,0			31			1,4	3,55	B9	3,4
4909 δ Draconis . 23 247,2 38 34 28 6,5 7,3 8,8 3,24 Ko 3,9  4912 δ Lyrae 23 247,2 - 7 11 12 - 22,5 20,6 4,46 Ko -0,5 4923 κ Cygni 17 182,7 35 27 22 5,2 6,8 8,3 3,98 Ko 4,6 4940 τ Draconis 18 193,5 12 16 48 16,1 12,1 4,0 4,63 Ko 8,0 4942 3 Vulpeculae . 2 24,5 9 6 2,4 3,6 4,92 B5 0,8 4948 π Draconis 2 21,5 16 22 18 1,3 1,0 1,2 4,63 A2 2,9  4949 2 Cygni 1 10,8 4 5 2,7 2,2 4,86 B3 0,4 4953 δ Aquilae . 8 86,0 57 56 54 1,5 1,5 1,6 3,44 F0 5,6 4962 π Aquilae 6 64,5 -12 32 13 - 2,0 5,0 4,86 F0 0,1 4976 6 Vulpeculae 29 311,7 13 12 17 24,0 26,0 18,3 4,63 Ma 5,8 4986 β Cygni 43 462,2 3 29 19 (154,4) 15,9 24,3 3,24 Ko -2,0												B3	
4923       κ Cygni       .       17       182,7       35       27       22       5,2       6,8       8,3       3,98       K 0       4,6         4940       τ Draconis       .       18       193,5       12       16       48       16,1       12,1       4,0       4,63       K 0       8,0         4942       3 Vulpeculae       .       2       21,5       9       6       2,4       3,6       4,92       B5       0,8         4948       π Draconis       .       2       21,5       16       22       18       1,3       1,0       1,2       4,63       A2       2,9         4949       2 Cygn1       .       1       10,8       4       5       2,7       2,2       4,86       B3       0,4         4953       δ Aquilae       .       8       86,0       57       56       54       1,5       1,5       1,6       3,44       F0       5,6         4962       π Aquilae       .       6       64,5      12       32       13        2,0       5,0       4,86       F0       0,1         4976       6 Vulpeculae       .       29       <	4909				38			6,5		8,8		Ko	3.9
4940 r Draconis													
4942 3 Vulpeculae 2 21,5 9 6 2,4 3,6 4,92 B5 0,8 4948 π Draconis 2 21,5 16 22 18 1,3 1,0 1,2 4,63 A2 2,9 4949 2 Cygn 1 1 10,8 4 5 2,7 2,2 4,86 B3 0,4 4953 δ Aquilae 8 86,0 57 56 54 1,5 1,5 1,6 3,44 F0 5,6 4962 π Aquilae 6 6 64,5 -12 32 13 - 2,0 5,0 4,86 F0 0,1 4976 6 Vulpeculae 29 311,7 13 12 17 24,0 26,0 18,3 4,63 Ma 5,8 4986 β Cygn 1 2 43 462,2 3 29 19 (154,1) 15,9 24,3 3,24 K0 -2,0													4,6
4948 π Draconis 2 21,5 16 22 18 1,3 1,0 1,2 4,63 A2 2,9 4949 2 Cygn 1 10,8 4 5 2,7 2,2 4,86 B3 0,4 4953 δ Aquilae 8 86,0 57 56 54 1,5 1,5 1,6 3,44 F0 5,6 4962 π Aquilae 6 64,5 -12 32 13 - 2,0 5,0 4,86 F0 0,1 4976 6 Vulpeculae 29 311,7 13 12 17 24,0 26,0 18,3 4,63 Ma 5,8 4986 β Cygn 43 462,2 3 29 19 (154,1) 15,9 24,3 3,24 K0 -2,0				21,5	12			10,1					
4953 δ Aquilae . 8 86,0 57 56 54 1,5 1,5 1,6 3,44 F0 5,6 4962 π Aquilae . 6 64,5 -12 32 13 - 2,0 5,0 4,86 F0 0,1 4976 6 Vulpeculae . 29 311,7 13 12 17 24,0 26,0 18,3 4,63 Ma 5,8 4986 β Cygn 43 462,2 3 29 19 (154,1) 15,9 24,3 3,24 K0 -2,0		π Draconis .	2		16		18	1,3					
4962 π Aquilae 6 64,5 -12 32 13 - 2,0 5,0 4,86 F0 0,1 4976 6 Vulpeculae 29 311,7 13 12 17 24,0 26,0 18,3 4,63 Ma 5,8 4986 β Cygni 43 462,2 3 29 19 (154,1) 15,9 24,3 3,24 K0 -2,0					27			1 .					
4976 6 Vulpeculae 29 311.7 13 12 17 24.0 26.0 18.3 4.63 Ma 5.8 4986 β Cygni 43 462.2 3 29 19 (154.1) 15.9 24.3 3.24 Kο -2.0	4962	r Aquilae		64,5				- 1,3					
		6 Vulpeculae		311.7	13	12	17		26,0	18.3	4,63	Ma	5,8
	<del>ተ</del> አያዕ	p Cygin	43	402,2	3	29		(154,1)	15,9			AO AO	-2,0

1

ţ

		Hypothe-			Contra	Spectrul	Sam	l diamete	-13			
No. Bom PGC	Name	Hypothe- tical radine (unit is 0",0001)	107,5 × milhs	Trig parallax #1	Spectro- graphic parallax	proper motion perallax #1	4 3	<u>d</u> 1 2	<u>d<sub>0</sub></u>	(Her vard)	Spectral Class (Harvard)	H
4988 4992 4995 4998 5004	. Cygni 8 Cygni μ Aquilae 9 Vulpeculao . Aquilae	5 1 19 2 3	53,8 10,8 204,2 21,5 32,2	5 24	28 5 21 12 9	28 4 21 4 10	10,8 8,5	1,9 2,2 9,7 1,8 3,6	1,9 2,7 9,7 5,4 3,2	3,94 4,85 4,65 4,88 4,28	A2 B3 K0 B8 B5	4,4 -2,1 6,7 -2,1 0,4
5009 5014 5021 5023 5027	a Draconis .  Cygni . Cygni . Cygni . Segittae .	10 4 11 10 14	107,5 43,0 118,2 107,5 150,5	181 70 14 0 12	158 57 15 11 15	201 49 13 16 15	0,6 0,6 8,4 — 12,6	0,7 0,8 7,9 9,8 10,0	0,5 0,9 9,1 6,7 10,0	4,78 4,64 4,79 4,37 4,45	Ko F5 Ko Go Ko	11,1 6,6 2,5 2,1 2,1 2,3
5047 5048 5052 5058 5062	7 Aquilae . 8 Cygni 8 Sagittae \$ Sagittae 6 Aquilae	63 6 46 2 20	677,2 64,5 494,5 21,5 215,0	18 28 3 24 204	30 42 16 13 145	17 22 10 15 152	37,6 2,3 (164,8) 0,9 1,1	22,6 1,5 30,9 1,7 1,5	39,8 2,9 49,4 1,4 1,4	2,80 2,97 3,78 4,95 0,89	K2 A0 Ma, A0 A2 A5	-1,5 2,0 -1,4 2,4 5,0
5068 5071	12 Vulpeculae η Aquilae	2 14	21,5 150,5	6	6 5	8 5	25,1	3,6 30,0	2,7 30,0	4,91 3,5 to	B3 G0p	2,2 -0,9
5079 5086 5089	e Druconis 13 Vulpoculae 6 Aquilae	14 2 12	150,5 21,5 129,0	14 9 38	26 16 16	20 17 15	10,7 2,4 3,4	5.9 1.3 8,1	7,5 1,3 8,6	4.7 3.99 4.50 4.86	Ko Ko	3.7 2,5 5,4
5093 5102 5103 5105 5118	β Aquilno	14 1 16 2 46	150,5 10,8 172,0 21,5 494,5	78 16 5 10	90 6 42 17 25	115 7 19 19 18	1,9 10,7 4,3 49,4	1,7 1,8 4,1 1,3 19,8	1,3 1,5 9,0 1,2 27,5	3,90 4,87 4,03 4,80 3,71	Ko B3 Ko A3 K5	7,3 0,1 2,6 3,3 2,7
5132 5153 5170 5171 5182	15 Vulpeculae	3 26 2 4	32,2 279,5 21,5 43,0 21,5	- 8 15	20 16 19 22	11 15 28 13	2,9	1,6 17,5 2,3 1,0	2,9 18,6 0,8 3,3 1,3	4,74 4,66 4,82 3,37 4,96	A5 K0 B2p A0 A0	3,3 3,2 -0,2 0,9 4,3
5186 5187 5188 5190 5191	o <sup>1</sup> Cygni	2 32 2 1 4	21,5 344,0 21,5 10,8 43,0	- 3 - 42	15 8 18	7 11 16 4 28	1,0	1,4 43,0 1,2 7,2	3,1 31,3 1,2 2,7 1.5	4,96 3,95 4,98 4,82 4,32	A2 K0, B8 A0 B3 A3	1,1 -4,6 4,8 -2,2 4,4
5195 5199 5200 5208 5229	23 Vulpeculae	5	322.5 21,5 354.7 53.8 247,2	15 11 2 21 2	16 8 6 8	12 16 4	21,5 2,0 — —	1,3 44,3 9,0 30,9	26,9 1,3 13,5	4,73 4,40 4,16 4,88 2,32	K5 B9 K0, A3 B1p F8p	2,9 1,7 -2,3 0,9 -5,3
5235 5255 5265 5270 5272	39 Cygni		279,5 64,5 10,8 53,8 32,2	16 -19	15 9 6 30 10	13 11 5 24 11	17.5 — (32.2)	18,6 7,2 1,8 1,8 3,2	21,5 5,9 2,1 2,2 2,9	4,60 4,09 4,89 4,28 3,98	K2 IF5P B3 A5 B5	2,7 -0,9 -0,1 2,7 1,2
5279 5282 5291 5294 5301	# Delphini	3 8 10	483.7 32.2 86.0 107.5 21.5	6 15 24 4	5 23 45 17 15	8 16 52 14 17	(80,6) 2,1 3.6 (26,9) (21,5)	1,4 1,9 6,3	60,5 2,0 1,7 7,7 1,3	4,85 4,69 3,72 4,51 4,78	K 5, A 2 F 5 K 0 A 0	3 -0,6 2,6 4,0 1,8 3,6
, . <b>.</b>	071 Copheid variable.	The paralle	C Asper (Lo	on the per	ied iumie	sty relati	O,"O M PO	05.				

		<del>,</del>									<u> </u>	
No Boss PGC	Name	Hypothe tical radius (unit is 0',0001)	107,5 × 17dius	pirlax parallax n	Spectro graphic parallav n <sub>1</sub>	Spectral proper motion parallax  \$\pi_4\$	$\frac{d_1}{2}$	diamete d <sub>2</sub> 2	$\frac{d_3}{2}$	mvis (Har vard)	Spectral Class (Harvard)	11
5310 5320 5323 5331 5334	α Delphini α Cygni δ Delphini 52 Cygni y <sup>I</sup> Delphini	4 13 5 17 13	43,0 139,7 53,8 182,7 139,7	21 5 11 13 31	21 29 25 32	24 24 15 26	2,0 27,9 4,9 11,1 4,5	2,0 1,9 7,3 4,4	1,8 2,2 12,2 5,4	3,86 1,33 4,53 4,34 4,12	B8 A2p A5 K0 G5	2,9 8,7 3,3 1,5 5,6
5336 5344 5346 5350 5361	ε Cygnı Cephei η Cephei / Cygnı 55 Cygnı	32 8 21 2 7	344,0 86,0 225,7 21,5 75,3	41 41 71 27 18	51 62 92 12	47 57 158 6 3	8,4 2,1 3,2 0,8 4,2	6,7 1,4 2,5 1,8 18,8	7,3 1,5 1,4 3,6 25,1	2,64 4,63 3,59 4,47 4,89	K0 G0 K0 B5 B2	6,1 6,5 8,2 0,1 1,6
5373 5375 5393 5410 5431	31 Vulpeculae 57 Cygnι ν Cygnι Γ¹ Cygnι ξ Cygnι	11 2 3 3 51	118,2 21,5 32,2 32,2 548,2	27 7 6	9 8 17 3 6	16 7 10 3 8	4,4 4,6 91,4	13,1 2,7 1,9 10,7 91,4	7,4 3,1 2,0 10,7 68,5	4,76 4,68 4,04 4,86 3,92	G5 B3 A0 Bop K5	4,8 1,0 1,0 -0,6 1,9
5436 5443 5452 5455 5460	f <sup>8</sup> Cygnı γ Equuloı ζ Cygnı δ Equuloι τ Cygnı	26 4 19 6	279,5 43,0 204,2 64,5 86,0	13 23 24 60 50	8 19 15 59 46	7 32 9 52 63	21,5 1,9 8,5 1,1 1,7	34.9 2.3 13.6 1.1 1.9	39,9 1,3 22,7 1,2 1,4	4,88 4,76 3,40 4,61 3,82	K5 Fop K0 F5 F0	0,6 5,9 -3,2 7,0 7,1
5461 5469 5471 5480 5489	α Equulei σ Cygni υ Cygni α Cephei 1 Pegasi	8 4 2 8 20	86,0 43,0 21,5 86,0 215,0	35 1 16 83 25	30 61 30	22 7 9 60 20	2,5 - 1,3 1,0 8,6	2,9 1,4 7,2	3,9 6,1 2,4 1,4 10,7	4,14 4,28 4,42 2,60 4,24	F8, A3 Aop B3P A5 K0	4,2 1,2 1,7 3,6 4,6
5522 5532 5543 5546 5563	2 Pegası  \$\beta\$ Cophes  \$\overline{c}\$ Cygns  72 Cygns  9 Cophes	34 3 12 19	365,5 32,2 129,0 204,2 43,0	10 7 6 12	13 6 29 15 4	8 6 19 15 3	36,6 4,6 21,5 17,0	28,1 5,4 4,4 13,6 10,7	45.7 5.4 6.8 13.6 14.3	4,76 3,32 4,22 4,98 4,87	K5 B1 K0 K0 B2	0,9 1,3 1,6
5580 5584 5587 5590 5592		1 64 6 17 7	10,8 688,0 64,5 182,7 75,3	45 10	26 57 11 34	4 29 54 12 32	(344,0) 1,4 18,3 2,9	1,1	2,7 23,7 1,2 15,2 2,4	4,78 2,54 4,45 4,52 4,27	B3 K0 F6 K0	-1,3 -0,5 7,1 1,8 1,9
5593	μ Cephei	73	784,7	11	7	5	71,3	112,1	156,8	3,92-t		-4,0
5594 5608 5609 5617	ν Cephei π² Cygni	13 6 2 2	139.7 64.5 21.5 21.5	- 11	15 19 5 12	3	8,2  5,4	3,4	7,1 1,5	4,85 4,46 4,26 5,00	Ko A2p B3	5,8 -4,0 -2,2 3,0
5663 5674 5676 5677 5688	ν Pegası α Aquarıı ξ <sup>1</sup> Cephei	2 32 18 6 7	24,5 344,0 193,5 64,5 75,3	15 9 39	12 8 30 77	13	22,9 21,5 1,7 1,6	24,2		4,90 3,19 4,40	K5 G0 A3, G	5,7 -0,9
570: 570: 571: 571: 573:	π Pegası 4 ζ Cephei 5 24 Cephei	4 6 35 9 24	43,0 64,1 376,2 96,1 258,0	5 5 2 26 7	26	28 12 10	(12,9	2,5	2,3 31,3 9,7	4,38 3,62 4,99	F 5 2 Ko 5 G5	5,9 1,5 1,0 2,2 3,1

5532 Cepheid variable The partilax value from the period luminosity curve is 0",022 This attributes an astonishing small diameter (2,9 ) to the star

No.		Hypotho- tical		7-1-	Spectro-	Spectral-	8-	اعصمتك-ان	err.			
Nom PGC	Nagon	radios (unit in 0",0001)	107,3 × 1=11=1	Trig parellax **1	graphic parallax #4	proper motion paralles ar <sub>e</sub>	412	4 2	4 2	(Hor- vard)	Spectral Class (Harvard)	H
5742 5746 5761 5762 5763	e Cophol . i Lacertae y Aquarii 31 Pogasi 32 Pogasi	5 29 3 1	53.8 311.7 32.2 10.8 21.5	46 2 64	37 15	55 15 28 4 9	1,2 155,8 0,5	1,5 20,8	1,0 20,8 1,1 2,7 2,4	4,23 4,22 3,97 4,93 4,88	FO KO AO B3. p B8	7.5 0,7 4,4 -1,2 -1,6
5764 5776 5777 5779 5790	2 Lacertae β Lacertae π Aquarii 4 Lacertae 35 Pogosi	2 14 3 3 10	21,5 150,5 32,2 32,2 107,5	37 17 33	11 26 23	8 19 3 12 21	0,6 8,9 3,3	2,0 5,8 4,7	2,7 7,9 10,7 2,7 5,1	4,66 4,58 4,64 4,64 4,93	B5 K0 B1p B8p K0	1,2 6,0 -0,4 0,4 7,5
5793 5805 5804 5810 5813	c Aquarii d Cophei 5 Lacertae 6 Lacertae 7 Lacertae	9 13 44 2 4	96,7 139,7 473,0 21,5 43,0	13 5 34	28 3 7	26 13 6 31	7,4 94,6 1,3	3.5 157.6 3.0	3,7 36,4 3,6 1,4	4,59 (3,7) 4,61 4,54 3,85	F2 F5, G0 K0, A B3 A0	5,8 -0,9 1,2 0,1 4,6
5824 5837 5844 5852 5853	9 Aquarii , 9 Lacertae , 10 Lacertae 11 Lacertae , 6 Pegasi , .	2 3 1 24 4	21,5 32,2 10,8 258,0 43,0	20 - 2	17 20	27 26 3 16 28	1,6	15,2 2,1	0,8 1,2 3,6 16,1 1,5	4,13 4,83 4,91 4,64 3,61	B8 A5 O05 K0 B8	4,2 5,2 -0,3 4,6 3,1
5858 5865 5874 5875 5885	o Pognal φ Pogasi ξ Pegasi λ Pogasi μ Pogasi	2 21 7 15 18	21,5 225,7 75,3 161,2 193,5	- 1 51 37 31	19 23 61 15 32	16 17 69 18 24	1.5 4,4 6,2	1,1 9,8 1,2 10,7 6,0	1,3 13,3 1,1 9,0 8,1	4,85 3,10 4,31 4,14 3,67	AO GO F5 KO KO	2,6 0,9 8,0 3,0 4,6
5891 5899 5910 5927 5933	Cophel	18 19 2 22 4	193,5 204,2 21,5 236,5 43,0	40 2 3	34 19 14 13 16	24 13 17 15 12	4,8 (10,7) (14,3)	5.7 10,7 1,6 18,2 2,7	8,1 15,7 1,3 15,8 3,6	3,68 4,97 4,95 4,96 3,63	K0 K0 A0 K5 B5.A2p	4,4 4,0 4,2 5,1 1,2
5939 5940 5942 5944 5952	β Piscium β Pognal 3 Andromedae 2 Pognal 55 Pognal	2 90 12 6 36	21,5 967,5 129,0 64,5 387,0	16 - 4 38 - 3	25 19 37 12	34 18 36 8	60,5 1,7	38,7 6,8 1,7 32,2	3,6 28,5 7,2 1,8 48,4	4,58 2,61 4,91 2,57 4,69	B5p Ma K0 A0 Ma	0,2 4,6 6,7 1,9 0,7
5954 5955 5966 5975 5988	56 Pegasi	17 2 11 4 17	182,7 21,5 118,2 43,0 182,7	- 5 0 48 28	16 3 19 40 24	12 4 12 33 41	 0,9 6,5	11,4 7,2 6,2 1,1 7,6	15,2 5,4 9,8 1,3 4,5	4,98 4,93 4,56 4,62 3,85	Ko Bi G5 F0 Ko	2,9 0,3 1,8 6,3 8,2
5993 6000 6005 6024 6031	8 Andromedae o Cophol . , , , т Pogasi . , , , v Pogasi . , , , к Pisclum .	28 9 2 8 2	301,0 96,7 21,5 86,0 21,5	26 34 25 41	10 16 20 16	9 14 10 20 29	3,7 0,6 3,4 0,5	30,1 6,0 4,3 1,3	33.4 6,9 2,2 4.3 0,7	4,99 4,90 4,65 4,57 4,94	Ma G 5 A 5 G 0 A 2 p	2,9 4,0 2,4 6,0 5,4
6037 6040 6046 6071 6073	# Piscium	12 13 2 17 3 19 period 1	129,0 139,7 21,5 182,7 32,2	•	16 16 5 47	20 15 8 32 16	4.7	8,1 8,7 4,3 3,9	6,5 9,3 2,7 5,7	4,45 4,67 4,89 4,00 4,28	G5 Ko B3 Ko B8	5,2 3,6 2,1 7,3 1,4

No		Hy pothe		Trig	Spectro	Spectral	Sei	nı diamet	eis	m <sub>vis</sub>	Spectial	
Boss PGC	Name	radius (unit is 0 ',0001)	107,5 y radius	parallax	graphic parallix	motion paraliza r <sub>3</sub>	$\frac{d_1}{2}$	$\frac{d_s}{2}$	<u>d</u> <sub>1</sub> /2	(Har- vard)	Glass (Harvard)	II I
6077	4 Piscium	6	64,5	73	70	87	0,9	0,9	0,7	4,28	F8	8,1
6078	y Cephei	26	279,5	69	69	27	4,1	4,3	10,4	3,42	Ko	4,6
6080	ж Andromedae	2	21,5	8		21	2,7	1	1,0	4,33	A <sub>0</sub>	3,9
6084	A Piscium	3	32,2	30	32	34	1,1	1,0	0,9	4,61	A 5	6.1
6094	78 Pegası	13	139.7	18	17	13	7.7	8,2	10,7	4,98	K0	4,5
6135	g Cassiopojae	18	193.5	29	2	10	6,7	96,7	19,3	4,85	1.8p	0,9
6150	ψ Pegasi	36	387,0		12	11		32,3	35,2	4,75	Ma	3,5
6155	<ul> <li>Cassiopejae</li> </ul>	2	21,5	12	4	5	1,8	5,4	4,3	4,93	132	0,3
6156	o Piscium	8	86,0	11	37	57	7,8	2,3	1,5	4,03	IF 5	5,4

When a scrittiny is made as to the average size and distribution of linear diameters in the pieceding table it will be noted that the mean values for the diameters computed with aid of the trigonometric, spectrographic and spectral-proper motion parallaxes respectively, will on an average agree very well. This is to be expected because the two latter parallax methods are founded upon the trigonometric method and possibly existing systematic errors in  $\pi_1$  are to a certain extent taken over by the series  $\pi_2$  and  $\pi_3$ . But what is remarkable as to the linear diameters is the good agreement in individual cases. Any justified discussion of the material will show that our knowledge of parallaxes evidently has advanced in such a way, that we now can compute the linear diameters of the stars with a high, nay, unexpected degree of accuracy. It also seems that the material as to  $\pi_1$  added since 1929 has in the majority of cases increased the agreement between the three series of linear stellar diameters.

A recent investigation by Jesse Greenstein [Haiv Bull 876, p 32 (1930)] reveals the existence of systematic errors in IIlrezerrune's colour equivalent  $c_2/I$  Greenstein computes the quantity  $c_2/T - c_2/T_a$ , where  $T_a$  is the mean temperature for a cortain spectral class S. These quantities show a seasonal variation, which indicates a reddening of the winter stars, probably due to elimatelogical phenomena. Errors of that kind affect the diameter values to a certain extent and it seems that a revision of the derivation of the stellar diameters is warranted. On that account an extensive statistical treatment of the data in the preceding catalogue is postponed until such a revision has been undertaken During the mean time the preceding table will represent a summary of our present knowledge as to the distribution of the stellar diameters.

## Sachverzeichnis.

Absorption des Lichtes im interstellaren Raum 1024ff. of light in space 555ff Accuracy attainable with photographic mothods 355 Antinometry, Yorkes 311, 396-Aktinometrie, Göttinger 314f Aroas, selected 317ff. Astorium 22. Astron 430, 778 Binaries, angular motion to of visual 695 may-ratio, statistical investigation 683f. eriain of 695 relation between mass and form of orbits of **690**. spectroscopio, dwarf nature of 658. masses of 653ff visual, masses of 612ff Brightness 212 Candle, international 212. power 212. Carto du Ciel 300ff Catalogues, photometric, influence of multitade and lucompleteness on 336f of the Pleisdon 312, 316 of stollar spectra 106. Changes in the colour of Sirius 3861. socular, in the light of the stars 356ff. Classification of stollar spectra 311 CANNON'S 34, 50ff. DEAPER Catalogue 27f additions and modifications 58ff. description, tabular 4910 descriptions, verbal 44 ff. development of the - from 1901-1924 3511 LOOKYRE'S 19. MAURY'S 321L SECCHI'S SII Voorl's 15ff. by line intensity ratios 55. by measurements of offective wave length 100ff. by measures of colour index and heat 1041 **xa**bal comparison of the principal 57f Clouds of calcium 784. commio. HAGEN'S 787 IL interatollar 782. star-, distance of the 543ff.

stationary 782.

Clusters, galactic, classification 704f compact 704. field irregularities 704. loose and irregular 704. Star associations 704. distribution, apparent, of the 710 parallance 747 spectra in individual 715ff structure of the 730f orientation 730f shoulder affect 731f eystam of 755 Clusters, globular, classes of SHAPLEY and SAWYER 705f classification 705. dimensions and star densities 749f distance modulus 742, 745 distance to the galactic centre 758. distances from Cophoids and bright stars from dismotors and integrated magnitudes 744 (f from angular diameters 744. from integrated appearon transmitude 744 distribution, apparent 708f of stars in the 720ff. forms of the 724ff. definition 724. ellipticity 726. orientation of major axes 727 inclination to the galactic circle 727 elongation of Mossior 13 725f. higher systems of 755 ft. integrated spectra 711 in Magallanic clouds 751 peculiar 728f period-inminosity curve 737 f. mro point 739. radial velocities 7481 relation of the - - to the Magellanic aloude 753 space distribution of the 755ff. stellar types in the 712. colour-magnitudo arrays 7121. common spectral classes 712. superayatems 758 variables in the 717ff. frequency and general properties 717 minmary of known 718f Clusters, stollar, catalogues of galactic 746. definition 698. alactic and globular 698 historical notes on 6981.

Clusters, stellar, number of 700 variable stars in the 717f frequency and general properties 717	Diameters, from seintiliation observations 599 historical 575f
summary of known 718f	method of Danjon 596
Colour-catalogues, index catalogue 371	of Hamy 591ff
Krücer 3701	of Pokrowsky 599
LAU 375f	of Russell 582
MALMOUIST 307	of Wilsing 578
MOLLER 379	varying 500
Colour, changes, of Smus 386f in the — of the stars 375f direct estimates of 363f	Distance method of Otto Struvi 489ff
sources of error in the 371 ff	modulus 712, 745 Distribution of Helium stars, Charlii r's
equation of catalogues 214, 427ff equivalents 389f	deferminations 509ff
ındex 215	Gerasimovic's investigations 512
as a function of m 400	Robb's determination 513
from photoelectric measurements 545ff	Distribution, relative, of $N(m)$ 351f
indices, absolute 392	Doppler's formula, Modssard's modification
existence of preferential 424f	907 ff
from the Göttinger Aktinometrie 391f	DRAPER Catalogue, classes, tabular descrip- tion 49ff
-mass density relation 641	classification, verbal descriptions 44ff
nuance 363	additions and modifications 58ff
saturation 364	distribution of the stars in the 537ff
scale of Argelander 366	Draper-Katalog, statistische Auswertung
of Franks 366	des 111
of Hagen 369	Durchmusterung, Bonner 259ff
of Osthoff 367.	Cape photographic 299f, 306ff
of Potsdam 369	Córdoba 265ff
of Schmidt 360	Potsdam, photometric 279ff, 285ff
of H C Vogni 365	Dynamik dei Milchstraße 1033f
linear 366	
relation between the of Hagen and	Eclipsing binaries, masses and luminosities
the scales of other observers 367 two dimensional 366	686 <b>f</b>
shade 363	parallaxes and absolute magnitudes 606
tone 363	statistics 607
tone scale 364	Effective wave lengths, determinations at
Colours of bright stars 548	Greenwich 409f
of double stars, BELL's study 380	by Kreiken 4121
reduction of the - to a standard system	discussion of the methods 415ff
421 ff	von Kluber's modification 411
stellar 363 ff	of faint Milky Way stars 408
Convergence of the sum of stellar light 361f	of the Pleades 407 minimum 406
Cosmogonic time-scale of Eddington 662ff	standardization of the 415
of JEANS and SMART 672	visual 401f
Criterion of Olbers 888	
of Sceliger 888f	Emissionsvermögen 146 Energiekurve 129
Donata tauta 404	Equipartition of energy 617f
Dazzle tints 381	Erdicht 948, 981
Densities of the stars 600ff	Exposure-ratio method 393f, 398f
binary stars 600f	Extinction 565f
echpsing binaries 604f ratio of the — in double stars 603	Eye, as a photometric instrument 215ff
Density or back-ground effect 335f	
Development, stellar, Russell's investigati-	Farbenindex 171
ons 442ff	absoluter 172, 176
Diametei, equivalent 578	Farbtemperatur der Sonne 184f
laws 296ff	spektralphotometrische 165f
of Sirius B 596ff	der Sterne aus der Farbe oder einen
Diameters of the stars 575ff	Farbenäquivalent 168ff
equivalent 578	aus der Gestalt der Energiekurve 148fi
from $c_2/T$ 584	und Strahlungstemperatur, Beziehun
from interferometer measurements 587ff.	zwischen der 143
from radiometric measurements 585f	Farbtönung 171

Pehlerquellen, systematische, bei der Bestimmung der Temperatur aus der Enorgiekurve 194ff. Fixsterntemperatur 130. Foot-candie 211

Galaktische Ebene 937 Koordinaten 972

Tafeln zur Berechnung der 973f

Galaxy, avorage 8681f

dimensions of the 754ff.

distance to the galectic centre 7581 bigher systems of globular clusters 755 eccentric position of the solar system

755f. region of avoidance 758.

motion of our - in space 906 ties and structure of the 759ff

supergalaxies 838.

system of galactic clusters 755

value of the motion of our — in space 906. GALLESOT phenomenon 290, 292 f.

Gas, interstollares 1033

als Quelle der kosmischen Strahlung 1033.

Temperatur 1028. Totalmasse des 1033

Geschwindigkeitsellipseid n. Rotation 1065 f. Geschwindigkeitsvertellung, asymmetrische, in ihrer Besiehung sur Rotation, nach

LINDBIAD 1048ff, nach Oort 1052f.

Glants and dwarfs 437ff.

Giant stars, masses of 714 Goulnecher Kreis 972,

Gradationstemperatur u schwarze Temperatur, Beziehung zwischen der 144f Groenwich estalogues 313f

HAGENS dunkle Nebel 979if.

Flänfigkeit, scheinbere, der einselnen Spoktraiklassen 111

Hänfigkeitsverteilung, wahre, der Spektralklassen 120.

HERECHEL (unit of distance) 430.

Himmolshintsrgrund, absolute Helligkeit des 948ff.

Illumination 211 Index, spectral 397f, Intensity, luminous 212. physiological 580.

K-Rifeht der Radialgeschwindigkeiten 1069 f. Kaleinminien, stationäre 1059 fl

Kalsinmwolken 1027 f.

galaktische Verfollung der Intensitäten der 1030.

mittlerer Absorptionskoeifisient per Parsec 1031.

Vertellung der, mit bekannten Radialgeschwindigkeiten 1061.

KAPTEYN's method 353, phenomenon 380, 390.

universum 991£ Handbuch der Astropkysik V. 2. Kinchhorn Funktion 128 Gesets 128 Kallisionsiunktion 1035.

LAMBERT 212 mill- 212

Leiden catalogue 320.

Loughtkraftsfunktion 988.

Light, units, definition of the 211ff -vest 430, 778

Lillputhan stars 585

Limiting magnitude of star catalogues 342f.

Limits of unaided vision 354

Line intensity ratios for classification purposes 55f

Lockyer, definitions of stellar genera 221. Lumen 211

Luminositate funktion 988.

Luminosity curve from differences in magnitude of double stars 504ff.

for individual spectral classes 530f of different spectral classes 441

Luminous flux 211.

Macron 778.

Magallanic alouds 750ff

distances of 752.

globular clusters in the 751 relation of clusters to the 753£ type of clusters and nobulae 750.

Magellanacho Wolken 965f.

Natur der 1022ff

Magnitudo, absoluto, differential determinations 537

general distribution 498ff.

relation between - and colour 541f.

and proper motion 514ff and radial velocity 509. and spectral class, 493ff

balametria 554.

limiting, of star estalogues 342i.

of the stars 212.

total, of star agglomerations 359.

Mass-function 619f.

Mass-luminosity law, Robinston's 662 fL

BRILL's theory 6731

discrepancies between SEARES's and

EDDINGTON'S results 666 TRANS'S theory 667 if.

RARE's thoory 678 ff.

Voor's extension of Endingrou's theory 682f.

relation 658ff.

Mam of Orion nebulae 691 of planetary nebulae 692.

of the abiliar system 693.

Mass-ratios in binaries, statistical investigations 683f.

thorretical derivation of the 684.

of stollar systems 694.

Mass-reduction by annihilation of protons and electrons 676ff.

Mam, stellar, relation between — and form of orbits of binaries 690.

and proper motion 689f.

Nebulae, classification 777f Masses, determination, Sproul, of 626 systems of classification 919ff equipartition of energy 617f frequency of - for different spectral dark 784ff classes 622ff distance of the 534ff methods of deriving 608ff types of the 784 of Freundlich and Heiskanen 645f diffuse, definition 779 of Ludendorff 619ff distances and dimensions 792 of MARTENS 646ff emission valiations in the 801 of PITMAN 627f evolutionary status 805f gaseous spectra 799f of SCHLESINGER and BAKER 619 of SEARES 631ff internal motion 795f of von Zeipel 641ff luminosity 799ff preferential values of 656ff reflection or resonance effects 8021 real and apparent 630 number and distribution 779 of F-K stars 638ff physical characteristics 781ff of spectroscopic binaries 653 ff irregularity 781 of visual binaries 612ff tenuity 781ff from spectrographic parallaxes 637 f variation in apparent luminosity 781 statistics of accurately determined 629f proper motions 795 of stellar systems 694 radial velocities 797 upper limit for the stellar 687 reflection or resonance effects 8021 Messungen, radiometrische und thermospectra, continuous 802. elektrische 164 gaseous 799f turbulence effect in the 797f spektralphotometrische differentielle 154ff variable 803 Metron 430 extragalactic 777 Milchstraße, Anschauungen über die Natur nongalactic 777 des Systems der 1069ff planetary, classification of the 816 Beschierbung und zeichnerische Darsteldefinition 806 lung 938 ff distance and dimensions 810ff Definition der 937 distribution 807 Dimensionen, Masse, Rotationsdauer der evolutionary status 8311 forms of 808 1067 f dip (Tiefe) 969 number 807 Ebene der 937 parallaxes 810ff effektive Entfernung der Sterne der 985ff. proper motions 809 offektive Sterngröße des Lichtes der 981 ff 1adial velocities 817 Farben der Sterne der 986f rotation 817 Helligkeitsschützungen 944f spectra of nebulous matter 813f photometrische Eichung der Isophoten of nuclei 815 947 spectroscopic distribution effects in the Integralspektrum der 985 ff Kalziumwelken in der 1027 ff temperatures 831 Lage der 967ff theories, mechanical 823f Phänomen der 937, 1046 theory, quantum- 824ff turbulence effects in the 819ff Photographie der 952ff Photometrie, photographische der 960 reproductions of 922ff Pol der 969 white 833 aus der maximalen scheinbaren Sterndichtigkeit 970ff Olbers's criterion 888 Bestimmungsmethoden 969f Rotation der 1056ff Parallax methods 430ff Sternleeren und Sternwolken in der 1010ff Brill's - for binaries 673ff Tiefe (dip) der 969 dynamical 431 Verlauf der - am Himmel 962ff moving cluster 432 Zeichnungen der - auf Grund photospectral-proper motion 433, 488 graphischer Aufnahmen 960ff spectrographic 434, 454ff Milky Way, siehe Milchstraße spectroscopic 434 trigonometric 431, 434ff Nebelfelder, galaktische, Einfluß auf das Parallaxes, photometric 219 Milchstraßenbild 975ff radiation-energy 675f Verteilung gegen die galaktische Ebene spectrographic, distribution of - with

Nebelleuchten, Theorie des 205ff

Nebulae, anagalactic 777

regard to m and spectral class 508

systematic errors in the 436

Parsec 430, 778

Parmec, cubic- 778	Spectrum analysis, stellar, history of the,
kilo- 778	D'ARREST 15
mega- 778	DONATI 3
Passagefunktion 1035	Donta 19
Period-luminosity curve, photographic 737ff	Flexing 28
sero point 739f	FRAUNHOFER 1.
Phot 211	HUDGINS 18
Photometry, Harvard, Revised 276ff	LOCKYER 19f
photoelectric 558	MAURY 29
Yerkos — of Selected Areas 404	McCLEAN 25 Provening 27t
PLANCKS Strahlungsgesets 131 Podson's constant 213	Pickering 271 Rutherford 4
ratio 261	Seconi 511.
Protometals 22.	Vogel 15f
Trouding and	Spoktralstatistik der schwächeren Storne 1171.
Radiation temperature 674.	Spirals, colour indicas 854
Radiometric measurements 559ff	cosmogonical deductions 887 ff.
Reflecting offect in collipsing variables 339	direction of rotation of the 852.
Rieson- und Zworgsterne, Temperatur der	distance-velocity relation 863 IL.
197 ff	distances and dimensions 873 ff
Vortollung der 119.	from Cepheids 861
Rotation, differentiale, der Milchstraße,	from distance-valority correlation 863ff.
Theorie nach GYLD#N 1057	from novae 858if
nach OORT 1056, 1058.	from parallaxes 858.
nach OPPRENEIM 1057	from photometric observations 868 ff
nach Plaskett und Plasce 1059 II	distribution, apparent 838
Rotationsoffekte, differentielle, in den Go- schwindigkeiten 1056 ff	evolutionary status 887
SCHAIRGISTORY: JOSOTI	forms of 840f.
Schwarzer Körper 128	barrod 842.
Seeliger's Criterion 888L	elliptical 843.
Sequence, Mount Wilson - and Internatio-	irregular 844.
nal scale 326ff	Magellanic typo 844.
Poler 323ff.	groups of 838
Shedows cast by starlight 354	historical note 833ff
Siriometer 430, 778	internal motions 850.
Sirius, colour change 386f.	isolated 858
Strius H 596 ft.	local 858. masses of the 876
Sirinawelto 430, 778. Solar system, eccentric position in the system	mathematical 879
of globular clusters 755 f	Wilczynaki's gravitational 881.
Sonne, Entfernung dar - von dar Sym-	minuto 8431
motricobene der Michetraße 1009	number of 839.
exsentrische Stellung im System 997	occulting matter in the 844ff.
Gradationstemperatur der 165ff	proper motions 847ff.
schwarze oder Strahlungstemperatur der	recomion, apparent of the 905f
185ff	rotation 851 L
spoktralphotometrische Farbtomperatur	spectra of the, stellar type 852
der 165ff	emission lines 853
Space penetrating power 350	theories of spiral structure 878 ff.
Spectra of stars of class	of Brown 882L
P 36, 641.	of JRAMB 882.
O 67 ff.	of LDTDBLAD 884f
В 73.0	true 842.
A 76ff.	velocities, radial, of the 855f. Spirals and relativity universes 89fff.
F, G, K 80ff.	Star clusters sielle clusters.
M 36, 89fL	colours, old observations of 3831.
R 37, 94f. N 38, 94f.	relation between — and spectra 382.
	light, total amount 340f
S 38, 921. Q 621.	Stern, Illiputian 585
Spectral criteria, variation curves of 53f.	number of — within certain limits of
photometry 549 ff.	magnitude 347ff
Spectrum analysis, stellar, history of the,	variable, in star clusters, frequency and
Сантон 34.	general properties of 717
CARPENTER 5.	summary of known 7181
	73*

STEFANSCHES Strahlungsgesetz 132	Temperature radiation 674
Stellar system, mass of the 693	Temperature, stellar, determination of 549 if.
Sterne, galaktische Konzentration der 982ff	Transparency of space 733ff
Sternfarbe 168	early investigations 733
Sternhaufen siehe clusters	from blue stars in Messier 13 733f
System det 996	from colours in distant objects 735
Zentralpunkt des 996	light scattering 733
Sternleeren und Sternwolken in der Milch-	relative speeds of blue and yellow light
straße 1010f	735f
Steinstratum, dunkle Flecke im 979	1337
	Units of distance 430, 778
Sternstromung im typischen System 1039f	Universe, CHARLIER'S infinite 888ff
nach JEANS 1040	continent- 761
nach Kapteyn 1039f	expanding relativity 898ff
Sternsystem, Dynamik des, nach Jeans 1040	
nach Kapteyn 1039f	ısland- 833, 835, 837, 838
das große, nach Lindblad 1042ff	relativity- 891 ff
das größere, nach Shapley 1006f	of DE SITIER 893
das lokale 998, 999, 1008, 1012, 1014,	of Eddington, Friedman, Llmaitre,
1017, 1018, 1027, 1040, 1042, 1064,	McCrea and McVittle 898ff
1069, 1070, 1073, 1074, 1075	of Einstlin 892
Mechanik, statistische des 1034ff	of Silberstein 902
nach Charlier 1035	Untersysteme 1049, 1075
	Uranometria Argentina 254f
nach Jrans 1035	Nova 251f
nach Lundaire 1036	Oxoniensis 275f
schematisches 990	C tollionom 2/J1
typisches 990	Veränderliche Sterne, Temperatur der 201ff
nach Kapteyn 1042	Verteilung, galaktische, der Kugelhaufen
Theorie der Sternströmung im typischen	1008
1039f	von Objekten großer absoluter Leucht-
Sternweite 778	kiast 1003ff
Strahler, grauer 129	
schwarzer 128	der Spektralklassen 112f
Strahlungskonstanten, numerische Weite dei	B-Sterne 114
133f	A-Sterne 115
Strahlungstemperatur der Sonne 185ff	F-Steine 115
der Sterne 188 ff	K- und M-Sterne 116
	O-, P-, N-, R-Sterne 117
aus der Strahlungsintensität begrenzter	der offenen Sternhaufen 1007
Spektralbezirke 185ff	ıäumliche, der verschiedenen Spektral-
Supergalactic groups 875	klassen 122f
Supergalaxy 761, 838	der Sterne im Raume, statistische Untei-
Symbols of W Herschll 245ff	suchungen 987
System, galactic 754	nach Charlier 994f
galaktisches, Ursprung des 1038f	nach Kapteyn 991f
of galactic clusters 755	nach Malmouist 995
isophoter Wellenlängen 174	nach Schwarzschild 992f
der B-Sterne 125f	
stellar -, mass of the 693	nach Seeliger 988ff
	Verteilungsgesetze der Spektraltypen 999ff
Temperatur, Bestimmung der, aus der Form	der Sterne der Spektralklasse B 1000ff
der Spektralkurve, Fehlerquellen 194ff	Wärmeindex 181ff
effektive 131	
Farb- 142,	Wasserzellenabsorption 181 ff
	Wellenlänge, effektive 170, 175
spektralphotometrische 141	isophote 174f
Gradations- 141	fundamentale 174
ım ınterstellaren Raum 1028	minimale 170
schwarze 142	Weltinsel 833, 1071f
-skala der Frysterne 191 ff	Wiensches Strahlungsgesetz 132
der Sterne, photosphärische 204	Verschiebungsgesetz 133
spektralphotometrische Farb 204	
Strahlungs- 204	Zero-point of the photographic scale 311, 324.
Strahlungs- 142	of photometric measures 344f
	-